# Dalton Transactions

## PAPER

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**Cite this:** *Dalton Trans.*, 2018, **47**, 429

Received 6th November 2017, Accepted 25th November 2017 DOI: 10.1039/c7dt04178k

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### Introduction

As crucial frequency-conversion components in solid-state lasers, second-order nonlinear optical (NLO) crystals have attracted increasing attention in the fields of civilian and military applications.<sup>1</sup> Until recently, there have been already numerous commercial second-order NLO materials that satis-

## Experimental and theoretical studies on the NLO properties of two quaternary noncentrosymmetric chalcogenides: BaAg<sub>2</sub>GeS<sub>4</sub> and BaAg<sub>2</sub>SnS<sub>4</sub>†

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New middle and far-infrared (MFIR) nonlinear optical (NLO) chalcogenides have been receiving increasing attention for their great importance in military and civil fields. In addition, the current challenge in the efforts for identifying a promising MFIR NLO material lies in achieving simultaneously large second-harmonic generation (SHG) intensity and high laser-induced damage threshold (LIDT) in the same material. In this study, two quaternary non-centrosymmetric (NCS) sulfides,  $BaAg_2GeS_4$  (**1**) and  $BaAg_2SnS_4$  (**2**), were synthesized from a high-temperature solid-state reaction using  $BaCl_2$  flux in evacuated closed silica tubes. Although **1** and **2** show identical stoichiometry, they crystallize in different NCS space groups, tetragonal  $I\overline{4}2m$  (no. 121) and orthorhombic *I*222 (no. 23), respectively, based on the results of crystal structure solution. In their structures, highly distorted AgS<sub>4</sub> tetrahedra interconnect together *via* corner-sharing to form two-dimensional (2D) layers, which are further bridged with isolated GeS<sub>4</sub> or SnS<sub>4</sub> units to produce a three-dimensional (3D) framework structure with Ba cations lying in the tunnels. Remarkably, they not only possess phase-matchable (PM) abilities but also exhibit a good balance between strong SHG responses (1.7× and 0.4× AgGaS<sub>2</sub>) and high LIDTs (3.2× and 1.5× AgGaS<sub>2</sub>). Moreover, theoretical calculations based on density functional theory (DFT) methods have aided the understanding of energy bands, electronic structures, and linear and NLO properties.

fied the practical application requirements in the ultravioletvisible (UV-Vis) and near-infrared (NIR) regions, such as KH<sub>2</sub>PO<sub>4</sub> (KDP),<sup>2</sup>  $\beta$ -BaB<sub>2</sub>O<sub>4</sub> (BBO),<sup>3</sup> LiB<sub>3</sub>O<sub>5</sub> (LBO)<sup>4</sup> and LiNbO<sub>3</sub> (LNO).<sup>5</sup> In contrast, only a few commercially available secondorder NLO crystals [*e.g.*, chalcopyrite-like semiconductors ZnGeP<sub>2</sub>,<sup>6</sup> AgGaSe<sub>2</sub><sup>7</sup> and AgGaS<sub>2</sub> (AGS)<sup>8</sup>] are available in the middle and far-infrared (MFIR) region. Unfortunately, these crystals still possess a series of inherent performance defects, including harmful two-photon absorption (TPA), non-phasematching (NPM) behaviour (small birefringence  $\Delta n$ ) or low laser-induced damage threshold (LIDT), which seriously hinder their widespread applications.<sup>9</sup> Therefore, the development and exploration of new high-performance MFIR NLO materials is of great significance and challenging in the field of science and technology.

The prerequisite of a NLO material is that it should possess crystallographically non-centrosymmetric (NCS) structure. In the past decades, NCS metal-chalcogenides with two or more types of asymmetric building units have been receiving unprecedented attention not only for their fascinating structural features but also for their excellent NLO properties (*e.g.*, strong second harmonic generation (SHG) response, high LIDT, suit-

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#### Paper

able  $\Delta n$ , and wide MFIR transparency range).<sup>10-43</sup> The wellexamples include  $Li_2Ga_2GeS_6$ ,<sup>10</sup> Li<sub>2</sub>CdGeS<sub>4</sub>,<sup>11</sup> known  $Li_4HgGe_2S_7$ ,<sup>12</sup> Na<sub>2</sub>ZnGe<sub>2</sub>S<sub>6</sub>,<sup>13</sup> NaGaIn<sub>2</sub>Se<sub>5</sub>,<sup>14</sup> Cs<sub>5</sub>BiP<sub>4</sub>Se<sub>12</sub>,<sup>15</sup>  $CsM^{III}Sn_2Se_6$  (M<sup>III</sup> = Ga, In),<sup>16</sup> AZrPQ<sub>6</sub> (A = K-Cs; Q = S, Se),<sup>17</sup>  $A_3Ta_2AsS_{11}$  (A = K, Rb),<sup>18</sup>  $A_4GeP_4Q_{12}$  (A = K-Cs; Q = S, Se),<sup>19</sup>  $A_2Hg_3M_2^{IV}S_8$  (A = Na, K, Rb; M<sup>IV</sup> = Si, Ge and Sn),<sup>20</sup>  $[AX_3][Ga_3PS_8]$  (A = K, Rb; X = Cl, Br),<sup>21</sup> AM<sub>4</sub><sup>II</sup>M<sub>5</sub><sup>III</sup>Q<sub>12</sub> (A = K-Cs;  $M^{II} = Mn$ , Zn, Cd, Hg;  $M^{III} = Ga$ , In; Q = S, Se),<sup>22</sup> PbGa<sub>2</sub> $M^{IV}$ Se<sub>6</sub> = Si, Ge),<sup>23</sup>  $Ba_6Li_2CdSn_4S_{16}$ ,<sup>24</sup>  $Ba_{23}Sb_2Ga_8S_{38}$ ,<sup>2</sup>  $(M^{IV})$ studies, Pan et al. carried out detailed exploratory synthesis on the quaternary Ba- $M_2^{I}$ - $M^{IV}$ - $Q_4$  system (M<sup>I</sup> = Li, Na, Cu; M<sup>IV</sup> = Si, Ge, Sn; Q = S, Se) and discovered a series of novel MFIR NLO candidates.44 Interestingly, these studies indicated that the slight change in cation size (M<sup>I</sup> or M<sup>IV</sup> atoms) would result in different structural features, further affecting their NLO performances. For instance, BaLi<sub>2</sub>M<sup>IV</sup>Q<sub>4</sub> compounds show large SHG efficiencies with compressed chalcopyrite-like (CCL) structures and all of them exhibit the PM abilities,<sup>44c</sup> while BaCu<sub>2</sub>M<sup>IV</sup>Q<sub>4</sub> crystallizes in three different space groups and they exhibit the NPM behavior.44b

With the above considerations in mind, we focused our investigations on the quaternary Ba/M<sup>I</sup>/M<sup>IV</sup>/S system and successfully obtained two Ag-containing compounds, BaAg<sub>2</sub>GeS<sub>4</sub> and BaAg<sub>2</sub>SnS<sub>4</sub>. Crystal structures of these two compounds were first characterized by Teske *et al.* in 1976<sup>45</sup> and 1979,<sup>46</sup> respectively, but their critical NLO properties (*e.g.*, SHG, LIDT or  $\Delta n$ ) have not been reported. In this paper, the synthesis, structural comparison and thermal stability are systemically presented. Moreover, the SHG responses, LIDTs as well as theoretical NLO properties are presented for the first time.

### Experimental section

### Materials and methods

All of the chemicals were obtained from commercial sources and used without further purification. Ba rod (2 N), Ag powder (3 N), Ge shot (5 N), Sn shot (5 N) and S powder (5 N) were purchased from Alfa-Aesar. It should be noted that the external oxide layer on the surface of Ba rod, which is used as a reagent, needs to be thoroughly scraped before use. Powder X-ray diffraction (PXRD) patterns were measured on the Rigaku Mini-Flex II powder diffractometer using  $Cu-K_{\alpha}$  radiation ( $\lambda$  = 1.5416 Å) at room temperature, and the 2-theta range was from 10 to 70° with a step size of 0.02°. The semi-quantitative energy-dispersive X-ray (EDX, Oxford INCA) spectra were recorded on a field emission scanning electron microscope (FESEM, JSM6700F). The UV-Vis-NIR diffuse reflectance spectra were performed at room temperature using a PerkinElmer Lambda 950 UV-Vis spectrophotometer in the wavelength range of 190-2500 nm and BaSO<sub>4</sub> was used as a standard. The absorption spectra were calculated from the reflection spectra according to the Kubelka-Munk function:  $\alpha/S = (1 - R)^2/2R$ , where  $\alpha$  is the absorption coefficient, *S* is the scattering coefficient and *R* is the reflectance.<sup>47</sup> The thermal stability analyses were carried out with a NETZSCH STA 449C simultaneous analyser and heated from 300 to 1273 K at a rate of 10 K min<sup>-1</sup> under a constant flow of nitrogen atmosphere.

### Syntheses

After a series of explorations on the experimental conditions, including annealing temperature, starting reactant and loading ratio, the optimal synthesis route is as follows. The chemicals were loaded in fused silica tubes and sealed under vacuum ( $<10^{-3}$  Pa). The tubes were heated at 573 K for 20 h, raised to 1173 K and maintained for 100 h; then they were cooled to 473 K at 3 K  $h^{-1}$  before turning off the furnace. For compound 1, dark-red irregular bulk crystals were obtained by reacting 1.0 mmol Ba, 2.0 mmol Ag, 1.0 mmol Ge, 4.0 mmol S, and 2.7 mmol BaCl<sub>2</sub>. For compound 2, black irregular bulk crystals were obtained by reacting 1.0 mmol Ba, 2.0 mmol Ag, 1.0 mmol Sn, 4.0 mmol S and 3.1 mmol BaCl<sub>2</sub>. The results of EDX analyses on several single crystals gave average molar ratios of Ba/Ag/M/S of 1/2.1(3)/1.0(1)/4.1(2) for compound 1 and 1/2.1(2)/1.1(3)/4.0(1) for compound 2 (ESI, Fig. S1<sup>+</sup>), respectively, which are in good agreement with those determined from single-crystal XRD data. The products with a yield of about 95% for compound 1 and 90% for compound 2 were obtained after washing with deionized water to remove the BaCl<sub>2</sub> flux and soluble by-products, and dried with ethanol in air. The homogeneous target products were obtained as indicated by the PXRD patterns shown in Fig. 1 and no impure



Fig. 1 Experimental and simulated PXRD patterns of (a)  $BaAg_2GeS_4$  and (b)  $BaAg_2SnS_4$ .

phase was observed within the detection limits of the equipment. The title compounds appeared stable in air over periods of time longer than five months.

#### Crystal structure determinations

High-optical-quality title crystals were selected for the singlecrystal XRD collection. All diffraction data were collected at room temperature on the Saturn 724 diffractometer with Mo- $K_{\alpha}$  radiation ( $\lambda = 0.71073$  Å). The absorption corrections were performed and the structures were solved by direct methods<sup>48</sup> and refined by full-matrix least-squares fitting on  $F^2$  by SHELX-2014 program package.<sup>49</sup> All the non-hydrogen atoms were refined with anisotropic thermal parameters and the coordinates were standardized using STRUCTURE TIDY.50 Table 1 summarizes crystal data and structure refinements information for the title compounds, the atomic coordinates and isotropic displacement parameters are listed in Table S1<sup>+</sup> and the selected bond distances are listed in Table S2 in the ESI.†

#### Second harmonic generation (SHG) measurements

Powder SHG responses were measured on polycrystalline powder samples using a 2050 nm Q-switch laser based on a modified Kurtz-NLO system. The title compounds and reference crystalline AGS ( $2 \times 2 \times 3$  cm<sup>3</sup> single crystals supplied from Anhui Institute of Optics and Fine Mechanics, CAS) were ground and sieved into a series of distinct particle size ranges (30-46, 46-74, 74-106, 106-150, 150-210 µm) to accomplish the size-dependent SHG signals, which was carried out as described elsewhere.16,22,51

#### Laser induced damage threshold (LIDT) measurements

Through the single-pulse measurement method,<sup>52</sup> powder LIDTs of polycrystalline title compounds at the range of 150-210 µm were investigated. AGS single crystals of similar

Table 1 Crystallographic data and refinement details of BaAg<sub>2</sub>GeS<sub>4</sub> and BaAg<sub>2</sub>SnS<sub>4</sub>

Formula	$BaAg_2GeS_4$	BaAg <sub>2</sub> SnS <sub>4</sub>
fw	553.91	600.01
Crystal system	Tetragonal	Orthorhombic
Crystal color	Red	Black
Space group	<i>I</i> 42 <i>m</i> (no. 121)	I222 (no. 23)
a (Å)	6.820(9)	6.885(6)
b (Å)	6.820(9)	7.122(4)
c (Å)	8.021(2)	8.136(6)
$\alpha$ (°)	90	90
$\beta$ (°)	90	90
$\gamma$ (°)	90	90
$V(Å^3)$	373.1(2)	399.0(5)
Z	2	2
$D_{\rm c} ({\rm g}{\rm cm}^{-3})$	4.93	4.99
$\mu (\mathrm{mm}^{-1})$	15.4	13.7
GOOF on $F^2$	1.004	1.005
$R_1, WR_2 (I > 2\sigma(I))^a$	0.0432, 0.1063	0.0452, 0.1160
$R_1, wR_2$ (all data)	0.0442, 0.1069	0.0494, 0.1166
Largest diff. peak and hole( $e Å^{-3}$ )	2.241, -1.223	1.918, -2.494

$${}^{a}R_{1} = \sum ||F_{o}| - |F_{c}|| / \sum |F_{o}|, wR_{2} = [\sum w(F_{o}^{2} - F_{c}^{2})^{2} / \sum w(F_{o}^{2})^{2}]^{1/2}$$

#### **Computational sections**

Theoretical studies were performed by the density functional theory (DFT)<sup>53a</sup> with the generalized gradient approximation (GGA)<sup>53b</sup> as implemented in the Vienna ab initio simulation package (VASP).<sup>53c</sup> The plane-wave basis with projector augmented wave (PAW)<sup>53d,e</sup> potentials was used to represent the core electrons. The plane-wave cut-off energy of 600 eV was chosen for all calculations and denser  $\kappa\text{-point grids}$  of 0.02  $\text{\AA}^{-1}$  were carried out in the optical property calculations. For calculating the optical properties, scissors operators were applied for title compounds and AGS. The second-order nonlinear susceptibility  $\chi^{abc(-2\omega, \omega, \omega)}$  was calculated through the so-called lengthgauge formalism.<sup>54</sup> The specific parameter settings were described in our previously reported papers.16,22,51

### Results and discussion

### Structural description and comparison

Compounds 1 and 2 show the identical stoichiometry 1-2-1-4, but they belong to different crystal systems. Compound 1 crystallizes in the NCS tetragonal space group  $I\bar{4}2m$  (no. 121) with a = b = 6.820(9) Å, c = 8.021(2) Å, V = 373.1(2) Å<sup>3</sup>, and Z =2. Such crystal data are well-consistent with the previously reported phase.45 In the structure, there are four crystallographically unique atoms, including one Ba atom (Wyckoff 2b special position), one Ag atom (Wyckoff 4d special position), one Ge atom (Wyckoff 2a special position) and one S atom (Wyckoff 8i special position) in the asymmetric unit. Compound 2 crystallizes in the NCS tetragonal space group *I*222 (no. 23) with a = 6.885(6) Å, b = 7.112(4) Å, c = 8.316(6) Å, V = 399.0(5) Å<sup>3</sup>, and Z = 2. In the symmetric unit, each atom occupies one crystallographically unique position (Ba: Wyckoff 2a; Ag: Wyckoff 4j; Sn: Wyckoff 2c; S: Wyckoff 8k, respectively). It should be noted that such structural transformation comes from the simple element replacement (Ge to Sn), and the detailed symmetric operation change illustrated in Fig. 2 clearly shows the loss of the glide plane and the inversion axis from compound 1 to compound 2. The symmetry breaking is accompanied by the decrease in symmetry elements from 8 to 4. Moreover, the space group I222 in compound 2 is a subgroup of  $I\bar{4}2m$  in compound 1, which has maximum non-isomorphic subgroups, including I4, Fmm2, I222, P421c, P421m,  $P\bar{4}2c$ , and  $P\bar{4}2m$ . A similar structural change based on element substitution is also observed in the Ba-I<sub>2</sub>- $M^{IV}$ -Q<sub>4</sub> (I = Cu, Na;  $M^{IV}$  = Ge, Sn; Q = S, Se) system<sup>44</sup> and some other Ba-containing chalcogenides, e.g., Ba2BiGaS5 vs. Ba2BiInS5 (Pnma vs.



**Fig. 2** Spatial symmetry operation change from supergroup  $I\overline{4}2m$  (no. 121) to subgroup I222 (no. 23).

 $Cmc2_1$ ),<sup>55</sup> Ba<sub>4</sub>Ga<sub>2</sub>S<sub>8</sub> vs. Ba<sub>4</sub>In<sub>2</sub>S<sub>8</sub> ( $P\bar{1}$  vs.  $P2_1$ ),<sup>56</sup> Ba<sub>2</sub>Ga<sub>2</sub>S<sub>5</sub> <sup>57</sup> vs. Ba<sub>2</sub>In<sub>2</sub>S<sub>5</sub> (C2/c vs. Pbca)<sup>58</sup> and Ba<sub>3</sub>GaS<sub>4</sub>Cl<sup>59</sup> vs. Ba<sub>3</sub>InS<sub>4</sub>Cl (Pnma vs. I4/mcm).<sup>60</sup>

As depicted in Fig. 3, the structural evolution of the title compounds  $BaAg_2MS_4$  (M = Ge, Sn) is derived from the ternary chalcopyrite-like AgGaS<sub>2</sub> [space group:  $I\bar{4}2d$  (no. 122), as shown in Fig. 3a] parent structure<sup>61</sup> by replacing the 2Ga cations with the M cations and with Ba<sup>2+</sup> cations maintaining the charge balance. It can be observed from Fig. 3b that the basic structural unit of compound 1 is the two-dimensional (2D) Ag–S layer, which is composed of highly distorted  $AgS_4$ tetrahedra connected with each other via corner-sharing. Such paralleled lavers are further linked with the isolated GeS4 tetrahedra by sharing corners to form a three-dimensional (3D) open tunnel structure along the *c* direction with  $Ba^{2+}$  cations located in the cavities. Compound 2 has a similar 3D tunnel structure to that of 1 except for their *b* and *c* axes interchanged (Fig. 3c). Of course, the different features in their structures are visible, for instance, the 2D straight Ag-S layer (e.g., Ag-Ag-Ag



**Fig. 3** Structural evolution from (a) classic chalcopyrite-type  $AgGaS_2$  (SG:  $I\bar{A}2d$ ) to the compressed chalcopyrite-like structure of (b)  $BaAg_2GeS_4$  (SG:  $I\bar{A}2m$ ) and (c)  $BaAg_2SnS_4$  (SG: I222).

angle is 90°) exists in compound 1, while the wave-like Ag-S layer (e.g., Ag-Ag-Ag angle is 81.3° or 98.7°) was observed in compound 2 (Fig. 4). The distorted AgS<sub>4</sub> tetrahedra have Ag-S distances of 2.594(3) Å for compound 1, and 2.491(5)-2.786(5) Å for compound 2, which are consistent with those of BaAg<sub>8</sub>S<sub>5</sub> (2.438-2.905 Å),<sup>62</sup> BaAgSbS<sub>3</sub> (2.433-2.727 Å)<sup>63</sup> and BaAgErS<sub>3</sub> (2.542-2.748 Å).<sup>64</sup> Then, irregular MSe<sub>4</sub> (M = Ge, Sn) tetrahedra have typical  $d_{(Ge-S)} = 2.210(4)$  Å in compound 1 and typical  $d_{(Sn-S)} = 2.388(5)$  Å in compound 2. Furthermore, the Ba atoms fill the 3D channels (Fig. 3b and c) and are present in the centre of the distorted S<sub>8</sub> polyhedra (Fig. 3c). The Ba-S interatomic distances vary from 3.251(5) to 3.307(6) Å in compound 1, and from 3.292(6) to 3.337(6) Å in compound 2, which is close to those of other related Ba-based sulfides, including  $Ba_3KSb_4S_9Cl (3.169-3.449 \text{ Å}),^{65} BaRh_2Ge_4S_6 (3.289-3.361 \text{ Å})^{66}$ and  $Ba_3Ho_2P_4S_{16}$  (3.230–3.391 Å).<sup>67</sup> Taking compound 1 as an example, it is worth mentioning that the BaS<sub>8</sub> polyhedra in the different tunnels interlink together by sharing corners and edges to make up the 3D channel structure (Fig. 5a), but the BaS<sub>8</sub> polyhedra occupy discrete positions in the same tunnel (Fig. 5b).

#### Optical properties and thermal stabilities

The solid-state diffuse-reflectance UV–Vis–NIR spectra of title compounds were measured at room temperature, and the spectral results indicate that the experimental band gaps ( $E_g$ ) are 2.02 eV for compound 1 and 1.77 eV for compound 2, respectively (seen from Fig. 6a and b), which are consistent with their polycrystalline colours. Such values are smaller than that of benchmark AGS ( $E_g = 2.56 \text{ eV}$ ),<sup>22</sup> but still comparable to those of other commercial MFIR NLO materials, for instance, chalcopyrite-type semiconductors AgGaSe<sub>2</sub> ( $E_g = 1.75 \text{ eV}$ )<sup>6</sup> and ZnGeP<sub>2</sub> ( $E_g = 1.65 \text{ eV}$ ).<sup>7</sup> As shown in Fig. 6c and d, results of TG and DTA measurements indicate that the compounds are thermally stable up to 1174 K for compound 1 and 1106 K for compound 2 under nitrogen atmosphere. In addition, the endothermic peak indicates that the title compounds decom-



Fig. 4 The 2D straight Ag–S layer in compound 1 (a) and 2D wave-like Ag–S layer in compound 2 (b). The S atoms are omitted for a better view.



Fig. 5 (a)  $BaS_8$  polyhedra via corner- and edge-sharing to make up the 3D framework structure in the *ac* plane with the unit cell marked. (b) Isolated  $BaS_8$  polyhedra locate in the same tunnel (blue dashed-box) alone the *a*-axis.



**Fig. 6** Experimental results of compounds **1** and **2**: (a) and (b) are the solid-state UV–Vis–NIR optical absorption spectra, inserted are the photographs of title crystals; (c) and (d) are TG-DTA diagrams.

posed after this temperature, which is in accordance with the PXRD analysis (detailed information is given in ESI, Fig. S2<sup>†</sup>).

### NLO properties and powder LIDTs

As the title compounds belong to a NCS space group ( $I\overline{4}2m$  and I222), their powder SHG properties were systemically investigated in different particle sizes using the Kurtz and Perry method with 2050 nm Q-switch pulse laser and AgGaS<sub>2</sub> (AGS) as a benchmark material. As shown in Fig. 7a, the SHG responses of the two compounds increase with the increase in particle size, which indicates a type-I PM behavior. Compound 1 has a strong SHG intensity, which is about 1.7 times that of benchmark AGS at a particle size of 150–210 µm, while compound 2 shows the weak SHG response about 0.4 times of AGS in the same particle size.



Fig. 7 (a) Particle size vs. SHG intensity curves for title compounds and AGS (reference) at 2050 nm radiation. The solid curves are drawn to guide the eyes and not fit to the data. (b) The relative SHG and LIDT intensities of title compounds and AGS in the particle size of 150–210  $\mu$ m.

In recent years, estimating the LIDTs of novel MFIR NLO materials on powder sample has become a feasible and semiquantitative method.<sup>62</sup> In this study, the powdered LIDTs of title compounds were systemically evaluated with AGS sample as the reference under a 1064 nm pulse laser, and the results are shown in Fig. 7b and listed in Table 1. Both of them show high LIDTs, and the measured values (4.61 and 2.16 MW cm<sup>-2</sup>) are about 3.2 and 1.5 times that of powdered AGS (1.44 MW cm<sup>-2</sup>), respectively. These data are comparable to those of exceptional MFIR NLO materials, such as powdered BaNa<sub>2</sub>SnS<sub>4</sub> (1.0× AGS),<sup>44*a*</sup> powdered BaLi<sub>2</sub>MSe<sub>4</sub> (M = Ge, Sn; 1.0× AGS),<sup>44*c*</sup> and powdered AgGa<sub>2</sub>PS<sub>6</sub> (5.1× AGS),<sup>34</sup> and single-crystal LiInS<sub>2</sub> (2.5× AGS)<sup>68</sup> and single-crystal BaGa<sub>4</sub>S<sub>7</sub> (3.0× AGS).<sup>69</sup>

Based on the above overall experimental results, title compounds can achieve the balance of two important NLO parameters (large SHG intensities and high LIDTs), which indicates that they are promising candidates for MFIR NLO application.

### Theoretical studies

The theoretical electronic structures as well as linear and NLO properties were investigated using VASP software to better understand and analyse the structure-property relationship of

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the title compounds. As shown in Fig. S3 in ESI,† the top of the valence band (VB) and bottom of the conduction band (CB) are located at different points for compounds 1 and 2, which indicate that they are indirect band gap semiconductors. Calculated results show that the theoretical band gaps are 0.62 and 0.48 eV for compounds 1 and 2, respectively. Such values are smaller than the measured values (2.02 and 1.77 eV) due to the discontinuity of the exchange correlation potential that underestimates the band gap in semiconductors and insulators.<sup>70</sup> In addition, the calculated partial densities of states (PDOSs) of title compounds with main contributions near the Fermi level ( $E_{\rm F}$ ) are shown in Fig. 8a.

Based on the PDOSs of compound 1, in the VB region below the  $E_{\rm F}$ , the Ag-4d and S-3p states dominating the VB-1 region are mixing with minor Ge-4s and Ge-4p states. Above the Fermi level, the CB-1 region is derived primarily from the S-3p and Ge-4s states mixing with small amounts of Ag-4d and Ge-4p states. The Ba atoms almost make no contribution around  $E_{\rm F}$  and act as electron donors to stabilize the structure. As for the compound 2, the PDOSs were also achieved and are similar to that of compound 1 as shown in Fig. 8b. Therefore, the band gap absorptions are primarily ascribed to the charge transitions from the S-3p states to Ag-4d, Ge-4s/Sn-5s, and Ge-4p/Sn-5p states.

Furthermore, the SHG coefficients  $(d_{ij})$  for title compounds were also calculated, as the space group of compound **1** is  $I\bar{4}2m$ , which belongs to the class  $\bar{4}2m$  and has two non-vanishing coefficients in the SHG tensors  $(d_{14} \text{ and } d_{36})$ , of which only



Fig. 8 (a) PDOSs of compounds 1 and 2 (the orbitals with minor contributions are omitted for clarity). (b) Static SHG coefficients of compounds 1 and 2 as a function of the cut-off energy. Dashed line,  $E_{\rm F}$ ; dotted line, different regions in valence bands (VB) and conduction bands (CB).

one is independent  $(d_{14})$  under the restriction of Kleinman's symmetry.<sup>71</sup> In addition, compound 2 belongs to 222 point group that allows for three nonzero coefficients in the SHG tensor and only one is independent:  $d_{14} = d_{25} = d_{36}$ . Moreover, the cut-off energy, which depends on the largest second-order SHG tensor  $d_{14}$ , was investigated to understand the origin of the SHG component of title compounds. Fig. 8b shows that in the regions of VB-1 (dominated by S-3p and Ag-4d orbitals) and CB-2 (dominated by S-3p, Ag-4d and Ge(Sn)-ns/np orbitals), the  $d_{14}$  values are most sharply increased, which contribute primarily to the second-order NLO susceptibility. In other words, the NLO activities of title compounds originate from the condensation of AgS<sub>4</sub> and MS<sub>4</sub> (M = Ge, Sn) tetrahedral units that built the 3D CCL structures.

It should be noted that the calculated  $d_{14}$  coefficient for compound 1 ( $d_{14} = 15.7 \text{ pm V}^{-1}$ ) is close to AGS ( $d_{36} =$ 18.2 pm V<sup>-1</sup>) at a wavelength of 2050 nm (*ca.* 0.61 eV), which is in accordance with the experimental observations (Fig. 9a). However, the SHG experimental observation (0.4× AGS) is smaller than the calculated value ( $d_{14}$  (2050 nm) = 14.5 pm V<sup>-1</sup>) of compound 2. Such low SHG intensity could be due to the narrow optical  $E_g$  (1.77 eV) and strong absorption of both fundamental light (2050 nm) and frequency-doubled light (1025 nm). Thus, in order to obtain the precise SHG signals of compound 2, it is necessary to use a fundamental light source with a much longer wavelength (*e.g.*, CO<sub>2</sub> laser).

As shown in Fig. 9b, the calculated birefringence ( $\Delta n$ ) values of compounds 1 and 2 are 0.198 and 0.052 at a wavelength of 2050 nm (*ca.* 0.61 eV), respectively; these values are clearly larger than that of AGS ( $\Delta n$  (2050 nm) = 0.039). The relatively large  $\Delta n$  values in the MFIR region indicate PM behaviors, which is consistent with the experimental observations (Fig. 7). Furthermore, the frequency-dependent dielectric function ( $\varepsilon$ ), refractive index (n), absorption coefficient ( $\alpha$ ) and reflectivity (R) (Fig. S4–S5 in ESI†) were also investigated and several important parameters taken for comparison (including unit cell, space group, phase-matchability,  $\Delta n$  and the relative powder SHG and LIDT intensities) in the quaternary Ba–M<sub>2</sub><sup>1</sup>–M<sup>IV</sup>–Q<sub>4</sub> family and benchmark AGS are summarized in Table 2, indicating that the title compounds satisfy the key requirements as promising MFIR NLO materials.



**Fig. 9** (a) Calculated frequency-dependent SHG coefficients ( $d_{in}$ ) and (b) calculated birefringence ( $\Delta n$ ) for compounds **1** and **2** and AGS (as a reference).

Table 2 Structure-NLO property comparison in the quaternary Ba-M<sup>1</sup><sub>2</sub>-M<sup>1V</sup>-Q<sub>4</sub> family and benchmark AgGaS<sub>2</sub>

Paper

Compounds	Unit cell	Space group	$E_{\rm g} \left( {\rm eV} \right)$	PM/NPM <sup>a</sup>	Calculated $\Delta n$	Powder SHG	Powder LIDT	Ref.
AgGaS <sub>2</sub>	Tetragonal	$I\bar{4}2d$	2.56	PM	0.039	AGS	AGS	8 and 22
BaLi2GeS4	Tetragonal	$I\bar{4}2m$	3.66	PM	0.031	0.5× AGS	11× AGS	44 <i>c</i>
BaLi <sub>2</sub> SnS <sub>4</sub>	Tetragonal	$I\bar{4}2m$	3.07	PM	0.033	0.7× AGS	6.5× AGS	
BaLi <sub>2</sub> GeSe <sub>4</sub>	Tetragonal	$I\bar{4}2m$	2.40	PM	0.038	1.1× AGS	1× AGS	
BaLi <sub>2</sub> SnSe <sub>4</sub>	Tetragonal	$I\bar{4}2m$	2.18	PM	0.066	1.3× AGS	1× AGS	
BaNa <sub>2</sub> GeS <sub>4</sub>	Trigonal	R3c	3.70	PM	0.037	0.3× AGS	8× AGS	44 <i>a</i>
$BaNa_{2}SnS_{4}$	Tetragonal	$I\bar{4}2d$	3.27	PM	0.07	0.5× AGS	5× AGS	
BaNa₂GeSe₄	Trigonal	R3c	2.46	NPM	0.026	0.9× AGS	1× AGS	
$BaNa_{2}SnSe_{4}$	Trigonal	R3c	2.25	NPM	0.011	1.3× AGS	1× AGS	
BaCu <sub>2</sub> GeS <sub>4</sub>	Trigonal	$P3_{1}21$	2.47	NPM	N/A	0.3× AGS	N/A	44b
BaCu <sub>2</sub> SnS <sub>4</sub>	Trigonal	P3 <sub>2</sub> 21	1.96	NPM	N/A	1.6× AGS	N/A	
BaCu <sub>2</sub> SiSe <sub>4</sub>	Trigonal	$P3_{2}21$	2.62	NPM	N/A	0.3× AGS	N/A	
BaCu <sub>2</sub> GeSe <sub>4</sub>	Trigonal	P3121	1.88	NPM	N/A	0.3× AGS	N/A	
BaCu <sub>2</sub> SnSe <sub>4</sub>	Orthorhombic	Ama2	1.72	NPM	N/A	0.3× AGS	N/A	
BaAg <sub>2</sub> GeS <sub>4</sub>	Tetragonal	$I\bar{4}2m$	2.02	PM	0.198	1.7× AGS	3.2× AGS	This work
BaAg <sub>2</sub> SnS <sub>4</sub>	Orthorhombic	I222	1.77	PM	0.052	0.4× AGS	1.5× AGS	

<sup>a</sup> PM = phase-matchability, NPM = non-phase-matchability, and these are Type-I otherwise noted.

### Conclusions

In summary, two new NCS compounds,  $BaAg_2GeS_4$  (1) and  $BaAg_2SnS_4$  (2), have been synthesized using the  $BaCl_2$  flux method with high yields. Both these compounds exhibit compressed chalcopyrite-like structures compared with that of typical chalcopyrite-type AgGaS<sub>2</sub>. For the first time, their NLO activities were discovered and systematically studied. It should be noted that the title compounds exhibit the type-I phasematching abilities and excellent NLO performances, including strong SHG (1.7× and 0.4× AgGaS<sub>2</sub>), high LIDTs (3.2× and 1.5× AgGaS<sub>2</sub>) and large  $\Delta n$  (0.198 and 0.052), which indicates that they are promising candidates for NLO materials used in MFIR region. In addition, the Vienna ab initio theoretical studies show that the electronic transitions from S-3p states to Ag-4p and Ga-4p or Sn-4p states make the main contributions to the strong NLO activities for compounds 1 and 2, respectively. Further efforts pursuing the growth of large-sized single crystals with good quality are in need.

### Conflicts of interest

There are no conflicts to declare.

### Acknowledgements

This work was supported by the National Natural Science Foundation of China (21771179, 21301175, 21233009, 21571020 and 91422303), the Major State Basic Research Development Program of China (973 Program, no. 2014CB845603), the Strategic Priority Research Program of the Chinese Academy of Sciences (no. XDB20010200), and the Natural Science Foundation of Fujian Province (2015J01071). We thank Professor Yong-Fan Zhang at Fuzhou University for helping with the DFT calculations.

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