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First-principles method for calculating the rate constants of internal-conversion and intersystem-crossing transitions†

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A method for calculating the rate constants for internal-conversion (k_{IC}) and intersystem-crossing (k_{ISC}) processes within the adiabatic and Franck–Condon (FC) approximations is proposed. The applicability of the method is demonstrated by calculation of k_{IC} and k_{ISC} for a set of organic and organometallic compounds with experimentally known spectroscopic properties. The studied molecules were pyromethene-567 dye, psoralene, hetero[8]circulenes, free-base porphyrin, naphthalene, and larger polyacenes. We also studied *fac*-Alq₃ and *fac*-Ir(ppy)₃, which are important molecules in organic light emitting diodes (OLEDs). The excitation energies were calculated at the multi-configuration quasi-degenerate second-order perturbation theory (XMC-QDPT2) level, which is found to yield excitation energies in good agreement with experimental data. Spin–orbit coupling matrix elements, non-adiabatic coupling matrix elements, Huang–Rhys factors, and vibrational energies were calculated at the time-dependent density functional theory (TDDFT) and complete active space self-consistent field (CASSCF) levels. The computed fluorescence quantum yields for the pyromethene-567 dye, psoralene, hetero[8]circulenes, *fac*-Alq₃ and *fac*-Ir(ppy)₃ agree well with experimental data, whereas for the free-base porphyrin, naphthalene, and the polyacenes, the obtained quantum yields significantly differ from the experimental values, because the FC and adiabatic approximations are not accurate for these molecules.

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1. Introduction

Molecular photophysics is a rapidly developing research area of molecular and chemical physics.^{1–3} Interaction of the electromagnetic radiation with molecules, molecular luminescence properties, and transformations of excited electronic energy into vibrational energy are important photophysical processes. Detailed knowledge about these photophysical properties is needed when designing optical molecular devices such as organic light-emitting diodes,^{4,5} laser applications,⁶ and other devices that convert light energy or other forms of energy.⁷ The mechanism of light-induced processes such as the light absorption of photosynthesis can also be understood by studying the photophysical properties of the chlorophylls and other involved molecules.⁸

Photophysical processes in molecules can be divided into intramolecular and intermolecular ones.⁹ The intermolecular processes play a key role in luminescence quenching and

in deactivating excited electronic states at high molecular concentrations,¹⁰ whereas the intramolecular processes depend almost completely on the intrinsic properties of the molecule.¹¹ Photophysical properties like the quantum yields of fluorescence (ϕ_f) and phosphorescence (ϕ_{phos}) are determined by the ratio between the rate constants of radiative (k_r) and nonradiative (k_{nr}) intramolecular processes.^{9,10}

When a photon is absorbed, molecular systems transfer from the ground state to an excited electronic state, and they can be de-excited *via* different channels. Radiative deactivation channels comprise emission of a photon with an energy that is smaller than or equal to the excitation energy. Nonradiative channels do not involve any photon emission but the excess energy transfers to vibrational energy leading to an increase of the temperature. Internal conversion (IC) and the intersystem crossing (ISC) are main intramolecular nonradiative processes.^{9–11} The electronic energy in both processes is converted into molecular vibrations. In the case of IC, the spin multiplicity of the molecule is conserved, whereas ISC involves the initial and final states of different spin multiplicities.¹ The IC process occurs due to nonadiabatic coupling interactions. ISC is caused by the spin–orbit coupling interaction. When the concentration of molecules is low, it can be assumed that the total rate constant for the nonradiative process is the sum of the rate

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constants of the two channels $k_{\text{nr}} = k_{\text{IC}} + k_{\text{ISC}}$, where k_{IC} and k_{ISC} are the rate constants for IC and ISC, respectively.^{9,12} The total rate constant for the nonradiative process k_{nr} can be estimated experimentally from the quantum yields (ϕ_{fl} , ϕ_{phos}) and from the rate constant of the radiative processes (k_{r}).^{9,10} However, the experimental determination of k_{IC} and k_{ISC} is very difficult.^{13,14} The rate constants for the radiative transitions can be calculated quantum chemically^{15–17} employing nonadiabatic molecular dynamics simulations at *ab initio* levels of theory^{18–22} or by using specific approximations considering empirical corrections.^{1,15,23} Molecular dynamics simulations are computationally expensive, which limits their application to smaller molecular systems. The semiempirical approach by Plotnikov, Artyukhov and Maier, which is based on the incomplete neglected differential overlap (INDO) method with a spectroscopic parameterization, can be used for calculating the photophysical properties of large organic molecules.^{24–31} Maier and Artyukhov employed computational methods based on the theory developed by Robinson, Jortner¹¹ and Plotnikov²⁴ to estimate k_{IC} and k_{ISC} at the INDO level of theory.^{25–28} They calculated the matrix elements of the nonadiabatic coupling and spin-orbit coupling operators for the singlet and triplet electronic states at the INDO level of theory, whereas the vibrational integrals were estimated from the experimental spectroscopic data. The INDO approach renders routine calculations of k_{IC} and k_{ISC} for large organic molecules consisting of up to 200 atoms feasible.

However, the semiempirical INDO approach of Artyukhov and Maier can be applied only to molecules consisting of light atoms such as H, C, N, O, F, S, and Cl, whereas it cannot be employed in studies of photophysical properties of organometallic compounds. The semiempirical method has also been found to lead to large errors in the rate constants k_{IC} and k_{ISC} for porphyrins and [8]circulenes, because the INDO calculations are not able to provide accurate electronic excitation energies for these molecules. A better accuracy has been obtained for porphyrins and [8]circulenes by combining the INDO method with excitation energies calculated at the time-dependent density functional theory (TDDFT) and correlated *ab initio* levels of theory.^{29–33} However, for some [8]circulenes the matrix elements of the nonadiabatic coupling (NACME) and the spin-orbit coupling (SOCME) operators calculated at the INDO level were found to be inaccurate. In this work, the electronic excitation energies, the coupling matrix elements, and the vibrational integrals are calculated at the density functional theory (DFT) and correlated *ab initio* levels of theory, opening new possibilities of employing the theory of Plotnikov, Robinson, and Jortner without relying on any semiempirical parameters.

In this work we employ the theory of Plotnikov, Robinson, Jortner²⁴ using NACME and SOCME calculated at the DFT and *ab initio* levels to obtain accurate values for the k_{IC} and k_{ISC} rate constants for nonradiative intramolecular transitions. The methods have been used in studies of pyromethene-567 dye, psoralene, acenes, *fac*-Alq₃, *fac*-Ir(ppy)₃, hetero[8]circulenes, and free-base porphyrin, which are important in the different

research areas of photonics. The reference values for the rate constants are also available for these molecules,^{34–40} since the photophysical properties of these compounds have previously been studied by other groups.^{29,31,33}

2. Theory

2.1. Non-radiative electronic transitions

The general expression for the rate constant of non-radiative electronic transitions derived by Plotnikov, Robinson, Jortner reads^{11,24}

$$k_{\text{nr}} = \sum_n |V_{i0,fn}|^2 \Gamma_{fn} \left[\Delta_{if}^2 + \frac{\Gamma_{fn}^2}{4} \right]^{-1}, \quad (1)$$

where i is the initial electronic state, f is the final electronic state, n is a vibrational level of f , Γ_{fn} is the relaxation width of the vibronic level $|fn\rangle$, $\Delta_{if} = |E_{i0} - E_{fn}|$ is the energy difference between the initial and final vibronic states, and $V_{i0,fn}$ is the matrix element of the perturbation operator. Only the lowest vibronic state is considered for the initial state. The perturbation operator is the spin-orbit coupling interaction for ISC transitions and the non-adiabatic coupling interaction for the IC process. eqn (1) written in atomic units holds at ambient temperatures ($T \leq 300$ K) when $k_{\text{nr}} \ll \Gamma_{fn}$. The conditions are generally fulfilled in experimental studies of luminescence properties. Γ_{fn} of about 10^{14} s^{-1} is generally much larger than the k_{nr} of about 10^7 – 10^{12} s^{-1} .²⁴ The Δ_{if} value is not larger than 100 cm^{-1} for polyatomic molecules.²⁴ The expression can be simplified to eqn (2) when assuming that Γ_{fn} depends only weakly on the vibrational level n and that $\Delta_{if} \ll \Gamma_{fn}$.²⁴

$$k_{\text{nr}} = \frac{4}{\Gamma_{\text{f}}} \sum_n |V_{i0,fn}|^2. \quad (2)$$

2.2. IC rate constant

In the framework of the adiabatic and Franck-Condon (FC) approximation, $V_{i0,fn}$ can be written as^{24,41}

$$V_{i0,fn} = \langle i | T_{\text{R}} | f \rangle \cdot \langle 0 | n \rangle - \sum_{\nu} M_{\nu}^{-1} \left\langle 0 \left| \frac{\partial}{\partial R_{\nu}} \right| n \right\rangle \cdot \left\langle i \left| \frac{\partial}{\partial R_{\nu}} \right| f \right\rangle, \quad (3)$$

where T_{R} is the kinetic energy operator of the electrons, ν is a nuclear index, M_{ν} is the mass of nucleus ν , $\left\langle i \left| \frac{\partial}{\partial R_{\nu}} \right| f \right\rangle$ is the nonadiabatic coupling matrix element between the electronic states $|i\rangle$ and $|f\rangle$, $|0\rangle$ is the lowest vibration state of $|i\rangle$ and $|n\rangle$ is a vibration state of the final electronic state $|f\rangle$, R_{ν} is the nuclear coordinates of nucleus ν , and $\left\langle 0 \left| \frac{\partial}{\partial R_{\nu}} \right| n \right\rangle$ is the nonadiabatic coupling matrix element between $|0\rangle$ and $|n\rangle$. The $\left\langle i \left| \frac{\partial}{\partial R_{\nu}} \right| f \right\rangle$ and $\left\langle 0 \left| \frac{\partial}{\partial R_{\nu}} \right| n \right\rangle$ integrals are calculated for the equilibrium geometry ($R = R_0$) of the $|f\rangle$ state. Since the first term in eqn (3)

is usually much smaller than the second term, eqn (3) can be written as^{24,42}

$$V_{i0,fn} = - \sum_{\nu} M_{\nu}^{-1} \left\langle 0 \left| \frac{\partial}{\partial R_{\nu}} \right| n \right\rangle \cdot \left\langle i \left| \frac{\partial}{\partial R_{\nu}} \right| f \right\rangle, \quad (4)$$

which can be expressed in Cartesian coordinates as

$$V_{i0,fn} = - \sum_{\nu} \sum_{q=x,y,z} M_{\nu}^{-1} \left\langle 0 \left| \frac{\partial}{\partial R_{\nu q}} \right| n \right\rangle \cdot \left\langle i \left| \frac{\partial}{\partial R_{\nu q}} \right| f \right\rangle. \quad (5)$$

$\left\langle 0 \left| \frac{\partial}{\partial R_{\nu q}} \right| n \right\rangle$ can be written using normal coordinates when the rotational and translational motions have been identified and removed

$$\left\langle 0 \left| \frac{\partial}{\partial R_{\nu q}} \right| n \right\rangle = \left\langle 0_1 0_2 \dots 0_{3N-6} \left| \sum_{j=1}^{3N-6} B_{\nu q j} \frac{\partial}{\partial Q_j} \right| n_1 n_2 \dots n_{3N-6} \right\rangle, \quad (6)$$

In eqn (6), $|0_k\rangle$ and $|n_k\rangle$ are the harmonic oscillator wave functions of the initial and final states, n_k is the n th excitation of the k th oscillator, Q_j is the normal coordinate of the j th oscillator, $B_{\nu q j}$ are matrix elements that describe the connection between the displacements in Cartesian coordinates of ν th atom ($\Delta R_{\nu q}$) in respect to the equilibrium of and normal coordinate (Q_j). By inserting eqn (6) into eqn (5) one obtains

$$V_{i0,f\{n_1 n_2 \dots n_{3N-6}\}} = - \sum_{\nu} \sum_{q=x,y,z} M_{\nu}^{-1} \left\langle i \left| \frac{\partial}{\partial R_{\nu q}} \right| f \right\rangle \times \left[\sum_{j=1}^{3N-6} B_{\nu q j} \left\langle 0_j \left| \frac{\partial}{\partial Q_j} \right| n_j \right\rangle \prod_{\substack{k \neq j \\ k=1}}^{3N-6} \langle 0_k | n_k \rangle \right] \quad (7)$$

$\left\langle 0_j \left| \frac{\partial}{\partial Q_j} \right| n_j \right\rangle$ can be expressed in harmonic approximation as

$$\left\langle 0_j \left| \frac{\partial}{\partial Q_j} \right| n_j \right\rangle^2 = \frac{1}{2n_j!} \omega_j (n_j - y_j)^2 y_j^{n_j-1} \cdot \exp(-y_j), \quad (8)$$

where y_j is the Huang–Rhys factor and ω_j is the vibration frequency of the j th mode. The Franck–Condon factor $\langle 0_k | n_k \rangle$ can then be written as⁴¹

$$\langle 0_k | n_k \rangle^2 = \frac{\exp(-y_k) y_k^{n_k}}{n_k!}. \quad (9)$$

The final expression is obtained by inserting eqn (8) and (9) into eqn (7):

$$V_{i0,f\{n_1 n_2 \dots n_{3N-6}\}} = - \sum_{\nu} \sum_{q=x,y,z} M_{\nu}^{-1} \left\langle i \left| \frac{\partial}{\partial R_{\nu q}} \right| f \right\rangle \times \left[\left(\prod_{\substack{k \neq j \\ k=1}}^{3N-6} \sqrt{\frac{\exp(-y_k) y_k^{n_k}}{n_k!}} \right) \times \left(\sum_{j=1}^{3N-6} B_{\nu q j} \sqrt{\frac{1}{2n_j!} \omega_j (n_j - y_j)^2 y_j^{n_j-1} \exp(-y_j)} \right) \right]. \quad (10)$$

The IC rate constant can be calculated using

$$k_{IC} = \frac{4}{\Gamma_f} \sum_{n_1, n_2, \dots, n_{3N-6}}^{E_{if} = n_1 \omega_1 + n_2 \omega_2 + \dots + n_{3N-6} \omega_{3N-6}} (V_{i0,f\{n_1 n_2 \dots n_{3N-6}\}})^2, \quad (11)$$

where the expression for $V_{i0,f\{n_1 n_2 \dots n_{3N-6}\}}$ is given in eqn (10). E_{if} is the energy gap between the electronic states $|i\rangle$ and $|f\rangle$.

2.3. ISC rate constant

The spin–orbit coupling is the perturbation operator of the ISC process. The spin–orbit coupling matrix elements depend only on the space and spin coordinates of the electrons but not on the nuclear ones.^{1,24} The expression for the ISC rate constant can then be written as

$$k_{ISC} = \frac{4}{\Gamma_f} \sum_n \langle i | H_{SO} | f \rangle^2 \cdot \langle 0 | n \rangle^2 = \frac{4}{\Gamma_f} \langle i | H_{SO} | f \rangle^2 \left(\sum_{n_1, n_2, \dots, n_{3N-6}}^{E_{if} = n_1 \omega_1 + n_2 \omega_2 + \dots + n_{3N-6} \omega_{3N-6}} \prod_{k=1}^{3N-6} \sqrt{\frac{\exp(-y_k) y_k^{n_k}}{n_k!}} \right)^2. \quad (12)$$

The excitations of the normal vibrations with the high frequency at $\omega = \sim 1000\text{--}1800\text{ cm}^{-1}$ and significant Huang–Rhys factor ($y > 0.1$) are the largest contributions to the summation ($E_{if} = n_1 \omega_1 + n_2 \omega_2 + \dots + n_{3N-6} \omega_{3N-6}$) in the expressions for the FC factor in eqn (11) and (12).^{6,12,24}

2.4. Parameters for the calculation of the ISC and IC rate constants

To calculate the ISC and IC rate constants, values for $\left\langle i \left| \frac{\partial}{\partial R_{\nu q}} \right| f \right\rangle$, $\langle i | H_{SO} | f \rangle$, y_j and ω_j , E_{if} and Γ_f are needed. In this work, $\left\langle i \left| \frac{\partial}{\partial R_{\nu q}} \right| f \right\rangle$ is calculated for molecules consisting of more than 50 atoms at the TDDFT level using Turbomole⁴² and for smaller molecules they are calculated at the CASSCF level of theory in GAMESS-US.⁴³ The Huang–Rhys factors and the vibration frequencies (ω_j) are calculated at the DFT and correlated *ab initio* levels of theory.⁴⁴ The $\langle i | H_{SO} | f \rangle$ matrix elements have been computed at the CASSCF and TDDFT levels.^{45,46} The line width (Γ_f) has been estimated using the Lax and Pekar models^{47–49} in the simulation of molecular vibronic spectra using the displaced oscillator model.

3. Computational methods and studies

3.1 Studied molecules

The computational methods described above have been employed on a number of molecules with interesting photophysical properties. The studied molecules shown in Fig. 1 comprise the commercial laser dye 1,3,5,7,8-pentamethyl-2,6-diethylpyrromethene-difluoroborate (PM567),³⁴ 7H-furo[3,2-g]chromen-7-one (psoralene),³⁵ *fac*-tris(8-hydroxyquinolinato)aluminium (*fac*-Alq₃)³⁸ and *fac*-tris(2-phenylpyridine)iridium (*fac*-Ir(ppy)₃),³⁹ tetraoxa[8]circulene (4B)³⁶ and its NH substituted and benzoannelated derivatives

Fig. 1 The molecular structures of the studied molecules.

(AOC) and (1B3N),²⁹ polyacenes (naphthalene, anthracene, tetracene, pentacene, and hexacene),³⁷ and free-base porphyrin (H₂P).⁴²

The molecules were chosen for the following reasons. PM567 has a very large fluorescence quantum yield of $\phi_{\text{fl}} = 0.9\text{--}1.0$ and is therefore often used in laser devices.³⁸ Psoralene has a very small fluorescence quantum yield of $\phi_{\text{fl}} \sim 0.1$ and a large k_{ISC} ³⁷ and is therefore used in photodynamic therapy applications.³⁷ Alq₃ and Ir(ppy)₃ are used in OLED devices.^{38,39} The electroluminescence of Alq₃ and Ir(ppy)₃ is due to fluorescence and phosphorescence, respectively.^{38,39} The photophysical properties of [8]circulenes have previously been studied by us at the INDO level of theory using the method of Plotnikov, Robinson, Jortner.²⁹

The chosen compounds have very different fluorescence quantum yields ϕ_{fl} . The fluorescence spectrum of the polyacenes has a complicated vibronic fine structure requiring calculations of transition moments between many excited states with different spins.⁵⁰ The energy gap between the first excited singlet state (S_1) and the ground state (S_0) systematically reduces from the ultraviolet to infrared spectral region when increasing the number of benzoic rings in the polyacene.⁵⁰ The calculations on the polyacenes yield a relation between k_{IC} and the optical gap. The present approach is also applied to free-base porphyrin (H₂P), because it is well known that the calculation of k_{IC} and k_{ISC} for H₂P is challenging.¹

3.2 Computational methods

The molecular structures of the ground electronic states (S_0) of all the molecules except Alq₃ and Ir(ppy)₃ were optimized at the density functional theory (DFT) level⁵¹ using the B3LYP⁵² exchange–correlation functional and def2-TZVP⁵³ basis sets. For Alq₃ and Ir(ppy)₃, the ω B97xD functional was employed in the DFT optimization of the molecular structures.⁵⁴ The def2-TZVP basis sets were used for Alq₃. For Ir(ppy)₃, we used the LANL2DZ basis set and effective core potentials for Ir and the 6-31G(d,p) basis sets for the rest of the atoms.⁵⁵ The equilibrium geometry of the first excited electronic state (S_1) was obtained at the TDDFT/B3LYP/def2-TZVP level of theory for PM567, psoralene, polyacenes, and free-base porphyrin. The molecular structures of the first excited state (S_1) of Alq₃ and Ir(ppy)₃ were optimized at the TDDFT level using the ω B97xD functional.⁵⁴

We chose the ω B97xD functional for Alq₃ and Ir(ppy)₃, because difficulties arise when using the B3LYP functional to properly describe excited states of metal–ligand compounds with significant charge-transfer characteristics, whereas the ω B97xD functional is expected to be able to describe such states better, since it has the correct long-range shape of the potential.³⁹ The molecular structure optimizations were carried out using Gaussian-09 software.⁵⁶ Only the lowest isomers of fac-Alq₃ and fac-Ir(ppy)₃ were considered.

Calculations of singlet and triplet excitation energies were carried out using the extended multi-configuration quasi-degenerate perturbation theory at the second order (XMC-QDPT2),⁵⁷ because this level of theory has been found to yield the correct relative order of the lowest singlet and triplet electronic states for organic and organometallic compounds.⁵⁸ The XMC-QDPT2 calculations were performed using the optimized molecular structures of the S_1 state. In the XMC-QDPT2 calculations, 30 states were included in the effective Hamiltonian. The number of active electrons (e), number of active orbitals (o), and the number of states (s) of the state-average (SA) complete active self-consistent space field (CASSCF) calculations are PM567 (8 e, 6 o, 5 s), psoralene (10 e, 9 o, 5 s), Alq₃ (12 e, 9 o, 5 s), Ir(ppy)₃ (12 e, 9 o, 5 s), tetraoxa[8]circulene (4B) (10 e, 10 o, 10 s), o-dinaphthalene-containing azatrioxa[8]circulene (AOC) (10 e, 10 o, 10 s), trinaphthalene-containing tetraoxa[8]circulene (1B3N), (10 e, 11 o, 10 s), free-base porphyrin (H₂P) (11 e, 14 o, 10 s), naphthalene (12 e, 9 o, 10 s), anthracene (10 e, 10 o, 10 s), tetracene (10 e, 11 o, 10 s), pentacene (8 e, 8 o, 10 s), and hexacene (8 e, 8 o, 10 s). The XMC-QDPT2 calculations were carried out using Firefly.⁵⁹

The discrepancy between the TDDFT and XMC-QDPT2 excitation energies for the $S_1 \rightarrow S_0$ electronic transitions does not exceed 1000–1500 cm^{−1} for any of the studied compounds. Thus, a combination of the XMC-QDPT2 and TDDFT levels of theory can be used in the calculation of photophysical properties.

3.3 Huang–Rhys factors and vibrational relaxation widths

The y_j , ω_j , and Γ_f values were obtained using the Lax and Pekar model,^{47–49} which is described in detail in ref. 48 and 49.

The potential energy surfaces of S_0 and S_1 are assumed to be harmonic with the same vibrational energies (ω_j) for the two states. The energy functions for the two states can then be written as

$$E^i(Q) = E^i(Q^0) + \sum_j V_j^i (Q_j - Q_j^0) + \frac{1}{2} \sum_j \omega_j^2 (Q_j - Q_j^0)^2,$$

$$E^f(Q) = E^f(Q^0) + \sum_j V_j^f (Q_j - Q_j^0) + \frac{1}{2} \sum_j \omega_j^2 (Q_j - Q_j^0)^2 \quad (13)$$

where $\{Q\}$ is the set of normal coordinates of the harmonic oscillators, $V_j^{i,f} = \partial E^{i,f} / \partial Q_j|_{Q=Q^0}$ is the gradient of the potential energy surface along the j th mode at a chosen point Q^0 . From eqn (13) it is easily seen that

$$\frac{\partial E^{i,f}(Q)}{\partial Q_j} = V_j^{i,f} + \omega_j^2 (Q_j - Q_j^0)$$

$$\frac{\partial E^f(Q)}{\partial Q_j} - \frac{\partial E^i(Q)}{\partial Q_j} = V_j^f - V_j^i = \text{const} \quad (14)$$

$$Q_j^{i,f} - Q_j^0 = -\frac{V_j^{i,f}}{\omega_j^2}.$$

Thus, $\Delta Q_j = -(V_j^f - V_j^i)/\omega_j^2$ and finally the Huang-Rhys factors (y_j) are obtained as

$$y_j = \frac{1}{2} \omega_j \Delta Q_j^2 = \frac{(V_j^f - V_j^i)^2}{2\omega_j^3}. \quad (15)$$

The line width Γ_f is taken from the generation function for the simulation of the profile of the vibration spectra within the Lax-Pekar model.^{47–49} The calculated value for Γ_f is about $1.6 \times 10^{14} \text{ s}^{-1}$ for the S_1 state of the studied molecules.

The optimized molecular structures of the S_0 and S_1 states as well as the gradient and the Hessian calculated for the S_0 state were used in the calculation of ω_j and $V_j^{i,f}$. In the calculation of the IC rate constants, the Hessian was calculated for the S_0 state, whereas the gradient for the S_1 state was calculated using the molecular structure of the S_0 state. We assume that the vibrational energies (ω_j) and the Huang-Rhys factors y_j are the same for the IC and ISC processes. Our previous calculations showed that this assumption yields good estimates for the ISC rate constants for several molecules.^{29,58}

3.4 Calculation of matrix elements

The nonadiabatic coupling matrix elements $\left\langle S_0 \left| \frac{\partial}{\partial R_{qv}} \right| S_1 \right\rangle$ were calculated with Turbomole at the TDDFT level of theory using the perturbation theory.^{42,60} The spin-orbit coupling matrix elements $\langle S_1 | H_{SO} | T_i \rangle$ between the S_1 state and the energetically lower i th triplet state T_i were calculated at the CASSCF level using Gamess-US.⁶¹ The excitation energies calculated at the XMC-QDPT2 level were used as the zeroth-order values. In order to calculate k_{ISC} , the one-electron spin-orbit coupling operator of the Pauli-Breit Hamiltonian was used.⁶² The contributions from the two-electron part of the spin-orbit coupling operator are beyond the Franck-Condon approximation.¹ However, previous calculations have shown that the use of the one-electron spin-orbit operator within the FC approximation leads to accurate k_{ISC} values for the organic and organometallic compounds.^{29,58,63}

3.5 Radiative rate constants and fluorescence quantum yields

When contributions from higher excited states can be neglected, the fluorescence quantum yield from the S_1 state can be obtained as^{9,12}

$$\varphi_{\text{fl}} = \frac{k_r}{k_r + k_{\text{IC}} + \sum_i k_{\text{IST}_i}}, \quad (16)$$

where k_{IST_i} is a ISC rate constant between S_1 and energetically lower triplet states T_i , k_r and k_{IC} are the radiative and IC rate constants of the electronic transition from S_1 to S_0 , respectively. The k_r can be estimated using the Strickler-Berg equation⁶⁴

$$k_r = \frac{1}{1.5} \cdot f \cdot E^2(S_1 \rightarrow S_0), \quad (17)$$

where f is the oscillator strength and $E(S_1 \rightarrow S_0)$ is the de-excitation energy from S_1 to S_0 .

The table illustrating the employed level of theory is given for clear understanding of the subsequent discussions (Table 1).

4. Results and discussion

4.1. Pm567

The optimized molecular structure of the S_1 state is shown in Fig. 2a. The energy levels of the lowest singlet and triplet states and the k_{IC} and k_{ISC} rate constants of the transitions are shown

Table 1 The employed levels of theory for the compounds under investigation

Properties	PM567, psoralene, [8]circulenes and H ₂ P, polyacenes	Alq ₃	Ir(ppy) ₃
Geometries of S_0 and S_1 states	DFT/B3LYP/def2-TZVP	DFT/ ω B97xD/def2-TZVP	DFT/ ω B97xD/LANL2DZ and 6-31G(d,p)
Energies of $S_1 \rightarrow S_0$ electronic transition and triplet states, oscillator strength (f)	XMC-QDPT2/def2-TZVP	XMC-QDPT2/ ω B97xD/def2-TZVP	XMC-QDPT2/ ω B97xD/LANL2DZ and 6-31G(d,p)
$\left\langle S_0 \left \frac{\partial}{\partial R_{qv}} \right S_1 \right\rangle$	TD-DFT/B3LYP/def2-TZVP	TDDFT/B3LYP/def2-TZVP	TDDFT/B3LYP/def2-TZVP
$\langle S_1 H_{SO} T_i \rangle$	MCSCF/def2-TZVP	MCSCF/ ω B97xD/def2-TZVP	MCSCF/ ω B97xD/LANL2DZ and 6-31G(d,p)
y , ω and Γ	(TD)-DFT/B3LYP/def2-TZVP	(TD)-DFT/ ω B97xD/def2-TZVP	(TD)-DFT/ ω B97xD/LANL2DZ and 6-31G(d,p)

Fig. 2 (a) The optimized molecular structure of PM567. (b) The energy level diagram for PM567 including the computed values for the radiative and nonradiative rate constants.

Table 2 The calculated excitation energies (in eV) of the studied molecules are compared to available experimental data. Calculated oscillator strengths are given in parenthesis

Compound	State	XMC-QDPT2	Exp.
PM567	S ₁	2.13(0.2)	2.22 ^a
	T ₁	1.75	—
	T ₂	2.08	—
Psoralene	S ₁	3.09(0.2)	3.02 ^b
	T ₁	2.75	2.73 ^b
	T ₂	3.02	—
4B	S ₁	2.64	2.44 ^c
	T ₁	1.89	—
	T ₂ (T ₃)	2.58	—
AOC	S ₁	3.00(0.3)	3.02 ^c
	T ₁	1.89	—
	T ₂	2.9	—
1B3N	S ₁	2.68(0.5)	3.08 ^c
	T ₁	2.1	—
	T ₂	2.24	—
	T ₃	2.34	—
	T ₄	2.64	—
H ₂ P	S ₁	1.92	2.01 ^d
	T ₁	1.62	1.58 ^d
	T ₂	1.8	—
Alq ₃	S ₁	2.33(0.1)	2.38–2.48 ^e
	T ₁	1.86	—
Ir(ppy) ₃	S ₁	2.74	2.69 ^f
	T ₁	2.37	2.44 ^f

^a Ref. 38. ^b Ref. 37. ^c Ref. 29. ^d Ref. 40. ^e Ref. 34. ^f Ref. 35.

in Fig. 2b. Table 2 contains the calculated excitation energy of the S₁ state and the excitation energies calculated for the triplet states that are energetically below S₁. The calculated excitation energy for S₁ agrees well with the experimental value with a deviation of only 0.09 eV. The rate constants in Fig. 2b show that k_f is a main deactivation channel of the S₁ state. The largest rate constant among the nonradiative transitions is k_{ISC2} due to the small energy gap between S₁ and T₂. The calculated fluorescence quantum yield (ϕ) is 0.79, which qualitatively

agrees with the experimental one of 0.9.³⁸ Thus, the present approach is able to predict the large (ϕ_f) observed for PM567. The largest values for the Huang–Rhys factors (y_j) and corresponding wavenumbers (ω_j) are given in Table 3. The vibrational mode at 1255 cm^{−1} has a large y value of 0.1. Since only one vibrational mode has a large y value in that energy range the nonradiative rate constants k_{IC} and k_{ISC} are small as compared with the rate constant of the radiative transition k_f .

4.2. Psoralene

The optimized molecular structure of the S₁ state of psoralene is shown in Fig. 3a. The energies of the lowest singlet and triplet states and the k_{IC} and k_{ISC} rate constants are shown in Fig. 3b. The excitation energies listed in Table 2 agree well with the experimental values. The dominating deactivated channel of the S₁ state is *via* the k_{ISC1} channel, because of the strong spin–orbit coupling interaction between S₁ and T₁. See Table S1 in the ESI.† The calculated and experimental quantum yields of 0.08 are in perfect agreement.³⁵ The calculated excitation energies were found to agree very well with the experimental ones, even though the solvent effect can be as large as 1% for psoralene.³⁵ The calculated y_j and ω_j values for psoralene are given in Table 3, where one sees that many vibrational modes with energies larger than 1000 cm^{−1} have large y_j values leading to a high density of FC factors and fast nonradiative transitions. The calculated rate constants explain the low value and the high triplet quantum yield of psoralene.

4.3. [8]circulenes 4B, AOC and 1B3N

The optimized molecular structures of the S₁ state of tetraoxa[8]circulene (4B) and its NH substituted and benzoannulated derivatives (AOC) and (1B3N) are shown in Fig. 3a, c, and e. The energy levels of their lowest singlet and triplet states and the k_{IC} and k_{ISC} rate constants are shown in Fig. 3b, d and f, respectively. The lowest excitation energies are given in Table 2. The intensity for the radiative S₀–S₁ transition for tetraoxa[8]circulene (4B) vanishes in the FC approximation. The transition becomes allowed in the Herzberg–Teller approximation.⁶⁵ An oscillator strength for 4B of 0.03 is obtained from the experimental extinction coefficient $f = 4.32 \times 10^{-9} \int \epsilon(\nu) d\nu$.⁶⁶ The spin–orbit

Table 3 Calculated wavenumbers ω_j (in cm^{-1}) for a few relevant vibrational modes. The largest Huang–Rhys factors (y_j) for the $S_1 \rightarrow S_0$ and $S_1 \rightarrow T_j$ nonradiative transitions are given in parenthesis

Compound	ω_j (y_j)
PM567	210 (0.05); 571 (0.12); 1255 (0.1)
Psoralene	234 (0.29); 396 (0.65); 742 (0.42); 1103 (0.15); 1164 (0.25); 1190 (0.54); 1615 (0.14); 1689 (0.24); 1877 (0.08)
4B	662 (0.17); 1051 (0.07); 1276 (0.35); 1453 (0.19); 1536 (0.16); 1703 (0.84)
AOC	1308 (0.05); 1473 (0.14); 1675 (0.15); 1678 (0.05)
1B3N	232 (0.05); 1474 (0.15); 1518 (0.05); 1687 (0.05)
H ₂ P	157 (0.05); 310 (0.14); 1393 (0.03)
Alq ₃	141 (0.36); 151 (0.25); 164 (0.08); 185 (0.08); 213 (0.06); 357 (0.54); 422 (0.09); 458 (0.10); 506 (0.12); 554 (0.34); 585 (0.11); 587 (0.13); 661 (0.33); 670 (0.21); 1434 (0.1); 1634 (0.07); 1637 (0.29); 1659 (0.07)
Ir(ppy) ₃	121 (0.28); 146 (0.46); 187 (0.08); 258 (0.31); 269 (0.06); 1040 (0.01); 1512 (0.14); 1615 (0.11)

Fig. 3 (a) The optimized molecular structure of psoralene. (b) The energy level diagram for psoralene including the computed values for the radiative and nonradiative rate constants.

coupling matrix elements between S_1 and T_j vanish due to symmetry reasons since the molecule belongs to the D_{4h} point group. Thus, IC is the main deactivation channel of the S_1 state. The calculated value for ϕ_{fl} is 0.13, which agrees well with the experimental value of 0.09.³⁶ AOC has the largest quantum yield (ϕ_{fl}) of about 1.0, because the rate constant k_{ISC} is close to zero and k_{IC} is significantly smaller than k_r . The experimental ϕ_{fl} value for AOC is 0.91.²⁹ 1B3N has a smaller calculated ϕ_{fl} of 0.56 which is in reasonable agreement with the experimental value of 0.36.²⁹ The reason for the smaller ϕ_{fl} value is the presence of several low-lying triplet states. The main deactivation channel of the S_1 state is then the ISC process. The present calculations explain why the studied [8]circulenes have different quantum yields. The largest y_j values and the corresponding vibrational energies (ω_j) are listed in Table 3. The main vibrational mode for the nonradiative transition is at about 1400 cm^{-1} for AOC and 1B3N. We have previously calculated k_{IC} and k_{ISC} at the INDO level of theory using one vibrational mode with an energy of 1400 cm^{-1} .²⁹ The obtained results were in good agreement with the present ones except for k_{IC} of tetraoxa[8]circulenes (4B), because the NACMEs calculated at the INDO level are inaccurate. The reason for the deviation can be traced back to the large y_j factor for the vibrational mode at 1703 cm^{-1} , which consists of vibrational motion inside the macrocycle.⁶⁵ For the other [8]circulenes (AOC and 1B3N), this mode has a smaller y_j value. The present calculations show that the INDO approach does not yield accurate nonradiative rate constants for tetraoxa[8]circulene (4B) (Fig. 4).

4.4. Free-base porphyrin

Calculation of the nonradiative rate constants k_{IC} and k_{ISC} for H₂P is a challenge.¹ Several previous works have shown that the FC approximation is not enough to obtain accurate rate constants.^{1,15} The intensity of the Q band in the electronic absorption spectrum for H₂P can be accurately simulated only when considering vibrational effects at the Herzberg–Teller approximation.⁶⁷ In this work, we adopted the experimental value 0.03 for the oscillator strength (f) in the calculation of k_r using eqn (17). The molecular structure of free-base porphyrin is shown in Fig. 5a and the calculated energy levels and rate constants are presented in Fig. 5b. The calculated rate constants for the nonradiative transitions k_{IC} and k_{ISC} are underestimated, because the present calculations yield a quantum yield of 0.96, which is an order of magnitude larger than the experimental value of 0.08.⁴⁰ A previously calculated value for $k_{\text{ISC}1}$ is $\sim 10^7 \text{ s}^{-1}$.¹⁵ The largest Huang–Rhys factors (y_j) and the corresponding vibrational frequencies are listed in Table 3. The calculated y_j values are very small leading to an underestimation of the rate constants of the nonradiative transitions. The vibrational modes with energies in the range $1000 \text{ cm}^{-1} < \omega_j < 3000 \text{ cm}^{-1}$ contribute significantly to the FC factor. The y_j values of the vibrational modes in this energy range should be about 0.1–0.4. However, the largest y_j value is 0.03 for the vibrational mode at 1393 cm^{-1} , which is about one order of magnitude too small. In our previous INDO study considering one vibrational mode at 1400 cm^{-1} , an empirical y_j value of 0.3 was used leading to the rather accurate values for k_{IC} and k_{ISC} .³³ Thus, one has to go beyond the FC

Fig. 4 The optimized molecular structures of (a) 4B, (c) AOC and (e) 1B3N. The energy levels and rate constants are given for the same molecules in (b), (d), and (f), respectively.

approximation in order to obtain accurate values for the non-radiative rate constants of free-base porphyrin.

4.5. Alq₃ and Ir(ppy)₃

The optimized molecular structures of the S₁ state of *fac*-tris(8-hydroxyquinolinato)aluminium (*fac*-Alq₃) and *fac*-tris(2-phenylpyridine)iridium (*fac*-Ir(ppy)₃) are shown in Fig. 6a and c. The energy levels of the lowest singlet and triplet states and the k_{IC} and k_{ISC} rate constants of the transitions are shown in Fig. 6b and d. The calculated excitation energies of the S₁ and

T₁ states are compared with the experimental data in Table 2. The calculated excitation energies agree well with the experimental data. Only the lowest triplet state lies below the S₁ state. For Alq₃, the radiative and the two nonradiative deactivation channels of the S₁ state have almost the same rate constants. The calculated quantum yield (ϕ_f) of 0.25 agrees with the experimental values of 0.04–0.3 that strongly depend on environmental effects.³⁸ For Ir(ppy)₃, the ISC process dominates the deactivation of the S₁ state due to the strong spin-orbit coupling effects. See Table S1 in the ESI.† The rate constant

Fig. 5 (a) The optimized molecular structure of free-base porphyrin (H₂P). (b) The energy level diagram for H₂P including the computed values for the radiative and nonradiative rate constants.

Fig. 6 (a) The optimized molecular structure of fac-Alq₃. (b) The energy-level diagram for fac-Alq₃ including the computed values for the radiative and nonradiative rate constants. (c) The optimized molecular structure of fac-Ir(ppy)₃. (d) The energy-level diagram for fac-Ir(ppy)₃ including the computed values for the radiative and nonradiative rate constants.

Fig. 7 The calculated energy levels for (a) naphthalene, (b) anthracene, (c) tetracene, (d) pentacene, (e) hexacene and the computed values of the radiative and nonradiative rate constants.

k_{ISC1} is much larger than k_r leading to a very small quantum yield, which agrees with the previously calculated value of about 10^{12} s^{-1} for k_{ISC1} and the experimental results.⁶⁸ The largest y_j values and the corresponding vibrational energies (ω_j) are reported in Table 3. Alq_3 has many more vibrational modes with large y_j values than Ir(ppy)_3 , which explains why Alq_3 has a larger k_{IC} rate constant than Ir(ppy)_3 .

4.6. Polyacenes

The energy levels of the lowest singlet and triplet states and the k_{IC} and k_{ISC} rate constants of the transitions of the polyacenes are shown in Fig. 7. The calculated excitation energies of the S_1 and T_1 states are compared with the experimental data in Table 4.

Table 4 The calculated excitation energies (in eV) of the polyacenes are compared with the experimental data

Compound	State	XMC-QDPT2	Exp. ^a
Naphthalene	S_1	3.66(0.003)	3.86
	T_1	2.67	2.63
Anthracene	S_1	2.97(0.2)	3.3
	T_1	1.57	1.85
Tetracene	S_1	2.7(0.1)	2.6
	T_1	1.16	1.26
Pentacene	S_1	1.9(0.1)	2.1
	T_1	0.7	0.95
Hexacene	S_1	1.6(0.1)	1.8
	T_1	0.5	0.81

^a The experimental data are taken from ref. 37.

Table 5 Calculated wavenumbers (ω_j in cm^{-1}) of the significant vibrational modes for the nonradiative transitions and the corresponding Huang–Rhys factors (y_j) for the S_1 to S_0 nonradiative transition of the polyacenes

Compound	ω_j (y_j)
Naphthalene	519 (0.06); 775 (0.23); 1055 (0.1); 1413 (0.36)
Anthracene	398 (0.37); 640 (0.02); 765 (0.02); 1039 (0.01); 1194 (0.08); 1301 (0.16); 1443 (0.44); 1606 (0.40)
Tetracene	318 (0.26); 633 (0.03); 765 (0.04); 1032 (0.01); 1190 (0.04); 1243 (0.17); 1425 (0.15); 1441 (0.19); 1573 (0.02); 1589 (0.25)
Pentacene	263 (0.18); 615 (0.02); 764 (0.05); 1190 (0.03); 1228 (0.17); 1426 (0.24); 1449 (0.08); 1570 (0.15)
Hexacene	225 (0.15); 579 (0.01); 765 (0.1); 1030 (0.01); 1183 (0.05); 1212 (0.11); 1216 (0.01); 1217 (0.06); 1418 (0.25); 1560 (0.06)

The calculated quantum yields (ϕ_{fl}) for naphthalene, anthracene, tetracene, pentacene, hexacene, and heptacene are 0.94, 0.99, 0.99, 0.03, and 0.001 respectively, which can be compared with the experimental values of 0.23, 0.24, 0.21, 0.08, and 0.01.⁴¹ The calculated quantum yields differ from the experimental ones, whereas a similar trend is obtained for the polyacenes. The calculated ϕ_{fl} values are not very accurate, because the S_1 state is not a pure adiabatic state but consists of a mixture of higher energy states.⁵⁰ The estimated quantum yields (ϕ_{fl}) agree qualitatively with the experimental ones only when k_{IC} is larger than k_{ISC} . For the polyacenes, the calculated k_{ISC} contribution to the nonradiative rate constant k_{nr} is underestimated. The calculated k_{IC} and k_{ISC} rate constants are expected to be rather accurate, whereas they cannot be used for estimating the quantum yield when $k_{\text{IC}} < k_{\text{ISC}}$. The values of y_j and ω_j are of the vibrational modes that are most important for the nonradiative transitions are listed in Table 5. The vibrational mode at about 1400 cm^{-1} has a y value of about 0.3 for all the polyacenes except for tetracene. This mode yields the main contribution to the k_{ISC} rate constant. In the calculation of k_{ISC} for the polyacenes, it is necessary to consider only this mode, as done by Maier and Artyukhov.^{25–28}

4.7. The analysis of nonadiabatic integrals

Calculations of the nonadiabatic integrals (8) show that the largest integral value of 0.007 a.u. is obtained for the vibrational modes with energies of about 3000 cm^{-1} , because the y value is very small for them. For the other vibrational modes, the integrals (10) are a factor of 2–22 times smaller. The high-frequency modes with $\sim 3000 \text{ cm}^{-1}$ usually correspond to X–H stretching vibrations, where X = C, N, O or another light atom. The present study shows that in the IC channel, the excitation energy of the S_1 state transforms into stretching vibrations of X–H modes, which supports the theory by Plotnikov, Maier and Artyukhov.^{24–28}

5. Summary and conclusions

The proposed computational approach has been used for calculating the rate constants for internal conversion (k_{IC}) and inter-system crossing (k_{ISC}) of a number of organic and organometallic compounds. The calculations show that the radiative process dominates for PM567 and AOC. The non-radiative ISC process dominates for psoralene and $\text{Ir}(\text{ppy})_3$, whereas the non-radiative IC process dominates for tetraoxa[8]circulene. For Alq_3 , the rate constants of the radiative and the non-radiative (IC and ISC) processes are of the same size. When the Franck–Condon (FC) and adiabatic approximations are valid, the proposed approach can be used for estimating the fluorescence quantum yield (ϕ_{fl}).

For polyacenes and H_2P , it is necessary to go beyond the FC and adiabatic approximations. The FC approximation breaks down, when the Huang–Rhys factor (y) is about 0.01–0.04 for modes with energies of about $1000\text{--}1800 \text{ cm}^{-1}$ leading to strongly underestimated FC factors. Small values for the FC factor lead to too small calculated values for k_{IC} and k_{ISC} . The value of y can be used as a criterion for the applicability of our approach. For H_2P , the y value of the vibrational mode at 1393 cm^{-1} has a small Huang–Rhys factor suggesting that the present approach cannot be applied to free-base porphyrin.

The computations show that in the IC process the excitation energy transfers into the vibrations of the X–H (X = C, N and O) bonds supporting the theory by Plotnikov, Maier and Artyukhov.^{24–28} However, when estimating the FC factors of the ISC process, all the vibrational modes have to be taken into account, because many vibrational modes with energies in the range of $1000\text{--}1800 \text{ cm}^{-1}$ contribute significantly to the FC factor.

The accuracy of the calculated k_{IC} and k_{ISC} rate constants depends strongly on the accuracy of the calculated excitation energies of the excited singlet and triplet states. Since the obtained k_{IC} and k_{ISC} rate constants depend strongly on the accuracy of the calculated values for the singlet and triplet excitation energies, we calculated the excitation energies at the XMC-QDPT2 level of theory, which is computationally expensive but a feasible level for molecules of this size.^{69,70}

The present approach makes it possible to estimate rate constants for nonradiative transitions (k_{IC} and k_{ISC}) for organic and organometallic compounds within the FC and adiabatic approximation by using calculated values for the matrix elements of the spin–orbit coupling interaction and nonadiabatic coupling interaction.

Conflicts of interest

There are no conflicts to declare.

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