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# Predicting sulfur solubility in hydrogen sulfide, carbon dioxide, and methane with an improved thermodynamic model

Changjun Li,<sup>a</sup> Gang Liu <sup>\*a</sup> and Yang Peng<sup>b</sup>

During development of high sulfur-content natural gas fields, gaseous sulfur is likely to precipitate and deposit in the reservoir and transmission pipelines owing to changes in the temperature, pressure, and gas components. It is important to accurately predict the elemental sulfur solubility in hydrogen sulfide, carbon dioxide, and methane because these are the three main components of high-sulfur-content natural gas. The binary interaction coefficients between sulfur and hydrogen sulfide, carbon dioxide, and methane are the key parameters for predicting the sulfur solubility with a thermodynamic model. In this work, we show that the binary interaction coefficients are not constant, but temperature dependent. Three-parameter temperature-dependent equations for the binary interaction coefficients between sulfur and solvents are proposed. The corresponding regression equations for calculating the binary interaction coefficients between sulfur and hydrogen sulfide, carbon dioxide, and methane are obtained using experimental sulfur solubility data. The average relative errors of the sulfur solubility predicted using the experimental data in hydrogen sulfide, carbon dioxide, and methane using the thermodynamic model with the improved binary interaction coefficients are 6.30%, 1.69%, and 4.34%, and the average absolute relative errors are 7.90%, 13.12%, and 14.98%, respectively. Comparing the improved binary interaction coefficients with four other sets of reported values shows that the solubility values predicted by the thermodynamic model with improved binary interaction coefficients fit the experimental data better.

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## 1. Introduction

High-sulfur-content natural gas contains hydrogen sulfide, mercaptans, sulfoethers, and other sulfurous substances, with hydrogen sulfide gas comprising the majority of all sulfurous substances. There are many high-sulfur-content gas fields. For example, the hydrogen sulfide volume contents in natural gas mixtures are 15% to 18% in the Puguang Gas Field (China).<sup>1</sup> High-sulfur-content natural gas fields supply not only clean energy, but also raw materials for sulfur series products.<sup>2</sup> However, deposited elemental sulfur may cause pore formation, wellbore blockage, and even transmission pipeline blockage and corrosion with changes in pressure, temperature, and gas components.<sup>3–5</sup> This can lead to the normal production of the gas field being severely inhibited.<sup>6–9</sup> In recent years, the problem of sulfur deposition has received extensive attention. Notably, elemental sulfur solubility in high-sulfur-content natural gas is the key factor determining whether sulfur deposition occurs.<sup>10–12</sup>

Many researchers have measured the sulfur solubility in hydrogen sulfide (H<sub>2</sub>S), carbon dioxide (CO<sub>2</sub>), and methane (CH<sub>4</sub>), because high-H<sub>2</sub>S-content natural gas mainly comprises these three gas components. Kennedy and Wieland<sup>3</sup> were the first to measure elemental sulfur solubility in pure H<sub>2</sub>S, CO<sub>2</sub>, CH<sub>4</sub> and their mixtures in 1960. Their work showed that elemental sulfur solubility increases with increasing pressure and temperature. Roof found that the solubility in H<sub>2</sub>S first increases and then decreases with increasing temperature.<sup>13</sup> Swift, Brunner, and Gu *et al.* extended the pressure and temperature range for sulfur solubility in H<sub>2</sub>S.<sup>14–16</sup> Serin *et al.* developed an experimental apparatus for measuring elemental sulfur solubility in CO<sub>2</sub>.<sup>17</sup> Using the same experimental apparatus, Cloarec *et al.*<sup>18</sup> obtained experimental data of sulfur solubility in CH<sub>4</sub>.

The above experimental results of solubility in H<sub>2</sub>S, CO<sub>2</sub>, and CH<sub>4</sub> provide the basis for establishing a solubility predicting model, and strongly support the development of high-sulfur-content natural gas fields.<sup>19–24</sup> The binary interaction coefficients between sulfur and H<sub>2</sub>S, CO<sub>2</sub>, and CH<sub>4</sub> in natural gas are important parameters when using a thermodynamic predicting model based on the equation of state (EoS). As shown in Table 1, Heidemann<sup>25</sup> reported that the binary interaction coefficients between sulfur and H<sub>2</sub>S, CO<sub>2</sub>, or CH<sub>4</sub> after regression of the experimental data were 0.0812, 0.135, and 0.155, respectively.<sup>25</sup> In Sun's model,<sup>26</sup> the binary interaction coefficients between

<sup>a</sup>School of Petroleum Engineering, Southwest Petroleum University, Chengdu 610500, China. E-mail: [sci-tech@hotmail.com](mailto:sci-tech@hotmail.com); Tel: +86 132 2817 0900

<sup>b</sup>Gas Management Office, PetroChina Southwest Oil & Gas Field Company, Chengdu 610215, China



Table 1 The binary interaction coefficient values

Comp.	Binary interaction coefficient $k_{ij}$							Author
S <sub>8</sub> -H <sub>2</sub> S	0.0812							Heidemann R. A. <sup>25</sup> Sun C. Y. <sup>26</sup> Cézac P. <sup>27</sup>
	0.0758							
	0.093–2.079/ <i>T</i>							
	316.3 K	338.7 K	366.5 K	374.8 K	373.2 K	363.2 K	383.2 K	Gu M. X. <sup>16</sup>
0.1111	0.1112	0.1042	0.1062	0.1038	0.1033	0.0892		
S <sub>8</sub> -CO <sub>2</sub>	0.135							Heidemann R. A. <sup>25</sup> Sun C. Y. <sup>26</sup> Cézac P. <sup>27</sup>
	0.190							
	0.2423–21.44/ <i>T</i>							
	363.2 K						383.2 K	Gu M. X. <sup>16</sup>
0.2107						0.1993		
S <sub>8</sub> -CH <sub>4</sub>	0.155							Heidemann R. A. <sup>25</sup> Sun C. Y. <sup>26</sup> Cézac P. <sup>27</sup>
	0.115							
	1.154–377/ <i>T</i>							
	0.1345							Gu M. X. <sup>16</sup>

sulfur and H<sub>2</sub>S, CO<sub>2</sub>, and CH<sub>4</sub> are 0.0758, 0.190, and 0.115, respectively. However, Gu<sup>16</sup> and Cézac *et al.*<sup>27</sup> suggested that the binary interaction coefficients are related to the gas mixture temperature. Based on the experimental data of Roof, Brunner, and their own work, Gu<sup>16</sup> reported binary interaction coefficients between sulfur and H<sub>2</sub>S, CO<sub>2</sub>, and CH<sub>4</sub> of 316.3–374.8 K, 363.2 and 383.2 K, and 383.2 K, respectively. Cézac *et al.*<sup>27</sup> proposed three equations for calculating the binary interaction coefficients between sulfur and H<sub>2</sub>S, CO<sub>2</sub>, and CH<sub>4</sub> based on analysis of experimental data. The binary interaction coefficients from the above studies are considerably different, and it is unclear which set represents better experimental data.

This work aims to evaluate differences in the binary interaction coefficients between sulfur and H<sub>2</sub>S, CO<sub>2</sub>, and CH<sub>4</sub>. We investigated the relationships between the binary interaction coefficients and temperature to extend the range and improve the accuracy of predicting the sulfur solubility in H<sub>2</sub>S, CO<sub>2</sub>, and CH<sub>4</sub> using a thermodynamic model based on the Peng–Robinson (PR) EoS. Based on experimental data analysis, new three-parameter temperature-dependent equations for calculating the binary interaction coefficients are proposed. The equation parameters are obtained by regression analysis of the experimental data. Furthermore, we compared the solubility results calculated using the thermodynamic model with the binary interaction coefficients reported by Heidemann, Sun, Cézac, Gu, and in this work.

## 2. Model description

### 2.1. Governing equations

The model is based on thermodynamic gas–solid phase equilibrium theory, which assumes perfect mixing of the sulfur and gas components. As mentioned by Gu, Sun, and Heidemann, solid sulfur should be treated as single molecule S<sub>8</sub>.<sup>16,25,26</sup> The phase equilibrium condition of the gas–solid system requires the fugacity of gaseous sulfur to be the same as that of the solid phase, as expressed by eqn (1):<sup>28</sup>

$$f_{S_8}^S(T, P) = f_{S_8}^V(T, P, y) \quad (1)$$

### 2.2. Solid phase fugacity

The solid sulfur fugacity is related to the saturation vapor pressure of solid sulfur, as expressed by eqn (2):<sup>28</sup>

$$f_{S_8}^S(T, P) = \phi_{S_8}^{\text{sat}} P_{S_8}^{\text{sat}} \exp \frac{V_{S_8}^S (P - P_{S_8}^{\text{sat}})}{RT} \quad (2)$$

The sulfur saturation vapor pressure is always small in the gas–solid phase equilibrium system, so  $\phi_{S_8}^{\text{sat}} = 1.0$  in this model.<sup>28</sup> Shuai and Meisen<sup>29</sup> reported regression equations of the sulfur saturation vapor pressure at different temperatures.

When  $T < 368$  K,  $P_{S_8}^{\text{sat}}$  is expressed by eqn (3):

$$\ln P_{S_8}^{\text{sat}} = -37.566 + 0.1003T \quad (3)$$

When  $T > 368$  K,  $P_{S_8}^{\text{sat}}$  is expressed by eqn (4):

$$\ln P_{S_8}^{\text{sat}} = -30.736 + 0.0816T \quad (4)$$

$$V_{S_8}^S = \frac{M}{\rho} = \frac{32.064 \times 8 \text{ g mol}^{-1}}{2070 \text{ kg m}^{-3}} = 1.2392 \times 10^{-4} \text{ m}^3 \text{ mol}^{-1} \quad (5)$$

Using eqn (2)–(5), we can calculate the fugacity of sulfur in solid phase.

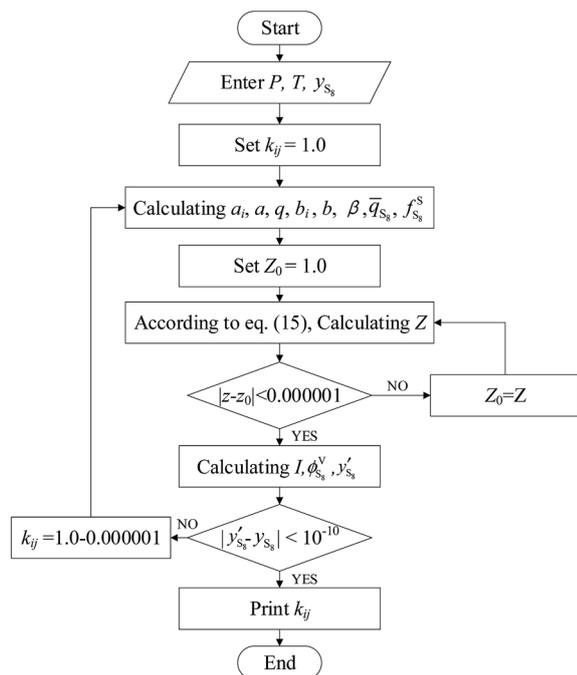
### 2.3. Elemental sulfur fugacity in the gas phase

The elemental sulfur fugacity in the gas phase can be expressed with eqn (6):<sup>28</sup>

Table 2 Critical parameters and acentric factors

Component	Critical pressure (MPa)	Critical temperature (K)	Acentric factor
S <sub>8</sub>	5.2	1065.0	0.3805
H <sub>2</sub> S	8.963	373.5	0.094
CO <sub>2</sub>	7.383	304.2	0.224
CH <sub>4</sub>	4.599	190.6	0.012



Fig. 1 Calculating diagram of  $k_{S_8j}$ .

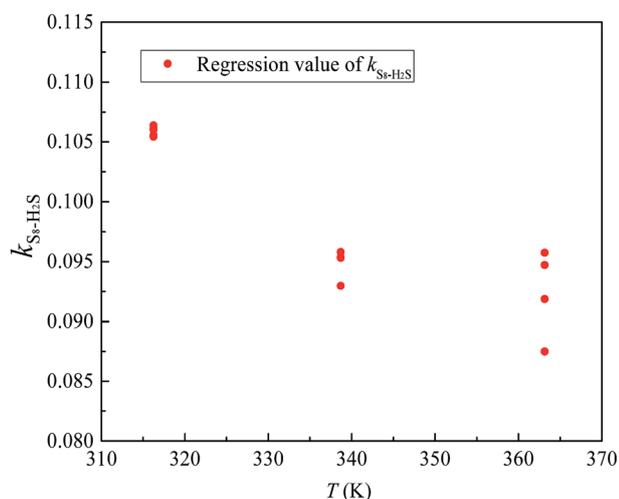
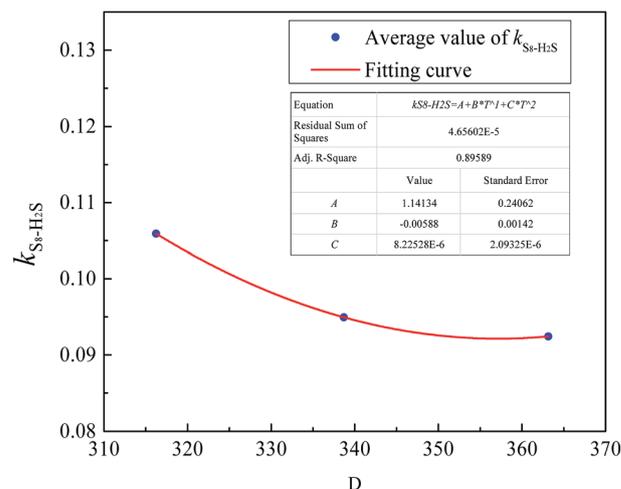
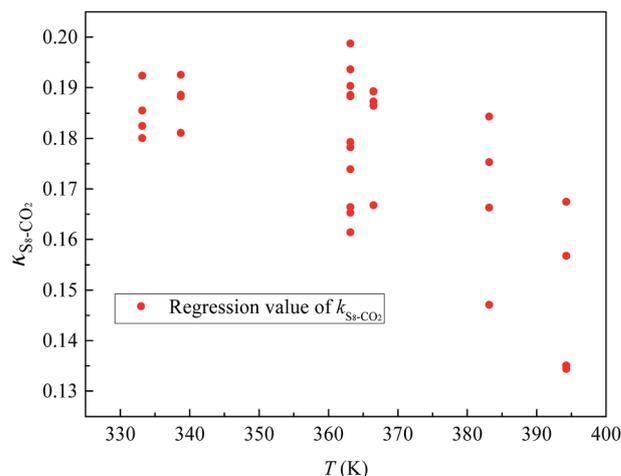
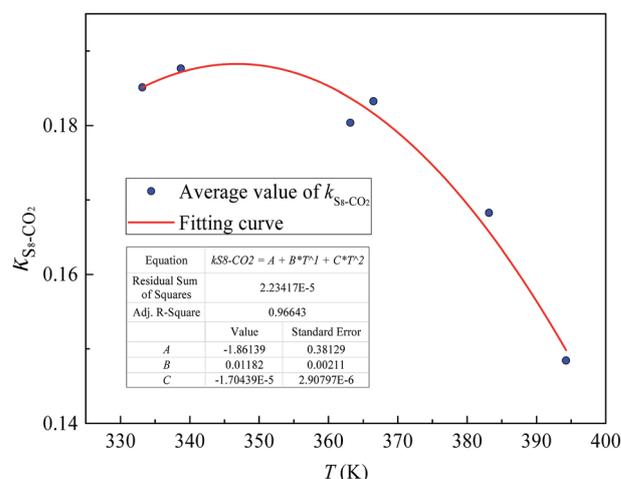
$$f_{S_8}^V(T, P, y) = y_{S_8} \phi_{S_8}^V P \quad (6)$$

**2.3.1. Peng–Robinson (PR) EoS.** According to eqn (6),  $\phi_{S_8}^V$  is the key parameter for calculating the gaseous sulfur fugacity, and can be described by the PR EoS. The basic form of the PR EoS is shown in eqn (7):<sup>30</sup>

$$P = \frac{RT}{V-b} - \frac{a}{V(V+b) + b(V-b)} \quad (7)$$

where  $a$  and  $b$  are the parameters of PR EoS. When gas mixtures are single component,  $a$  and  $b$  can be expressed as follows:

$$a = 0.45724 \frac{R^2 T_c^2}{P_c} \alpha \quad (8)$$

Fig. 2 The  $k_{ij}$  between  $S_8$  and  $H_2S$ .Fig. 3 The  $k_{ij}$  fitting curve between  $S_8$  and  $H_2S$ .Fig. 4 The  $k_{ij}$  between  $S_8$  and  $CO_2$ .Fig. 5 The  $k_{ij}$  fitting curve between  $S_8$  and  $CO_2$ .

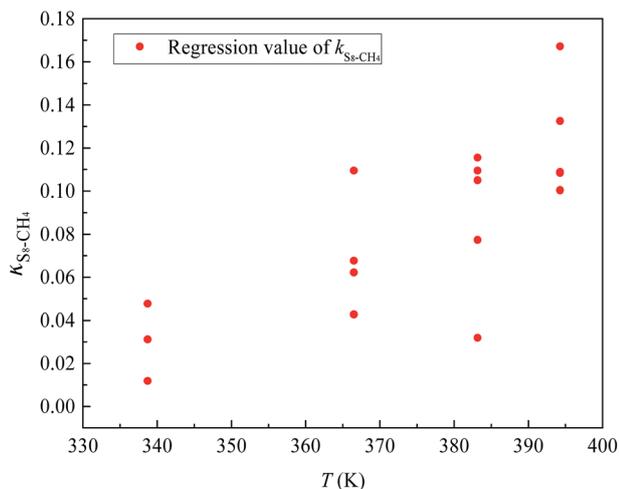


Fig. 6 The  $k_{ij}$  between  $S_8$  and  $CH_4$ .

$$b = 0.07780 \frac{RT_c}{P_c} \quad (9)$$

$$\alpha = [1 + (1 - T_r^{0.5})(0.37464 + 1.54226\omega - 0.26992\omega^2)]^2 \quad (10)$$

$$T_r = \frac{T}{T_c} \quad (11)$$

Table 2 shows the critical parameters and acentric factors of  $S_8$ ,  $H_2S$ ,  $CO_2$ , and  $CH_4$ .<sup>27,28</sup>

After the solid and gas phase sulfur reach the equilibrium state, the gas phase is composed of a solvent gas component and gaseous sulfur. The  $a$  and  $b$  parameters need be calculated using the mixing rule according to the values of the single components. In this model,  $b$  is calculated by the classic mixing rule, as follows:

$$b = \sum_{i=1}^n y_i b_i \quad (12)$$

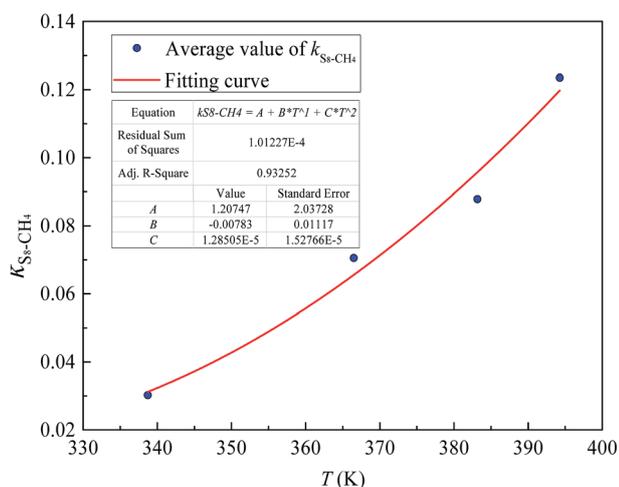


Fig. 7 The  $k_{ij}$  fitting curve between  $S_8$  and  $CH_4$ .

Table 3 Deviation comparisons of predicting solubility in  $CO_2$  with different  $k_{S_8-CO_2}$

Deviation	Improved $k_{S_8-CO_2}$	$k_{S_8-CO_2}$		0.2423– 21.44/T	
		0.190	0.135		
ARE (%)	1.69	-14.57	111.32	-34.20	-3.11
AARE (%)	13.12	16.38	111.36	34.20	18.22

The  $a$  parameter of the gas mixture components will be discussed in detail in Section 3.

The fugacity coefficient of gaseous sulfur  $\phi_{S_8}^V$  can be expressed as:

$$\ln \phi_{S_8}^V = \frac{b_{S_8}}{b} (Z - 1) - \ln(Z - \beta) - \bar{q}_{S_8} I \quad (13)$$

where

$$b_{S_8} = 0.07780 \times R \frac{T_{cS_8}}{P_{cS_8}} \quad (14)$$

$Z$  is calculated using

$$Z = 1 + \beta - q\beta \frac{Z - \beta}{[Z + (1 - \sqrt{2})\beta][Z + (1 + \sqrt{2})\beta]} \quad (15)$$

Relevant parameters in eqn (15) are expressed by eqn (16)–(19):

$$\beta = \frac{bP}{RT} \quad (16)$$

$$q = \frac{a}{bRT} \quad (17)$$

$$\bar{q}_{S_8} = q \left[ \frac{2 \sum_j y_j a_{jS_8}}{a} - \frac{b_{S_8}}{b} \right] \quad (18)$$

$$I = \frac{1}{2\sqrt{2}} \ln \left[ \frac{Z + (1 + \sqrt{2})\beta}{Z + (1 - \sqrt{2})\beta} \right] \quad (19)$$

In this work, this equation was solved using the Newton-Raphson method. The elemental sulfur solubilities in  $H_2S$ ,  $CO_2$ , and  $CH_4$  can be calculated easily using eqn (1)–(19).

Table 4 Deviation comparisons of predicting solubility in  $CH_4$  with different  $k_{S_8-CH_4}$

Deviation	Improved $k_{S_8-CH_4}$	$k_{S_8-CH_4}$			1.154– 377/T
		0.115	0.155	0.1345	
ARE (%)	4.34	-20.08	-40.70	-26.58	-33.04
AARE (%)	14.98	25.23	41.66	26.58	34.07



### 3. Proposed method

The classical mixing rule for  $a$  is:<sup>28</sup>

$$a = \sum_{i=1}^n \sum_{j=1}^n y_i y_j (a_i a_j)^{0.5} (1 - k_{ij}) \quad (20)$$

where  $k_{ij}$  are the binary interaction coefficients between  $S_8$  and the gas solvents ( $H_2S$ ,  $CO_2$ , and  $CH_4$ ). Eqn (20) shows that  $k_{ij}$  are important parameters.

The reported binary interaction coefficients between  $S_8$  and  $H_2S$ ,  $CO_2$ , and  $CH_4$  obtained by regression of the sulfur solubility experimental data are shown in Table 1. The binary interaction coefficients reported by Sun and Heidemann are constant.<sup>25,26</sup> However, as mentioned by Gu<sup>16</sup> and Cézac,<sup>27</sup> the binary interaction coefficients are temperature dependent. Therefore, we proposed a new mixing rule for  $a$  to calculate the gaseous  $S_8$  fugacity:

$$a = \sum_{i=1}^n \sum_{j=1}^n y_i y_j (a_i a_j)^{0.5} [1 - (A + BT + CT^2)] \quad (21)$$

Therefore,

$$k_{ij} = A + BT + CT^2 \quad (22)$$

The  $k_{ij}$  values with temperature were regressed based on the experimental data of Kennedy, Roof, Brunner, Serin, and Gu,<sup>3,13,15–17</sup> and the calculated diagram is shown in Fig. 1.

According to Eslamimanesh's study of the consistency of the experimental results of sulfur solubility in  $H_2S$ , only ~45% of the values are reliable.<sup>20</sup> To obtain an equation for the binary interaction coefficient between sulfur and  $H_2S$ , we chose the 14 sets of experimental data at temperatures of 316.26, 338.71, and 363.15 K reported by Roof and Gu.<sup>13,16</sup> Fig. 2 shows the binary interaction coefficient between  $S_8$  and  $H_2S$  calculated at temperatures of 316.26–363.15 K. To better fit the  $k_{ij}$  value, we obtained the average  $k_{ij}$  values at the same temperatures shown in Fig. 3, and a new equation and fitting curve of  $k_{S_8-H_2S}$  with temperature were obtained. The adjusted  $R^2$  value ( $R_{adj}^2$ ) was 0.896, which showed that the fitting precision was high. The new equation for the binary interaction coefficient between  $S_8$  and  $H_2S$  is:

$$k_{S_8-H_2S} = 1.14134 - 0.00588T + 8.22528 \times 10^{-6}T^2 \quad (23)$$

Fig. 4 and 5 show the new equation and fitting curve for  $k_{S_8-CO_2}$  in the temperature range 333.15–394.26 K ( $R_{adj}^2 = 0.966$ ). The new equation for the binary interaction coefficient between  $S_8$  and  $CO_2$  is:

$$k_{S_8-CO_2} = -1.86139 + 0.01182T - 1.70439 \times 10^{-5}T^2 \quad (24)$$

Fig. 6 and 7 show the new equation and fitting curve for  $k_{S_8-CH_4}$  in the temperature range 338.71–394.26 K ( $R_{adj}^2 = 0.933$ ). The new equation for the binary interaction coefficient between  $S_8$  and  $CH_4$  is:

$$k_{S_8-CH_4} = 1.20747 - 0.00783T + 1.28505 \times 10^{-5}T^2 \quad (25)$$

### 4. Results and discussion

#### 4.1. Predicting the sulfur solubility using the proposed binary interaction coefficients

The sulfur solubility in  $H_2S$  predicted by the thermodynamic model using the proposed binary interaction coefficient between sulfur and  $H_2S$  obtained by eqn (23) is shown in Table 5, along with the experimental results of Roof and Gu at temperatures of 316.26, 338.71, and 363.15 K and in the pressure range 7.03–32.03 MPa.<sup>13,16</sup> Parameter  $a$  in this model was calculated with the proposed mixing rule (eqn (21)) and (23).

There are 14 sets of experimental data in Table 5. The RE, ARE, and AARE values were calculated using eqn (26)–(28):

$$RE = \frac{Z_i^{pred} - Z_i^{exp}}{Z_i^{exp}} \quad (26)$$

$$ARE\% = \frac{100}{N} \sum_{i=1}^N \left( \frac{Z_i^{pred} - Z_i^{exp}}{Z_i^{exp}} \right) \quad (27)$$

$$AARE\% = \frac{100}{N} \sum_{i=1}^N \left( \left| \frac{Z_i^{pred} - Z_i^{exp}}{Z_i^{exp}} \right| \right) \quad (28)$$

Based on Table 5, the total ARE and AARE values for predicting the sulfur solubility were 6.30% and 7.90%, respectively.

Fig. 8 and 9 show the ARE and AARE values of sulfur solubility in  $H_2S$  calculated from the experimental data at three different temperatures (316.26, 338.71, and 363.15 K). Fig. 8 shows that the ARE values were positive at temperatures of 316.26, 338.71, and 363.15 K. The lowest ARE value was 5.69% at 316.26 K, with a highest ARE value of 7.64% at 363.15 K. Fig. 9 shows that the greatest AARE value was 12.61% at 363.15 K. The

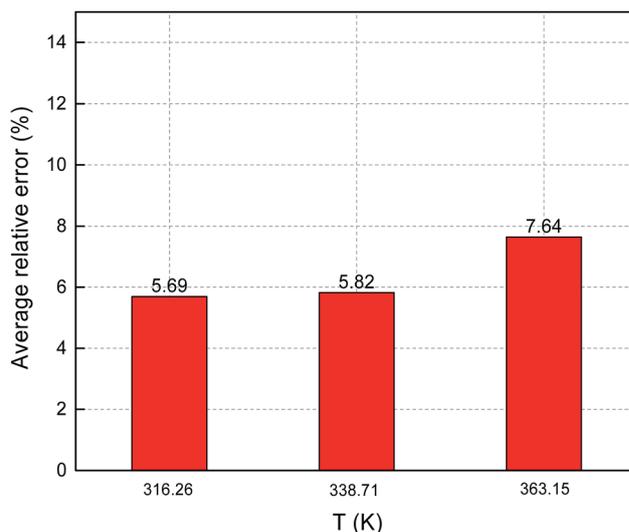
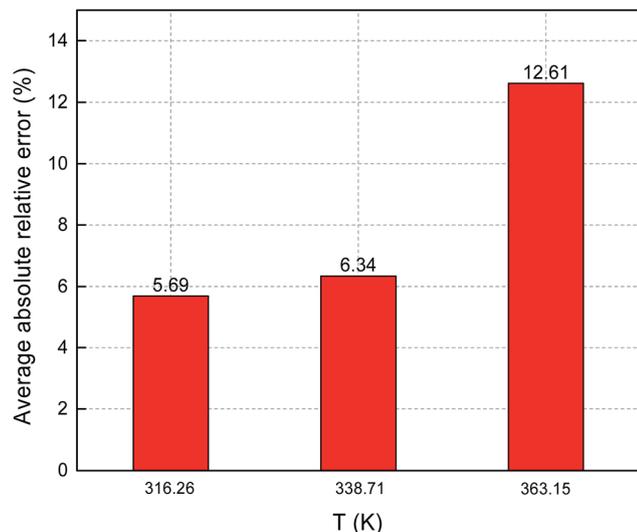
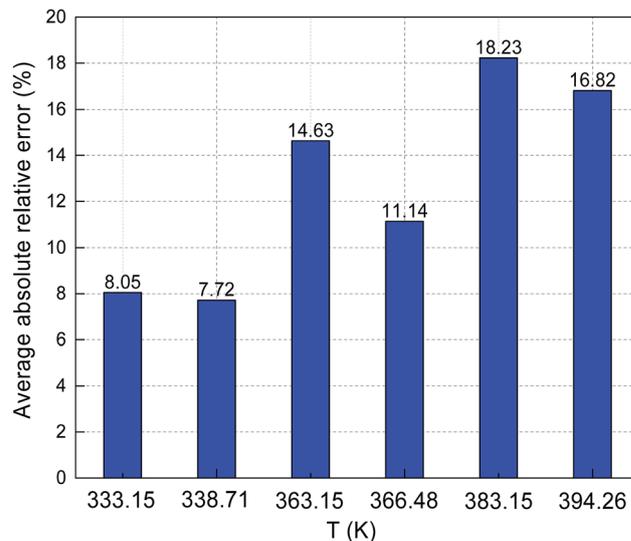
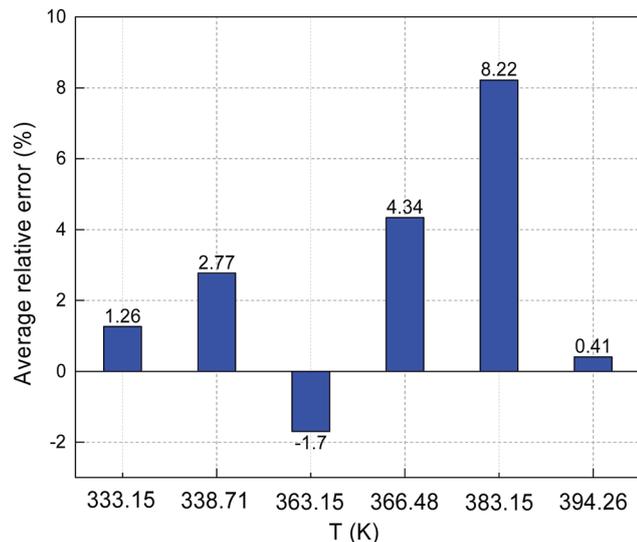


Fig. 8 ARE of sulfur solubility in  $H_2S$ .



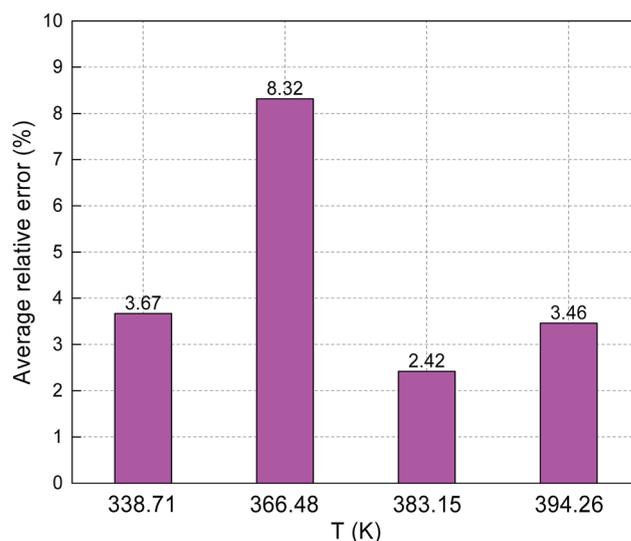
Fig. 9 AARE of sulfur solubility in H<sub>2</sub>S.Fig. 11 AARE of sulfur solubility in CO<sub>2</sub>.Fig. 10 ARE of sulfur solubility in CO<sub>2</sub>.

other AARE values were all below 7%. Considering the critical temperature of H<sub>2</sub>S (373.5 K), the large deviation at 363.15 K could be due to the kinetic characteristics of the solvent molecule (H<sub>2</sub>S) being influenced by external factors near the critical temperature and pressure.<sup>16</sup>

The predicted sulfur solubility in CO<sub>2</sub> using the proposed binary interaction coefficient, along with the experimental data of Kennedy, Gu, and Serin, in the temperature range 333.15–394.26 K at pressures of 15.1–41.4 MPa are shown in Table 6.<sup>3,16,17</sup> Parameter  $a$  with the proposed mixing rule (eqn (21)) was calculated using eqn (24). There were 32 sets of experimental data included in Table 6. Based on these calculated results, the total ARE and AARE values of the predicted sulfur solubility in CO<sub>2</sub> were 1.69% and 13.12%, respectively. Fig. 10 and 11 show the ARE and AARE values of sulfur solubility

in CO<sub>2</sub> calculated using the experimental data for six temperature ranges from 333.15–394.26 K. The lowest ARE value was 0.41% at 394.26 K, and the highest ARE value was 8.22% at 383.15 K (Fig. 10). Fig. 11 shows that the highest AARE value was 18.23% at 383.15 K.

The predicted sulfur solubility in CH<sub>4</sub> using the proposed binary interaction coefficient, along with the experimental data of Kennedy and Gu in the temperature range 338.71–394.26 K and pressures range 6.89–41.4 MPa, are shown in Table 7.<sup>3,16</sup> Parameter  $a$  with the proposed mixing rule (eqn (21)) was calculated with eqn (25). There are 17 sets of experimental data in Table 7. Based on the calculated results in Table 7, the total ARE and AARE values calculated with eqn (27) and (28) were 4.34% and 14.98%, respectively. Fig. 12 and 13 show the ARE and AARE values of sulfur solubility in CH<sub>4</sub> calculated using the

Fig. 12 ARE of sulfur solubility in CH<sub>4</sub>.

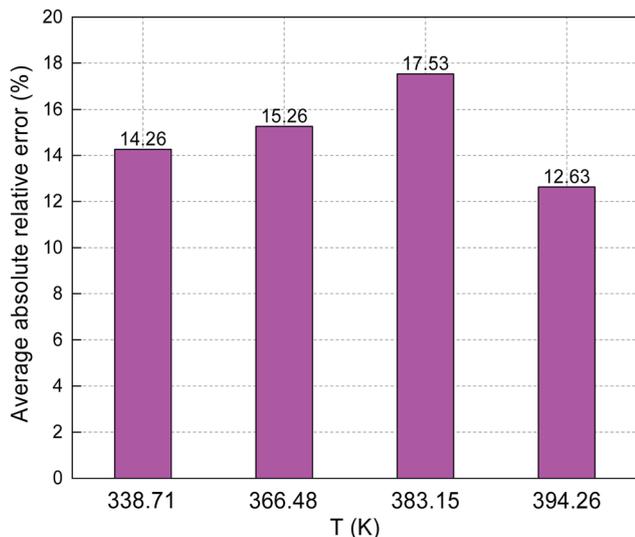


Fig. 13 AARE of sulfur solubility in  $\text{CH}_4$ .

experimental data for four temperatures in the range 338.71–394.26 K. Fig. 12 shows that the lowest ARE value was 2.42% at 383.15, while the highest ARE value was 8.32% at 366.48 K. The highest AARE value was 17.53% at 383.15 K (Fig. 13). Combined with the results of the calculated sulfur solubilities in  $\text{CO}_2$  and  $\text{CH}_4$ , the main reason for the large deviation could be that the solubility values in  $\text{CO}_2$  and  $\text{CH}_4$  are too small.

## 4.2. Comparison of binary interaction coefficients

**4.2.1. Comparison of sulfur solubility in  $\text{H}_2\text{S}$  with different  $k_{\text{S}_8-\text{H}_2\text{S}}$ .** As mentioned above, Sun and Heidemann suggested that  $k_{\text{S}_8-\text{H}_2\text{S}}$  is temperature independent.<sup>15,16</sup> However, Gu and Cézac *et al.* suggested that  $k_{\text{S}_8-\text{H}_2\text{S}}$  is temperature dependent.<sup>16,27</sup> Gu determined  $k_{\text{S}_8-\text{H}_2\text{S}}$  values at different temperatures from 316.3 to 383.2 K based on experimental data, and Cézac proposed a temperature-dependent  $k_{\text{S}_8-\text{H}_2\text{S}}$  equation.<sup>16,27</sup> Here, we compared the sulfur solubilities predicted using these different  $k_{\text{S}_8-\text{H}_2\text{S}}$  values with our proposed  $k_{\text{S}_8-\text{H}_2\text{S}}$  model (eqn (23)). Fig. 14

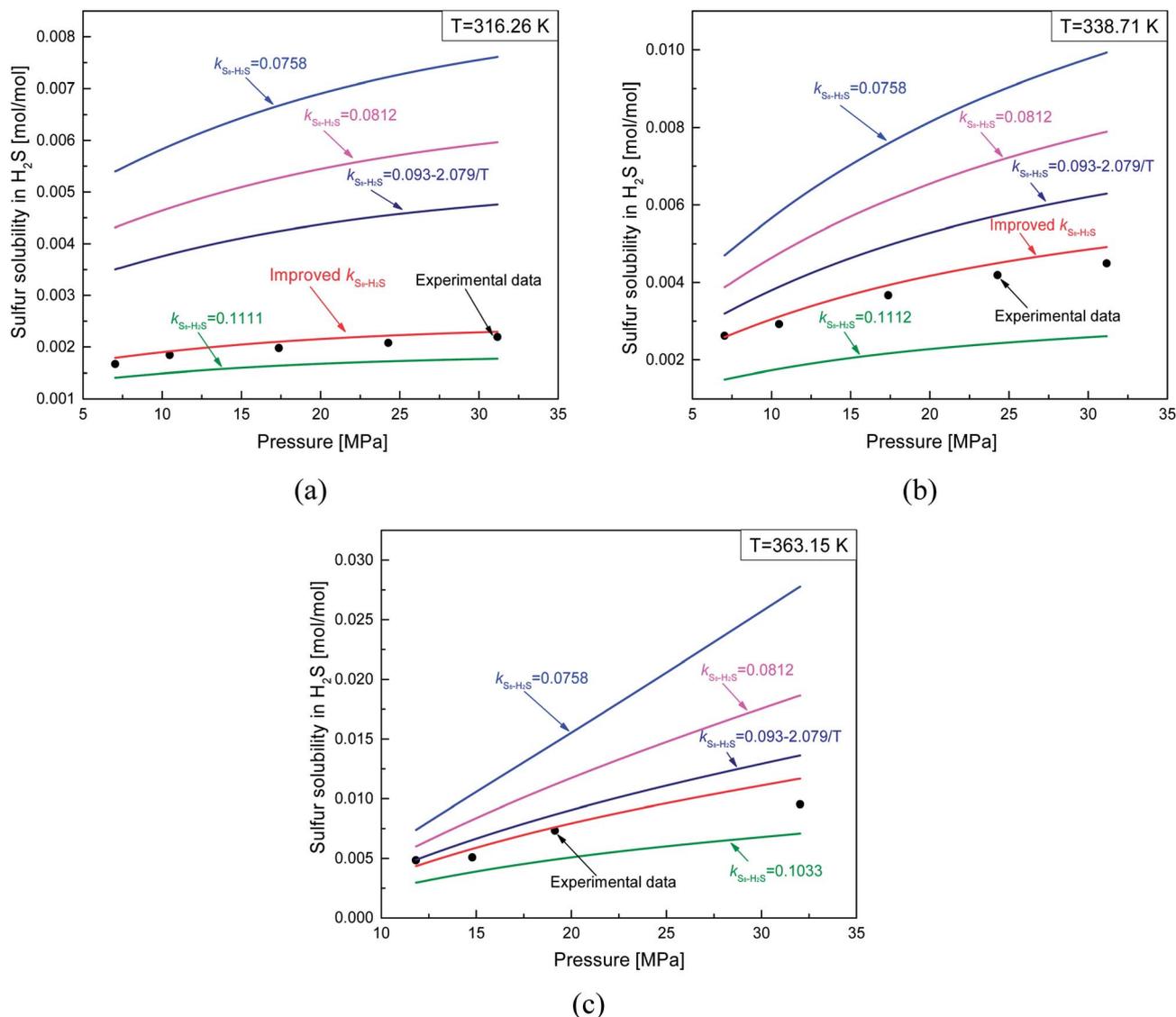
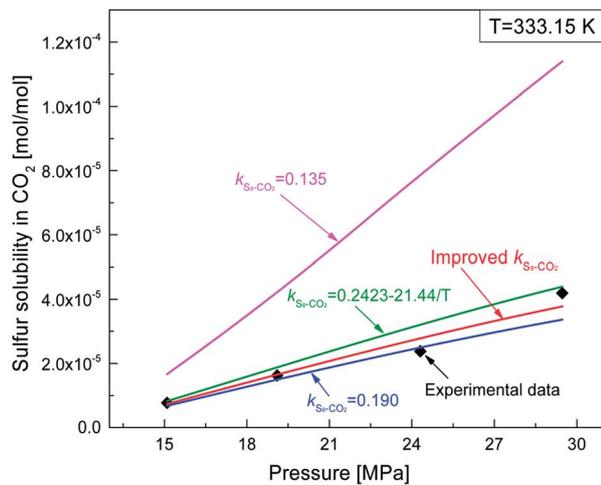
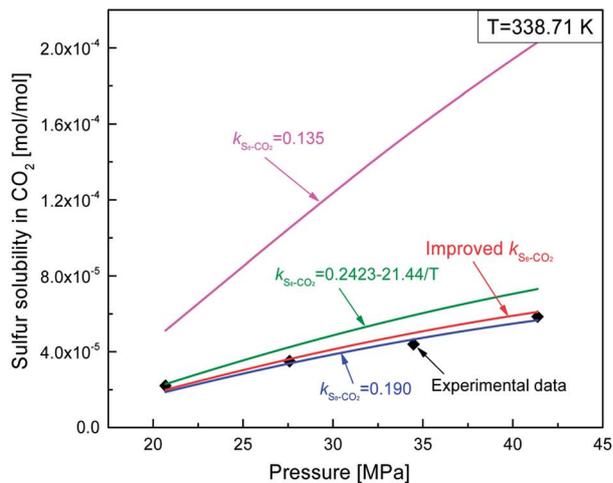


Fig. 14 Comparisons of predicting sulfur solubility in  $\text{H}_2\text{S}$  with different  $k_{\text{S}_8-\text{H}_2\text{S}}$ .

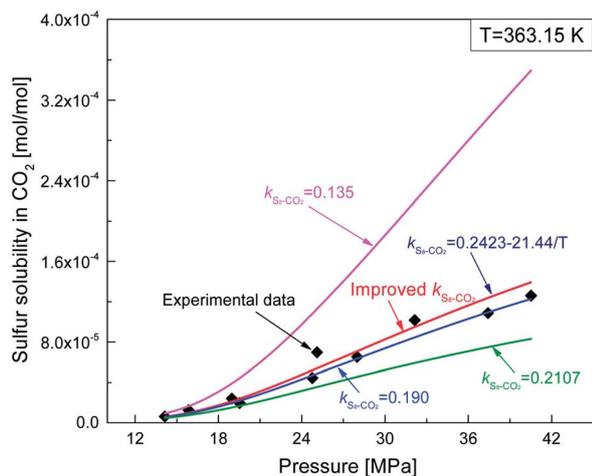




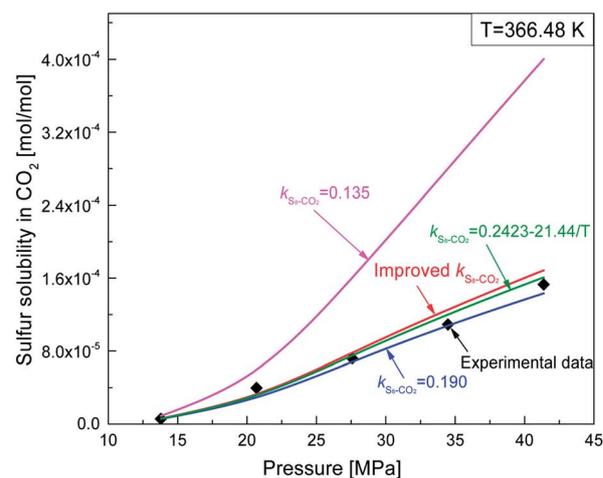
(a)



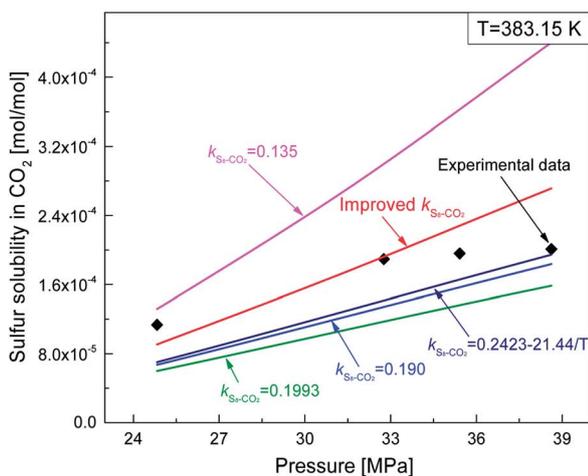
(b)



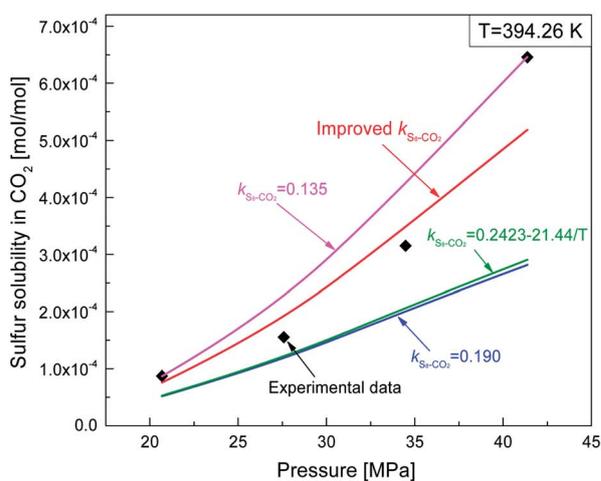
(c)



(d)



(e)



(f)

Fig. 15 Comparisons of predicting sulfur solubility in  $\text{CO}_2$  with different  $k_{\text{Sr}-\text{CO}_2}$ .



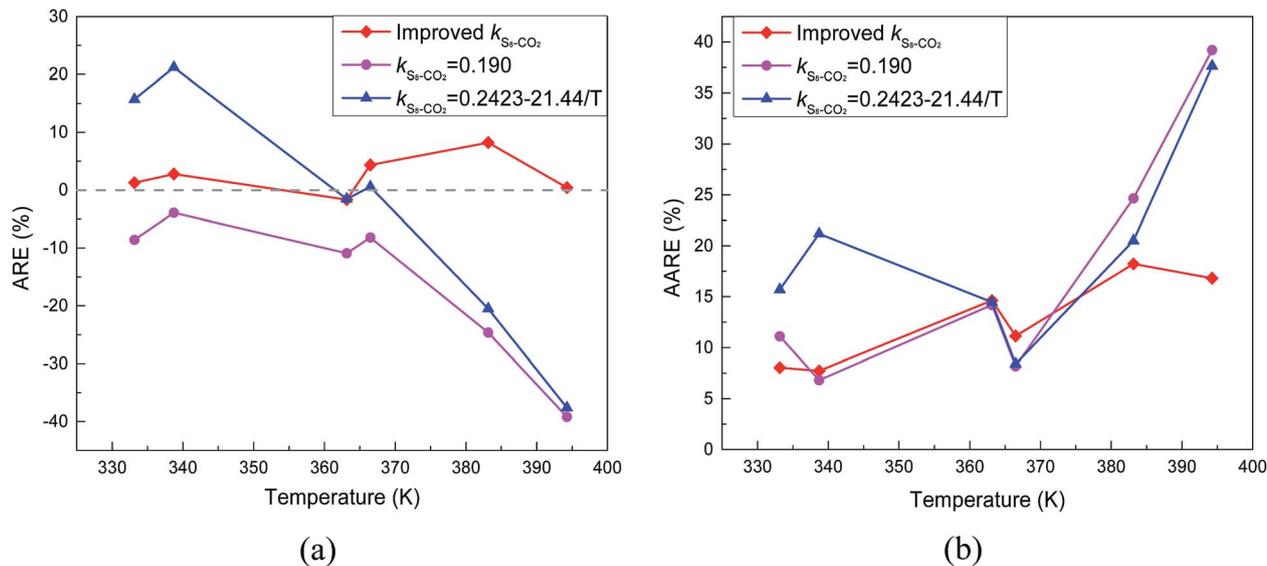


Fig. 16 The deviation of predicting solubility in CO<sub>2</sub> with different  $k_{Sg-CO_2}$ .

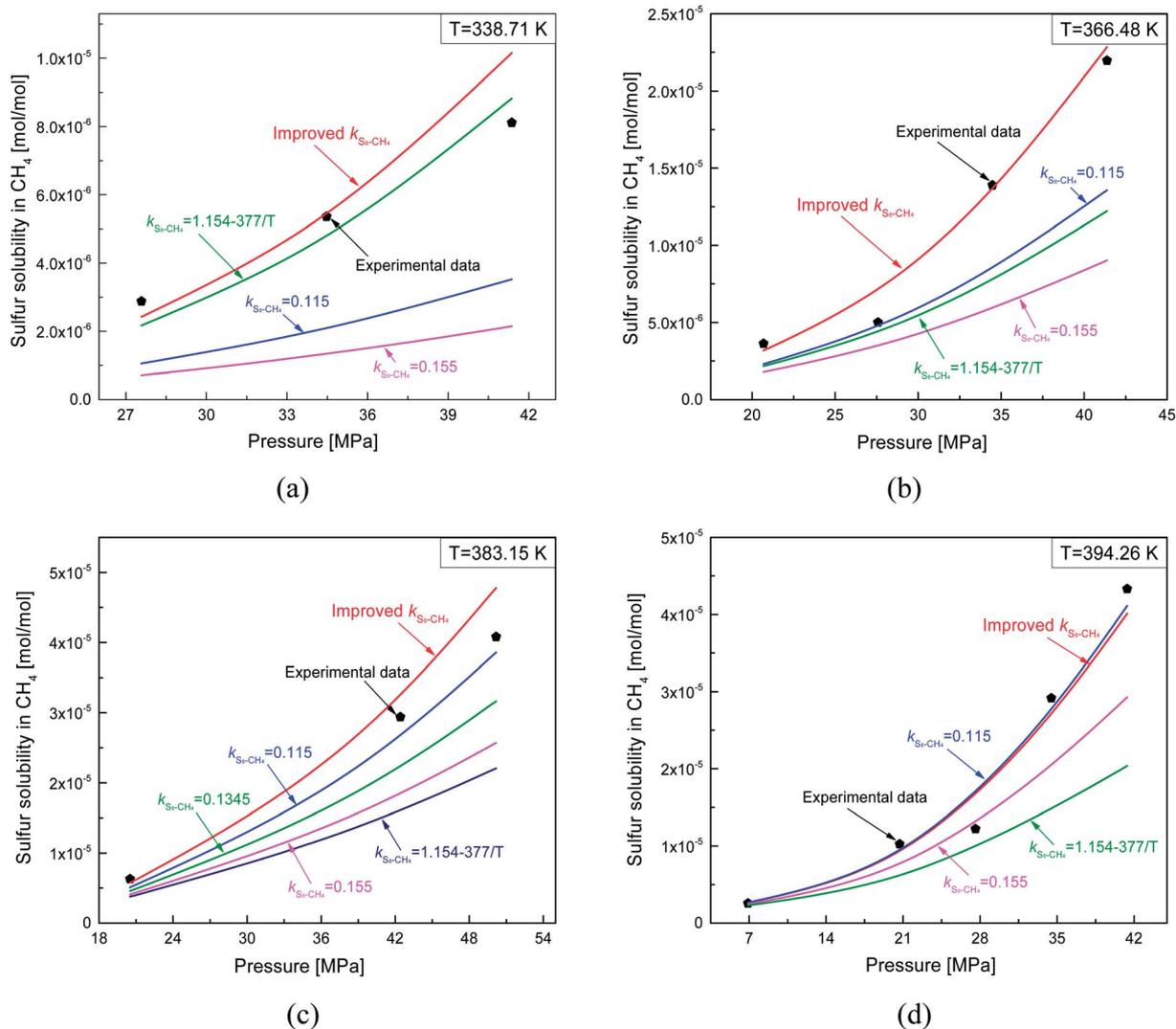


Fig. 17 Comparisons of predicting sulfur solubility in CH<sub>4</sub> with different  $k_{Sg-CH_4}$ .



shows that the accuracy of the predicted sulfur solubility in H<sub>2</sub>S with the proposed  $k_{S_8-H_2S}$  was significantly higher than those of the other four  $k_{S_8-H_2S}$  values. At 316.26 K, the value proposed by Gu was more reasonable than the three other values. The deviation in the solubility calculated with the thermodynamic model and the experimental data was relatively large using the values reported by Sun, Heidemann, and Cézac. The three values also showed that the predicted solubility was closely related to the binary interaction coefficient between sulfur and H<sub>2</sub>S. Furthermore, for the sulfur solubility in H<sub>2</sub>S, the model with the proposed  $k_{S_8-H_2S}$  applied to temperatures ranging from 316.26 to 363.15 K and pressures ranging from 7.03 to 32.03 MPa.

**4.2.2. Comparison of sulfur solubility in CO<sub>2</sub> with different  $k_{S_8-CO_2}$ .** Fig. 15 shows a comparison of the sulfur solubility in CO<sub>2</sub> calculated using the thermodynamic model with five different  $k_{S_8-CO_2}$  values at temperatures ranging from 333.15 to 394.26 K. When  $k_{S_8-CO_2}$  was 0.135, the difference between the calculated sulfur solubility and the experimental data was the largest at 383.15 K. Based on Fig. 15, the accuracy of the predicted sulfur solubility seemed to be acceptable using all of the other four  $k_{S_8-CO_2}$  values except 0.135.

As shown in Table 1, the  $k_{S_8-CO_2}$  values obtained by Sun and Heidemann were 0.190 and 0.135.<sup>25,26</sup> Gu *et al.*<sup>16</sup> related the  $k_{S_8-CO_2}$  parameter to the temperature, and reported  $k_{S_8-CO_2}$  values of 0.2107 and 0.1993 at 363.2 and 383.2 K.<sup>16</sup> Cézac<sup>27</sup> suggested that  $k_{S_8-CO_2}$  was temperature dependent and proposed an equation for calculating  $k_{S_8-CO_2}$ , as shown in Table 1. A comparison of the total ARE and AARE values of the calculated sulfur solubility in CO<sub>2</sub> with different  $k_{S_8-CO_2}$  values is shown in Table 3. From Table 3, the deviations of the solubility values calculated using the proposed  $k_{S_8-CO_2}$  from the experimental data were smaller than those using the other four  $k_{S_8-CO_2}$  values.

A comparison of the ARE and AARE values for different  $k_{S_8-CO_2}$  at temperatures of 333.15 to 394.26 K is shown in Fig. 16. Fig. 16(a) shows that ARE is the closest to 0% with the proposed  $k_{S_8-CO_2}$ , ARE < 0 when  $k_{S_8-CO_2}$  is 0.190, and ARE is both negative and positive for the  $k_{S_8-CO_2}$  reported by Cézac.<sup>27</sup> Using the  $k_{S_8-CO_2}$  and  $k_{S_8-CO_2}$  values reported by Cézac,<sup>27</sup> the ARE values were -1.67% and -1.57% at 363.15 K, and 4.34% and 0.55% at 366.48 K, respectively.

As shown Fig. 16(b), the AARE values were smaller using the proposed  $k_{S_8-CO_2}$  than using the other two  $k_{S_8-CO_2}$  values. At 338.71 K, the AARE values were 7.72% and 6.82% using the proposed  $k_{S_8-CO_2}$  and  $k_{S_8-CO_2} = 0.190$ , respectively. Using the proposed  $k_{S_8-CO_2}$ , the  $k_{S_8-CO_2}$  reported by Sun, and the  $k_{S_8-CO_2}$  reported by Cézac, the AARE values were 14.63%, 14.18%, and 14.64% at 363.15 K, and 11.14%, 8.18%, and 8.40% at 366.48 K, respectively. Fig. 16 shows that the accuracy of the predicted solubility using  $k_{S_8-CO_2}$  reported by Cézac was higher than that using the  $k_{S_8-CO_2}$  proposed in this paper at 363.15 and 366.48 K. However, the total deviation was still the lowest using the proposed binary interaction coefficient between sulfur and CO<sub>2</sub> (Table 6 and Fig. 16).

**4.2.3. Comparison of sulfur solubility in CH<sub>4</sub> with different  $k_{S_8-CH_4}$ .** As shown in Table 1, the  $k_{S_8-CH_4}$  values reported by Heidemann and Sun are 0.155 and 0.115, respectively.<sup>25,26</sup> Gu *et al.* related  $k_{S_8-CH_4}$  to temperature, but only reported the  $k_{S_8-CH_4}$  value at 383.2 K.<sup>16</sup> Cézac *et al.*<sup>27</sup> proposed a temperature-

dependent equation for calculating  $k_{S_8-CH_4}$  (Table 1). The total ARE and AARE values of the calculated sulfur solubility in CH<sub>4</sub> using the different values of  $k_{S_8-CH_4}$  are shown in Table 4. The lowest ARE and AARE values of 4.34% and 14.98% were obtained using the proposed  $k_{S_8-CH_4}$ . When  $k_{S_8-CH_4} = 0.155$ , the deviations between the calculated solubility values and the experimental data were the largest. From Table 4, the deviations between the solubility values calculated using the proposed  $k_{S_8-CH_4}$  and the experimental data were smaller than those using the other four  $k_{S_8-CH_4}$ .

Fig. 17 shows a comparison of the predicted sulfur solubility in CH<sub>4</sub> using the thermodynamic model with five different  $k_{S_8-CH_4}$  at temperatures ranging from 338.71 to 394.26 K. Fig. 17(c) shows the calculated sulfur solubility in CH<sub>4</sub> with five different  $k_{S_8-CH_4}$  at 383.15 K, because  $k_{S_8-CH_4} = 0.1345$  reported by Gu was only suitable at 383.2 K. Therefore, Fig. 17(a), (b), and (d) only show the predicted solubility with four different  $k_{S_8-CH_4}$ .

As shown in Fig. 17, the predicted solubility values were negative, except for that calculated using the proposed  $k_{S_8-CH_4}$ . When  $k_{S_8-CH_4} = 0.115$  at 394.26 K, the calculated solubility in CH<sub>4</sub> was close to the experimental data (Fig. 17(d)). Using  $k_{S_8-CH_4} = 0.115$  and the proposed  $k_{S_8-CH_4}$ , the ARE values were 5.25% and 3.46%, while the AARE values were 12.11% and 12.63%, respectively. This indicated that the predicted solubility at 394.26 K using the  $k_{S_8-CH_4}$  value reported by Sun was also acceptable.<sup>26</sup>

## 5. Conclusions

We have proposed new three-parameter equations to calculate the binary interaction coefficients between sulfur and H<sub>2</sub>S, CO<sub>2</sub>, and CH<sub>4</sub>. The parameters in these three equations were obtained by regression of the experimental sulfur solubility data in H<sub>2</sub>S, CO<sub>2</sub>, and CH<sub>4</sub>. The relationship between the binary interaction coefficients and temperature was quadratic. The binary interaction coefficients  $k_{S_8-H_2S}$ ,  $k_{S_8-CO_2}$ , and  $k_{S_8-CH_4}$  were expressed by eqn (23)–(25), and the  $R_{adj}^2$  values of the new fitting equations were 0.896, 0.966, and 0.933, respectively, which indicated that the new three-parameter equations were reliable.

By comparing the experimental solubility data with the solubility results predicted using the binary interaction coefficients proposed by this work and those reported by Sun, Heidemann, Gu, and Cézac, the total ARE and AARE values were significantly smaller when using the proposed binary interaction coefficients than those when using the other four. However, the accuracy of the predicted sulfur solubility in CO<sub>2</sub> using  $k_{S_8-CO_2}$  reported by Cézac was slightly higher than that using  $k_{S_8-CO_2}$  proposed in this article at temperatures of 363.15 and 366.48 K. Furthermore, the calculated solubility in CH<sub>4</sub> using  $k_{S_8-CH_4}$  reported by Sun was acceptable.

In general, the predicted results were satisfactory considering the ARE and AARE values obtained using the proposed binary interaction coefficients. The accuracies of the predicted sulfur solubilities in H<sub>2</sub>S, CO<sub>2</sub>, and CH<sub>4</sub> using the thermodynamic model with the proposed binary interaction coefficients based on the PR EoS were greatly improved, and the thermodynamic model was suitable for a wide range of temperatures and pressures.



## Conflicts of interest

There are no conflicts to declare.

## Appendix

Table 5 Elemental sulfur solubility in H<sub>2</sub>S

<i>T</i> /K	<i>P</i> /MPa	Solubility (experiment)/ mol mol <sup>-1</sup>	Solubility (this model)/mol mol <sup>-1</sup>	Relative error
316.26	7.03	0.001669	0.001790	0.0722
	10.48	0.001846	0.001915	0.0373
	17.37	0.001977	0.002099	0.0619
	24.27	0.002078	0.002220	0.0682
338.71	31.16	0.002196	0.002294	0.0448
	7.03	0.00262	0.002586	-0.0129
	10.48	0.002926	0.003120	0.0662
	17.37	0.00367	0.003927	0.0701
363.15	24.27	0.004189	0.004502	0.0747
	31.16	0.004494	0.004913	0.0932
	11.83	0.004832	0.004352	-0.0993
	14.79	0.005081	0.005789	0.1393
394.26	19.14	0.007313	0.007613	0.0410
	32.03	0.009523	0.011664	0.2248

Table 6 Elemental sulfur solubility in CO<sub>2</sub>

<i>T</i> /K	<i>P</i> /MPa	Solubility (experiment)/ mol mol <sup>-1</sup>	Solubility (this model)/mol mol <sup>-1</sup>	Relative error
333.15	15.10	7.682 × 10 <sup>-6</sup>	7.400 × 10 <sup>-6</sup>	-0.0368
	19.10	1.624 × 10 <sup>-5</sup>	1.650 × 10 <sup>-5</sup>	0.0144
	24.31	2.377 × 10 <sup>-5</sup>	2.790 × 10 <sup>-5</sup>	0.1718
	29.47	4.193 × 10 <sup>-5</sup>	3.780 × 10 <sup>-5</sup>	-0.0991
338.71	20.68	2.205 × 10 <sup>-5</sup>	1.990 × 10 <sup>-5</sup>	-0.0991
	27.58	3.504 × 10 <sup>-5</sup>	3.610 × 10 <sup>-5</sup>	0.0316
	34.47	4.395 × 10 <sup>-5</sup>	4.990 × 10 <sup>-5</sup>	0.1351
	41.37	5.851 × 10 <sup>-5</sup>	6.100 × 10 <sup>-5</sup>	0.0431
363.15	15.86	1.252 × 10 <sup>-5</sup>	9.960 × 10 <sup>-6</sup>	-0.2044
	19.53	1.961 × 10 <sup>-5</sup>	2.390 × 10 <sup>-5</sup>	0.2174
	24.76	4.439 × 10 <sup>-5</sup>	5.190 × 10 <sup>-5</sup>	0.1684
	27.99	6.528 × 10 <sup>-5</sup>	7.080 × 10 <sup>-5</sup>	0.0845
	14.14	6.200 × 10 <sup>-6</sup>	5.920 × 10 <sup>-6</sup>	-0.0455
	18.97	2.400 × 10 <sup>-5</sup>	2.130 × 10 <sup>-5</sup>	-0.1109
	25.10	6.970 × 10 <sup>-5</sup>	5.380 × 10 <sup>-5</sup>	-0.2276
	25.10	7.090 × 10 <sup>-5</sup>	5.380 × 10 <sup>-5</sup>	-0.2407
	32.14	1.017 × 10 <sup>-4</sup>	9.490 × 10 <sup>-5</sup>	-0.0673
	37.41	1.087 × 10 <sup>-4</sup>	1.236 × 10 <sup>-4</sup>	0.1374
	40.52	1.260 × 10 <sup>-4</sup>	1.392 × 10 <sup>-4</sup>	0.1051
	366.48	13.79	5.805 × 10 <sup>-6</sup>	6.110 × 10 <sup>-6</sup>
20.68		3.966 × 10 <sup>-5</sup>	3.290 × 10 <sup>-5</sup>	-0.1700
27.58		7.193 × 10 <sup>-5</sup>	7.800 × 10 <sup>-5</sup>	0.0843
34.47		1.091 × 10 <sup>-4</sup>	1.253 × 10 <sup>-4</sup>	0.1487
383.15	41.37	1.530 × 10 <sup>-4</sup>	1.685 × 10 <sup>-4</sup>	0.1012
	24.83	1.135 × 10 <sup>-4</sup>	9.080 × 10 <sup>-5</sup>	-0.2001
	32.76	1.894 × 10 <sup>-4</sup>	1.921 × 10 <sup>-4</sup>	0.0142
	35.41	1.960 × 10 <sup>-4</sup>	2.281 × 10 <sup>-4</sup>	0.1640
394.26	38.62	2.009 × 10 <sup>-4</sup>	2.714 × 10 <sup>-4</sup>	0.3509
	20.68	8.716 × 10 <sup>-5</sup>	7.570 × 10 <sup>-5</sup>	-0.1317
	27.58	1.554 × 10 <sup>-4</sup>	1.924 × 10 <sup>-4</sup>	0.2382
	34.47	3.153 × 10 <sup>-4</sup>	3.489 × 10 <sup>-4</sup>	0.1064
41.37	6.457 × 10 <sup>-4</sup>	5.188 × 10 <sup>-4</sup>	-0.1966	

Table 7 Elemental sulfur solubility in CH<sub>4</sub>

<i>T</i> /K	<i>P</i> /MPa	Solubility (experiment)/ mol mol <sup>-1</sup>	Solubility (this model)/mol mol <sup>-1</sup>	Relative error
338.71	27.5792	2.882 × 10 <sup>-6</sup>	2.420 × 10 <sup>-6</sup>	-0.1588
	34.474	5.357 × 10 <sup>-6</sup>	5.450 × 10 <sup>-6</sup>	0.0178
	41.3688	8.113 × 10 <sup>-6</sup>	1.020 × 10 <sup>-5</sup>	0.2511
366.48	20.6844	3.623 × 10 <sup>-6</sup>	3.170 × 10 <sup>-6</sup>	-0.1241
	27.5792	5.008 × 10 <sup>-6</sup>	7.170 × 10 <sup>-6</sup>	0.4316
	34.474	1.389 × 10 <sup>-5</sup>	1.370 × 10 <sup>-5</sup>	-0.0146
	41.3688	2.196 × 10 <sup>-5</sup>	2.280 × 10 <sup>-5</sup>	0.0400
383.15	20.517	8.100 × 10 <sup>-6</sup>	5.750 × 10 <sup>-6</sup>	-0.2903
	20.517	6.300 × 10 <sup>-6</sup>	5.750 × 10 <sup>-6</sup>	-0.0875
	42.414	2.940 × 10 <sup>-5</sup>	3.260 × 10 <sup>-5</sup>	0.1077
	42.414	2.670 × 10 <sup>-5</sup>	3.260 × 10 <sup>-5</sup>	0.2197
394.26	50.172	4.080 × 10 <sup>-5</sup>	4.780 × 10 <sup>-5</sup>	0.1711
	6.8948	2.588 × 10 <sup>-6</sup>	2.660 × 10 <sup>-6</sup>	0.0282
	20.6844	1.027 × 10 <sup>-5</sup>	9.380 × 10 <sup>-6</sup>	-0.0861
	27.5792	1.223 × 10 <sup>-5</sup>	1.680 × 10 <sup>-5</sup>	0.3742
394.26	34.474	2.918 × 10 <sup>-5</sup>	2.720 × 10 <sup>-5</sup>	-0.0695
	41.3688	4.331 × 10 <sup>-5</sup>	4.010 × 10 <sup>-5</sup>	-0.0737

## Nomenclature

### Abbreviations

EoS	Equation of state
RE	Relative error
ARE	Average relative error
AARE	Absolute average relative error

### Roman symbols

$f_{S_8}^S$	Fugacity of the pure solid specie S <sub>8</sub> [Pa]
$f_{S_8}^V$	Fugacity of sulfur in vapor phase [Pa]
$P$	Absolute pressure [Pa]
$T$	Temperature [K]
$y$	Sulfur solubility in gas [mol mol <sup>-1</sup> ]
$\phi_{S_8}^{sat}$	Fugacity factor of sulfur saturation vapor
$R$	Gas constant [8.314 J (mol <sup>-1</sup> K <sup>-1</sup> )]
$P_{S_8}^{sat}$	Sulfur saturation vapor pressure at temperature $T$ [Pa]
$V_{S_8}^{sat}$	Molar volume of solid sulfur [m <sup>3</sup> mol <sup>-1</sup> ]
$y_{S_8}$	Mole fraction of gaseous sulfur
$\phi_{S_8}^V$	Fugacity coefficient of gaseous sulfur
$V$	Specific volume [m <sup>3</sup> mol <sup>-1</sup> ]
$T_c$	Critical temperature [K]
$P_c$	Critical pressure [Pa]
$\omega$	Acentric factor
$T_r$	Reduced temperature
$Z$	Gas mixtures compressibility factor
$n$	Number of gas component
$y_i$	Mole fraction in gas mixtures of component $i$
$y_j$	Mole fraction in gas mixtures of component $j$



$k_{ij}$	Binary interaction coefficients between component $i$ and component $j$
$Z_i^{\text{pred}}$	Predicting sulfur solubility with model
$Z_i^{\text{exp}}$	Sulfur solubility from experiment
$k_{S_8-H_2S}$	Binary interaction coefficient between $S_8$ and $H_2S$
$k_{S_8-CO_2}$	Binary interaction coefficient between $S_8$ and $CO_2$
$k_{S_8-CH_4}$	Binary interaction coefficient between $S_8$ and $CH_4$

### Subscripts and superscripts

$i, j$	Species index
S	Solid sulfur
V	Vapor
sat	Saturation
r	Reduced state
c	Critical state
pre	Predicting results
exp	Experimental data

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