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Auxeticity enhancement due to size polydispersity in fcc crystals of hard-core repulsive Yukawa particles†

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The Poisson's ratio of the fcc hard-core repulsive Yukawa crystals with size polydispersity was determined by Monte Carlo simulations in the isothermal–isobaric ensemble. The effect of size polydispersity on the auxetic properties of Yukawa crystals has been studied. It has been found that an increase of particle size polydispersity causes a decrease of the Poisson's ratio in auxetic directions as well as appearance of a negative Poisson's ratio in formerly non-auxetic directions. A measure of auxeticity was introduced to estimate quantitatively an enhancement of auxetic properties in polydisperse Yukawa crystals. The proposed measure of auxeticity can be applied to appraise the auxeticity of any studied system. PAPER
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1 Introduction

Interest in colloidal crystals¹ comes from their potential applications in optoelectronics, 2 photonics, 3 and medicine. 4 In order to obtain materials with desired physical properties, studies are made on colloids composed of both spherically symmetric and more complex molecules like dumbbells^{5,6} and further on mixtures of spherical and cylindrical molecules.⁷ Electric or magnetic fields are also used to control the selfassembly of colloidal crystals, $8,9$ as well as to obtain desired structures $10,11$ through the changes of molecular orientation. The electric field can also impact the optical properties of colloids composed from spherically symmetric particles.¹² In the case of spherical particles, a large difference in the elastic properties of face-centered-cubic (fcc) and hexagonal-closepacked hard-sphere crystals was also found.¹³ The latter model molecule (hard sphere) is important for colloids and is the limiting case of Yukawa particles. Spherical particles with hardcore repulsive Yukawa interaction form body-centered-cubic or face-centred-cubic crystals depending on the Debye screening length and the volume fraction, which have been observed in experiments¹⁴ and computer simulations.^{15,16} Recently it has been shown that such fcc Yukawa crystals exhibit interesting elastic properties.17 Namely, in these crystals a negative Poisson's ratio in one of the main crystallographic directions is observed.

Systems exhibiting unusual elastic properties such as negative compressibility,¹⁸ negative Poisson's ratio¹⁹ (known as auxetics²⁰),

or both these properties²¹ have attracted increasing attention²²⁻⁴⁸ over the past few decades due to their potential applications. Poisson's ratio is defined as the negative ratio of the relative change in the transverse dimension to the relative change in the longitudinal dimension when infinitesimal change of the longitudinal strain is applied. Its value for isotropic materials ranges from -1 (so called ideal auxetic) through 0 (e.g. cork) up to 1/2 (e.g. rubber). In the case of materials that exhibit anisotropy of elastic properties, the value of Poisson's ratio depends on both the direction in which the deformation is applied and the direction in which the response of the system is studied. It has been shown that most metals (with a cubic crystallographic structure) exhibit negative Poisson's ratio in some directions 49 – they are called partial auxetics.⁵⁰ A number of man-made materials also exhibit negative Poisson's ratio, e.g. polyurethane foams, 19 composites, 51 and other structures based on the rotating rigid units model.⁵²

Studies of two-dimensional Yukawa crystals revealed that this system is not auxetic.⁵³ However, as mentioned before, the three-dimensional Yukawa crystals exhibit negative Poisson's ratio in the $[110][1\overline{1}0]$ -direction and are partial auxetics, supposedly with a similar mechanism of partial auxeticity as discussed for fcc crystals by Milstein and Huang 54 and as found in the hard sphere model near melting⁵⁵ and near close packing⁵⁶ and as reported by Baughman *et al.* for some fcc metals.⁴⁹ Moreover, the value of Poisson's ratio can be modified by changing the screening length – an increase of the screening length causes Poisson's ratio to decrease.¹⁷ Furthermore, very recently, other possibilities to control Poisson's ratio in Yukawa systems have been proposed. It has been shown that structural modifications of Yukawa crystals (by introducing nano-slits or nano-channels) decrease

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the value of the Poisson's ratio in known auxetic directions⁵⁷ or even induce completely new auxetic directions in the studied crystal.58

On the other hand, it is known that the particle size polydispersity, manifested by different diameters of particles in the system, is one of the characteristic features of colloidal systems. The particle size polydispersity is associated with the synthesis of colloidal particles and has a key impact on the thermodynamic properties of hard-particle systems.59,60 The influence of polydispersity on the elastic properties of systems with both hard⁶¹ and soft (inverse power)⁶² interaction potentials was investigated. It has been shown that polydispersity significantly influences the phase diagram of Yukawa systems by shifting the phase transition towards higher packing fractions with increasing size polydispersity. $63,64$ Paper

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The main aim of this work is to study the influence of particle size polydispersity on the auxetic properties of Yukawa crystals, which combine the hard and soft interactions.

2 Model and method

We modeled the system of N particles forming a face centred cubic lattice under periodic boundary conditions, where particles exhibit dispersion of size, *i.e.* their diameters are not identical. It is known from experiments that in real colloidal systems the distribution of particle diameters can be described approximately by Gaussian or log-normal distribution.⁶⁵ In this study, we used the Gaussian distribution of diameters of particles, as in previous works. $60,61$ The parameter that describes the polydispersity of particles in the studied system is defined $as⁶⁰$ $\delta = \langle \sigma \rangle^{-1} \sqrt{\langle \sigma^2 \rangle - \langle \sigma \rangle^2}$. The particles in the system interact through the hard-core repulsive Yukawa potential^{15,16} in which the polydispersity has been included: $63,64$

$$
\beta u(r) = \begin{cases} \infty, & r < \sigma', \\ \beta \varepsilon \frac{\sigma_i \sigma_j}{\bar{\sigma} r} \exp[-\kappa(r - \sigma')], & r \ge \sigma', \end{cases}
$$
 (1)

where $\beta = 1/(k_B T)$, T is the temperature, k_B is the Boltzmann constant, ε is the contact potential, κ is the inverse screening length, σ_i and σ_j are the diameters of interacting particles, $\sigma' = (\sigma_i + \sigma_j)/2$, and $\bar{\sigma}$ is the typical particle diameter in the system. In this work the polydispersity varied between 0 and 0.08. For these values, according to the phase diagram obtained by Dijkstra et al.,^{63,64} the fcc structure is observed in a wide range of dimensionless parameters of Yukawa potential ($\beta \varepsilon$, $\kappa \sigma$).

The elastic properties of the systems have been determined using Monte Carlo simulations in the isothermal–isobaric ensemble by averaging strain tensor fluctuations based on the idea of Parrinello and Rahman $66-68$ (more details in the work by Wojciechowski et al.⁶⁹ and ESI[†]). In this approach, the components of the tensor of elastic compliances are calculated as follows: $S_{ijkl} = \beta V_p \langle \Delta \varepsilon_{ij} \Delta \varepsilon_{kl} \rangle$, where V_p is the average volume of the system under pressure p and $\Delta \varepsilon_{ij}$ = ε_{ij} – $\langle \varepsilon_{ij} \rangle$. In the following, we will use matrix notation in Voigt's form instead of tensor notation.⁷⁰ In the case of cubic symmetry we have only

three independent elements of elastic compliance tensor S. A knowledge of the elastic compliances (S_{11}, S_{12}, S_{44}) allows one to calculate the Poisson's ratio in any crystallographic direction:

$$
\nu_{\hat{\mathbf{n}}(\theta,\phi)}(\alpha)
$$
\n
$$
= -\{\sin(\theta)\left(16S_{12}\csc(\theta)\sin^{2}(\alpha) + \cos^{2}(\alpha)\csc(\theta)(2S_{11} + 14S_{12} - S_{44} - (2S_{11} - 2S_{12} - S_{44})(\cos(4\phi) + 2\cos(2\theta)\sin^{2}(2\phi))\right)
$$
\n
$$
+ (2S_{11} - 2S_{12} - S_{44})(\left(14 + 2\cos(4\phi)\right)\cos^{2}(\theta) \cdot \sin^{2}(\alpha)\sin(\theta) + \sin(2\alpha)\sin(4\phi)\sin(2\theta))\} / \{2(8S_{11}\cos^{4}(\theta) + (6S_{11} + 2S_{12} + S_{44} + (2S_{11} - 2S_{12} - S_{44})\cos(4\phi))\sin^{4}(\theta) + 2(2S_{12} + S_{44})\sin^{2}(2\theta)\} \}. (2)
$$

In the above equation, $\hat{\mathbf{n}}(\theta, \phi)$ is the versor (in polar coordinates) representing the direction of applied stress, whereas α is an angle in the plane perpendicular to $\hat{\mathbf{n}}$, which indicates the direction of measurement of Poisson's ratio (for details see ESI†). All other details of simulations are summarised in the ESI.†

3 Results and discussion

In order to estimate the size effect of Poisson's ratio, the latter has been determined in the thermodynamic limit $(N \to \infty)$ for a monodisperse system and two polydisperse systems with δ = 0.02 and δ = 0.05. The obtained results are shown in Fig. 1. Based on the data presented, one can conclude that the Poisson's ratio for a system consisting of $N = 256$ differs from its value in the thermodynamic limit by about 3%. Similar conclusions regarding the methodology used can also be found in the literature.57,69,71 Therefore, majority of studies in this paper have been performed for systems consisting of 256 particles.

Previous studies of the elastic properties of monodisperse hard-core repulsive Yukawa crystals in a wide range of pressures and densities have shown that Poisson's ratio depends weakly on density at a constant value of the contact potential but is sensitive to changes in the screening length.¹⁷ So, because this research is about the impact of particle polydispersity on the auxetic properties of the system, here we studied the Poisson's ratio of Yukawa crystals at $p^* = 60$. At this pressure the Yukawa system has a face centred cubic structure over a wide range of screening length (6.7 $\leq \kappa \sigma \leq 16.7$) and contact potential $(20 \le \beta \varepsilon \le 81).^{63,64}$

The effect of polydispersity on Poisson's ratio in the auxetic crystallographic direction of $[110][1\bar{1}0]$ is shown in Fig. 2 (for other directions and the effect of temperature on auxeticity see ESI†). We observe here a decrease in the Poisson's ratio with increasing polydispersity for all investigated crystals over a wide range of Yukawa parameters (contact potential and screening length). As mentioned above, in anisotropic systems, the Poisson's ratio depends not only on the direction of applied stress $(\hat{\mathbf{n}}(\theta, \phi))$ but also on the transverse direction of measurement (see ESI†); thus a question arises whether this is the only auxetic direction in the Yukawa systems. In response, using formula (2), the minimal

Fig. 1 Poisson's ratio in the direction [110][110] of Yukawa crystals with selected values of size polydispersity (δ = 0, δ = 2% i δ = 5%) plotted as a function of the inverse of system size (1/N) at $p^* = 50$, $\beta \varepsilon = 20$, $\kappa \sigma = 10$. The lines represent linear fits to determine the values of Poisson's ratio in the thermodynamic limit $(N \to \infty)$.

Fig. 2 The Poisson's ratio $\nu_{[110][1\bar{1}0]}$ of Yukawa crystals with different screening lengths and different values of contact potential plotted as a function of polydispersity. Lines are drawn to guide the eyes.

Poisson's ratio has been calculated in all crystallographic directions. In Fig. 3, the Poisson's ratio for monodisperse (δ = 0.00) and polydisperse systems at δ = 0.05 and δ = 0.08 has been plotted in spherical coordinates. We observe not only a decrease of Poisson's ratio with increasing polydispersity but also an increase in the range of auxetic directions, which is manifested by increasing volume of the obtained shape in Fig. 3. The increase of the range of auxetic directions can be clearly seen by analysis of the Poisson's ratio at some given crystallographic direction as a function of the angle α . In Fig. 4, the dependence of Poisson's ratio on the angle α , which describes the direction of measurement of the response to the applied stress, has been shown. We observe here new auxetic directions (within the range $\alpha_1 \leq \alpha \leq \alpha_2$) which are induced by increasing particle

Fig. 3 The absolute value of minimal negative Poisson's ratio in all crystallographic directions of the Yukawa system at $\beta \varepsilon = 20$, $\kappa \sigma = 10$ and with polydispersity values: $\delta = 0.00$, $\delta = 0.05$, $\delta = 0.08$. The absolute value of the minimal negative Poisson's ratio for the given direction $\hat{\mathbf{n}}$ |min($\nu_{\hat{\mathbf{n}}}(x)$, 0)|.

size polydispersity. So, Fig. 4 shows that an increase of the polydispersity results in an enhancement of auxeticity of the system not only by decreasing the value of Poisson's ratio but also by increasing the range of crystallographic directions for which the Poisson's ratio takes negative values. This effect of enhanced auxeticity due to polydispersity can be explained as follows. As shown by Tretiakov and Wojciechowski, 17 the Poisson's ratio in the $[110][1\overline{1}0]$ -direction decreases with increasing Debye screening length and/or with decreasing density of the system. In the studied system an introduction or an increase of polydispersity in the system is accompanied by a slight decrease of density (with the other thermodynamic parameters kept constant, *i.e.* pressure and temperature) which is originated from the increase in the effective size of particle's hard-core. This in turn leads to a small increase of the ''effective'' Debye screening length. Both these mechanisms lead to an enhancement of auxeticity in the $[110][1\overline{1}0]$ -direction. Taking into account that we are dealing with a continuous process, the directions that are very close to the $[110][1\overline{1}0]$ -direction also become auxetic. As a result, we have an enhancement of the auxeticity (in the $[110][1\overline{1}0]$ -direction) and an extension of the range of crystallographic directions with increasing polydispersity. Soft Matter
 $\frac{3}{24}$ -0.14
 $\frac{1}{24}$ -3.25
 $\frac{1}{24}$ -1.13
 $\frac{1}{24}$ -1.13
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 $\frac{1}{24}$ -1.13
 $\frac{1}{24}$ -1.13
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 $\frac{1}{24}$

Fig. 4 Poisson's ratio as a function of the transverse direction described by α for the following parameters: $\beta \varepsilon = 20$, $\kappa \sigma = 10$ ($\alpha_1 = 1.4193$, $\alpha_2 = 2.3377$

Fig. 5 Absolute value of the average negative Poisson's ratio for all crystallographic directions of monodisperse Yukawa crystals ($\delta = 0$) and polydisperse Yukawa crystals with $\delta = 0.05$ and $\delta = 0.08$.

In order to perform a quantitative analysis of the auxeticity enhancement effect, we define the degree of auxeticity of the studied system with respect to the ideal auxetic as (for details see ESI†)

$$
\chi_{\delta} = \sqrt[3]{\frac{3A_{\delta}}{4\pi}},\tag{3}
$$

where A_{δ} is the integral over absolute values of the mean negative Poisson's ratio of the Yukawa crystal in all crystallographic directions, which is shown in Fig. 5 for mono- and polydisperse systems at $\beta \varepsilon = 20$, $\kappa \sigma = 10$. An increase of the negative Poisson's

Fig. 6 (a) Auxeticity degree as a function of polydispersity. (b) Auxeticity enhancement as a function of polydispersity. In both figures, lines are drawn to guide the eyes.

ratio amplitude and range with increasing size polydispersity of particles indicates an enhancement of the auxetic properties in the studied system. The quantitative enhancement of auxeticity caused by polydispersity is described by auxeticity enhancement. It is defined as the difference between the degree of auxeticity of a system with given polydispersity and the degree of auxeticity of a monodisperse system

$$
\eta = \chi_{\delta} - \chi_{0}. \tag{4}
$$

Fig. 6 represents both the degree of auxeticity and the auxeticity enhancement parameter as functions of polydispersity. In Fig. 6a, we observe larger values of the degree of auxeticity of systems with polydispersity than for a monodisperse Yukawa system. This enhancement comes from both a decrease of Poisson's ratio and an extension of the range of auxetic directions (see Fig. 6b).

4 Conclusions

Extensive computer simulations have shown that the increase of size polydispersity of particles in Yukawa crystals leads to enhancement of the auxetic properties of the system, both by reducing Poisson's ratio and by extending the range of auxetic directions. In other words, the fcc hard-core repulsive Yukawa crystals with larger polydispersity of particles exhibit lower negative Poisson's ratio values and have more crystallographic directions in which the value of Poisson's ratio is negative. The introduced measure of auxeticity allows a quantitative evaluation of the enhancement of auxetic properties caused by polydispersity of particles.

The auxeticity degree (χ) and the auxeticity enhancement parameter (η) proposed in this paper can be used to assess changes of auxetic properties in various systems.

This work is a part of a project aimed at finding materials with unusual elastic properties and establishing mechanisms leading to them. It is worth noticing that an interesting direction in the search of such properties is the study of systems with various defects, which on the one hand can affect the functionality of the system, and on the other hand can strongly influence the stability of the studied system. It is known, for example, that the value of Poisson's ratio is influenced by point defects in hardsphere crystals⁷¹ or dislocations in colloidal crystals of soft thermosensitive spheres. 72 Therefore, it is interesting to investigate the effect of various defects on the elastic properties of polydisperse Yukawa crystals. Another important direction of future research, from the point of view of practical applications, is to investigate the elastic properties of polydisperse Yukawa systems both with and without defects in case of large deformations. Such studies should be conducted with special attention devoted to the stability of the system because large loads may lead to mechanical instability of the systems under consideration.

Finally, we believe that the effect of polydispersity on the auxetic properties of the crystal is not only interesting and important in itself from the cognitive point of view but it may be also useful in future for designing new metamaterials⁷³ and for synthesizing materials with required elastic properties.

Conflicts of interest

There are no conflicts to declare.

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