



Cite this: *Soft Matter*, 2018, 14, 9083

Received 25th June 2018,  
Accepted 31st October 2018

DOI: 10.1039/c8sm01298a

rsc.li/soft-matter-journal

## Charge polarization, local electroneutrality breakdown and eddy formation due to electroosmosis in varying-section channels†

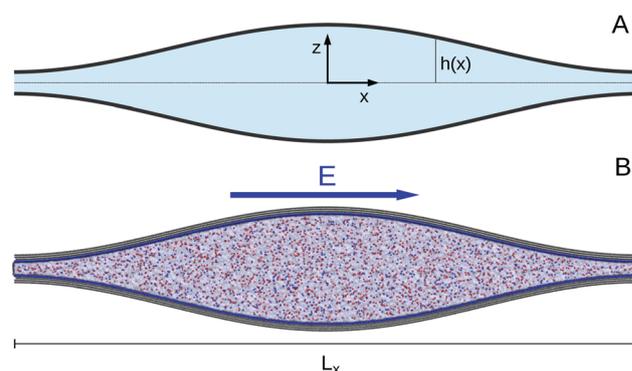
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**We characterize the dynamics of an electrolyte embedded in a varying-section channel under the action of a constant external electrostatic field. By means of molecular dynamics simulations we determine the stationary density, charge and velocity profiles of the electrolyte. Our results show that when the Debye length is comparable to the width of the channel bottlenecks a concentration polarization along with two eddies sets inside the channel. Interestingly, upon increasing the external field, local electroneutrality breaks down and charge polarization sets leading to the onset of net dipolar field. This novel scenario, that cannot be captured by the standard approaches based on local electroneutrality, opens the route for the realization of novel micro and nano-fluidic devices.**

The transport of ions, molecules and polymers across constrictions such as pores, membranes or varying-section micro-nano-channels is crucial for several biological as well as synthetic systems. For example, in biological cells ion channels control the uptake of ions from the environment<sup>1</sup> whereas, in resistive pulse sensing techniques, the interactions of colloidal particles<sup>2</sup> or macromolecules<sup>3–7</sup> with the nano- or micro-pore are measured from the variation of the electric conductance of the pore induced by the presence of the particle. Moreover, electro-osmotic flux can play a crucial role in molecule capturing in nanopores.<sup>8–10</sup> Recent studies have shown that ionic transport and electro-osmotic flow in micro- and nano-fluidic circuitry can be controlled by tuning the geometry of the micro-nano-channel.<sup>11–13</sup> Indeed, conical<sup>14–16</sup> or heterogeneously charged<sup>17</sup> pores have been used to realize nano-fluidic diodes and to rectify electro-osmotic flows.<sup>18,19</sup> Moreover, periodic varying-section channels have been used to realize nano-fluidic transistors.<sup>20</sup> Similarly, recent contributions have shown that the shape of the confining vessel and the boundary conditions

therein imposed can be exploited to control the flow. Indeed, electro-osmotic transport can be strongly enhanced by grafting charged brushes on the channel walls<sup>21</sup> and by hydrophobic surfaces.<sup>22</sup>

In this contribution, we study, *via* molecular dynamics simulations the electro-osmotic flow of an electrolyte embedded in a varying-section channel. The advantage of our approach, as compared to others based on the solution of some continuum models,<sup>23–27</sup> is that the ionic densities are left free to relax according to the interactions among ions and between ions and the channel walls. Therefore our approach allows us to critically discuss, for example, the local electroneutrality assumption and its possible breakdown. Our results show that when the systems is driven by a constant electrostatic field acting along the longitudinal axis of the channel, inhomogeneous ionic and charge densities are induced due to the variations of local channel section. This phenomenon is similar to concentration polarization (CP) reported for electrolytes transported across



**Fig. 1** System set-up. (A) Sketch of the system. The electrolyte solution (light blue) is confined between two curved charged walls. Half section is  $h(x) = h_0 + h_1 \cos \frac{2\pi x}{L_x}$ . Periodic boundary conditions are applied in the  $x$  and  $y$  direction. (B) Snapshot of molecular dynamics set-up. The solid walls (gray) are constituted by Lennard-Jones atoms. The atoms of the layer exposed to the liquid are charged (blue). Water molecules are not reported while blue and red spheres represent  $K^+$  and  $Cl^-$  ions. An external electrical field parallel to the  $x$ -axes is applied.

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† Electronic supplementary information (ESI) available. See DOI: 10.1039/c8sm01298a



ionic-selective membranes<sup>23,25,28</sup> (see also ref. 29 and 30 for recent reviews) *i.e.*, in open circuit conditions and under severe modulations of channel section.<sup>25,27,28</sup> Interestingly, our results show that CP can be obtained also for close circuit conditions and for smooth variations of channel section. In particular, we observe CP when the Debye length is comparable with the channel bottlenecks, *i.e.*, in the entropic electrokinetic regime.<sup>31</sup> Concerning local electroneutrality, our numerical results confirm that even in the entropic electrokinetic regime, the local electroneutrality assumed by previous works<sup>26,27,30,32</sup> is fulfilled for mild values of the external field. However, upon increasing the external field our numerical simulations show that local electroneutrality breaks down and charge polarization (QP) sets, leading to the onset of a net dipolar contribution to the electrostatic field. Interestingly, a similar phenomenon has been recently observed for pressure-driven flows across conical pores.<sup>33</sup>

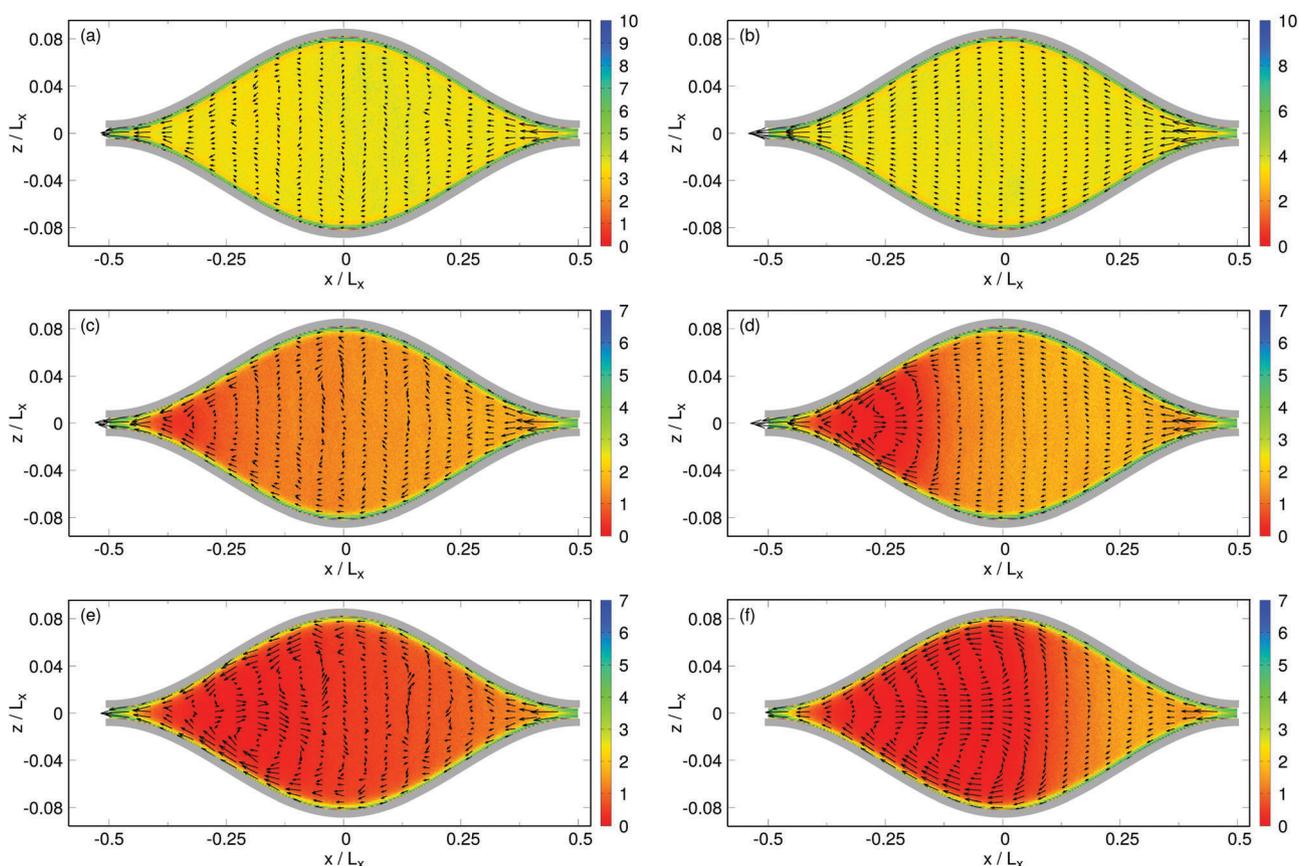
## Results

We study the electro-osmotic flow (see ESI† for the details) of a KCl water solution across a channel with half section

$$h(x) = h_0 + h_1 \cos(2\pi x/L_x) \quad (1)$$

with average section  $h_0 = 38.5 \text{ \AA}$  and modulation  $h_1 = 32.5 \text{ \AA}$  and periodicity  $L_x = 836.6 \text{ \AA}$ , see Fig. 1. Channel section is constant along the  $y$  direction, with thickness  $L_y = 60.37 \text{ \AA}$ , and periodic boundary conditions are applied along  $x$  and  $y$ . Both channel walls are covered with a constant charge density  $\sigma = 0.15 \text{ C m}^{-2}$ . The system is globally electroneutral since we compensated the wall charge with additional  $\text{Cl}^-$  ions. After equilibration, a homogeneous and constant external electric field  $E = (E_x, 0, 0)$  is applied to the whole system.

We begin our analysis by focusing on the case of larger ionic concentration  $\rho_0 \simeq 3 \text{ M}$ . The density profile of both  $\text{Cl}^-$  and  $\text{K}^+$  is expected to decay over a length scale comparable to the Debye length,  $\lambda_D = \sqrt{\frac{\epsilon}{2\beta(z e)^2 \rho_0}}$ , where  $e$  is the elementary charge,  $z$  is the valence of the ions ( $z = 1$ , in our case),  $\beta = (k_B T)^{-1}$  with  $k_B$  the Boltzmann constant and  $T$  the absolute temperature and  $\epsilon = 80 \cdot \epsilon_0$  is the dielectric constant with  $\epsilon_0$  the vacuum dielectric constant. For 3 M ionic solution we estimate a Debye length of  $\lambda_D \simeq 1.8 \text{ \AA}$  and therefore  $\lambda_D \ll h_{\min}$  being  $h_{\min} = h_0 - h_1 = 6 \text{ \AA}$  the half-section calculated at channel bottlenecks. In such a case, since there is only a small overlap between the Debye layers of the two facing walls, we do not expect the onset of any entropic electrokinetic effects.<sup>31</sup>



**Fig. 2** Net concentration of  $\text{Cl}^-$  and velocity profile (arrows) for external fields corresponding to potential drop  $\Delta V = 0.6$  V (left) and  $\Delta V = 2.4$  V (right). Panels (a and b) (first row) refer to ion concentration  $\rho_0 = 3 \text{ M}$ , panels (c and d) (central row) refer to  $\rho_0 = 1 \text{ M}$  and panels (e and f) (bottom row) refer to  $\rho_0 = 0.3 \text{ M}$ . The labels in the color bar refer to the concentration expressed in  $\text{mol L}^{-1}$ . For clarity sake, the arrows of the velocity profile are rescaled in each panel. The upper and bottom grey solid lines indicate the channel walls.



As expected, the accumulation of  $\text{Cl}^-$  ions at the positively charged solid wall induces an electro-osmotic flow, opposed to the direction of the external electrostatic field, that is almost symmetric with respect to the  $z$ -axis (see panels (a) and (b) of Fig. 2).

We have then increased the Debye length by reducing the ionic concentration  $\rho_0$ . For  $\rho_0 \sim 1$  M we have  $\lambda_D \simeq 3.1$  Å. Hence, the Debye layers of the facing walls overlap in the narrower sections ( $\lambda_D/h_{\min} \sim 1$ ,  $h_{\min} = 6$  Å) highlighting that the system is within the entropic electrokinetic regime.<sup>31</sup> Panel (d) of Fig. 2 shows that, for  $\Delta V = 2.4$  V, the ionic densities are quite affected by the flow. In particular,  $\text{Cl}^-$  concentration largely increases in the channel bottleneck, see e.g. the region  $x/L_x \in (0.45, 0.5)$  in Fig. 2d. This increase in  $\text{Cl}^-$  concentration is associated to  $\text{K}^+$  depletion, that will be discussed more in details in next paragraphs. This feature is associated to the onset of eddies in the electro-osmotic velocity profile, as shown in panels (c) and (d) of Fig. 2. These eddies form for sufficiently large driving forces. Indeed, while for  $\Delta V = 0.6$  V we do not observe major discrepancies with the previous case, for  $\Delta V = 2.4$  V two eddies form inside the channel. Interestingly, such eddies break down the left-right symmetry of the channel, for instance, Fig. 2d, shows that the eddies are shifted in the direction of the volumetric fluid flow, i.e. negative  $x$  in our reference frame. This occurrence is in contrast to the prediction obtained in linear regime<sup>31</sup> for which the eddies center is in the channel center,  $x/L_x = 0$ . Then we further increase the Debye length by setting  $\rho_0 \sim 0.3$  M, for which  $\lambda_D \simeq 5.6$  Å. In such a regime panels (e) and (f) of Fig. 2 show that the zone in which  $\text{K}^+$  are depleted is enhanced as compared to the previous cases. Moreover, comparing panels (e) and (f) to (c) and (d) in Fig. 2 we notice that, for  $\rho_0 \sim 0.3$  M, the onset of the eddies occurs for smaller values of the external force as compared to  $\rho_0 \sim 1$  M.

In order to quantitatively capture the accumulation of ions density, we have analyzed the dependence of the ionic densities averaged over the channel section as a function of the longitudinal position. Fig. 3 shows that the dependence of normalized densities profiles  $\bar{\rho}^\pm(x)$  defined as

$$\bar{\rho}_\pm(x) \equiv \frac{1}{2h(x)L_y} \int_0^{L_y} dy \int_{-h(x)}^{h(x)} \rho_\pm(x, y, z) dz \quad (2)$$

on the longitudinal position strongly depends on the value of the Debye length as compared to the channel section at the bottleneck. Indeed, when  $\lambda_D/h_{\min} \ll 1$ , i.e. for  $\rho_0 = 3$  M, panel (a) of Fig. 3 shows that the density profiles are almost constant along the channel for all the values of the external force we have tested. The only relevant difference occurs close to the narrowest sections  $x/L_x \simeq \pm 0.5$ . In contrast, when  $\lambda_D/h_{\min} \sim 1$ , i.e. for  $\rho_0 = 1$  M and  $\rho_0 = 0.3$  M panels (b) and (c) of Fig. 3 show the onset of a region where the cations ( $\text{K}^+$ ) are depleted and the left-right symmetry is broken. Once we have analyzed the density of  $\text{Cl}^-$  and  $\text{K}^+$  separately we move to the local total charge and local ionic densities defined as:

$$q(x) \equiv 2h(x)[\bar{\rho}_+(x) - \bar{\rho}_-(x)] \quad (3)$$

$$\bar{\rho}(x) \equiv \bar{\rho}_+(x) + \bar{\rho}_-(x) \quad (4)$$

We stress that we choose a different normalization for  $q(x)$  and  $\bar{\rho}(x)$  so that in a plane channel  $|q(x)|$  always match the total surface charge of channel walls  $2|\sigma|$  whereas  $\bar{\rho}(x)$  is the average density that, in the Debye-Hückel regime, determines the local value of the Debye length. Interestingly, Fig. 4a shows that in the limit of small Debye lengths,  $\lambda_D/h_{\min} < 1$ , local electroneutrality is recovered, i.e.  $q(x) \simeq 2\sigma$ , and the ionic density profile is almost constant along the channel. Only at very high voltages a small deviation is present at  $x/L_x \simeq 0.4$ .

In contrast, for larger values of the Debye length,  $\lambda_D/h_{\min} \simeq 1$ , neither  $q(x)$  nor  $\bar{\rho}(x)$  are constant. Such inhomogeneities trigger the onset of modulations in the magnitude of the local electrostatic potential. In particular, an accurate inspection of panels (b) and (c) of Fig. 4 reveals that weaker values of the external field triggers solely an inhomogeneity in the ionic density but do not affect the local electroneutrality. Interestingly, upon increasing the strength of external electric field local electroneutrality breaks down and on top of the well-known concentration polarization (CP),<sup>26,27,30,32,34</sup> a charge polarization (QP) appears. We remark that charge polarization sets for smaller values of the external force for smaller values of the Debye length. This can be due to finite liquid slippage at solid wall that cannot be disregarded in the regime under study. Indeed, slippage is commonly described in terms of the Navier boundary

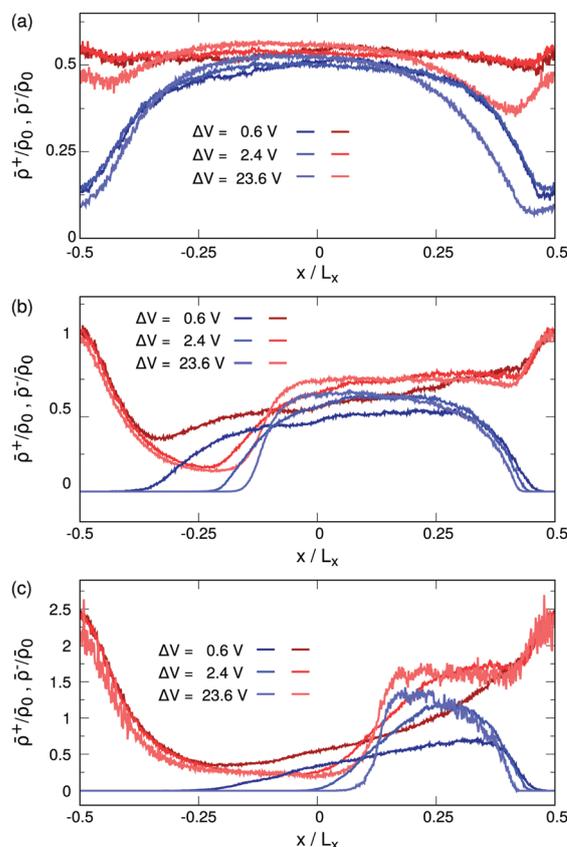


Fig. 3  $\bar{\rho}^+(x)$  (blue) and  $\bar{\rho}^-(x)$  (red) curves as a function of the longitudinal position for  $\rho = 3$  M (panel a),  $\rho = 1$  M (panel b) and  $\rho = 0.3$  M (panel c).  $\bar{\rho}^+(x)$  and  $\bar{\rho}^-(x)$  are calculated via eqn (2).



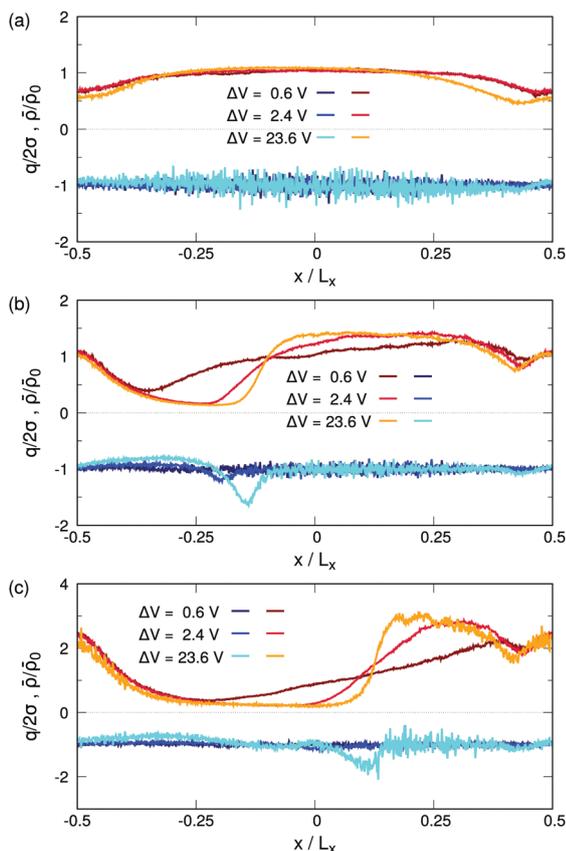


Fig. 4  $\bar{\rho}(x)$  (red curves) and  $q(x)$  (blue curves), defined respectively in eqn (3) and (4), as a function of the longitudinal position for  $\rho = 3$  M (panel a),  $\rho = 1$  M (panel b) and  $\rho = 0.3$  M (panel c). Lighter color stand for large values of the potential drop  $\Delta V$ , see legend.

condition that, for a plane channel, reads  $u_t|_{\text{wall}} = L_s \partial u_t / \partial n$  with  $u_t$  the component of the velocity field tangent to the wall,  $n$  the normal to the wall and  $L_s$  the slip length.<sup>35</sup> Atomistic simulation showed that for smooth hydrophilic and slightly hydrophobic (contact angle  $< 120^\circ$ ) surfaces  $L_s$ , hardly exceeds a nanometer.<sup>36–38</sup> In addition, the presence of a strong surface charge, further reduces the slip length for hydrophobic surfaces.<sup>39</sup> When comparing simulations performed with different ionic concentrations it should be taken into account that the slip length  $L_s$  in the three setups may be slightly different. Indeed, the relevant parameter ruling the effect of slippage on the electroosmotic flow is the ratio  $L_s / \lambda_D$ .<sup>40</sup> This feature is emphasized by Fig. S1 in ESI† that shows that the mismatch between the prediction of the analytical model (see ref. 31) and the numerical results increases upon decreasing  $\lambda_D$ .

In conclusion, we have reported on numerical simulations concerning a KCl solution embedded in a varying-section channel under the action of a constant electrostatic field. Our simulations show that, when the Debye length is comparable to the width of the channel bottlenecks, the system is in the entropic electrokinetic regime that is characterized by the onset of eddies.<sup>31</sup> In this perspective we observe, in agreement with what has been reported in the literature, the onset of a concentration polarization and local recirculation of the fluid

velocity that comes along with the onset of a standing shock in the ionic concentration. Surprisingly, for stronger external fields the local electroneutrality breaks down and an additional charge polarization (QP) sets in. Such a novel phenomena has been observed thanks to our microscopic approach based on Molecular Dynamics simulations in which the ionic densities are not constrained. In this perspective, our results show that for mild external fields local electroneutrality is recovered. This can justify *a posteriori* the assumption of local electroneutrality in these regimes. However, for larger external fields, local electroneutrality does not hold and a net electric dipole sets in inside the channel.

## Conflicts of interest

There are no conflicts to declare

## Acknowledgements

PM acknowledges Dr Mathijs Janssen for useful discussions. This research used the computational resource from CINECA (NATWE project), and the Swiss National Super-computing Centre (CSCS), project ID sm11. Open Access funding provided by the Max Planck Society.

## References

† We stress that according to eqn (4) we have that  $\frac{1}{L_x} \int_0^{L_x} \bar{\rho}(x) dx \neq \bar{\rho}_0$  where  $\bar{\rho}_0 = \frac{\int_0^L dx \int_0^{L_y} dy \int_{-h(x)}^{h(x)} \rho_+(x, y, z) + \rho_-(x, y, z) dz}{\int_0^L 2h(x) L_y dx}$  is the density averaged over the full volume.

- 1 B. Hille, *Ion channels of excitable membranes*, Sinauer, Sunderland, MA, 2001, vol. 507.
- 2 E. Weatherall and G. R. Willmott, *Analyst*, 2015, **140**, 3318.
- 3 H. Bayley, O. Braha and L.-Q. Gu, *Adv. Mater.*, 2000, **12**, 139.
- 4 G. Celaya, J. Perales-Calvo, A. Muga, F. Moro and D. Rodriguez-Larrea, *ACS Nano*, 2017, **11**, 5815–5825.
- 5 E. L. Bonome, R. Lepore, D. Raimondo, F. Cecconi, A. Tramontano and M. Chinappi, *J. Phys. Chem. B*, 2015, **119**, 5815.
- 6 A. Asandei, A. Ciuca, A. Apetrei, I. Schiopu, L. Mereuta, C. H. Seo, Y. Park and T. Luchian, *Sci. Rep.*, 2017, **7**, 6167.
- 7 M. Chinappi and F. Cecconi, *J. Phys.: Condens. Matter*, 2018, **30**, DOI: 10.1088/1361-648X/aababe.
- 8 A. Asandei, I. Schiopu, M. Chinappi, C. H. Seo, Y. Park and T. Luchian, *ACS Appl. Mater. Interfaces*, 2016, **8**, 13166.
- 9 M. Boukhet, F. Piguet, H. Ouldali, M. Pastoriza-Gallego, J. Pelta and A. Oukhaled, *Nanoscale*, 2016, **8**, 18352–18359.
- 10 G. Huang, K. Willems, M. Soskine, C. Wloka and G. Maglia, *Nat. Commun.*, 2017, **8**, 935.
- 11 P. Maggaretti, I. Pagonabarraga and J. M. Rubi, *Macromol. Symp.*, 2015, **357**, 178.
- 12 P. Maggaretti, I. Pagonabarraga and J. M. Rubi, *J. Chem. Phys.*, 2016, **144**, 034901.



- 13 A. Bolet, G. Linga and J. Mathiesen, *Phys. Rev. E*, 2018, **97**, 043114.
- 14 W. Guo, Y. Tian and L. Jiang, *Acc. Chem. Res.*, 2013, **46**, 2834.
- 15 S. Balme, T. Ma, E. Balanzat and J.-M. Janot, *J. Membr. Sci.*, 2017, **544**, 18.
- 16 J. Experton, X. Wu and C. R. Martin, *Nanomaterials*, 2017, **7**, 445.
- 17 C. B. Picallo, S. Gravelle, L. Joly, E. Charlaix and L. Bocquet, *Phys. Rev. Lett.*, 2013, **111**, 244501.
- 18 N. Laohakunakorn and U. F. Keyser, *Nanotechnology*, 2015, **26**, 275202.
- 19 P. Bacchin, *Membranes*, 2018, **8**, 10.
- 20 E. Kalman, I. Vlassiuk and Z. Siwy, *Adv. Mater.*, 2008, **20**, 293.
- 21 G. Chen and S. Das, *J. Phys. Chem. B*, 2017, **121**, 3130.
- 22 S. R. Maduar, A. V. Belyaev, V. Lobaskin and O. I. Vinogradova, *Phys. Rev. Lett.*, 2015, **114**, 118301.
- 23 I. Rubinstein and B. Zaltzman, *Phys. Rev. E: Stat. Phys., Plasmas, Fluids, Relat. Interdiscip. Top.*, 2000, **62**, 2238.
- 24 S. Y. Park, C. J. Russo, D. Branton and H. A. Stone, *J. Colloid Interface Sci.*, 2006, **297**, 832.
- 25 A. Mani, T. A. Zangle and J. G. Santiago, *Langmuir*, 2009, **25**, 3898.
- 26 A. Mani and M. Bazant, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2011, **84**, 061504.
- 27 Y. Green, S. Shloush and G. Yossifon, *Phys. Rev. E: Stat., Nonlinear, Soft Matter Phys.*, 2014, **89**, 043015.
- 28 T. A. Zangle, A. Mani and J. G. Santiago, *Langmuir*, 2009, **25**, 3909.
- 29 H.-C. Chang, G. Yossifon and E. A. Demekhin, *Annu. Rev. Fluid Mech.*, 2012, **44**, 401.
- 30 V. V. Nikonenko, A. V. Kovalenko, M. K. Urtenov, N. D. Pismenskaya, J. Han, P. Sizat and G. Pourcelly, *Desalination*, 2014, **342**, 85.
- 31 P. Magaretti, I. Pagonabarraga and J. M. Rubi, *Phys. Rev. Lett.*, 2014, **113**, 128301.
- 32 H. Leese and D. Mattia, *Microfluid. Nanofluid.*, 2014, **16**, 711.
- 33 L. Jubin, A. Poggioli, A. Siria and L. Bocquet, *Proc. Natl. Acad. Sci. U. S. A.*, 2018, **115**, 4063.
- 34 M. Andersen, K. Wang, J. Schiffbauer and A. Mani, *Electrophoresis*, 2017, **38**, 702.
- 35 E. Lauga, M. Brenner and H. Stone, *Springer handbook of experimental fluid mechanics*, Springer, 2007, pp. 1219–1240.
- 36 M. Chinappi and C. Casciola, *Phys. Fluids*, 2010, **22**, 042003.
- 37 D. M. Huang, C. Sendner, D. Horinek, R. R. Netz and L. Bocquet, *Phys. Rev. Lett.*, 2008, **101**, 226101.
- 38 M. Sega, M. Sbragaglia, L. Biferale and S. Succi, *Soft Matter*, 2013, **9**, 8526–8531.
- 39 D. M. Huang, C. Cottin-Bizonne, C. Ybert and L. Bocquet, *Langmuir*, 2008, **24**, 1442–1450.
- 40 L. Bocquet and E. Charlaix, *Chem. Soc. Rev.*, 2010, **39**, 1073–1095.

