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# Hydration of the methanesulfonate–ammonia/amine complex and its atmospheric implications†

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Methanesulfonate (MSA<sup>-</sup>), found in substantial concentrations in the atmosphere, is expected to enhance aerosol nucleation and the growth of nanoparticles, but the details of methanesulfonate clusters are poorly understood. In this study, MSA<sup>-</sup> was chosen along with ammonia (NH<sub>3</sub>) or three common amines and water (H<sub>2</sub>O) to discuss the roles of ternary homogeneous nucleation and ion-induced nucleation in aerosol formation. We studied the structural characteristics and thermodynamics of the clusters using density functional theory at the PW91PW91/6-311++G(3df,3pd) level. The analysis of noncovalent interactions predicts that the amines can form more stable clusters with MSA<sup>-</sup> than NH<sub>3</sub>, in agreement with the results from structures and thermodynamics; however, the enhancement in stability for amines is not large enough to overcome the difference in the concentrations of NH<sub>3</sub> and amines under typical atmospheric conditions. In addition, the favorable free energies of formation for the (MSA<sup>-</sup>)(NH<sub>3</sub>/amines)(H<sub>2</sub>O)<sub>*n*</sub> (*n* = 0–3) clusters at 298.15 K show that MSA<sup>-</sup> could contribute to the aerosol nucleation process with binding NH<sub>3</sub>/amines and H<sub>2</sub>O up to *n* = 3. There are strong temperature and humidity dependences for the formation of complexes; higher humidity and temperature promote the formation of larger hydrates. Finally, for the (MSA<sup>-</sup>)(NH<sub>3</sub>/amines)(H<sub>2</sub>O)<sub>*n*</sub> clusters, the evaporation rates were determined to further investigate the atmospheric implications.

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## 1. Introduction

Atmospheric aerosols have significant impact in several areas including earth climate, air quality and public health.<sup>1–5</sup> Direct atmospheric nucleation *via* the formation of solid or liquid aerosols from gas-phase species is an important source of aerosol particles.<sup>6–10</sup> Although the nucleation mechanism has been studied continuously, there are still many uncertainties in the compositions and the actual species that contribute to the nucleation and growth of nanoparticles in the atmosphere, especially at the molecular cluster level.<sup>5,10–13</sup>

Both experimental and theoretical results have indicated that sulfuric acid (H<sub>2</sub>SO<sub>4</sub>) plays a critical role in atmospheric nucleation, and it has been widely identified as one of the major atmospheric nucleating species.<sup>11,14,15</sup> The main source of H<sub>2</sub>SO<sub>4</sub> in the atmosphere is the emitted SO<sub>2</sub> from fossil fuel and biomass burning, which readily reacts with hydroxyl radicals (·OH) and water vapor.<sup>16,17</sup> Gas-phase H<sub>2</sub>SO<sub>4</sub> has low vapor

pressure and can easily supersaturate;<sup>15,18,19</sup> therefore, it has been found that the H<sub>2</sub>SO<sub>4</sub> undergoes a quick gas-condensed phase transition and serves as an effective nucleating species for water vapor, the key nucleating species in the atmosphere.<sup>11,14,15,20,21</sup> However, the binary homogeneous nucleation of H<sub>2</sub>SO<sub>4</sub> and water (H<sub>2</sub>O) is not enough to understand the observed nucleation events in the atmosphere, implying that some other compounds are involved in the nucleation phenomena.<sup>6,11,13</sup>

The importance of ammonia (NH<sub>3</sub>) in atmospheric nucleation has been extensively discussed.<sup>22–25</sup> According to previous studies, NH<sub>3</sub> has an enhancing effect on H<sub>2</sub>SO<sub>4</sub> nucleation, responsible for the formation of NH<sub>4</sub>HSO<sub>4</sub> and (NH<sub>4</sub>)<sub>2</sub>SO<sub>4</sub> clusters.<sup>20,26</sup> These species represent the three major forms of sulfur-containing aerosols, along with particulate sulfuric acid. Apart from NH<sub>3</sub>, amines are among the few basic compounds present in the actual atmosphere, and as such can be expected to bind strongly to H<sub>2</sub>SO<sub>4</sub> or other nucleation precursors. All the field, laboratory, and modelling studies have suggested that the amines might play a significant role in the formation and subsequent growth of aerosol particles;<sup>10,27,28</sup> some amines may even be more effective than NH<sub>3</sub> at enhancing the particle formation. In the recent quantum chemical study involving several amines possibly existing in the atmosphere, it was pointed out that they could form more strongly bound structures with H<sub>2</sub>SO<sub>4</sub> than NH<sub>3</sub>.<sup>27,29,30</sup> Proton transfer of some

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amine-acid clusters is easier than  $\text{NH}_3$ -acid clusters, leading to stronger binding.<sup>31,32</sup> It is possible that amines, instead of  $\text{NH}_3$ , are the major enhancers of  $\text{H}_2\text{SO}_4$ - $\text{H}_2\text{O}$  nucleation, or may significantly contribute to particle formation in the atmosphere. The smog chamber experiments and field measurements demonstrate that the acid-base reaction may play a significant role in particle formation, and it is viewed as an important nucleation mechanism, for example, the particle formation involving  $\text{H}_2\text{SO}_4$  with  $\text{NH}_3$  and amines.<sup>27,33</sup> Quantum calculations also explain the important role of acid-base reactions, which enhance neutral and ion-induced  $\text{H}_2\text{SO}_4$ - $\text{H}_2\text{O}$  nucleation.<sup>32,34,35</sup>

Methanesulfonic acid (MSA) and  $\text{H}_2\text{SO}_4$  are viewed as the two main oxidation products of ocean-released dimethyl sulfide in the atmosphere.<sup>36-39</sup> MSA is widely detected in particles, and its typical gas-phase concentration is roughly 10–100% of that of  $\text{H}_2\text{SO}_4$  in the coastal marine boundary layer.<sup>39-42</sup> Based on previous work, it has been shown that MSA is a less potent clustering agent in comparison with  $\text{H}_2\text{SO}_4$ , but its role is far from negligible in the atmosphere.<sup>43,44</sup> The results of experiments and quantum chemical calculations indicate that the reactions of MSA with  $\text{NH}_3$  and amines including methylamine (MA), dimethylamine (DMA), and trimethylamine (TMA) can contribute to the new particle formation under normal conditions.<sup>39,45,46</sup> Although the concentration of amines is 1–3 orders of magnitude lower than that of  $\text{NH}_3$  in the actual atmosphere, they still play a key role in new particle formation (NPF) with MSA.<sup>46</sup> MSA also enhances the formation of molecular clusters containing  $\text{H}_2\text{SO}_4$  and DMA, and its effect is related to the temperature and concentrations of MSA and DMA.<sup>43</sup> The research on the contribution of MSA to NPF with the common nucleation precursors such as MSA, methanol, formic acid, acetone, dimethylether, formaldehyde and methyl formate has emphasized the importance of MSA in NPF.<sup>44</sup>

In addition, the role of ions in atmospheric nucleation processes has been intensively debated.<sup>47-52</sup> The mechanism of ion-mediated nucleation has been proposed to explain nucleation events in the earth's atmosphere. Previous studies at the Cosmics Leaving Outdoor Droplets (CLOUD) facility at CERN indicate that ions surely enhance the formation of particles to a certain extent.<sup>53</sup> In the ambient atmosphere, the clusters containing  $\text{HSO}_4^-$  are frequently observed. The results of experimental thermodynamics on some  $(\text{HSO}_4^-)(\text{H}_2\text{SO}_4)$  clusters suggest that these clusters have a high  $\text{H}_2\text{SO}_4$  affinity and are able to promote cluster growth by  $\text{H}_2\text{SO}_4$  uptake. The atmospheric ions as the nucleation catalysts could attract  $\text{H}_2\text{SO}_4$ ,  $\text{H}_2\text{O}$  and most of the common organic pollutants, providing an evident increase in nanoparticle formation.<sup>54</sup> For MSA, it binds one or two water molecules with several hydrogen bonds to form the relatively stable clusters; however, the addition of more water would result in the proton transfer from MSA to the neighboring water molecules.<sup>55,56</sup> Upon reaching a critical cluster size, the separation of methanesulfonate ( $\text{MSA}^-$ ) and the hydrated proton occurs.<sup>55,56</sup> Proton transfer from MSA to  $\text{NH}_3$  or amines might be another source of  $\text{MSA}^-$ .<sup>57</sup> In this work,  $\text{MSA}^-$  is selected for further research.

The ion-mediated nucleation of  $\text{MSA}^-$  is expected to enhance the nucleation and growth of nanoparticles, but the details about the methanesulfonate clusters are poorly understood. In this study,  $\text{MSA}^-$  is chosen along with  $\text{NH}_3$  or three other common amines possibly present in the atmosphere, and water to discuss the roles of ternary homogeneous nucleation and ion-induced nucleation in the aerosol nucleation. The three common amines discussed here are MA, DMA, and TMA. The hydration of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})$  is investigated with density functional theory (DFT) at the PW91PW91/6-311++G(3df,3pd) level. We have searched for the energy minima of structures of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ) and determined their thermodynamic properties. The results were then used to gain further insight into the ternary nucleation of  $\text{MSA}^-$ ,  $\text{NH}_3$ /amines and  $\text{H}_2\text{O}$ , as well as the weak attraction analysis at the molecular level. The effects of humidity and temperature on the formation of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ) and its atmospheric relevance are studied. Besides, the evaporation rates of these clusters are investigated for the first time. This work is a continuation of longstanding efforts to investigate ion-molecule interactions, hydrogen-bonded interactions, water cluster formation and atmospheric processes.<sup>49</sup>

## 2. Theoretical methods

The initial geometries of the various monomers and  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ) clusters have been obtained using the Basin Hopping (BH) algorithm<sup>58-60</sup> coupled with DFT, and the generalized gradient approximation in the Perdew-Burke-Ernzerhof (PBE) functional, and the double numerical plus  $d$ -functions (DND) basis set implemented in the DMol<sup>3</sup> software package<sup>61</sup> are applied in the procedure. This BH method was highly efficient at exploring atomic and molecular systems based on our previous studies.<sup>62-69</sup> In this work, the number of BH searches range from 10 to 20 according to the cluster sizes, and each BH search consists of 1000 sampling steps at 3000 K with randomly generated molecular structures.

The initial geometries of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ) clusters were optimized at the PW91PW91/6-31+G\* level by DFT. The stable isomers from the first optimization were selected to be further optimized by the PW91PW91/6-311++G(3df,3pd) level of theory as a higher level of theory to get the final configurations. The PW91PW91/6-311++G(3df,3pd) level implemented in the Gaussian 09 software package<sup>70</sup> was used for the second optimization and frequency calculation. This methodology was adopted because it would take much less time to get the final structures with two-step optimizations than that through once direct optimization with the PW91PW91/6-311++G(3df,3pd) level of theory. The PW91PW91 functional showed great performance on a large number of atmospheric clusters containing sulfuric acid, water and the common organic acids, including predictions of structural characteristics, the thermodynamics of cluster formation and satisfactory similarity compared with experimental results.<sup>71-74</sup> In order to make sure the results are consistent, the other three methods (CAM-B3LYP, M06-2X and  $\omega$ B97x-D) were utilized for the smallest clusters, including different monomers and dimers.



The density functional rather than wave function theory method (*i.e.* MP2) has been used in the systems for comparison with each other, as in the work of Elm *et al.*<sup>75</sup> Due to the absence of wave function theory, the computational costs could be reduced. Besides, the recent benchmark studies proposed the pool of potential density functional methods, which are applied in our benchmark work,<sup>75,76</sup> and thus the accuracy of our benchmark is maintained. The benchmark results with four functionals are displayed in Table 1 for the  $(\text{MSA}^-)(\text{NH}_3)$ ,  $(\text{MSA}^-)(\text{MA})$ ,  $(\text{MSA}^-)(\text{DMA})$  and  $(\text{MSA}^-)(\text{H}_2\text{O})$ . The Gibbs free energy calculated by PW91PW91 is close to that calculated by CAM-B3LYP, M06-2X and  $\omega$ B97x-D, and the deviation is very low

**Table 1** Calculated Gibbs free energies and free energy changes for different monomers and dimers using various DFT functionals with the 6-311++G(3df,3pd) basis set

Isomer	Functional	$G$ (Hartree)	$\Delta G$ (kcal mol <sup>-1</sup> )
$\text{MSA}^-$	CAM-B3LYP	-663.87	
	M06-2X	-663.82	
	$\omega$ B97x-D	-663.86	
	PW91PW91	-663.87	
$\text{NH}_3$	CAM-B3LYP	-56.54	
	M06-2X	-56.54	
	$\omega$ B97x-D	-56.55	
	PW91PW91	-56.54	
MA	CAM-B3LYP	-95.80	
	M06-2X	-95.80	
	$\omega$ B97x-D	-95.82	
	PW91PW91	-95.81	
DMA	CAM-B3LYP	-135.07	
	M06-2X	-135.07	
	$\omega$ B97x-D	-135.10	
	PW91PW91	-135.09	
TMA	CAM-B3LYP	-174.34	
	M06-2X	-174.35	
	$\omega$ B97x-D	-174.39	
	PW91PW91	-174.36	
$\text{H}_2\text{O}$	CAM-B3LYP	-76.43	
	M06-2X	-76.42	
	$\omega$ B97x-D	-76.43	
	PW91PW91	-76.43	
$(\text{MSA}^-)(\text{NH}_3)$	CAM-B3LYP	-720.41	0.88
	M06-2X	-720.35	0.96
	$\omega$ B97x-D	-720.41	1.29
	PW91PW91	-720.41	1.02
$(\text{MSA}^-)(\text{MA})$	CAM-B3LYP	-759.67	0.24
	M06-2X	-759.62	-0.32
	$\omega$ B97x-D	-759.68	0.28
	PW91PW91	-759.68	-0.66
$(\text{MSA}^-)(\text{DMA})$	CAM-B3LYP	-798.94	0.24
	M06-2X	-798.90	-0.64
	$\omega$ B97x-D	-798.96	-0.15
	PW91PW91	-798.96	-0.74
$(\text{MSA}^-)(\text{TMA})$	CAM-B3LYP	-838.21	3.03
	M06-2X	-838.16	5.03
	$\omega$ B97x-D	-838.24	2.58
	PW91PW91	-838.23	2.18
$(\text{MSA}^-)(\text{H}_2\text{O})$	CAM-B3LYP	-740.31	-5.48
	M06-2X	-740.25	-6.39
	$\omega$ B97x-D	-740.30	-5.43
	PW91PW91	-740.31	-5.88

with the values less than 1 kcal mol<sup>-1</sup>. In the  $(\text{MSA}^-)(\text{TMA})$  cluster, the free energy change calculated by PW91PW91 is closer to that by CAM-B3LYP and  $\omega$ B97x-D, where the deviation is also less than 1 kcal mol<sup>-1</sup>, rather than M06-2X; it could be acceptable in that the differences among the results of different functionals are considered to increase with the increasing clusters size. Thus, the PW91PW91 was chosen as the specific DFT method in our systems. In addition, the energy differences caused by various functionals do not change the order of stability for different dimers, that is,  $(\text{MSA}^-)(\text{DMA}) > (\text{MSA}^-)(\text{MA}) > (\text{MSA}^-)(\text{NH}_3) > (\text{MSA}^-)(\text{TMA})$ .

Finally, the optimized geometries were used for single point energy calculations with the DF-LMP2-F12/VDZ-F12 (second-order Møller-Plesset perturbation theory-explicitly correlated methods with density fitting) method implemented in Molpro 2010.1 (ref. 77) to get more accurate structure parameters. This level of theory is accurate for single-point energy calculations according to the previous work.<sup>52</sup> The PW91PW91/6-311++G(3df,3pd) thermodynamic corrections were combined with DF-LMP2-F12/VDZ-F12 single-point energies to evaluate the zero-point corrected energies [ $E(0\text{ K})$ ], energies including atmospheric temperature enthalpies [ $H(T)$ ] and Gibbs free energies [ $G(T)$ ]. Compared with the PW91PW91/6-311++G(3df,3pd) binding energies ( $\Delta E$ ), the energies obtained by the DF-LMP2-F12/VDZ-F12 single-point energies with the PW91PW91/6-311++G(3df,3pd) thermodynamic corrections are closer to the results of CCSD(T)-F12a/VDZ-F12, as shown in Table 2.

## 3. Results and discussion

### 3.1 Structures

Fig. 1 displays the optimized global minimum clusters at the PW91PW91/6-311++G(3df,3pd) level of theory for the  $(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_n$  ( $n = 0-3$ ),  $(\text{MSA}^-)(\text{MA})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ),  $(\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ), and  $(\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ) systems, that will be discussed in this section. The “ $n$ ” ( $n = 0-3$ ) represents the number of water molecules up to three. The sulfur atoms are depicted in yellow, oxygen atoms in red, nitrogen atoms in blue, carbon atoms in dark gray and the hydrogen atoms in light gray. The hydrogen bonds are indicated with dotted lines. The Cartesian coordinates for the optimized global minimum clusters are shown in the ESI.†

In Fig. 1, for the  $(\text{MSA}^-)(\text{NH}_3)$  dimer, the  $\text{SO}_3$  group of  $\text{MSA}^-$  serves as the hydrogen bond acceptor from the  $\text{NH}_3$ , forming two O–H hydrogen bonds with the lengths of 2.263 Å and 2.270 Å, respectively. For the  $(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})$  cluster, the added  $\text{H}_2\text{O}$  builds a ring structure with the  $\text{MSA}^-$  and  $\text{NH}_3$ . In this configuration, the  $\text{NH}_3$ – $\text{H}_2\text{O}$  dimer is bound to  $\text{MSA}^-$  with shorter hydrogen bond lengths than those in the  $\text{MSA}^-$ – $\text{NH}_3$  dimer, the hydrogen bond between the  $\text{NH}_3$  and water is also less than 2 Å. In  $(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_2$ , the  $(\text{H}_2\text{O})_2$  dimer binds the  $\text{SO}_3$  group of  $\text{MSA}^-$  with two strong hydrogen bonds, while the  $\text{NH}_3$  forms a weak hydrogen bond to the  $\text{MSA}^-$  as a donor and a relatively strong hydrogen bond with the  $(\text{H}_2\text{O})_2$  dimer as an acceptor. The  $(\text{H}_2\text{O})_3$  trimer and  $\text{NH}_3$  are combined with the  $\text{SO}_3$  group in the  $(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_3$  cluster to form an



**Table 2** The PW91PW91/6-311++G(3df,3pd) binding energies ( $\Delta E$ ) and the zero-point corrected energies based on the DF-MP2-F12/VDZ-F12 single-point energies with the PW91PW91/6-311++G(3df,3pd) thermodynamic corrections for different monomers and dimers, compared against CCSD(T)-F12a/VDZ-F12 results

Isomer	Method	$E$ (Hartree)	$\Delta E$ (kcal mol <sup>-1</sup> )
MSA <sup>-</sup>	PW91PW91	-663.15	
	DF-LMP2-F12/VDZ-F12//PW91PW91	-663.10	
	CCSD(T)-F12a/VDZ-F12	-663.14	
NH <sub>3</sub>	PW91PW91	-56.48	
	DF-LMP2-F12/VDZ-F12//PW91PW91	-56.45	
	CCSD(T)-F12a/VDZ-F12	-56.49	
MA	PW91PW91	-95.71	
	DF-LMP2-F12/VDZ-F12//PW91PW91	-95.64	
	CCSD(T)-F12a/VDZ-F12	-95.72	
DMA	PW91PW91	-134.93	
	DF-LMP2-F12/VDZ-F12//PW91PW91	-134.84	
	CCSD(T)-F12a/VDZ-F12	-134.96	
TMA	PW91PW91	-174.17	
	DF-LMP2-F12/VDZ-F12//PW91PW91	-174.05	
	CCSD(T)-F12a/VDZ-F12	-174.21	
H <sub>2</sub> O	PW91PW91	-76.36	
	DF-LMP2-F12/VDZ-F12//PW91PW91	-76.34	
	CCSD(T)-F12a/VDZ-F12	-76.36	
(MSA <sup>-</sup> )	PW91PW91	-719.65	-7.32
(NH <sub>3</sub> )	DF-LMP2-F12/VDZ-F12//PW91PW91	-719.56	-7.67
	CCSD(T)-F12a/VDZ-F12	-719.64	-8.91
(MSA <sup>-</sup> )	PW91PW91	-758.76	-8.56
	DF-LMP2-F12/VDZ-F12//PW91PW91	-758.80	-9.04
(MA)	CCSD(T)-F12a/VDZ-F12	-758.88	-9.87
	PW91PW91	-798.10	-9.31
(DMA)	DF-LMP2-F12/VDZ-F12//PW91PW91	-797.96	-10.26
	CCSD(T)-F12a/VDZ-F12	-798.12	-10.82
(MSA <sup>-</sup> )	PW91PW91	-837.33	-6.10
	DF-LMP2-F12/VDZ-F12//PW91PW91	-837.17	-6.39
(TMA)	CCSD(T)-F12a/VDZ-F12	-837.36	-6.85
	PW91PW91	-739.53	-13.70
(MSA <sup>-</sup> )	DF-LMP2-F12/VDZ-F12//PW91PW91	-739.46	-13.72
	CCSD(T)-F12a/VDZ-F12	-739.52	-15.79

approximate cubic structure, in which six oxygens, one sulfur and one nitrogen atom are viewed as the vertices of the cube. Eight hydrogen bonds found in this geometry make the structure stable, and the SO<sub>3</sub> group of MSA<sup>-</sup> is the hydrogen bond acceptor from the NH<sub>3</sub> and several waters.

For the (MSA<sup>-</sup>)(MA) dimer, the NH<sub>2</sub> group of MA is bound to the MSA<sup>-</sup>, forming two hydrogen bonds with the same length of 2.247 Å, which are stronger than the those in (MSA<sup>-</sup>)(NH<sub>3</sub>). The one added water breaks the conformation of (MSA<sup>-</sup>)(MA) and allows the formation of a ring structure with three strong hydrogen bonds less than 2 Å in the (MSA<sup>-</sup>)(MA)(H<sub>2</sub>O) cluster. The structure of (MSA<sup>-</sup>)(MA)(H<sub>2</sub>O)<sub>2</sub> is the same as that of (MSA<sup>-</sup>)(NH<sub>3</sub>)(H<sub>2</sub>O)<sub>2</sub>, and it can be seen that the NH<sub>3</sub> is replaced by the MA. Just like the (MSA<sup>-</sup>)(NH<sub>3</sub>)(H<sub>2</sub>O)<sub>3</sub>, an approximate cubic structure is formed in the (MSA<sup>-</sup>)(MA)(H<sub>2</sub>O)<sub>3</sub>. The amino group of MA serves as a single acceptor–two donors bridge the MSA and water. Besides, the amino group, regardless of being from the NH<sub>3</sub> or the MA, plays a key role in the establishment of the structure, in which the other part, just like the nitrogen

atom and methyl group, can be ignored. Therefore, the structures of the (MSA<sup>-</sup>)(MA)(H<sub>2</sub>O)<sub>n</sub> system are highly similar to those of the (MSA<sup>-</sup>)(NH<sub>3</sub>)(H<sub>2</sub>O)<sub>n</sub> system for up to three water molecules.

In (MSA<sup>-</sup>)(DMA), the oxygen atom of the SO<sub>3</sub> group as the hydrogen bond acceptor forms a strong hydrogen bond (1.970 Å) with the NH group of DMA. For the (MSA<sup>-</sup>)(DMA)(H<sub>2</sub>O) cluster in the ring structure built by the MSA<sup>-</sup>, DMA and H<sub>2</sub>O, the NH group of DMA acts as a single donor and a single acceptor, where the hydrogen bond between MSA<sup>-</sup> and DMA is stronger than that in (MSA<sup>-</sup>)(NH<sub>3</sub>)(H<sub>2</sub>O) and (MSA<sup>-</sup>)(MA)(H<sub>2</sub>O) clusters. The (MSA<sup>-</sup>)(DMA)(H<sub>2</sub>O)<sub>2</sub> cluster has a similar structure to the (MSA<sup>-</sup>)(NH<sub>3</sub>)(H<sub>2</sub>O)<sub>2</sub> and (MSA<sup>-</sup>)(MA)(H<sub>2</sub>O)<sub>2</sub>. DMA can form a stronger N–H hydrogen bond with the (H<sub>2</sub>O)<sub>2</sub> dimer, with the length of 1.913 Å, compared to that in (MSA<sup>-</sup>)(NH<sub>3</sub>)(H<sub>2</sub>O)<sub>2</sub> (1.956 Å) and (MSA<sup>-</sup>)(MA)(H<sub>2</sub>O)<sub>2</sub> (1.918 Å), and another O–H hydrogen bond with length 1.967 Å, which is stronger than those in (MSA<sup>-</sup>)(NH<sub>3</sub>)(H<sub>2</sub>O)<sub>2</sub> (2.033 Å) and (MSA<sup>-</sup>)(MA)(H<sub>2</sub>O)<sub>2</sub> (2.000 Å). It can be expected that the DMA can form a more stable structure than NH<sub>3</sub> or MA with MSA<sup>-</sup> in the presence of water. In (MSA<sup>-</sup>)(DMA)(H<sub>2</sub>O)<sub>3</sub>, the (H<sub>2</sub>O)<sub>3</sub> trimer bridges the MSA<sup>-</sup> with DMA to form a similar cubic structure. The added water molecules promote the formation of multi-bridging hydrogen bonds. Moreover, the two methyl groups of DMA are still free and rarely participate in the formation of structures.

Two weak hydrogen bonds with lengths of 2.288 Å and 2.287 Å, respectively, are found between the MSA<sup>-</sup> and TMA in the (MSA<sup>-</sup>)(TMA) dimer, where the hydrogen bonds are weaker than those in the dimer of (MSA<sup>-</sup>)(NH<sub>3</sub>), (MSA<sup>-</sup>)(MA), and (MSA<sup>-</sup>)(DMA). Because of the existence of three methyl groups in TMA, the one added water cannot form a ring structure with the other molecules, and an oxygen atom of MSA<sup>-</sup> forms two hydrogen bonds (2.320 Å and 2.396 Å, respectively) with the two methyl groups of TMA. For the (MSA<sup>-</sup>)(TMA)(H<sub>2</sub>O)<sub>2</sub>, the (H<sub>2</sub>O)<sub>2</sub> dimer binds with the two oxygen atoms in MSA<sup>-</sup>, and the TMA forms two hydrogen bonds with the remaining oxygen atom of the CH<sub>3</sub>O group. In this structure, the three oxygen atoms accept four hydrogen bonds without free oxygen atoms, in comparison with the other (MSA<sup>-</sup>)(NH<sub>3</sub>/amines)(H<sub>2</sub>O)<sub>2</sub> clusters. The (MSA<sup>-</sup>)(TMA)(H<sub>2</sub>O)<sub>3</sub> cluster is based on the (MSA<sup>-</sup>)(TMA)(H<sub>2</sub>O)<sub>2</sub> with the third water bound to the (H<sub>2</sub>O)<sub>2</sub> dimer and MSA<sup>-</sup>, forming two hydrogen bonds.

From the analysis above, it can be seen that the MSA<sup>-</sup> is combined with NH<sub>3</sub> or different amines through one or more hydrogen bonds. It is obvious that the hydrogen bond with the length less than 2 Å in the (MSA<sup>-</sup>)(DMA) cluster is stronger than those in the other dimers. With the addition of water molecules, more hydrogen bonds are formed in the (MSA<sup>-</sup>)(NH<sub>3</sub>/amines)(H<sub>2</sub>O)<sub>n</sub> clusters, which might promote cluster formation in the actual atmosphere. For all the hydrates in Fig. 1, the water is always viewed as the hydrogen bond donor, and the MSA<sup>-</sup> is the hydrogen bond acceptor. Additionally, the possible evolution routes are found in the hydrates of (MSA<sup>-</sup>)(NH<sub>3</sub>/amines): for the monohydrate, the added water breaks the conformation of the (MSA<sup>-</sup>)(NH<sub>3</sub>/amines) dimer to allow the formation of a ring structure. The (H<sub>2</sub>O)<sub>2</sub> dimer in the dihydrate connects the



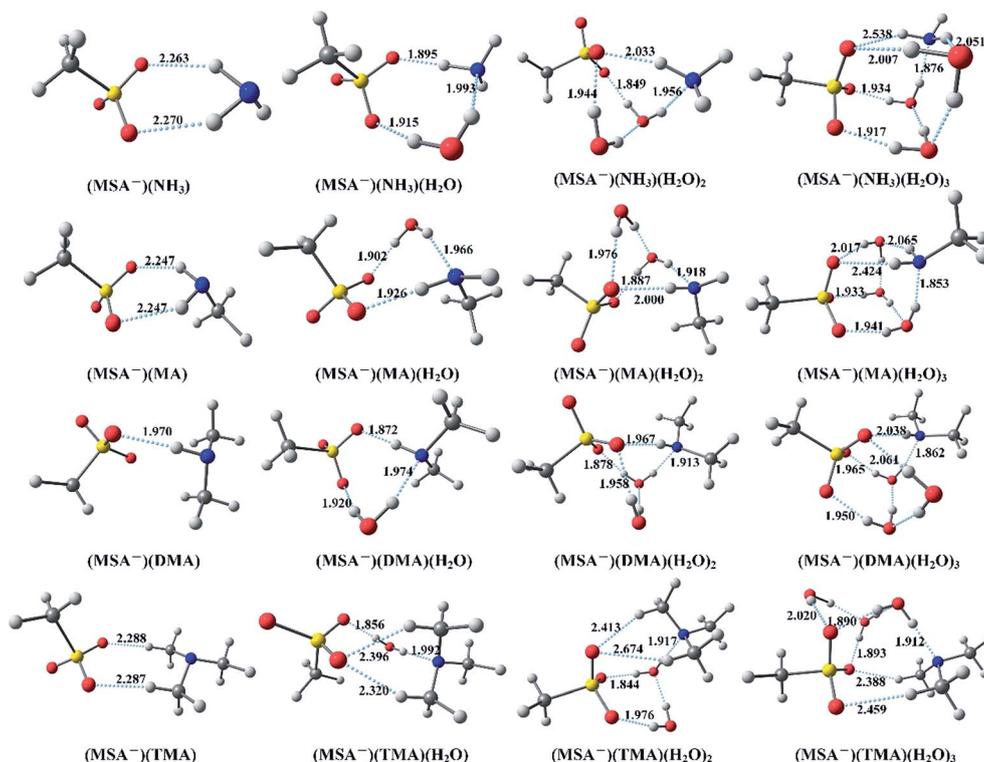


Fig. 1 The global minima for  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ) optimized at the PW91PW91/6-311++G(3df,3pd) level.

$\text{MSA}^-$  and the  $\text{NH}_3/\text{amines}$ . The ammonia/amines and the  $(\text{H}_2\text{O})_2$  dimer form several hydrogen bonds with the  $\text{SO}_3$  group of  $\text{MSA}^-$ . However, the  $\text{CH}_3$  group of  $\text{MSA}^-$  could be ignored in the cluster conformation. For the trihydrate of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})$ , the  $(\text{H}_2\text{O})_3$  trimer, the  $\text{SO}_3$  group and ammonia/amines are combined with about eight hydrogen bonds to form an approximate cubic stable structure.

### 3.2 Analysis of noncovalent interactions

In the  $(\text{MSA}^-)(\text{NH}_3/\text{amines})$  dimers, the  $\text{NH}_3$  or amine binds to the  $\text{MSA}^-$  with one or more hydrogen bonds. According to the structural results, the DMA can possibly form more stable clusters than the other  $\text{NH}_3/\text{amines}$  with  $\text{MSA}^-$ , but the details are lacking and need further investigation. "Atoms in Molecules (AIM)" has been regarded as one of the most efficient tools to explore the intermolecular interactions, such as hydrogen bonds.<sup>78–82</sup> In this study, the topological analysis of electron density at bond critical points (BCPs), which provides evidence for the existence of the hydrogen bonds and deepens the nature of the intermolecular hydrogen bond in the compounds, is analyzed with the AIM methodology to discuss the interactions between the  $\text{MSA}^-$  and  $\text{NH}_3$  or different amines. For the investigation of the topological characteristics at the bond critical point, the electron density ( $\rho$ ), its Laplacian ( $\nabla^2\rho$ ), the electronic energy density ( $H$ ), the electronic kinetic energy density ( $G$ ), and the electronic potential energy density ( $V$ ) are presented in Table 3.

As shown in Table 3, the electronic densities in intermolecular hydrogen bonds are from 0.0132 to 0.0254 a.u. for the

$(\text{MSA}^-)(\text{NH}_3/\text{amines})$  dimers, which are in the accepted range for a hydrogen bond of (0.0070 to 0.0302) a.u. The value of electronic density indicates the strength of the hydrogen bond.<sup>83,84</sup> The larger the value of  $\rho$ , the stronger the hydrogen bond is. From Table 3, we found that the order of the  $\rho$  value for the dimers is  $(\text{MSA}^-)(\text{DMA}) > (\text{MSA}^-)(\text{MA}) > (\text{MSA}^-)(\text{NH}_3) > (\text{MSA}^-)(\text{TMA})$ , indicating the bond strength. Their corresponding positive  $\nabla^2\rho$  values imply the closed-shell system interactions in all dimers, which are hydrogen bonding, ionic interactions or van der Waals forces, rather than a covalent bond. Their values of  $\nabla^2\rho$  are also in the general range of 0.024 to 0.139 a.u. for a hydrogen bond.<sup>85,86</sup> The strongest and weakest hydrogen bonds are found in the  $(\text{MSA}^-)(\text{DMA})$  and  $(\text{MSA}^-)(\text{TMA})$  dimers, respectively, in view of their  $\nabla^2\rho$  values. Furthermore, the electronic energy density ( $H$ ) is viewed as an important index to explore the non-covalent interaction. The positive  $H$  values show that these  $(\text{MSA}^-)(\text{NH}_3/\text{amines})$  dimers are basically electrostatic in closed-shell system interactions, while the interaction is predominantly covalent in the case of  $H < 0$ . The value of  $-G/V$  is used to determine whether the regions correspond to covalent or noncovalent interactions. The  $-G/V$  values are larger than 1 in Table 3, showing that the interaction for all the dimers are noncovalent. On the other hand, the smaller the value of  $-G/V$ , the stronger the hydrogen bond is. Thus, the intermolecular hydrogen bond interaction between  $\text{MSA}^-$  and DMA is the strongest.

The noncovalent interaction (NCI) index, which is based on the relationship between the electron density and the reduced density gradient, has been mentioned as an extension of AIM by



**Table 3** Topological parameters at intermolecular bond critical points of all (MSA<sup>-</sup>)(NH<sub>3</sub>/amines) dimers at the PW91PW91/6-311++G(3df,3pd) level

Parameter	(MSA <sup>-</sup> )(NH <sub>3</sub> )	(MSA <sup>-</sup> )(MA)	(MSA <sup>-</sup> )(DMA)	(MSA <sup>-</sup> )(TMA)
$\rho/\text{a.u.}$	0.0134/0.0141	0.0148/0.0148	0.0254	0.0132/0.0132
$\nabla^2\rho/\text{a.u.}$	0.0451/0.0457	0.0477/0.0477	0.0804	0.0423/0.0423
$H/\text{a.u.}$	0.0014/0.0014	0.0014/0.0014	0.0008	0.0014/0.0014
$G/\text{a.u.}$	0.0099/0.0100	0.0105/0.0105	0.0193	0.0091/0.0091
$V/\text{a.u.}$	-0.0086/-0.0087	-0.0091/-0.0091	-0.0185	-0.0077/-0.0077
$-G/V$	1.1511/1.1494	1.1538/1.1538	1.0432	1.1818/1.1818

Yang and coworkers.<sup>79</sup> The reduced density gradient (RDG),  $s$ , in DFT as a fundamental dimensionless quantity was calculated to reveal the deviation from a homogeneous electron distribution:

$$s = \frac{1}{2(3\pi^2)^{1/3}} \frac{|\nabla\rho|}{\rho^{4/3}} \quad (1)$$

where  $\nabla$  is the gradient operator and  $|\nabla\rho|$  is the electronic density gradient mode. According to the previous studies, the NCI index is a practical tool to identify and visualize the non-covalent interactions as regions of real space, therefore, it is useful to compare the ability of intermolecular hydrogen bond interactions between MSA<sup>-</sup> and NH<sub>3</sub> or different amines.

Plots of the RDG ( $s$ ) vs. the electron density ( $\rho$ ) multiplied by the sign of the second Hessian eigenvalue ( $\lambda_2$ ) for the (MSA<sup>-</sup>)(NH<sub>3</sub>), (MSA<sup>-</sup>)(MA), (MSA<sup>-</sup>)(DMA), and (MSA<sup>-</sup>)(TMA) dimers is shown in Fig. 2 using the Multiwfn program. The reduced gradient spikes in the low densities indicate the existence of the stabilizing interactions of noncovalent bonding. For the (MSA<sup>-</sup>)(DMA) dimer, there is only one low-reduced gradient spike at low density of the  $\text{sign}(\lambda_2)\rho$  value of  $-0.0254$  a.u., showing a stable hydrogen bond interaction. From (MSA<sup>-</sup>)(NH<sub>3</sub>) to (MSA<sup>-</sup>)(MA), and to (MSA<sup>-</sup>)(TMA), the characteristic peaks directed toward the  $\text{sign}(\lambda_2)\rho$  values are very near zero, which are  $-0.0134/-0.0141$ ,  $-0.0148/-0.0148$  and  $-0.0132/-0.0132$ , respectively, indicative of the relatively weak hydrogen bond interactions between the MSA<sup>-</sup> and the NH<sub>3</sub> or the corresponding amines. In the case of (MSA<sup>-</sup>)(MA), (MSA<sup>-</sup>)(NH<sub>3</sub>) and (MSA<sup>-</sup>)(TMA), although the number of peaks is more than one, their locations are so close that only one spike is seen for each dimer in Fig. 2. The characteristic peaks directed toward  $\text{sign}(\lambda_2)\rho$  values larger than the hydrogen bond interaction is weaker, therefore, the hydrogen bond interactions become weaker from (MSA<sup>-</sup>)(MA) to (MSA<sup>-</sup>)(NH<sub>3</sub>), and to (MSA<sup>-</sup>)(TMA).

Fig. 2 also shows that there exists a bonding isosurface between the middle region of the MSA<sup>-</sup> and NH<sub>3</sub>/amines. From the (MSA<sup>-</sup>)(TMA) to (MSA<sup>-</sup>)(NH<sub>3</sub>), to (MSA<sup>-</sup>)(MA), and to (MSA<sup>-</sup>)(DMA), the color coding of these bonding isosurfaces is from green to blue, which demonstrates that the stability order of the hydrogen bonding interactions for different dimers is (MSA<sup>-</sup>)(DMA) > (MSA<sup>-</sup>)(MA) > (MSA<sup>-</sup>)(NH<sub>3</sub>) > (MSA<sup>-</sup>)(TMA). The reduced gradient isosurface ( $s = 0.05$  au) obtained by the VMD program<sup>87</sup> agrees well with the analysis of the scatter plots above.

### 3.3 Thermodynamics of the cluster formation

Thermodynamic analysis provides a significant method to investigate the possibility of cluster formation. Gibbs free

energy changes are effective for evaluating the strength of the intermolecular interaction and the spontaneity of the process of the cluster formation,<sup>28</sup> and are therefore used to understand the interaction of methanesulfonate with NH<sub>3</sub> or amine and their hydration. The relative single-point energies,  $\Delta E$  (0 K), of the (MSA<sup>-</sup>)(NH<sub>3</sub>)(H<sub>2</sub>O)<sub>*n*</sub> ( $n = 0-3$ ) clusters are calculated using the following eqn (2) and (3). The intermolecular enthalpy,  $\Delta H$  (298.15 K), and the Gibbs free energy,  $\Delta G$  (298.15 K), are obtained in the same way for all the systems:

$$\Delta E = E_{(\text{MSA}^-)(\text{NH}_3)} - E_{\text{MSA}^-} - E_{\text{NH}_3} \quad (2)$$

$$\Delta E = E_{(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_n} - E_{(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_{n-1}} - E_{\text{H}_2\text{O}} \quad (3)$$

where  $E$  is the total energy of monomers and hydrates. The values of  $\Delta E$  (0 K),  $\Delta H$  (298.15 K) and  $\Delta G$  (298.15 K) of the global minima for the (MSA<sup>-</sup>)(NH<sub>3</sub>/amines)(H<sub>2</sub>O)<sub>*n*</sub> ( $n = 0-3$ ) structures (in kcal mol<sup>-1</sup>) are displayed in Table 4.

The relative single-point energy at 0 K of MSA<sup>-</sup> with NH<sub>3</sub> ( $-7.67$  kcal mol<sup>-1</sup>) is much weaker than that with MA ( $-9.04$  kcal mol<sup>-1</sup>) and DMA ( $-10.26$  kcal mol<sup>-1</sup>), while a little stronger than that with TMA ( $-6.39$  kcal mol<sup>-1</sup>), shown in Table 4. The temperature effect is taken into account to acquire the thermochemical properties of the clusters under atmospheric conditions. At 298.15 K, the interaction of MSA<sup>-</sup> with NH<sub>3</sub>/amines and their hydrates contain the contributions from the translational, rotational and vibrational energies, and the thermodynamics of clusters are with regard to enthalpies and entropies. Even if the enthalpies or the entropies are considered, the interaction of MSA<sup>-</sup> with DMA is still the strongest, followed by MA, NH<sub>3</sub> and TMA. The enthalpy changes of the reactions are  $-9.68$ ,  $-8.51$ ,  $-7.51$  and  $-5.71$  kcal mol<sup>-1</sup>, and the Gibbs free energy changes are  $-1.68$ ,  $-1.14$ ,  $-0.45$  and  $1.90$  kcal mol<sup>-1</sup> for (MSA<sup>-</sup>)(DMA), (MSA<sup>-</sup>)(MA), (MSA<sup>-</sup>)(NH<sub>3</sub>) and (MSA<sup>-</sup>)(TMA), respectively.

The thermodynamic properties of hydrates are also shown in Table 4. For the (MSA<sup>-</sup>)(NH<sub>3</sub>)(H<sub>2</sub>O)<sub>*n*</sub> ( $n = 1-3$ ) system, the formation of (MSA<sup>-</sup>)(NH<sub>3</sub>) hydrates by the stepwise addition of water is exothermic by  $11.78-12.39$  kcal mol<sup>-1</sup>. For the clusters formed by the (MSA<sup>-</sup>)(MA) dimer and one to three waters,  $11.41-12.86$  kcal mol<sup>-1</sup> is released. The formation of the clusters containing the (MSA<sup>-</sup>)(DMA) dimer and one to three waters is exothermic by  $11.21-13.07$  kcal mol<sup>-1</sup>, and  $11.53-14.23$  kcal mol<sup>-1</sup> is released during the formation of the (MSA<sup>-</sup>)(TMA)(H<sub>2</sub>O)<sub>*n*</sub> ( $n = 1-3$ ) clusters. The Gibbs free energies of the formation of hydrates are in the range of about  $-1$  to  $-4$  kcal mol<sup>-1</sup>. The favorable free energies of formation for the



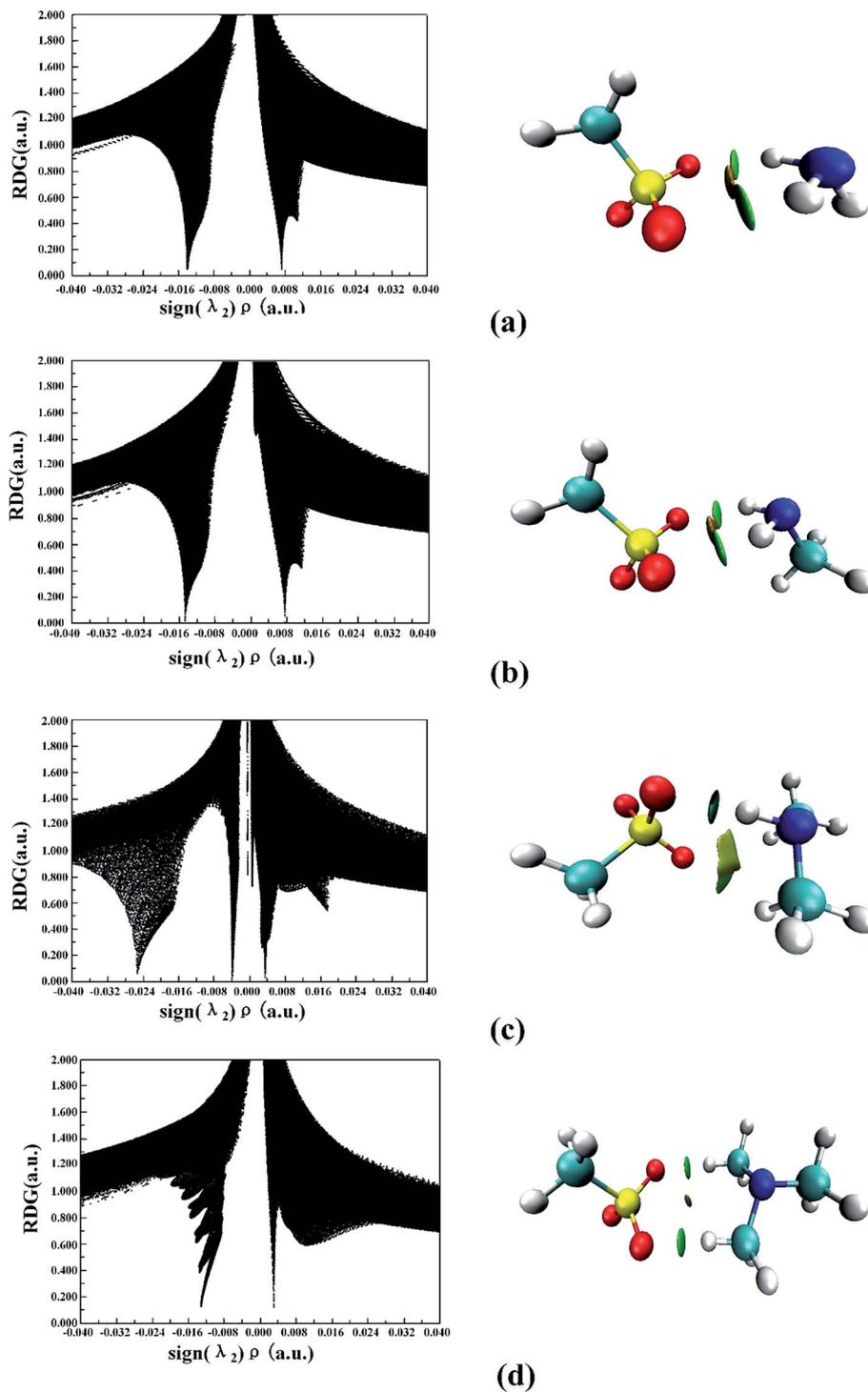


Fig. 2 Noncovalent interactions (NCI) analysis among the global minima for  $(\text{MSA}^-)(\text{NH}_3)$  (a),  $(\text{MSA}^-)(\text{MA})$  (b),  $(\text{MSA}^-)(\text{DMA})$  (c),  $(\text{MSA}^-)(\text{TMA})$  (d).

$(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 1-3$ ) clusters at 298.15 K predicted that  $\text{MSA}^-$  can contribute to the aerosol nucleation process by binding to  $\text{NH}_3/\text{amines}$  and water until  $n = 3$ . From the  $\Delta G$  values, we also find that the initial formation of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})$  monohydrate is highly favorable. However, entropic effects may limit the stepwise addition of more water, and the subsequent addition of water molecules to an existing monohydrate is less thermodynamically favorable.

Moreover, the  $\Delta G$  values of the global minima for the  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ) clusters increase with increasing the temperature from 260 K to 300 K in Table 5, which shows that the stability of the clusters decreases with the increasing temperature. In other words, the clusters discussed in this study might be more favorable in the conditions of lower temperatures.



**Table 4** Energy changes associated with the formation of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ). The energies are in  $\text{kcal mol}^{-1}$ , and were calculated at the DF-LMP2-F12/VDZ-F12//PW91PW91/6-311++G(3df,3pd) level of theory

Reaction	$\Delta E$ (0 K)	$\Delta H$ (298.15 K)	$\Delta G$ (298.15 K)
$\text{MSA}^- + \text{NH}_3 \leftrightarrow (\text{MSA}^-)(\text{NH}_3)$	-7.67	-7.51	-0.45
$(\text{MSA}^-)(\text{NH}_3) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})$	-12.24	-13.31	-2.56
$(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_2$	-12.39	-13.29	-3.27
$(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_2 + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_3$	-11.78	-12.96	-1.51
$\text{MSA}^- + \text{MA} \leftrightarrow (\text{MSA}^-)(\text{MA})$	-9.04	-8.51	-1.14
$(\text{MSA}^-)(\text{MA}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{MA})(\text{H}_2\text{O})$	-12.86	-13.88	-3.16
$(\text{MSA}^-)(\text{MA})(\text{H}_2\text{O}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{MA})(\text{H}_2\text{O})_2$	-12.36	-13.25	-2.63
$(\text{MSA}^-)(\text{MA})(\text{H}_2\text{O})_2 + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{MA})(\text{H}_2\text{O})_3$	-11.41	-12.46	-1.85
$\text{MSA}^- + \text{DMA} \leftrightarrow (\text{MSA}^-)(\text{DMA})$	-10.26	-9.68	-1.68
$(\text{MSA}^-)(\text{DMA}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})$	-13.07	-13.99	-3.49
$(\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})_2$	-12.47	-13.32	-3.30
$(\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})_2 + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})_3$	-11.21	-12.14	-1.16
$\text{MSA}^- + \text{TMA} \leftrightarrow (\text{MSA}^-)(\text{TMA})$	-6.39	-5.71	1.90
$(\text{MSA}^-)(\text{TMA}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})$	-14.23	-15.08	-4.43
$(\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_2$	-12.68	-13.54	-3.19
$(\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_2 + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_3$	-11.53	-12.41	-2.04

**Table 5** Stepwise binding free energies ( $\Delta G$ ) for the formation of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ) with the various temperatures of 260 K, 280 K and 300 K. The energies are in  $\text{kcal mol}^{-1}$ , and were calculated at the DF-LMP2-F12/VDZ-F12//PW91PW91/6-311++G(3df,3pd) level of theory

Reaction	$\Delta G$ (260 K)	$\Delta G$ (280 K)	$\Delta G$ (300 K)
$\text{MSA}^- + \text{NH}_3 \leftrightarrow (\text{MSA}^-)(\text{NH}_3)$	-1.35	-0.87	-0.40
$(\text{MSA}^-)(\text{NH}_3) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})$	-3.93	-3.21	-2.49
$(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_2$	-4.54	-3.87	-3.20
$(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_2 + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_3$	-2.97	-2.20	-1.43
$\text{MSA}^- + \text{MA} \leftrightarrow (\text{MSA}^-)(\text{MA})$	-2.09	-1.59	-1.09
$(\text{MSA}^-)(\text{MA}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{MA})(\text{H}_2\text{O})$	-4.53	-3.81	-3.09
$(\text{MSA}^-)(\text{MA})(\text{H}_2\text{O}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{MA})(\text{H}_2\text{O})_2$	-3.99	-3.27	-2.56
$(\text{MSA}^-)(\text{MA})(\text{H}_2\text{O})_2 + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{MA})(\text{H}_2\text{O})_3$	-3.20	-2.49	-1.78
$\text{MSA}^- + \text{DMA} \leftrightarrow (\text{MSA}^-)(\text{DMA})$	-2.71	-2.16	-1.62
$(\text{MSA}^-)(\text{DMA}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})$	-4.83	-4.12	-3.42
$(\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})_2$	-4.58	-3.91	-3.23
$(\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})_2 + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})_3$	-2.56	-1.82	-1.09
$\text{MSA}^- + \text{TMA} \leftrightarrow (\text{MSA}^-)(\text{TMA})$	0.92	1.44	1.95
$(\text{MSA}^-)(\text{TMA}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})$	-5.79	-5.07	-4.36
$(\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O}) + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_2$	-4.51	-3.81	-3.12
$(\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_2 + \text{H}_2\text{O} \leftrightarrow (\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_3$	-3.36	-2.66	-1.97

### 3.4 Atmospheric relevance

In view of the results and analysis of geometry, noncovalent interactions and thermodynamics discussed above, it has been found that the  $\text{MSA}^-$  could form more stable clusters with amines (especially DMA and MA) than  $\text{NH}_3$ . However, this does not imply that the amines are more important for the atmospheric nucleation, compared with  $\text{NH}_3$ , and their difference in concentrations should be included. Whether the enhancement in stability due to amines could be large enough to overcome the difference in typical atmospheric concentrations of  $\text{NH}_3$  and amines is poorly understood and needs to be further researched. The exact values depend on the initial concentrations of  $\text{NH}_3$  and amines.

The earlier studies show that the amines are more easily oxidized by OH than  $\text{NH}_3$ , resulting in a much higher

concentration of  $\text{NH}_3$  than that of amine by at least two orders of magnitude.<sup>88</sup> The typical concentrations of  $\text{NH}_3$  are in the range of 0.1–10 ppb in the continental air, meaning that the amine concentrations are about 1–100 ppt. Sellegri *et al.*<sup>89</sup> concluded that the trimethylamine concentrations are from 34 to 80 ppt during a spring measurement campaign in Hyytiälä, Finland, which is close to the estimation above. However, higher amine concentrations have been reported at a number of sites in the boundary layer recently, *i.e.*, the concentrations for some amines are more than 100 ppb in the vicinity of a dairy farm in California, based on the investigation by Rabaud *et al.*<sup>90</sup> Nevertheless, the concentration of  $\text{NH}_3$  should be obviously higher than the amines in most cases.

From the law of mass balance, the ratio of the concentrations of  $\text{NH}_3$ -containing to DMA-containing clusters is defined by the following:



$$\frac{[(\text{MSA}^-)(\text{NH}_3)]}{[(\text{MSA}^-)(\text{DMA})]} = \frac{[\text{NH}_3]}{[\text{DMA}]} e^{\frac{-\Delta\Delta G}{RT}} \quad (4)$$

where  $[\text{NH}_3]$ ,  $[\text{DMA}]$ ,  $[(\text{MSA}^-)(\text{NH}_3)]$  and  $[(\text{MSA}^-)(\text{DMA})]$  are the concentrations of different monomers and dimers,  $R$  is the molar gas constant,  $T$  is the temperature in kelvin and  $\Delta\Delta G$  is the difference in free energies of formation for the  $(\text{MSA}^-)(\text{NH}_3)$  and the  $(\text{MSA}^-)(\text{DMA})$  dimers.

According to the eqn (4) and the free energies, we have calculated the ratio of the concentrations of  $(\text{MSA}^-)(\text{NH}_3)$  to  $(\text{MSA}^-)(\text{DMA})$  dimer as a function of the gas-phase concentration ratio of  $\text{NH}_3$  to DMA. The results are given in Table 6. We found that the ratio of  $\text{NH}_3$  and DMA concentrations is only 10 : 1, and the concentration of  $(\text{MSA}^-)(\text{NH}_3)$  is equal to that of the  $(\text{MSA}^-)(\text{DMA})$  dimer. When the ratio is increased to 100 : 1 and 1000 : 1, correspondingly,  $(\text{MSA}^-)(\text{NH}_3)$  concentrations are at one and two orders of magnitude higher than those of  $(\text{MSA}^-)(\text{DMA})$ . Chen *et al.*<sup>45,46</sup> have indicated that the neutral MSA contributes to NPF with the reaction of amines/ $\text{NH}_3$  and water. MSA tends to form particles with amines rather than  $\text{NH}_3$ , and the particle formation rates of amines with MSA are 2–3 orders of magnitude higher than that of  $\text{NH}_3$ , but the concentrations of amines are 1–3 orders of magnitude lower compared to those of ammonia. Therefore, although the amines have relatively low concentrations in the actual atmosphere, it is considered as a significant role in NPF. Kurtén *et al.*<sup>27</sup> investigated the structure and thermodynamics of the dimers of  $\text{H}_2\text{SO}_4$  or  $\text{HSO}_4^-$  with  $\text{NH}_3$  and amines, and found that the  $(\text{H}_2\text{SO}_4)(\text{NH}_3/\text{amine})$  complexes are more stable than the  $(\text{HSO}_4^-)(\text{NH}_3/\text{amine})$ . Moreover, the  $(\text{H}_2\text{SO}_4)(\text{amine})$  cluster is remarkably stronger than that of  $(\text{H}_2\text{SO}_4)(\text{NH}_3)$ , while the  $(\text{HSO}_4^-)(\text{amine})$  is a little stronger than  $(\text{HSO}_4^-)(\text{NH}_3)$ . The greater stability of the  $(\text{H}_2\text{SO}_4)(\text{amine})$  or  $(\text{HSO}_4^-)(\text{amine})$  cluster compared to those with  $\text{NH}_3$  does overcome the difference in concentration. However, for  $\text{MSA}^-$ , the advantage of amines in  $\Delta G$  contributes to ten times stronger stabilizing effects than  $\text{NH}_3$  with  $\text{MSA}^-$ . The stabilizing effect could be determined by two factors, which are the stepwise Gibbs free energy changes and the concentration ratios of amines with respect to  $\text{NH}_3$ . If the  $\text{NH}_3$  concentrations are more than one order of magnitude higher than that of DMA, the enhancement in stability due to amines appears not to be large enough to overcome the difference in the concentrations of  $\text{NH}_3$  and amines.

In this work, the method for calculating the concentration of clusters is only a limited and simplistic approximation; the situation in the atmosphere is actually much more complicated. Eqn (4) presumes a pseudo-steady-state situation, in which the

formation of clusters does not significantly exhaust the gas-phase reservoir of reactant molecules. Unfortunately, in the actual condition, the formation of  $\text{MSA}^-$ -amine clusters depletes the amine reservoir quickly, and then the steady-state conditions in eqn (4) will not apply. However, it could be a valid way to get a qualitative assessment of how important the various clusters are in their formations, and compare their different contributions to the aerosol nucleation. A quantitatively precise result of the relative importance of amine-containing and  $\text{NH}_3$ -containing clusters in the atmosphere would not only rely on much more accurate concentration data of  $\text{NH}_3$  and amines, but also the reliable kinetic nucleation simulations, which should be acquired in further studies.

### 3.5 Influences of humidity and temperature on hydrate distributions

For the hydrates, the water molecules could easily bind to the  $(\text{MSA}^-)(\text{NH}_3/\text{amines})$  core based on the favorable stepwise free energies of formation of the  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ) clusters except for the  $(\text{MSA}^-)(\text{TMA})$  dimer in Table 4, to promote the aerosol formation process. However, the binding number of water molecules in the clusters could be affected by the various relative humidities (RHs). To get further results, the hydrate distributions of non-aqueous “cores” ( $(\text{MSA}^-)(\text{NH}_3/\text{amines})$  heterodimer) were estimated at various RHs in Fig. 3(a).<sup>32,91</sup>

For the  $(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_n$  ( $n = 0-3$ ) system, 44% of  $(\text{MSA}^-)(\text{NH}_3)$  is non-hydrated at 20% RH, but that number decreases to 13% and 5% at 50% RH and 80% RH, respectively. The most common hydrated cluster is always the dihydrate, and its population increases from 32% to 60% and to 64% throughout the RH range from 20% to 80%, but the second hydrated cluster is changed with the various RH, which is the monohydrate at the RH = 20% and 50%, and the trihydrate at the RH = 80%. For  $(\text{MSA}^-)(\text{MA})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ), the number of hydrates gets to 96% at the RH of 80%. The most abundant cluster in this system is the monohydrate at RH = 20%, which is replaced by the dihydrate if the RH is more than 50%. The peak of the cluster distribution moves from the monohydrate cluster to the dihydrate. The most common cluster is the dihydrate for the DMA-containing and TMA-containing systems. In  $(\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})_n$ , the content of  $(\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})_2$  is the largest and increases with the increasing RH. When the RH gets to 80%, the  $(\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})_2$  accounts for 74% of the total amount. For  $(\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_n$ , the total concentration of  $(\text{MSA}^-)(\text{TMA})$  was mainly dispersed into the  $(\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_2$  and  $(\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_3$  clusters, and these two clusters occupy 83% of all the  $(\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_n$  clusters at RH = 50%, which is 90% at RH = 80%. In this case, the trihydrate content increases, and the number reaches 40% at the RH of 80%, although a little less than the dihydrate.

The obvious sensitivity of hydrate distributions to relative humidity can be seen through the results in Fig. 3(a) as we previously determined,<sup>35</sup> where the degree of change for hydrate distributions varies according to the different systems. The unhydrated cluster dominates only when the relative humidity

**Table 6** Ratio of concentrations of clusters for  $(\text{MSA}^-)(\text{NH}_3)$  to  $(\text{MSA}^-)(\text{DMA})$ , as a function of the  $\text{NH}_3$  to DMA concentration ratio

$[\text{NH}_3]/[\text{DMA}]$ ratio	$[(\text{MSA}^-)(\text{NH}_3)]/[(\text{MSA}^-)(\text{DMA})]$ ratio
10	1.243
100	12.43
1000	124.3



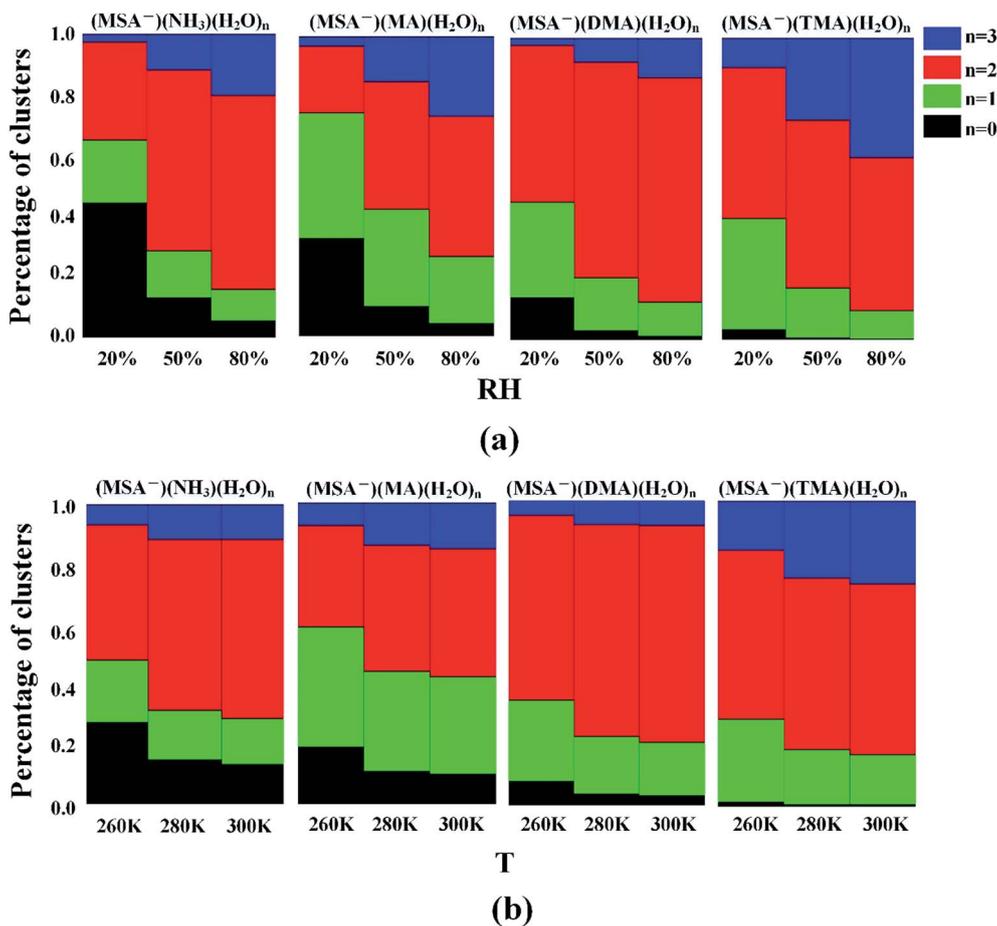


Fig. 3 Hydrate distributions of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0-3$ ) clusters at three different relative humidities (RHs) with the temperature of 298.15 K (a), and three different temperatures with the RH of 50% (b).

is very low. Once the RH reaches 50%, more than 87% of clusters are hydrated in all the cases, and the population is nearly 100% for the  $(\text{MSA}^-)(\text{DMA})$  and  $(\text{MSA}^-)(\text{TMA})$ . With the increasing humidities, the number of monohydrates is lower, which contributes to the enhanced content of dihydrate and trihydrate. This denotes that the increasing RH not only promotes the formation of hydrates, but also the larger hydrates, such as the dihydrate and the trihydrate in our study.

According to the earlier studies, the variation of temperature is another factor impacting the hydrate distributions.<sup>35</sup> As shown in Table 5, there is a strong temperature dependence of the Gibbs free energies of stepwise hydration, which affects the formation of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  hydrates. The study in Fig. 3(b) suggests that the higher temperature favors the formation of dihydrate and trihydrate, compared with nonhydrate and monohydrate. For the temperature range of 260 K to 280 K, the obvious variation of hydration distribution is seen from Fig. 3(b), and the change is relatively slow from  $T = 280$  K to 300 K. The general trend is that the dihydrate and trihydrate contents increase, while the number of nonhydrates and monohydrates decrease with higher temperature in the systems. The effect of temperature mainly results from the change of  $\Delta G$  and the saturation vapor pressure of water vapor from the temperature of 260 K to 300 K.

### 3.6 Evaporation rates

Previous studies revealed that the cluster evaporation rates based on the formation free energy obtained by quantum chemical calculation is a significant parameter for understanding the very early stages of particle formation.<sup>30,92</sup> As shown in Fig. 4, for all the unhydrated clusters, the evaporation rates of  $\text{MSA}^-$  are as large as  $10^9-10^{11} \text{ s}^{-1}$  for  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$ . When one water molecule is added to the dimers, the evaporation of  $\text{MSA}^-$  is significantly reduced by about three orders of magnitude. The  $\text{MSA}^-$  evaporation continues dropping from  $10-10^3 \text{ s}^{-1}$  to nearly zero with the increasing water molecules from  $n = 2$  to 3. The evaporation of  $\text{NH}_3/\text{amines}$  in Fig. 4 changes in a different way compared to  $\text{MSA}^-$  with the various water molecules. Once the clusters are hydrated, the evaporation has an obvious increase from  $10^9-10^{11} \text{ s}^{-1}$  to about  $10^{11}-10^{12} \text{ s}^{-1}$ . The change in evaporation rate for water is different for the different systems. In the  $(\text{MSA}^-)(\text{MA})(\text{H}_2\text{O})_n$ ,  $(\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})_n$  and  $(\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_n$  clusters, they increase monotonically with the added water; in particular, its evaporation rate is close to the DMA evaporation for the  $(\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})_n$  clusters at  $n = 3$ . There is a little difference in the  $(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_n$  clusters where the change is non-monotonic, however, the water evaporation



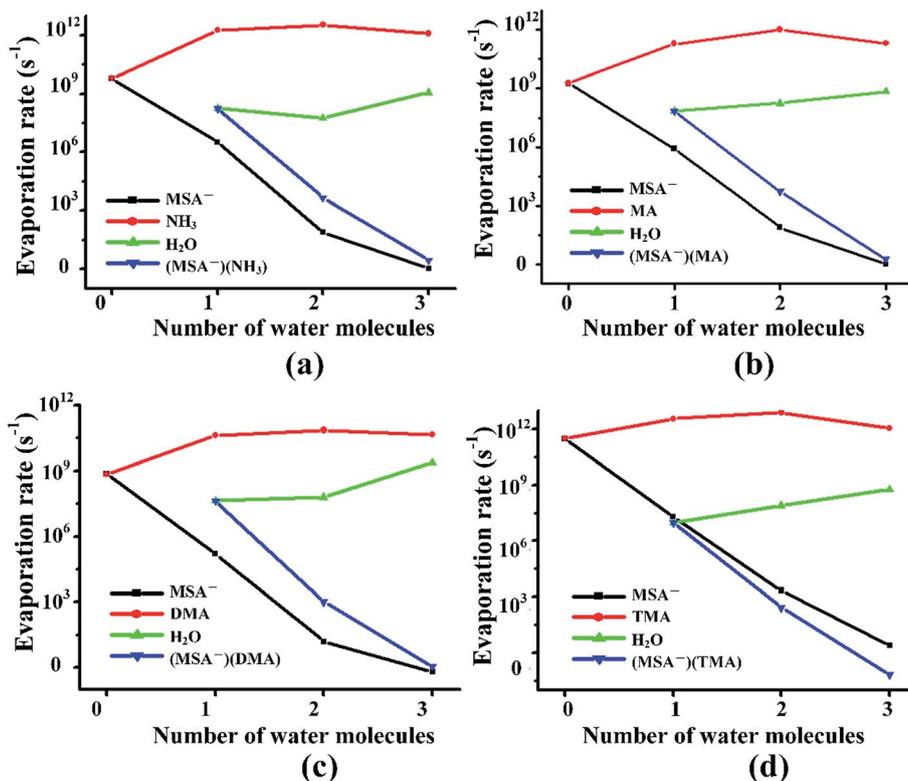


Fig. 4 Evaporation rates of  $MSA^{-}$ ,  $NH_3$ /amines,  $H_2O$  and  $(MSA^{-})(NH_3)$ /amines from  $(MSA^{-})(NH_3)(H_2O)_n$  ( $n = 0-3$ ) clusters (a),  $(MSA^{-})(MA)(H_2O)_n$  ( $n = 0-3$ ) clusters (b),  $(MSA^{-})(DMA)(H_2O)_n$  ( $n = 0-3$ ) clusters (c) and  $(MSA^{-})(TMA)(H_2O)_n$  ( $n = 0-3$ ) clusters (d), respectively.

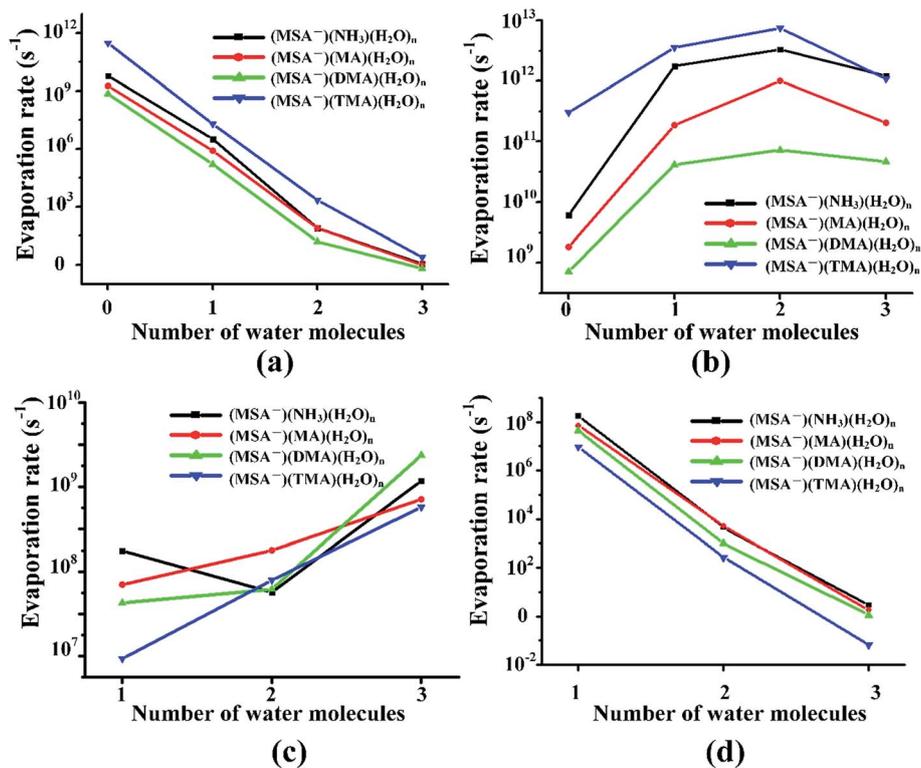


Fig. 5 Evaporation rates from the  $(MSA^{-})(NH_3)$ /amines/ $(H_2O)_n$  ( $n = 0-3$ ) clusters. The top left (a), top right (b), bottom left (c) and bottom right (d) panels give the results for evaporation of  $MSA^{-}$ ,  $NH_3$ /MA/DMA/TMA,  $H_2O$  and  $(MSA^{-})(NH_3)$ / $(MSA^{-})(MA)$ / $(MSA^{-})(DMA)$ / $(MSA^{-})(TMA)$ , respectively.



increases more or less with the addition of more water in general. The evaporation of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})$  decreases rapidly with the addition of one to three water molecules in the  $(\text{MSA}^-)(\text{NH}_3/\text{amines})$  hydrates. In the  $(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_n$ ,  $(\text{MSA}^-)(\text{MA})(\text{H}_2\text{O})_n$  and  $(\text{MSA}^-)(\text{DMA})(\text{H}_2\text{O})_n$  clusters, the order of evaporation rate is  $\text{NH}_3/\text{amines} > \text{H}_2\text{O} > (\text{MSA}^-)(\text{NH}_3/\text{amines}) > \text{MSA}^-$ . However, the order is changed in  $(\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_n$  where the evaporation of  $(\text{MSA}^-)(\text{TMA})$  is even less than  $\text{MSA}^-$ , and the gap is enhanced with more water.

In the different systems containing  $\text{MSA}^-$ ,  $\text{NH}_3/\text{amines}$  and several waters, the  $\text{MSA}^-$  in Fig. 5(a) gets a marked drop in the evaporation rate from  $10^9$ – $10^{12} \text{ s}^{-1}$  at  $n = 0$  to nearly zero at  $n = 3$ . The evaporation rate order of  $\text{MSA}^-$  is the sequence of  $(\text{MSA}^-)(\text{TMA}) > (\text{MSA}^-)(\text{NH}_3) > (\text{MSA}^-)(\text{MA}) > (\text{MSA}^-)(\text{DMA})$ . For the larger hydrates containing three waters, the  $\text{MSA}^-$  evaporation rate for the different systems is close to zero, which indicates that the evaporation of  $\text{MSA}^-$  could be ignored with the addition of more water. The order of evaporation of  $\text{NH}_3/\text{amines}$  in Fig. 5(b) is also  $(\text{MSA}^-)(\text{TMA}) > (\text{MSA}^-)(\text{NH}_3) > (\text{MSA}^-)(\text{MA}) > (\text{MSA}^-)(\text{DMA})$ , consistent with the results of  $\text{MSA}^-$ . The evaporation number increases as the water molecules increase until  $n = 2$  as the turning point. In Fig. 5(c), except for the  $(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_n$  ( $n = 0$ – $3$ ), the water evaporation increases from  $n = 1$  to 3. In the  $(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_n$  clusters, the evaporation rate of  $n = 2$  is the lowest point. The results could be proved by the analysis of  $\Delta G$ , shown in Table 4, in which the stability order of hydrates is  $(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_2 > (\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O}) > (\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_3$ , and  $(\text{MSA}^-)(\text{NH}_3)(\text{H}_2\text{O})_2$  is the most stable cluster in this system. In addition to the evaporation of monomers, we also investigated the cluster fission, as shown in Fig. 5(d). Our results showed that the value of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0$ – $3$ )  $\rightleftharpoons$   $(\text{MSA}^-)(\text{NH}_3/\text{amines}) + (\text{H}_2\text{O})_n$  ( $n = 0$ – $3$ ) fission rate is close to the  $\text{MSA}^-$  evaporation rate with respect to the number of water molecules. The  $(\text{MSA}^-)(\text{TMA})$  dimer is unfavorable compared to the  $(\text{MSA}^-)(\text{NH}_3)$ ,  $(\text{MSA}^-)(\text{MA})$  and  $(\text{MSA}^-)(\text{DMA})$  dimer, but it could easily bind to water to form the stable  $(\text{MSA}^-)(\text{TMA})(\text{H}_2\text{O})_n$  hydrates based on the thermodynamic values in Table 4, contributing to the relatively low evaporation of the  $(\text{MSA}^-)(\text{TMA})$  cluster.

Comparing the evaporation rates, we can see that the evaporation reactions of  $\text{NH}_3/\text{amines}$  are more important than the evaporation reactions of the acid ions and water molecules. The presence of water markedly changes the effect of  $\text{MSA}^-$  and  $\text{NH}_3/\text{amines}$  on the evaporation rates. The base molecules and water evaporations increase more or less with the increasing waters, while the  $\text{MSA}^-$  and  $(\text{MSA}^-)(\text{NH}_3/\text{amines})$  evaporations decrease due to the formation of the stable  $\text{MSA}^-$ -containing hydrates. The lifetime of a cluster will be determined by the evaporation rate of the base molecules rather than the others.

## 4. Conclusions

For the  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0$ – $3$ ) clusters, the global minimum was obtained for each sized cluster. We investigated the thermodynamics of hydration of

$(\text{MSA}^-)(\text{NH}_3/\text{amines})$  using high-level DFT calculations, and discussed its implication on atmospheric nucleation.

Multiple strong hydrogen bonds are formed in the  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0$ – $3$ ) complexes to promote the cluster formation. Due to the acid–base reactions that are expected to give birth to neutral or charged clusters that have relevance for NPF,  $\text{MSA}^-$  probably forms clusters with  $\text{NH}_3$  or amines in the atmosphere. The favorable stepwise free energies of formation for the hydrates at 298.15 K suggest that  $\text{MSA}^-$ , acting as a stabilizer of small clusters, can contribute to the nucleation process by binding with  $\text{NH}_3$  or different amines and water until  $n = 3$ .

The stability order for the  $\text{MSA}^-$  – base dimers is  $(\text{MSA}^-)(\text{DMA}) > (\text{MSA}^-)(\text{MA}) > (\text{MSA}^-)(\text{NH}_3) > (\text{MSA}^-)(\text{TMA})$ , according to the analysis of weak attraction, which is in agreement with the results of structures and thermodynamics. Although  $\text{MSA}^-$  could form more stable clusters with amines, compared to  $\text{NH}_3$ , the enhancement in stability for amines cannot be large enough to overcome the difference in the concentrations between  $\text{NH}_3$  and amines under typical atmospheric conditions. It implies that  $(\text{MSA}^-)(\text{NH}_3)$  clusters are more abundant and important in the atmospheric nucleation, compared with  $(\text{MSA}^-)(\text{amines})$ .

There are strong humidity and temperature dependences for the  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  complexes: the higher humidity and temperature promote the formation of hydrates. The populations of larger hydrates, including the dihydrate and trihydrate, are enhanced with the increasing RH and temperature, rather than the monohydrate. From the analysis of evaporation rates, we found that the evaporation reactions of  $\text{NH}_3/\text{amines}$  are more important than the evaporation reactions of the ionic acid and water molecules, which determine the lifetime of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$  ( $n = 0$ – $3$ ). In addition, the presence of water changes the effects of  $\text{MSA}^-$  and  $\text{NH}_3/\text{amines}$  on the evaporation rates markedly.

Based on the study of  $(\text{MSA}^-)(\text{NH}_3/\text{amines})(\text{H}_2\text{O})_n$ , this work tentatively provides a reference for the further investigation of NPF. Further theoretical, experimental and field research are required to investigate the synergy of  $\text{MSA}^-$  and  $\text{NH}_3$  or amines on the nucleation system involving  $\text{H}_2\text{SO}_4$ ,  $\text{MSA}^-$ ,  $\text{NH}_3$ , amines and  $\text{H}_2\text{O}$ , which is beyond the scope of the present paper.

## Conflicts of interest

There are no conflicts to declare.

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