Characterization of magnetic relaxation when biofunctionalized magnetic nano-particles are associated with biomarkers in the liquid state in biomedical applications

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This study determined the characteristics of the time-dependent effective relaxation time $\tau_{\text{eff}}$ and magnetization $M$ when biofunctionalized magnetic nanoparticles (BMNPs) associated with biomarkers in a liquid immunoassay. Carcinoembryonic antigen (CEA) was used as the biomarker. BMNP is an anti-CEA that was coated onto dextran-coated Fe$_3$O$_4$ and labeled as Fe$_3$O$_4$-anti-CEA. The phase lag $\theta$ of $M$ with respect to the applied field $H$ was measured using a sensitive homemade alternative-current-susceptometer, and $\theta$ was measured using lock-in detection. The results were used to estimate $\tau_{\text{eff}}$ using the relationship $\tan \theta(t) = \omega \tau_{\text{eff}}(t)$, where $2\pi f = \omega$ and $f$ is the excitation frequency. $\Delta_{\text{eff}}$ increased with $\Phi_{\text{CEA}}$, where $\Delta_{\text{eff}}$ was the increment of $\tau_{\text{eff}}$ after Fe$_3$O$_4$-anti-CEA associated with CEA, and $\Phi_{\text{CEA}}$ was the concentration of CEA. Additionally, $M$ enhanced when $\Phi_{\text{CEA}}$ increased. We attributed these enhancements to magnetic dipole–dipole interactions among MNPs that contributed extra $M$ and in turn enhanced $\tau_{\text{eff}}$. Magnetic clusters after the association were verified using a transmission electron microscope. This study established the relationship between $\Delta_{\text{eff}}/\tau_{\text{eff},0}$ and $\Phi_{\text{CEA}}$, where $\tau_{\text{eff},0} = \tau_{\text{eff}}(\Phi_{\text{CEA}} = 0)$, allowing the assay of an unknown amount of CEA molecules.

I. Introduction

Imunoassays use a variety of labels for assaying antibodies or antigens. These labels are typically chemically conjugated or linked to desired analyses. The most common methods are enzyme-linked immunosorbent assay, radioimmunoassay, and real-time quantitative polymerase chain reaction. Recently, magnetic immunoassays (MIAs) have gained considerable attention because there is negligible magnetic background in a biomolecular sample during magnetic detection; thus, MIAs can reach a high detection sensitivity. In MIAs, biofunctionalized magnetic nanoparticles (BMNPs) are used as labels. The assays involve the specific binding of a bioprobe to its analyte, and a magnetic label is conjugated to one element of the pair to form magnetic clusters. Because of molecular interactions between MNPs, their magnetic properties change after the association. These changes in magnetic characteristics provide a sensing mechanism. The signal for magnetic clusters is then detected using magnetic sensors, which measure the change of magnetic signals that is induced by magnetic clusters. Changes in magnetic signals are proportional to the concentrations of analytes (e.g., viruses, bacteria, tumor markers, and cardiac markers) in samples. Different sensing mechanisms have been used for MIAs, such as Brownian relaxation time, Néel relaxation time, remanent magnetization, saturation magnetization, spin–spin relaxation time, and alternative-current (AC) susceptibility.

Effective relaxation time $\tau_{\text{eff}}$ is one of the magnetic properties that are affected by the magnetic clustering of BMNPs when they associate with biomarkers. The value of $\tau_{\text{eff}}$ reflects the effect of clustered MNPs on Brownian and Néel relaxations. To study $\tau_{\text{eff}}$, Liao et al. used a homemade AC susceptometer.

In the current study, a sensitive homemade AC susceptometer was used to characterize $\tau_{\text{eff}}$ when BMNPs that are composed of Fe$_3$O$_4$-anti-carcinoembryonic antigen (CEA) associated with CEA in biomedical applications. This study found that $\Delta_{\text{eff}}$ increased with the concentration of CEA, $\Phi_{\text{CEA}}$, where $\Delta_{\text{eff}}$ was the increment of $\tau_{\text{eff}}$. This increase was attributed to dipole–dipole interactions between MNPs, which contributed extra magnetization and in turn increased the value of $\tau_{\text{eff}}$. A relationship between $\Delta_{\text{eff}}/\tau_{\text{eff},0}$ and $\Phi_{\text{CEA}}$ was established, where $\tau_{\text{eff},0} = \tau_{\text{eff}}(\Phi_{\text{CEA}} = 0)$. This relationship is based on a $(\Delta_{\text{eff}}/\tau_{\text{eff},0})$ versus $\Phi_{\text{CEA}}$ curve and can be used to determine an unknown amount. This paper also discusses the merits of using the $\Delta_{\text{eff}}/\tau_{\text{eff},0}$ ratio for biosensing.
II. Experiments

BMNPs are anti-CEAs that were coated onto dextran-coated MNPs and labeled as Fe₃O₄-anti-CEA (MF-CEA-0060, MagQu Co., Taiwan). The biotarget was CEA (AbD). A feasibility study for clinical use reported the development of antibody-functionalized magnetic nanoparticles for the immunoassay of CEA. The mean diameter of BMNPs was 53.8 ± 17.8 nm as detected through dynamic light scattering (Nanotrac-150, Microtrac) and shown in Fig. 1a. The magnetization reagent was characterized using a vibrating sample magnetometer (Hystermag MagQu Co. Taiwan). The magnetization was given as a function of the concentration of biomarkers to characterize their abundance.

III. AC susceptibility

The AC susceptibility $\chi_{ac}(\omega)$ of the samples is expressed as follows:\textsuperscript{28,30}

$$\chi_{ac} = \chi' + i\chi''$$

(1)

with

$$\chi' = \chi_0[1/(1 + (\omega\tau_{eff})^2)],$$

(2)

$$\chi'' = \chi_0(\omega\tau_{eff})/[1 + (\omega\tau_{eff})^2]$$

(3)

where $i = (-1)^{1/2}$, $\theta = \tan^{-1} \omega\tau_{eff}(t) = \chi''/\chi'$ is the phase lag for the time-varying magnetization, $M(t)$, with respect to the applied AC magnetic field, $H(t)$, and $\tau_{eff}$ is the effective relaxation time. In this study, $\theta(t)$ was detected using a homemade AC susceptometer and the lock-in detection technique at 18 kHz. The time evolution of $\tau_{eff}(t)$ was measured by monitoring $\theta(t)$. The value of $\tau_{eff}(t)$ was estimated using the relationship $\theta = \tan^{-1} \omega\tau_{eff}(t)$. The value of $\Delta\tau_{eff} = [\tau_{eff}(t = 0) - \tau_{eff}(t = \infty)]$ was given as a function of the concentration of biomarkers to characterize their abundance.

IV. Results and discussion

To explore and confirm the combination of Fe₃O₄-anti-CEA and CEA, a TEM was used to verify the presence of magnetic clustering when CEA associated with Fe₃O₄-anti-CEA. Fig. 2a shows a TEM image of CEA molecules; single CEA molecules are marked with small dashed circles. A CEA molecule has a mean length of approximately 29 nm, which is close to the value given in Fig. 2b. Fig. 2b shows a TEM image of magnetic clusters when Fe₃O₄-anti-CEA associated with CEA molecules; some magnetic clusters are marked with a large dashed circle. Each magnetic cluster was composed of several small magnetic clusters. Also marked is the independent Fe₃O₄-anti-CEA and MNPs inside the magnetic clusters; the formation of magnetic clusters was verified using a TEM. The size of associations with CEA molecules was changeable; if the concentration of CEA molecules was higher, then a magnetic cluster was formed. Thus, the size of Fe₃O₄-anti-CEA associated with CEA molecules increased.

Fig. 3 illustrates curves for $M$ as a function of $H$ after the reagents that were composed of Fe₃O₄-anti-CEA associated with different concentrations of CEA in a liquid state. This shows that when $H = 0.16$ T and $M = 0.07$ emu g⁻¹ for the reagent, then $M$ increased to 0.011, 0.154, and 0.218 emu g⁻¹ after the
reagent with $\Phi_{\text{CEA}} = 1, 5,$ and 10 $\mu$g mL$^{-1}$ associated with CEA, respectively. This increase is attributable to dipole–dipole interactions between MNPs in the magnetic clusters. Thus, the magnetization increased with the CEA concentration.

For a homogeneous MNP with a total number of particles, $N$, a mean magnetic moment, $\langle m \rangle$, and an effective mean diameter, $d_{\text{eff}}$, the magnetization $M(H)$ at $H$ is expressed as follows:

$$M(H) = N\langle m \rangle L(\alpha H) = \alpha L((\beta H))$$

and

$$L(x) = \coth(x) - 1/x$$

where $M_{\text{sat}} = N\langle m \rangle$ and $\beta = \mu_0\langle m \rangle/k_BT$; $k_B$ is Boltzmann’s constant and $T$ is the absolute temperature (a distribution of magnetic nanoparticles, the magnetic properties, such as the magnetization, are detailed in the ref. 32).

Fig. 2 (a) A TEM picture of CEA molecules and (b) magnetic clusters after Fe$_3$O$_4$-anti-CEA associated with CEA molecules.

Fig. 3 Curves for $M$ as a function of $H$ after the reagents that are composed of Fe$_3$O$_4$-anti-CEA associated with different concentrations of CEA in a liquid state.

Fig. 4a exhibits the change in $\theta$ over time when Fe$_3$O$_4$-anti-CEA associated with different CEA concentrations. $\Phi_{\text{CEA}}$ was detected using an AC susceptometer and a lock-in technique. $\theta$ increased over time and $\theta = 6^\circ$ for the reagent. The value of $\theta$ increased to $\theta = 9.4^\circ$ when $t = 7200$ s for CEA with a $\Phi_{\text{CEA}} = 10$ $\mu$g mL$^{-1}$ conjugated with Fe$_3$O$_4$-anti-CEA. Fig. 4b shows the relationship between $t_{\text{eff}}$ and time for the reaction process when the reagent conjugated with different concentrations of $\Phi_{\text{CEA}}$. The value of $t_{\text{eff}}$ for the reagent was 0.93 $\mu$s when $t = 0$ and remained constant until $t = 7200$ s, which demonstrated that the AC susceptometer had stable performance. In the reaction with 10 $\mu$g mL$^{-1}$ CEA, the value of $t_{\text{eff}}$ was approximately 0.93 $\mu$s when $t = 0$ and the value of $t_{\text{eff}}$ increased to 1.43 $\mu$s when $t = 7200$ s. The $t_{\text{eff}}$ versus $t$ curve showed saturation at approximately $t = 7200$ s.

Yang et al. studied the effect of temperature on immuno-reaction kinetics for a BMNP assay of biomarkers for colorectal cancer. The activation energy that was required for the reaction in immunoassay was determined to be $10^{19}$ J per molecule. At higher temperatures, a significant increase was observed in the number of molecules with energy that was higher than the activation energy, which is the principal reason for the increase in the reaction rate. The current study indicated that it takes approximately 2 h to complete the association at 298 K. An increase in the reaction temperature decreased the reaction time.

Fig. 5 illustrates the value of $t_{\text{eff}}$ as a function of $\Phi_{\text{CEA}}$ when the reagent associated with various concentrations of CEA; the red line is a guide. It is seen that $t_{\text{eff}} = 0.93$ $\mu$s for a reagent that consisted of Fe$_3$O$_4$-anti-CEA. The value of $t_{\text{eff}}$ increased to 1.43 $\mu$s when $\Phi_{\text{CEA}} = 10$ $\mu$g mL$^{-1}$ associated with the reagent. The increase in the value of $t_{\text{eff}}$ after association with Fe$_3$O$_4$-anti-CEA is due to magnetic interactions between MNPs in the associated magnetic clusters. The value of $M$ increased; therefore, the value of $t_{\text{eff}}$ increased.

Two simultaneous relaxations occur during the reaction process: Néel and Brownian relaxation. In Brownian relaxation,
the magnetic moment is locked to the crystal axis and the particle rotates. The corresponding relaxation time is \( \tau_B \) when the field is turned off. In Néel relaxation, the magnetic moment rotates within the crystal, and the corresponding relaxation time is \( \tau_N \). The Brownian relaxation time \( \tau_B \) is expressed as \( \tau_B = 3\eta V_H/k_B T \), where \( \eta \) is the viscosity coefficient, \( k_B = 1.38 \times 10^{-23} \text{ J K}^{-1} \) is the Boltzmann constant, \( T \) is the absolute temperature (K), and \( V_H \) is the hydrodynamic volume of BMNPs.

The Néel relaxation time, \( \tau_N \), is given by the expression,

\[
\tau_N = [(\pi/2)^3/2]_0 \exp[\rho/(\rho)]^{1/2},
\]

where \( \rho = KV_M/k_B T \), \( K \) is the anisotropy constant, \( \tau_0 \) is the relaxation time, and \( V_M = (4\pi/3)R^3 \) is the magnetic volume of MNPs with radius \( R \). The approximate mean core value was \( \langle R \rangle = 37 \text{ nm} \) in this study. If \( \langle R \rangle = 37 \text{ nm} \), then \( \tau_{\text{Brownian}} \) is in the order of microseconds and \( \tau_{\text{Néel}} \) is in the order of milliseconds or longer.\(^{25}\) The mean hydrodynamic diameter of BMNPs in this work was approximately 47 nm, which equates to a core size of approximately 38 nm. Because \( 1/\tau_{\text{eff}} = 1/\tau_{\text{Brownian,eff}} + 1/\tau_{\text{Néel,eff}} \) and \( 1/\tau_{\text{Brownian,eff}} > > 1/\tau_{\text{Néel,eff}} \), the values of \( 1/\tau_{\text{eff,eff}} \sim 1/\tau_{\text{Brownian,eff}} \) can be approximated.

Brownian relaxation dominates the time dependency of \( \tau_{\text{eff}} \) in the association process that is shown in Fig. 4b.

Fig. 6 illustrates \( \Delta \tau_{\text{eff}}/\tau_{\text{eff,0}} \) as a function of \( \Phi_{\text{CEA}} \) when \( \text{Fe}_3\text{O}_4 \)-anti-CEAs conjugated with CEAs, where \( \Delta \tau_{\text{eff}} = \tau_{\text{eff}} (\Phi_{\text{CEA}}) - \tau_{\text{eff}} (\Phi_{\text{CEA}} = 0) \) and \( \tau_{\text{eff},0} = \tau_{\text{eff}} (\Phi_{\text{CEA}} = 0) \) at \( t = 7200 \text{ s} \). In an assay of \( 10 \mu\text{g ml}^{-1} \) CEA molecules, \( \Delta \tau_{\text{eff}}/\tau_{\text{eff,0}} = 0.05 \) as \( \Phi_{\text{CEA}} \).

Fig. 6 \( \Delta \tau_{\text{eff}}/\tau_{\text{eff,0}} \) as a function of \( \Phi_{\text{CEA}} = 0.01 \mu\text{g ml}^{-1} \) and \( \Delta \tau_{\text{eff}}/\tau_{\text{eff,0}} \) increases to 0.54 when \( \Phi_{\text{CEA}} = 0.01 \mu\text{g ml}^{-1} \); \( \Delta \tau_{\text{eff}}/\tau_{\text{eff,0}} \) increases when \( \Phi_{\text{CEA}} \) increases.

The value of \( \Delta \tau_{\text{eff}}/\tau_{\text{eff,0}} \) as a function of \( \Phi_{\text{CEA}} \) is described by a logistic function:

\[
\Delta \tau_{\text{eff}}/\tau_{\text{eff,0}} = (A - B)/(1 + [(\Phi_{\text{CEA}})/(\tau_0)])^\gamma + B \tag{6}
\]

where \( \Delta \tau_{\text{eff}} = \tau_{\text{eff}} (\Phi_{\text{CEA}} = 0) \) and \( \tau_{\text{eff},0} = \tau_{\text{eff}} (\Phi_{\text{CEA}} = 0) \). The solid line is a fitting curve to eqn (6), with fitting parameters \( A = 0.03, B = 13.9, \Phi_0 = 7243 \mu\text{g ml}^{-1} \), and \( \gamma = 0.49 \).

This relationship, \( \Delta \tau_{\text{eff}}/\tau_{\text{eff,0}} \) versus \( \Phi_{\text{CEA}} \), allows the assay of an unknown amount
of CEA molecules for biosensing. Colorectal tumors, which are caused by uncontrolled cell growth in the colon or rectum, are the most commonly diagnosed cancer, especially in developed countries. Quantitative measures of CEA molecules are used as a tumor marker to monitor colorectal carcinoma treatment, to identify recurrences after surgical resection, and to stage or localize the spread of cancer. The detection sensitivity in this study can be determined from the variation of $\Delta t_{\text{eff}}/t_{\text{eff},0}$. The standard deviation of $\Delta t_{\text{eff}}/t_{\text{eff},0}$ was 0.033 as $\Phi_{\text{CEA}} = 0.001 \mu\text{g mL}^{-1}$. The estimated detection limit of 0.0037 $\mu\text{g mL}^{-1}$ was obtained by the highest value of $\Delta t_{\text{eff}}/t_{\text{eff},0}$ and transferred using a logistic function. The detection limit in our system reached the detection criteria for colorectal carcinoma diagnosis.

V. Conclusions

This study determined the relationship between time and $t_{\text{eff}}$ when a reagent that consisted of Fe3O4-anti-CEA associated with CEA molecules. Because of magnetic interactions between MNPs in magnetic clusters, which contributed extra magnetization, Néel relaxation and Brownian relaxation increased, which resulted in an increase in the value of $\tau_{\text{eff}}$. Magnetic clustering was verified using a TEM. A relationship between $\Delta t_{\text{eff}}/t_{\text{eff},0}$ and $\Phi_{\text{CEA}}$ was established, which obeyed a logistic function, allowing the assay of an unknown amount of CEA molecules. The $\chi_{\text{ac}}$ detection platform for sensing biomarkers is highly sensitive, easy to use, and can be used to assay a wide variety of analytes, such as proteins, DNA, viruses, and tumor markers.

Conflicts of interest

There are no conflicts to declare.

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References


