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# Fragment motion in motor molecules: basic concepts and application to intra-molecular rotations

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The complex motion of atoms inside large molecules can be analyzed by considering translation, rotation, and flexibility of corresponding molecular fragments and by applying classical mechanics based on Pulay forces on the atoms, as in molecular dynamics. We propose a fragment motion analysis that provides a basic qualitative understanding of the motion of the different molecular components. Further, it can help to describe or design simplified fragment motions, e.g. the rotation of a rotator with respect to its stator counterpart in a rotor molecule, despite the higher actual complexity due to flexibility of rotator and stator or due to a variable rotation axis. The formal aspects of the fragment motion analysis are discussed in detail. Its application is illustrated by the rotational motion inside the BTP-BCO molecule and by rotational transitions between *cis*- and *trans*-stilbene isomers.

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## 1. Introduction

All molecules have internal degrees of freedom that allow many types of internal motion, such as vibration, bending and rotation of individual atoms or of subgroups of atoms. Normally, motions within molecules are complex combinations of such elementary motions: for example, a rotating fragment is never totally rigid, but actually is itself flexible, allowing vibration, bending and even internal differential rotation and other types of distortion within itself. While humans can easily recognize in a movie, for example, a rotating fragment even when it is not rigid, this is a more difficult task to program for a computer: to that end, we need a general formalism to decompose the complex real motion into its simpler superposed constituents – translation for stretching vibrations, rotation for back and forth swinging as well as for spinning, and flexing for all other distortions. Our aim here is to describe such a decomposition for an arbitrary molecule, with particular application to rotor molecules, *i.e.* molecules that contain rotating parts.

Macromolecules, in particular large rotor molecules with 100 and more atoms, have attracted considerable attention due to their exciting physical and chemical properties,<sup>1</sup> which have,

for example, been acknowledged by the award of the 2017 Nobel Prize in Chemistry for molecular machines.<sup>2</sup> Their complex rotational behavior manifested by the motion of atom groups inside the molecules has been examined in numerous studies, both experimentally and theoretically. Examples are molecular rotors with chiral rotators sticking out on one end,<sup>1,3</sup> molecules with internal rotators, such as BTP-BCO,<sup>4–6</sup> or large molecules combining internal rotation with translation, such as [c2]daisy chain supramolecules.<sup>7,8</sup> In addition, rotational motion can also appear in conformation changes of larger molecules. An example is given by the rotational modes of the isomer transitions between *cis*- and *trans*-stilbene.<sup>9–14</sup>

Theoretical work on the time evolution of large molecules is often based on molecular dynamics methods using classical equations of motion<sup>15</sup> to account for atom motion. The atoms are represented by point masses moving under the influence of external forces and of forces between them, which are either given by model potentials (force field methods<sup>16</sup>) or obtained from quantum calculations (*e.g.* Pulay forces<sup>17</sup>). These studies yield geometric conformations as well as transitions between them described by classical paths and physical parameters, such as energies, atom positions and velocities, linear and angular momenta, or torques. Appropriate ensemble averages can then provide information about statistical and thermodynamic quantities, such as free energy, entropy, and chemical potentials. However, the atom based molecular dynamics approach makes it difficult to highlight and visualize concerted motions of groups of atoms within molecules, such as relative

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rotations and translations/vibrations of comparatively rigid but movable parts of the molecules.

We therefore propose an approach that is often conceptually simpler to describe the internal motion within large molecules. We focus our attention on the concerted motion of those relatively rigid parts of the molecules, which we will call “fragments” in this work. In this approach, the complex motion of the set of individual atoms inside the molecule is approximated by that of relatively rigid fragments which allow also some internal flexibility during their rotation and vibration. Then the rotation and translation/vibration of the fragments can be obtained by applying classical mechanics to the whole fragments, based on Pulay forces on the atoms as obtained from quantum mechanical calculations. Our resulting fragment motion analysis, applied to the rigid approximant of each fragment, provides a qualitative but realistic understanding of the motion of the different molecular components. It also helps us to predict and design simplified fragment paths in the multi-dimensional configuration space, such as those of the motion of a rotator fragment relative to a stator fragment in a rotor molecule.

Clearly, the assumption of a fragment as a rigid subset of a molecule that can translate and rotate by coupled motions of the fragment atoms can only be approximate. We therefore include individual atom motion beyond cooperative effects in our detailed quantitative description of fragment dynamics. This can be connected with local flexibility or elasticity of a fragment and has to be evaluated on an individual basis where explicit atom forces are taken into account. If flexibility makes a major contribution to the motion of a fragment, the concept of fragment motion becomes questionable. Thus, our fragment motion analysis relies on the assumption of a relatively rigid fragment where flexibility can be treated as a minor perturbation or ignored in a qualitative analysis. This assumption can often be easily evaluated intuitively for a given system.

Section 2 discusses formal aspects of the fragment motion analysis in detail, while Section 3 illustrates the importance of the three different contributions – fragment rotation, translation, and flexibility – for the molecular rotor BTP-BCO<sup>4–6</sup> and for rotational isomer transitions between *cis*- and *trans*-stilbene.<sup>9–14</sup> Finally, Section 4 summarizes our conclusions.

## 2. Theoretical details

### 2.1 Basic concepts of fragment motion in molecules

In the present approach the atoms of a molecule are described by classical point masses at given positions, with velocities, and experiencing forces due to interatomic coupling as well as due to external fields. Details of this description on an individual atom basis can be rather complex and difficult to grasp. However, in large molecules one can often identify distinct fragments, whose atoms move together in a similar fashion, *e.g.* rotating, shifting, or vibrating as a more or less rigid fragment.

The motion of a fragment becomes particularly simple and easy to describe if its *N* atoms are rigidly interconnected with fixed interatomic distances and angles. Then the motion of

each constituent atom is determined by the global motion of the rigid fragment. Rigid fragment motion can only be *translation* (as in vibration or isomeric transitions) and/or *rotation* (as in back and forth swinging or continuous spinning about a fixed point on the static part<sup>18</sup> of the molecule). Here a formal description of translation is based on a reference point  $\underline{R}_{\text{ref}}$  representing the fragment, which can be, for example, its center of mass (CoM) given by

$$\underline{R}_{\text{ref}} = \underline{R}_{\text{CoM}} = \frac{1}{M} \sum_{i=1}^N m_i \underline{r}_i, \quad M = \sum_{i=1}^N m_i \quad (1)$$

Then the corresponding fragment velocity  $\underline{V}_{\text{ref}}$  shifting all fragment atoms (including the CoM) equally determines the translational motion.

The fragment atoms of a molecule may experience forces  $\underline{F}_i$  that are partly internal forces due to other atoms in the molecule and possibly external forces originating *e.g.* from external charges or from other force fields. These forces, evaluated in the present work as quantum mechanical Pulay forces between atoms of the molecule,<sup>17,19</sup> accelerate the atoms. Assuming a rigid fragment, the total force  $\underline{F}_{\text{tot}}$  acting on it is given by the sum of forces on all fragment atoms and, if the fragment does not rotate, the total force will accelerate all atoms equally, giving rise to a linear translational fragment motion.

Rigid fragment rotation is described by its atoms rotating with the same angular velocity  $\omega$  about a common rotational axis through a pivot point  $\underline{R}_{\text{ref}}$ . Thus, the velocity of each rotating fragment atom at position  $\underline{r}_i$  can be described as

$$\underline{v}_i^{\text{rot}} = \underline{\omega} \times (\underline{r}_i - \underline{R}_{\text{ref}}) \quad (2)$$

where the rotation vector  $\underline{\omega}$  defines the direction of the rotational axis and its length denotes the angular velocity of the rotation. The rotation can be further characterized by the angular momentum of the fragment with respect to its pivot  $\underline{R}_{\text{ref}}$  which, for a rigid fragment, is given by

$$\underline{L}_{\text{ref}} = \sum_{i=1}^N m_i [(\underline{r}_i - \underline{R}_{\text{ref}}) \times \underline{v}_i^{\text{rot}}] \quad (3)$$

where  $m_i$  are masses of the fragment atoms. Together with (2), this can be written as

$$\underline{L}_{\text{ref}} = \underline{\Theta} \underline{\omega}, \quad \underline{\omega} = \underline{\Theta}^{-1} \underline{L}_{\text{ref}} \quad (4)$$

where  $\underline{\Theta}$  is the moment of inertia of the fragment. Assuming Cartesian coordinates,  $\underline{r}_i = (x_{i1}, x_{i2}, x_{i3})$  and  $\underline{R}_{\text{ref}} = (X_{\text{ref}1}, X_{\text{ref}2}, X_{\text{ref}3})$ , the moment of inertia is given by a  $3 \times 3$  matrix with elements

$$\Theta_{kl} = \sum_{i=1}^N m_i \left[ (\underline{r}_i - \underline{R}_{\text{ref}})^2 \delta_{kl} - (x_{ik} - X_{\text{ref}k})(x_{il} - X_{\text{ref}l}) \right], \quad (5) \\ k, l = 1, 2, 3$$

Thus, there is a direct relation between the rotation vector  $\underline{\omega}$  and the fragment angular momentum  $\underline{L}_{\text{ref}}$ , and one quantity can be evaluated from the other according to (4) and (5).



Further, from relations (2)–(4) it can be shown that the scalar product  $(\underline{L}_{\text{ref}} \underline{\omega})$  is always positive (or zero). Thus, allowing unrestricted rotation about  $\underline{R}_{\text{ref}}$ , the rotation vector  $\underline{\omega}$  and the fragment angular momentum  $\underline{L}_{\text{ref}}$  always form an angle less than or equal to  $90^\circ$ . In looser language, this means that  $\underline{\omega}$  and  $\underline{L}_{\text{ref}}$  rotate essentially in the same direction since a right-handed angular momentum will favor a right-handed rotation, and a left-handed angular momentum will favor a left-handed rotation. Therefore, the direction of  $\underline{L}_{\text{ref}}$  can be used to qualitatively indicate possible directions of fragment rotation axes and their rotational sense (right- vs. left-handed) without having to evaluate  $\underline{\omega}$  explicitly, a useful simplification that provides a very helpful guide to understand the rotational behavior of fragments.

If, on the other hand, the direction of the rotation axis parallel to  $\underline{\omega}$  through  $\underline{R}_{\text{ref}}$  is fixed and predefined (examples are attached fragment rotations restricted to rotating about an interatomic bond), the acting angular momentum is forced to be collinear with  $\underline{\omega}$  and is determined by the projection of  $\underline{L}_{\text{ref}}$  onto  $\underline{\omega}$ , yielding  $\underline{L}_{\text{ref}}^{\text{eff}}$  according to

$$\underline{L}_{\text{ref}}^{\text{eff}} = \left( \underline{L}_{\text{ref}} \frac{\underline{\omega}}{\omega} \right) \frac{\underline{\omega}}{\omega} = \Theta^{\text{eff}} \underline{\omega} \quad (6)$$

with a scalar moment of inertia  $\Theta^{\text{eff}}$  given by

$$\Theta^{\text{eff}} = \sum_{i=1}^N m_i \left( \frac{\underline{\omega}}{\omega} \times (\underline{r}_i - \underline{R}_{\text{ref}}) \right)^2 \quad (7)$$

In addition to linear acceleration of the rigid fragment discussed above, atom forces  $\underline{F}_i$  may also lead to a rotational acceleration about a pivot  $\underline{R}_{\text{ref}}$  which is induced by a torque  $\underline{T}_{\text{ref}}$  with respect to the pivot given by

$$\underline{T}_{\text{ref}} = \sum_{i=1}^N (\underline{r}_i - \underline{R}_{\text{ref}}) \times \left( \underline{F}_i - \frac{m_i}{M} \underline{F}_{\text{tot}} \right) \quad (8)$$

$$= \sum_{i=1}^N (\underline{r}_i - \underline{R}_{\text{ref}}) \times \underline{F}_i - \underline{T}_{\text{trans}}$$

$$\underline{T}_{\text{trans}} = (\underline{R}_{\text{CoM}} - \underline{R}_{\text{ref}}) \times \underline{F}_{\text{tot}} \quad (8a)$$

Here the contribution due to translational motion of the fragment,  $\underline{T}_{\text{trans}}$ , has been removed.<sup>20</sup> This can also be written as the time derivative of the angular momentum, *i.e.*

$$\underline{T}_{\text{ref}} = \frac{d}{dt} \underline{L}_{\text{ref}} = \frac{d}{dt} \sum_{i=1}^N m_i [(\underline{r}_i - \underline{R}_{\text{ref}}) \times (\underline{v}_i - \underline{V}_{\text{ref}})] \quad (9)$$

$$= \frac{d}{dt} \left( \sum_{i=1}^N m_i [(\underline{r}_i - \underline{R}_{\text{ref}}) \times \underline{v}_i] - \underline{L}_{\text{trans}} \right)$$

$$\underline{L}_{\text{trans}} = (\underline{R}_{\text{CoM}} - \underline{R}_{\text{ref}}) \times \underline{V}_{\text{ref}} \quad (9a)$$

where similarly the contribution of the angular momentum due to translational motion of the fragment,  $\underline{L}_{\text{trans}}$ , has been removed. Thus, while a finite angular momentum  $\underline{L}_{\text{ref}}$  implies a rotational motion of the rigid fragment with an angular velocity

according to the rotation vector  $\underline{\omega}$ , a non-zero torque yields an angular acceleration of the fragment.

In reality, molecular fragments will not be exactly rigid, but exhibit flexibility, including rapid individual atomic vibrations and elasticity. The atoms thus can have individual velocity contributions  $\underline{v}_i^{\text{flex}}$  beyond rigid fragment translation and rotation. Here we limit flexibility to motions that maintain the integrity and identifiability of the fragments. In particular we do not consider bond breaking and bond making between different fragments. In the simplest case, flexibility makes only a small contribution to the atom displacement inside the fragment and can be treated as a perturbation of the approximately rigid fragment; small organic components inside larger hydrocarbons can serve as examples. Altogether, the absolute velocities of the fragment atoms are described by contributions due to fragment translation, rotation about the pivot, and flexibility according to

$$\underline{v}_i = \underline{V}_{\text{ref}} + \underline{v}_i^{\text{rot}} + \underline{v}_i^{\text{flex}} \quad (10)$$

where  $\underline{v}_i^{\text{flex}}$  includes both slow deformations of the fragment changing its shape and rapid atomic vibrations about given fragment positions. Relations (1)–(10) will be the basis of the fragment motion analysis described in the following.

## 2.2 Mechanical analysis applied to fragments

Our fragment motion analysis starts with a quasi-static approach which assumes that initially all  $N$  atoms of the fragment are at rest with positions  $\underline{r}_i$  and velocities  $\underline{v}_i = 0$ . Then forces  $\underline{F}_i$  are applied to the atoms for a short time  $\tau$ , leading to finite velocities  $\underline{v}_i$  which can be described in linear approximation, by using the impulse-momentum equivalence, as

$$\underline{v}_i = \frac{1}{m_i} \underline{F}_i \tau \quad (11)$$

This leads to a translational motion of the fragment with a velocity  $\underline{V}_{\text{ref}}$  given approximately by that of the fragment CoM, *i.e.* by

$$\underline{V}_{\text{ref}} = \frac{1}{M} \sum_{i=1}^N m_i \underline{v}_i = \frac{1}{M} \underline{F}_{\text{tot}} \tau \quad (12)$$

where  $\underline{F}_{\text{tot}}$  denotes the sum of the  $N$  fragment atom forces  $\underline{F}_i$ . Now we can estimate an approximate translation  $\Delta \underline{R}_{\text{ref}}$  of the fragment, by using the average speed  $\frac{1}{2} \underline{V}_{\text{ref}}$  during the acceleration, which yields

$$\Delta \underline{R}_{\text{ref}} = \frac{1}{2} \underline{V}_{\text{ref}} \tau = \frac{1}{2M} \underline{F}_{\text{tot}} \tau^2 \quad (13)$$

This result allows us to estimate the displacement of the fragment as a whole along the direction of  $\underline{F}_{\text{tot}}$ . Further, the fragment torque  $\underline{T}_{\text{ref}}$  defined by (8) and (9) leads to a fragment angular momentum  $\underline{L}_{\text{ref}}$  which, in linear approximation after a short time  $\tau$ , becomes

$$\underline{L}_{\text{ref}} = \underline{T}_{\text{ref}} \tau \quad (14)$$



We next determine a rotation vector  $\underline{\omega}$  for unconstrained rotation about  $R_{\text{ref}}$  according to (4) and (5), which helps to describe rotational details of a fragment that is only constrained to rotate around a pivot without a predefined axis. However, in real molecules, internal binding of a fragment with its neighborhood may restrict rotations to specific axes given by fixed directions parallel to  $\underline{\omega}$  through the pivot  $R_{\text{ref}}$ . Then, starting from a resting fragment, the acting angular momentum  $L_{\text{ref}}^{\text{eff}}$ , collinear with  $\underline{\omega}$  and pointing in the same direction, can be evaluated using relations (6) and (7) from which the magnitude of the angular velocity,  $\omega = |\underline{\omega}|$ , is obtained as

$$\omega = \frac{1}{\Theta_{\text{eff}}} |L_{\text{ref}}^{\text{eff}}| = \frac{1}{\Theta_{\text{eff}}} \left| T_{\text{ref}} \frac{\underline{\omega}}{\omega} \right| \tau \quad (15)$$

In addition, the degree of flexibility for the individual atom motion and, thus, the quality of the assumption of an approximately rigid rotating/translating fragment, can be estimated by comparing the rigid-fragment motion with that of the flexible fragment. This is achieved by comparing the absolute velocities  $\underline{v}_i$  of the individual atoms at time  $\tau$  according to (11) with their flexibility contributions  $\underline{v}_i^{\text{flex}}$ , where the difference is given, according to (2) and (10), by

$$\underline{v}_i - \underline{v}_i^{\text{flex}} = \underline{V}_{\text{ref}} + \underline{\omega} \times (\underline{r}_i - \underline{R}_{\text{ref}}) \quad (16)$$

which combines the translational velocity  $\underline{V}_{\text{ref}}$  with rotational atom velocities  $\underline{v}_i^{\text{rot}}$  relative to the pivot  $R_{\text{ref}}$ .

The mechanical analysis discussed so far considers only an initial short time step where the approximation of a relatively rigid fragment with forces on initially resting atoms is justified. As each atom moves, the fragment can change both its orientation and internal structure, so that the forces  $F_i$  will also change over time and have to be recalculated at each subsequent time step if we want to accurately follow complete trajectories. However, if we limit our interest to the qualitative behavior of the fragment (such as approximate direction of the axis of rotation and right- vs. left-handed sense of rotation), there is no need to go beyond the initial time step, thus making the analysis very efficient.

In the following, we will discuss results of two example systems where the fragment motion analysis can give additional information in the evaluation of internal motion details. The first example deals with the BTP-BCO molecule,<sup>4-6</sup> in which the kinetic behavior of the internal rotating  $\text{C}_2(\text{C}_2\text{H}_4)_3$  fragment is studied. In the second example, the rotational isomer transition between *cis*- and *trans*-stilbene is examined, in which possible transition paths induced by light can be identified.<sup>9-14</sup> Clearly, the two example applications can also be dealt with by direct analytical methods based on simple algebra. It can be shown that in both examples the torque component along the rotational axis equals the negative angle derivative of the total energy. However, a comparison with results from our fragment motion analysis can serve as a useful double check.

The two applications in Section 3 deal only with the analysis of rotational motion of rigid fragments of the corresponding molecules. However, the theoretical details of the fragment motion analysis discussed in the present section are more

general and can lay the groundwork for detailed studies of more complex molecules in the future. In these systems a discrimination between fragment translation and rotation starts by treating the fragments as rigid subunits, which has to be followed by considering their flexibility according to atom motion described by eqn (10). This will assist the classification of complex collective motions inside the complex molecule.

It must be emphasized that the concept of fragment motion can only be based on a meaningful selection of fragments where chemical intuition as well as physical insight is of paramount importance. An automated fragment search considering many (mathematically) possible fragmentations of a molecule (in trial-and-error strategies) may not yield chemically/physically meaningful fragments and may not be feasible computationally.

### 3. Applications

#### 3.1 Random rotor inside BTP-BCO

This example refers to a large hydrocarbon molecule named (4',4''''-(bicyclo[2,2,2]octane-1,4-diyl-di-4,1-phenylene)-bis-2,2':6',2''-terpyridine) or BTP-BCO for short,<sup>5,6</sup> with a sum formula  $\text{C}_{50}\text{H}_{40}\text{N}_6$ . It contains a bicyclo[2,2,2]octane (BCO) group connected to one phenylene group on each side, each of which in turn binds to terminal terpyridine groups, see Fig. 1. Scanning tunneling microscopy (STM) experiments for BTP-BCO molecules adsorbed at the Cu(111) surface have shown<sup>5</sup> that the BCO group of approximately 3-fold rotational symmetry can be stimulated by tunneling electrons to rotate about its symmetry axis, which is parallel to the substrate surface. Theoretical studies<sup>6</sup> indicate that the five groups – the central BCO, the two phenylenes, and the terminal terpyridines – form quite rigid subunits which, in the gas phase, can rotate relative to each other about the connecting C–C bonds between the subunits. On a surface, the phenylene and terpyridine groups tend to stick flat to the surface, while the internal BCO rotor can still be excited to make rapid jumps between four non-equivalent rotational orientations that are stabilized by the substrate–molecule interactions.

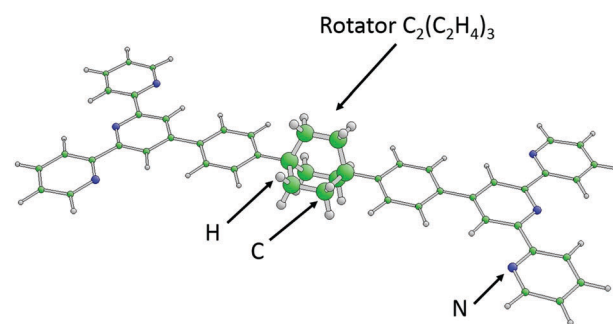
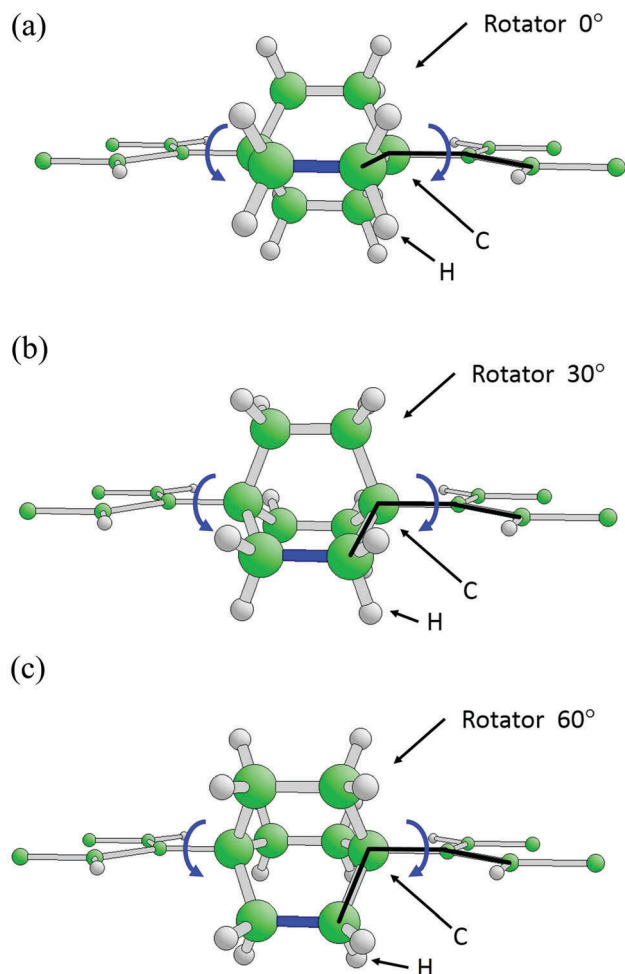


Fig. 1 Geometric structure of the symmetrized BTP-BCO molecule in its equilibrium configuration. Ball-and-stick model of the complete molecule with its five different components: 2 × terpyridine, 2 × phenylene, and BCO,  $\text{C}_2(\text{C}_2\text{H}_4)_3$ . The different atoms are color coded and labeled accordingly. The BCO rotor is emphasized by larger balls.





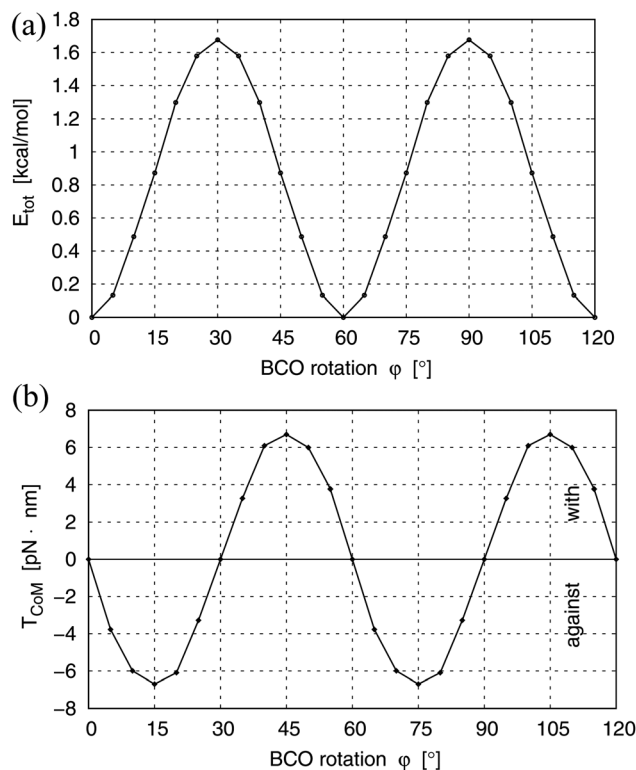
Here we examine details of the rotational motion of the BCO group,  $C_2(C_2H_4)_3$ , inside free BTP-BCO by using a symmetrized model structure where the BCO rotor itself is assumed to exhibit exact  $D_{3h}$  symmetry with its three  $C_2H_4$  flaps forming  $120^\circ$  angles with each other and the two outer carbons positioned at the 3-fold symmetry axis, see Fig. 2a. Further, we assume that the two phenylene and two terpyridine groups form a fixed planar BTP framework in which the BCO can rotate. (For comparison, no planarity of the BTP framework was imposed in earlier gas-phase molecular-dynamics simulations,<sup>6</sup> which allowed complete freedom of motion.) With these geometric constraints, density-functional theory calculations are performed to obtain optimized electronic and geometric structures analogous to those of an earlier study.<sup>6</sup> In the calculations, the B3LYP exchange–correlation functional<sup>21,22</sup> is used together with extended 6-31G# and 6-31G\* basis sets<sup>23</sup> as implemented in the GAUSSIAN 03 code.<sup>24</sup>



**Fig. 2** Geometric structure of the central portion of the symmetrized BTP-BCO. Ball-and-stick models with BCO,  $C_2(C_2H_4)_3$ , at different rotation angles: (a)  $\varphi = 0^\circ$  (equilibrium geometry), (b)  $\varphi = 30^\circ$  (metastable geometry), (c)  $\varphi = 60^\circ$  (alternative equilibrium geometry). One C–C bond is painted blue to highlight the rotation. The dihedral rotation angles  $\varphi$  are indicated by triplets of black lines along C–C bonds. The different atoms are labeled accordingly and the BCO rotor is emphasized by larger balls.

With the above symmetry constraints, the geometric optimization of BTP-BCO yields interatomic distances and bond angles defining the structure shown in Fig. 1. Here one of the three  $C_2H_4$  flaps (emphasized by a blue C–C bond in Fig. 2a) of BCO is parallel to the planar BTP framework while the other two protrude on both sides, each forming dihedral angles of  $60^\circ$  with the framework. Keeping the planar geometry of the BTP framework and the 3-fold symmetry of BCO with the common symmetry axis fixed allows us to describe a rotation of BCO by just one dihedral angle  $\varphi$ , the torsion angle defined by four carbon atoms as indicated in Fig. 2a–c.

Clearly, due to the 3-fold symmetry of BCO, its rotation by  $\varphi = 120^\circ$  inside the symmetrized BTP-BCO must reproduce the initial molecular geometry. This leads to a total energy of the molecule  $E_{\text{tot}}(\varphi)$  having an angular periodicity  $\Delta\varphi = 120^\circ$ . In fact, the additional 2-fold rotational symmetry of the BTP framework reduces the periodicity to  $\Delta\varphi = 60^\circ$  as shown in Fig. 3a. As a consequence, the energy minimum at  $\varphi = 0^\circ$  is reproduced at  $\varphi = 60^\circ$ . However, the equilibrium structures corresponding to the two angles differ by a mirror operation perpendicular to the planar BTP framework such that the  $C_2H_4$  flaps of BCO point in opposite directions. This becomes evident when comparing Fig. 2a with Fig. 2c. Between the energy minima at  $\varphi = 0^\circ$  and  $60^\circ$ , the total energy varies smoothly



**Fig. 3** (a) Total energy  $E_{\text{tot}}(\varphi)$  of the symmetrized BTP-BCO molecule as a function of the BCO rotation angle  $\varphi$ . (b) Torque component  $T_{\text{COM}}(\varphi)$  acting along the symmetry axis of the BCO rotor as a function of the rotation angle  $\varphi$ . For the definition of dihedral angle  $\varphi$  see Fig. 2. Positive  $T_{\text{COM}}(\varphi)$  favors accelerated rotation (labeled “with”) while negative  $T_{\text{COM}}(\varphi)$  indicates decelerated rotation (labeled “against”).



with  $\varphi$  going over a maximum at  $30^\circ$ , see Fig. 2b, which corresponds to an energy barrier of only  $1.68 \text{ kcal mol}^{-1}$  ( $0.07 \text{ eV}$ ). Thus, the barrier can be easily overcome by thermal excitations, which confirms the results obtained previously.<sup>6</sup> Further, the symmetry of the total energy  $E_{\text{tot}}(\varphi)$  allows rotation in both positive and negative angular directions with equal angular acceleration. This characterizes the BCO rotor as a random rotor without directional preference (vibrations can break the symmetry but are themselves equally probable in both directions).

The atoms of the BCO fragment rotating away from equilibrium inside BTP-BCO experience forces which result in a torque on the BCO rotor as defined by (8) and (9), where the CoM coincides with the symmetry center of the rotor. Clearly, this torque  $T_{\text{CoM}}(\varphi)$  depends on the rotation angle  $\varphi$  and, due to the symmetry constraints, its direction points always along the rotation axis of the BCO rotor (if we neglect vibrations). If vector  $\underline{T}_{\text{CoM}}(\varphi)$  is parallel to the rotation vector  $\underline{\omega}$ , described by a positive scalar  $T_{\text{CoM}}(\varphi) = |\underline{T}_{\text{CoM}}(\varphi)|$  in the following, the torque favors the rotation by increasing its angular velocity  $\omega$ . In contrast,  $\underline{T}_{\text{CoM}}(\varphi)$  antiparallel to  $\underline{\omega}$  will be denoted by a negative scalar  $T_{\text{CoM}}(\varphi) = -|\underline{T}_{\text{CoM}}(\varphi)|$  working against the rotation by decreasing  $\omega$ . Fig. 3b shows the variation of the torque component  $T_{\text{CoM}}(\varphi)$  with the rotation angle  $\varphi$  which, as for the total energy  $E_{\text{tot}}(\varphi)$ , is periodic with an angular periodicity of  $\Delta\varphi = 60^\circ$ . In fact, due to the functional form of  $E_{\text{tot}}(\varphi)$  (i.e. depending on angle  $\varphi$  only) it can be shown by simple algebra that the torque component  $T_{\text{CoM}}(\varphi)$  equals the negative derivative of the total energy. For angles between  $\varphi = 0^\circ$  and  $30^\circ$ , negative values of  $T_{\text{CoM}}(\varphi)$  are obtained, which indicates decelerated rotation (labeled “against” in Fig. 3b) and accompanies increasing total energy towards the energy barrier at  $\varphi = 30^\circ$ , see Fig. 3a. On the other hand, angles between  $\varphi = 30^\circ$  and  $60^\circ$  yield positive  $T_{\text{CoM}}(\varphi)$ , suggesting accelerated rotation (labeled “with” in Fig. 3b) which characterizes the motion from the energy barrier towards the equilibrium at  $\varphi = 60^\circ$ . Thus, the results of the torque analysis are consistent with those of the total energy and confirm the general behavior anticipated by the geometry of the symmetrized BTP-BCO.

While the symmetrized BTP-BCO model gives a good qualitative understanding of the rotational motion of the inner BCO rotor, it will not be sufficient to describe all details of the dynamical behavior of the BTP-BCO molecule in reality. This is evident from molecular dynamics studies of BTP-BCO<sup>6</sup> which yield rather complex motions of the complete molecule. The simulations reveal coupled rotations of the two phenylene groups adjacent to the inner BCO as well as of the outer terpyridine groups in addition to flexing and inner vibrations in all fragments. These couplings will distort the BCO rotor, changing its rotational axis with time, and, thus, affect its rotational symmetry. As a result, a prediction of the detailed BCO rotation in the real BTP-BCO molecule based on the present symmetrized and constrained model, chosen to double check rotational aspects of our fragment motion analysis, may become unreliable quantitatively. Clearly, fine details of the molecular motion require conventional quantum calculations which are expensive computationally while our approach gives

a quick and inexpensive way to describe the general rotational behavior of the inner BCO rotor.

### 3.2 Isomer transition in stilbene

The stilbene molecule,  $\text{C}_{14}\text{H}_{12}$ , can be described structurally as  $(\text{C}_6\text{H}_5)-\text{C}=\text{C}-(\text{C}_6\text{H}_5)$ , being composed of two phenyl rings connected by a  $\text{C}=\text{C}$  backbone; the phenyls form very stable and almost rigid entities. It allows two isomers which can be distinguished by the relative positions of the phenyls in the molecule. In the *trans*-stilbene isomer the  $\text{C}_6\text{H}_5$  groups reside on opposite sides of a plane through the  $\text{C}=\text{C}$  backbone whereas the *cis*-stilbene isomer contains the  $\text{C}_6\text{H}_5$  groups on the same side of the plane as shown in Fig. 4a and b (both planes are perpendicular to those of the figures).

These isomers have been extensively studied both by experiment<sup>9,25–28</sup> and theory<sup>10,11,14</sup> as model systems for photochemical *trans*-*cis* isomerization. They have also been proposed for possible applications in molecular electronics where light-driven transitions between the isomers can provide mechanisms for molecular switching devices.<sup>29,30</sup> The more stable of the two isomers is *trans*-stilbene<sup>10</sup> which has been suggested by experiment to be planar in its ground state<sup>25</sup> with slight torsions of the two  $\text{C}_6\text{H}_5$  groups about their *C*-phenyl axes.<sup>14,31</sup> The geometric structure of the *cis* isomer in its ground state, as obtained by quantum chemical calculations,<sup>11</sup> can be obtained qualitatively by rotating the upper phenyl of *trans*-stilbene about the  $\text{C}=\text{C}$  backbone axis by a twist angle of nearly  $180^\circ$ .

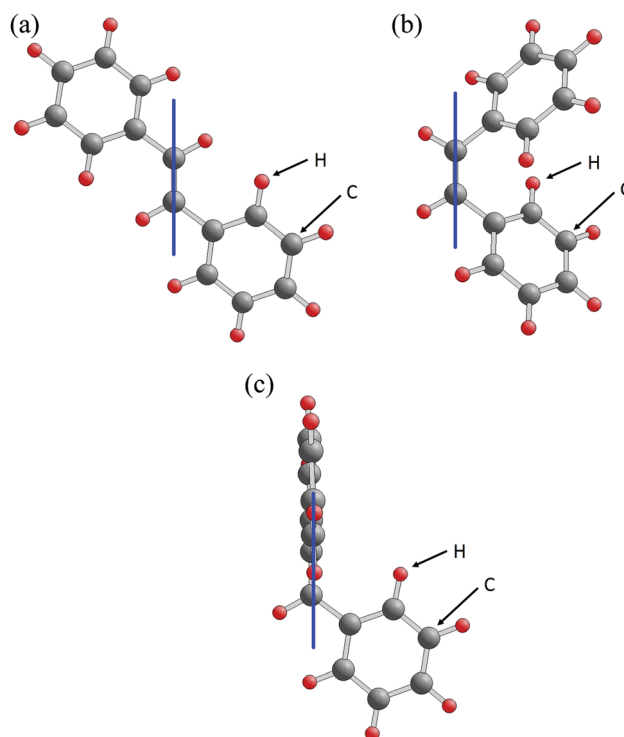


Fig. 4 Ball-and-stick models of stilbene isomers,  $\text{C}_{14}\text{H}_{12}$ . (a) Ground state (GS) geometry of *trans*-stilbene; (b) GS geometry of *cis*-stilbene; (c) transition state (conical intersection, CI) geometry. The  $\text{C}=\text{C}$  backbones in the GS isomers, (a) and (b), are indicated by blue lines.



In addition, the phenyl groups are rotated equally about their *C*-phenyl axes by a rotation angle close to  $40^\circ$  in order to minimize steric repulsion.

Transitions between the two isomers, both *trans* to *cis* and *cis* to *trans*, have been observed by photoexcitation.<sup>12,32,33</sup> The basic mechanism of the isomerization starts from one of the isomers, *e.g.* *trans*-stilbene, in its ground state (GS) which is transferred by photon absorption to an electronically excited state (ES) resulting in forces on the stilbene atoms. This drives the molecule along the ES potential energy surface until it reaches a point where the ES energy surface gets close to that of the GS. At this point, called conical intersection (CI), a transition to the GS is most probable and after the transition the molecule deexcites on the GS energy surface to the alternative isomer conformation, *e.g.* that of *cis*-stilbene.

As to details of the isomer transition, different geometric paths have been postulated.<sup>9,13</sup> In the simplest approach, these paths assume that the stilbene consists of two rigid phenyl groups joined by a C=C backbone where only three types of internal rotations are allowed. The twist rotation about the backbone is quantified by a tetrahedral angle  $\Theta$  (twist angle), illustrated in Fig. 5a. Internal rotations of each of the two phenyls about their corresponding *C*-phenyl axes are defined by dihedral angles  $\alpha_1$  and  $\alpha_2$  (*C*-phenyl angles) as shown in Fig. 5b and c. Thus, the total energy of the molecule along the isomerization path depends only on three parameters, *i.e.*  $E_{\text{tot}} = E_{\text{tot}}(\Theta, \alpha_1, \alpha_2)$  where the GS geometry of the *trans*-stilbene is given by  $\Theta = 180^\circ$ ,  $\alpha_1 = \alpha_2 = 0^\circ$  while *cis*-stilbene is described by  $\Theta$  near  $0^\circ$ ,  $\alpha_1$  and  $\alpha_2$  finite.

Considering the *trans* to *cis* isomerization, one model transition path, denoted as one-bond flip (OBF),<sup>9</sup> is described by a twist rotation only without *C*-phenyl rotations such that, setting  $\alpha_1 = \alpha_2 = 0^\circ$ , the total energy varies only with angle  $\Theta$  ranging from  $180^\circ$  (*trans*) to near  $0^\circ$  (*cis*). As a consequence, the relative orientation of the normal vectors of the two phenyl planes is inverted by the backbone rotation. Along a different model transition path, denoted as hula-twist (HT),<sup>9</sup> one of the *C*-phenyl angles, for example  $\alpha_1$ , is allowed to vary from  $0^\circ$  to near  $180^\circ$  (keeping  $\alpha_2 = 0^\circ$ ) while  $\Theta$  changes from  $180^\circ$  to near  $0^\circ$ . This guarantees that the relative orientation of the normal vectors of the two phenyl planes remains similar during the backbone rotation. In the present work, we examine an alternative model path for *trans* to *cis* isomerization which can be described as relaxed one-bond flip (rOBF). Here both the backbone angle and the two *C*-phenyl angles are allowed to vary such that the stilbene keeps its two-fold symmetry  $C_2$  normal to the C=C backbone axis. This constrains the *C*-phenyl angles to  $\alpha_1 = \alpha_2 = \alpha$  and the total energy of the molecule along the isomerization path depends only on two parameters, *i.e.*  $E_{\text{tot}} = E_{\text{tot}}(\Theta, \alpha)$ . The rOBF path can minimize the steric repulsion of the two phenyl rings in the vicinity of the *cis* geometry,  $\Theta$  near  $0^\circ$ , better than the OBF or HT model paths. Interestingly, the rOBF path includes also the geometry of the conical intersection (CI) very near  $\Theta = 90^\circ$ ,  $\alpha = 0^\circ$  considered to be essential for the isomerization as will be discussed below.

Total energy surfaces as well as details of the rOBF path and corresponding physical parameters, discussed in Section 2,

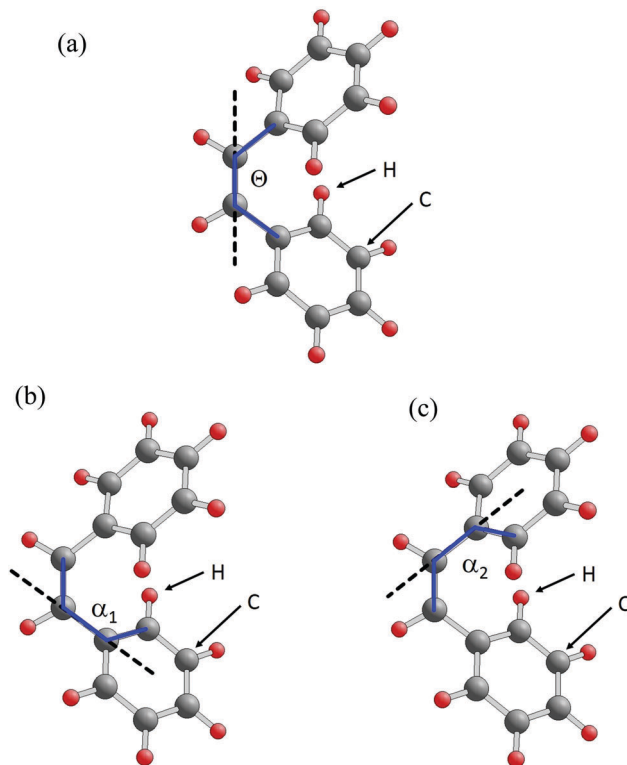


Fig. 5 Definition of rotational angles in the stilbene model isomer. (a) Tetrahedral angle  $\Theta$  (twist angle) describing phenyl rotation about the C=C backbone, (b) and (c) tetrahedral angles  $\alpha_1$ ,  $\alpha_2$  (rotation angles) for rotation of the lower, upper phenyl about the corresponding *C*-phenyl axis. The tetrahedral angles are indicated by blue lines connecting four carbon centers each. The rotation axes are shown by dashed black lines.

are evaluated using density-functional theory (DFT) together with the CAM-B3LYP exchange–correlation functional<sup>34</sup> and extended 6-311g(d) basis sets as implemented in the GAUSSIAN 03 code.<sup>24</sup> The isomerization process involves also electronically excited states of the molecule. Therefore, potential energy surfaces and derived quantities of both the ground and the lowest excited state are considered, where the latter are calculated applying time-dependent DFT.<sup>24</sup>

First, we evaluate total energies  $E_{\text{tot}}(\Theta, \alpha)$  of the molecular ground state for a range of C=C backbone and *C*-phenyl angles,  $0^\circ \leq \Theta \leq 180^\circ$ ,  $-30^\circ \leq \alpha \leq 60^\circ$  to obtain potential energy surfaces (PES) from which the equilibrium geometries of the *trans* and *cis* isomers are determined by energy minimization, see Fig. 6. As a result, *trans*-stilbene at equilibrium is found to be fairly close to planar,  $\Theta = 175^\circ$ ,  $\alpha = -12^\circ$  with the PES being extremely flat for  $\Theta$  between  $175^\circ$  and  $180^\circ$ . We have further verified the equilibrium geometry by unconstrained energy minimizations starting from the constrained equilibrium corresponding to  $\Theta = 175^\circ$ ,  $\alpha = -12^\circ$  which yields good agreement concerning both geometry and total energies. This is consistent with previous quantum chemical studies on the isomer suggesting a planar  $C_{2h}$  symmetry<sup>10</sup> but also slight  $\alpha$  deviations from zero.<sup>10,14</sup> The *cis*-stilbene of  $C_2$  symmetry stabilizes at  $\Theta = 5.5^\circ$ ,  $\alpha = 41.2^\circ$  which is also quite close to results from our corresponding unconstrained minimizations





and agrees with published quantum chemical calculations.<sup>11,14</sup> Further, the ground state PES shows a sharp barrier of 75 and 80 kcal mol<sup>-1</sup> above the equilibrium energies of *cis*- and *trans*-stilbene, respectively, at a C=C backbone angle close to  $\Theta = 90^\circ$  where one phenyl group stands perpendicular to the other, see Fig. 4c, separating between *cis*-like and *trans*-like stilbene isomer geometries. Additional optimizations, fixing the backbone angle at  $\Theta = 90^\circ$  and relaxing the atoms of the (initially planar) phenylene groups, yield an optimized total energy quite close to that with (constrained) planar phenylenes and only very minor geometry differences.

The PES of the lowest excited state of stilbene  $E_{\text{tot}}'(\Theta, \alpha)$  is also included in Fig. 6. It exhibits a pronounced dip for C=C twist angles  $\Theta$  close to  $90^\circ$  such that it gets very close to the ground state PES barrier for the same angles. In fact, for  $\Theta = 90^\circ$ ,  $\alpha = 0^\circ$  the energy difference between the GS and ES surfaces is below 2 kcal mol<sup>-1</sup>. Thus, the two states are almost degenerate, suggesting an energetically very easy transition between them. This defines a conical intersection (CI) available for possible isomerization paths.

The examination of a possible isomerization path between the *cis* and *trans* ground states *via* the transition state at the CI within the rOBF scheme starts from an optimized path on the ground state energy surface  $E_{\text{tot}}(\Theta, \alpha)$ . Here, for given C=C backbone angles  $\Theta$ , between  $0^\circ$  and  $180^\circ$  the C-phenyl angle  $\alpha$  is optimized according to lowest total energy. This yields a path shown in Fig. 7a with the CI transition state near  $\Theta = 90^\circ$ ,  $\alpha = 0^\circ$ . The color coded total energy map evidences the sharp ridge with energy barriers of about 80 kcal mol<sup>-1</sup> near  $\Theta = 90^\circ$ , as mentioned above. This ridge has to be overcome by the isomerization path if a path exclusively along the GS energy

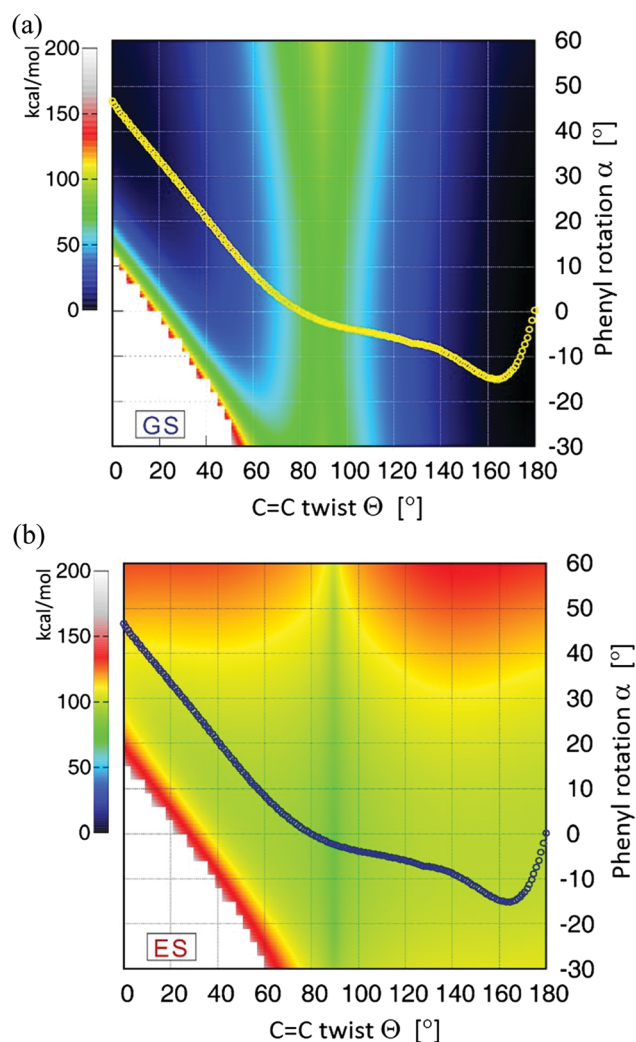


Fig. 7 (a) Ground state total energy map  $E_{\text{tot}}(\Theta, \alpha)$  of stilbene for  $0^\circ \leq \Theta \leq 180^\circ$  and  $-30^\circ \leq \alpha \leq 60^\circ$  with the optimized rOBF transition path between the *cis* isomer ( $\Theta = 5.5^\circ$ ,  $\alpha = 41.2^\circ$ ), the conical intersection (near  $\Theta = 90^\circ$ ,  $\alpha = 0^\circ$ ) and the *trans* isomer ( $\Theta = 175^\circ$ ,  $\alpha = -12^\circ$ ) included as yellow circles, see text. The total energy values are color coded according to the scheme shown to the left. (b) Excited state total energy map  $E_{\text{tot}}'(\Theta, \alpha)$  of stilbene with the optimized GS rOBF transition path included as in (a).

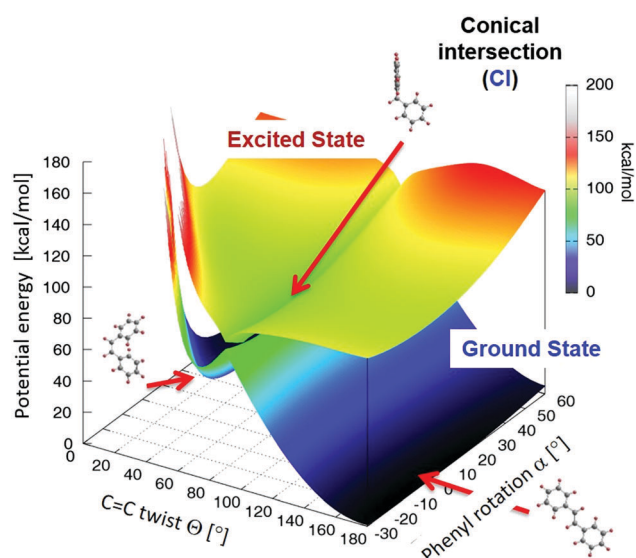


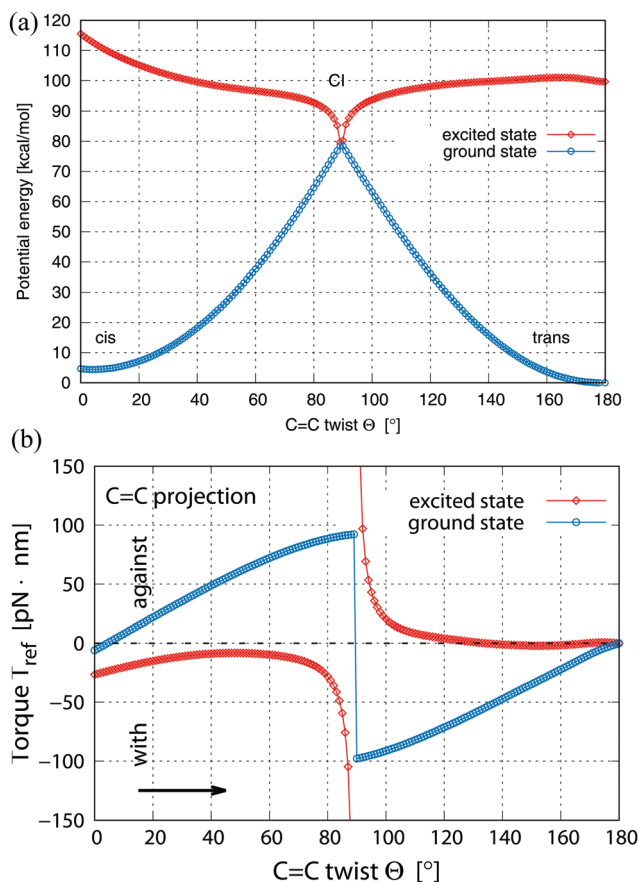
Fig. 6 Perspective view of the stilbene potential energy surface  $E_{\text{tot}}(\Theta, \alpha)$  described in the text. The energies of the ground and lowest excited state surfaces are color coded and labeled accordingly, see inset to the right. Molecular equilibrium structures of the *cis* and *trans* isomers as well as the stilbene geometry at the conical intersection are shown by ball-and-stick models and indicated by red arrows.

surface is assumed. Fig. 7b shows a color coded map of the energy surface  $E_{\text{tot}}'(\Theta, \alpha)$  of the lowest excited state with an approximate rOBF isomerization path which is assumed to be geometrically identical with that of the ground state, see Fig. 7a. This assumption is reasonable as evidenced by the behavior of  $E_{\text{tot}}'(\Theta, \alpha)$  near the isomerization path shown in Fig. 7b. The approximate excited state path crosses the energy dip at the conical intersection near  $\Theta = 90^\circ$  with energies that are very close to those of the ground state path; this is also clear from the ground and excited state total energies along the transition path shown in Fig. 8a.

Altogether, this suggests an isomerization transition between *cis*- and *trans*-stilbene based on an rOBF model path which combines the ground and lowest excited state energy surfaces. Here the *cis* isomer at equilibrium is initially excited from its







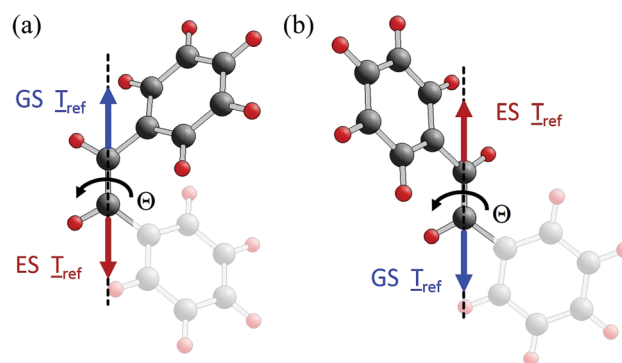
**Fig. 8** (a) Total energies  $E_{\text{tot}}(\Theta, \alpha)$  of stilbene along the rOBF transition path, assumed to be the ground state path. For each C=C twist angle  $0^\circ \leq \Theta \leq 180^\circ$ , the C-phenyl angle  $\alpha$  has been optimized (*cis* isomer at  $\Theta = 5.5^\circ$ ,  $\alpha = 41.2^\circ$ , CI near  $\Theta = 90^\circ$ ,  $\alpha = 0^\circ$ , *trans* isomer at  $\Theta = 175^\circ$ ,  $\alpha = -12^\circ$ ), see text. The energies are given as blue circles for the ground state and as red diamonds for the excited state. (b) Fragment torque  $T_{\text{ref}}(\Theta, \alpha)$  along the rOBF transition path as for (a), see text. The torque values refer to projections of the torque vector onto the C=C backbone axis. For *cis* to *trans* isomerization positive  $T_{\text{ref}}$  values denote the torque pointing opposite to the sense of rotation ("against") while for negative  $T_{\text{ref}}$  values the torque coincides with the sense of rotation ("with"). For *trans* to *cis* isomerization the correlation between torque and sense of rotation is reversed, see also Fig. 9.

ground to the lowest electronically excited state. This can be achieved by absorption of light in a photochemical process<sup>9,32</sup> where the excitation energy from the present calculations amounts to 105 kcal mol<sup>-1</sup> corresponding to soft UV light. This is consistent with the experimental findings.<sup>9</sup> In a subsequent step, the *cis* isomer is distorted by rotation about the C=C backbone axis combined with *O*-phenyl rotations descending on the excited state PES until it reaches the CI where its two phenyl groups are perpendicular to each other. At the CI the stilbene can easily switch to the ground state PES after which it descends further to become an almost planar *trans* isomer in the ground state. Due to the approximate symmetry of the energy curves w.r.t. the CI in Fig. 8a, the inverse isomerization transition between *trans*- and *cis*-stilbene can be described in a completely analogous way within the rOBF concept. For the *trans* isomer the

initial excitation energy from the present calculations amounts to 100 kcal mol<sup>-1</sup>, only slightly smaller than for the *cis* isomer.

The initial electronic excitation of the *cis*- to *trans*-stilbene isomerization transfers the *cis* isomer from its ground state to the lowest excited state, where the former reflects an equilibrium geometry while the latter does not. As a consequence, the atoms experience forces in the excited state which gives rise to torques of the phenyl fragments with respect to each other. The calculated torque on one of the fragments projected onto the C=C backbone axis,  $T_{\text{ref}}$ , is given as a function of the C=C twist angle  $\Theta$  in Fig. 8b. Here positive  $T_{\text{ref}}$  values denote torques pointing against the sense of the *cis* to *trans* rotation, thus, hindering the isomerization, while negative  $T_{\text{ref}}$  values point along the sense of rotation and support the isomerization. This is also sketched in Fig. 9 for the upper phenyl fragment. A comparison of Fig. 8a with b illustrates that along the chosen transition path the torque component parallel to the C=C axis equals the derivative of the total energy with respect to angle  $\Theta$  which can also be proven analytically. Fig. 8b evidences that for the rOBF path along the ground state PES (blue circles)  $T_{\text{ref}}$  values are positive between the *cis*-stilbene equilibrium, at  $\Theta = 5.5^\circ$ , and the CI, near  $\Theta = 90^\circ$ . Thus, the fragment torque in the ground state works against the isomer rotation for  $\Theta \leq 90^\circ$ , which is compatible with the isomer climbing toward the energetic transition barrier. At the CI  $T_{\text{ref}}$  jumps to negative values, decreasing to zero at the *trans*-stilbene equilibrium, at  $\Theta = 175^\circ$ . This means that the fragment torque favors the isomer rotation along the ground state PES for  $\Theta \geq 90^\circ$ , which is understood as the isomer going down in energy from the transition barrier along the path.

Fig. 8b includes also the rOBF path along the excited state PES (red diamonds). Here  $T_{\text{ref}}$  shows an opposite behavior compared with that of the ground state. For rotation angles between the *cis*-stilbene equilibrium and the CI, i.e. below  $\Theta = 90^\circ$ , the  $T_{\text{ref}}$  values are always negative. Thus, the fragment torque supports the isomer rotation for  $\Theta \leq 90^\circ$ . This is compatible



**Fig. 9** Torque directions along the C=C backbone,  $T_{\text{ref}}$ , for two characteristic angles of rotation about the backbone. (a)  $\Theta = 15^\circ$ , towards *trans* isomer equilibrium; (b)  $\Theta = 140^\circ$ , towards *cis* isomer equilibrium. The vectors  $T_{\text{ref}}$  are shown by blue (ground state, GS) and red (excited state, ES) arrows, while the rotation axis is indicated by a dashed line with the sense of rotation for the *cis*- to *trans*-stilbene isomerization denoted by a black curved arrow.



with the isomer approaching the energetic dip of the excited state PES along the path near the CI. At the CI  $T_{\text{ref}}$  switches to strongly positive values, decreasing to zero at the *trans*-stilbene equilibrium. Thus, the fragment torque hinders the isomer rotation along the excited state PES for  $\theta \geq 90^\circ$ , again in tune with the isomer increasing its energy from the transition barrier along the path. The absolute torque values close to the CI increase by much more along the excited state path than along the ground state path. This is connected with the fact that the dip in the excited state PES near the CI is much sharper than the corresponding ridge of the ground state PES. However, some of this difference may be attributed to numerical inaccuracies due to convergence problems of the excited state wavefunctions very close to the CI. Altogether, the torque results are consistent with the total energy behavior along the *cis*- to *trans*-stilbene isomerization path within the rOBF model and confirm the combination of ground and lowest excited state energy paths supporting the photochemical process discussed above.

The inverse *trans*- to *cis*-stilbene isomerization (going from right to left in Fig. 7 and 8 along a reversed rOBF path) can be understood by the same energetic and torque behavior as for *cis* to *trans* isomerization. Due to the reversed variation of  $\theta$ , positive  $T_{\text{ref}}$  values in Fig. 8b refer to torques pointing along the sense of *trans* to *cis* rotation, thus, supporting the isomerization; negative  $T_{\text{ref}}$  values point against the sense of rotation and hinder the isomerization. Fig. 9a, b evidence that, starting from the *trans*-stilbene ground state, at  $\theta = 175^\circ$ , and after excitation to the lowest excited state, the total energy decreases along the transition path towards the CI at  $\theta = 90^\circ$ , which is supported by the torque along the C=C backbone axis. After switching to the ground state PES at the CI, the total energy decreases further towards the *cis*-stilbene equilibrium at  $5.5^\circ$ , which is again confirmed by the torque along the C=C backbone axis.

## 4. Conclusions

The complex motion of atoms inside large molecules can be analyzed by considering translation, rotation, and flexibility of molecular fragments within the molecule and by applying classical mechanics based on quantum mechanical Pulay forces on the atoms. In this work we propose a simple fragment motion analysis which provides a basic qualitative understanding of the motion of the different molecular components with emphasis on fragment rotation. This allows us to efficiently predict motion paths and can help design simplified fragment paths in the multi-dimensional configuration space. Examples are rotations of a flexible rotator with respect to its flexible stator counterpart in a rotor molecule, but also rotational isomerization paths inside a large molecule.

After dealing in detail with formal aspects of the fragment motion analysis, we have discussed two example applications where the analysis of fragment torques can give additional insight into the mechanism of rotational motion beyond total energy considerations. In the symmetrized model of the

BTP-BCO molecule, the rotation of the inner BCO rotator is well described by the periodic variation of the total energy as a function of the rotation angle  $\phi$ . Here the results of the torque analysis are confirmed to be consistent with those of the total energy and efficiently predict the general behavior anticipated by the geometry of the molecule. Further, model paths describing the photochemical isomerization between *cis*- and *trans*-stilbene by a relaxed one-bond flip (rOBF) scheme are examined in detail and verify the mechanism proposed earlier. After an initial excitation of the isomer from its equilibrium ground state to its lowest excited state (which is induced experimentally by UV light absorption) the molecule relaxes by rotating about its C=C backbone axis with additional rotation of the phenyl groups about their *C*-phenyl axes. This allows stilbene to reach a conical intersection where it can easily switch from the excited state energy surface to the ground state surface, after which it can relax further to the equilibrium of the alternative isomer. The torque analysis for the molecule confirms and illustrates the isomerization mechanism suggested by the rOBF model paths along the different potential energy surfaces and supports the photochemical process.

The mechanical analysis together with the concept of fragment motion will prove its usefulness in subsequent studies which include more complex types of motion. Examples are combinations of fragment translation and rotation as found in [c2]daisy chain supramolecules<sup>7,8</sup> or the influence of fragment flexibility as identified in molecular dynamics calculations on BTP-BCO. Also details of interlocking rotor molecules, such as those examined recently,<sup>35,36</sup> will be interesting as candidates for the mechanical analysis. Studies along these lines are currently under way.

## Conflicts of interest

There are no conflicts of interest to declare.

## Acknowledgements

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