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The impact of lone-pair electrons on the lattice thermal conductivity of the thermoelectric compound CuSbS_2

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The discovery and design of compounds with intrinsically low thermal conductivity, especially compounds with a special bonding nature and stable crystal structure, is a new direction to broaden the scope of potential thermoelectric (TE) materials. This study revealed unambiguously the origin of the impact of the lone pair electrons on lattice thermal conductivity in Cu–Sb–S compounds by correlating the special bonding on the Sb site with the phonon dispersion spectrum and density of states. By substitution of Sb with the transition metal Fe and group III_A element Ga without s^2 electrons, lone-pair electrons on some of the Sb sites were removed, which created a scenario with opposite influences on lattice thermal conductivity from the loss of lone-pair electrons and gain of alloy scattering. We investigated the competition between the alloy phonon scattering and the extra phonon scattering mechanism linked to lone-pair electrons on trivalent Sb^{3+} sites in chalcostibite CuSbS_2 , which is a model system for benchmarking and quantifying the impact of lone-pair electrons on the lattice thermal conductivity of Cu–Sb–S compounds. A significant deviation from the classic alloy model was observed. Along with the impact of the lone-pair electrons on the bonding arrangement and crystal structure, the role of lone-pair electrons in the phonon transport of the TE compound CuSbS_2 was well demonstrated and quantified. Two Sb-related quasi-single-frequency vibration modes behaving like localised Einstein harmonic oscillators were discovered and correlated with the bonding circumstance around Sb sites. These results give unequivocal evidence that the trivalent V_A atom creates special bonding and vibration modes because of its nonbonding 5s lone-pair electrons.

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Introduction

The ability to discover and design materials with low lattice thermal conductivity is technologically important for thermoelectric (TE) generators and Peltier coolers,^{1,2} which demand TE materials with crystal-like electrical transport properties and glass-like thermal conductivity, an ideal concept (phonon glass-electron crystal, PGEC) coined by Slack.³ Several strategies have been explored over the last decade to minimize the thermal conductivity of TE materials while delicately avoiding any detrimental effects on electrical properties. Benefiting from the difference between the phonon and charge carrier mean-free paths,^{4,5} introducing a high density of grain boundaries by embedding nanoscale ‘guest domains’ or nanopores in a ‘host matrix’ is an effective way to block/scatter the movement of phonons without serious degradation of electrical conductivity. A series of record high TE figure-of-merits, zT , were achieved in $\text{AgPb}_m\text{SbTe}_{2+m}$,⁶ BiSbTe ,^{7,8} nano-microporous AgSbTe_2 (ref. 9),

skutterudites¹⁰ and other systems by this method.^{11,12} Another strategy is to use the ‘crystal complexity’ to decrease the thermal conductivity and enhance the electrical properties.¹³ Some quantitative discussion has been carried out for the complex disordered system $\text{YbB}_{44}\text{Si}_2$ (ref. 14). For layered materials, it is an effective way to optimise the TE properties by decoupling the interrelated thermal and electrical transport parameters by designing a complex crystal structure with one block exhibiting excellent electrical properties, and another block acting as a phonon scatterer to minimize the thermal transport. Layered materials, including Na–Co–O,¹⁵ TiS_2 (ref. 16) and Bi–Cu–O–Se¹⁷ are representative examples of this design strategy. Inserting/filling rattling atoms into oversized cages/voids is another proven promising method to obtain the ideal phonon-glass thermal conductivity, while still maintaining electron-crystal electrical transport properties along the crystalline frame sublattice or cages.^{18,19} The vibration of the rattler strongly couples to the frame/cage vibration modes, which lowers the velocity of the phonons and results in low thermal conductivity.^{20,21} This strategy was well demonstrated both in skutterudites and clathrates.^{22,23}

Recently, Li *et al.*²⁴ discovered the link between lattice vibration anharmonicity and electronic orbitals in SnSe^{25} and

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revived the idea of designing materials with large Grüneisen parameters by anharmonicity engineering as proposed by Händel.²⁶ Heremans²⁷ pointed out that high anharmonicity mostly occurs under conditions that are very close to a collapse of the crystal structure itself, which is verified by the unstable electrical structure and the ferroelectric-like lattice instability aroused by orbital interactions in SnSe.²⁴ Another extreme example supporting Heremans's theory is copper selenide where Se atoms form a rigid cubic lattice with superionic copper ions with liquid-like mobility around them.²⁸ The extraordinary 'liquid-like' nature of copper ions decreases the number of phonon modes and results in an intrinsically very low thermal conductivity in Cu_{2-x}Se (around or less than $1 \text{ Wm}^{-1}\text{K}^{-1}$ for Cu_2Se).^{28,29} So, the discovery and design of compounds with intrinsically low thermal conductivity is a new direction to broaden the scope of potential TE materials, especially compounds with a special bonding nature and stable crystal structure.

In 2011, Skoug and Morelli³⁰ investigated the thermal transport properties of the Cu–Sb–Se (CASE) system and found that the Cu_3SbSe_3 compound exhibits an abnormally low and nearly temperature-independent lattice thermal conductivity, whereas the structurally related Cu_3SbSe_4 does not show the same behaviour.^{31–33} They proposed that the electrostatic repulsion between the $5s^2$ orbital lone-pair electrons on the trivalent Sb atoms and neighbouring chalcogenide ions results in soft phonon modes and strong vibrational anharmonicity, which in turn arouse the ultralow thermal conductivity of Cu_3SbSe_3 compound.^{30,34} This concept has been further validated by first-principles density-functional theory calculations of several group $\text{I}_B\text{--V}_A\text{--(VI}_A)_2$ and other compounds.^{35–38} The compounds always show lattice instabilities or different structures to those of the starting rocksalt structure, which result in strong phonon–phonon interactions and ultralow thermal conductivity approaching the amorphous limit.³⁵ In fact, seminal work in 2008 reported $\text{I}_B\text{--V}_A\text{--(VI}_A)_2$ compounds with abnormally high Grüneisen parameters and soft frequency lattice vibration modes, for example AgSbTe_2 and AgBiSe_2 (ref. 34). The phonon mean free path is restricted to the interatomic distance by intrinsic normal and Umklapp phonon–phonon scattering processes alone because of the strong anharmonicity related to the special bonding arrangement. This has motivated research interest in the effect of bonding around trivalent group V_A atoms on lattice thermal conductivity in related $\text{I}_B\text{--V}_A\text{--VI}_A$ compounds, containing group I_B (Cu, Ag), group V_A (P, As, Sb, Bi), and group VI_A (S, Se, Te) elements.^{39,40} Most of the research focused on elucidating the relationship between the bonding arrangement and the low thermal conductivity by comparison of materials incorporating nominally trivalent VI_A elements with materials incorporating only V_A or III_A elements.^{30,34,41} Actually, there is another way to assess the impact of the lone-pair electrons on thermal conductivity by partly substituting the V_A atoms by III_A atoms without lone-pair electrons. First, this operation would introduce extra point defect phonon scattering and reduce the thermal conductivity based on the alloying model. Simultaneously, the substitution would break the special bonding arrangement related to the lone-pair

electrons on some of the trivalent V_A atom sites, which would likely restore the thermal conductivity to a typical value for a $\text{I}_B\text{--III}_A\text{--VI}_A$ compound. Since both effects happen on the atomic scale, it is reasonable to evaluate the role of the lone-pair electrons by analysing the doping concentration dependence of thermal conductivity as long as a system is free from the influences of any other factors.

AgSbTe_2 is a representative example of $\text{I}_B\text{--V}_A\text{--(VI}_A)_2$ group compounds, and is a well-studied system with intrinsic minimum thermal conductivity ($<0.6\text{--}0.7 \text{ Wm}^{-1}\text{K}^{-1}$).^{9,34–36,42,43} However, its 'cubic' crystal structure is still a controversial issue.³⁶ Also, the spontaneously generated nanostructure produced by a natural formation of nanoscale domains with different ordering on the cation sublattice plays some role in scattering phonons and achieving a low thermal conductivity.⁴⁴ Bismuth copper oxysulphides BiOCuQ ($\text{Q} = \text{S, Te}$) are another hot topic related to the impact of lone-pair electrons on thermal conductivity.^{45,46} Recently, first-principles calculations and *in situ* neutron diffraction analysis have suggested that the low thermal conductivity of those materials may be attributed to the weak bonding of copper atoms within the structure, rather than to the Bi^{3+} lone pairs.⁴⁷ There is a sulphide counterpart (Cu–Sb–S, CAS system) of the CASE system.³⁹ The four main crystalline phases of the CAS compounds are Cu_3SbS_4 (famatinitite),^{48,49} $\text{Cu}_3\text{SbS}_{3.25}$ (tetrahedrite, $\text{Cu}_{12}\text{Sb}_4\text{S}_{13}$),^{50–52} Cu_3SbS_3 (skinnerite),⁵³ and CuSbS_2 (chalcostibite).^{54–56} Fig. 1 shows the temperature dependence of the lattice thermal conductivity of all of the four compounds.^{41,57} Famatinitite has the highest value in nearly the whole temperature range, while tetrahedrite and skinnerite exhibit abnormally low and nearly temperature-independent lattice thermal conductivity. Fig. 2 shows the crystal structures of the members of the CAS system. The Sb atoms in famatinitite are tetrahedrally coordinated with four S atoms by sp^3 hybridisation.⁵⁸ No non-bonded Sb $5s^2$ lone-pair electrons exist, which results in a relatively high lattice thermal conductivity. In contrast, the other three compounds

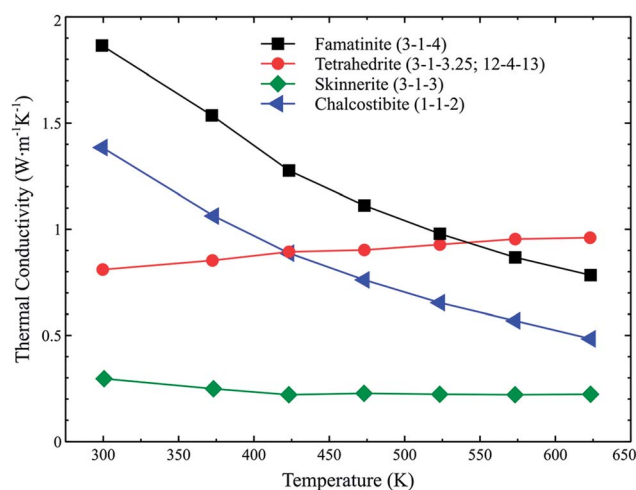


Fig. 1 Temperature dependence of the lattice thermal conductivity of copper antimony sulphide, including famatinitite, tetrahedrite, skinnerite, and chalcostibite.^{41,57}



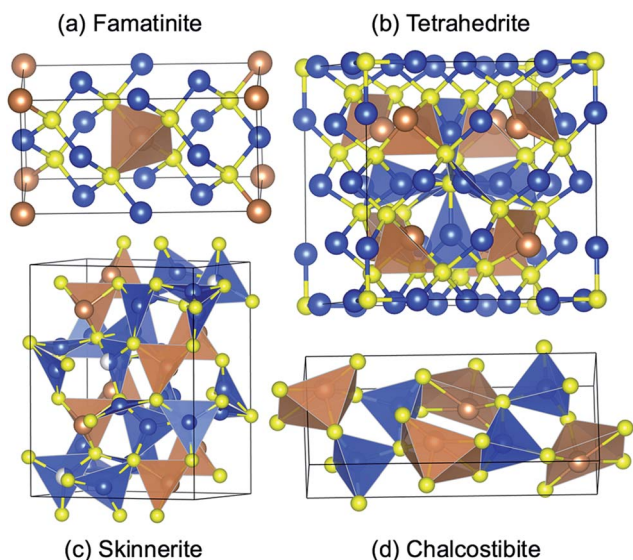


Fig. 2 Crystal structures of (a) famatinite (3-1-4), (b) tetrahedrite (3-1-3.25 or 12-4-13), (c) skinnerite (3-1-3) and (d) chalcostibite (1-1-2). The small balls represent S (yellow), medium size Cu (blue) and large ones indicate Sb atoms (brown). All the structures were created using Vesta software.

have spare Sb $5s^2$ electrons free to orient along the missing vertex of their associated polyhedron. Tetrahedrite, which does not have a counterpart in the CAsE system, forms a cubic structure, where half of the copper atoms occupy three-fold coordinated CuS_3 trigonal sites. The Sb lone-pair electrons on both sides of the CuS_3 triangular plane weaken the bonding of the Cu atoms in the direction perpendicular to the CuS_3 plane, which leads to quasi-localised and anharmonic out-of-plane rattling modes. This is likely to be the origin of the low thermal conductivity of tetrahedrite.^{30,59} There are no less than three temperature-dependent polymorphs of Cu_3SbS_3 (ref. 53). All of the structures show mixed character with lone-pair electron bonding arrangement and CuS_3 trigonal bonding units or fractionally occupied Cu sites, including the room temperature polymorph skinnerite. For similar reasons, both tetrahedrite and skinnerite are more thermally insulating than famatinite at room temperature and have nearly constant thermal conductivity with increasing temperature. So, both tetrahedrite and Cu_3SbS_3 are not ideal compounds to evaluate the effect of lone-pair electrons on thermal conductivity because of the influences of other factors. Chalcostibite forms a stable orthorhombic structure (space group $Pnma$) until its melting point.⁶⁰ It has lower thermal conductivity than famatinite but exhibits a similar trend, with intrinsic Umklapp phonon scattering dominating its thermal conductivity behaviour. All the Cu atoms are tetrahedrally coordinated in CuS_4 units. The edge-shared square pyramidal SbS_5 units are separated by CuS_4 units and face one another, which directs the lone-pair electrons into the void separating the SbS_5 units. In contrast to the co-contributions from mixed factors in tetrahedrite and skinnerite, the lone-pair electrons are the solo possible factor accounting for the low thermal conductivity in chalcostibite. So, chalcostibite is an ideal system to assess the role of lone-pair electrons free from the influences of other factors.

To clarify the importance of lone-pair electrons on trivalent Sb^{3+} sites in CuSbS_2 compound, alloy phonon scattering was purposely introduced and set up as a benchmark to quantify the impact of lone-pair electrons on thermal conductivity. By substitution of Sb with the transition metal Fe and group III_A element Ga, lone-pair electrons on a fraction of the Sb sites were removed. All of the outer shell electrons around the Fe (Ga) sites involve in the formation of sp^3 hybridisation due to the valence number difference between Sb and Fe (Ga). We expected that there would be a deviation from the alloy mode of thermal conductivity in a system with opposite influences of the loss of lone-pair electrons and gain of point defects. In this study, the competing impacts of lone-pair electrons and point defects on thermal conductivity were analysed. The doping concentration dependent thermal conductivity and phonon spectrum were also studied and correlated.

Experimental details

Two alloy systems $\text{CuFe}_x\text{Sb}_{1-x}\text{S}_2$ and $\text{CuGa}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0, 0.01, 0.025, 0.05, 0.1, 0.2, 0.9, \text{ and } 1$) were designed to remove lone-pair electrons from some of the Sb sites by incorporating the trivalent transition metal atom Fe and group III_A atom Ga in chalcostibite. Both systems were synthesised using a mechanical-alloying spark-plasma-sintering synthesis route. Pure elements Cu (150 mesh, 99.5%), Sb (100 mesh, 99.5%), S (reagent grade, purified by sublimation, 100 mesh) and Fe (200 mesh, 99+%) were used as raw materials to synthesise $\text{CuFe}_x\text{Sb}_{1-x}\text{S}_2$, while Ga_2S_3 (powder, 99.99%, metals basis) was used as the gallium source to synthesise $\text{CuGa}_x\text{Sb}_{1-x}\text{S}_2$. The powders were weighed and then sealed in stainless steel milling jars in an Ar filled glovebox. The jars were mounted and milled in a planetary mill at a rotational speed of 450 rpm for 20 h. The samples with $x \leq 0.2$ were spark plasma sintered using a graphite die in vacuum at 400°C for 5 min. For samples with $x = 0.9$ or 1, the sintering temperature was adjusted based on the melting point of CuFeS_2 (950°C) and CuGaS_2 (1236°C) to achieve dense pellets. For comparison, Cu_3SbS_3 was synthesised using the same processing method and its thermal conductivity is listed in Fig. 1 with tetrahedrite, famatinite and chalcostibite.

The constituent phases of the samples were characterized using powder X-ray diffraction (XRD, X'Pert PRO-PANalytical, $\text{CuK}\alpha$) in the range $5\text{--}120^\circ$. RAMAN spectra were obtained from powders using a RENISHAW machine equipped with a He-Ne laser source with 633 nm wavelength and optical lens of $50\times$. The error associated with RAMAN measurements was 1 cm^{-1} . The microstructure images of freshly fractured surfaces were observed using a scanning electron microscope (SEM, FEI Inspect TM-F) with energy dispersive X-ray spectroscopy (EDS). The temperature dependent electrical resistivity and Seebeck coefficient of $\text{CuFe}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0.9, \text{ and } 1$) were measured using a commercial instrument (ZEM-3, Ulvac, Inc.) in a He atmosphere. The error of resistivity and Seebeck coefficient measurements are less than 5%. Thermal conductivity κ was determined using the equation $\kappa = \lambda C_p d$. The temperature dependent thermal diffusivity λ was measured using a laser flash method (LFA-457, Netzsch) on a pellet (ϕ 12.7 mm, height



1.5 mm). The machine was calibrated using a standard specimen within the same temperature range. The repeatability of the measurement was better than 2%, while the error of the thermal diffusivity was less than 5%. The specific heat C_p was calculated using the Dulong–Petit law to avoid the large uncertainty in the routine differential scanning calorimetry method. The density d was obtained using the mass and volume of the sintered pellets with an error less than 1%.

Computational details

First principles calculations were performed using the Quantum-ESPRESSO package.⁶¹ We used the Garrity–Bennett–Rabe–Vanderbilt (GBRV) high-throughput pseudopotential library.⁶² The Perdew–Burke–Ernzerhof (PBE) function was used along with ultrasoft pseudopotentials for all the atoms. A plane wave basis with kinetic energy cut off of at 500 eV and a dense k -point sampling of $7 \times 11 \times 3$ were used to ensure the convergence in all of the calculations. The atomic positions were relaxed until all the force components on each atom were less than 10^{-3} a.u., and the lattice constants were optimized until the stress was less than 0.5 kbar. The phonon dispersions and partial phonon density of states were calculated using the density perturbation functional theory (DPFT) and Quasi-Harmonic Approximation (QHA) package, both implemented in Quantum-ESPRESSO.

Results and discussion

According to the literature and the above structural analysis, the lone-pair electrons are probably the solo decisive factor in determining the ultralow thermal conductivity of single crystal chalcostibite. To discuss the competing impacts of the loss of lone-pair electrons and the gain of point defects in the substituted polycrystalline samples, we need to separate their

effect from other influences, such as phase structure and microstructure.

Phase structure

Fig. 3 shows the X-ray diffraction spectra of (a) $\text{CuGa}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0, 0.01, 0.025, 0.05, 0.1, 0.2, 0.9, \text{ and } 1$) and (b) $\text{CuFe}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0, 0.01, 0.025, 0.05, 0.1, 0.2, 0.9, \text{ and } 1$). The two bottom traces were generated based on the crystal structures of pure CuSbS_2 and $\text{CuGaS}_2/\text{CuFeS}_2$. For both the Fe and Ga substituted samples, the samples are divided into two groups based on the crystal structure. Samples with x up to 0.2 crystallise with the chalcostibite structure without any trace of impurity. Samples with $x = 0.9$ and 1 are phase-pure materials with a chalcopyrite structure (cation ordered structure based on zinc blende) for both Ga and Fe substituted samples. This confirmed that it is possible to maintain the structure of chalcostibite even when 20% of the lone-pair electrons are removed from the trivalent Sb sites. Based on the principle of minimum energy, the Fe/Ga atoms should be randomly distributed on the Sb sites of chalcostibite, which in turn restrains the formation of a secondary phase. However, the chalcostibite structure collapses without the support from the lone-pair electrons in the voids separating the SbS_3 units in samples with a specific value of x between 0.2 and 0.9. The phases of CuFeS_2 and CuGaS_2 with the chalcopyrite structure then form with tetrahedral coordination geometry similar to famatinite.

Raman spectroscopy analysis

To clarify the effect of Ga doping on the structure, the Raman-active modes were investigated at ambient temperature for CuSbS_2 , $\text{CuGa}_{0.025}\text{Sb}_{0.975}\text{S}_2$ and CuGaS_2 (Fig. 4). The CuSbS_2 sample has three pronounced peaks at about 187, 250 and 329 cm^{-1} , along with a much weaker peak at about 450 cm^{-1} , which is in agreement with data reported in the literature.⁶³ The broad peak at 329 cm^{-1} includes two adjoining modes with A_g symmetry, which are assigned to the vibration modes from the

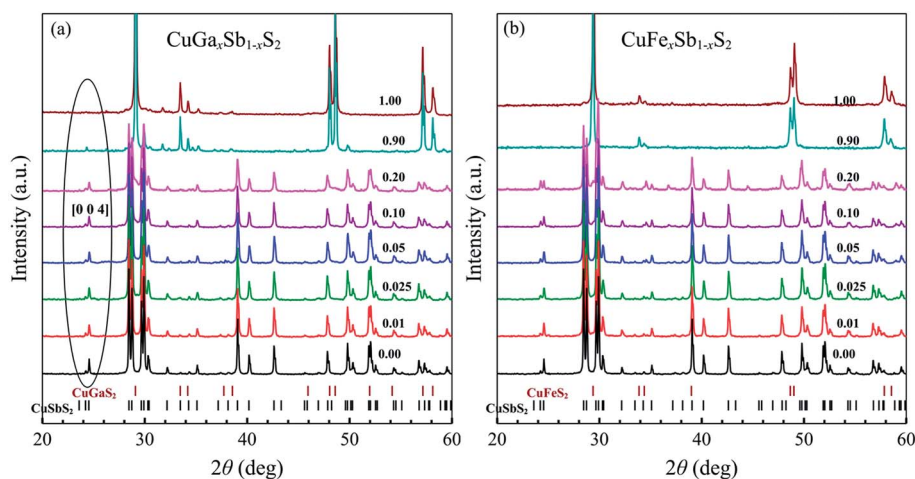


Fig. 3 X-ray diffraction spectra of (a) $\text{CuGa}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0, 0.01, 0.025, 0.05, 0.1, 0.2, 0.9, \text{ and } 1$) and (b) $\text{CuFe}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0, 0.01, 0.025, 0.05, 0.1, 0.2, 0.9, \text{ and } 1$). The peaks related to the [0 0 4] plane are labeled in (a). The two bottom traces were generated for pure CuSbS_2 and $\text{CuGaS}_2/\text{CuFeS}_2$. The samples are categorized into two groups based on the crystal structure in both Ga and Fe doped systems.



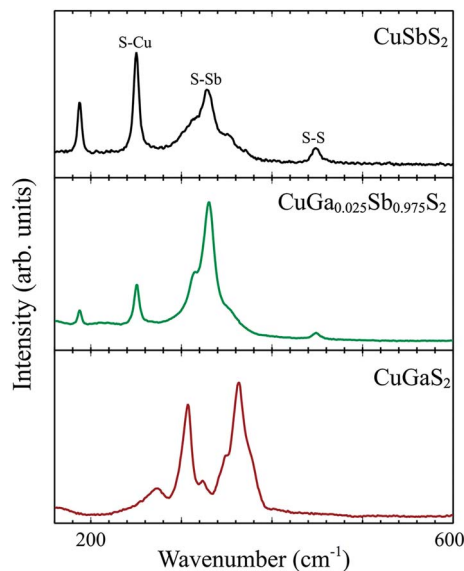


Fig. 4 Raman spectra of (a) CuSbS_2 , (b) $\text{CuGa}_{0.025}\text{Sb}_{0.975}\text{S}_2$ and (c) CuGaS_2 samples.

Sb–S bonds. Peaks at 250 and 450 cm^{-1} are attributed to the vibration of Cu–S and S–S bonds, respectively. Compared to CuSbS_2 , the peak positions of $\text{CuGa}_{0.025}\text{Sb}_{0.975}\text{S}_2$ are not shifted, but there is a significant change in the relative peak intensities. This probably means that 2.5 mol% of Ga doping shifts the orientation of the Sb–S bonds, which also manifested itself in the XRD pattern. As shown in Fig. 3(a), the intensity of the [0 0 4] peak at 24.5° (2θ) decreases with increasing Ga substitution. In pristine CuSbS_2 , two S atoms of the bottom face of one pyramidal CuS_5 and the top S atom of the opposite CuS_5 unit form the [0 0 4] atomic plane. Any doping on the Sb sites with atoms without lone-pair electrons causes a delicate reconstruction of the CuS_5 unit, which leaves a ragged [0 0 4] lattice plane, which in turn decreases the XRD intensity from the plane. In moving from CuSbS_2 to CuGaS_2 , the peak at 329 cm^{-1} disappears completely and an intense peak at 307 cm^{-1} emerges due to the A_1 vibrational mode in the chalcopyrite structure. The above discussion showed that the special bonding circumstance on Sb sites in chalcostibite plays an important role in determining its crystal structure.

Microstructure

Fig. 5 shows the typical SEM images of the $\text{Cu}(\text{Fe}/\text{Ga})_x\text{Sb}_{1-x}\text{S}_2$ samples. All samples are free of pores and have relative densities between 98% and 99%. Due to the different crystalline structures and sintering temperatures, samples with x up to 0.2 have very fine grain size ranging from 100 to 300 nm as shown in Fig. 5(a), while samples with the chalcopyrite structure ($x = 0.9$ and 1) have coarse grains between 1 and 4 μm as shown in Fig. 5(b). According to the phase structure and microstructure, we separated the samples into two categories. One is the samples with x up to 0.2 sharing the chalcostibite structure and fine average grain size, the other is the samples with $x = 0.9$ and 1 with tetrahedral coordination geometry and coarse grains.

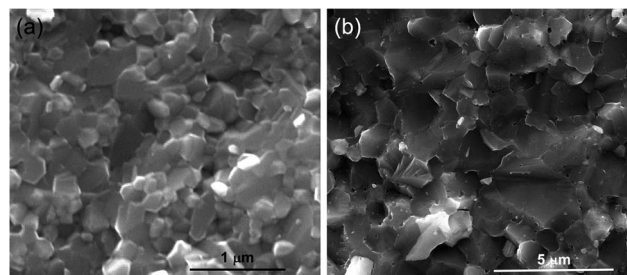


Fig. 5 Typical SEM images of bulk $\text{Cu}(\text{Fe}/\text{Ga})_x\text{Sb}_{1-x}\text{S}_2$ samples with (a) x up to 0.2 and (b) $x = 0.9$ or 1.

This classification made it possible to put aside the influences of phase and microstructure on thermal conductivity in the following discussion.

Thermal conductivity and TE properties of the $\text{CuFe}_x\text{Sb}_{1-x}\text{S}_2$ system

Fig. 6 shows the temperature dependence of thermal conductivity κ for $\text{CuFe}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0, 0.01, 0.025, 0.05, 0.1, 0.2, 0.9$, and 1). The sample category with x up to 0.2 possesses much lower thermal conductivity than the other category with $x = 0.9$ and 1. The thermal conductivities decrease with increasing temperature for all of the samples, which indicates that Umklapp phonon scattering prevails in the testing temperature range. No apparent ambipolar transport phenomenon was observed. The overall thermal conductivity is the sum of two nearly independent terms $\kappa = \kappa_{\text{latt}} + \kappa_{\text{carr}}$, where κ_{latt} and κ_{carr} are the lattice and carrier contributions, respectively. The carrier term is related to the electrical resistivity ρ via the Wiedemann–Franz law, $\kappa_{\text{carr}} = LT/\rho$, where L is the Lorentz constant, which is $2.45 \times 10^{-8} \text{V}^2 \text{K}^{-2}$ for a fully degenerate semiconductor.⁶⁴ The high resistivity of the samples with x up to 0.2 means that their carrier thermal conductivity accounts for less than 0.1% of their overall thermal conductivity. However, the carrier contributions

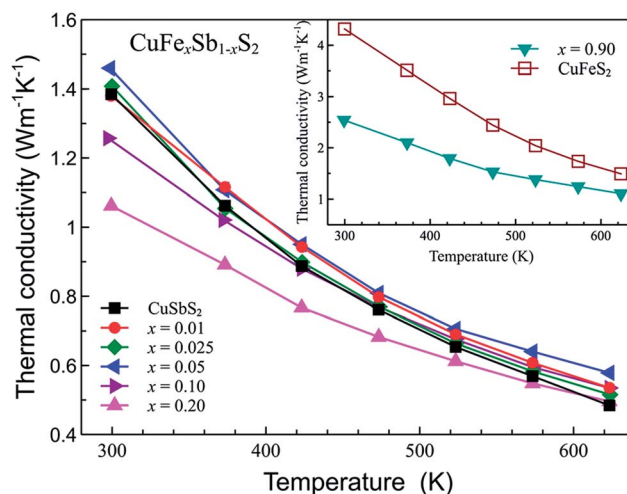


Fig. 6 Temperature dependence of thermal conductivity of $\text{CuFe}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0, 0.01, 0.025, 0.05, 0.1, 0.2, 0.9$, and 1).



in $\text{CuFe}_{0.9}\text{Sb}_{0.1}\text{S}_2$ and CuFeS_2 are not negligible, and were calculated using the Wiedemann–Franz law. Fig. 7 displays the resistivity, Seebeck coefficient, lattice/carrier thermal conductivity and figure-of-merit of the $\text{CuFe}_{0.9}\text{Sb}_{0.1}\text{S}_2$ and CuFeS_2 samples. Both samples have rather high Seebeck coefficient and moderate resistivity and thermal conductivity. A figure-of-merit zT of 0.19 was obtained for the $\text{CuFe}_{0.9}\text{Sb}_{0.1}\text{S}_2$ sample. This value is comparable to values reported in the literature,^{65,66} which demonstrates that n-type CuFeS_2 is a good candidate to work with the *p*-type members of the CAS system in TE generators in the intermediate temperature range.

Lattice thermal conductivity

Fig. 8 displays the temperature dependence of lattice thermal conductivity for (a) $\text{CuFe}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0, 0.01, 0.025, 0.05, 0.1, 0.2, 0.9, \text{ and } 1$) and (b) $\text{CuGa}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0, 0.01, 0.025, 0.05, 0.1, 0.2, 0.9 \text{ and } 1$). The carrier thermal conductivity for all of the Ga substituted samples is negligible, including the CuGaS_2 sample due to their high resistivity.⁶⁷ So, we regarded the total thermal conductivity of all the Ga substituted samples as their lattice thermal conductivity in the following discussion. The $\text{CuGa}_x\text{Sb}_{1-x}\text{S}_2$ system is also divided into two categories based on their crystal structure and microstructure, as was done for the $\text{CuFe}_x\text{Sb}_{1-x}\text{S}_2$ system. Excluding the $x = 0.9$ and 1 samples with different crystal structures, the thermal conductivities initially increase slightly, reach a maximum, and then decrease with the increasing substitution in both systems. This trend apparently contradicts with the alloying model. In conventional solid solutions or alloys, point defect phonon scattering is one of the dominant factors in reducing the lattice thermal conductivity because of mass contrast, charge fluctuation, local

strain and other accompanying changes around the foreign atoms. Historically, alloying is the cornerstone for the design of the most commercial room temperature TE materials (bismuth chalcogenide solid solutions)⁶⁸ and high temperature materials (SiGe).⁶⁹ To illustrate the results more clearly, the lattice thermal conductivities are re-plotted against substitution concentration at chosen temperatures, 300, 373 and 600 K in Fig. 9. A 5% error bar was used for each point. In both Fe and Ga substituted systems and at all temperatures, the lattice thermal conductivity increases in the lightly doped samples. Taking into account the special bonding arrangements and the electron density distribution around the trivalent Sb sites in chalcostibite, the abnormal lattice thermal conductivity increment in lightly doped samples is naturally connected to the $5s^2$ lone-pair electrons. To quantify the impact of the lone-pair electrons on lattice thermal conductivity, the modelled lattice thermal conductivities based on an alloy model are also plotted in Fig. 9. According to Klemens and Abeles's model,^{70,71} the lattice thermal conductivity κ of a disordered alloy can be calculated from the κ_p value in the absence of point defects (pure CuSbS_2 in this work),

$$\frac{\kappa}{\kappa_p} = \left[1 + \frac{5}{9}a \right]^{-1} \times \left[\frac{\tan^{-1} U}{U} + \frac{(1 - (\tan^{-1} U/U))^2}{[(1+a)/5a]U^4 - \frac{1}{3}U^2 + 1 - (\tan^{-1} U/U)} \right],$$

where a is the ratio of the relaxation times of three-phonon normal and Umklapp process, and U is calculated by the equation

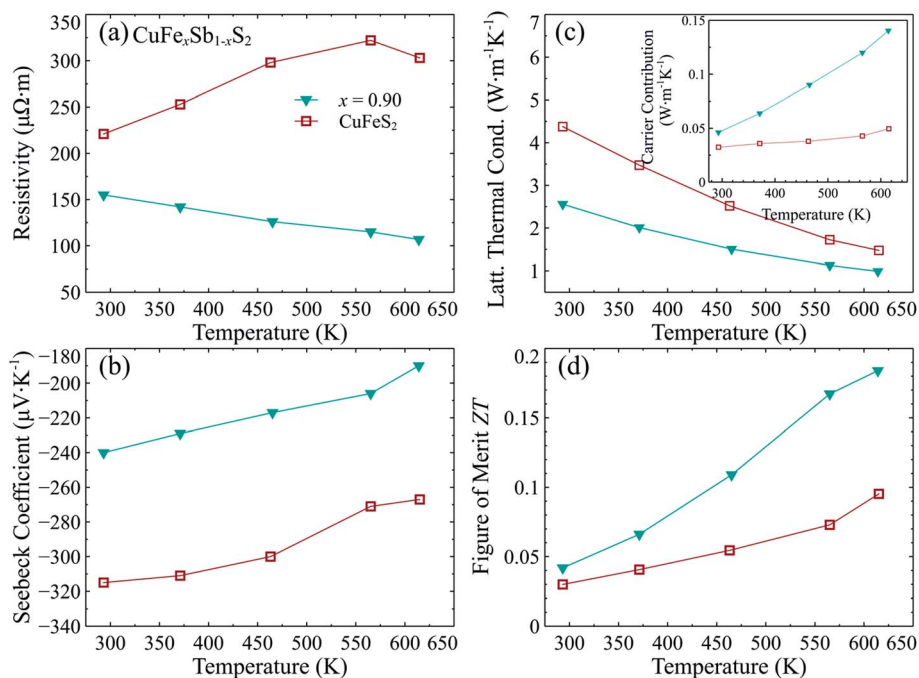


Fig. 7 Electrical, thermal transport properties, and figure-of-merit zT of $\text{CuFe}_{0.9}\text{Sb}_{0.1}\text{S}_2$ and CuFeS_2 samples.



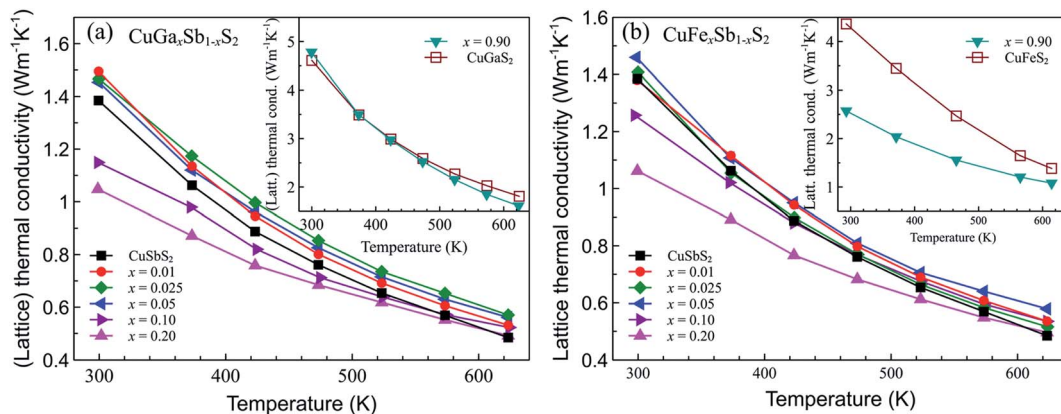


Fig. 8 Temperature dependence of lattice thermal conductivity of (a) $\text{CuGa}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0, 0.01, 0.025, 0.05, 0.1, 0.2, 0.9$, and 1) and (b) $\text{CuFe}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0, 0.01, 0.025, 0.05, 0.1, 0.2, 0.9$ and 1).

$$U = 8.69 \times 10^6 \left(1 + \frac{5}{9}a\right)^{1/2} \gamma^{-1} \beta \Gamma^{1/2} \delta^{-1/2} T^{-1/2}.$$

β is nearly a constant within a given covalent crystal system. Γ is a function of the strain parameter ε and other known basic alloy parameters. δ^3 is the atomic volume derived from Vegard's law. So, there are three adjustable parameters, the ratio of normal and Umklapp scattering rate a , the anharmonicity parameter γ , and the strain parameter ε , to estimate the thermal conductivities of alloys. As shown in Fig. 9, the discrepancy between the model values and the experimental data highlights the significance of the lone-pair electrons in chalcostibite. In alloy or solid solution, the lattice thermal conductivity is quite sensitive to the point defects due to its effective scattering of short and medium-wavelength heat-carrying phonons. However, the lattice thermal conductivity witnesses an increase rather than a decrease in lightly Fe and Ga doped chalcostibite. This suggests that the influence of the loss of lone-pair electrons outweighs the impact of point defects in lightly doped samples. With further increase in doping, the effect of phonon scattering

by point defects becomes more dominant in the trend of the lattice thermal conductivity. This trend also manifested itself at 373 K and 600 K, which indicates that lone-pair electrons play an important role in thermal transport properties both at low and high temperature. Taking into account the origins of point defects scattering and lone-pair electrons, both mechanisms are closely related to the bonding properties at the atomic scale. So both phonon scattering mechanisms should have a similar working temperature range and compete with each other in the whole temperature range. Actually, the lattice thermal conductivity is controlled by the competition between the opposite effects of point defects and the loss of lone-pair electrons on Sb sites. This is the first direct demonstration of the role of lone-pair electrons in comparison with another well-known scattering mechanism. It demonstrates that lone-pair electrons provide a strong mechanism to transform phonon transport and may eclipse point defects in lightly doped solid solution/alloys. This suggests that compounds with lone-pair electrons (trivalent V_A atoms) provide a new direction to design low thermal conductivity materials, and can be used to screen for prospective TE materials.

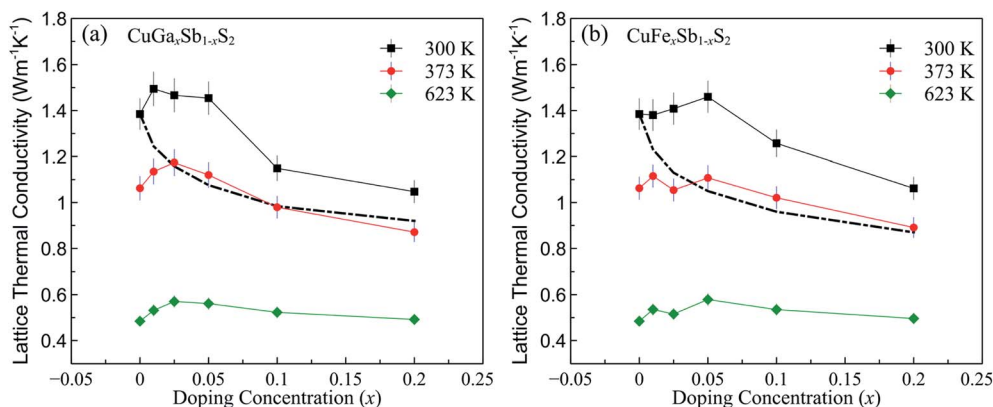


Fig. 9 Lattice thermal conductivity of (a) $\text{CuGa}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0, 0.01, 0.025, 0.05, 0.1, 0.2, 0.9$, and 1) and (b) $\text{CuFe}_x\text{Sb}_{1-x}\text{S}_2$ ($x = 0, 0.01, 0.025, 0.05, 0.1$, and 0.2) at 300 K, 373 K and 600 K. The dashed lines show the calculated lattice thermal conductivity of $\text{CuGa}_x\text{Sb}_{1-x}\text{S}_2$ and $\text{CuFe}_x\text{Sb}_{1-x}\text{S}_2$ based on the alloy model.^{70,71}



Phonon band structure and density of states

To illustrate the mechanism of the effect of lone-pair electrons on thermal transport properties, the phonon spectra of CuSbS₂ and CuGaS₂ were calculated (Fig. 10). Although the chalcostibite structure has been reported for CuSbS₂ at room temperature, the negative phonon frequencies indicate that this structure is unstable at 0 K, at which the first principles calculations were performed. The eigen-displacements of the negative modes (soft modes) will lead to phase transition at low temperatures, known as 'soft mode hardening'. In the following discussions, the phonon dispersion of the CuSbS₂ chalcostibite structure will be used because the discussions focus on the lattice thermal conductivity above room temperature. Besides, most of the optical modes and the three acoustic modes are unaffected by the soft modes and have positive values.

Due to the high symmetry of the chalcopyrite structure, CuGaS₂ has much fewer optical modes than CuSbS₂. Most of the optical modes exhibit frequencies higher than 125 cm⁻¹, except two modes at 92 and 94 cm⁻¹. Compared to its Ga counterpart, the most obvious feature of CuSbS₂ is that the frequencies of the optical modes are very low, although an underestimation of the frequencies may be possible because of the band-gap problem in generalized gradient approximation (GGA). In fact, most of the optical modes are located in a narrow low frequency range of 20–80 cm⁻¹, which is similar to AgSbTe₂. Ye *et al.* linked the softness of those modes to the heavy atomic masses, the relatively weak bonds between Te and Sb, and the large anion-cation distances.³⁶ In chalcostibite, the Sb5s² electrons orienting toward the voids between the SbS₃ units are nonbonding, which may lead to a softening of the optical modes. The small gap between the optical modes and acoustic modes suggests that the energy transfer between those modes is very likely and easy. As a result, the softening optic modes must have a strong scattering effect on the heat-carrying acoustic modes, which may be the mechanism of the ultralow lattice thermal conductivity in chalcostibite.

Fig. 11 shows the calculated total and partial phonon density of states (DOS) of (a) CuSbS₂ and (b) CuGaS₂. The peaks of the DOS shift toward higher frequency in CuGaS₂ because of the lower mass of Ga compared with Sb. In fact, most of the

modes with frequency higher than 160 cm⁻¹ in CuSbS₂ (275 cm⁻¹ in CuGaS₂) are only connected to the S and Cu bonds, while the Sb bonds contribute to the peaks below 153 cm⁻¹ in chalcostibite (Ga below 236 cm⁻¹ in CuGaS₂). To elaborate the difference between the two materials, the details of the phonon DOS between 20 and 150 cm⁻¹ are highlighted in Fig. 11(c) and (d). In CuGaS₂, there is only one Ga-related broad peak at around 90 cm⁻¹. There are no significant contributions from Ga out of the range of 70–105 cm⁻¹. In sharp contrast to CuGaS₂, there are three apparent Sb related peaks at 82, 111 and 138 cm⁻¹ for CuSbS₂. Except for the peak at around 111 cm⁻¹ showing a broad shoulder similar to that observed in Ga substituted CuGaS₂, the other two peaks are very sharp and show nearly no shoulders on the high frequency side. This is the characteristic of quasi-single-frequency Einstein modes created by the individual 'rattling' of the guest atoms in skutterudites and clathrates.^{21,72} In CuSbS₂, the phonon structure is well defined and can be understood in terms of the ideal crystal. No glass-like behaviour was observed. However, the two Sb-related quasi-single-frequency vibration modes behave like localised Einstein harmonic oscillators and qualitatively modified the whole vibration spectrum.⁷³ These results give unequivocal evidence that the trivalent V_A atom creates special bonding and vibration modes because of its nonbonding 5s lone-pair electrons. Combined with the crystal structure shown in Fig. 2(d), we conjecture that quasi-single-frequency modes may be related to the Sb vibration in a direction perpendicular to the SbS₄ plane of the pyramidal SbS₅ unit. Due to the asymmetric bonding, Sb atoms are free to undergo large displacement or shift toward the voids separating the SbS₅ units, while the movement toward the vertex is restrained by the opposing S atoms. Moreover, the non-bonding 5s² electrons are expected to form a shell of relatively large radius, especially in the direction toward the voids. During the thermal vibration, the wave functions of lone-pair electrons overlap with each other, which leads to an additional repulsive force to the restoring force that in turn leads to extreme anharmonicity of the lattice vibrational spectrum.³⁴ This is likely to be the origin of the ultralow lattice thermal conductivity in systems with lone-pair electrons.

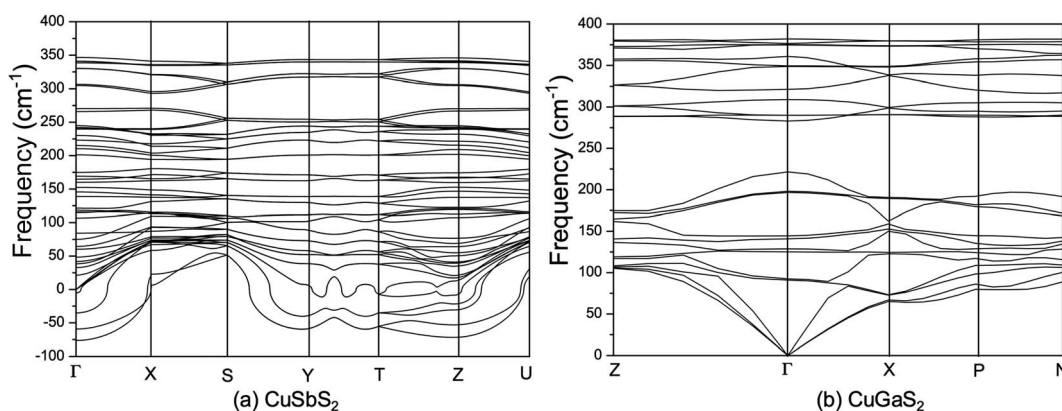


Fig. 10 The phonon dispersions of (a) CuSbS₂ and (d) CuGaS₂ compounds.



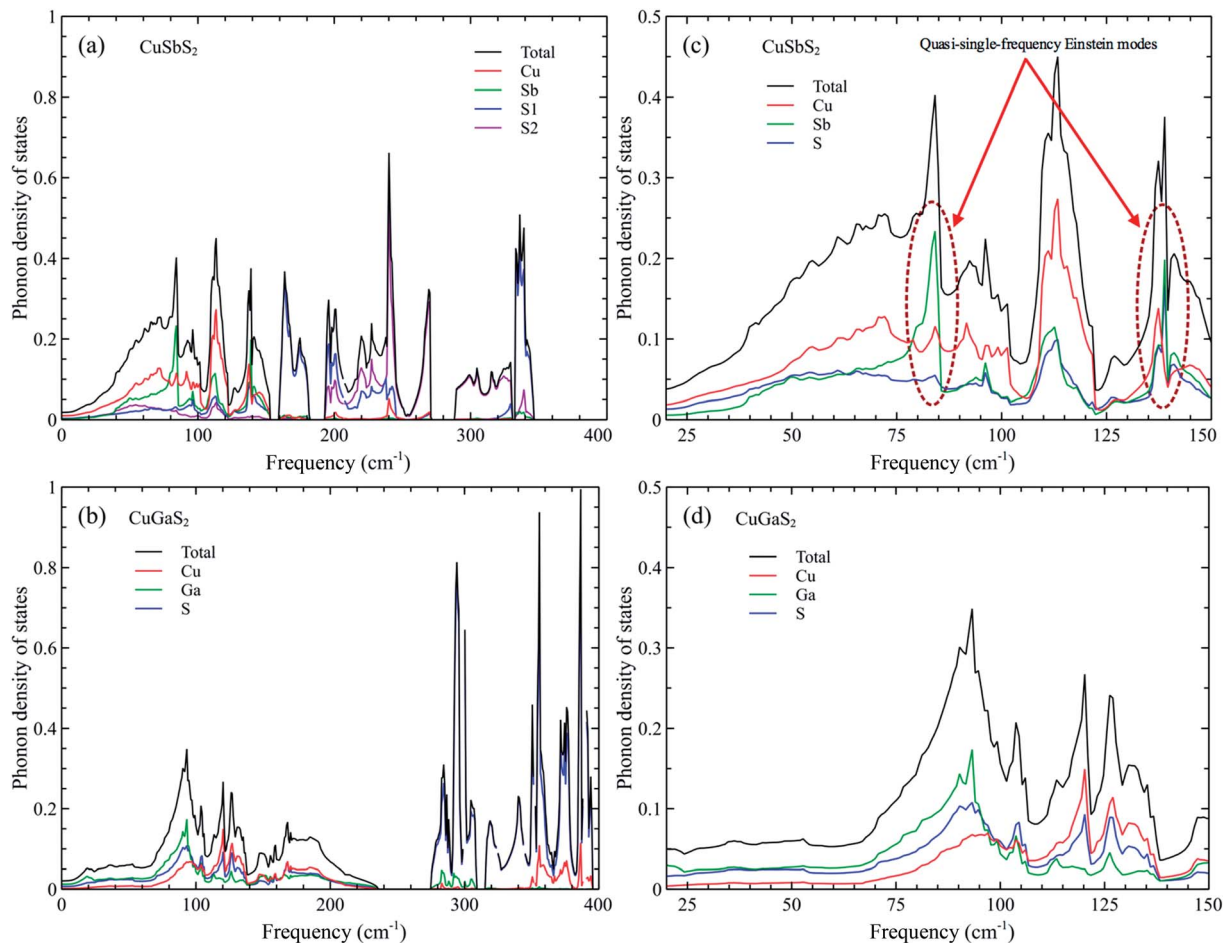


Fig. 11 Calculated total and partial phonon density of states (DOS) with appropriate scaling of (a, c) CuSb_2 and (b, d) CuGaS_2 . Two quasi-single-frequency Einstein modes created by lone-pair electrons on Sb site are labelled in (c).

Conclusions

To clarify the importance of lone-pair electrons on trivalent Sb^{3+} sites in Cu–Sb–S systems, we purposely introduced alloy phonon scattering in the carefully chosen chalcostibite CuSb_2 and used it as a benchmark to quantify the impact of lone-pair electrons on thermal transport properties. The thermal conductivity measurements show an apparent deviation from the conventional alloy model. Most impressively, the role of lone-pair electrons eclipses point defects in lightly doped solid solutions, which gives the first direct demonstration of the importance of the lone-pair electrons by comparison with another well-known scattering mechanism. Phonon dispersion calculations disclosed two Sb related quasi-single-frequency vibration modes behaving like localised Einstein harmonic oscillators, similar to the modes created by the individual ‘rattling’ of the guest atoms in skutterudites and clathrates. Combined with the crystal structure evolution with increasing substitution, we conjecture that quasi-single-frequency modes may be related to the Sb vibration in a direction perpendicular to the SbS_4 plane of the pyramidal SbS_5 unit. Due to the asymmetric bonding, the wave functions of lone-pair electrons in the voids overlap with each other during thermal vibration, which leads to an additional

repulsive force on the restoring force, which leads to extreme anharmonicity of the lattice vibrational spectrum and ultralow lattice thermal conductivity in chalcostibite. This suggests that compounds with lone-pair electrons (trivalent V_A atoms) are a new direction to design low thermal conductivity materials.

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