High-capacity and selective ammonium removal from water using sodium cobalt hexacyanoferrate†

Yong Jiang, a Kimitaka Minami, Koji Sakurai, Akira Takahashi, Durga Parajuli, Zhongfang Lei, Zhenya Zhang and Tohru Kawamoto

A new NH$_4^+$ adsorbent with high capacity and selectivity, sodium cobalt(II) hexacyanoferrate(II) (NaCoHCF, Na$_2$Co(s)[Fe$_3^{2+}$(CN)$_6$]$_2$H$_2$O), was prepared. The adsorption performance was investigated by varying the mixing ratio of [Fe(CN)$_6$]$^{4-}$ to Co$^{2+}$ during synthesis, $R_{\text{mix}}$. The ammonia capacity was found to be proportional to $R_{\text{mix}}$, indicating that the NH$_4^+$ capacity can be increased by increasing the Na$^+$-ion content in NaCoHCF. To conduct a detailed study, we prepared homogeneous nanoparticles by flow synthesis using a micromixer with $R_{\text{mix}} = 1.00$. Even on the addition of a saline solution (NaCl) with an Na$^+$-ion concentration of 9350 mg L$^{-1}$, the capacity was maintained: $q_{\text{max}} = 4.28$ mol kg$^{-1}$. Using Markham–Benton analysis, the selectivity factor, defined by the ratio of equilibrium constants for NH$_4^+$ to that for Na$^+$, was calculated to be $\alpha = 96.2$, and 4.36 mol kg$^{-1}$ was found to be the maximum capacity. The high selectivity of NaCoHCF results in good NH$_4^+$-adsorption performance, even from seawater. In comparison with other adsorbents under the same conditions and even for a NH$_4$Cl solution, NaCoHCF showed the highest capacity. Moreover, the coexisting Na$^+$ caused no interference with the adsorption of ammonium by NaCoHCF, whereas the other adsorbents adsorbed ammonia only slightly from the saline solution. We also found that the pores for NH$_4^+$ adsorption changed their sizes and shapes after adsorption.

1. Introduction

Ammonium, NH$_4^+$, is a widely synthesized chemical, most of which is used as a fertilizer. This distributed ammonium is oxidized to nitrite, NO$_2^-$, and then further converted to nitrate, NO$_3^-$, in rivers, lakes, and oceans through nitrification processes. When humans and animals drink water containing ammonia (NO$_3^-$ $\geq$ 45 mg L$^{-1}$ or NO$_3^-$-N $\geq$ 10 mg L$^{-1}$), they can become ill or even die. In aquatic systems, especially those near densely populated settlements or large-scale livestock facilities, the high concentrations of ammonia in water cause concern. Excess ammonia in aquatic systems can cause eutrophication, harmful algal blooms, and anoxic conditions in estuaries, rivers, and even the coastal environment. Consequently, biodiversity, fisheries, and overall ecosystem health are adversely affected by this N nutrient imbalance. Furthermore, N$_2$O, a byproduct of ammonium oxidation, is an important greenhouse gas and ozone-depleting agent. The Intergovernmental Panel on Climate Change (IPCC) has estimated that the N$_2$O emissions from the open ocean represent 3.8 Tg N per year, 35% of the total natural emissions.

In fact, various nations have set standards for ammonia in effluent or environmental water. For example, the U.S. Environmental Protection Agency (EPA) lowered the limit in 2013 for aquatic life in ambient water bodies to 17 and 1.9 mg L$^{-1}$ total ammonia nitrogen one-hour and 30 day averages, respectively. China and India have also established standards for effluents of 15–50 and 50 mg L$^{-1}$ ammonium nitrogen. Reducing the ammonium concentration is also important for biogasification technology with anaerobic digestion because the digestion is inhibited by high concentrations of ammonium. Depending on the conditions, 1500–5000 mg L$^{-1}$ of total ammonium nitrogen can cause the slow down or failure of digestion. For the removal of NH$_4^+$ from wastewater or digestion liquids, methods for the selective removal of NH$_4^+$ are necessary because various ions coexist in these solutions.

For the uptake of NH$_4^+$, removal with an adsorbent is an easily controllable and highly efficient method. Strong acid cation (SAC) exchange resins, analogs of Amberlite IR-120 (Alfa Aesar, UK), show the highest adsorption capacity, reaching 5.34 mol kg$^{-1}$ for aqueous solution without coexisting cations and using glass-packed bed columns. Nevertheless, SAC resins have low selectivity to NH$_4^+$ when other competing ions are present. He et al. studied alkaline-activated and lanthanum-impregnated zeolites and found a maximum adsorption...
capacity, $q_{\text{max}}$ of 1.54 mol kg$^{-1}$ in a pure water solution. However, the removal efficiency, $P_{\text{r}}$, decreased from 90% to 36% in the presence of Na$^+$. Soetardji et al. reported that sodium-hydroxide-modified zeolite mordenite has $q_{\text{max}} = 3.0$ mol kg$^{-1}$ in aqueous solution and that $P_{\text{r}}$ decreased from 81% to 66.9% when competing with other ions. Guaya et al. studied a hydrated aluminum-oxide-modified zeolite, which showed $q_{\text{max}} = 2.14$ mol kg$^{-1}$ in aqueous solution and $P_{\text{r}} = 12\%$ with coexisting Na$^+$ ions.

Thus, conventional adsorbents have lower selectivity. As mentioned above, for the removal of NH$_4^+$ from wastewater or the digestion liquids, adsorbents with high-selectivity are crucial. In particular, for digestion liquids, a large capacity is also essential because the NH$_4^+$ concentration is quite high. For these reasons, the development of new adsorbents with both large capacity and high selectivity is desirable.

In our earlier study, we found that potassium copper hexacyanoferrate, KCuHCF, has a high ammonium adsorption capacity of 1.94 mol kg$^{-1}$, as well as high selectivity for dissolved ammonia. Potassium copper hexacyanoferrate (KCuHCF), a metal hexacyanoferrate (MHCF), is a Prussian blue analog. MHCFs have the chemical composition of $A_yM_{x-y}[Fe(CN)_6]_x\cdot yH_2O$, where A and M, respectively, denote alkali and transition metals, and x indicates the concentration of $[Fe(CN)_6]^{3-}$ vacancies. With respect to MHCFs, many researchers have studied their use in catalysis, electrodes in secondary batteries, electrochromism, sensors, gas storage, and adsorbents for radioactive Cs$^+$ ions. The ionic radii of hydrated Cs and NH$_4^+$ are similar (3.29 and 3.31 Å, respectively). Therefore, assuming a size-based adsorption model, MHCFs could also have substantial adsorption capability for NH$_4^+$. This has implications as a potential for recyclability.

The NH$_4^+$-adsorption mechanism is affected by the porous network in MHCFs. The crystal structure of MHCF is shown in Fig. 1, where two kinds of adsorption sites exist: one is an interstitial site, a cubic confined space surrounded by eight metal sites and twelve cyano-groups. Its pore size is less than 0.5 nm. The other is a vacancy site, represented as $M_{x-y}[Fe(CN)_6]_x\cdot yH_2O$, where M denotes alkali metal sites and twelve cyano-groups. Its pore size is less than 0.5 nm. The other is a vacancy site, represented as $[Fe(CN)_6]^{1-}$ with fewer $[Fe(CN)_6]^{3-}$ dihexacyanoferrate, KCuHCF, has a high ammonium adsorption capacity and high selectivity is desirable.

However, with substitution with Co, the introduction of a small number of $[Fe(CN)_6]^{1-}$ vacancies becomes possible. Additionally, the affinity of MHCF for the mono-cation is known to depend on the hydrated radius, implying that utilization of Na$^+$ instead of K$^+$ can increase the NH$_4^+$ adsorption performance. Our study has two parts. The first is a composition-dependent study. Five kinds of NaCoHCF-nanoparticles (NaCoHCF-NPs), Na$_x$Co$_{1-x}$Fe$_6$[CN$_6$]$_x$•yH$_2$O, were synthesized by changing the molar concentration ratio of the reagent solution ($R_{\text{mix}}$) using a batch method. The second part is a detailed study of $R_{\text{mix}} = 1.00$. Quantitative analysis into the adsorption capacity and selectivity was conducted. The changes to the crystal structure are also discussed. By comparison with earlier studies, we found that our NaCoHCF exhibits a very high capacity when using the batch-adsorption method. Particularly for NH$_4^+$ adsorption from saline solutions, the benefits of NaCoHCF are enhanced by its high selectivity. We also demonstrate its potential for recyclability.

2. Experimental section
2.1 Synthesis of NaCoHCF-NPs
First, NaCoHCF-NPs with compositions of Na$_{4x-3}$Co$_{1-x}$Fe$_6$[CN$_6$]$_x$ (water omitted) were prepared according to the following chemical reaction.

![Scheme 1](https://example.com/scheme1.png)

**Scheme 1** Schematic view of the synthesis of NaCoHCF by micromixer.
To study the composition dependence, the NaCoHCF-NPs were synthesized using a batch method by mixing two aqueous solutions of Na\textsubscript{x}[Fe(CN)\textsubscript{6}]\textsubscript{3−x}\textsubscript{2}Co[Fe(CN)\textsubscript{6}]\textsubscript{x} + 2NaNO\textsubscript{3}.

2.3 NH\textsuperscript{4}\textsuperscript{+} adsorption tests
To evaluate the composition dependence, a batch-shaking method was used to evaluate the NH\textsuperscript{4}\textsuperscript{+} adsorption capacity of the NaCoHCF-NPs, as shown schematically in Fig. S1(a).† The method was conducted as follows: 40 mg of an NaCoHCF sample (Batch-0.50, 0.75, 1.00, 1.50, or 2.00) was added to a 40 mL aqueous solution of NH\textsubscript{4}Cl with a NH\textsuperscript{4}\textsuperscript{+} concentration of 90 mg L\textsuperscript{−1}. The suspension was shaken using a multi shaker (SI-300C; AS One Corp.) at 600 rpm for 180 min at 30 °C. After shaking, the supernatant was obtained via centrifuging and further separation using a 0.45 μm filter (MCE syringe filter; Membrane Solutions). The NH\textsuperscript{4}\textsuperscript{+} concentration in the supernatant was evaluated using ion chromatography (IC, 883 Basic IC plus; Metrohm AG).

2.4 Evaluation of recyclability
The potential for recyclability was also investigated. The experimental setup is shown in Fig. S1(b).† A membrane filter with NaCoHCF-NPs was prepared for the flow test. The Flow-1.00 powder was mixed with 2 mL Milli-Q (3.76 mg mL\textsuperscript{−1}) using an ultrasonic cleaner (W-113MK-II; Honda). Then, 100 μL solutions were dropped on the membrane filter (Φ 25 mm, 0.45 μm pore size, JHWP01300; Merck), followed by drying at 60 °C for 2 min. Thus prepared, the solutions were set on a circular plastic plate of Φ 25 mm with a hole of Φ 5 mm in the middle. They were pased on the film for effective adsorption-desorption. An FT-IR spectrometer (iD1 transmission iS5; Nicolet Biomedical Inc.) was used to confirm adsorption and desorption of NH\textsuperscript{4}\textsuperscript{+}. For the adsorption test, the NH\textsuperscript{4}\textsuperscript{+} solution of 500 mg L\textsuperscript{−1} was flowed through the NaCoHCF-NP-dipped membrane for 30 min at the rate of 0.2 mL min\textsuperscript{−1}. For the
desorption test, a NaCl solution of 5 mol L$^{-1}$ was similarly flowed for 2 h at a rate of 1 mL min$^{-1}$.

3. Results and discussion

3.1 Composition dependence

The dependence of the chemical composition on the mixing ratio, $R_{\text{mix}}$, is presented in Table 1. For $R_{\text{mix}} < 1.00$, $x$ is an almost equal to $R_{\text{mix}}$. The value of $y$, the number of Na$^+$ ions in NaCoHCF, also increased. In contrast, when $R_{\text{mix}} > 1.00$, the chemical composition was almost unchanged, demonstrating that the composition can be controlled by changing the reaction $R_{\text{mix}}$ to $x < 1$.

The crystal structure of NaCoHCF depends on the chemical composition (see Fig. S2†). When $R_{\text{mix}} \geq 1.00$, the crystal structure is rhombohedral ($R$3), as reported. On the other hand, the structure for $R_{\text{mix}} = 0.50$ is unclear. Earlier reports described the space group as monoclinic ($P2_1/m$ or $P2_2_1/m$) or cubic ($Pm3m$). In our case, the XRD pattern is explained as a mixture of $R$3c and $P2_1/m$ structures, as shown in Table 1. The NaCoHCF with $R_{\text{mix}} = 0.67$ is also explainable as a mixture. Such a mixture could be the result of the batch synthesis because homogeneous synthesis is difficult using the batch method, resulting in the fluctuation of the chemical composition.

The BET surface areas of Batch-0.50, −0.67, and 1.00 were evaluated to be 28, 76, and 46 m$^2$ g$^{-1}$, respectively. The N$_2$ isotherms are shown in Fig. S3 in the ESI.† These values are much smaller than those of other Prussian blue analogs synthesized for gas adsorption. For example, that of Co$_{1.00}$Fe$_{0.60}$CN$_{0.38}$ was 848 m$^2$ g$^{-1}$. The smaller surface area originated from the inclusion of Na$^+$ cations. Because the interstitial sites of NaCoHCF are fully or partially occupied by Na$^+$, it would be impossible for N$_2$ to penetrate into the NaCoHCF lattice. This presumption is also supported by the fact that the averaged pore diameter is comparable to the particle size, as shown later in the analysis of Flow-1.00.

Fig. 2(a) shows that the NH$_4^+$ adsorption capacity improved with increasing $R_{\text{mix}}$. The amount of adsorbed ammonia of Batch-2.00 is about twice that of Batch-0.5. Fig. 2(b) shows that the amount of Na$^+$ from the adsorbent has an almost linear correlation with the NH$_4^+$ adsorption amount, indicating the NH$_4^+$ adsorption occurred through ion exchange with Na$^+$. These results demonstrate that the increase in the Na$^+$ composition in NaCoHCF enhances the NH$_4^+$ adsorption capacity, and that NaCoHCF retains its structure even after long-term shaking in water. However, for $R_{\text{mix}} > 1.00$, the adsorption capacity increased by only 2.9–3.9% from $R_{\text{mix}} = 1.00$ because the upper limit of $x$ is 1.0.

3.2 Detailed study with flow-synthesized NaCoHCF with $R_{\text{mix}} = 1.00$

Based on results of the composition dependence of the NH$_4^+$ capacity, we chose to conduct a detailed study of NaCoHCF-NPs with $R_{\text{mix}} = 1.00$ because we obtained the desired chemical

---

Table 1: The mixing ratio, $R_{\text{mix}}$, in synthesis and the chemical compositions and crystal structure of the NaCoHCF-NP samples

<table>
<thead>
<tr>
<th>Samples</th>
<th>$R_{\text{mix}}$</th>
<th>$x$</th>
<th>$y$</th>
<th>$z$</th>
<th>Chemical compositions</th>
<th>Space group</th>
<th>$a$ (Å)</th>
<th>$b$ (Å)</th>
<th>$c$ (Å)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Batch-0.50</td>
<td>0.50</td>
<td>0.57</td>
<td>0.49</td>
<td>3.64</td>
<td>Na$<em>{0.49}$Co$</em>{1.00}$[Fe(CN)$_{0.57}$]H$_2$O</td>
<td>$P2_1/m$</td>
<td>11.83</td>
<td>9.52</td>
<td>7.47</td>
</tr>
<tr>
<td>Batch-0.67</td>
<td>0.67</td>
<td>0.63</td>
<td>0.74</td>
<td>3.41</td>
<td>Na$<em>{0.74}$Co$</em>{1.00}$[Fe(CN)$_{0.63}$]H$_2$O</td>
<td>$P2_1/m$</td>
<td>11.66</td>
<td>9.27</td>
<td>7.28</td>
</tr>
<tr>
<td>Batch-1.00</td>
<td>1.00</td>
<td>0.87</td>
<td>1.65</td>
<td>2.84</td>
<td>Na$<em>{1.65}$Co$</em>{1.00}$[Fe(CN)$_{0.87}$]H$_2$O</td>
<td>$R$3c</td>
<td>12.77</td>
<td>12.77</td>
<td>29.06</td>
</tr>
<tr>
<td>Batch-1.33</td>
<td>1.33</td>
<td>0.90</td>
<td>3.00</td>
<td>2.84</td>
<td>Na$<em>{1.71}$Co$</em>{1.00}$[Fe(CN)$_{0.90}$]H$_2$O</td>
<td>$R$3c</td>
<td>7.43</td>
<td>7.43</td>
<td>17.46</td>
</tr>
<tr>
<td>Batch-2.00</td>
<td>2.00</td>
<td>0.90</td>
<td>3.36</td>
<td>3.00</td>
<td>Na$<em>{2.25}$Co$</em>{1.00}$[Fe(CN)$_{0.90}$]H$_2$O</td>
<td>$R$3c</td>
<td>7.45</td>
<td>7.45</td>
<td>17.45</td>
</tr>
<tr>
<td>Flow-1.00</td>
<td>1.00</td>
<td>0.82</td>
<td>1.46</td>
<td>3.79</td>
<td>Na$<em>{1.46}$Co$</em>{1.00}$[Fe(CN)$_{0.82}$]H$_2$O</td>
<td>$Fm3m$</td>
<td>10.16</td>
<td>10.16</td>
<td>10.16</td>
</tr>
</tbody>
</table>

Fig. 2 (a) Amount of adsorbed NH$_4^+$ by the batch-synthesized NaCoHCF with different compositions. (b) The relationship between adsorbed NH$_4^+$ and released Na$^+$. The adsorption experiment was conducted at initial NH$_4^+$ of 90 mg L$^{-1}$, 30 °C, and at 600 rpm for 3 h.
composition by using this value of $R_{\text{mix}}$ and because it showed sufficiently high capacity. For our detailed study, we used the flow-synthesized sample, Flow-1.00, to avoid the fluctuation of the chemical composition and particle size. Table 1 shows that the chemical composition of Flow-1.00 is almost identical to that of Batch-1.00. The adsorption kinetics was studied at an initial $\text{NH}_4^+$ concentration of 500 mg L$^{-1}$, 30 °C, and at 600 rpm for 8 h (see Fig. S4†). The results showed that the $\text{NH}_4^+$ adsorption was almost completed in 30 min. Such fast adsorption is similar to the case of KCuHCF.15

Using BET analysis, we estimated the surface area to be 53 m$^2$ g$^{-1}$, which is also comparable to that of Batch-1.00, 46 m$^2$ g$^{-1}$. As described before, this value is not very high because the interstitial sites of NaCoHCF are filled with Na$^+$, preventing the penetration of N$_2$ into the porous network in the crystal. The average pore size was estimated to 31 nm for Flow-1.00, consistent with the size of the crystallites, as shown later.

After $\text{NH}_4^+$ adsorption, the crystal structure was maintained, except for a slight trigonal distortion. Fig. 3 shows the XRD patterns obtained before and after $\text{NH}_4^+$ adsorption. Some splitting of the Bragg peaks is apparent. The slight structural transformation observed is the same as that in the case of ion exchange between Na$^+$ and K$^+$.45 Before adsorption, NaCoHCF had a rhombohedral ($R3c$) structure. However, after $\text{NH}_4^+$ adsorption, it changed to a cubic lattice ($Pm3m; Z = 4$). Thus, the ion exchange reversibly changed the structure.

The structural change also influenced the shape and size of the interstitial sites in which Na$^+$ or $\text{NH}_4^+$ are located. The lattice parameters of the crystal are shown in Table 1. A schematic view of the relationship between the interstitial site and the lattice distortion is shown in Fig. 4. Note that the crystal symmetry is different before and after the $\text{NH}_4^+$ adsorption. Before adsorption, the lattice has the rhombohedral symmetry with slight distortion from the cubic lattice. That is, it was compressed along the (1,1,1) direction. In contrast, after adsorption, the crystal maintained the cubic structure. This difference is consistent with previous reports of the ion exchange between Na$^+$ and K$^+$ but not $\text{NH}_4^+$.45

Because the symmetry of the crystal is different before and after $\text{NH}_4^+$ adsorption, we investigated the distance between the nearest Co neighbors and the volume of the (pseudo)-cubic cage of the interstitial site to evaluate the changes to the interstitial sites. Before $\text{NH}_4^+$ adsorption, the distance between the nearest Co neighbors was calculated as the length of the unit vector of the rhombohedral primitive cell, 7.24 Å. On the other hand, after $\text{NH}_4^+$ adsorption, the separation was reduced to 7.18 Å, resulting in reduction in the volume of the cage from 138 to 131 Å$^3$. It is interesting that the cage became smaller although the ionic radius of $\text{NH}_4^+$ is larger than that of Na$^+$. This could be due to the difference in the H$_2$O accompanying the cations. Because the interaction with H$_2$O is stronger with Na$^+$ than that with $\text{NH}_4^+$. Therefore, before $\text{NH}_4^+$ adsorption, H$_2$O is adsorbed along with Na$^+$, even if cage expansion is energetically disadvantageous. This is consistent with the previous studies of the electrochemical injection of Na$^+$ into copper hexacyanoferrate thin films.46

No nanoparticle degradation occurred during adsorption. The crystallite sizes estimated by Scherrer analysis of the XRD patterns (Fig. 3) before and after sorption were, respectively, 37.9 and 51.7 nm. This result is consistent with the SEM images in Fig. 5. The particle sizes estimated using SEM images were 33 ± 10 and 47 ± 13 nm. The data indicate no degradation, but there is a possibility of some particle growth. The reason for the growth remains unclear, but it could be due to the immobilization of the Co$^{2+}$ and [Fe(CN)$_6$]$^{3-}$ ions eluted from the adsorbent onto the other part of the adsorbent. If so, the adsorbent would retain the eluted species. The surface morphology in SEM images shows no marked change after adsorption. Furthermore, we also evaluated the release of CN$^-$ after adsorption. The concentration of CN$^-$ in solution was only 0.33 mg L$^{-1}$, sufficiently smaller than effluent standard in Japan, 1 mg L$^{-1}$.20

Fig. 6 shows the $\text{NH}_4^+$ adsorption isotherms in aqueous NH$_4$Cl solution and that in aqueous saline solution. In the saline solution, the concentration of the Na$^+$ solution was set to 9350 mg L$^{-1}$, the same as that of artificial seawater. The curves fit to the Langmuir, Freundlich, and Markham–Benton...
Table 2 The fitting parameters with the Langmuir, Freundlich, and the Markham–Benton equations for the NH$_4^+$ adsorption using the flow-synthesized NaCoHCF with $R_{\text{mix}} = 1.00$

<table>
<thead>
<tr>
<th></th>
<th>NH$_4$Cl(aq)</th>
<th>Saline</th>
<th>NH$_4$Cl(aq)</th>
<th>Saline</th>
<th>NH$_4$Cl(aq) &amp; saline</th>
</tr>
</thead>
<tbody>
<tr>
<td>$K$ (L mol$^{-1}$)</td>
<td>$q_{\text{max}}$ (mol kg$^{-1}$)</td>
<td>$K$ (L mol$^{-1}$)</td>
<td>$q_{\text{max}}$ (mol kg$^{-1}$)</td>
<td>$K_f$ (mol kg$^{-1}$)</td>
<td>$q_{\text{max}}$ (mol kg$^{-1}$)</td>
</tr>
<tr>
<td>13.99</td>
<td>3.97</td>
<td>0.28</td>
<td>4.28</td>
<td>22.27</td>
<td>0.77</td>
</tr>
</tbody>
</table>

where $C_e$, $q_e$, $q_{\text{max}}$, and $K$ respectively represent the NH$_4^+$ concentration in solution at equilibrium, loaded NH$_4^+$ in the adsorbent, maximum adsorption capacity, and the equilibrium constant. The same data are also shown with other axes in Fig. S5,$^\dagger$ and the adsorption behavior fits the Langmuir equation well. We also carried out fitting to the Freundlich equation,

$$q_e = K_c C_e^{1/n}.$$  

For the Freundlich equation, only the region where the loaded NH$_4^+$ concentration was less than 1.95 mol kg$^{-1}$, about a half the maximum capacity, was considered because the Freundlich equation is only suitable far from saturated loading. However, in this region, the Freundlich equation also well reproduced the experimental data.

In the fitting of the Langmuir or Freundlich equations, we used different parameters for NH$_4$Cl(aq) and the salt solutions because the effect of the coexistent Na$^+$ ions can only be modeled by changing the fitting parameters. For a more quantitative evaluation of the effect of the coexistent Na$^+$ ions, we also considered the Markham–Benton model for a solution with multi-alkali cations. As a type of extended Langmuir equation, the Markham–Benton equation$^{31}$ was used to examine adsorption isotherms for multiple components to estimate the ease of desorption of the adsorbents. The results also provide some understanding of the selectivity of the sorbents for some ions. The Markham–Benton equation is

$$q_e = \frac{q_{\text{max}} K C_e}{1 + K C_e + K' C_e},$$  

where $C_e$, $q_e$, and $K$ respectively represent the NH$_4^+$ ion concentration in equilibrium, the adsorption capacity, and the equilibrium constant. $C'_e$ and $K'$ respectively denote the Na$^+$ ion concentration in equilibrium and the equilibrium constant. Considering the Na$^+$-ion exchange for NH$_4^+$ ions, i.e., even in NH$_4$Cl aqueous solution, an equal amount of Na$^+$ ions would be exchanged out, adversely affecting the adsorption capacity. When we consider both sources of Na$^+$ ions (those in NaCoHCF and that in the solution), the equation can be expressed by as

$$q_e = \frac{-\left(1 + K C_e + K' C'_e\right) + \sqrt{\left(1 + K C_e + K' C'_e\right)^2 + 4 K_m (\frac{q_{\text{max}}}{1/n})^2 K C_e}}{2 K_m (\frac{1}{1/n})},$$  

where $C_e$, $q_e$, and $K$ respectively represent the NH$_4^+$ concentration in solution at equilibrium, loaded NH$_4^+$ in the adsorbent, maximum adsorption capacity, and the equilibrium constant. The same data are also shown with other axes in Fig. S5,$^\dagger$ and the adsorption behavior fits the Langmuir equation well. We also carried out fitting to the Freundlich equation,

$$q_e = K_c C_e^{1/n}.$$  

For the Freundlich equation, only the region where the loaded NH$_4^+$ concentration was less than 1.95 mol kg$^{-1}$, about a half the maximum capacity, was considered because the Freundlich equation is only suitable far from saturated loading. However, in this region, the Freundlich equation also well reproduced the experimental data.

In the fitting of the Langmuir or Freundlich equations, we used different parameters for NH$_4$Cl(aq) and the salt solutions because the effect of the coexistent Na$^+$ ions can only be modeled by changing the fitting parameters. For a more quantitative evaluation of the effect of the coexistent Na$^+$ ions, we also considered the Markham–Benton model for a solution with multi-alkali cations. As a type of extended Langmuir equation, the Markham–Benton equation$^{31}$ was used to examine adsorption isotherms for multiple components to estimate the ease of desorption of the adsorbents. The results also provide some understanding of the selectivity of the sorbents for some ions. The Markham–Benton equation is

$$q_e = \frac{q_{\text{max}} K C_e}{1 + K C_e + K' C_e},$$  

where $C_e$, $q_e$, and $K$ respectively represent the NH$_4^+$ ion concentration in equilibrium, the adsorption capacity, and the equilibrium constant. $C'_e$ and $K'$ respectively denote the Na$^+$ ion concentration in equilibrium and the equilibrium constant. Considering the Na$^+$-ion exchange for NH$_4^+$ ions, i.e., even in NH$_4$Cl aqueous solution, an equal amount of Na$^+$ ions would be exchanged out, adversely affecting the adsorption capacity. When we consider both sources of Na$^+$ ions (those in NaCoHCF and that in the solution), the equation can be expressed by as

$$q_e = \frac{-\left(1 + K C_e + K' C'_e\right) + \sqrt{\left(1 + K C_e + K' C'_e\right)^2 + 4 K_m (\frac{q_{\text{max}}}{1/n})^2 K C_e}}{2 K_m (\frac{1}{1/n})},$$  

where $C_e$, $q_e$, and $K$ respectively represent the NH$_4^+$ concentration in solution at equilibrium, loaded NH$_4^+$ in the adsorbent, maximum adsorption capacity, and the equilibrium constant. The same data are also shown with other axes in Fig. S5,$^\dagger$ and the adsorption behavior fits the Langmuir equation well. We also carried out fitting to the Freundlich equation,

$$q_e = K_c C_e^{1/n}.$$  

For the Freundlich equation, only the region where the loaded NH$_4^+$ concentration was less than 1.95 mol kg$^{-1}$, about a half the maximum capacity, was considered because the Freundlich equation is only suitable far from saturated loading. However, in this region, the Freundlich equation also well reproduced the experimental data.
where \( C_0 \), \( m \), and \( V \) respectively denote the initial Na\(^+\) ion concentration in solutions, adsorbent mass, and solution volume.

The fitting parameters, \( q_{\text{max}} \), \( K \), and \( K' \), are shown in Table 2. Fig. 6 shows that the experimental data were well fitted using the Markham–Benton model. Again, with the Markham–Benton model, we use the same parameter set for NH\(_4\)Cl(aq) and the saline solutions. A selectivity factor, \( \alpha \), defined by the ratio of equilibrium constants for NH\(_4\)\(^+\) to that for Na\(^+\) was calculated to be \( \alpha = 96.2 \), indicating the high selectivity of NH\(_4\)\(^+\) against Na\(^+\).

Such high selectivity is expected to lead to extremely high capacity, even in an aqueous saline solution. To clarify the high capacity of NaCoHCF among the various adsorbents, we used two approaches. First, we surveyed and compared results with those of earlier studies, and we also conducted experimental investigations to assess the adsorption capacity of adsorbents in identical conditions. For the literature survey, we picked reports of adsorption tests carried out using a batch style because column-style tests generally report higher capacities, rendering a comparison of results difficult between batch-style tests and column tests.

Information from earlier studies is presented in Table 3 for the adsorption capacity of adsorbents for NH\(_4\)\(^+\) from aqueous solution in batch style, indicating that the NaCoHCF (Flow-1.00) capacity exceeds that of all earlier reports. However, as described above, SAC resins have been reported to have high capacities, although these values were achieved using the column method without coexistent cations. For comparison under the same conditions, we evaluated the respective adsorption capacities of a synthetic zeolite, Amberlite IR-120(H) as a representative SAC, sepiolite, and NaCoHCF (Flow-1.00). Even in the NH\(_4\)Cl aqueous solution (500 mg L\(^{-1}\)) solutions immediately, resulting in the suppression of the possibility of the reverse reaction (A\(^-\) adsorption–NH\(_4\)\(^+\) desorption).

The benefits of NaCoHCF were amplified in the case of aqueous saline solution with 9350 mg L\(^{-1}\)-Na and 500 mg L\(^{-1}\)-NH\(_4\). Fig. 7 shows that NaCoHCF has an adsorption capacity that is almost identical to that of the case without Na\(^+\), whereas the other adsorbents showed little adsorption.

Although our main aim, the preparation of an NH\(_4\)-adsorbent with high capacity and high selectivity, has been achieved, the recyclability of the adsorbent is also important for practical use. Therefore, finally, we demonstrate the potential for recyclability by attempting desorption tests. Fig. 8 shows that the adsorption–desorption–adsorption process was confirmed by measuring the infrared absorption corresponding to NH\(_4\)\(^+\) vibration mode at around 1415 cm\(^{-1}\). Using the continuous flow of NaCl solution for desorption, the peak height was found to decrease to 28% the original value before flow, indicating the potential for NaCoHCF recyclability. Next, further study on the adsorption performances, including the column sorption, quantitatively reusability test would be conducted.

Finally, we mention concerning the cost of the materials. As mentioned above, NaCoHCF is synthesized only mixing two solutions immediately, resulting in the suppression of the manufacturing cost. For NH\(_4\) removal from salt water, NaCoHCF would be cost effective in comparison with Amberlites and zeolites, despite the utilization of the cobalt, one of the rare metals. This is because the amount of the adsorbent can be drastically decreased with its high selectivity.

![Fig. 7 Adsorption capacity of various adsorbents in NH\(_4\)Cl aqueous solution (500 mg L\(^{-1}\)) and saline solution with a concentration fixed at 9350 mg L\(^{-1}\)-Na.](image)

Table 3  \( \text{NH}_4^+ \) adsorption capacities of adsorbents in aqueous solutions evaluated in batch experiments reported in the literature

<table>
<thead>
<tr>
<th>Adsorbent</th>
<th>Maximum capacity (mol kg(^{-1}))</th>
<th>Ref.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Alkaline activated and lanthanum-impregnated zeolite</td>
<td>1.54</td>
<td>12</td>
</tr>
<tr>
<td>Sodium hydroxide modified zeolite mordenite</td>
<td>3.0</td>
<td>13</td>
</tr>
<tr>
<td>Natural zeolite</td>
<td>2.36</td>
<td>14</td>
</tr>
<tr>
<td>Modified natural zeolite</td>
<td>2.14</td>
<td>14</td>
</tr>
<tr>
<td>Dowex 50w-x8</td>
<td>2.64</td>
<td>52</td>
</tr>
<tr>
<td>Sepiolite</td>
<td>3.70</td>
<td>53</td>
</tr>
<tr>
<td>Carbon nanotubes</td>
<td>0.95</td>
<td>54</td>
</tr>
<tr>
<td>Poly ligand exchanger resin</td>
<td>2.51</td>
<td>55</td>
</tr>
<tr>
<td>Cation exchange resin</td>
<td>0.81</td>
<td>56</td>
</tr>
<tr>
<td>KCuHCF</td>
<td>1.94</td>
<td>15</td>
</tr>
<tr>
<td>NaCoHCF (Flow-1.00)</td>
<td>4.36</td>
<td>This study</td>
</tr>
</tbody>
</table>
4. Conclusions

Na₄Co[Fe(CN)₆]ₓ·zH₂O (NaCoHCF) was synthesized using a batch method and various chemical compositions. Synthesis was also carried out using a flow method and a fixed composition. The adsorption capacity increased as the number of [Fe(CN)₆] vacancies decreased and the material was stable in water. Such stability is unlike that of copper hexacyanoferrate. We compared the NH₄⁺ adsorption performance with other high-capacity adsorbents under the same conditions: zeolites, Amberlite ion-exchange resin, and sepiolite. The results show that NaCoHCF exhibited the highest capacity in NH₄Cl aqueous solution. Using aqueous saline solutions with a Na⁺ ion concentration of 9350 mg L⁻¹, the benefits of using NaCoHCF are enhanced drastically. The Markham–Benton model revealed the high selectivity for NH₄⁺ against coexisting Na⁺. In addition, ammonium desorption from the adsorbent (enabling recycling) was demonstrated using an NaCl aqueous solution.

Author contributions

The manuscript was written through contributions of all authors. All authors have given approval to the final version of the manuscript.

Conflicts of interest

The authors declare no competing financial interest.

Abbreviations

SAC: Strong acid cation
MHCFs: Metal hexacyanoferrates
NaCoHCF-NPs: NaCoHCF-nanoparticles

Acknowledgements

The authors thank Ms Keiko Noda for the SEM training given to Y. J. The authors also thank Ms Ying Wang for the valuable discussion related to the Langmuir equation.

References