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# Catalytic effect of $(H_2O)_n$ (n = 1-3) on the $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$ reaction under tropospheric conditions†

Tianlei Zhang, \*\* Kai Wang, \*\* Zhangyu Qiao, \*\* Yongqi Zhang, \*\* Lin Geng, \*\* Rui Wang, Zhiyin Wang, Caibin Zhao \*\* and Linxia Jin\*\*

The effects of  $(H_2O)_n$  (n=1-3) clusters on the  $HO_2+NH_2\to NH_3+^3O_2$  reaction have been investigated by employing high-level quantum chemical calculations with M06-2X and CCSD(T) theoretical methods, and canonical variational transition (CVT) state theory with small curvature tunneling (SCT) correction. The calculated results show that two kinds of reaction,  $HO_2\cdots(H_2O)_n$  (n=1-3) +  $NH_2$  and  $H_2N\cdots(H_2O)_n$  (n=1-3) +  $NH_2$  are involved in the  $(H_2O)_n$  (n=1-3) catalyzed  $NH_2+NH_2\to NH_3+^3O_2$  reaction. Due to the fact that  $NH_2+NH_2+NH_3+^3O_2$  reaction. Due to the fact that  $NH_2+NH_3+^3O_3$  complexes have much larger stabilization energies and much higher concentrations than the corresponding complexes of  $NH_2+NH_2+NH_3+^3O_3+NH_3+^3O$ 

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### Introduction

The hydroperoxyl radical ( $HO_2$ ) and amidogen radical ( $NH_2$ ) are two important reactive radicals in atmospheric processes and combustion chemistry. As one of the most abundant free radicals in the atmosphere,  $HO_2$  is a very important and reactive intermediate in atmospheric pollutant degradation, <sup>1,2</sup> photocatalysis, <sup>3</sup> and molecular oxygen activation on metal surfaces <sup>4,5</sup> or in enzymes. <sup>6</sup> Produced from the gas phase oxidation of ammonia ( $NH_3$ ) by the hydroxyl radical (eqn (1)),  $NH_2$  is not only interesting in the combustion of fossil fuels, but is also considered to play an important role in the atmospheric formation and elimination of  $NO_x$  (ref. 7) and in the oxygen isotopic exchange of  $N_2O$ . Meanwhile,  $NH_2$  reacts with nitric acid can regenerate ammonia (eqn (2)). This reaction and the reaction shown in eqn (1) have been proposed as a potential

new catalytic-like cycle which couples the oxidation of ammonia by hydroxyl radicals and the reaction of nitric acid with amidogen radicals in the Earth's atmosphere. Based on these facts, the kinetics and mechanism of the NH $_2$  + HO $_2$  reaction (eqn (3)) have been studied experimentally and theoretically.  $^{9-15}$ 

$$NH_3 + HO \rightarrow NH_2 + H_2O \tag{1}$$

$$NH_2 + HNO_3 \rightarrow NH_3 + NO_3$$
 (2)

$$NH_2 + HO_2 \rightarrow NH_3 + O_2$$
 (3)

On experimental aspect, Sarkisov  $et~al.^{10}$  have measured the gas-phase reaction between NH<sub>2</sub> and HO<sub>2</sub> by the analytical technique of the VIS-UV absorption at a total pressure of 133–9.33  $\times$  10<sup>4</sup> Pa and the rate constant of the reaction (3) has been found to be 7.51  $\times$  10<sup>-11</sup> cm<sup>3</sup> per molecule per s at 300 K. Meanwhile, the rate constant of NH<sub>2</sub> + HO<sub>2</sub> reaction has been estimated indirectly by flash-photolysis, which is 2.5  $\times$  10<sup>-11</sup> cm<sup>3</sup> per molecule per s at 300 K.9 Theoretically, Sumathi  $et~al.^{14}$  obtained the singlet potential energy surface of reaction (3) at QCISD(T)/6–311++ G(2df,2pd)//6–311++ $G^{**}$ /MP2 level. In their work, to obtain the ratio of their product formation and to estimate the contribution of different channels over a wide range of temperature, the primary concern is to analyze the

Institute of Theoretical and Computational Chemistry, Shaanxi Key Laboratory of Catalysis, School of Chemical & Environment Science, Shaanxi University of Technology, Hanzhong, Shaanxi 723001, China. E-mail: ztianlei88@l63.com; jinlx@snut.edu.cn; Fax: +86-0916-2641083; Tel: +86-0916-2641083

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<sup>‡</sup> Kai Wang, Zhangyu Qiao, Yongqi Zhang and Lin Geng contributed equally to this work.

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competition among the various reaction channels. However, the triplet potential energy surface of reaction (3), especially, the triplet hydrogen abstraction (HA) is not involved, which is not neglected for the HA in many previous reports reaction between radical and HO2 radical.16-30 Even in some HA reaction, triplet HA is favorable kinetically. 16,18,20,23,26,29,30 So, both the singlet and triplet HA have been investigated at the CCSD(T)//B3LYP/6-311++G(3df,3pd) level by Xiang et al.31 In their work, for the favorable HA, the reaction mechanism on the triplet potential surface to be mainly a barrierless addition of HO2 to NH2 leading to an intermediate OOH···NH<sub>2</sub> (<sup>3</sup>im1), and then the adduct 3im1 goes through an H transfer forming the product of  $NH_3$  and  $^3O_2$ .

These investigations provide meaningful information about the HA of NH<sub>2</sub> + HO<sub>2</sub> reaction under atmospheric conditions. Nevertheless, these studies did not take into consideration the influence of water vapors on the reaction. In fact, firstly, water is ubiquitous in the Earth's atmosphere and its monomer can form hydrogen bonded complexes with other abundant radicals changing their photochemical features.32 Such as previous investigations showed that in the process of HO2 self-reaction, hydrogen bonded complexes HO2···H2O are formed with approximately 30% of the HO2 in the atmosphere bonding with water under typical atmospheric conditions.33 Another example is that water monomer can bind with NH2 radical, forming H<sub>2</sub>O···H<sub>2</sub>N, and H<sub>2</sub>N···H<sub>2</sub>O complexes.<sup>34</sup> Secondly, it is also known that water was found to actively participate in the atmospheric reactions of HO<sub>2</sub> + HO<sub>2</sub>, 25,35 HO<sub>2</sub> + HS, 28 HO<sub>2</sub> + HO, 26,36 HO<sub>2</sub> + SO<sub>2</sub>,37 HO<sub>2</sub> + NO<sub>2</sub> (ref. 24) and HO<sub>2</sub> + O<sub>3</sub> (ref. 38 and 39) reactions. Meanwhile, in these processes, water vapor had a catalytic effect by increasing the stability of pre-reactive complexes and reducing the activation energy of transition states. The above facts forecast that it cannot ignore water in modeling the different atmospheric HA reactions. These situations stimulated our interest in modeling the gas-phase reaction of H<sub>2</sub>O···HO<sub>2</sub>···NH<sub>2</sub> ternary system, in which the single water molecule serves as a catalyst.

Although atmospheric water molecule implies a significant catalytic effect by monomers, the catalytic effect of water dimers and also water trimers can't be ignored, because their concentrations are up to  $9 \times 10^{14}$  and  $2.6 \times 10^{12}$  molecules per cm<sup>3</sup> at 298 K.40,41 Moreover, the experimental and theoretical studies have been reported in the literature on the electronic structure of the clusters  $HO_2\cdots(H_2O)_n$   $(n=2-3)^{28,39}$  Thus, the catalytic effects of  $(H_2O)_n$  (n=2-3) are worth being investigated further on the  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  reaction.

In the present study, based on the  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$ reaction without water molecule, a detailed effects of  $(H_2O)_n$  (n =1-3) on the HA reaction of  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  have been studied at the CCSD(T)/CBS//M06-2X/6-311+G(3df,2pd) level of theory, which is organized as follows: firstly, the triplet HA reaction of  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  was investigated to compare with  $(H_2O)_n$  (n = 1-3)-assisted processes. Secondly, the reactions of  $H_2O\cdots HO_2 + NH_2$ ,  $HO_2\cdots H_2O + NH_2$ ,  $H_2O\cdots H_2N + HO_2$  and H<sub>2</sub>N····H<sub>2</sub>O + HO<sub>2</sub> with water monomer were evaluated by investigating direct HA process and double hydrogen transfer mechanism. In what follows, direct HA processes of  $HO_2 \cdots (H_2O)_2$ 

(water dimer and the whole HO2 radical formed a ring by hydrogen bonds) + NH<sub>2</sub>, HO<sub>2</sub>···(H<sub>2</sub>O)<sub>2</sub>-I (water dimer and the HO moiety of HO<sub>2</sub> radical formed a ring by hydrogen bonds) + NH<sub>2</sub> and  $H_2N\cdots(H_2O)_2 + HO_2$  reactions with  $(H_2O)_2$  were also calculated. Then, based on the discussed results of water dimer, the reactions of  $HO_2 \cdots (H_2O)_3 + NH_2$  and  $H_2N \cdots (H_2O)_3 + HO_2$  were mainly investigated for the channel of NH<sub>3</sub> + <sup>3</sup>O<sub>2</sub> formations with water trimer. Finally, the effective rate constants of the HA reaction of  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  with  $(H_2O)_n$  (n = 1-3) were calculated to investigate the atmospheric relevance of the effect of  $(H_2O)_n$  (n = 1-3). Overall, this work may lead to a better understanding of the effects of  $(H_2O)_n$  (n = 1-3) on the gas-phase reactions under tropospheric conditions.

### Computational methods

### **Electronic structure calculation**

The electronic structure calculations were performed using Gaussian 09 program package42 software. The geometries of all the reactants, intermediates, transition states and products have been optimized using the M06-2X<sup>43-46</sup> method using the 6-311+G(3df,2pd) basis set. The corresponding frequencies of the optimized geometries were computed at the same level to confirm the characteristics of the transition states with one imaginary frequency and the stationary points without imaginary frequency. Moreover, the minimum energy path (MEP) was obtained by the intrinsic reaction coordinate (IRC)47-49 theory with a gradient step size of 0.01 - 0.05 (amu)<sup>1/2</sup> bohr to prove that the TS connects to minima along the reaction path. In order to obtain more accurate relative energies, single-point energy calculations for the stationary points were performed at the CCSD(T) method50 in conjunction with CBS basis set based on the M06-2X/6-311+G(3df,2pd)-optimized geometries. The single point energy calculations of CCSD(T)/CBS have been carried out for all the species at CCSD(T) level of theory using aug-cc-pVDZ and aug-cc-pVTZ basis sets. The energy values obtained at DZ and TZ levels have been used to extrapolate the results to a complete basis set (CBS) limit.51

#### 2.2 Rate constant calculations

To estimate the effect of  $(H_2O)_n$  (n = 1-3) added, the theoretical rate constants of canonical variational transition (CVT) state theory<sup>52–54</sup> with small curvature tunneling (SCT) correction<sup>55,56</sup> for every H-abstraction channels were calculated by employing VKLab program<sup>57</sup> coupled with the steady state approximation.

In the presence of  $(H_2O)_n$  (n = 1-3), all the processes for the formations of NH $_3$  and  $^3O_2$  from the reaction of HO $_2$  and NH $_2$ involve two major steps as follows.

Step a: 
$$A + B \xrightarrow{k_1} C$$

Step b:  $C + D \xrightarrow{k_2} E \xrightarrow{k_{uni}} F$ 

Here, A and B are any two among  $HO_2$ ,  $NH_2$  and  $(H_2O)_n$  (n=1-3) clusters (water monomer, WM; water dimer, WD; and water trimer, WT), C is the binary complex formed by A and B. D is the remaining third species other than A and B. E is the ternary complex formed by  $HO_2$ ,  $NH_2$  and  $(H_2O)_n$  (n=1-3). In the step a, A combines with B to from an adduct C, whereas the step b consists of two elementary processes: in the first one, C reacts with D to form E and subsequently E undergoes uni-molecular transformation to produce the formation F via the corresponding TS.

Assuming that the intermediate E was in equilibrium with the corresponding reactants (C and D) and was at steady state, <sup>58</sup> the rate constant for step b can be written as

$$k_{\rm b} = \frac{k_2}{k_{-2} + k_{\rm uni}} k_{\rm uni} \tag{4}$$

If  $k_{\rm uni} \ll k_{-2}$ , the rate constant of  $k_{\rm b}$  was rewritten as

$$k_{\rm b} = \frac{k_2}{k_{-2} + k_{\rm uni}} k_{\rm uni} = K_{\rm eq_2} k_{\rm uni}$$
 (5)

The rate constant  $k_{\rm uni}$  in eqn (5) has been evaluated by VKLab program<sup>57</sup> in the framework of the canonical variational transition state theory (CVT).<sup>54</sup> To include the tunneling effects for motion along the reaction coordinate for the title reactions at the CCSD(T)/CBS//M06-2X/6-311+G(3df,2pd) level, the small curvature tunneling (SCT)<sup>55</sup> approximation has been adopted in this study. Besides,  $K_{\rm eq}$ , in eqn (5) was given by eqn (6).

$$K_{\text{eq}_2}(T) = \sigma \frac{Q_{\text{E}}}{Q_{\text{C}}Q_{\text{D}}} \exp\left(\frac{E_{\text{D}} + E_{\text{C}} - E_{\text{E}}}{RT}\right) \tag{6}$$

In eqn (6), the various Q values denote the partition functions of the intermediate E, reactants C and D, respectively. All partition functions were obtained using the M06-2X/6-311+G(3df,2pd) method.  $E_{\rm D}$ ,  $E_{\rm C}$  and  $E_{\rm E}$  stand for the energies of the species of D, C and E, respectively;  $\sigma$  is the symmetry factor. In the present work,  $k_{\rm b}$  has been used to compare the rates between bare reaction and catalyzed reactions.

### 2.3 Effective rate constant calculations

If one incorporates the effect of step a, the resultant rate constant  $(k_t)$  can be written as:

$$k_{\rm t} = K_{\rm eq} K_{\rm eq} k_{\rm uni} \tag{7}$$

where  $K_{\text{eq}_1}$  stands for the equilibrium constant in step a *i.e.*  $K_{\text{eq}_1} = k_1/k_{-1}$ , and  $K_{\text{eq}_1}$  was given by eqn (8).

$$K_{\text{eq}_1}(T) = \sigma \frac{Q_{\text{C}}}{Q_{\text{A}} Q_{\text{B}}} \exp\left(\frac{E_{\text{A}} + E_{\text{B}} - E_{\text{C}}}{RT}\right)$$
(8)

In eqn (8), the various Q values denote the partition functions of the complex C, reactants A and B, respectively.  $E_{\rm A}$ ,  $E_{\rm B}$  and  $E_{\rm C}$  stand for the energies of the species of A, B and C,

respectively. From the above, the rate of the reaction  $(\nu)$  in the presence of catalysts can be written as:

$$v = K_{eq} K_{eq} k_{uni}[A][B][D] = k_t[A][B][D] = k'_t[A][B]$$
 (9)

 $k'_{\rm t}$  is the effective rate constant, which could be considered as a measure of the relative efficiencies of the different catalysts under atmospheric conditions, as it includes the concentration as well as rate constant of a particular catalyst.

### 3. Results and discussion

The transition states in each reaction channel were signed by "TS" followed by a number, and intermediates were denoted by "IM" followed by a number. The letters "a", "b", and "c" were used to distinguish the transition states and intermediates that were conformers of each other and therefore had the same features; a species in the presence of water monomer, water dimer and water trimer was respectively denoted by a "WM", "WD", and "WT" suffix.

## 3.1 Potential energy surfaces and the rate constants for the hydrogen abstraction of $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$ reaction

The  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  reaction was investigated theoretically by Xiang et al.31 at the CCSD(T)/6-311++G(3df,3pd)// B3LYP/6-311++G(3df,3pd) level. In this study, we have reinthat work at the CCSD(T)/CBS//M06-2X/6-311+G(3df,2pd) level to determine the outcome of this reaction when  $(H_2O)_n$  (n = 1-3) was present. As seen in Fig. 1, regarding the HA reaction of  $HO_2$  +  $NH_2$  to produce  $NH_3$  +  $^3O_2$ , only one elementary reaction path was identified (Channel R1). Starting from HO<sub>2</sub> + NH<sub>2</sub> reactants, Channel R1 began with the intermediate IM. The binding energy of IM was  $6.9 \text{ kcal mol}^{-1}$ , agree with that (3im1, 7.4 kcal mol-1) in the literature reported by Xiang et al. 31 For IM, from geometrical point of view, a hydrogen bond shown in Fig. 1 was formed between the H atom of HO<sub>2</sub> and the N atom of NH2 radical (with a computed H···N bond distance of 1.81 Å at the M06-2X/6-311+G(3df,2pd) level of theory). With the N atom of NH2 radical attacks the H atom of HO2, the intermediate IM in Channel R1 proceeded through a transition state TS with the energy predicted to be at 4.5 kcal mol<sup>-1</sup> below the initial reactants. The energy of TS is quite different from 3ts3 (6.8 kcal mol-1 below HO<sub>2</sub> + NH<sub>2</sub>

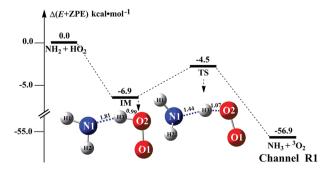


Fig. 1 Schematic energy diagram for the  $HO_2 + NH_2$  reaction; energies (kcal  $mol^{-1}$ ) at the CCSD(T)/CBS//M06-2X/6-311+G(3df,2pd)) level of theory.

reactants) in the literature reported by Xiang et al.31 This difference is possible due to the fact that the different levels of theory used for the ZPE and single-point energy calculation. Besides, the  $\Delta H$  (298) of  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  reaction was predicted to be -57.0 kcal mol<sup>-1</sup>, compared with the experimental<sup>59</sup> estimation of  $-58.5 \pm 0.4$  kcal mol<sup>-1</sup>. For reaction (1) without water, Table S1† lists its CVT/SCT rate constant. As seen in Table S1,† tunneling slightly increases the rate constant, while the recrossing effects decrease the rate constant. For example, the rate constant is increased by 62% due to tunneling, while the rate constant is decreased to 52% because of recrossing effects at the M06-2X/6-311+G(3df,2pd) level and at 298 K (Table S1†). It is noted that tunneling and recrossing effects slightly depend on temperature. Tunneling slightly increases with the decrease of temperature, while recrossing effects slightly increase with the increase of temperature as listed in Table S1.† Specifically, the calculated results using M06-2X/aug-cc-pVTZ indicate that the rate constant is increased by 32% and 20% due to tunneling, while the rate constant is decreased to 44% and 60% at 275 and 320 K, respectively. So, similar with previous investigations,60,61 the tunneling transmission coefficients are very large for the hydrogen atom transfer process. Thus, herein the computed CVT/SCT rate constants have been used to estimate the catalytic effect of  $(H_2O)_n$  (n = 1-3). CVT/SCT rate constant calculations were carried out for Channel R1 at various temperatures. The values are listed in Table S1.† At 300 K, the calculated value of  $k_{\rm R}$  was  $2.68 \times 10^{-11} \text{ cm}^3 \text{ per molecule per s}$  The calculated values compare closely with  $7.51 \times 10^{-11}$  cm<sup>3</sup> per molecule per s and

# 3.2 Geometrical analysis and the concentration calculation for $HO_2\cdots(H_2O)_n$ (n=1–3) and $H_2N\cdots(H_2O)_n$ (n=1–3) complexes

 $2.5 \times 10^{-11} \text{ cm}^3$  per molecule per s, at 300 K respectively pre-

dicted by Sarkisov et al. 10 and Cheskis et al. 9 indicating that the

calculations for the  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  reaction without

and with  $(H_2O)_n$  (n = 1-3) at the CCSD(T)/CBS//M06-2X/6-

311+G(3df,2pd) level of theory are acceptable.

In the presence of  $(H_2O)_n$  (n = 1-3), both bodies of  $HO_2$  and  $NH_2$ can respectively interact with the second body of  $(H_2O)_n$  (n=1-3) via hydrogen bond to form two-body complexes of HO<sub>2</sub>···  $(H_2O)_n$  (n = 1-3) and  $H_2N\cdots(H_2O)_n$  (n = 1-3) first in the entrance channels before interacting with the third body of NH<sub>2</sub> or HO<sub>2</sub>. So, it is very necessary to find the stable configurations of the complexes  $HO_2\cdots(H_2O)_n$  (n=1-3) and  $H_2N\cdots(H_2O)_n$  (n=1-3)firstly. In order to find all possible stable configurations of the complexes  $HO_2 \cdots (H_2O)_n$  (n = 1-3) and  $H_2 N \cdots (H_2O)_n$  (n = 1-3), the global minimum searching of geometric structures were carried out using Tsinghua Global Minimum (TGMin). 62,63 Then the initial structures for  $HO_2\cdots(H_2O)_n$  (n=1-3) and  $H_2N\cdots$  $(H_2O)_n$  (n = 1-3) were selected for geometry optimization using the M06-2X/6-31G(d) method. The isomer structures within 6.0 kcal mol<sup>-1</sup> of the global minimum were re-optimized by M06-2X/6-311+G(3df,2pd) method. The Fig. 2 and S1† show the optimized geometrical reactants of  $HO_2 \cdots (H_2O)_n$  (n = 1-3) and  $H_2N\cdots(H_2O)_n$  (n = 1-3), which are in good agreement with

available previous results.<sup>64,65</sup> As seen in Fig. 2 and S1,† as the number of water molecules increases in a given cluster of  $HO_2\cdots$   $(H_2O)_n$  (n=1-3) and  $H_2N\cdots(H_2O)_n$  (n=1-3), the number of possible configurations for the cluster increases quickly, and each of the configurations becomes increasingly complicated. Regarding to each type equilibrium structure of  $HO_2\cdots(H_2O)_n$  (n=1-3) and  $H_2N\cdots(H_2O)_n$  (n=1-3), herein we only focus on the stable configuration shown in Fig. 2, which has the larger stabilization energy and the higher concentration than its isomers.

As seen in Fig. 2 and Table S2,† consistent with previous reports, 24,25,28,37,66 five-membered ring complex H2O···HO2 was much more stable than the single hydrogen bond complexes HO<sub>2</sub>···H<sub>2</sub>O, H<sub>2</sub>N···H<sub>2</sub>O and H<sub>2</sub>O···H<sub>2</sub>N with its binding energy larger by 3.6-5.9 kcal mol<sup>-1</sup> than those of latter ones. The equilibrium constants of these complexes at 298 K are 1.83 imes $10^{-19}$ ,  $3.05 \times 10^{-22}$ ,  $1.34 \times 10^{-22}$  and  $8.40 \times 10^{-21}$  cm<sup>3</sup> per molecule, respectively (Table S3†). Considering typical tropospheric concentrations of 7.73 × 10<sup>17</sup> molecules per cm<sup>3</sup> of  ${\rm H_2O}$ , 3  $\times$  10<sup>8</sup> molecules per cm<sup>3</sup> of  ${\rm HO_2}$ , 67 and our estimated concentrations of NH<sub>2</sub> (6.0  $\times$  10<sup>-11</sup> molecules per cm<sup>3</sup> seen in ESI†), it is estimated that the atmospheric concentration of the  $H_2O\cdots HO_2$  complex to be  $4.24 \times 10^7$  molecules per cm<sup>3</sup>, which is larger by  $6.00 \times 10^2$  times than that of  $HO_2 \cdots H_2O$ . However, in our previous works, 25,26 the reaction channels of HO2...H2O + HO<sub>2</sub> and HO<sub>2</sub>···H<sub>2</sub>O + HO were not neglected in water-catalyzed  $HO_2 + HO_2$  and  $HO_2 + HO$ . So, for water catalyzed  $HO_2 + NH_2 \rightarrow$  $NH_3 + {}^3O_2$  reaction, both  $H_2O\cdots HO_2 + NH_2$  and  $HO_2\cdots H_2O +$ NH<sub>2</sub> reactions have been investigated in the following section. Besides these, at 298 K, the concentrations of H<sub>2</sub>N···H<sub>2</sub>O (3.90  $\times$  10<sup>-13</sup> cm<sup>3</sup> per molecule) and H<sub>2</sub>O···H<sub>2</sub>N (6.21  $\times$  10<sup>-15</sup> cm<sup>3</sup> per molecule) shown in Table S3† were much lower than those of  $H_2O\cdots HO_2$  (4.24 × 10<sup>7</sup> cm<sup>3</sup> per molecule) and  $HO_2\cdots H_2O$  $(7.07 \times 10^4 \text{ cm}^3 \text{ per molecule})$ . Thus, in water catalyzed HO<sub>2</sub> +  $NH_2 \rightarrow NH_3 + {}^3O_2$  reaction, we predict that the atmospheric relevance of  $H_2O\cdots HO_2 + NH_2$  and  $HO_2\cdots H_2O + NH_2$  reactions will be much more obvious than those of  $H_2N\cdots H_2O + HO_2$  and  $H_2O\cdots H_2N + HO_2$  reactions. Thus, only  $H_2O\cdots HO_2 + NH_2$  and HO<sub>2</sub>···H<sub>2</sub>O + NH<sub>2</sub> reactions have been taken into account in the following section, whereas, for comparison, the potential energy surfaces (PESs) for H2N···H2O + HO2 and H2O···H2N + HO<sub>2</sub> reactions has been displayed in Fig. S5,† and their corresponding rate constants were shown in Table S7.†

For the clusters constituted by  $HO_2$  (or  $NH_2$ ) radical and water dimer, in geometrical point of view,  $HO_2\cdots(H_2O)_2$  (water dimer and the whole  $HO_2$  radical formed a ring by hydrogen bonds) shows seven-membered ring structure, whereas both  $HO_2\cdots(H_2O)_2$ –I (water dimer and the HO moiety of  $HO_2$  radical formed a ring by hydrogen bonds) and  $H_2N\cdots(H_2O)_2$  involves a sixmembered ring. So, the binding energy of  $HO_2\cdots(H_2O)_2$  (shown in Table  $S2^{\dagger}$ ) was 12.6 kcal  $mol^{-1}$ , which was larger by 3.9–6.4 kcal  $mol^{-1}$  than those of  $HO_2\cdots(H_2O)_2$ –I and  $H_2N\cdots(H_2O)_2$  due to smaller ring tension. Similarity, nine-membered ring  $HO_2\cdots(H_2O)_3$  (water trimer and the whole  $HO_2$  radical formed a ring by hydrogen bonds) was larger by 2.0–7.3 kcal  $mol^{-1}$  than those of eight-membered ring  $HO_2\cdots(H_2O)_3$ –I (water trimer and the HO moiety of  $HO_2$  radical formed a ring by hydrogen bonds)

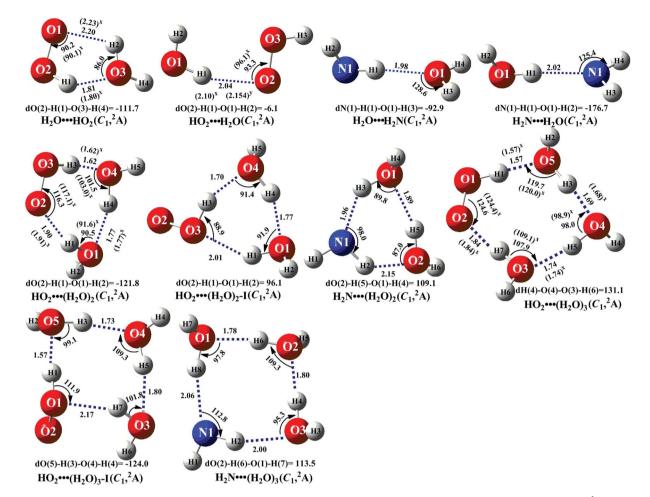


Fig. 2 The geometrical structures of the optimized complexes at the M06-2X/6-311+G(3df,2pd) level of theory (bond length Å, bond angle °).

and  $H_2N\cdots(H_2O)_3$ . From another point of view shown in Table S3,† the concentrations of  $H_2N\cdots(H_2O)_2$  (5.13  $\times$  10<sup>-17</sup> cm<sup>3</sup> per molecule) and  $H_2N \cdots (H_2O)_3$  (1.02 × 10<sup>-19</sup> cm<sup>3</sup> per molecule) are also much lower than those of  $HO_2 \cdots (H_2O)_2$  (5.14 × 10<sup>5</sup> cm<sup>3</sup> per molecule) and  $HO_2 \cdots (H_2O)_3$  (8.02 × 10<sup>3</sup> cm<sup>3</sup> per molecule) at 298 K, thus we predict that the atmospheric relevance of H<sub>2</sub>N····  $(H_2O)_2 + HO_2$  and  $H_2N \cdots (H_2O)_3 + HO_2$  reactions can be neglected. However, for comparison, the PESs for  $H_2N\cdots(H_2O)_2 + HO_2$  and  $H_2N\cdots(H_2O)_3 + HO_2$  reactions have been displayed in Fig. S6 and S7,† and their corresponding rate constants were shown in Table S7.† Besides these, the concentrations of  $HO_2\cdots(H_2O)_2$  and  $HO_2\cdots(H_2O)_3$  are respectively larger by 140 and 9 times than the corresponding complexes of HO2···(H2O)2-I and HO2···(H2O)3-I at 298 K. So, we predict that the catalytic effect of  $HO_2 \cdots (H_2O)_2$ -I + NH<sub>2</sub> and HO<sub>2</sub>···(H<sub>2</sub>O)<sub>3</sub>-I + NH<sub>2</sub> reactions are less obvious than the corresponding reactions of  $HO_2\cdots(H_2O)_2 + NH_2$  and  $HO_2\cdots$  $(H_2O)_3 + NH_2$ .

### 3.3 Potential energy surfaces and the rate constants for HO<sub>2</sub> + NH<sub>2</sub> $\rightarrow$ NH<sub>3</sub> + ${}^{3}$ O<sub>2</sub> reaction with H<sub>2</sub>O

It has been pointed out in Section 3.2 that water-catalyzed the reaction (3) is mainly occurring through H<sub>2</sub>O···HO<sub>2</sub> + NH<sub>2</sub> and HO<sub>2</sub>···H<sub>2</sub>O + NH<sub>2</sub> reactions. So, Fig. 3 presents the PESs for

H<sub>2</sub>O···HO<sub>2</sub> + NH<sub>2</sub> (Channel WM1) and HO<sub>2</sub>···H<sub>2</sub>O + NH<sub>2</sub> (Channel WM2) reactions along with the local minimum geometries on the corresponding reaction pathways.

Regarding to Channel WM1, by different collisions between H<sub>2</sub>O···HO<sub>2</sub> and NH<sub>2</sub>, two kinds of reaction types have been found, which were labeled as Channel WM1a and Channel WM1b. For Channel WM1a, starting from  $H_2O\cdots HO_2 + NH_2$ reactants, hydrogen-bonded complex IM\_WM1 was formed by the interaction between N atom of NH2 radical and one H atom of the H<sub>2</sub>O moiety in H<sub>2</sub>O···HO<sub>2</sub> complex with a bonding energy of 5.5 kcal mol<sup>-1</sup>. After a flat potential energy surface through TS\_WM1, with an energy barrier of 4.3 kcal mol<sup>-1</sup>, the formation of seven-member cyclic complex IM\_WM2 was formed with a binding energy of 7.3 kcal mol<sup>-1</sup> relative to  $H_2O\cdots HO_2 + NH_2$ reactants. Following complex IM\_WM2, Channel WM1a proceeded through transition state TS\_WM2 to produce the product of  $NH_3 \cdots H_2O$  and  $^3O_2$  after climbing the barrier height of 3.4 kcal mol<sup>-1</sup>. In the transition state TS\_WM2, the sevenmembered ring structure was still conserved with the N atom of NH<sub>2</sub> radical abstracting the H atom of HO<sub>2</sub> moiety in H<sub>2</sub>O··· HO2 complex.

Similar with Channel WM1a, Channel WM1b also followed stepwise process. In the first step, similar with the ring enlargement from IM\_WM1 to IM\_WM2 in Channel WM1a, the

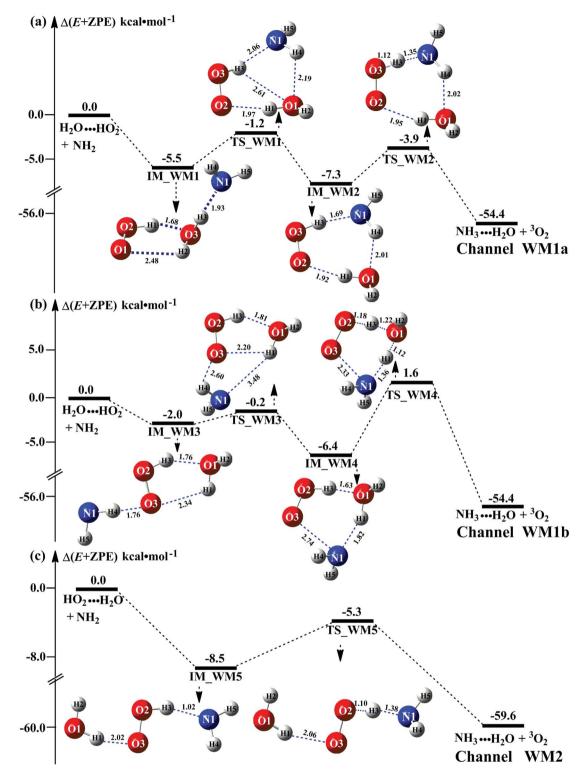


Fig. 3 Schematic energy diagram for the water assisted  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  reaction occurring through  $H_2O \cdots HO_2 + NH_2$  (a and b), and  $HO_2 \cdots H_2O + NH_2$  (c) reactions; energies (kcal mol<sup>-1</sup>) at the CCSD(T)/CBS//M06-2X/6-311+G(3*df*,2*pd*) level of theory.

five-membered ring complex IM\_WM3 is rearranged into sevenmembered ring complex IM\_WM4 through TS\_WM3. In geometrical point of view, complex IM\_WM4 has similar sevenmembered cyclic structure as IM\_WM2 with the NH<sub>2</sub> radical and the water molecule exchanging their positions. The binding energy of IM\_WM4 is 6.4 kcal mol<sup>-1</sup>, lowered by 0.9 kcal mol<sup>-1</sup> than that of IM\_WM2. In the second step, differently from transition state TS\_WM2 in Channel WM1a that involves a direct HA, transition state TS\_WM4 in Channel WM1b contains a double hydrogen transfer mechanism. Consistent

Table 1 Rate constants (cm<sup>3</sup> per molecule per s) of the HO<sub>2</sub> + NH<sub>2</sub>  $\rightarrow$  NH<sub>3</sub> + <sup>3</sup>O<sub>2</sub> reaction with (H<sub>2</sub>O)<sub>n</sub>(n = 1-3)<sup>a,b</sup>

<i>T</i> (K)	$k_{\rm b}({ m WM1a})$	$k_{\rm b}({ m WM1b})$	$k_{\rm b}({ m WM2})$	$k_{\rm b}({ m WD1})$	$k_{\rm b}({ m WD2})$	$k_{\rm b}({ m WT1})$
275	$6.53 \times 10^{-11}$	$6.36 \times 10^{-15}$	$2.21 \times 10^{-11}$	$1.35 \times 10^{-15}$	$1.84 \times 10^{-17}$	$1.47 \times 10^{-14}$
280	$5.23 \times 10^{-11}$	$5.85 \times 10^{-15}$	$1.70 \times 10^{-11}$	$1.39 \times 10^{-15}$	$1.92 \times 10^{-17}$	$1.45 \times 10^{-14}$
290	$3.46 \times 10^{-11}$	$5.00  imes 10^{-15}$	$1.04  imes 10^{-11}$	$1.48 \times 10^{-15}$	$2.07 \times 10^{-17}$	$1.42 \times 10^{-14}$
298	$2.54 \times 10^{-11}$	$4.44\times10^{-15}$	$7.19 \times 10^{-12}$	$1.56 \times 10^{-15}$	$2.20 \times 10^{-17}$	$1.41 \times 10^{-14}$
300	$2.38 \times 10^{-11}$	$4.32 \times 10^{-15}$	$6.62 \times 10^{-12}$	$1.58 \times 10^{-15}$	$2.23 \times 10^{-17}$	$1.40 \times 10^{-14}$
310	$1.68 \times 10^{-11}$	$3.79 \times 10^{-15}$	$4.34 \times 10^{-12}$	$1.68 \times 10^{-15}$	$2.39 \times 10^{-17}$	$1.39 \times 10^{-14}$
320	$1.23 \times 10^{-11}$	$3.35 \times 10^{-15}$	$2.92 \times 10^{-12}$	$1.78 \times 10^{-15}$	$2.55 \times 10^{-17}$	$1.38 \times 10^{-14}$

 $<sup>{}^{</sup>a} \ k_{b}(\text{WM1a}), k_{b}(\text{WM1b}), k_{b}(\text{WM2}) \ \text{and} \ k_{b}(\text{WD1}), k_{b}(\text{WD2}), k_{b}(\text{WT1}) \ \text{is the rate constants of} \ (\text{H}_{2}\text{O})_{n} \ (n = 1 - 3) \ \text{-assisted HO}_{2} + \text{NH}_{3} + {}^{3}\text{O}_{2} \ \text{reaction occurring through Channels WM1a}, WM1b, WM2 WD1, WD2, and WT1, respectively. } \\ {}^{b} \ 1/k_{uni}(\text{WM1a}) = 1/k(\text{TS}_{wm1}) + 1/k(\text{TS}_{wm2}); 1/k_{uni}(\text{WM1b}) \\ = 1/k(\text{TS}_{wm3}) + 1/k(\text{TS}_{wm4}); 1/k_{uni}(\text{WD1}) = 1/k(\text{TS}_{wm1}) + 1/k(\text{TS}_{wm1}) +$ 

with our previous reports,28 such mechanism discrepancy between Channels WM1a and WM1b may lead that the energy barrier of the second step in Channel WM1a is 3.4 kcal mol<sup>-1</sup>, which is lower by 4.6 kcal mol<sup>-1</sup> than that of the second step in Channel WM1b. The reason can be possibly explained in three following aspects: (1) transition state TS\_WM2 in the former reaction shows seven-member ring structure, whereas the transition state TS\_WM4 in the latter reaction shows sixmember ring structure. That is, TS\_WM4 has larger ring tension than that of TS\_WM2; (2) different from the structures in the process of IM\_WM4 -> TS\_WM4 where the three hydrogen atoms (H2, H4 and H5) are out of plane, the structure in the process of IM\_WM2 → TS\_WM2 is close to the coplanar structure, which makes the conjugated hydrogen bonding system (H3···N1, H4···O1 and H1···O2) more stable; (3) NBO charge analysis shows that (Fig. S8†), the distance between the negatively NBO charged O3 and N1 atoms was decreases from IM-WM4 (2.70 Å)  $\rightarrow$  TS-WM4 (2.33 Å), resulting in enhanced repulsive interactions, and hence the energy of the system is

As shown in Table 1, it is worth noting that the rate constants both of Channel WM1a (kb(WM1a)) and Channel WM1b  $(k_b(WM1b))$  are increased with the decrease of temperature. This is because the calculated bimolecular rate constant contains two different components, (see Table S7 $\dagger$ )); (1)  $K_{eq}$ from the first step (bimolecular addition between H2O···HO2 and NH<sub>2</sub>) and (2) k<sub>2</sub> from the second step (IM\_WM1 (or  $IM_WM3) \rightarrow NH_3\cdots H_2O + {}^3O_2$ ). The second step always contributes to the positive activation energy due to the finite positive barrier, while the first step corresponds to negative activation energy as it involves barrierless addition of isolated reactants to form the complex IM\_WM1 (or IM\_WM3). Consequently,  $K_{eq}$  always decreases with increase in temperature, whereas  $k_2$  behaves in opposite manner (Table S7†). Whenever  $k_2$  dominates over  $K_{eq}$  the overall activation energy of the reaction is found to be positive and when  $K_{eq}$  dominates over  $k_2$  then the overall activation energy of the reaction become negative. For example, for Channel RW1a,  $K_{\rm eq}$  decreases by  $\sim$ 6.69 times and  $k_2$  value increases  $\sim$ 1.26 times with increasing temperature from 275 to 320 K. The rate constant of Channel WM1a  $(k_b(WM1a))$  within the temperature range of 275–320 K is much larger than the corresponding value of  $k_b$ (WM1b) in Channel

WM1b, given that the ratio of  $k_b$ (WM1a)/ $k_b$ (WM1b) is  $3.67 \times 10^3$  to  $1.03 \times 10^4$ . As a result, in the following section, the reaction type where water dimer and water trimer act as a "bridge" will not be considered in the reactions between  $HO_2\cdots(H_2O)_2 + NH_2$  and  $HO_2\cdots(H_2O)_3 + NH_2$ .

Differently from Channel WM1a and Channel WM1b above which involve a stepwise process, HO<sub>2</sub>···H<sub>2</sub>O + NH<sub>2</sub> reaction (Channel WM2) contains a one-step mechanism. As for Channel WM2, the reaction started with the formation of a pre-reactive hydrogen bond complex IM\_WM5. Compared with the naked complex IM (Fig. 1), in view of geometry, complex IM\_WM5 was stabilized by an additional weak hydrogen bond (O3···H1, 2.02 Å) and thus, the binding energy of IM WM5 was enhanced by 1.6 kcal mol<sup>-1</sup> than that of IM. Starting from IM\_WM5, Channel WM2 proceeded through transition state TS\_WM5, which is similar in structure to the naked transition state TS, where the N atom of NH2 radical directly abstracted the hydrogen of HO2. The rate constant of Channel WM2 ( $k_b$ (WM2)) listed in Table 1 is only lower by 3-4 times than the corresponding value of  $k_b$ (WM1a) in Channel WM1a. However, for  $H_2O\cdots HO_2$  complex, both the concentration and equilibrium constant at 298 K is larger by 2 orders of magnitude than that of HO2····H2O. As a result, atmospheric relevance of H2O···HO2 + NH2 reaction occurring through directing HA will be obvious than that of  $HO_2 \cdots H_2O + NH_2$  reaction. Besides these, compared with the rate constant of  $H_2N\cdots H_2O + HO_2$  reaction ( $k_b(WM3)$ ) listed in Table S7,† though the value of  $k_b$ (WM1a) is smaller by 2 orders of magnitude, atmospheric relevance of H<sub>2</sub>N···H<sub>2</sub>O + HO<sub>2</sub> reaction will be neglected with respect to H2O···HO2 + NH2 reaction, due to the fact that the concentration of H2N···H2O complex is much lower than that of  $H_2O\cdots HO_2$ . This result can be further proved by the effective rate constant in the following section. So, atmospheric relevance of H<sub>2</sub>O···HO<sub>2</sub> + NH<sub>2</sub> reaction occurring through directing HA will be most obvious in water monomer catalyzed  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  reaction.

# 3.4 Potential energy surfaces and the rate constants for $HO_2$ + $NH_2 \rightarrow NH_3 + {}^3O_2$ reaction with $(H_2O)_2$

As the discussion in Section 3.2 that the atmospheric relevance of  $HO_2\cdots(H_2O)_2 + NH_2$  reaction is most obvious in water dimercatalyzed the reaction (3). So, Fig. 4 shows the PESs of  $HO_2\cdots(H_2O)_2 + NH_2$  reaction (Channel WD1) with its rate constant

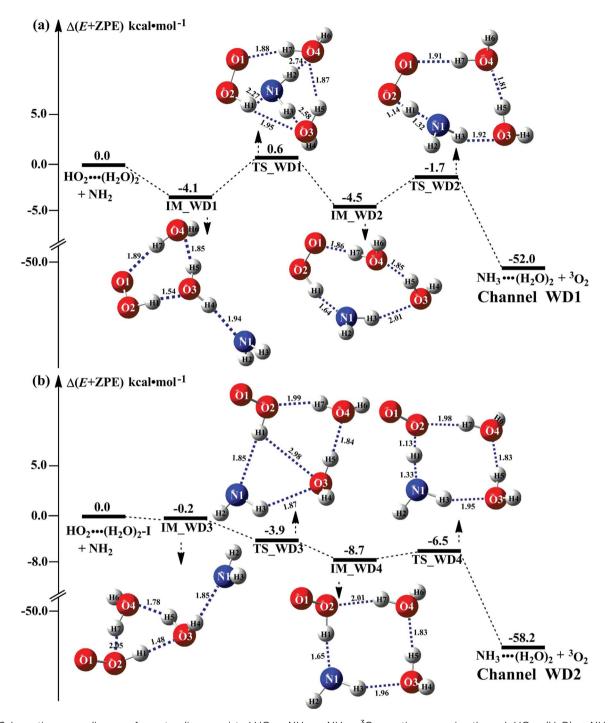


Fig. 4 Schematic energy diagrams for water dimer-assisted  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  reaction occurring through  $HO_2 \cdots (H_2O)_2 + NH_2$  (a) and  $HO_2 \cdots (H_2O)_2 - I + NH_2$  (b) reactions; energies (kcal mol<sup>-1</sup>) at the CCSD(T)/CBS//M06-2X/6-311+G(3df,2pd) level of theory.

listed in Table 1. For comparison, PESs for  $HO_2\cdots(H_2O)_2$ -I + NH<sub>2</sub> reaction (Channel WD2) was displayed in Fig. 4, and its corresponding rate constant was shown in Table 1.

For Channels WD1 and WD2 shown in Fig. 4, both reactions proceeded through a stepwise mechanism, where the reaction firstly occurred via a ring enlargement, and then proceed through a direct HA. However, the rate constant of Channel WD2 ( $k_b$ (WD2)) listed in Table 1 is much smaller than

the corresponding value of  $k_b(WD1)$  in Channel WD1, given that the ratio of  $k_b(WD1)/k_b(WD2)$  is 69.8–73.4. Meanwhile, the value of  $k_b(WD1)$  is larger by 6 orders of magnitude than that of  $k_b(WD3)$  (H<sub>2</sub>N···(H<sub>2</sub>O)<sub>2</sub> + HO<sub>2</sub> reaction). Thus, for the reaction (3) with water dimer,  $HO_2 \cdots (H_2O)_2 + NH_2$  reaction (Channel WD1) is of great atmospheric relevance due to its larger rate constant, and only this channel has been mainly taken into account here.

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Consistent with the favorable channel of H<sub>2</sub>O···HO<sub>2</sub> + NH<sub>2</sub> reaction (Channel WM1a) above, as for Channel WD1, with the collision between NH2 and HO2···(H2O)2, the reaction occurred via a stepwise mechanism. In the first step, Channel WD1 went through a ring enlargement from seven-membered ring complex IM WD1 to nine-membered ring complex IM WD2 via transition state TS\_WD1 with an energy barrier of 4.7 kcal mol<sup>-1</sup>. In geometrical point of view, complexes IM\_WD1 and IM\_WD2 have similar structures as the corresponding complexes of IM WM1 and IM WM2, expecting that water monomer was substituted by water dimer. So, in energetic point of view, similar with the fact that the complex IM\_WM2 in Channel WM1a (Fig. 3) is more stable than IM\_WM1, complex IM\_WD2 in Channel WD1 is stable than IM\_WD1. However, the stabilization energy of IM WD2 has been reduced by 2.8 kcal mol<sup>-1</sup> than that of IM\_WM2. In the second step, following IM WD2 complex, with the N atom of NH2 abstracting the H atom of  $HO_2$  moiety in  $HO_2 \cdots (H_2O)_2$ , Channel WD1 can proceed via an elementary reaction of direct HA (TS\_WD2) to form the products of  $NH_3\cdots(H_2O)_2 + {}^3O_2$ . Similar with complex IM\_WD2, TS\_WD2 also shows a nine-membered ring structure with water dimer, NH2 radical and HO2 radical involved. The relative energy of TS\_WD2 to  $HO_2 \cdots (H_2O)_2 + NH_2$ is -1.7 kcal mol<sup>-1</sup>, which is higher by 2.2 kcal mol<sup>-1</sup> than that of the water-assisted transition state TS\_WM2 to H2O···HO2 + NH<sub>2</sub> reactants. Meanwhile, the rate constant of Channel WD1,

as shown in Table 1, is smaller by 3-4 orders of magnitude than

that of  $k_b$ (WM1a) with single water. Due to the fact that  $H_2O\cdots$   $HO_2$  has higher concentration than that of  $HO_2\cdots(H_2O)_2$ , we predict that Channel WD1 has less obvious positive influence on enhancing the rate of the reaction (eqn (3)) than Channels WM1a.

# 3.5 Potential energy surfaces and the rate constants for $HO_2$ + $NH_2 \rightarrow NH_3 + {}^3O_2$ reaction with $(H_2O)_3$

It is of interest to known whether  $(H_2O)_3$  will affect the  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  reaction. Thus, based on the discussed results above that the reaction of  $NH_2$  radical with  $HO_2 \cdots (H_2O)_2$  is more favorable than the reactions of  $NH_2$  radical with  $HO_2 \cdots (H_2O)_2$ –I in the presence of water dimer, only the reaction of  $NH_2$  radical with  $HO_2 \cdots (H_2O)_3$  was mainly investigated for the channel of  $NH_3 + {}^3O_2$  formations with water trimer due to that the binding energy (Table S2†) and the concentration (Table S3†) of  $HO_2 \cdots (H_2O)_3$  are much larger than those of  $H_2N \cdots (H_2O)_3$ ,  $HO_2 \cdots (H_2O)_3$ –I. The schematic potential energy surfaces for  $HO_2 \cdots (H_2O)_3 + NH_2$  reaction was shown in Fig. 5, meanwhile its rate constant is also listed in Table 1, which is larger by 6 orders of magnitude than that of  $k_b(WT2)$  ( $H_2N \cdots (H_2O)_3 + HO_2$  reaction) involved in Table S7.†

Regarding the reaction of  $HO_2\cdots(H_2O)_3 + NH_2$ , the prereactive complex  $IM\_WT1$  was formed with the energy of 1.1 kcal  $mol^{-1}$  with respect to the  $HO_2\cdots(H_2O)_3 + NH_2$  reactants. Starting from complex  $IM\_WT1$ , the reaction occurs via

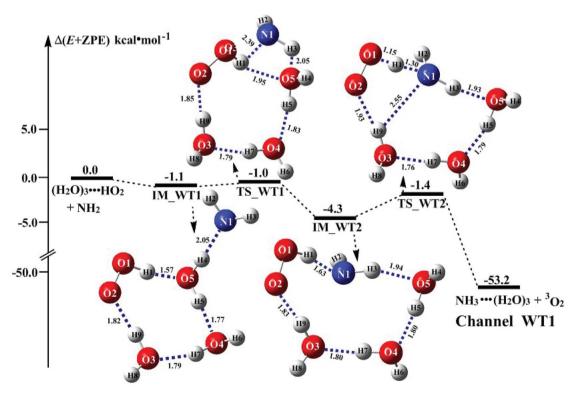


Fig. 5 Schematic energy diagrams for water trimer-assisted  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  reaction occurring through  $HO_2 \cdots (H_2O)_3 + NH_2(a)$  reactions; energies (kcal mol<sup>-1</sup>) at the CCSD(T)/CBS//M06-2X/6-311+G(3*df*,2*pd*) level of theory. \*Value was from ref. and key interatomic distances (angstroms) and angles (degrees) of molecular structures was given at the M06-2X/aug-*cc*-pVTZ. \*Value was from ref. and key interatomic distances (angstroms) and angles (degrees) of molecular structures was given at the MP2/6-31G\* level of theory.

transition state TS\_WT1 and to form a complex IM\_WT2 with a barrier of 0.1 kcal mol<sup>-1</sup> relative to the pre-reactive complex IM\_WT1. This step involves a geometric rearrangement that plays a crucial role in HO<sub>2</sub>···(H<sub>2</sub>O)<sub>3</sub> + NH<sub>2</sub> reaction. IM\_WT2 is more stabilized than IM WT1 by 3.2 kcal mol<sup>-1</sup>. From the geometric point of view, complex IM WT2 has similar quasiplanar structure as that of IM\_WD2 with the additional water molecule inserted between HO2 and NH2. The relative energy of IM\_WT2 is -4.3 kcal mol<sup>-1</sup> with respect to  $HO_2 \cdots (H_2O)_3 + NH_2$ .

Transition state TS WT2 was found between IM WT2 and the products  $(H_3N\cdots(H_2O)_3$  and  $^3O_2)$ . For the TS\_WT2, a HA reaction occurs by the N atom of NH2 abstracted the H atom of HO2 radical as that in TS\_WD2 with the additional water molecule inserted between HO2 and NH2. TS\_WT2 lies 1.4 kcal mol<sup>-1</sup> below the  $HO_2 \cdots (H_2O)_3 + NH_2$  reactants, which is 0.3 kcal mol<sup>-1</sup> higher in energy than the relative energy of TS\_WD2 to  $HO_2 \cdots (H_2O)_2 + NH_2$  reactants. Meanwhile, the rate constant of Channel WT1 (shown in Table 1) is larger by 8-11 times than that of  $k_b(WD1)$  with water dimer. Due to the fact that  $HO_2\cdots(H_2O)_2$  has higher concentration than that of  $HO_2\cdots$ (H<sub>2</sub>O)<sub>3</sub>, thus, whether the atmospheric relevance of HO<sub>2</sub>···  $(H_2O)_3$  + NH<sub>2</sub> reaction is obvious than that of  $HO_2\cdots(H_2O)_3$  + NH2 reaction or not, needs further discussion in the next section.

### 3.6 Application in atmospheric chemistry

Beyond above mechanisms and rate constant without and with  $(H_2O)_n$  (n = 1-3), another aim of our work was to study the influence of  $(H_2O)_n$  (n = 1-3) on the  $HO_2 + NH_2$  reaction under atmospheric conditions. Thus, it is necessary to compare the title rate in the absence of  $(H_2O)_n$  (n = 1-3) with the effective rates of the favorable reactions in the presence of  $(H_2O)_n$  (n=1-3). Table 2 lists the calculated effective rate constants for the favorable channels of  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  reaction without and with  $(H_2O)_n$  (n = 1-3). For comparisons, the effective rate constants of other channels have been displayed in Table S7.†

As shown in Table 2, within the temperature range of 275-320 K, the effective rate constant of H<sub>2</sub>O···HO<sub>2</sub> + NH<sub>2</sub> reaction  $(k'_{t}(WM1a))$  is  $2.42 \times 10^{-12}$  to  $6.02 \times 10^{-12}$  cm<sup>3</sup> per molecule

per s, which is larger by 3 orders of magnitude than the corresponding value of  $HO_2 \cdots H_2O + NH_2$  reaction  $(k'_t(WM2))$ , as shown in Table S7.† Meanwhile, the value of  $k'_{t}(WM1a)$  is respectively larger by 23.5-46.0 and 1.17  $\times$  10<sup>10</sup> to 4.10  $\times$  10<sup>11</sup> times than the value of  $k'_{t}(WM3)$  (H<sub>2</sub>O···H<sub>2</sub>N + HO<sub>2</sub> reaction) and  $k'_{+}(WM4)$  (H<sub>2</sub>N···H<sub>2</sub>O + HO<sub>2</sub> reaction) listed in Table S7.† This indicates that the catalytic effect of water monomer is mainly taken from  $H_2O\cdots HO_2 + NH_2$  reaction.

For the catalytic effect of water dimer, the effective rate constant of  $HO_2 \cdots (H_2O)_2 + NH_2(k'_t(WD1))$  is 1.33  $\times 10^{-18}$  to  $4.43 \times 10^{-18}$  cm<sup>3</sup> per molecule per s, which is larger by 3-4 and 9-10 orders of magnitude than the corresponding value of  $HO_2 \cdots (H_2O)_2 - I$  $k'_{t}(WD2)$  $NH_2$ reaction  $NH_2\cdots(H_2O)_2 + HO_2(k'_t(WD3))$  listed in Table S7,† showing that the catalytic effect of water dimer is mainly taken from  $HO_2\cdots(H_2O)_2$  +  $NH_2$  reaction. Similarity, the catalytic effect of water trimer is mainly taken from  $HO_2 \cdots (H_2O)_3 + NH_2$  reaction  $(k'_{t}(WT1))$ , with the rate constant of  $k'_{t}(WT1)$  is larger by 10–11 orders of magnitude than the corresponding value of  $NH_2\cdots(H_2O)_3 + HO_2(k'_t(WT2))$  listed in Table S7.† Besides, the effective rate constant of  $HO_2 \cdots (H_2O)_2 + NH_2(k'_t(WD1))$  is larger by 6-10 times than the corresponding value of  $HO_2 \cdots (H_2O)_3 + NH_2(k'_t(WT1))$ . This shows that compared with water trimer, the catalytic effect of water dimer is not neglected. However, the value of  $k'_{t}(WD1)$  is smaller by 5-6 orders of magnitude than the effective rate constant of  $H_2O\cdots HO_2 + NH_2$ reaction  $(k'_{t}(WM1a))$ . So, the catalytic effect of single water is the largest among the effect of water, water dimer and water trimer, and the catalytic effect taken from water dimer and water trimer is neglected.

To obtain a more complete understanding of the influence of a water vapor on the title reaction, it is also necessary to compare the title rate constant  $(k_{R_1})$  in the absence of a water vapor with the effective rate constant of the most favorable channel of  $H_2O\cdots HO_2 + NH_2$  reaction  $(k'_t(WM1a))$ . The result in Table 2 is also estimated that within the temperature range of 275-320 K, the enhancement factor of water vapor  $(k'_{t}(WM1a)/k_{tot})$  is 10.06–13.30%, showing, in the whole calculated range, the positive water effect is obvious under atmospheric conditions.

Table 2 Effective rate constants (cm<sup>3</sup> per molecule per s) for the favorable channels of HO<sub>2</sub> + NH<sub>2</sub>  $\rightarrow$  NH<sub>3</sub> +  $^3$ O<sub>2</sub> reaction with (H<sub>2</sub>O)<sub>n</sub> (n = 1-3)<sup>a,b,c</sup>

T(K)	$k_{ m R_1}$	$k_{\mathrm{t}}^{\prime}(\mathrm{WM1a})$	$k_{\mathrm{t}}'(\mathrm{WD1})$	$k_{\mathrm{t}}'(\mathrm{WT1})$	$k_{\rm t}'({ m WM1a})/k_{ m tot}$
275	$5.50 \times 10^{-11}$	$6.02 \times 10^{-12}$	$1.33 \times 10^{-18}$	$1.40 \times 10^{-19}$	10.06%
280	$4.72 \times 10^{-11}$	$5.25  imes 10^{-12}$	$1.51  imes 10^{-18}$	$1.69 \times 10^{-19}$	10.24%
290	$3.52 \times 10^{-11}$	$4.20  imes 10^{-12}$	$2.05  imes 10^{-18}$	$2.60 \times 10^{-19}$	10.94%
298	$2.82  imes 10^{-11}$	$3.59  imes 10^{-12}$	$2.64  imes 10^{-18}$	$3.76 \times 10^{-19}$	11.64%
300	$2.68  imes 10^{-11}$	$3.36 \times 10^{-12}$	$2.77  imes 10^{-18}$	$4.05  imes 10^{-19}$	11.47%
310	$2.08  imes 10^{-11}$	$2.90  imes 10^{-12}$	$3.59  imes 10^{-18}$	$5.90 \times 10^{-19}$	12.64%
320	$1.64 \times 10^{-11}$	$2.42  imes 10^{-12}$	$4.43 \times 10^{-18}$	$7.99 \times 10^{-19}$	13.30%

<sup>&</sup>lt;sup>a</sup> Effective rate constants (cm<sup>3</sup> per molecule per s) of  $k'_t$ (WM1a) and  $k'_t$ (WD1), and  $k'_t$ (WT1) have been calculated using 100% relative humidity.  $^b$   $k_{\text{tot}} = k_{R_1} + k'_{\text{t}}(\text{WM}), k'_{\text{t}}(\text{WM1a}), k'_{\text{t}}(\text{WD1})$  and  $k'_{\text{t}}(\text{WT1})$  is respectively the effective rate constants of  $\text{H}_2\text{O} \cdot \text{HO}_2 + \text{NH}_2(\text{a}), \text{HO}_2 \cdot \cdot \cdot (\text{H}_2\text{O})_2 + \text{NH}_2(\text{a})}$ and  $HO_2 \cdots (H_2O)_3 + NH_2$  reaction.  ${}^c k_t'(WM1a) = k_b(WM1a)K_{eq}(H_2O \cdots HO_2)[H_2O]; k_t'(WD1) = k_b(WD1)K_{eq}(HO_2 \cdots (H_2O)_2)[(H_2O)_2];$  and  $k_{\mathsf{t}}'(\mathsf{WT1}) = k_{\mathsf{b}}(\mathsf{WT1}) K_{\mathsf{eq}}(\mathsf{HO}_2 \cdots (\mathsf{H}_2\mathsf{O})_3) [(\mathsf{H}_2\mathsf{O})_3]. \quad K_{\mathsf{eq}}(\mathsf{H}_2\mathsf{O} \cdots \mathsf{HO}_2), \quad K_{\mathsf{eq}}(\mathsf{HO}_2 \cdots (\mathsf{H}_2\mathsf{O})_2) \quad \text{and} \quad K_{\mathsf{eq}}(\mathsf{HO}_2 \cdots (\mathsf{H}_2\mathsf{O})_3) \quad \text{is respectively the equilibrium } K_{\mathsf{eq}}(\mathsf{HO}_2 \cdots (\mathsf{H}_2\mathsf{O})_3) = k_{\mathsf{eq}}(\mathsf{HO}_2 \cdots (\mathsf{H}_2\mathsf{O})_3) \quad \text{is respectively } K_{\mathsf{eq}}(\mathsf{HO}_2 \cdots (\mathsf{H}_2\mathsf{O})_3) = k_{\mathsf{eq}}(\mathsf{HO}_2 \cdots (\mathsf{H}_2$ constants for the formation of the H<sub>2</sub>O···HO<sub>2</sub>, HO<sub>2</sub>···(H<sub>2</sub>O)<sub>2</sub> and HO<sub>2</sub>···(H<sub>2</sub>O)<sub>3</sub> complexes, whereas [H<sub>2</sub>O], [(H<sub>2</sub>O)<sub>2</sub>], and [(H<sub>2</sub>O)<sub>3</sub>] are the concentrations of water vapor, water dimer and water trimer.65

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### 4. Summary and conclusions

The  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  reaction catalyzed by  $(H_2O)_n$  (n = 1-3) has been studied theoretically using quantum chemical methods and the canonical variational transition state theory, which results in the following conclusions:

- (a) Regarding to each type equilibrium structure of  $HO_2\cdots$   $(H_2O)_n$  (n=1-3) and  $H_2N\cdots(H_2O)_n$  (n=1-3), complexes of  $H_2O\cdots HO_2$ ,  $HO_2\cdots H_2O$ ,  $HO_2\cdots (H_2O)_2$ , and  $HO_2\cdots (H_2O)_3$  are the most stable configurations, which have larger stabilization energies and higher concentrations than their isomers, and thus  $(H_2O)_n$  (n=1-3) catalyzed  $HO_2+NH_2\rightarrow NH_3+^3O_2$  reactions are mainly occurring through four kinds of reactions of  $H_2O\cdots HO_2+NH_2$ ,  $HO_2\cdots H_2O+NH_2$ ,  $HO_2\cdots (H_2O)_2+NH_2$  and  $HO_2\cdots (H_2O)_3+NH_2$ .
- (b) For water-assisted  $HO_2 + NH_2 \rightarrow NH_3 + {}^3O_2$  reaction, the channel occurring through the  $H_2O\cdots HO_2 + NH_2$  reactants may be of great atmospheric relevance due to its larger effective rate constant and the larger concentration of  $H_2O\cdots HO_2$ . Besides, though  $HO_2\cdots H_2O + NH_2$  reaction has lower activation energy, its effective rate constant is smaller by 3 orders of magnitude than the corresponding value of  $H_2O\cdots HO_2 + NH_2$  reaction. So, the catalytic effect of water monomer is mainly taken from  $H_2O\cdots HO_2 + NH_2$  reaction.
- (c) For  $HO_2\cdots(H_2O)_2 + NH_2$  and  $HO_2\cdots(H_2O)_3 + NH_2$  reactions, both the reactions followed through a stepwise mechanism, where the reaction firstly occurred via a ring enlargement, and then proceed through a direct HA. However, the effective rate constant of  $H_2O\cdots(H_2O)_2 + NH_2(k'_t(WD1))$  is larger by 6-10 times than the corresponding value  $H_2O\cdots(H_2O)_3 + NH_2(k'_t(WT1))$ , showing that compared with water trimer, the catalytic effect of water dimer is not neglected. However, the effective rate constant of  $HO_2 \cdots (H_2O)_2 + NH_2$  is smaller by 5-6 orders of magnitude than that of H<sub>2</sub>O···HO<sub>2</sub> + NH<sub>2</sub> reaction, showing that the catalytic effect of single water is the largest among the effect of water, water dimer and water trimer, and the catalytic effect taken from water dimer and water trimer is neglected.
- (d) The enhancement factor of water vapor  $(k'_{\rm t}({\rm WM1a})/k_{\rm tot})$  is 10.06–13.30% within the temperature range of 275–320 K, showing that, in the whole calculated range, the positive water effect is obvious under atmospheric conditions.

### Conflicts of interest

The authors declare no conflicts of interest.

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