Bulk and surface properties of metal carbides: implications for catalysis†

Matthew G. Quesne, † Alberto Roldan, † Nora H. de Leeuw † and C. Richard A. Catlow

We present a comprehensive study of the bulk and surface properties of transition metal carbides with rock salt structures and discuss their formation energies and electronic structures. The bonding character of the materials is shown to be dependent on the periodic position of the transition metal as well as the surface termination, which in turn tunes the densities of states and electronic surface properties. Specific focus is given to the possible catalytic implications of the surface properties on CO₂ hydrogenation.

The physical properties of TMCs also depend on the surface; for instance, the electronic structure of TiC displays more covalent character in the {001} direction and more electron localization (ionic character) in the {111} faces. Finally, the position of the TM along the series is also important, with ZrC a considerably more ionic transition metal carbide than δ-MoC. Nevertheless, no systematic studies have been reported into the structure and electronic properties of all three low-index surfaces for all available monocarbides. In 2004, Hugosson et al. published a theoretical study into the unrelaxed {001} surface of a range of TMCs; this work was then followed by a less extensive study into the properties of the relaxed {001} surfaces of various TMCs. However, whilst it is true that studies have pointed to the {001} surface as being the most stable in, for example, TiC it is also true that the {111} surfaces of TMCs are generally more active than the corresponding {001} surfaces. For a good overview of the current literature see ref. 25.

In view of the growing importance of TMC materials, we have undertaken a comprehensive theoretical study into the properties of the bulk and three low-index surfaces, i.e. {001} {011} {111}, of all reported TMCs with 1:1 stoichiometry: ScC, TiC, Vc, CrC, CoC, NiC, YC, ZrC, NbC, δ-MoC, HfC, TaC and WC. Those carbides with groups 3–5 metals form stable bulk crystals, whereas carbides with 1:1 stoichiometry and post group 5 metals are usually formed from either modifying the surfaces of bulk TMs as thin films or even 2D materials. Therefore, the future of carbide chemistry will not be limited to those materials that readily anneal into homogeneous bulk crystals and the study of monocarbides with post group five transition metals will also be considered here. Our work employs calculations based on the density functional theory (DFT) with a careful evaluation of three different functionals.

Introduction

It has been known since the seminal work of Levy and Boudart in 1973 that the addition of carbon to elemental transition metals can bestow the resulting materials with the properties of precious metals. Subsequent generations of transition metal carbides (TMCs) have demonstrated the ability to catalyse hydrogenation, water-gas shift and CO oxidation reactions. The focus of this study will be a detailed investigation of the bulk and surface properties of all known transition metal monocarbides. However, we also intend to highlight aspects of these materials that relate to their potential future utilization as catalysts in the reduction of carbon dioxide (CO₂). We have chosen this process as an example of a major aim of contemporary chemical science and because many of the materials that have been used to catalyse such reactions, using CO₂ as a feedstock on pathways to fuels and chemicals, are made from expensive precious metals, or have low catalytic activity. Excitingly, some TMCs have been shown to hydrogenate CO₂ and such activity hints at the prospect of a possible integrated industrial approach for H₂ generation and CO₂ conversion.

TMCs combine the physical properties of transition metals, ionic solids and covalent solids. They have the conductivity of TMs, the structural coordination and high melting point of ionic solids and the hardness of covalent solids. The band structures and therefore electronic properties of each TMC are, to a large degree, driven by the extent of metallic, covalent and ionic bonding character of the metal-metal and metal-carbon bonds. The physical properties of TMCs also depend on the surface; for instance, the electronic structure of TiC displays more covalent character in the {001} direction and more electron localization (ionic character) in the {111} faces. Finally, the position of the TM along the series is also important, with ZrC a considerably more ionic transition metal carbide than δ-MoC. Nevertheless, no systematic studies have been reported into the structure and electronic properties of all three low-index surfaces for all available monocarbides. In 2004, Hugosson et al. published a theoretical study into the unrelaxed {001} surface of a range of TMCs; this work was then followed by a less extensive study into the properties of the relaxed {001} surfaces of various TMCs. However, whilst it is true that studies have pointed to the {001} surface as being the most stable in, for example, TiC it is also true that the {111} surfaces of TMCs are generally more active than the corresponding {001} surfaces. For a good overview of the current literature see ref. 25.

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† Electronic supplementary information (ESI) available: Tables showing the benchmarking of k-points and cut-offs as well as the relaxation energies of each layer for all surfaces are shown here. Also included are charts and tables for the raw bulk data for each TMC. See DOI: 10.1039/c7cp06336a
Methodology

All calculations were performed with the Vienna Ab initio Simulation (VASP) package, which was used to test several types of generalized gradient approximation (GGA) functionals within the framework of periodic density functional theory. Results obtained using the standard version of the Perdew–Burke–Ernzerhof exchange functional (PBE) were supplemented first by a version that was developed specifically for solids (PBEsol) and finally by a revised version (RPBE). We have not considered the computationally much more costly Meta GGA or hybrid functionals, since such methods are most valuable in determining band gaps in semiconducting and insulating materials. Plane-wave basis sets were applied to the valence electrons, whereas the core electrons were described by the projected augmented wave method (PAW) developed by Blöchl. Additionally, long range interactions were modelled using the Grimme dispersion D3 method. Bulk metal carbides were modelled using the Grimme dispersion D3 method. Calculations of solids (PBEsol) and finally by a revised version (RPBE). We have not considered the computationally much more costly Meta GGA or hybrid functionals, since such methods are most valuable in determining band gaps in semiconducting and insulating materials. Plane-wave basis sets were applied to the valence electrons, whereas the core electrons were described by the projected augmented wave method (PAW) developed by Blöchl. Additionally, long range interactions were modelled using the Grimme dispersion D3 method. Bulk metal carbides were modelled using the Grimme dispersion D3 method. Calculations of solids (PBEsol) and finally by a revised version (RPBE).

Results

Bulk metal carbides

The carbide crystal structures for ScC, TiC, VC, CrC, CoC, NiC, NbC, MoC, HfC, TaC and WC were taken from the Inorganic Structure Database (ICSD). These comprise all the published monocarbide materials with the rock salt structure. For every TMC, geometry optimizations were then carried out to relax the atomic coordinates in each unit cell, using all three functionals. This procedure was repeated for a series of different unit cell parameters to produce potential energy curves for each material (see ESI†). From these data sets, lattice constants (a0), unit cell volumes (a0^3) and bulk moduli (B0) were assigned. Alongside these values, the shortest atomic distances inside each unit cell were calculated and compared to experiment, using a previously described protocol (see Table S14, ESI†). The lattice parameters are reported in Table 1 and compared to the experimental data. The theoretical results across all functionals are generally in reasonable agreement with experiment and no obvious systematic errors were observed; the exception to this agreement is found for CoC, where a somewhat larger deviation from experiment is observed with all three functionals. The crystal structure for cobalt-carbide was published by Caderville and Lapierre in 1972 using X-ray crystallographic techniques, while the other carbide structures were mostly determined by neutron scattering techniques. As noted above, TMCs with post-5th transition metals such as cobalt do not readily anneal into single crystals with 1:1 stoichiometry. Caderville and Lapierre were able to show that the addition of carbon was able to stabilize the face-centered cubic phase of cobalt-carbide. However, the structure they provide is the only such rock salt crystal phase of cobalt-carbide and the presence of low carbon occupancies throughout the crystal probably explains the discrepancy between experiment and theory. Therefore, it is possible to argue that this crystal structure is more accurately described as cobalt metal stabilized by variable amounts of interstitial carbons, whereas the theoretical models more accurately represent CoC, with a stoichiometry of 1:1.

By utilizing eqn (1), it was subsequently possible to use the previous geometric calculations to compute bulk moduli:

\[ B_0 = -V_0 \frac{\partial P}{\partial V} \]  

The bulk moduli (B0), calculated for each functional, are given in Table 2 alongside a range of experimentally determined values for some of the TMCs. It should be noted that there is a lack of experimental data on the B0 of 3d carbides beyond group 5 (CrC-NiC), since, as mentioned earlier, only monocarbides with groups 3–5 metals form stable bulk carbides, with

<table>
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<tr>
<th>Carbid</th>
<th>a0^3</th>
<th>a0</th>
<th>b0</th>
<th>B0</th>
<th>B0©</th>
<th>B0©</th>
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<td>TiC</td>
<td>4.328</td>
<td>4.308</td>
<td>4.276</td>
<td>4.319</td>
<td>0.46</td>
<td>1.20</td>
<td>0.21</td>
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<td>4.165</td>
<td>4.132</td>
<td>4.098</td>
<td>4.138</td>
<td>0.80</td>
<td>1.61</td>
<td>0.66</td>
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<td>CrC</td>
<td>4.030</td>
<td>4.043</td>
<td>4.010</td>
<td>4.057</td>
<td>-0.33</td>
<td>0.49</td>
<td>-0.68</td>
</tr>
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<td>CoC</td>
<td>3.551</td>
<td>3.977</td>
<td>3.932</td>
<td>3.982</td>
<td>0.04</td>
<td>1.01</td>
<td>0.09</td>
</tr>
<tr>
<td>NiC</td>
<td>4.077</td>
<td>4.047</td>
<td>4.009</td>
<td>4.070</td>
<td>0.73</td>
<td>1.66</td>
<td>0.18</td>
</tr>
<tr>
<td>YC</td>
<td>5.080</td>
<td>5.060</td>
<td>5.017</td>
<td>5.090</td>
<td>0.51</td>
<td>1.35</td>
<td>-0.08</td>
</tr>
<tr>
<td>ZrC</td>
<td>4.698</td>
<td>4.682</td>
<td>4.650</td>
<td>4.694</td>
<td>0.34</td>
<td>1.20</td>
<td>0.21</td>
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<td>4.969</td>
<td>4.458</td>
<td>4.430</td>
<td>4.458</td>
<td>0.25</td>
<td>0.87</td>
<td>0.25</td>
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<tr>
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<td>4.351</td>
<td>4.317</td>
<td>4.353</td>
<td>-1.82</td>
<td>-1.04</td>
<td>-1.87</td>
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<tr>
<td>HfC</td>
<td>4.631</td>
<td>4.662</td>
<td>4.588</td>
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<td>-0.66</td>
<td>0.93</td>
<td>-0.05</td>
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<td>TaC</td>
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<td>4.456</td>
<td>4.276</td>
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<td>-0.14</td>
</tr>
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<td>4.328</td>
<td>4.360</td>
<td>0.28</td>
<td>1.04</td>
<td>0.31</td>
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</tbody>
</table>

- PBE values
- PBEsol values
- RPBE values
rock salt structures. It is also important to keep in mind that variations in the numbers of vacancies as well as the precise physical conditions of the materials can lead to a broad range of experimental values. Therefore, it can be problematic to make direct comparisons between calculated and experimental bulk moduli. However, in many cases our computed values are reasonably close to the experimentally determined ones.

Heats of formation

Heats of formation were calculated by subtracting the sum (per atom values) of bulk metal and graphite from the energy (per atom) of the bulk carbide. The heats of formation (ΔE) were found to show a clear trend across each series, with an early minimum in ΔE around group 4d (see Fig. 2). As previously noted, carbides that contain TMs early in the periodic series readily anneal into monocarbides, whilst metals with increasingly filled d-bands form more TM-rich carbides. Inserting interstitial carbons into a transition metal lattice causes the weakening of TM–TM bonds and replaces them with TM–C bonds. Therefore, a carbide’s heat of formation reflects the competition between these two effects. The nobleness of the parent metal increases from left to right (along each period) causing a weakening in the TM–C bonds. Our data are in excellent agreement with the available experimental values: TiC, VC, ZrC, NbC, δ-MoC, HfC, TaC & WC. No experimental data are available for the monocarbides, containing 3d transition metals past group five. However, formation enthalpies (per atom) are available for some of the more transition metal-rich stoichiometries: (Cr2C) −0.21 eV, (Co2C) 0.06 eV and (Ni3C) 0.09 eV.

These energies also support our theoretical findings, since even the more transition metal-rich carbides (containing post group six TMs) show endothermic formation energies. Therefore, the insertion of even relatively low amounts of interstitial carbon into the transition metal lattices of post group six metals is not thermodynamically favoured. The trends reported here are also consistent with a previous study into the relative formation energies of groups IV to VIII transition metal carbides, published in 2016 by Wang et al. The authors reported highly exothermic formation energies per atom, of −0.81 eV (TiC), −0.82 eV (ZrC) and −0.94 eV (HfC) for group four carbides, followed by less exothermic ΔE for group five monocarbides: −0.42 eV (VC), −0.53 eV (NbC) and −0.59 eV (TaC). Apart from δ-MoC (−0.09 eV) and WC (−0.13), all other TMCs analysed had positive ΔE, which the authors suggest as an explanation for the lack of stable group seven and eight monocarbides with 1:1 stoichiometry.

Evaluation of the different functionals

In order to better describe the performance of each functional, we have performed a statistical analysis of their performance versus the experimentally determined values, by summarizing the mean absolute errors of the a₀ and B₀, as previously described, presenting our findings in Chart 1. Here we see, that although some functionals do perform better in certain types of analysis, no one functional can be said to clearly outperform the others and all functionals show reasonable overall performance.

Low-index surfaces of metal carbides

The slab models for all three low-index surfaces were prepared with the aid of the METADISE code. Since calculations with all three functionals showed very similar bulk trends, and no obvious systematic errors could be assigned to any functional, it was decided to perform the surface calculation using the PBE functional only. The {001} and {011} faces for each TMC contained six atomic layers terminated by a mixed carbon-metal surfaces. The {111} surfaces of each TMC contain alternating layers of metal and carbon atoms and thus they can either be terminated by carbon or by the metal. Each unit cell was multiplied 2 × 2 × 3 to give a total of 96 atoms (with three times the original number of atomic layers in the Z-direction). Subsequently, a vacuum region of 10 Å was added above each surface termination. As an example, the different surfaces of ScC are illustrated in Fig. 2, whilst the energy differences resulting from the relaxation of the layers are included in the ESL.†

After sequentially relaxing each layer, the resulting energies were plotted as a function of the number of relaxed atomic layers which indicated that in all cases a stable plateau was reached between layers three and four. Therefore, it was decided that relaxing just half the slab on each surface would be sufficient to obtain accurate surface properties. A similar protocol has previously been reported by Santos-Carballal et al. and it was followed here, because relaxing the whole slab would relax both the carbon- and metal-terminated layers. Thus, any values obtained would represent an average of the two faces. Since it has previously been reported that surface properties may be affected by slab thickness, we created alternative 2 × 2 × 2 supercells of all {111} surfaces, giving a total of 64 atoms per model. Previous work on TMCs has shown that 4-layer surfaces lead to a sufficiently thick slab for the accurate modelling of surface properties. However, the results obtained using these structures did not correlate very well to those previously determined using 6-layer models; with discrepancies in the values of several work functions of greater than 0.5 eV (see Table S37, ESI†). However, additional test calculation using 8-layer slabs showed excellent correlation.
with the 6-layer slab models (see Table S39, ESI†). These observations correlate well with previous work by Viñes et al. that also showed a variation in the relaxation of {001} carbide surfaces between their 4- and 8-layer slabs.18 Finally, we decided to benchmark the pristine {111} faces with reconstructed surfaces, whereby migration of surface atoms cancels the perpendicular dipole. Our results are shown in Table S39 (see ESI†). Although the energies of the resulting reconstructed surfaces are slightly lower (∼1 eV), the relative trends in relaxed surfaces energies remain constant, thereby confirming the validity of our unreconstructed models in this work. In light of the discrepancies between the 4- and 6-layer models only the data from the latter are shown here, with full data sets from the other systems being available in the ESI.†

Once all the different surfaces were fully relaxed, it was possible to assess surface energies (σ), work functions (ϕ) and rumpling caused by the uneven displacement of metal and carbon atoms at the surface (r). The surface energy and work function are perhaps the most fundamental characteristics of any material that help to determine the trends in growth rate, surface segregation and catalytic activity.22 However, despite its predictive importance, an experimental determination of the surface energies of various TMCs has proven very difficult due to the very high melting points of this class of materials.22

We therefore begin our analysis of the properties of various surface terminations by relaxing each layer of the surface models sequentially (see ESI†). Surface energies (σ) for the unrelaxed surfaces were calculated using eqn (2). A denotes the area of each surface with Eslab signifying the total energy of the unrelaxed slab and n standing for the number of bulk unit cells used to form the slab volume. The factor of 2 in the denominators is necessary as two surfaces are formed for each system. It is important to note that, in the case of the {111} surfaces, two different surface terminations are considered. Therefore, the energy values are better described as cleavage values ([{111avg}) that represent an average between the σ of the carbon- and metal-terminated surfaces. These values are calculated in the same way as for σu (see eqn (2)).

$$\sigma_u = \frac{E_{\text{slab}} - nE_{\text{bulk}}}{2A}$$  \hspace{1cm} (2)

When only half the slab is relaxed, the relaxed surface energy (σ’) must be determined as shown in eqn (3); here the area of only one surface is included in the denominator and this energy is subtracted from that of the unrelaxed surfaces. The computed σ’ for each surface are reported in Table 3. In the case of the {111} surfaces, the difference in energy between the average cleavage value and the relaxed surface value gives the energy of the purely carbon- or metal-terminated surface relaxation (∆σ). The unrelaxed value for the surface energy of a material is roughly equal to half of its cohesive energy (Ecoh),75 although, because of variations in dangling bonds, protocols such as the bond-cutting theory22,76,77 have been used to accurately correlate these two energies. All values are positive since a negative surface energy would imply a negative cohesive energy and any resulting terminations would be unstable and liable to cause the material to disintegrate.78 Consistent with previous studies,23 our calculated surface energies confirm the {001} surfaces to be the most stable for all the systems investigated.

Fig. 3 illustrates the change in preference for the metal-over carbon-terminated {111} surface, across the TMC series. The values were obtained by subtracting the energies of the carbon-terminated surfaces from those of the corresponding metal-terminated surfaces. The results show that the level of preference for a metal-terminated {111} surface decreases across the groups and down the periods. These observations indicate a decreased dominance of the metal-terminated {111} surfaces as the nobleness of the carbide’s parent metal increases, to the point where NbC, δ-MoC, TaC and WC demonstrate a preference for carbon-terminated {111} faces. These results help to explain the observation that TiC appears to be exclusively terminated by titanium, when the {111} surface is characterized experimentally.17,79 Also, it has been suggested that, at high temperatures, the preference for termination by the TM could increase due to the higher evaporation rate of the carbon.79 In general, the surface energies are highest for the group 4d carbides, which trend was also reported in

<table>
<thead>
<tr>
<th>Carbide</th>
<th>{001}</th>
<th>{111}</th>
<th>{111}avg</th>
<th>{111}cation</th>
<th>{111}metal</th>
<th>Δσ</th>
<th>Δσ</th>
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<tbody>
<tr>
<td>ScC</td>
<td>1.32</td>
<td>1.31</td>
<td>2.86</td>
<td>2.72</td>
<td>5.41</td>
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<tr>
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<td>4.27</td>
<td>7.94</td>
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<tr>
<td>CrC</td>
<td>1.64</td>
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<td>6.50</td>
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<tr>
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<td>1.09</td>
<td>0.57</td>
<td>2.79</td>
<td>1.73</td>
<td>4.82</td>
<td>2.56</td>
<td>1.99</td>
</tr>
<tr>
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<td>3.44</td>
<td>1.46</td>
<td>1.49</td>
</tr>
<tr>
<td>YC</td>
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<td>1.07</td>
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<td>2.12</td>
<td>4.48</td>
<td>0.70</td>
<td>1.08</td>
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<td>4.27</td>
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<td>0.52</td>
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<tr>
<td>NbC</td>
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<td>4.09</td>
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<tr>
<td>δ-MoC</td>
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<td>5.79</td>
<td>1.63</td>
<td>0.69</td>
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</table>

σ, unrelaxed surface energy; σ’, relaxed surface energy; Coad, average cleavage energy; ∆σ, relaxation surface energy.
They found that one pattern common to all three periodic series was an early maximum for group four TMCs, that may be due to their fully occupied lowest energy d-orbital, which in turn helps to increase the ionic nature of the materials.interestingly, the heats of formation ($\Delta E$) were found to show a similar (if opposite) trend with an early minimum in $\Delta E$ around group 4d (see Fig. 1).

### Surface rumpling

As a result of the under-coordination of the surface atoms upon the creation of the surface, a general trend across almost every carbide termination is that atoms making up the surface layer relax into the bulk (see Table 4). Most studies appear to show that often such contraction results in rumpling because of a higher level of inward relaxation of the metal atoms, which leads to a relative displacement of the carbons outwards into the vacuum. These observations are consistent with our calculations, with the two surface terminations that preserve the stoichiometry of the bulk, {001} and {011}, showing a strong tendency for rumpling in a manner that exposes more of the carbons to the vacuum.

Across all TMCs there is consistently a larger contraction of the {011} and metal/carbon-terminated {111} surfaces away from the vacuum, which is to be expected due to the lower coordination of the surface ions – 4 and 3 for the {011} and {111} facets, respectively, compared to 5 for the surface atoms in the {001} surface. The consequence of this effect is that the relative positions of the metals at the TMC {011} faces move further into the bulk than those found on the corresponding {001} surfaces. However, since the carbon atoms also migrate into the bulk, the actual rumpling is similar between the {001} and {011} surfaces (Fig. 2 and 3).
interaction between the endothermic process associated with removing an electron from the bulk carbide and the energy gained in terms of the electron affinity of $\text{CO}_2$ and the new bond formed between $\text{CO}_2$ and the surface. Since the electron affinity of $\text{CO}_2$ is the same for each system and the bond formation energy can only be obtained by a comprehensive study into possible adsorption state, which are not considered here, we will focus on the left-hand side of eqn (3).

$$\Delta G_{\text{bond}} = G_{\text{TMC(CO}_2)} - G_{\text{TMC}} - G_{\text{CO}_2} \tag{4}$$

$$\text{BDE}_{\text{CO}_2} = \text{IP}_{\text{TMC}} - \text{EA}_{\text{CO}_2} - \Delta G_{\text{bond}} \tag{5}$$

$$\phi = V_{\text{C}} - E_{\text{F}} \tag{6}$$

$$\text{BDE}_{\text{CO}_2} = \phi_{\text{TMC}} - \text{EA}_{\text{CO}_2} - \Delta G_{\text{bond}} \tag{7}$$

When calculating the ionization energies of a solid-state system ($\text{IE} = \Delta E^0 - \Delta E^1 + e^-$), it is often useful to consider a system’s work function ($\phi$), which is calculated as shown in eqn (6). Here $V_{\text{C}}$ refers to the electrostatic potential inside the vacuum and $E_{\text{F}}$ is the aforementioned Fermi energy (i.e. the highest energy of electrons in a given bulk volume at zero degrees Kelvin).

In essence, this value relates to the minimum amount of energy (in this case in the form of an overpotential) required to excite one electron from the Fermi level out of the finite potential well, that is the carbide bulk, into the vacuum. In non-degenerate semiconductors, the Fermi level is found at least $3k_B T$ away from the edge of either the valence or conduction bands. However, in strongly metallic systems the electrons are degenerate and some density of states is invariably found at the Fermi level, meaning that the work function is in essence a measure of the vertical ionization potentials. Therefore, we can substitute work function for ionization potential in eqn (3), as is seen in eqn (5). The electron affinity (EA) of a material is defined as the energy between the $V_{\text{C}}$ and the conduction band. In the case of metallic systems, there is no gap between the conduction and valence bands; therefore, a higher work function would indicate a larger electron affinity.

In spite of the inconsistencies in experimentally determined work functions, reported values of 3.8/4.1 eV (TiC), 4.3 eV (VC), 3.5 eV (ZrC), 4.1 eV (NbC), 4.63 eV (HfC), and 4.38 eV (TaC) are generally very consistent with the calculated $\{001\}$ values (see Fig. 4). Experimental studies have determined that the work functions of the parent transition metal carbides steadily increase until a peak is reached towards the end of all three series. This trend is replicated reasonably well in the $\{001\}$ and $\{011\}$ surfaces of the TMCs. However, this trend is not seen so markedly in any of the $\{111\}$ terminations, as the work functions of $\{111\}$-terminated carbides appear to peak considerably earlier in the series, with maximum values found for VC, NbC and TaC. Since there have not been the same systematic studies into surface properties of the $\{111\}$ termination, these results may at first seem surprising. However, it is important to note that even the $\{001\}$ surfaces show markedly different trends from their parent elemental metals, a point highlighted by Hudosson et al. in 2004.

Generally, the lowest work functions are found on the $\{011\}$ terminations. The uniform nature of the unrelaxed $\{011\}$ faces leads to a uniformity in the extent of surface relaxation. However, there is somewhat greater diversity observed in the contraction of the metal and carbon surfaces, than that which is to be seen in the surface energies, due to the varying number of carbon vacancies at the surface. However, it is often a very susceptible to discrepancies due to variable numbers of d-orbitals and dangling bonds causing different surface valences at each termination.

### Work functions of metal carbides

We now consider the relative redox characteristics of each material. As with the previously discussed bulk moduli, experimental characterization of a TMC’s work functions ($\phi$) is also very susceptible to discrepancies due to variable numbers of carbon vacancies at the surface. However, it is often a very useful descriptor of the reactivity of a range of different materials. Redox processes are critical to many reaction mechanisms and therefore one may assume that the relative redox potentials of each material will have a strong influence on that material’s relative reactivity. To gain insight into the redox behavior of this series of materials we have calculated the work functions of each surface.

For the purposes of this discussion, we will focus on the initial reaction steps required for $\text{CO}_2$ reduction by molecular hydrogen. However, the same principles are relevant to many different redox-driven catalytic reactions. The same carbide surfaces are responsible for reducing electronegative substrates such as $\text{CO}_2$ as well as oxidizing electron-donating substrates like $\text{H}_2$. A breakdown of the thermochromical contributions to the carbon dioxide adsorption energy are given in eqn (3). Contributions from the ionization energy of the carbide ($\text{IP}_{\text{TMC}}$) are subtracted from the sum of the electron affinity of $\text{CO}_2$ and the energy associated with the new TMC($\text{CO}_2$) bond formation ($\Delta G_{\text{bond}}$). Studies have shown that it is possible to rationalize the respective heights of a very broad range of activation barriers in terms of a valence bond approach. In theory, the activation energy associated with $\text{CO}_2$ adsorption is indicative of an

<table>
<thead>
<tr>
<th>Material</th>
<th>${001}$</th>
<th>${011}$</th>
<th>${111}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$Z_{\text{C}}$</td>
<td>$Z_{\text{M}}$</td>
<td>$Z_{\text{C}}$</td>
<td>$Z_{\text{M}}$</td>
</tr>
<tr>
<td>ScC</td>
<td>-0.01</td>
<td>0.00</td>
<td>-0.22</td>
</tr>
<tr>
<td>TiC</td>
<td>-0.18</td>
<td>-0.30</td>
<td>-0.28</td>
</tr>
<tr>
<td>VC</td>
<td>-0.09</td>
<td>-0.27</td>
<td>-0.11</td>
</tr>
<tr>
<td>CrC</td>
<td>-0.05</td>
<td>-0.27</td>
<td>-0.08</td>
</tr>
<tr>
<td>CoC</td>
<td>0.11</td>
<td>-0.08</td>
<td>0.19</td>
</tr>
<tr>
<td>NiC</td>
<td>-0.16</td>
<td>0.09</td>
<td>0.47</td>
</tr>
<tr>
<td>YC</td>
<td>-0.19</td>
<td>-0.11</td>
<td>0.47</td>
</tr>
<tr>
<td>ZrC</td>
<td>-0.27</td>
<td>-0.35</td>
<td>-0.38</td>
</tr>
<tr>
<td>NbC</td>
<td>-0.05</td>
<td>-0.24</td>
<td>-0.11</td>
</tr>
<tr>
<td>$\delta$-MoC</td>
<td>0.09</td>
<td>-0.18</td>
<td>0.02</td>
</tr>
<tr>
<td>HfC</td>
<td>-0.05</td>
<td>-0.14</td>
<td>-0.18</td>
</tr>
<tr>
<td>TaC</td>
<td>-0.12</td>
<td>-0.32</td>
<td>-0.18</td>
</tr>
<tr>
<td>WC</td>
<td>-0.04</td>
<td>0.00</td>
<td>-0.03</td>
</tr>
</tbody>
</table>

$Z_{\text{C}}$, carbon displacement; $Z_{\text{M}}$, metal displacement.
terminations followed closely by the \{001\} surfaces. Importantly, it has been demonstrated that the more open faces such as those found in the \{111\} terminations are in several cases more reactive than the higher-coordinated ones (such as the \{001\} faces), regardless of work function.\(^{98,99}\) In terms of redox properties the carbides with the lowest work functions (such as NiC, ScC, YC & HfC) could be expected to be good electron donors. Therefore, these carbides could possibly be suitable reducing agents, for example in the activation of CO\(_2\).

Density of states

The high work functions seen in the \{111\} faces of almost all TMCs would be expected to lead to a higher ionization energy and therefore may indicate lower reduction rates of electronegative substrates, as in the case of CO\(_2\) redox activation. However, this has not been demonstrated in the experimental studies.\(^{17,24}\) It has been suggested that a reason for the observed increase in reactivity of the \{111\} surface over the \{001\} surface is due to the difference in surface states between the surfaces.\(^{24}\) Experimental evidence points to many more surface states close to the Fermi level of the \{111\} surfaces of a range of carbides.\(^{36}\) We therefore compare the density of states (DOS) of the different materials.

The increased number of surface states in the \{111\} terminations of the 5d transition metal carbides are illustrated in Fig. 5, where many peaks in the DOS are found at either side of the Fermi levels. A further trend sees an increase in the intensity of the DOS as the transition metal moves from HfC to WC, as a result of which the most localized peaks are seen for WC in the 3d and 4d carbide series (see Fig. 5); a trend that is also replicated for the groups 3–6 in the 3d and 4d carbide series (see Fig. S39 and S40, ESI†). This effect can be explained by the decrease in the strength of the carbon–metal covalent bonds in the group 6 carbides.\(^{17}\) Additionally, as the position of the metal component of the carbide moves from left to right along the series, the resulting negative shift in the DOS causes a shrinking of the conduction band as the covalent character of the material decreases. The decrease of charge transfer in the carbides of the metals later in the series is consistent with experimental studies, where the near-edge X-ray adsorption fine structure (NEXAFS) technique indicated a decrease in ionic character when the position of the parent transition metal moves from the left hand side to the middle of the transition metal block of the periodic table.\(^{100}\)

Kitchin et al.\(^{101}\) and Stottlemyer et al.\(^{25}\) showed a strong correlation between the binding energy of a hydrogen molecule...
and the d-band center in the density of states calculation. The Fermi level was set to zero and the more negative the center of the d-band density of states the higher the hydrogen binding energy. Importantly, this trend could also be used to explain the increase in reactivity of the TMCs over their parent transition metals, since bonds present in the elemental metals are purely metallic. In order to establish the presence of any such trend in the surfaces reported here, we have assessed the d-band centres of each surface, using the established protocol developed by Norskov et al. The results of this analysis are presented in Table 5 and clearly demonstrate that the centre of the d bands moves away from the Fermi level as more d-electrons are added to the parent metal. More interestingly, it appears that the d-band centres are lowest in the {001} surfaces and highest in the {111} terminations, in a result that mirrors the work function values (see Fig. 4). These results indicate that we could expect the {111} surface to be more active than the {001} faces, in spite of the lower work function in the former, which is related to the potential redox acidity of each surface. These results are in excellent agreement with previous work conducted by Norskov et al., who found that the d-band centre of metallic Platinum changed by ~1 eV between the {001} and {111} surfaces.

In 2005 Viñas et al. explored shifts in the core level density of states by comparing the C(2s) bands in diamond and graphite structures to those found in TMCs. Studying TiC, these C(2s) bands were the dominant component in a peak located at ~9.5 eV with respect to the Fermi energy. Similar peaks at approximately ~10 eV from the Fermi level were also found for all surfaces tested in this study. As with the metallic components, these intense peaks indicate more localized electrons, whilst a shift of those peaks towards the EF indicates a more negative character of the carbons. Djellouli and Aourag demonstrated that TMCs have more ionic character when terminated in the {111} plane, which assists in driving this shift in the density of states to higher energy occupations. Therefore, as we increase the ionic character of the carbide, either by moving from right to left across the periodic table or by terminating at the {111} surface, the density of surface available states increases.

Another interesting observation is that TMCs containing group 4d metals (TiC, ZrC & HfC) show very little overlap between their valence and conduction bands. In most cases the density of states at the Fermi energy drops to negligible levels. The one group 4 termination that does not follow the same pattern is the {111} face of HfC. Here the Fermi levels are positioned directly in the middle of a very sharp peak in the DOS, which indicates a much more metallic character to these two surfaces. These exceptions notwithstanding, the fact remains that in all other cases, the group four transition metal carbides appear not to have substantial densities of states at their EF. Stottlemeyer et al. hypothesized that this may be due to the lack of occupied d bands, thereby decreasing the amount of charge transfer between the metal and carbon components.

Conclusions

Periodic boundary DFT calculations have been used to undertake an extensive study into the low-index surface properties of a range of 3d, 4d and 5d transition metal carbides with rock-salt structures. In our bulk calculations, almost all the lattice parameters and bulk moduli are in very good agreement with experimentally derived values. Higher levels of surface rumpling are generally observed on surfaces with higher surface energy, i.e. the less stable surfaces. Generally, the lowest energy surfaces were the {001} faces and the lowest work functions appear to be obtained on the {011} terminations. The work functions of the two {111} surface terminations were determined to be higher in energy, whilst shifts in the density of states and d-band centres could indicate interesting activity towards electron-donating substrates. The present study lays the groundwork for more detailed investigations of these systems.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

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