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Brønsted/Lewis acid sites synergistically promote the initial C–C bond formation in the MTO reaction
Brønsted/Lewis acid sites synergistically promote the initial C–C bond formation in the MTO reaction†

Yueying Chu, Xianfeng Yi, Chengbin Li, Xianyong Sun and Anmin Zheng†

The methanol-to-olefin (MTO) reaction is an active field of research due to conflicting mechanistic proposals for the initial carbon–carbon (C–C) bond formation. Herein, a new methane–formaldehyde pathway, a Lewis acid site combined with a Brønsted acid site in zeolite catalysts can readily activate dimethyl ether (DME) to form ethene, is identified theoretically. The mechanism involves a hydride transfer from Al–OCH₃ on the Lewis acid site to the methyl group of the protonated methanol molecule on the adjacent Brønsted acid site leading to synchronous formation of methane and Al–COH₂⁺ (which can be considered as formaldehyde (HCHO) adsorbed on the Al³⁺ Lewis acid sites). The strong electrophilic character of the Al–COH₂⁺ intermediate can strongly accelerate the C–C bond formation with CH₄ as indicated by the significant decrease of activation barriers in the rate-determining-step of the catalytic processes. These results highlight a synergy of extra-framework aluminum (EFA) Lewis and Brønsted sites in zeolite catalysts that facilitates initial C–C bond formation in the initiation step of the MTO reaction via the Al–COH₂⁺ intermediate.

An industrial breakthrough stemmed from the discovery of the methanol to olefin (MTO) process, which allowed the catalytic conversion of methanol to ethylene and propylene by zeolites. This process constitutes an alternative route to light alkenes not relying on crude oil. The mechanism of this process has become a matter of intense debate and investigation both in industry and academia. On the basis of experimental and theoretical studies, two types of mechanisms, the direct one, and the hydrocarbon pool (HCP) one, have been proposed to explain C–C bond formation. The popularly accepted one is the HCP mechanism, in which carbenium species have been confirmed as the active species, and a complete catalytic cycle combining theory and experiment has been put forward for HZSM-5 and HSAPO-34 zeolites. Aromatics like polymethylbenzenes (MBs) or olefins like higher olefins represent two kinds of important HCP species during the process of MTO conversion. However, the active sites and the formation mechanism of the initial C–C bond in the induction period, has remained a controversial issue. More than 20 mechanisms have been put forward to explain the formation of the initial C–C bond with participation of various reactive intermediates such as oxonium ylides, carbocations, carbenes and free radicals catalyzed by Brønsted acid sites of zeolite catalysts. It has been evaluated by theoretical calculations that all the proposed direct mechanisms, e.g. carbene, oxonium ylide and methane–formaldehyde mechanisms were inhibitive of the C–C bond formation on account of their high activation barriers (54–44 kcal mol⁻¹). Recently, several new mechanisms that are responsible for the initial C–C bond formation were proposed. Lercher and Weckhuysen et al. proposed that methyl acetate was the intermediate responsible for the initial C–C formation during the MTO reaction. Fan and coworkers proposed a route involving methoxymethyl cation (CH₃OCH₂⁺) intermediates, in which the barrier for initial C–C formation has a low activation energy (<39.0 kcal mol⁻¹) over the Brønsted acid sites of HSAPA-34 and HZSM-5 zeolites. Besides the Brønsted acid catalysis, Copéret and Sautet et al. demonstrated that the surface Lewis acid sites on γ-Al₂O₃ also readily activate dimethyl ether (DME) to yield alkenes involving an Al-oxonium ion intermediate with a relatively low barrier (38.0 kcal mol⁻¹). Recently, Liu et al. obtained some new insights into the initial C–C bond formation by using in situ solid-state NMR. They suggested that a surface methyleneoxo-analogue was the crucial intermediate for the initial C–C bond formation and the C–C bond direct formation via an interesting synergistic mechanism, involving C–H bond breakage and C–C bond coupling during...
the initial methanol reaction in the chemical environment of zeolite catalysis.

It’s well known that a mild hydrothermal/thermal treatment usually results in a partial release of aluminum from a zeolite framework and causes formation of extra-framework aluminum (EFAl) species. Our previous NMR studies revealed that the formed EFAl species and the Brønsted site could be adjacent. Additionally, White et al. also demonstrated that the Brønsted site and the extra-lattice Al–OH species are adjacent by using the 2D exchange NMR experiment, and a synergistic effect of Lewis sites near Brønsted bridging acid sites (BAS) existed. Inspired by the pioneering work by Hutchings and Hirao that HCHO and CH₄ could be formed during methanol transformation over the Bronsted site of ZSM-5 zeolite and the reaction pathway proposed by Copéret that the surface Lewis acid sites on γ-Al₂O₃ readily activate dimethyl ether (DME) to yield alkenes, a new methane–formaldehyde mechanism associated with Bronsted acid and Lewis acid (i.e., EFAl species) sites in the zeolite catalysts for the initial C–C bond formation over the ZSM-5 zeolite and the reaction pathway during the methanol transformation over the Bronsted site are systematically investigated to explore the possible active sites and detailed reaction mechanisms for the C–C bond formation over the ZSM-5 zeolite catalyst.

**Calculation method**

ZSM-5 and SSZ-13 zeolites are represented by 72T and 74T models, respectively, which were extracted from their crystallographic structural data. The 72T contains the complete double 10-MR intersection pores of ZSM-5 zeolite. The 74T SSZ-13 model includes two complete cages connected via an 8-MR window. The terminal Si–H was fixed at a bond length of 1.47 Å, oriented along the direction of the corresponding Si–O bond. Based on the previous studies, the Si₁₂–O₃(Al)–O₃ and Si₁–O₃–O₃(H)–Al₁ were chosen as the acid site positions for H-ZSM-5 and H-SSZ-13, respectively. It’s theoretically demonstrated that the terminal oxygen (Al=O) atoms were not favored, but were prone to protonation to form EFAl hydroxy groups.

**Scheme 1** The newly proposed mechanism for the C–C bond formation at the synergistical BAS/LAS sites over zeolite catalysts. (Ads, represents the adsorbed DME; A, represents Al–OH–bound methyl (Al–OHCH₂); A', represents the Al–OHCH₂⁺ intermediate; B, represents the Al–OCH₂⁺ intermediate; C, represents the Al–OHCH₂⁺ intermediate; TS, represents the transition state).
HZSM-5, a spontaneous intramolecular acidic proton transfer readily occurred and resulted in the proton bound to the oxygen atom of the Al=O and resulted in AlOH2+ structure formation in HZSM-5 zeolite in the structure optimization, and a similar tendency was also observed in USY zeolite.\textsuperscript{31} For AlO1-3HSSZ-13, AlOOH/HSSZ-13 and AlO/HZSM-5 with terminal oxygen (Al=O) atoms, the intramolecular proton transfer produced more stable structures as well. As indicated in Fig. S1,\textsuperscript{†} the Gibbs free energies of the AlOH2+ at SSZ-13 (−29.4 kcal mol\textsuperscript{−1}), Al(OH)2+ at SSZ-13 (−62.3 kcal mol\textsuperscript{−1}) and Al(OH)3+ at ZSM-5 (−50.9 kcal mol\textsuperscript{−1}) were much lower than those of the corresponding forms with separated terminal Al=O and BAS sites at 573 K. It's noteworthy that these AlOH2+ and Al(OH)2+ were the isolated AlOH2+ and Al(OH)3+ EFAI species since the nearby BAS have been consumed. In contrast to EFAI that contained a terminal Al=O group, the other EFAIs (\textit{i.e.}, AlOH2+, Al(OH)2+, Al(OH)3+) were stable with the adjacent BAS in the ZSM-5 and SSZ-13 zeolites, and can be considered as AlOH2+/BAS, Al(OH)2+/BAS, and Al(OH)3+/BAS models. Thus, the five EFAI/BAS structures over the two zeolites were modeled as AlOH2+/BAS (Fig. S2a and S2f), Al(OH)2+/BAS (Fig. S2c and S2i), Al(OH)3+/BAS (Fig. S2d and S2j) and isolated AlOH2+ (Fig. S2b and S2g) and Al(OH)3+ (Fig. S2e and S2j) inside the two zeolite frameworks.

In order to maintain the electrical neutrality of calculated models, 1 or 2 framework Al atoms were used. This method has been extensively used in theoretical calculations to investigate the dealumination process and the effect of EFAI species on the acidity of zeolites.\textsuperscript{31−33} The previous studies have demonstrated that Al=O–(Si–O)\textsubscript{2}–Al exists in Si-rich H-ZSM-5 zeolites.\textsuperscript{34} Additionally, the multiple Brønsted acid protons (multiple framework Al atoms) in HZSM-5 zeolite have been directly observed by White's group using a combination of 1D and 2D MAS NMR experiments.\textsuperscript{36} Thus, two framework Al atoms separated by two framework Si sites used in this work for HZSM-5 zeolite are in agreement with the experimental structures.

In this work, the active site atoms and the adsorbed hydrocarbon complex were treated as the high-level layer (see Fig. S1†), while the rest of the frameworks were treated as the low-level layer. To retain the structural integrities of the modeled zeolite, partial structure optimizations of the 72T and 74T clusters were performed by relaxing the atoms in the high-level layer while keeping the rest of atoms fixed at their crystallographic positions. All the TS structures are found by the QST3 method using the Gaussian program. Then based on the imaginary vibrational model of the optimized TS, we adjusted the positions of the vibrational atoms slightly along the calculated reaction coordinate in the two directions toward the reactant and the product, respectively, and finally optimized the resulting structures to the minimum structures. These methods have been widely employed in other previous theoretical studies.

A combined theoretical approach, namely ONIOM (\textit{ω}B97XD/6-31G(d,p); am1) was used for the geometry optimization of adsorption states and transition states (TS). The \textit{ω}B97XD hybrid density function, combined with 6-31G(d,p) basis sets, was employed for the energy calculation. This method was a recently developed long-range-corrected hybrid functional by Chai and Head-Gordon, which implicitly accounted for empirical dispersion and could describe long-range dispersion interactions well with respect to the traditional density functional theory methods.\textsuperscript{38} This functional was also recently found to perform very well for the description of adsorption and reactions on zeolites. Since the AM1 method is believed to underestimate the local level interaction energies, all energies reported herein were predicted at the \textit{ω}B97XD/6-31G(d,p) level based on the optimized structures. The combined method could reproduce the experimental results obtained on MTO zeolite catalysts.\textsuperscript{36}

The harmonic frequency calculations employing a partial Hessian vibrational analysis (PHVA),\textsuperscript{37} including the high layer active acid sites and organic species were performed to check whether the stationary points found exhibit the appropriate number of imaginary frequencies. In frequency calculations, besides the atoms in the high-level layer and the organic fragment, the constraints of the zeolite framework were also kept the same as in geometry optimizations, so that only one imaginary frequency would be observed for transition state points and none for minima. The Gibbs free energies at 573 K were then calculated from harmonic frequencies.

Results and discussion

The initial C–C bond formation over ZSM-5 zeolite

Compared with methanol, dimethyl ether (DME) is more suitable for exploring the direct C–C bond formation route due to its higher reactivity in the initial MTO process. The calculated results have demonstrated the feasible formation of DME during the MTO reaction with the energy barriers of 15.4 kcal mol\textsuperscript{−1} for ZSM-5 and 28.0 kcal mol\textsuperscript{−1} for SSZ-13 zeolite (the optimized TS structure, see Fig. S3†) which is in agreement with the experimental results that DME could easily be produced at the initial stage of the MTO reaction.\textsuperscript{39} The DME adsorption on the five active sites is an entropy reduction step, and the entropy losses are ca. −34.0 to −46.0 cal K\textsuperscript{−1} mol\textsuperscript{−1} for all five sites accompanied by the adsorption Gibbs free energies (\Delta G\textsubscript{ads}) in the range of 2.3 to −23.2 kcal mol\textsuperscript{−1} (see Table S1†). It’s apparently observed that DME is more readily adsorbed (\Delta G\textsubscript{ads} = −23.2 kcal mol\textsuperscript{−1}) at AIOH/HZSM-5 among the five active centers and the optimized adsorption structure is provided in Fig. S4.† Thus, the C–C bond formation from the most stable state of DME adsorbed on the AIOH/BAS center, will be discussed in detail (Fig. 1 and S5†). In this case, the AIOH causes the CH3 migration of the protonated DME to produce AlOCH3 and leave a methanol molecule adsorbed on the conjugated alkaline oxygen center around the Brønsted acid site, via a barrier of 26.7 kcal mol\textsuperscript{−1}. The lower energy barrier demonstrates that the Al–OCH3 intermediate could be readily generated, in agreement with Sautet’s work that Al–OCH3 could be formed at the AIOH site during the DME transformation.\textsuperscript{39} Then, the generated methanol molecule allows abstraction of a hydride from the CH3 group in AIOCH3, generating methane and an Al–OCH3+ intermediate (B).
As illustrated in Fig. 1, the intermediate B will be formed with a barrier of 29.8 kcal mol\(^{-1}\). It’s interesting to note that Al–COH\(_2\)\(^{+}\) (B) can be considered as formaldehyde (HCHO) adsorbed on the Al\(^{3+}\) Lewis acid sites. Thus, the newly proposed mechanism is an analogous methane–formaldehyde route. It’s revealed experimentally by Morton et al. that the C–H bond of alkoxide species could be weakened and lead to aldehyde group formation based on the lower CH stretching frequencies relative to the neutral alkanol molecule by using IR multiple photon dissociation (IRMPD) spectra.\(^{38}\) In this work, the low energy barrier for the Al–COH\(_2\)\(^{+}\) formation from Al–OCH\(_3\) (Al methoxide) through TS2 is in good agreement with this experimental result. Additionally, Lercher et al. also demonstrated that the LAS sites could promote the yield of HCHO in ZSM-5 zeolite by hydride transfer.\(^{39}\) As a comparison, the methane–formaldehyde route for the C–C bond formation on the BAS is also investigated (see Fig. 1). In this mechanism, the surface CH\(_3\) attached to the hydrogen in the methyl group of methanol to form methane and HCHO, and subsequently, the methane reacts with HCHO to form ethanol (see Scheme S1\(^{†}\)). As shown in Fig. 1, the C–C bond formation on the zeolite BAS site is strongly prohibited in the methane–formaldehyde mechanism due to the relatively high barrier (>40 kcal mol\(^{-1}\)), which has also been illustrated in the previous work.\(^{16}\) However, due to the synergy of the BAS/LAS, the newly proposed mechanism of the C–C bond formation differs from the conventional one. Under synergistical BAS/LAS conditions, the strong electrophilic character of the Lewis acid site facilitates the addition reaction between the Al–OCH\(_2\)\(^{+}\) and CH\(_3\) molecules, which leads to the C–C bond formation with the barrier decreasing to 30.2 kcal mol\(^{-1}\).

Fig. 2 provides the transition state structures of the concerted reactions for Al–COH\(_2\)\(^{+}\) (Fig. 2a) and C–C bond (Fig. 2b) formation over the AlOH/BAS site in ZSM-5, and the
complete structural change during the C–C bond formation is shown in Fig. S6 and Table S2†. For the Al–OCH$_3^+$ formation, the generated methanol molecule allows abstraction of a hydride from AlOCH$_3$ to generate methane, Al–OCH$_2^+$ oxo-nium and H$_2$O. The oxonium species is characterized by a C–O distance equal to 1.354 Å at the transition-state, while the distance of the newly formed C–H bond is equal to 1.417 Å and the one being broken is equal to 1.209 Å (see TS2 in Fig. 2a). Subsequently, the water molecule acting as an H bridge abstracts an H$^+$ of the CH$_4$ molecule and then returns a proton (H$^+$) to the conjugated O site of the zeolite. The corresponding transition state for the C–C bond formation step displays the incoming C–C and the O–H bond formation with the distance of 1.820 and 1.805 Å, respectively (see Fig. 2b). It’s noteworthy that the barrier of the rate-determination step (39.7 kcal mol$^{-1}$) is close to that of in the MTO cycles (40 kcal mol$^{-1}$). Therefore, the initial C–C bond is possibly formed by the synergism of Al(OH)$_2$/Brønsted sites. However, compared with the barriers of AlOH (26.7–30.2 kcal mol$^{-1}$), the relatively higher barriers apparently indicated the formation of kinetically less favorable Al(OH)$_3$ species. While for the Al(OH)$_3$/Brønsted sites, formation of Al–OCH$_2^+$ intermediates is unlikely because its barrier is as high as 56.7 kcal mol$^{-1}$ in step 2 (see Table 1 and Fig. S8†). This trend is in good agreement with the experimental results for the Al$_2$O$_3$ samples that the Al(OH)$_3$ species over fully hydrated Al$_2$O$_3$ surfaces are inactive for the C–H bond activation. For the isolated Al(OH)$_2^+$ (originated from terminal oxygen of AlOOH protonated by proximal Brønsted acid sites) at the ZSM-5 framework, the initial C–O bond activation route with the transfer of the methoxy group on the isolated EFAl AlOH$^{2-}$ site is associated with a barrier of 68.4 kcal mol$^{-1}$, indicating that the reaction cannot occur during the MTO reaction. It is illustrated that the synergistical BAS/LAS sites were an indispensable factor to accelerate the DME reaction. The corresponding barriers of the C–C bond formation ($\Delta G_{\text{act1}}$, $\Delta G_{\text{act2}}$, and $\Delta G_{\text{act3}}$) are 35.8, 39.7 and 39.7 kcal mol$^{-1}$, respectively (see Table 1 and Fig. 3), on the Al(OH)$_2$/BAS site. It’s noteworthy that the barrier of the rate-determination step (39.7 kcal mol$^{-1}$) is close to that of in the MTO cycles (40 kcal mol$^{-1}$). Therefore, the initial C–C bond is possibly formed by the synergism of Al(OH)$_2$/Brønsted sites. 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zeolite, it can be concluded that both AlOH and Al(OH)$_2$ are effective active sites for the C–C bond formation, while, the C–C bond cannot be realized on the neutral species Al(OH)$_3$ and isolated AlOH$_2^+$ and Al(OH)$_2$ species in the MTO reaction.

The effective route for ethene formation

It is well known that ethene plays a crucial role in the MTO reaction, which can act not only as the olefin product but also as the key intermediate for HCP formation. Thus, the next important case is the pathway of ethene formation from the Al-bound ethoxide (C). Three possible routes involving H$_2$O, methanol and DME are considered in this work. The reactions contain three elementary steps: (1) abstracting the ethyl group from the Al-bound ethoxide intermediate and regeneration of LAS; (2) yielding the surface ethoxide; (3) formation of ethene and regeneration of BAS (see Scheme S2†). As shown in Fig. 4, the barriers of the rate-determining steps in the three routes over ZSM-5 zeolite are 36.6 (H$_2$O), 32.4 (methanol) and 35.0 kcal mol$^{-1}$ (DME), respectively. The low activation barriers reveal that all three routes are feasible. Noticeably, the DME route is related to the CH$_3$CH$_2$O$^+$ (CH$_3$)$_2$ oxonium ion (F, in Fig. 4). This is in agreement with the previous studies by Liu et al. that the oxonium ion could be captured during the initial period of the MTO reaction by the in situ SSNMR experiment and it acted as a paramount intermediate during the initial ethene formation.$^{25}$ Among the three routes, the CH$_3$OH-mediated route prevails, which could be ascribed to the well fit dimension of protonated CH$_3$CH$_2$OCH$_3$ (E) with the ZSM-5 pore structure. Overall, it is apparently indicated that the DME reaction over the AlOH/BAS site of ZSM-5 could produce alkenes readily, and then, the alkenes can generate HCP species to initiate the MTO cycles self-sustained in the steady state.

The initial C–C bond formation over SSZ-13 zeolite

SSZ-13 zeolite with the CHA topology structure is another extensively used zeolite catalyst for the MTO reaction due to the pore selectivity, which possesses a cage-like pore structure with an effective pore diameter of 7.31 Å.$^{41}$ Thus, the initial alkene formations involving the Al–OCH$_3^+$ intermediate over SSZ-13 zeolite are also investigated in this work. In contrast to ZSM-5 zeolite, the AlOH/BAS in SSZ-13 results in a larger barrier for the initial C–O bond activation of DME (54.4 kcal mol$^{-1}$, see Fig. S10†). Such a large barrier could be ascribed to the severe deformation of the AlOH group from the adsorbate to the transition state (Fig. S10†). The energy barriers at 573 K (Table 1, Fig. 1 and S10–S14 in the ESI†) show that the Al(OH)$_3$/BAS site

### Table 1 Computed Gibbs free energy barriers (kcal mol$^{-1}$) of the conventional and newly proposed methane–formaldehyde routes on the Bronsted acid sites and synergistic Bronsted/Lewis acid sites for the C–C bond formation in the MTO reaction at 573 K. The detailed reaction routes are shown in Schemes 1, S1 and S2 (see the ESI)

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<th>Isolated Lewis acid</th>
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<th>Conventional Bronsted Acid mechanism</th>
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<td>AlOH$^{2+}$/BAS</td>
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<td>TMO</td>
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<td>$\Delta G_{\text{act2}}$ 82.6</td>
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<td>$\Delta G_{\text{act4}}$ 30.2</td>
<td>$\Delta G_{\text{act5}}$ 39.7</td>
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<td>$\Delta G_{\text{act1}}$ 19.7</td>
<td>$\Delta G_{\text{act2}}$ 32.4</td>
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</table>
over SSZ-13 zeolite is more effective for catalyzing the C–C bond formation among the five species. The adsorption energy of DME at the Al(OH)/BAS site over SSZ-13 zeolite is 

\[-5.9 \text{ kcal mol}^{-1}\] similar to that over SAPO-34 (\[-8.1 \text{ kcal mol}^{-1}\]).\textsuperscript{19} The energy barriers of the C–C bond formation are shown in Fig. 1, and the complete structure changes during the C–C bond formation are shown in Fig. S15 and Table S3\textsuperscript{†}. The energy barriers are in the range of 25.0–33.0 kcal mol\textsuperscript{-1} similar to that over AIOH/HZSM-5 zeolite (Fig. 1 and Fig. S5\textsuperscript{†}), indicating that the C–C bond could be easily formed over H-SSZ-13 zeolite in the induction stage. The calculated results show that the C–C bond formation between CH\textsubscript{4} and Al–OCH\textsubscript{2}\textsuperscript{+} via TS3 readily occurred over ZSM-5 and SSZ-13 zeolites. Different from ZSM-5, which has a high Si/Al ratio and prevents the proximity of two EFAL centers, the low Si/Al ratio in SSZ-13 results in the proximity of two EFAL centers. Therefore, the C–C bond formation between CH\textsubscript{4} and Al–OCH\textsubscript{2}\textsuperscript{+} via another neighboring Lewis acid site is also explored over SSZ-13 zeolite. The transition state displays the C–C formation and the C–H bond breakage with the distance of 1.970 and 1.227 Å (see Fig. S16b\textsuperscript{†}), which is similar to the transition state via the bridge H\textsubscript{2}O (see Fig. 2d). The calculated energy barrier is 32.4 kcal mol\textsuperscript{-1} at 573 K, demonstrating the possibility of C–C bond formation through other neighboring Lewis acid sites in the low Si/Al ratio zeolite. Additionally, the ethene formation routes at the Al(OH)/BAS site over SSZ-13 zeolite are also investigated. Compared with the three routes for ethene formation (Fig. 4), the DME route is preferable, different from ZSM-5 zeolite (methanol route). The calculated barrier for ethox ide formation through the CH\textsubscript{3}CH\textsubscript{2}O\textsuperscript{+}(CH\textsubscript{3})\textsubscript{2} oxonium (F) intermediate is 16.8 kcal mol\textsuperscript{-1} lower than that in ZSM-5 (35.0 kcal mol\textsuperscript{-1}), which could be ascribed to the larger zeolite pore dimension of SSZ-13 (\(D_1 = 7.31\) Å) than ZSM-5 (\(D_1 = 6.30\) Å).\textsuperscript{41} Obviously, the ethene formation is favored kinetically, with the barrier of 23.7 kcal mol\textsuperscript{-1} for the rate-determination step, signifying that the reaction readily occurs at 573 K.

**The driving force for the CH\textsubscript{4} activation**

On the basis of the aforementioned facts, the coupling of CH\textsubscript{4} and Al–OCH\textsubscript{2}\textsuperscript{+} intermediate is crucial for the C–C bond formation in the MTO reaction. As is well known, the CH\textsubscript{4} molecule is very inert and the C–H bond dissociation energy is as high as 105 kcal mol\textsuperscript{-1}.\textsuperscript{42} Therefore, the CH\textsubscript{4} activation mechanism on the synergistical Bronsted/Lewis acid sites should be investigated in detail. It is noteworthy that the CH\textsubscript{4} molecule could be polarized by a strong nucleophile (i.e., HCHO) to lead to the C–C bond coupling between CH\textsubscript{4} and HCHO with a barrier at 44.0 kcal mol\textsuperscript{-1} through the traditional methane–formaldehyde route inside ZSM-5 zeolite.\textsuperscript{43,44} Additionally, such a methane–formaldehyde route for the C–C bond formation on the BAS is also investigated in this work. As shown in Fig. 1, the barrier of the initial C–C bond formation between CH\textsubscript{4} and HCHO on the zeolite BAS site is 41.8–45.4 kcal mol\textsuperscript{-1}, which is in agreement with the previous work.\textsuperscript{46} Compared with neutral HCHO (the positive charge of C atom, 0.221|\textit{e}|), the HCHO bound to the Lewis acid site (e.g., Al–OCH\textsubscript{2}\textsuperscript{+}, positive charge of C atom, 0.357|\textit{e}|) would be more electrophilic and susceptible to polarizing CH\textsubscript{4}, and consequently a relatively lower barrier for the C–C bond formation will be obtained. In order to explore the driving force of the C–C bond formation step, the C–H bond length of CH\textsubscript{4} approaching the strong electrophilic Al–OCH\textsubscript{2}\textsuperscript{+} species has also been investigated. It is observed that the C–H bond of CH\textsubscript{4} is gradually activated as illustrated in Fig. 5 that the C–H bond length of CH\textsubscript{4} is elongated from 1.097 (adsorbed state) to 1.231 Å (transition state) with the decreasing
Propene formation following the newly proposed mechanism

The experimental work by Kondo demonstrated that the propene also serve as the initial product of MTO reactions by infrared (IR) spectroscopy.43 In terms of the newly proposed route, propene can be generated independent of the ethene route (Scheme S3†), which coincides with Kondo's experimental work.43 As illustrated in Fig. 7 and S17,† the Al-bound ethoxide (important intermediate for ethene formation) can further react with methanol and give rise to the intermediate G (Al-COCH3) formation with a barrier of 27.3 kcal mol⁻¹ over ZSM-5 zeolite. The intermediate G can be considered as acetaldehyde (CH3CHO) adsorbed on the Al⁺ Lewis acid site. The strong electrophilic character of the Al-OCH3⁺ intermediate is the driving force for the CH4 activation and C=C bond formation in our work.

Experimental evidence of the newly proposed mechanism

In this work, we theoretically identified a new methane–formaldehyde pathway for the initial alkene formation induced by synergistic interaction of BAS/LAS inside zeolite frameworks. It is noteworthy that extensive experimental work existed in previous work to support this new route. On the one hand, the synergistical Lewis/Bronsted acid activated center (e.g., Al(OH)₃ and AIOH EFAl species in close proximity to BAS) has been determined by the advanced NMR approach in the ZSM-5 and other zeolite catalysts.13,14 On the other hand, the CH₄, HCHO, Al–OCH₃ and oxonium ion intermediates involving the new mechanism also have been observed in the MTO catalytic reaction by Hutchings and coworkers.15 Lercher et al. indicated that the HCHO could be generated in ZSM-5 zeolite, and it’s further found that the LAS could accelerate the formation of HCHO.39 On the basis of the ¹³C NMR experiment, the Al–OCH₃ intermediate has also been detected on the surface AIOH site by...
Philippe et al. Furthermore, it’s illustrated that the reaction activity following this new proposed mechanism is considerably enhanced compared to the conventional pathways at the isolated Brønsted or Lewis acid sites. As shown in Table 1, the barriers for the initial ethene formation have significantly decreased from 41.8–45.4 kcal mol$^{-1}$ at the isolated BAS to 32.4–33.0 kcal mol$^{-1}$ at the synergistic BAS/LAS sites over ZSM-5 and SSZ-13 zeolites. Moreover, the new mechanism is also more effective at the synergistic BAS/LAS sites than at the isolated LAS sites of γ-Al$_2$O$_3$ surface (with the barrier of 38 kcal mol$^{-1}$). Consequently, the synergistic effect of the adjacent BAS/LAS sites in the zeolite catalysts could significantly decrease the energy barriers of the initial ethene formation in the MTO reaction through the new methane–formaldehyde route. On the other hand, it’s demonstrated that the effective FAI structures ($\text{AlO}_2^{2+}$ or $\text{Al(OH)}_3$) and detailed reaction pathways strongly determined by the zeolite unique framework properties.

**Concept of synergy of Brønsted and Lewis acid sites on other catalytic reactions**

The DFT calculations in our work give direct theoretical evidence that the synergy of FAI and Brønsted acid sites in zeolite catalysts could alter the reaction mechanism, and thus strongly reduce the activation barrier of the initial C–C bond formation in the MTO reaction. Therefore, it provided a paradigm for the synergy of Lewis acid sites (FAI) and Brønsted acid sites in zeolite catalysts and facilitated the catalytic reactions with the complete mechanism calculations. It’s noteworthy that such a synergistic concept has been directly or indirectly suggested in the catalytic experiments as well. For instance, Schallmoser et al. showed that the strong BAS vicinity of FAI displayed a rate enhancement in alkane cracking. Lercher et al. demonstrated that the synergy of FAI and BAS could promote the production of the aromatic and light alkanes during the MTH (methanol to hydrocarbon) reaction. Huang et al. also proved that the cooperativity of BAS and FAI significantly improved the yield of acrolein from the selective glycerol dehydration. Besides the FAI, interaction of other extra-framework metal cations such as La$^{3+}$ and Ga$^{2+}$ with BAS could improve the catalytic activity as well. Lercher et al. showed that the cooperative effect of La$^{3+}$ cations and the presence of BAS sites promoted catalytic isomerization, cracking, and alkylation of alkanes. Hensen et al. indicated that the synergy between Ga and BAS had the higher activity with relatively weak coke formation in the n-heptane cracking reaction. Despite the promoting effect of BAS/LAS synergy being widely explored, little mechanistic investigation for such synergistic effect on the pathways has been done. In principle, three possible ways of BAS/LAS synergy promote the zeolite catalytic performances. (I) A typical feature of the BAS/LAS synergistic effect is enhancing the strength of BAS resulting in the higher catalytic reactivity, as illustrated by the recent DFT theoretical calculations and catalytic experiments for alkane activations. (II) LAS can also act as a active center for hydrocarbon activation and transformation, and thus the presence of the Lewis acid site in the zeolite surface will provide an opportunity for the Lewis acid-catalyzed pathways distinct from Brønsted acid catalysis. (III) The synergy of proximal Lewis and Brønsted acid sites play a full role in the catalytic process resulting in the enhancement of the catalytic activity. Our calculation work brings new atomic-scale insights into understanding the detailed catalytic mechanism involved in BAS and LAS sites by the DFT calculation. The quantitative understanding of the reaction mechanism is key to design better and more stable BAS/LAS catalysts, and gives a clear blue print for material synthesis of new highly effective catalysts.

**Conclusions**

In this contribution, the initial C–C bond formation during the initial stage of MTO process via a new methane–formaldehyde pathway on zeolite LAS/BAS was identified theoretically. For the first time, a formaldehyde-analogue (Al–OCH$_2$) intermediate, originated from a hydride abstraction from a surface Al–OCH$_3$ species has been recognized to be the crucial intermediate for the initial C–C bond formation in MTO process over zeolite. The calculated Gibbs free energy barrier shows that the strong electrophilic character of the formaldehyde-analogue intermediate can strongly accelerate the C–C bond formation with CH$_4$ and the overall reaction process is energy favorable. The proposed pathway in this contribution shows for the first time the initial ethene formation involved in various intermediate species observed in the previous experimental work, such as Al–OCH$_3$, CH$_4$, HCHO and oxonium ions. Additionally, this contribution also proves the different mechanism of the initial C–C bond formation with systematic calculation of all the active sites in ZSM-5 and SSZ-13, which is very important for demonstrating the structure–performance correlation for the MTO reaction.

Furthermore, this contribution gives direct evidence that the synergy of LAS and BAS in zeolite catalysts could facilitate catalytic reactions with complete mechanism calculations, and provide a good paradigm to determine the active sites and mechanisms of heterogeneous catalysis using high level DFT calculations.

**Conflicts of interest**

The authors declare no competing financial interests.

**Acknowledgements**

This work was supported by the National Natural Science Foundation of China (No. 21403290, 21522310, 21473244, 91645112 and 21773296), and Natural Science Foundation of Hubei Province of China (2018CFA009), Key Research Program of Frontier Sciences, CAS (No. QYZDB-SSW-SLH026), Program for Applied Research on Super Computation of the NSFC-Guangdong Joint Fund (the second phase) under Grant No. U1501501.
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