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First-principles insights into tin-based two-dimensional hybrid halide perovskites for photovoltaics†

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The two-dimensional (2D) hybrid halide perovskites have recently attracted attention due to their excellent photovoltaic performance. In comparison to their three-dimensional (3D) analogues, they show superior long-term durability and moisture tolerance. Meanwhile, their layered topology offers greater flexibility for electronic structure tuning. To date, most devices containing 2D perovskites have been based on Pb, which presents environment concerns and a possible roadblock to commercialisation due to its toxicity. The development of lead-free alternatives is therefore immensely important to facilitate the uptake of perovskite-based photovoltaics. Herein, we investigate the geometrical, electronic and optical properties of the semiconducting 2D tin perovskites $(\text{CH}_3(\text{CH}_2)_3\text{NH}_3)_2(\text{CH}_3\text{NH}_3)_{n-1}\text{SnI}_{3n+1}$ ($n = 1, 2$ and 3), using relativistic hybrid density functional theory calculations. We demonstrate that the band gaps of the series decrease with increasing perovskite-like layer thickness, from 1.85 eV ($n = 1$) to 1.38 eV ($n = 3$). We find strong and broad optical absorption across the series, in addition to small effective masses of electrons and holes in the laminar plane. The $n = 3$ composition displays a high spectroscopic limited maximum efficiency of 24.6%. Our results indicate this series of homologous 2D tin halide perovskites are a promising class of stable and efficient light-absorbing materials for photovoltaics.

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Introduction

The drive towards reduced costs, higher conversion efficiencies and environmentally friendly alternatives to current photovoltaic technologies is immensely important in the search to relieve the world's reliance on fossil fuels and promote sustainable economic development.^{1–3} Since the first reports of solid-state hybrid perovskite solar cells in 2012,⁴ power conversion efficiencies (PCEs) have increased dramatically up to 22.1%.⁵ Despite the rapid rise in efficiencies of the hybrid lead perovskite such as $\text{CH}_3\text{NH}_3\text{PbI}_3$ (MAPbI₃), their poor long-term stability^{6,7} and the toxicity of water-soluble lead compounds,⁸ necessitates the development of alternative lead-free halide perovskite materials with improved moisture tolerance.

One solution to instability issues has been proposed in the form of the layered hybrid perovskites, which show less PCE

degradation over time than their 3D counterparts.^{9–12} 2D hybrid perovskites, with the formula $(\text{RNH}_3)_2(\text{MA})_{n-1}\text{BnI}_{3n+1}$ (where $\text{MA} = \text{CH}_3\text{NH}_3^+$), contain large cations which are sandwiched between slabs of perovskite-like sheets. 2D perovskites can be produced if the organic cation, such as $\text{CH}_3(\text{CH}_2)_3\text{NH}_3^+$ (BA), and $\text{C}_6\text{H}_5(\text{CH}_2)_2\text{NH}_3^+$ (PEA), is too big to fit in the perovskite cage.^{13,14} Although 2D hybrid halide perovskites have been known since they were first synthesised by Mitzi *et al.* in 1994,¹⁵ they were not investigated as solar cell absorbers until Smith *et al.* found the 2D perovskites to be more resistant to moisture than their 3D analogues,⁹ owing to the hydrophobicity of the organic cation¹⁶ and van der Waals interactions between the organic molecules and the surface of the inorganic framework.^{17,18}

Besides enhanced moisture tolerance, 2D perovskites also present other prospective benefits. For example, the inorganic framework provides the potential for high carrier mobilities, whereas the organic moiety can enable intense photoluminescence (PL), owing to the quantum confinement effect.^{19,20} Compared with the 3D hybrid perovskites, the 2D configuration provides greater flexibility for morphology and electronic structure engineering. This has been exemplified in the $\text{L}_2(\text{BX}_3)_{n-1}\text{BX}_4$ series (where L = octylammonium, butylammonium; B = Sn, Pb; X = Cl, Br, I), in which choice of alkyl chain length and perovskite-like layer thickness play a crucial role in controlling platelet size and band gap.²¹ Additionally, environmental concerns can be addressed by replacing Pb with less toxic elements, such as Sn and Ge.^{22–24} The band gaps of the

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2D series generally decrease monotonically with increasing perovskite-like layer thickness, finally tending to that of corresponding 3D perovskite.^{25,26} In this way, the 2D hybrid perovskites have attracted increasing attention and witnessed a sharp rise in efficiency over the past two years,²⁷ with champion devices (containing (PEA)₂(MA)₅₉Pb₆₀I₁₈₁) showing efficiencies of 15.3%.¹²

Despite these recent improvements, most devices containing 2D perovskites show efficiencies below 5%, due to the increase in band gap associated with moving from a 3D connected metal-halide framework to one with 2D connectivity.^{9,10,26,28} Based on the well-known Shockley–Queisser limit,²⁹ a solar absorber should possess a band gap between 1.0 and 1.5 eV (ref. 30) to maximise its efficiency. This limits the applicability of the butylammonium containing layered perovskites, (BA)₂(MA)_{*n*−1}Pb_{*n*}I_{3*n*+1}, which possess band gaps of 2.43, 2.17 and 2.03 eV for the *n* = 1, 2, and 3 compositions, respectively.¹⁰ Similar to the reduction in band gap seen when moving from MAPbI₃ (1.55 eV) to MASnI₃ (1.2 eV), the band gaps of the Sn-based butylammonium layered perovskites are smaller than to their Pb analogues.²⁶ As recently demonstrated by Cao *et al.*, the (BA)₂(MA)_{*n*−1}Sn_{*n*}I_{3*n*+1} series are semiconductors with band gaps decreasing from 1.83 eV (*n* = 1), to 1.64 eV (*n* = 2), and 1.50 eV (*n* = 3).²⁶ Particularly in the case of the *n* = 3 composition, these band gaps are closer to the ideal specified by the Shockley–Queisser limit and should enable increased efficiencies. Furthermore, it has been suggested that the Sn-based iodide perovskites possess much lower exciton binding energies than their lead counterparts, due to their larger dielectric constants, and should therefore show reduced open-circuit voltage losses. Thus, the low *n* tin-based 2D perovskites should possess the best of both worlds, with optimal band gaps and improved moisture stability.

In 2017, the *n* = 3 and 4 structures of the (BA)₂(MA)_{*n*−1}Sn_{*n*}I_{3*n*+1} series were fabricated into heterojunction solar cell devices, using mesoporous TiO₂ as an electron-accepting layer.²⁶ Despite growing the 2D perovskites with the sheets aligned perpendicular to the electrodes (as shown to be necessary in highly efficient 2D perovskite devices),¹⁰ the devices showed poor efficiencies of 1.94% (*n* = 3) and 2.53% (*n* = 4). This was, in part, due to low fill factor and small open-circuit voltages (*V*_{oc}) of 382 mV (*n* = 3) and 229 mV (*n* = 4), well below the optical band gaps of the materials. Importantly, however, the stability of the devices was drastically improved, with 90% of the initial efficiency retained after 1 month, in contrast to comparable MASnI₃ films which deteriorated to 0% efficiency in a similar timeframe. Despite poor efficiencies, this series shows promise for the future of lead-free perovskite solar cells, with the authors highlighting a clear path to improve efficiencies, through use of alternative electron contact materials to enable higher *V*_{oc}.

In this paper, we investigate the optoelectronic properties of a series of Sn containing layered hybrid perovskites, (BA)₂(MA)_{*n*−1}Sn_{*n*}I_{3*n*+1} (*n* = 1, 2 and 3), using relativistic hybrid density functional theory. We systematically assess the relationship between crystal structure and electronic properties, in particular the effect of octahedral distortions. Lastly, evaluation of

the thin-film photovoltaic ability of the series, indicates promising applications in the future of lead-free perovskite solar cells.

Computational methodology

First-principles calculations were performed using the Vienna *Ab initio* Simulation Package (VASP).^{31–34} The interactions between core and valence electrons were described *via* the projector augmented-wave (PAW) method.^{35,36} The plane wave cut-off energy was set to 580 eV, with a *Γ*-centered 3 × 3 × 1 *k*-point mesh employed for the unit cells of the *n* = 1 and *n* = 3 structures, and a *Γ*-centered 3 × 3 × 2 used for the unit cell of the *n* = 2 composition, of which structures are shown in Fig. S1 and the lattice parameters are provided in Table S1 of the ESI.† These parameters were necessary to converge the total energy of each system to within 1 meV per atom.

Based on previous studies on the hybrid perovskites, we tested lattice relaxations using two functionals:^{37–39} the Perdew–Burke–Ernzerhof functional⁴⁰ (PBE), with dispersion interactions included *via* Grimme's D3 dispersion correction⁴¹ (PBE-D3), and the PBESol functional,⁴² a version of PBE revised for solids. Both functionals have been shown to accurately reproduce the structural parameters of layered materials and those containing weak van der Waals' type forces.^{43,44} During geometry optimisation, the atomic positions, lattice shape and cell volume were allowed to relax, until the forces on each atom totalled less than 0.02 eV Å^{−1}.

In order to obtain an accurate description of the electronic structure of our systems, hybrid density functional theory was employed. Here, we used the Heyd–Scuseria–Ernzerhof (HSE) functional^{45,46} incorporating 43% Hartree–Fock exact exchange α and 100% of the correlation energy from PBE. This has been shown to reproduce the band gap of MAPbI₃,⁴⁷ and therefore we expect that it will perform well here. To properly account for the relativistic effects present on the heavy elements Sn and I,^{48–51} all electronic structure calculations explicitly included spin–orbit coupling (SOC). This combination of HSE43 + SOC was used for all band structure, density of states, optical absorption and charge density calculations. The high-frequency dielectric response was calculated from the optical transition matrix elements within the transversal approximation.^{52,53} The ionic dielectric contribution was calculated using density functional perturbation theory (DFPT),⁵⁴ using the PBE-D3 functional. Crystal Orbital Hamilton Population (COHP) analysis was performed using the LOBSTER program^{55,56} based on wavefunctions calculated using HSE43. Due to constraints of the LOBSTER program, spin–orbit effects were not included in the COHP analysis, however, we note that while SOC introduces a slight spin-splitting of the band edges, the orbital nature of the bands is expected to remain unchanged.

Results and discussion

Geometric structure

(CH₃(CH₂)₃NH₃)₂(CH₃NH₃)_{*n*−1}Sn_{*n*}I_{3*n*+1} (*n* = 1, 2 and 3) are members of the layered perovskite family adopting the Ruddlesden–Popper type crystal structure, where *n* is the number of



anionic perovskite-like layers, comprising 2D sheets of corner-sharing SnI_6^{4-} octahedra (Fig. 1).⁵⁷ The layers are separated from one another by organic butylammonium (BA) cations. The molecule acts to maintain charge neutrality and stabilises the perovskite structure.⁵⁸ For the $n > 1$ structures, methylammonium (MA) cations are present in the interstitial site at the centre of the perovskite cage. A larger value of n indicates a thicker perovskite-like component, with $n = \infty$ equivalent to the 3D perovskite, MASnI_3 . In this paper, $(\text{BA})_2\text{SnI}_4^{\text{rt}}$ ($n = 1$), $(\text{BA})_2(\text{MA})\text{Sn}_2\text{I}_7$ ($n = 2$) and $(\text{BA})_2(\text{MA})_2\text{Sn}_3\text{I}_{10}$ ($n = 3$) were optimised from the unit cells determined by X-ray diffraction,^{15,59,60} with the relaxed primitive cells displayed in Fig. S1 of the ESI.† Both a room temperature phase (273 K) and a low temperature phase (128 K) of the $n = 1$ composition were studied, identified herein as $(\text{BA})_2\text{SnI}_4^{\text{rt}}$ and $(\text{BA})_2\text{SnI}_4^{\text{lt}}$, respectively, with the low-temperature phase possessing greater tilting of the octahedra. The low temperature structure was found to be marginally lower in energy by 2.3 meV per atom.

Geometry relaxations were trialled using both PBEsol and PBE-D3, with the full results provided in Table S2 of the ESI.† Overall, the PBE-D3 lattice constants showed greater agreement with experiment (Table 1) and, as such, these structures were employed for the rest of this report. We note that the β parameter of the $n = 2$ structure increased upon lattice relaxation, likely due to the fixed orientations of the organic cations which will show significant flexibility in the room temperature

structure. All other lattice parameters showed acceptable agreement with the experimental values.

Electronic properties

The fundamental band gaps of the series, calculated using HSE43 + SOC, are listed in Table 2. In all cases, the band gaps are larger than that of MASnI_3 (1.3 eV).²² As expected, the band gaps decrease monotonically as the thickness of the perovskite layer increases (Fig. 1),^{24,61,62} from 1.85 eV ($n = 1$), to 1.50 eV ($n = 2$), and 1.38 eV in the $n = 3$ case. These are in good agreement with ultraviolet-visible spectroscopic measurements, which show band gaps of 1.83, 1.64 eV, and 1.50 eV for the $n = 1$, 2, and 3 structures, respectively.²⁶

Similar to MASnI_3 ,⁴⁹ the upper valence band of the series is determined by Sn 5s and I 5p anti-bonding orbitals, with the lower conduction band composed entirely of Sn 5p anti-bonding orbitals (Fig. 2), both of which give rise to excellent band dispersion. The antibonding character of these states is demonstrated by the Crystal Orbital Hamilton Population (COHP) analysis provided in Fig. S2 of the ESI.† Because the states of the organic cations are several eV away from the band edges, they will not play a role in determining the electron and hole transport properties. The HSE43 + SOC calculated band structures for the series are plotted in Fig. 2. The results indicate that all systems possess direct fundamental band gaps with the valence band minimum (VBM) and conduction band maximum (CBM) situated at the Γ point (0.0, 0.0, 0.0).

Both the VBM and CBM are dispersive along the directions parallel to the perovskite-like layers ($Y-\Gamma$ and $\Gamma-X$), while they are flat in the perpendicular direction ($\Gamma-Z$), due to the 2D connectivity of the tin iodide octahedra. As a result, the calculated effective masses are nearly infinite in the perpendicular direction, indicating carriers will be immobile across the layers (Table 2). Accordingly, any devices containing these systems should possess $[\text{Sn}_n\text{I}_{3n+1}]^{(1+n)-}$ slabs that are oriented perpendicular to the device contacts, allowing for efficient extraction of charge carriers to the electrodes. This has recently been demonstrated experimentally for the $(\text{BA})_2(\text{MA})_{n-1}\text{Sn}_n\text{I}_{3n+1}$ series, in which judicious choice of solvent enables control over the orientation of the perovskite-like layers.²⁶

Owing to the dispersive VBM and CBM, the series display light hole and electron effective masses in the directions

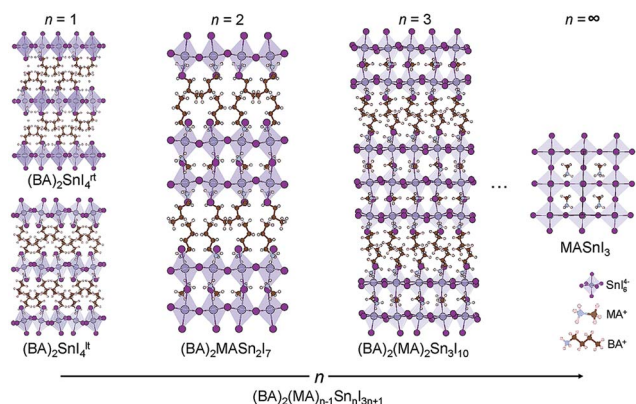


Fig. 1 Structures of the layered tin perovskite series, $(\text{BA})_2(\text{MA})_{n-1}\text{Sn}_n\text{I}_{3n+1}$ ($n = 1, 2$ and 3). The thickness of the inorganic slab increases with increasing n value, tending toward the structure of $\text{CH}_3\text{NH}_3\text{SnI}_3$.

Table 1 Lattice parameters of $(\text{BA})_2(\text{MA})_{n-1}\text{Sn}_n\text{I}_{3n+1}$ conventional cells, calculated using the PBE functional with Grimme's D3 dispersion correction, in comparison with experiment. Lattice lengths given in Å and lattice angles given in °

Compounds	Functional	<i>a</i>	<i>b</i>	<i>c</i>	α	β	γ
$(\text{BA})_2\text{SnI}_4^{\text{rt}}$	PBE-D3	8.497	8.724	28.034	90.0	90.0	90.0
	Ref. 59	8.591	8.814	27.644	90.0	90.0	90.0
$(\text{BA})_2\text{SnI}_4^{\text{lt}}$	PBE-D3	8.410	8.911	26.074	90.0	90.0	90.0
	Ref. 59	8.408	8.932	26.023	90.0	90.0	90.0
$(\text{BA})_2(\text{MA})\text{Sn}_2\text{I}_7$	PBE-D3	39.458	8.946	8.479	90.0	95.1	90.0
	Ref. 60	39.497	8.858	8.776	90.0	90.0	90.0
$(\text{BA})_2(\text{MA})_2\text{Sn}_3\text{I}_{10}$	PBE-D3	8.551	50.184	9.085	89.4	90.9	92.0
	Ref. 15	8.795	51.921	8.858	90.0	90.0	90.0



Table 2 Band gaps (E_g), Sn–I–Sn bond angles (\angle_{SnISn}), hole (m_h^{\parallel}) and electron (m_e^{\parallel}) effective masses, dielectric constants (ϵ_r), and SLMEs of the series $(\text{BA})_2(\text{MA})_{n-1}\text{Sn}_n\text{I}_{3n+1}$ ($n = 1, 2$ and 3). Hole and electron effective masses are averaged for the directions parallel to the perovskite layer. Superscripts \parallel and \perp indicate properties parallel (in-plane) and perpendicular (out-of-plane) to the 2D perovskite sheets, respectively. Band gaps given in eV, bond angles given in $^\circ$, effective masses given in units of electron rest mass (m_0), and SLME given in %

Compounds	E_g	\angle_{SnISn}	$\angle_{\text{SnISn}}^{\parallel}$	$\angle_{\text{SnISn}}^{\perp}$	m_h^{\parallel}	m_e^{\parallel}	ϵ_r^{\parallel}	ϵ_r^{\perp}	SLME ^a
$(\text{BA})_2\text{SnI}_4^{\text{rt}}$	1.85	153.5	26.4	2.3	0.13	0.15	21.24	4.36	19.01
$(\text{BA})_2\text{SnI}_4^{\text{lt}}$	2.13	149.6	21.3	22.3	0.20	0.18	31.87	5.19	15.24
$(\text{BA})_2(\text{MA})\text{Sn}_2\text{I}_7$	1.50	168.3	5.3	7.8	0.13	0.14	34.05	11.71	22.64
$(\text{BA})_2(\text{MA})_2\text{Sn}_3\text{I}_{10}$	1.38	168.2	7.3	9.1	0.13	0.13	47.99	9.77	24.64

^a Thickness: 0.5 μm .

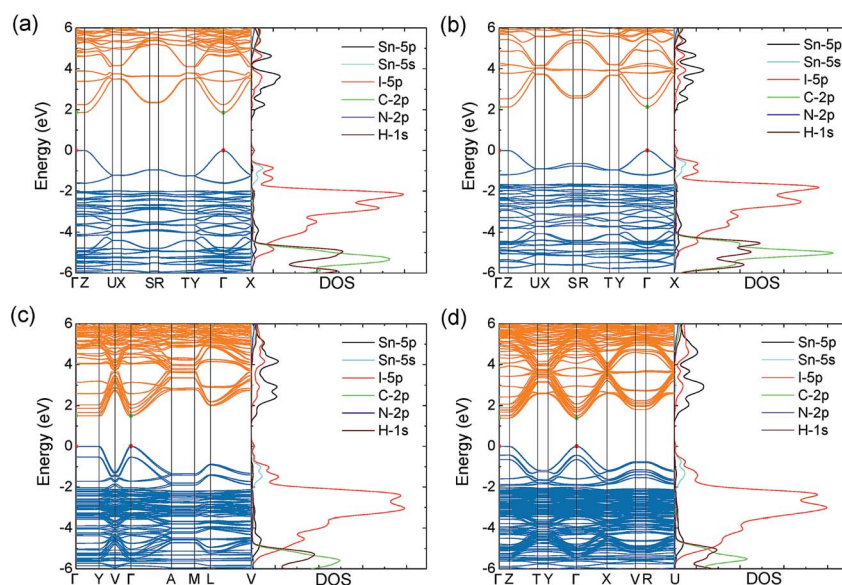


Fig. 2 HSE43 + SOC calculated band structures and density of states (DOS) for the layered tin hybrid perovskites: (a) $(\text{BA})_2\text{SnI}_4^{\text{rt}}$, (b) $(\text{BA})_2\text{SnI}_4^{\text{lt}}$, (c) $(\text{BA})_2(\text{MA})\text{Sn}_2\text{I}_7$, and (d) $(\text{BA})_2(\text{MA})_2\text{Sn}_3\text{I}_{10}$. The valence band maximum is set to 0 eV. Valence and conduction bands indicated by blue and orange lines, respectively. Red and green circles indicate the position of the valence band maximum and conduction band minimum.

parallel to the 2D sheets (in all cases below $0.2m_0$). Moving across the series, the carrier effective masses decrease as the thickness of the inorganic layer increases. In particular, the $n = 3$ composition possesses light hole and electron effective masses of $0.13m_0$ and $0.13m_0$, respectively, smaller than those of MAPbI_3 ($0.25m_0$ and $0.19m_0$) and comparable to the effective masses of MASnI_3 ($0.13m_0$ and $0.28m_0$) calculated by GW + SOC.⁴⁸ In general, the series shows slightly larger masses than their lead analogues, such as $(\text{BA})_2\text{PbI}_4$ ($0.14m_0$ and $0.08m_0$), $(\text{BA})_2(\text{MA})_2\text{Pb}_3\text{I}_{10}$ ($0.14m_0$ and $0.10m_0$), $(\text{BA})_2(\text{MA})_3\text{Pb}_4\text{I}_{13}$ ($0.15m_0$ and $0.09m_0$), as calculated by Stoumpos *et al.*²⁵ We note that the calculations performed by Stoumpos *et al.* did not include the effects of spin–orbit coupling, and may therefore not accurately represent the true properties of the systems.

Previous reports have indicated the Sn–I–Sn bond angle (\angle_{SnISn}) as a primary factor in the controlling electronic properties of lead and tin based layered perovskites.^{24,61,62} This bond angle quantifies the degree of distortion in the SnI_6^{4-} octahedra, with a value of 180° indicating the ideal (undistorted) structure. This distortion can be further broken down into its

in-plane ($\angle_{\text{SnISn}}^{\parallel}$) and out-of-plane ($\angle_{\text{SnISn}}^{\perp}$) components. Analysis of the distortion angle provides an explanation for the discrepancy in band gap between room temperature and low temperature $n = 1$ structures (Table 2). The greater distortion in the Sn–I–Sn bond angle of $(\text{BA})_2\text{SnI}_4^{\text{lt}}$ (149.6°) gives rise to an increased band gap of 2.13 eV, compared with a band gap of 1.85 eV for the room temperature structure (153.5°). The Sn–I–Sn angle, when decomposed into its out-of-plane and in-plane contributions, indicates the in-plane distortion remains similar (26.4° vs. 21.3°), whereas the out-of-plane distortion is significantly greater in the tilted structure (22.3° vs. 2.3°), and is therefore likely responsible for the variation in band gap. We note, that in general our results contrast previous reports, which suggest the in-plane distortion plays a greater role in tuning the band gap.^{61,62} In reality, as both distortions occur simultaneously, the effect of the distortions will be cooperative and should be considered at the same time, as quantified by the overall Sn–I–Sn bond angle. For the $n = 2$ and 3 structures, the tilting angles were found to be close to the ideal (168.3° and 168.2°), indicating relatively little structural distortion.



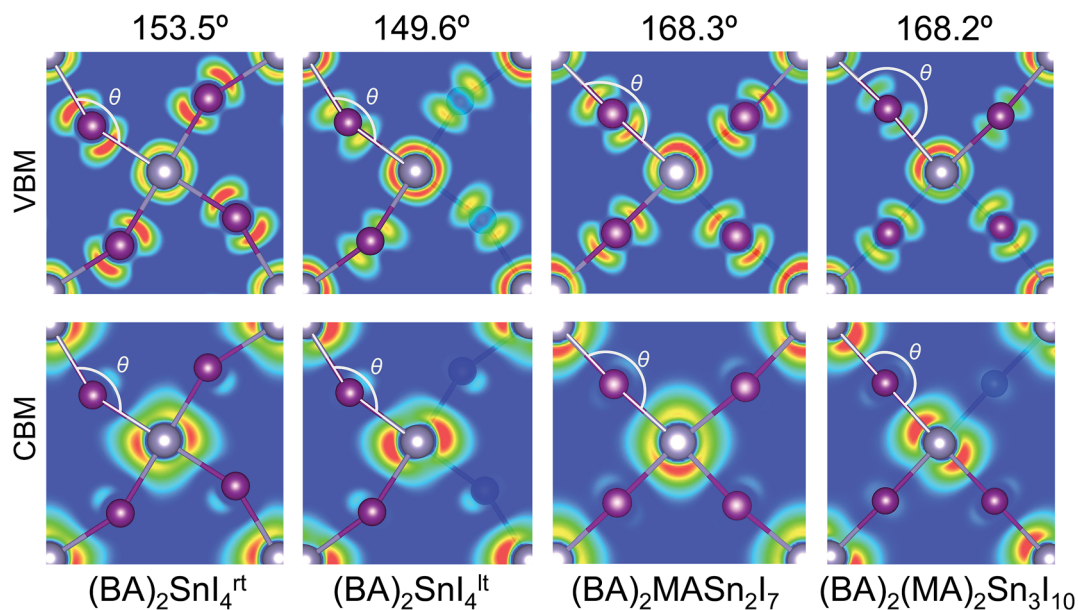


Fig. 3 Charge density isosurfaces of the VBM (above) and CBM (below), pictured along the (001) direction, for the layered tin hybrid perovskites: $(\text{BA})_2\text{SnI}_4^{\text{rt}}$, $(\text{BA})_2\text{SnI}_4^{\text{lt}}$, $(\text{BA})_2(\text{MA})\text{Sn}_2\text{I}_7$ and $(\text{BA})_2(\text{MA})_2\text{Sn}_3\text{I}_{10}$, where the Sn and I atoms are shown in light grey and purple, with the Sn–I–Sn bond angles of each compound indicated. The organic cations have been removed for clarity.

The charge density isosurfaces shown in Fig. 3, provide an explanation for the effect of Sn–I–Sn bond angle on electronic properties. Due to the structural distortion, the in-plane I atoms are displaced such that they do not sit directly between two adjacent Sn atoms. As demonstrated in the inorganic perovskite, CsPbI_3 ,^{61,62} greater distortion results in a reduction of the in-plane orbital overlap of the states that comprise the upper valence band (Sn 5s and I 5p), producing larger hole effective masses and a narrower valence band width. Likewise, a similar effect is found on the lower conduction band overlap (composed of Sn 5p and a small contribution from the I 5p), which increases its band width and results in greater electron effective masses. For example, within the $n = 1$ structures, the greater distortion of $(\text{BA})_2\text{SnI}_4^{\text{lt}}$ (149.6°) compared to $(\text{BA})_2\text{SnI}_4^{\text{rt}}$ (153.5°), results in a wider band gap (2.13 eV), larger effective masses of electrons ($0.20m_0$) and holes ($0.18m_0$), and reduced valence (0.95 eV) and conduction band widths (1.53 eV). Further analysis of the charge density isosurfaces in the two $n = 1$ structures (Fig. S3 of the ESI†), indicates the conduction band minima are derived mainly of Sn 5p_x and p_y orbitals, with the p_z orbital showing very little contribution. For this reason, the out-of-plane distortion will have a reduced impact on the electronic properties of the conduction band, compared with the in-plane distortion, explaining the limited variation in electron effective masses and conduction band widths between the two structures. For the $n = 2$, and 3 structures, the minimal distortion further produces optimal optoelectronic properties, such as small band gaps very light hole and electron effective masses.

Optical properties

In comparison to the 3D hybrid perovskites, the unique layered configuration introduces a directional dependence into the

dielectric constants and optical response. 2D perovskites can be regarded as quantum-well-like structures, of which the inorganic sheets (“wells”) are more polarisable, and the organic layers (“barriers”) are less polarisable.^{63,64} Previous computational studies have shown that in the 2D hybrid perovskites, the dielectric constant of the inorganic component is significantly greater than that of the organic layer.^{65,66} Since the bulk dielectric response calculated here corresponds to an average over both the inorganic and organic components, those compounds with thicker inorganic layers should possess greater dielectric constants. This is in agreement with our results, which show that both the in-plane ($\epsilon_{\parallel}^{\text{r}}$) and out-of-plane ($\epsilon_{\perp}^{\text{r}}$) dielectric constants increase as the thickness of the perovskite-like layer increases. For the $n = 1$ $(\text{BA})_2\text{SnI}_4^{\text{rt}}$ structure, the in-plane and out-of-plane dielectric constants are 21.24 and 4.36, respectively, which increase to 34.05 and 11.71 for the $n = 2$ structure, and 47.99 and 9.77 in the $n = 3$ case. As n decreases, the negative charge arising from the perovskite-like surface is distributed over a decreasing number of Sn and I ions. This has the effect of making these ions less positive, in turn reducing their polarisability and thus their ability to screen charge, as evidenced by the reduction in their Born effective charge (provided in Table S3 of the ESI†). In general, the dielectric constants for the direction perpendicular to the perovskite sheets are much smaller than those in the parallel directions. Again, the Sn–I–Sn bond angle plays an important role, with the low temperature, more distorted structure ($(\text{BA})_2\text{SnI}_4^{\text{lt}}$) actually showing larger in-plane and out-of-plane dielectric constants (31.87 and 5.19, respectively) than the room temperature compound.

As discussed in the introduction, one of the advantages of the tin layered perovskites over their lead analogues is that their fundamental band gaps are closer to the optimum value for



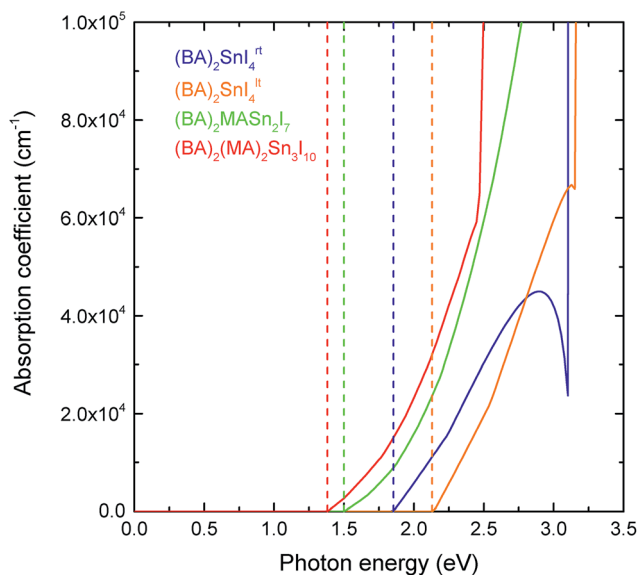


Fig. 4 Calculated optical absorption spectra for layered tin hybrid perovskites: $(\text{BA})_2\text{SnI}_4^{\text{TT}}$, $(\text{BA})_2\text{SnI}_4^{\text{IT}}$, $(\text{BA})_2(\text{MA})\text{SnI}_3\text{I}_7$ and $(\text{BA})_2(\text{MA})_2\text{Sn}_3\text{I}_{10}$, where the vertical dash lines are the corresponding fundamental band gaps.

a single junction solar cell.³⁰ The optical response for the series, calculated using HSE43 + SOC, is provided in Fig. 4. Similar to other layered perovskites,^{11,12,25} an increase in the perovskite-like layer thickness causes a red shifting of the absorption edge. In all cases, the optical absorption edges of the $(\text{BA})_2(\text{MA})_{n-1}\text{Sn}_n\text{I}_{3n+1}$ ($n = 1, 2$ and 3) series are located at the fundamental band gaps, indicating that the fundamental band gap transitions are symmetry allowed. All four perovskites studied exhibit strong optical absorption, with the absorption coefficient reaching 10^5 cm^{-1} within $\sim 1 \text{ eV}$ of the band edge. The strength of optical absorption is dependent on the thickness of the inorganic component—as the number of layers increases, the optical absorption gets stronger. This is to be expected as the organic cations do not contribute to the optical response until larger excitation energies.

In the Shockley–Queisser limit,²⁹ the efficiency of an absorber is dependant solely on its band gap. In practice, however, strong visible light absorption as well as a fundamental allowed band gap transition are also critical for achieving high efficiency cells. In a real solar cell, the maximum efficiency is also determined by the thickness of the absorber layer. After taking all the above factors into consideration, the maximum photovoltaic efficiency of an ideal absorber thin film can be simulated using the spectroscopic limited maximum efficiency (SLME) metric proposed by Yu and Zunger.⁶⁷ The SLME metric improves on the Shockley–Queisser limit in a number of ways: firstly, the non-radiative recombination rate is approximated, based on the difference between the lowest allowed optical transition and the fundamental band gap; secondly, the frequency dependant absorption coefficient of the material is taken into account; lastly, the thin-film thickness is also considered. The full details of how the SLME is calculated are provided in the ESI.†

In order to evaluate the photovoltaic performance of these 2D perovskites, the SLMEs, computed based on a thin film thickness of $0.5 \mu\text{m}$, are listed in Table 2. The $n = 3$ composition possesses the highest efficiency (24.6%) as expected based on its high optical absorption coefficient and favourable band gap (1.38 eV), which is close to the optimal value based on the Shockley–Queisser limit. The predicted SLME values are significantly higher than efficiencies of the devices produced by Cao *et al.*,¹⁰ highlighting the potential of further device engineering. The high SLME of $(\text{BA})_2(\text{MA})_2\text{Sn}_3\text{I}_{10}$ is comparable to that of many state-of-art solar cell absorbers, such as CdTe (24.85%) and CuZnSnS (25.71%), and even greater than that of MAPbI₃ (22.1%), further confirming its potential as a lead-free replacement to the 3D hybrid perovskites.⁶⁸

Conclusion

In summary, we have shown that the layered lead-free perovskites $(\text{BA})_2(\text{MA})_{n-1}\text{Sn}_n\text{I}_{3n+1}$ ($\text{BA} = \text{CH}_3(\text{CH}_2)_3\text{NH}_3^+$, $\text{MA} = \text{CH}_3\text{NH}_3^+$, $n = 1, 2$ and 3) exhibit intrinsic properties that are well suited for solar cell applications, including band gaps close to the ideal indicated by the Shockley–Queisser limit and strong optical absorption. Furthermore, both electrons and holes show small effective masses in the directions parallel to the perovskite-like sheets. We have further elucidated the role that structural distortions, in the form of octahedral tilting, play in determining the optoelectronic properties of the series. Impressively, the champion absorber, $(\text{BA})_2(\text{MA})_2\text{Sn}_3\text{I}_{10}$ ($n = 3$), displays a high spectroscopic limited maximum efficiency greater than 24%. Based on these properties, the structures where $n \leq 2$, are promising candidates for top cells in tandem devices, whereas the $n = 3$ composition is expected to perform well in a heterojunction solar cell in its own right. Despite the low power conversion efficiencies previously demonstrated by Cao *et al.*,²⁶ our results indicate a significant scope for improvement and suggest further device engineering and optimisation may be fruitful.

Conflicts of interest

There are no conflicts to declare.

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References

- 1 J. Chow, R. J. Kopp and P. R. Portney, Energy resources and global development, *Science*, 2003, **302**, 1528–1531.
- 2 Q. Schiermeier, J. Tollefson, T. Scully, A. Witze and O. Morton, Energy alternatives: Electricity without carbon, *Nature*, 2008, **454**, 816–823.
- 3 A. Polman, M. Knight, E. C. Garnett, B. Ehrler and W. C. Sinke, Photovoltaic materials: Present efficiencies and future challenges, *Science*, 2016, **352**, aad4424.
- 4 H.-S. Kim, C.-R. Lee, J.-H. Im, K.-B. Lee, T. Moehl, A. Marchioro, S.-J. Moon, R. Humphry-Baker, J.-H. Yum, J. E. Moser, M. Grätzel and N.-G. Park, Lead iodide perovskite sensitized all-solid-state submicron thin film mesoscopic solar cell with efficiency exceeding 9%, *Sci. Rep.*, 2012, **2**, 591.
- 5 W. S. Yang, B.-W. Park, E. H. Jung, N. J. Jeon, Y. C. Kim, D. U. Lee, S. S. Shin, J. Seo, E. K. Kim, J. H. Noh and S. I. Seok, Iodide management in formamidinium-lead-halide-based perovskite layers for efficient solar cells, *Science*, 2017, **356**, 1376–1379.
- 6 S. Ahmad, P. K. Kanaujia, H. J. Beeson, A. Abate, F. Deschler, D. Credgington, U. Steiner, G. V. Prakash and J. J. Baumberg, Strong Photocurrent from Two-Dimensional Excitons in Solution-processed Stacked Perovskite Semiconductor Sheets, *ACS Appl. Mater. Interfaces*, 2015, **7**, 25227–25236.
- 7 G. Nagabhushana, R. Shivaramaiah and A. Navrotsky, Direct calorimetric verification of thermodynamic instability of lead halide hybrid perovskites, *Proc. Natl. Acad. Sci. U. S. A.*, 2016, **113**, 7717–7721.
- 8 G. Niu, X. Guo and L. Wang, Review of recent progress in chemical stability of perovskite solar cells, *J. Mater. Chem. A*, 2015, **3**, 8970–8980.
- 9 I. C. Smith, E. T. Hoke, D. Solis-Ibarra, M. D. McGehee and H. I. Karunadasa, A Layered Hybrid Perovskite Solar-Cell Absorber with Enhanced Moisture Stability, *Angew. Chem., Int. Ed.*, 2014, **126**, 11414–11417.
- 10 D. H. Cao, C. C. Stoumpos, O. K. Farha, J. T. Hupp and M. G. Kanatzidis, 2D homologous perovskites as light-absorbing materials for solar cell applications, *J. Am. Chem. Soc.*, 2015, **137**, 7843–7850.
- 11 H. Tsai, W. Nie, J.-C. Blancon, C. C. Stoumpos, R. Asadpour, B. Harutyunyan, A. J. Neukirch, R. Verduzco, J. J. Crochet, S. Tretiak, L. Pedesseau, J. Even, M. A. Alam, G. Gupta, J. Lou, P. M. Ajayan, M. J. Bedzyk, M. G. Kanatzidis and A. D. Mohite, High-efficiency two-dimensional Ruddlesden-Popper perovskite solar cells, *Nature*, 2016, **536**, 312–316.
- 12 L. N. Quan, M. Yuan, R. Comin, O. Voznyy, E. M. Beauregard, S. Hoogland, A. Buin, A. R. Kirmani, K. Zhao, A. Amassian, D. H. Kim and E. H. Sargent, Ligand-stabilized reduced-dimensionality perovskites, *J. Am. Chem. Soc.*, 2016, **138**, 2649–2655.
- 13 G. Kieslich, S. Sun and A. K. Cheetham, An extended tolerance factor approach for organic–inorganic perovskites, *Chem. Sci.*, 2015, **6**, 3430–3433.
- 14 W. Travis, E. Glover, H. Bronstein, D. Scanlon and R. Palgrave, On the application of the tolerance factor to inorganic and hybrid halide perovskites: a revised system, *Chem. Sci.*, 2016, **7**, 4548–4556.
- 15 D. B. Mitzi, C. Feild, W. Harrison and A. Guloy, Conducting tin halides with a layered organic-based perovskite structure, *Nature*, 1994, **369**, 467–469.
- 16 D. Bi, P. Gao, R. Scopelliti, E. Oveisi, J. Luo, M. Grätzel, A. Hagfeldt and M. K. Nazeeruddin, High-Performance Perovskite Solar Cells with Enhanced Environmental Stability Based on Amphiphile-Modified $\text{CH}_3\text{NH}_3\text{PbI}_3$, *Adv. Mater.*, 2016, **28**, 2910–2915.
- 17 D. B. Mitzi, K. Chondroudis and C. R. Kagan, Organic–inorganic electronics, *IBM J. Res. Dev.*, 2001, **45**, 29–45.
- 18 W. Jiang, J. Ying, W. Zhou, K. Shen, X. Liu, X. Gao, F. Guo, Y. Gao and T. Yang, A new layered nano hybrid perovskite film with enhanced resistance to moisture-induced degradation, *Chem. Phys. Lett.*, 2016, **658**, 71–75.
- 19 T. Hattori, T. Taira, M. Era, T. Tsutsui and S. Saito, Highly efficient electroluminescence from a heterostructure device combined with emissive layered-perovskite and an electron-transporting organic compound, *Chem. Phys. Lett.*, 1996, **254**, 103–108.
- 20 G. V. Prakash, Naturally self-assembled nanosystems and their templated structures for photonic applications, *J. Nanopart.*, 2013, **2013**, 2013.
- 21 M. C. Weidman, M. Seitz, S. D. Stranks and W. A. Tisdale, Highly tunable colloidal perovskite nanoplatelets through variable cation, metal, and halide composition, *ACS Nano*, 2016, **8**, 7830–7839.
- 22 F. Hao, C. C. Stoumpos, D. H. Cao, R. P. Chang and M. G. Kanatzidis, Lead-free solid-state organic–inorganic halide perovskite solar cells, *Nat. Photonics*, 2014, **8**, 489–494.
- 23 N. K. Noel, S. D. Stranks, A. Abate, C. Wehrenfennig, S. Guarnera, A.-A. Haghighirad, A. Sadhanala, G. E. Eperon, S. K. Pathak, M. B. Johnston, A. Petrozza, L. M. Herz and H. J. Snaith, Lead-free organic–inorganic tin halide perovskites for photovoltaic applications, *Energy Environ. Sci.*, 2014, **7**, 3061–3068.
- 24 C. C. Stoumpos, L. Frazer, D. J. Clark, Y. S. Kim, S. H. Rhim, A. J. Freeman, J. B. Ketterson, J. I. Jang and M. G. Kanatzidis, Hybrid germanium iodide perovskite semiconductors: active lone pairs, structural distortions, direct and indirect energy gaps, and strong nonlinear optical properties, *J. Am. Chem. Soc.*, 2015, **137**, 6804–6819.
- 25 C. C. Stoumpos, D. H. Cao, D. J. Clark, J. Young, J. M. Rondinelli, J. I. Jang, J. T. Hupp and M. G. Kanatzidis, Ruddlesden–Popper hybrid lead iodide perovskite 2D homologous semiconductors, *Chem. Mater.*, 2016, **28**, 2852–2867.
- 26 D. H. Cao, C. C. Stoumpos, T. Yokoyama, J. L. Logsdon, T.-B. Song, O. K. Farha, M. R. Wasielewski, J. T. Hupp and M. G. Kanatzidis, Thin Films and Solar Cells Based on Semiconducting Two-Dimensional Ruddlesden–Popper $(\text{CH}_3(\text{CH}_2)_3\text{NH}_3)_2(\text{CH}_3\text{NH}_3)_{n-1}\text{Sn}_n\text{I}_{3n+1}$ Perovskites, *ACS Energy Lett.*, 2017, **2**, 982–990.



- 27 A. M. Ganose, C. N. Savory and D. O. Scanlon, Beyond Methylammonium Lead Iodide: Prospects for the Emergent Field of ns^2 Containing Solar Absorbers, *Chem. Commun.*, 2017, **53**, 20–44.
- 28 S. J. Lee, S. S. Shin, Y. C. Kim, D. Kim, T. K. Ahn, J. H. Noh, J. Seo and S. I. Seok, Fabrication of efficient formamidinium tin iodide perovskite solar cells through SnF_2 -pyrazine complex, *J. Am. Chem. Soc.*, 2016, **138**, 3974–3977.
- 29 W. Shockley and H. J. Queisser, Detailed balance limit of efficiency of p–n junction solar cells, *J. Appl. Phys.*, 1961, **32**, 510–519.
- 30 L. Yu, R. S. Kokenyesi, D. A. Keszler and A. Zunger, Inverse Design of High Absorption Thin-Film Photovoltaic Materials, *Adv. Energy Mater.*, 2013, **3**, 43–48.
- 31 G. Kresse and J. Hafner, *Ab initio* molecular dynamics for liquid metals, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1993, **47**, 558.
- 32 G. Kresse and J. Hafner, *Ab initio* molecular-dynamics simulation of the liquid-metal-amorphous-semiconductor transition in germanium, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1994, **49**, 14251.
- 33 G. Kresse and J. Furthmüller, Efficient iterative schemes for *ab initio* total-energy calculations using a plane-wave basis set, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1996, **54**, 11169.
- 34 G. Kresse and J. Furthmüller, Efficiency of *ab initio* total energy calculations for metals and semiconductors using a plane-wave basis set, *Comput. Mater. Sci.*, 1996, **6**, 15–50.
- 35 P. E. Blöchl, Projector augmented-wave method, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1994, **50**, 17953.
- 36 G. Kresse and D. Joubert, From ultrasoft pseudopotentials to the projector augmented-wave method, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1999, **59**, 1758.
- 37 F. Brivio, A. B. Walker and A. Walsh, Structural and Electronic Properties of Hybrid Perovskites for High-Efficiency Thin-Film Photovoltaics from First-Principles, *APL Mater.*, 2013, **1**, 042111.
- 38 K. T. Butler, J. M. Frost and A. Walsh, Band alignment of the hybrid halide perovskites $\text{CH}_3\text{NH}_3\text{PbCl}_3$, $\text{CH}_3\text{NH}_3\text{PbBr}_3$ and $\text{CH}_3\text{NH}_3\text{PbI}_3$, *Mater. Horiz.*, 2015, **2**, 228–231.
- 39 C. N. Savory, R. G. Palgrave, H. Bronstein and D. O. Scanlon, Spatial Electron-hole Separation in a One Dimensional Hybrid Organic-Inorganic Lead Iodide, *Sci. Rep.*, 2016, **6**, 20626.
- 40 J. P. Perdew, K. Burke and M. Ernzerhof, Generalized gradient approximation made simple, *Phys. Rev. Lett.*, 1996, **77**, 3865.
- 41 S. Grimme, Accurate description of van der Waals complexes by density functional theory including empirical corrections, *J. Comput. Chem.*, 2004, **25**, 1463–1473.
- 42 J. P. Perdew, A. Ruzsinszky, G. I. Csonka, O. A. Vydrov, G. E. Scuseria, L. A. Constantin, X. Zhou and K. Burke, Restoring the density-gradient expansion for exchange in solids and surfaces, *Phys. Rev. Lett.*, 2008, **100**, 136406.
- 43 A. M. Ganose, K. T. Butler, A. Walsh and D. O. Scanlon, Relativistic electronic structure and band alignment of BiSI and BiSeI: candidate photovoltaic materials, *J. Mater. Chem. A*, 2016, **4**, 2060–2068.
- 44 A. M. Ganose, C. N. Savory and D. O. Scanlon, Electronic and defect properties of $(\text{CH}_3\text{NH}_3)_2\text{Pb}(\text{SCN})_2\text{I}_2$ analogues for photovoltaic applications, *J. Mater. Chem. A*, 2017, **5**, 7845–7853.
- 45 J. Heyd, G. E. Scuseria and M. Ernzerhof, Hybrid functionals based on a screened Coulomb potential, *J. Chem. Phys.*, 2003, **118**, 8207–8215.
- 46 J. Heyd, G. E. Scuseria and M. Ernzerhof, Erratum: “Hybrid functionals based on a screened Coulomb potential” [*J. Chem. Phys.* 118, 8207 (2003)], *J. Chem. Phys.*, 2006, **124**, 219906.
- 47 M. H. Du, Efficient carrier transport in halide perovskites: theoretical perspectives, *J. Mater. Chem. A*, 2014, **2**, 9091–9098.
- 48 P. Umari, E. Mosconi and F. De Angelis, Relativistic GW calculations on $\text{CH}_3\text{NH}_3\text{PbI}_3$ and $\text{CH}_3\text{NH}_3\text{SnI}_3$ perovskites for solar cell applications, *Sci. Rep.*, 2014, **4**, 4467.
- 49 C. Bernal and K. Yang, First-principles hybrid functional study of the organic-inorganic perovskites $\text{CH}_3\text{NH}_3\text{SnBr}_3$ and $\text{CH}_3\text{NH}_3\text{SnI}_3$, *J. Phys. Chem. C*, 2014, **118**, 24383–24388.
- 50 J. Im, C. C. Stoumpos, H. Jin, A. J. Freeman and M. G. Kanatzidis, Antagonism between Spin-Orbit Coupling and Steric Effects Causes Anomalous Band Gap Evolution in the Perovskite Photovoltaic Materials $\text{CH}_3\text{NH}_3\text{Sn}_{1-x}\text{Pb}_x\text{I}_3$, *J. Phys. Chem. Lett.*, 2015, **6**, 3503–3509.
- 51 J. Even, L. Pedesseau, J.-M. Jancu and C. Katan, DFT and k-p modelling of the phase transitions of lead and tin halide perovskites for photovoltaic cells, *Phys. Status Solidi RRL*, 2014, **8**, 31–35.
- 52 P. E. Blöchl, O. Jepsen and O. K. Andersen, Improved tetrahedron method for Brillouin-zone integrations, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1994, **49**, 16223.
- 53 M. Gajdoš, K. Hummer, G. Kresse, J. Furthmüller and F. Bechstedt, Linear Optical Properties in the Projector-Augmented Wave Methodology, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2006, **73**, 045112.
- 54 S. Baroni, S. De Gironcoli, A. Dal Corso and P. Giannozzi, Phonons and related crystal properties from density-functional perturbation theory, *Rev. Mod. Phys.*, 2001, **73**, 515.
- 55 R. Dronskowski and P. E. Blochl, Crystal orbital Hamilton populations (COHP): energy-resolved visualization of chemical bonding in solids based on density-functional calculations, *J. Phys. Chem.*, 1993, **97**, 8617–8624.
- 56 S. Maintz, V. L. Deringer, A. L. Tchougréeff and R. Dronskowski, Analytic projection from plane-wave and PAW wavefunctions and application to chemical-bonding analysis in solids, *J. Comput. Chem.*, 2013, **34**, 2557–2567.
- 57 J. Calabrese, N. Jones, R. Harlow, N. Herron, D. Thorn and Y. Wang, Preparation and characterization of layered lead halide compounds, *J. Am. Chem. Soc.*, 1991, **113**, 2328–2330.
- 58 C. Motta, F. El-Mellouhi, S. Kais, N. Tabet, F. Alharbi and S. Sanvito, Revealing the role of organic cations in hybrid halide perovskite $\text{CH}_3\text{NH}_3\text{PbI}_3$, *Nat. Commun.*, 2015, **6**, 7026.
- 59 Y. Takahashi, R. Obara, K. Nakagawa, M. Nakano, J.-y. Tokita and T. Inabe, Tunable Charge Transport in Soluble Organic-Inorganic Hybrid Semiconductors, *Chem. Mater.*, 2007, **19**, 6312–6316.



- 60 C. C. Stoumpos, L. Mao, C. D. Malliakas and M. G. Kanatzidis, Structure-Band Gap Relationships in Hexagonal Polytypes and Low-Dimensional Structures of Hybrid Tin Iodide Perovskites, *Inorg. Chem.*, 2017, **56**, 56–73.
- 61 J. L. Knutson, J. D. Martin and D. B. Mitzi, Tuning the band gap in hybrid tin iodide perovskite semiconductors using structural templating, *Inorg. Chem.*, 2005, **44**, 4699–4705.
- 62 Z. Xiao, W. Meng, J. Wang, D. B. Mitzi and Y. Yan, Searching for promising new perovskite-based photovoltaic absorbers: the importance of electronic dimensionality, *Mater. Horiz.*, 2017, **4**, 206–216.
- 63 T. Ishihara, Optical properties of PbI-based perovskite structures, *J. Lumin.*, 1994, **60**, 269–274.
- 64 J. Even, L. Pedesseau and C. Katan, Understanding quantum confinement of charge carriers in layered 2D hybrid perovskites, *ChemPhysChem*, 2014, **15**, 3733–3741.
- 65 D. Saponi, M. Kepenekian, L. Pedesseau, C. Katan and J. Even, Quantum confinement and dielectric profiles of colloidal nanoplatelets of halide inorganic and hybrid organic–inorganic perovskites, *Nanoscale*, 2016, **8**, 6369–6378.
- 66 M. D. Smith, L. Pedesseau, M. Kepenekian, I. C. Smith, C. Katan, J. Even and H. I. Karunadasa, Decreasing the electronic confinement in layered perovskites through intercalation, *Chem. Sci.*, 2017, **8**, 1960–1968.
- 67 L. Yu and A. Zunger, Identification of potential photovoltaic absorbers based on first-principles spectroscopic screening of materials, *Phys. Rev. Lett.*, 2012, **108**, 068701.
- 68 Unpublished results provided by internal correspondence with C. N. Savory.

