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# Size and charge effect of guest cations in the formation of polyoxopalladates: a theoretical and experimental study†‡

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The development of rational synthetic procedures with desired nuclearity and high selectivity is a critical issue in inorganic chemistry. Here we demonstrate a comprehensive understanding of the template effect induced by metal cations in the formation mechanism of the class of polyoxopalladates ( $\{MPd_{12}L_8\}$  nanocube and  $\{MPd_{15}L_{10}\}$  nanostar) by combining computational and experimental techniques. The capture of a  $M^{n+}$  guest ion by a peripheral palladium(II)-oxo shell leads to a competition between the parent  $Pd^{2+}$  addenda ion and the respective guest metal ion. The present study reveals that (i) the selection of the incorporated guest ion has a thermodynamic control, (ii) the main factors governing the formation of a particular polyanion are the charge and size of the guest cation, (iii) the electrostatic interaction between the cation and the surrounding oxo ligands and (iv) the dehydration ability of the cation. As expected from the number of observed  $\{M^{n+}Pd_{12}L_8\}$  species, trivalent cations  $M^{3+}$  were found to be good templates resulting in several examples of  $\{M^{3+}Pd_{12}L_8\}$ , whereas monovalent cations  $M^+$  are much less prone to form  $\{M^+Pd_{12}L_8\}$ . For tetravalent cations the dehydration energies are very large, however, the formation of  $\{M^{4+}Pd_{12}L_8\}$  nanocubes is found to be still energetic favourable. Fully consistent with computational predictions, four novel polyoxo-12-palladates were synthesized: the  $La^{3+}$ -centered nanocube  $[LaPd_{12}O_8(PhAsO_3)_8]^{5-}$  (**LaPd<sub>12</sub>-closed**), the  $La^{3+}$ -centered "open" nanocube  $[LaPd_{12}O_6(OH)_3(PhAsO_3)_6(OAc)_3]^{3-}$  (**LaPd<sub>12</sub>-open**), the  $Ga^{3+}$ -centered  $[GaPd_{12}O_8(PhAsO_3)_8]^{5-}$  (**GaPd<sub>12</sub>**), and the  $In^{3+}$ -analogue  $[InPd_{12}O_8(PhAsO_3)_8]^{5-}$  (**InPd<sub>12</sub>**). All four compounds were fully characterized in the solid state and in solution by a multitude of physicochemical techniques, including  $^{71}Ga$  and  $^{115}In$  NMR as well as mass spectrometry. The experimentally observed selective incorporation of only  $In^{3+}$  ions in the presence of  $Ga^{3+}$  and  $In^{3+}$  confirmed the thermodynamic control of the formation mechanism, which we had predicted by theory.

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## 1. Introduction

In recent years significant advances have been made in the control of different variables involved in the formation mechanism of polyoxometalates (POMs). However, there is a lack of

systematic studies that aim at identifying unambiguously the driving forces related to the self-assembly or aggregation processes. The "template-directed" method is one popular and extremely important synthetic strategy for obtaining novel POMs. The nuclearity and topology of the products are strongly dependent on the size, shape, and charge of the template ions. For example, anions such as  $Cl^-$  and  $SO_4^{2-}$  could be encapsulated in the central cavities of discrete polyoxovanadates to form templated host-guest complexes.<sup>1</sup> On the other hand, many different heterogroups (e.g.,  $As^{III}O_3^{3-}$ ,  $Sb^{III}O_3^{3-}$ ,  $Si^{IV}O_4^{4-}$ ,  $Ge^{IV}O_4^{4-}$ ,  $P^{V}O_4^{3-}$ ,  $As^{V}O_4^{3-}$ , and  $I^{VII}O_6^{5-}$ ) can efficiently control the shape, size, and structure of high-nuclearity heteropolytungstates.<sup>2</sup>

Besides classical POMs,<sup>3</sup> in the last decade or so an "unconventional" POM family based exclusively on  $Pd^{II}$ ,  $Pt^{III}$ , or  $Au^{III}$  addenda has been developed.<sup>4</sup> Since noble metals are well-known active ingredients of many catalysts, the study of noble metal-containing POMs is a particularly interesting topic. In 2004, Wickleder's group synthesized the first polyoxoplatinate

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exclusively based on  $d^7$  addenda ions,  $[\text{Pt}^{\text{III}}_{12}\text{O}_8(\text{S}^{\text{VI}}\text{O}_4)_{12}]^{4-}$ .<sup>5</sup> Since then the Kortz group has pioneered the class of polyoxopalladates(II) in 2008,<sup>6</sup> and the class of polyoxoaurates(III) in 2010.<sup>7a</sup> The first polyoxopalladate was the  $[\text{H}_6\text{Pd}_{13}\text{O}_8(\text{AsO}_4)_8]^{8-}$  (**Pd<sub>13</sub>**) nanocube, prepared by simple condensation of  $\text{Pd}^{2+}$  and arsenate ( $\text{As}^{\text{V}}\text{O}_4^{3-}$ ) ions in aqueous medium.<sup>6</sup> In the following years it was demonstrated that the eight arsenate capping groups can be easily replaced by other heterogroups, such as selenite ( $[\text{Pd}_{13}\text{O}_8(\text{SeO}_3)_8]^{6-}$ , **Pd<sub>13</sub>Se**) or phenylarsonate ( $[\text{Pd}_{13}\text{O}_8(\text{PhAsO}_3)_8]^{6-}$ , **Pd<sub>13</sub>AsPh**).<sup>8</sup> Interestingly, substitution of the capping groups is accompanied by an increase of the coordination number of the central  $\text{Pd}^{2+}$  ion from 4 (**Pd<sub>13</sub>**) to 6 (**Pd<sub>13</sub>Se**) and even 8 (**Pd<sub>13</sub>AsPh**).

In addition to the capping groups the central palladium(II) ion in the nanocube  $\{\text{MPd}_{12}\text{L}_8\}$  (Fig. 1a) can also be replaced by other metal ion guests, including trivalent lanthanide ions ( $\text{Ln}^{3+} = \text{Y}, \text{Pr}, \text{Nd}, \text{Sm}, \text{Eu}, \text{Gd}, \text{Tb}, \text{Dy}, \text{Ho}, \text{Er}, \text{Tm}, \text{Yb}, \text{Lu}$ ) and 3d transition metal ions ( $\text{Sc}^{3+}, \text{Mn}^{2+}, \text{Fe}^{3+}, \text{Co}^{2+}, \text{Ni}^{2+}, \text{Cu}^{2+}, \text{Zn}^{2+}$ ).<sup>9</sup> Interestingly, the nanostar  $\{\text{MPd}_{15}\text{L}_{10}\}$  (Fig. 1b) can be formed only in the presence of  $\text{Na}^+, \text{K}^+, \text{Ag}^+$ , or  $\text{Ba}^{2+}$ ,<sup>10</sup> whereas in the presence of  $\text{Sr}^{2+}$  ions the “open” nanocube  $\{\text{SrPd}_{12}\text{L}_6\text{L}'_3\}$  ( $\text{L} = \text{phenylarsonate}$ ,  $\text{L}' = \text{acetate}$ ) is formed.<sup>10c</sup> Such observations bear similarities with the important template role of alkali and alkaline earth ions in the formation of various organic macrocycle-based structures (crown ethers *etc.*).<sup>11</sup> In addition to the above-mentioned nanocube, nanostar and open-nanocube structural types, some additional polyoxopalladates with unexpected geometries have been obtained, such as the bowl-shaped palladovanadate  $\{\text{Pd}_7\text{V}_6\}$ ,<sup>12a</sup> the double cuboid-shaped 22-palladates  $\{\text{Cu}_2\text{Pd}_{22}\}$ <sup>12b</sup> and  $\{\text{Na}_2\text{Pd}_{22}\}$ ,<sup>12c</sup> as well as palladate macrocycles  $\{\text{Pd}_n\}$  ( $n = 60, 72, 84, 96, 108$ ).<sup>13</sup>

It is evident that the central metal ion guest as well as the capping groups play a key role in the formation mechanism of polyoxopalladates, but details remain unknown. Hence the rational synthesis of novel polyoxopalladate structural types of

desired shape, size and composition is virtually impossible. On the other hand, density functional theory (DFT) methods have been applied to POMs significantly in the last two decades, in particular with respect to (i) electronic structure, (ii) rationalization of physicochemical properties, and (iii) reactivity as a function of shape and composition.<sup>14</sup> In order to obtain more insight into polyoxopalladate chemistry, in particular with respect to factors that govern guest metal ion encapsulation and to perhaps shed more light on selectivity issues, we have decided to perform systematic theoretical analysis for a series of 35 metal ion guests  $M$  involved in the formation of the  $\{\text{MPd}_{12}\text{L}_8\}$  nanocube and  $\{\text{MPd}_{15}\text{L}_{10}\}$  nanostar polyoxopalladate structural types.

The encapsulated cations were selected by considering both their charge and size, which range from alkali and alkaline earth ions to transition metal ions, as well as trivalent and tetravalent main group cations. We have discovered a remarkable competition between  $\text{Pd}^{2+}$  ions and other cations, which is key for the formation of a specific polyoxopalladate structural type. With a focus on eventually being able to computationally predict experimental results, we have carefully studied experimentally (i) the capture of the largest trivalent cation  $\text{La}^{3+}$  inside a polyoxopalladate, and (ii) the selective incorporation of  $\text{In}^{3+}$  vs.  $\text{Ga}^{3+}$  in a polyoxopalladate.

## 2. Computational and experimental details

### 2.1 Computational method

All calculations were performed with the Gaussian 09 package.<sup>15</sup> The computational scheme consists of two steps. Geometry optimizations of all nanocube  $\{\text{MPd}_{12}\text{L}_8\}$  and nanostar  $\{\text{MPd}_{15}\text{L}_{10}\}$  polyoxopalladates were carried out at the B3LYP level without symmetry restrictions.<sup>16</sup> The SDD effective core pseudopotential (ECP) basis set was used for La, Yb, Lu, Eu, Ce, Th, and U,<sup>17</sup> the small core potential (CRENBL ECP) was used for Ra,<sup>18</sup> whereas the LANL2DZ basis set was employed for the main group metals (Rb, Cs, Sr, Ba, Ga, In, Tl, Sn) and transition metals (Sc, Mn, Fe, Co, Ni, Cu, Zn, Y, Zr, Pd, Ag, Cd, Hf) with Los Alamos relativistic core potentials (ECPs).<sup>19</sup> In addition, the 6-31G\*\* basis set was used for O, C, As, Se, H, and the encapsulated small metal ions (Li, Na, K, Be, Mg, Ca).<sup>20</sup> From these calculations, we obtained the energies at the B3LYP level. In order to include the long-range interaction and dispersion effects, single point calculations were performed for all optimized polyanions with two additional functionals, M06 and  $\omega\text{B97XD}$ .<sup>21,22</sup> For all steps, the continuum SMD implicit solvation model was used to simulate the effect of the aqueous solution.<sup>23</sup>

As shown in Fig. 1, the nanocube  $\{\text{MPd}_{12}\text{L}_8\}$  and nanostar  $\{\text{MPd}_{15}\text{L}_{10}\}$  were selected, in which the central metal ion usually has an oxo-coordination number of 8 and 10, respectively. In order to evaluate the selective encapsulation of different guest metal ions, the reaction mechanism is simulated by scheme (1), and the complexation energy ( $E_{\text{com}}$ ) was calculated by eqn (2) and (3):

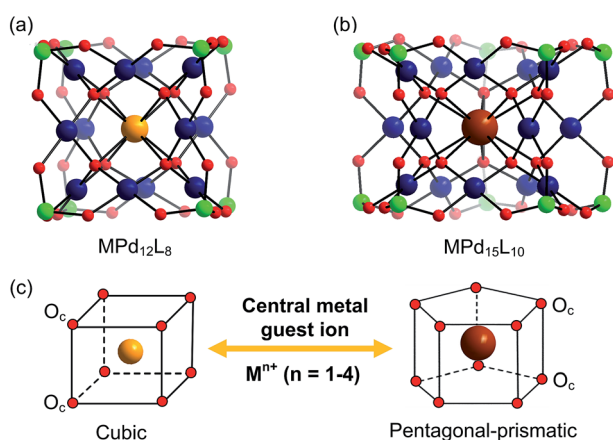
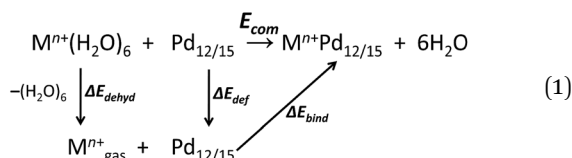


Fig. 1 Ball-and-stick representation of the polyoxopalladate (a) nanocube  $\{\text{MPd}_{12}\text{L}_8\}$  and (b) nanostar  $\{\text{MPd}_{15}\text{L}_{10}\}$ , respectively ( $M$  = central metal guest ion,  $L$  = capping group), and (c) the oxo-coordination sphere around  $M$  in both palladate structural types. Colour code:  $M$  (orange/brown),  $L$  (green),  $\text{Pd}$  (dark blue),  $\text{O}$  (red).





$$E_{\text{com}} = E(\text{M}^{n+}\text{Pd}_{12/15}) + E(6\text{H}_2\text{O}) - E(\text{Pd}_{12/15}) - E(\text{M}^{n+}(\text{H}_2\text{O})_6) \quad (2)$$

$$E_{\text{com}} = \Delta E_{\text{bind}} + \Delta E_{\text{def}} + \Delta E_{\text{dehyd}} \quad (3)$$

where  $\text{M}^{n+}(\text{H}_2\text{O})_6$  is the solvated cation model. Since dehydration is one fundamental factor for an accurate determination of the complexation energy, all cations were solvated by six explicit water molecules and also surrounding by the implicit model. With this explicit and implicit solvent combination model, the dehydration energy of the cations was well estimated when compared with the experimental hydration enthalpies, as all deviations are <10%, except for  $\text{Li}^+$ ,  $\text{Rb}^+$ ,  $\text{Cs}^+$ , and  $\text{Ra}^{2+}$  (Fig. S1†).<sup>24</sup> The entire polyoxopalladate formation process is completed when the relaxed  $\text{Pd}_{12/15}$  cage picks up the cation from the solvent and encapsulates it into the cage. The complexation energies ( $E_{\text{com}}$ ) for  $\text{Pd}_{12/15}$  with all different cations are computed, defined as the reaction energies involved in the encapsulation process. Three terms contribute to this process, (i) the cage deformation of each capsule with respect to the cation-free  $\text{Pd}_{12/15}$  cage ( $\Delta E_{\text{def}}$ ), (ii) dehydration of the guest cation from solvated to free ion ( $\Delta E_{\text{dehyd}}$ ), and (iii) the binding interaction ( $\Delta E_{\text{bind}}$ ) between the optimally-deformed cage and the “naked” cation, respectively.

## 2.2 Synthesis of $\text{Na}_5[\text{LaPd}_{12}\text{O}_8(\text{PhAsO}_3)_8] \cdot 31\text{H}_2\text{O}$ (Na-LaPd<sub>12</sub>-closed)

$\text{Pd}(\text{CH}_3\text{COO})_2$  (0.023 g, 0.102 mmol),  $\text{PhAsO}_3\text{H}_2$  (0.020 g, 0.099 mmol) and  $\text{LaCl}_3 \cdot 7\text{H}_2\text{O}$  (0.009 g, 0.024 mmol) were dissolved in 2 mL of 0.5 M NaOAc solution (pH 7.0). While stirring, the solution was heated to 80 °C. After dissolution of all components, the pH of the reaction mixture was adjusted to 7.3 by addition of 6 M NaOH. The resulting solution was heated at 80 °C for 1 hour. Then it was cooled to room temperature, filtered and allowed to crystallize at room temperature in an open vial. Dark red, block-shaped crystals of Na-LaPd<sub>12</sub>-closed were obtained after one week, which were filtered off and air dried. Yield: 0.008 g (25%, based on Pd). Elemental analysis calcd (%): Na 3.01, C 15.10, La 3.64, Pd 33.45, As 15.70; found: Na 3.28, C 15.51, La 3.76, Pd 33.44, As 15.43. IR (2% KBr pellet,  $\nu/\text{cm}^{-1}$ ): 1627 (m), 1479 (w), 1439 (m), 1093 (m), 792 (s), 742 (w), 694 (m), 592 (m), 547 (s).

## 2.3 Synthesis of $\text{Na}_3[\text{LaPd}_{12}\text{O}_6(\text{OH})_3(\text{PhAsO}_3)_6(\text{OAc})_3] \cdot 40\text{H}_2\text{O}$ (Na-LaPd<sub>12</sub>-open)

This compound was prepared by exactly the same procedure as Na-LaPd<sub>12</sub>-closed. The initially formed Na-LaPd<sub>12</sub>-closed was removed by filtration. The filtrate was left for further evaporation, which resulted in another portion of dark red, needle-like

crystals of Na-LaPd<sub>12</sub>-open within a few days, which were filtered off and air dried. Yield: 0.006 g (19% based on Pd). Elemental analysis calcd (%): Na 1.85, C 13.52, La 3.72, Pd 34.24, As 12.05; found: Na 1.94, C 13.75, La 3.51, Pd 34.69, As 12.66. IR (2% KBr pellet,  $\nu/\text{cm}^{-1}$ ): 1633 (m), 1539 (m), 1439 (w), 1419 (m), 1093 (m), 814 (s), 744 (m), 694 (m), 536 (s).

## 2.4 Synthesis of $\text{Na}_5[\text{GaPd}_{12}\text{O}_8(\text{PhAsO}_3)_8] \cdot 36\text{H}_2\text{O}$ (Na-GaPd<sub>12</sub>)

$\text{Pd}(\text{CH}_3\text{COO})_2$  (0.023 g, 0.102 mmol),  $\text{PhAsO}_3\text{H}_2$  (0.020 g, 0.099 mmol) and  $\text{Ga}(\text{NO}_3)_3$  (0.006 g, 0.024 mmol) were dissolved in 2 mL of 0.5 M NaOAc solution (pH 7.0). While stirring, the solution was heated to 80 °C for 1 hour. Then it was cooled to room temperature, filtered and allowed to crystallize at room temperature in an open vial. Red, block-shaped crystals of Na-GaPd<sub>12</sub> were obtained after three days, which were filtered off and air dried. Yield: 0.014 g (43% based on Pd). Elemental analysis calcd (%): Na 2.99, C 15.02, Ga 1.82, Pd 33.27, As 15.62; found: Na 2.90, C 15.71, Ga 1.96, Pd 32.34, As 16.14. IR (2% KBr pellet,  $\nu/\text{cm}^{-1}$ ): 1631 (m), 1479 (w), 1438 (m), 1094 (m), 804 (s), 744 (w), 694 (m), 657 (m), 538 (s).

## 2.5 Synthesis of $\text{Na}_5[\text{InPd}_{12}\text{O}_8(\text{PhAsO}_3)_8] \cdot 30\text{H}_2\text{O}$ (Na-InPd<sub>12</sub>)

This compound was prepared by exactly the same procedure as Na-GaPd<sub>12</sub>, but with  $\text{InCl}_3$  (0.005 g, 0.025 mmol) instead of  $\text{Ga}(\text{NO}_3)_3$ . Red, block-shaped crystals of Na-InPd<sub>12</sub> were obtained after three days, which were filtered off and air dried. Yield: 0.014 g (44% based on Pd). Elemental analysis calcd (%): Na 3.04, C 15.27, In 3.04, Pd 33.22, As 15.88; found: Na 2.82, C 15.89, In 3.80, Pd 32.30, As 16.06. IR (2% KBr pellet,  $\nu/\text{cm}^{-1}$ ): 1628 (m), 1479 (w), 1439 (m), 1093 (m), 802 (s), 744 (w), 694 (m), 629 (m), 540 (s).

# 3. Results and discussion

## 3.1 Size matching between guest $\text{M}^{n+}$ cations and the $\text{Pd}_{12/15}$ cages

Since the discovery in 2008 of the first member of the  $\text{Pd}_{12}$  family,  $\text{Pd}_{13}$ ,<sup>6</sup> Kortz's group has synthesized a large number (*ca.* 50) of palladate nanocube derivatives  $\{\text{MPd}_{12}\text{L}_8\}$  by systematically substituting the arsenate capping groups by selenite, phenylarsonate and phenylphosphonate, and the central  $\text{Pd}^{2+}$  ion by s, d and f block metal ions.<sup>4,6–9</sup> In order to better understand the templating role of the guest cation, systematic DFT calculations were performed by introducing different metal ions into the  $\text{Pd}_{12}$  and  $\text{Pd}_{15}$  cages. The empty “host” cages  $\text{Pd}_{12}$  and  $\text{Pd}_{15}$  and the corresponding host ( $\text{Pd}_{12}/\text{Pd}_{15}$  cage) – guest (cation M) systems capped by  $\text{PhAsVO}_3^{2-}$  ( $\{\text{MPd}_{12}(\text{AsPh})_8\}$ ) were optimized at the B3LYP level. The molecular electrostatic potential (MEP, Fig. S2†) analysis for the free  $\text{Pd}_{12}$  cage revealed an interesting distribution of most negative partial atomic charges at the centre of the inner  $\{\text{O}_8\}$  cage, indicating that electrophiles such as metal ions are most likely to be located at the central position of the palladate nanocube. This prediction is in line with the experimental results, which show that the guest cation indeed occupies such position. As shown in Table



S1,<sup>†</sup> the computed distances ( $O_c-O_c$ ,  $M-O_c$ , and  $M-Pd$ ) for a series of palladates reproduced fairly well the reported XRD data, although they are found systematically slightly longer than observed experimentally. It is worth mentioning that when  $M = Pd^{2+}$ ,  $Fe^{3+}$ ,  $Co^{2+}$ ,  $Ni^{2+}$ , and  $Eu^{3+}$  ions occupy the central site, the DFT calculations suggested that the high-spin state for  $M$  in  $\{MPd_{12}(AsPh)_8\}$  is more favourable than the low-spin state. Such result was indeed confirmed experimentally by magnetic and EPR studies.<sup>9b</sup>

For efficient encapsulation, the guest cation and the cavity in the palladate cage should match well. Due to the small flexibility of the  $\{O_8\}$  coordination shell, all guest cations are optimally located in the centre of the cube. The average  $O_c-O_c$  distance generally elongates as the effective ionic radius of  $M^{n+}$  increases, and this trend is perfectly in line with an increase of the  $M-O_c$  bond distances. To gain insight into the effect of cation size on the geometry of the cage, the  $O_c-O_c$  distortions after encapsulation of the cation are plotted in Fig. 2, by referring to the distance in the empty cage  $Pd_{12}$  ( $d_{O_c-O_c} = 2.728 \text{ \AA}$ ). We found that guest cations with a radius smaller than  $1.12 \text{ \AA}$  could induce a contraction of the  $\{O_8\}$  cavity (e.g.  $Co^{2+}$ ,  $Ni^{2+}$ ,  $Cu^{2+}$ ,  $Zn^{2+}$ ,  $Mn^{2+}$ ,  $Sc^{3+}$ ,  $Fe^{3+}$ ,  $Lu^{3+}$ ) and also guest ions that have not yet been incorporated in the  $Pd_{12}$  cage experimentally, such as  $Li^+$ ,  $Be^{2+}$ ,  $Mg^{2+}$ ,  $Ga^{3+}$ ,  $In^{3+}$ ,  $Sn^{4+}$ ,  $Zr^{4+}$ , and  $Hf^{4+}$ . In particular,  $Be^{2+}$ ,  $Fe^{3+}$ ,  $Ga^{3+}$ , and  $Sn^{4+}$  seem too small to be hosted efficiently, and consequently a large contraction occurs to maximize the  $M-O_c$  interactions. When the ion size is between  $1.13$  and  $1.26 \text{ \AA}$ , a small expansion with  $\Delta d$  less than  $0.1 \text{ \AA}$  is needed, except for

$Th^{4+}$ . However, a significant distortion of  $\{O_8\}$  was detected for ions larger than  $1.28 \text{ \AA}$ , such as  $Ce^{3+}$ ,  $La^{3+}$ ,  $Sr^{2+}$ ,  $Ag^+$ ,  $K^+$ ,  $Rb^+$ ,  $Cs^+$ ,  $Ba^{2+}$ , and  $Ra^{2+}$ , where for some cases elongations larger than  $0.4 \text{ \AA}$  were observed.

It is remarkable that for most of the experimentally observed palladate nanocubes, the distortion induced by guest metal ion encapsulation is no larger than  $0.1 \text{ \AA}$ , and therefore the size matching between the cation guests and the cavity of the  $Pd_{12}$  cage is an important factor that must be considered. Fig. 2 also suggests that guest cations with a size ranging from  $0.97$ – $1.26 \text{ \AA}$  fit well within the  $\{O_8\}$  cavity in  $Pd_{12}$  regardless of the charge (except  $Th^{4+}$ ). In contrast, smaller ( $r \leq 0.95 \text{ \AA}$ ) and larger ( $r \geq 1.28 \text{ \AA}$ ) cations are probably poor candidates for constructing  $\{MPd_{12}L_8\}$  palladate nanocubes from a size-matching point of view, with the optimal cation size being in the  $0.97$ – $1.26 \text{ \AA}$  range.

Large guest cations are more likely to accommodate themselves in larger polyoxopalladate assemblies with larger cavities. In order to compare with our computational results on the  $Pd_{12}$  nanocube, we inserted some selected cations ( $Li^+$ ,  $Na^+$ ,  $K^+$ ,  $Rb^+$ ,  $Cs^+$ ,  $Ag^+$ ,  $Be^{2+}$ ,  $Mg^{2+}$ ,  $Ca^{2+}$ ,  $Sr^{2+}$ ,  $Ba^{2+}$ ,  $Zn^{2+}$ ,  $Pd^{2+}$ ) also in the  $Pd_{15}$  nanostar cage. The  $Pd_{15}$  host provides a pentagonal-prismatic  $\{O_{10}\}$  inner coordination sphere, which appears too large for encapsulation of small guest cations, such as  $Li^+$ ,  $Be^{2+}$ ,  $Mg^{2+}$ , and  $Zn^{2+}$  ( $r < 1.2 \text{ \AA}$ ). In this case the cations move away from the  $C_5$  symmetry axis of the  $Pd_{15}$  cage and coordinate to less than 10 oxo-ligands. Two types of such off-center coordination modes were observed from our DFT calculations,  $C_4$  and  $C_5$  as depicted

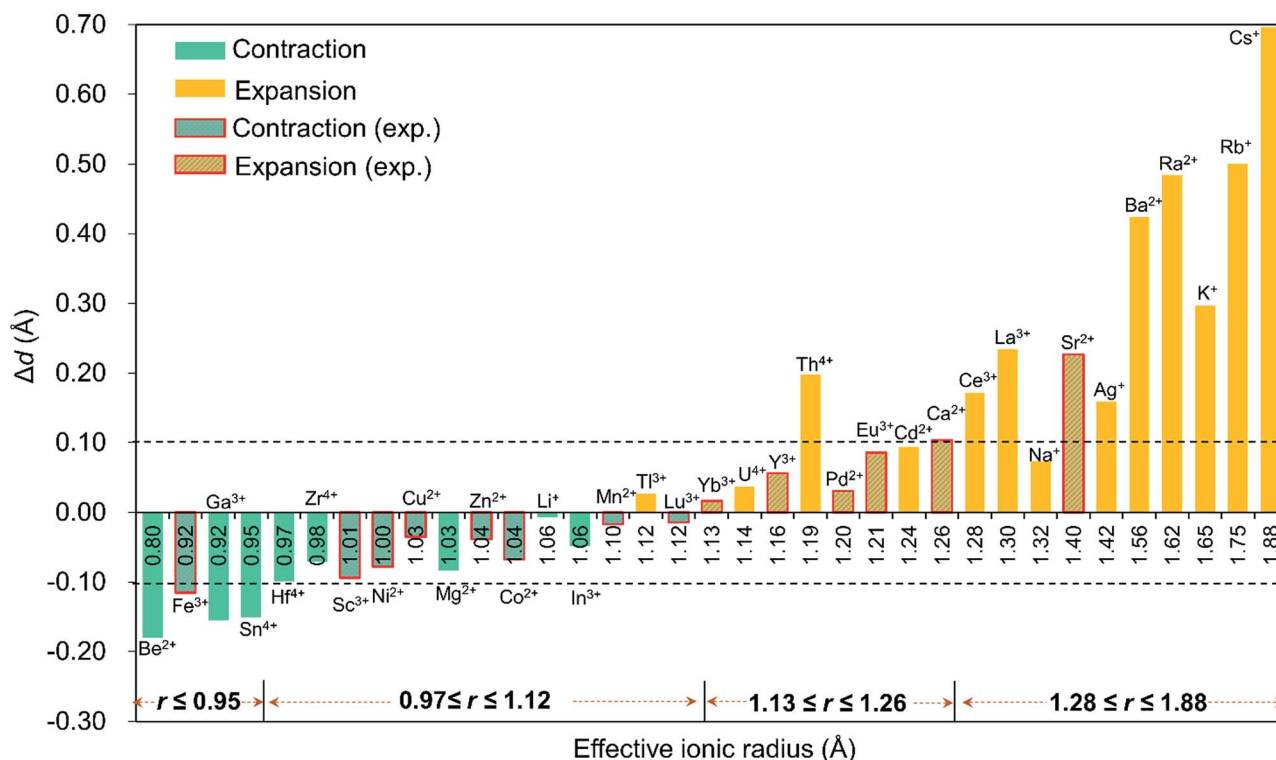


Fig. 2 The  $O_c-O_c$  distortions ( $\Delta d = d_{O_c-O_c} - 2.728$ , with respect to the distance in the empty cage) of the  $\{O_8\}$  cavity after encapsulation of the guest cation. The cations are organized from left to right according to their effective ionic radius. The columns with red edges represent palladates which have been prepared experimentally, whereas all other compounds have not been synthesized yet.



in Fig. 3. For example,  $\text{Li}^+$  could coordinate to five  $\text{O}_c$  from a  $\text{Pd}_5\text{O}_5$  fragment (2.107, 2.276, 2.261, 2.457, 2.336 Å) or to four  $\text{O}_c$  from a  $\text{Pd}_4\text{O}_4$  fragment (2.002, 2.023, 2.005, 2.022 Å). Although the former configuration includes five coordinated oxygen atoms, the shorter bonds in the latter situation indicate stronger interactions. As expected, the energy differences illustrate that the  $\text{C}_4$  mode is more stable than  $\text{C}_5$  by 6.1 kcal mol $^{-1}$  (Table S2†). On the other hand, encapsulation of  $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Rb}^+$ ,  $\text{Cs}^+$ ,  $\text{Ag}^+$ ,  $\text{Ca}^{2+}$ ,  $\text{Sr}^{2+}$ ,  $\text{Ba}^{2+}$ , and  $\text{Ra}^{2+}$  ( $r > 1.2$  Å) is expected to work well for the  $\text{Pd}_{15}$  nanostar cage. Some of them are strongly supported by experiments, which show that  $\text{NaPd}_{15}$ ,  $\text{KPd}_{15}$ ,  $\text{BaPd}_{15}$ , and  $\text{AgPd}_{15}$  can be easily observed in the presence of  $\text{Na}^+$ ,  $\text{K}^+$ ,  $\text{Ba}^{2+}$ , and  $\text{Ag}^+$ .<sup>10</sup> It is worth mentioning that  $\text{Na}^+$  prefers

to coordinate to a  $\text{Pd}_5\text{O}_5$  face ( $\text{C}_5$ ) rather than sitting at the body centre of  $\text{Pd}_{15}$ , as suggested by experiment.<sup>10a</sup> Interestingly,  $\text{Pd}^{2+}$  prefers a  $\text{C}_4$  mode, binding to only four  $\text{O}_c$  of the  $\text{Pd}_5\text{O}_5$  face, as shown by XRD.<sup>10a,c</sup> The good reproducibility of the experimental results by DFT reemphasizes that the size of the cation guest indeed plays an important role in the formation mechanism of the resulting palladate structure.

### 3.2 Complexation energy and competition between $\text{Pd}^{2+}$ and other metal cations

Although size-matching has been established as an essential factor during palladate formation, we have to be aware that (i) the cation–cavity interaction and (ii) the dehydration ability of the cation is not included in the analysis. Thus, we next analyse why the reported cations can be encapsulated by the  $\text{Pd}_{12/15}$  cages and predict some potential candidates from an energetic point of view. To rationalize this point, the complexation energy ( $E_{\text{com}}$ ) of  $\text{Pd}_{12}$  and  $\text{Pd}_{15}$  for the different guest cations was computed as described in the Computational section, and the results at B3LYP level (black points) are shown in Fig. 4, as well as the energy corrections with M06 (red points) and  $\omega\text{B97XD}$  (green points) functionals. The results for M06 give virtually identical values as those of B3LYP functional, whereas adding the dispersion correction in  $\omega\text{B97XD}$  increases the values of the complexation energies, without changing the overall trends. Therefore, the results at B3LYP level can reasonably identify the trend analysis. Generally, the  $E_{\text{com}}$  becomes more negative (exothermic) as the formal charge of the guest cation increases from +1 to +4. For alkali and alkaline earth ions the  $E_{\text{com}}$  is

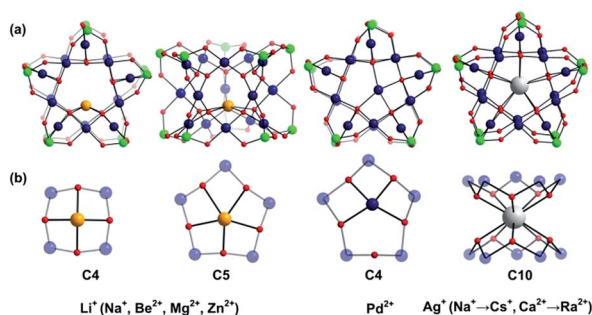


Fig. 3 (a) Ball-and-stick representation of the  $\{\text{MPd}_{15}(\text{AsPh})_{10}\}$  palladate cage encapsulated with different guest cations M. The phenyl groups are omitted for clarity; (b) Exclusive view on the central metal ion guest and its coordination sphere. Colour code: guest metal M (orange/dark blue/white), As (green), Pd (dark blue), O (red).

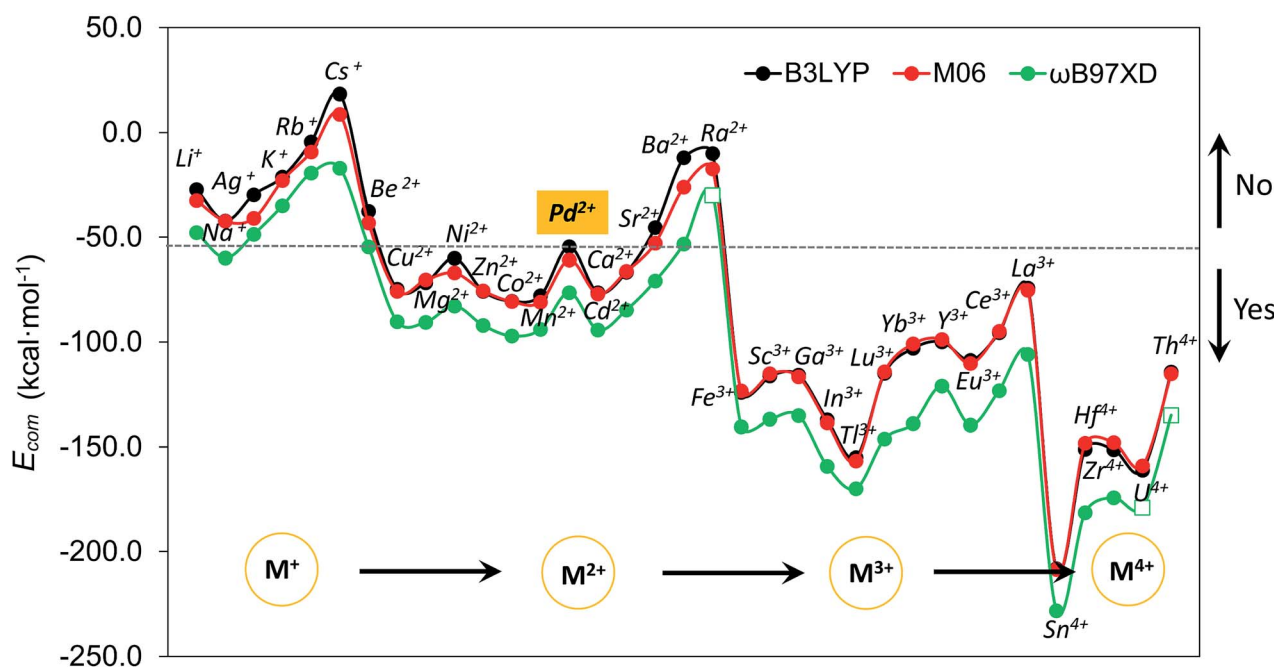


Fig. 4 Computed complexation energies (in kcal mol $^{-1}$ ) of  $\text{M}^{n+}$  ( $n = 1-4$ ) encapsulated in the  $\{\text{Pd}_{12}(\text{AsPh})_8\}$  nanocube cage as a function of the cation guest from monovalent to tetravalent at B3LYP (black), M06 (red), and  $\omega\text{B97XD}$  (green) functional level, respectively. The cations are organized by considering both their charge and size. Note that the more negative values indicate a higher affinity of  $\text{Pd}_{12}$  for the respective metal ion. The  $E_{\text{com}}$  for Ra, U, and Th at  $\omega\text{B97XD}$  level is not included (square) due to the unavailable van der Waals radius for these elements.

affected significantly by the size of the cations. All encapsulations seem to be thermodynamically favourable, except for  $\text{Cs}^+$ , which shows a positive  $E_{\text{com}}$  of  $18.3 \text{ kcal mol}^{-1}$ . It is illustrative that the first reported polyoxopalladate was  $\text{Pd}_{13}$  with a  $\text{Pd}^{2+}$  ion located at the center,<sup>6</sup> and that the synthesis occurred in the presence of both  $\text{Na}^+$  and  $\text{Pd}^{2+}$  ions. Encapsulation of  $\text{Pd}^{2+}$  in the  $\{\text{Pd}_{12}(\text{AsPh})_8\}$  nanocube cage is predicted to be very exothermic with a complexation energy of  $-54.6 \text{ kcal mol}^{-1}$ , whereas  $\text{Na}^+$  is much less competitive with  $-42.2 \text{ kcal mol}^{-1}$ . Thus, it is not surprising that the  $\text{Na}^+$  ions are not incorporated in the palladate structure, but rather act just as counter cations.

Following such strategy, all cations were divided into two domains with  $E_{\text{com}}$  of  $\text{Pd}^{2+}$  as a reference (dashed grey line). The  $E_{\text{com}}$  values below the reference line indicate that from a thermodynamic point of view, the respective ions are more favourable to stabilize the  $\text{Pd}_{12}$  host cage than the reference ion  $\text{Pd}^{2+}$ . Thus, polyanion nanocubes of the type  $\{\text{MPd}_{12}(\text{AsPh})_8\}$  are preferentially formed as compared to  $\{\text{Pd}_{13}(\text{AsPh})_8\}$  ( $\text{Pd}_{13}\text{AsPh}$ ). For instance, encapsulation of  $\text{Fe}^{3+}$  and  $\text{Sc}^{3+}$  ions inside the  $\text{Pd}_{12}$  shell has associated complexation energies of  $-124.1$  ( $\{\text{FePd}_{12}(\text{AsPh})_8\}$ ) and  $-116.2 \text{ kcal mol}^{-1}$  ( $\{\text{ScPd}_{12}(\text{AsPh})_8\}$ ), respectively, both being significantly more exothermic than  $\text{Pd}^{2+}$  ( $-54.6 \text{ kcal mol}^{-1}$ ,  $\text{Pd}_{13}\text{AsPh}$ ). Indeed, the nanocube family  $\{\text{MPd}_{12}(\text{AsPh})_8\}$  with  $\text{M} = \text{Ca}^{2+}, \text{Co}^{2+}, \text{Cu}^{2+}, \text{Ni}^{2+}, \text{Zn}^{2+}, \text{Mn}^{2+}, \text{Sc}^{3+}, \text{Fe}^{3+}, \text{Y}^{3+}, \text{Yb}^{3+}, \text{Lu}^{3+}, \text{and } \text{Eu}^{3+}$  has already been synthesized by using similar synthetic procedures.<sup>9</sup> In contrast, encapsulation of  $\text{M} = \text{alkali metal ions}, \text{Ag}^+, \text{Be}^{2+}, \text{Sr}^{2+}, \text{Ba}^{2+}, \text{and } \text{Ra}^{2+}$  in  $\{\text{MPd}_{12}(\text{AsPh})_8\}$  is expected to be difficult due to the less favourable complexation energy with respect to  $\text{Pd}^{2+}$ , in spite of some of them ( $\text{Li}^+$ ) having a suitable size. In fact, these hypothetical polyoxopalladates have not been synthesized yet in the laboratory. Such conclusions are also valid for nanocube derivatives with other capping groups, such as arsenate ( $\text{AsO}_4^{3-}$ ) and selenite ( $\text{SeO}_3^{2-}$ ), see Fig. S3.† The absolute values of  $E_{\text{com}}$  seem to be influenced by the charge of the capping group. Interestingly, almost identical complexation energies were obtained when replacing  $\text{PhAsO}_3^{2-}$  by  $\text{SeO}_3^{2-}$ , which have the same charge and the  $\text{As}^{\text{V}}\text{-O}$  and  $\text{Se}^{\text{IV}}\text{-O}$  distances are similar. As based on size only,  $\text{Ag}^+, \text{K}^+, \text{Rb}^+, \text{Cs}^+, \text{and } \text{Ba}^{2+}$  can be excluded as guests for the nanocube cage  $\text{Pd}_{12}$ .

We also decided to consider computationally the encapsulation of large guest cations by the 15-palladate nanostar cage  $\{\text{MPd}_{15}(\text{AsPh})_{10}\}$  (Fig. S4†), and then compare to  $\text{Pd}_{12}$ . As expected, the larger guest ions  $\text{Na}^+, \text{Ag}^+, \text{K}^+, \text{Rb}^+, \text{Ba}^{2+}, \text{and } \text{Ra}^{2+}$  ions were calculated to be both geometrically and energetically suitable for the  $\text{Pd}_{15}$  nanostar rather than the  $\text{Pd}_{12}$  nanocube, and these results are in full agreement with the experimental facts.<sup>10</sup> Most of the smaller cations such as  $\text{Mg}^{2+}$  and  $\text{Zn}^{2+}$  do not fit geometrically and are also energetically unfavourable in  $\text{Pd}_{15}$ . On the other hand,  $\text{Pd}^{2+}$  shows a similar ability to be encapsulated by the  $\text{Pd}_{12}$  nanocube and the  $\text{Pd}_{15}$  nanostar, which is consistent with the experimentally observed nanocube  $\text{Pd}_{13}\text{-AsPh}$ ,<sup>8</sup> as well as the mono- and di-palladium-centered nanostar derivatives  $\{\text{Pd} \subset \text{Pd}_{15}(\text{PhAsO}_3)_{10}\}$  and  $\{\text{Pd}_2 \subset \text{Pd}_{15}(\text{PhAsO}_3)_{10}\}$ .<sup>10a,c</sup> The medium-sized  $\text{Sr}^{2+}$  ion was shown experimentally to form an unexpected 'open-nanocube' structure  $[\text{SrPd}_{12}\text{O}_6(\text{OH})_3(\text{PhAsO}_3)_6(\text{OAc})_3]^{4-}$  ( $\text{SrPd}_{12}\text{-open}$ ),<sup>10e</sup> which

**Table 1** Computed complexation energy ( $\text{kcal mol}^{-1}$ ) for  $\text{La}^{3+}$  and  $\text{Sr}^{2+}$  encapsulated in open and closed  $\text{Pd}_{12}$  nanocubes. The experimental product yields are also listed

		B3LYP	M06	$\omega$ B97XD	Exp. ratio%
$\text{Pd}^{2+}$	Closed	-54.6	-60.8	-76.4	100%
$\text{Sr}^{2+}$	Open	-49.9	-61.0	-75.8	98%
	Closed	-45.4	-52.9	-70.9	2%
$\text{La}^{3+}$	Open	-70.6	-74.7	-105.7	40%
	Closed	-74.2	-75.2	-105.9	60%

inspired us to compute the complexation energies for both the open and closed nanocubes  $\text{Pd}_{12}$ , see Table 1. The energy required for encapsulating  $\text{Sr}^{2+}$  into the open form  $\text{SrPd}_{12}\text{-open}$  was computed to be  $-50.0 \text{ kcal mol}^{-1}$ , and for the closed form  $[\text{SrPd}_{12}\text{O}_8(\text{PhAsO}_3)_8]^{6-}$  ( $\text{SrPd}_{12}\text{-closed}$ ) it was slightly less exothermic,  $-45.4 \text{ kcal mol}^{-1}$ . Therefore, computationally it is predicted that the open form  $\text{SrPd}_{12}\text{-open}$  is preferentially formed compared to  $\text{SrPd}_{12}\text{-closed}$ . Amongst the unfavourable guest ions for the closed nanocube shell  $\text{Pd}_{12}\text{-closed}$ ,  $\text{Sr}^{2+}$  shows the smallest  $E_{\text{com}}$  difference compared to  $\text{Pd}^{2+}$  with only  $9.2 \text{ kcal mol}^{-1}$  (and only  $4.6 \text{ kcal mol}^{-1}$  for  $\text{Pd}_{12}\text{-open}$ ) at the B3LYP level, and even smaller differences at the M06 and  $\omega$ B97XD levels. Thus, a competition between  $\text{Pd}^{2+}$  and  $\text{Sr}^{2+}$  guest ions is predicated computationally for such reactions. Experiments showed that only 2% of  $\text{SrPd}_{12}\text{-closed}$  is formed, and that the  $\text{Sr}^{2+}$  ion can be substituted by  $\text{Pd}^{2+}$  to form  $\text{Pd}_{13}\text{AsPh}$  by simply increasing the pH of the solution.<sup>10e</sup> On the other hand,  $\text{SrPd}_{12}\text{-open}$  can indeed be isolated in clean form, but to date the  $\text{Pd}_{13}\text{-open}$  structural type has not been prepared yet.

It is interesting to note that  $E_{\text{com}}$  for  $\text{La}^{3+}$  is very close to that calculated for  $\text{Pd}^{2+}$ , which may lead to mixed products  $\text{LaPd}_{12}\text{-closed}$  and  $\text{Pd}_{13}\text{AsPh}$ . In contrast to  $\text{Sr}^{2+}$ , calculations suggest that for  $\text{La}^{3+}$  the closed nanocube ( $\text{LaPd}_{12}\text{-closed}$ ) is slightly more favourable than the open one ( $\text{LaPd}_{12}\text{-open}$ ), see Table 1. Accordingly, the nature and size of the guest cation directly influences the shape of the resulting poly-oxopalladate and this in turn strongly suggests a template effect of the cation in polyoxopalladate synthesis.

### 3.3 Potential new candidates for the 12-palladate family

The systematic study of the complexation energies for different cation guests has revealed that competition with  $\text{Pd}^{2+}$  plays a critical role when trying to determine the structure-type of the respective product. Although the energy trend should not be taken quantitatively, it appears to be qualitatively useful in the design of synthetic parameters for discovering new polyoxopalladates.

To date there is a dominance of 3d transition metal and lanthanide elements as central guests of the polyoxo-12-palladate nanocube family  $\{\text{MPd}_{12}\text{L}_8\}$ . Much less attention has been paid on p-block elements. We calculated the encapsulation of  $\text{Ga}^{3+}$ ,  $\text{In}^{3+}$ , and  $\text{Tl}^{3+}$  as very exothermic with energies of  $-115.8$ ,  $-137.1$  and  $-155.1 \text{ kcal mol}^{-1}$ , respectively. For all three cations, the encapsulation is predicted to be more



favourable than for the already reported  $\text{Sc}^{3+}$  derivative  $[\text{ScPd}_{12}\text{O}_8(\text{PhAsO}_3)_8]^{5-}$ .<sup>9b</sup> In addition, there is a clear trend of increasing encapsulation ability going down group IIIA (B, Al, Ga, In, Tl).

On the other hand, to date no cation with a charge larger than 3+ has been encapsulated in the  $\text{Pd}_{12}$  nanocube shell. Therefore, we analysed computationally the encapsulation of several tetravalent cations, such as  $\text{Sn}^{4+}$ ,  $\text{Zr}^{4+}$ ,  $\text{Th}^{4+}$ ,  $\text{U}^{4+}$ , and  $\text{Hf}^{4+}$ . As expected, all tetravalent cations exhibit much favourable complexation energies due to the large anion–cation electrostatic interactions. The small  $\text{Sn}^{4+}$  ion has the lowest energy of all computed tetravalent ions and is hence the most promising candidate for encapsulation.

In order to verify the various theoretical predictions experimentally, we designed several key experiments, which concern mainly (i) encapsulation of p-block elements in the  $\text{Pd}_{12}$  nanocube shell, (ii) synthesis of open- and closed-nanocube isomers for  $\text{La}^{3+}$ , and (iii) competition of three guest cations for  $\text{Pd}_{12}$  nanocube shell.

### 3.4 Synthesis and structural characterization of nanocubes $\text{LaPd}_{12}\text{-closed}$ , $\text{GaPd}_{12}$ , $\text{InPd}_{12}$ and open-nanocube $\text{LaPd}_{12}\text{-open}$

We have synthesized three new members of the  $\{\text{MPd}_{12}\text{L}_8\}$  nanocube family, the lanthanum-derivative  $[\text{LaPd}_{12}\text{O}_8(\text{PhAsO}_3)_8]^{5-}$  (**LaPd<sub>12</sub>-closed**), as well as the first examples of main group III derivatives, namely the gallium-containing  $[\text{GaPd}_{12}\text{O}_8(\text{PhAsO}_3)_8]^{5-}$  (**GaPd<sub>12</sub>**) and the indium-containing  $[\text{InPd}_{12}\text{O}_8(\text{PhAsO}_3)_8]^{5-}$  (**InPd<sub>12</sub>**), see Exp. section for details. Single-crystal X-ray analysis revealed that all three polyoxopalladates are isostructural (Fig. 5a, Tables S3 and S4†). The main differences between **LaPd<sub>12</sub>-closed**, **GaPd<sub>12</sub>**, and **InPd<sub>12</sub>** are the central M–O bond distances with  $\text{La–O} = 2.459(5)$  Å,  $\text{Ga–O} = 2.211(4)$  Å, and  $\text{In–O} = 2.293(4)$  Å, respectively. Notably,  $\text{La}^{3+}$  is the largest trivalent cation ever encapsulated inside a  $\text{Pd}_{12}$  nanocuboid cage and together with the relatively low complexation energy (Table S4†). **LaPd<sub>12</sub>-closed** presents a good test case for the present study. Interestingly, we are also able to synthesize the open nanocube  $[\text{LaPd}_{12}\text{O}_6(\text{OH})_3(\text{PhAsO}_3)_6(\text{OAc})_3]^{3-}$

(**LaPd<sub>12</sub>-open**, see Fig. 5b). This structure had so far only been observed for strontium(II) in the center,  $[\text{SrPd}_{12}\text{O}_6(\text{OH})_3(\text{PhAsO}_3)_6(\text{OAc})_3]^{4-}$ .<sup>10e</sup> This result perfectly supports the above mentioned calculations (Fig. 4 and Table 1), as the energetically lower closed structure **LaPd<sub>12</sub>-closed** is indeed isolated in higher yields compared to the open structure **LaPd<sub>12</sub>-open**. However, our efforts to prepare additional analogues of **MPd<sub>12</sub>-open** ( $\text{M} = \text{La}^{3+}$ ,  $\text{Sr}^{2+}$ ) with other large lanthanide ions have not been successful, suggesting that  $\text{La}^{3+}$  is a unique template amongst all lanthanide ions.

The  $^{13}\text{C}$  and  $^1\text{H}$  NMR spectra indicate good aqueous stability of all four polyanions (Fig. S5 and S6†). Moreover, we also performed  $^{71}\text{Ga}$  and  $^{115}\text{In}$  NMR studies on solutions of **Na-GaPd<sub>12</sub>** and **Na-InPd<sub>12</sub>**, respectively. The observed singlets in  $^{71}\text{Ga}$  NMR centred at 48.9 ppm (**GaPd<sub>12</sub>**, Fig. S7†) and the singlet in  $^{115}\text{In}$  NMR centred at 247.7 ppm (**InPd<sub>12</sub>**, Fig. S8†) are in full agreement with the solid-state structures. The spectra are clean, indicating that no impurities are present, and the signals are rather narrow, in spite of the quadrupolar nature of both isotopes ( $^{71}\text{Ga}$ ,  $S = 3/2$ ;  $^{115}\text{In}$ ,  $S = 9/2$ ), which is a result of the cubic coordination environment around the metal ions combined with the highly symmetrical (cuboctahedral) structure of the overall polyanion, rendering the electric field gradient virtually zero.

We also performed ESI-MS studies in order to study the solution and gas phase properties of **GaPd<sub>12</sub>** and **InPd<sub>12</sub>**. All peaks shown in the spectra can be assigned to species related to **GaPd<sub>12</sub>** and **InPd<sub>12</sub>**, with different numbers of protons or sodium ions attached. For instance, the major envelopes centred at  $m/z = 1025.45$  (Fig. S9a†) and  $m/z = 1041.45$  (Fig. S9b†) can be attributed to the triply negatively charged  $[\text{H}_2\text{GaPd}_{12}]^{3-}$  and  $[\text{H}_2\text{InPd}_{12}]^{3-}$ . Additional MS assignments are summarized in Table S5.†

### 3.5 Selective encapsulation of $\text{Ga}^{3+}$ or $\text{In}^{3+}$ in $\{\text{MPd}_{12}(\text{AsPh})_8\}$ nanocube

To date around 60–70 polyoxopalladates are known, and by far most of them belong to the  $\{\text{MPd}_{12}\text{L}_8\}$  class of nanocubes with being usually d or f block metal ions.<sup>9</sup> However, a competitive study using two or more potential guest cations has never been reported before. Considering that both **GaPd<sub>12</sub>** and **InPd<sub>12</sub>** can be followed by NMR in solution, we decided to perform competition studies for this system on fresh reaction solutions. Interestingly, we observed that if equimolar amounts of  $\text{Ga}^{3+}$  and  $\text{In}^{3+}$  ions were present, then only **InPd<sub>12</sub>** was formed, as confirmed by  $^{71}\text{Ga}$  (no signal) and  $^{115}\text{In}$  NMR (singlet at 254.1 ppm, Fig. 6a). This result indicates that a strong preference exists for **InPd<sub>12</sub>** compared to **GaPd<sub>12</sub>**. The free  $\text{Ga}^{3+}$  ions were detectable by  $^{71}\text{Ga}$  NMR at 0 ppm after the solution had been acidified to pH 1 by 1 M  $\text{HNO}_3$  (Fig. 6b).

For the same mixed, equimolar Ga/In system, the filtrated mother solution was allowed to evaporate until the maximum amount of crystals had formed, which were isolated when still covered by mother liquor. These crystals were analysed by ESI-MS and the spectrum obtained showed peaks corresponding exclusively to **InPd<sub>12</sub>**-related species (Fig. 6c). Notably, the envelopes appearing at  $m/z = 1021.46$  and  $1027.74$  can be unequivocally ascribed to  $\{\text{Na}[\text{InPd}_{12}\text{O}_8(\text{C}_6\text{H}_5\text{AsO}_3)_7(\text{AsO}_3)^+]\}^{3-}$

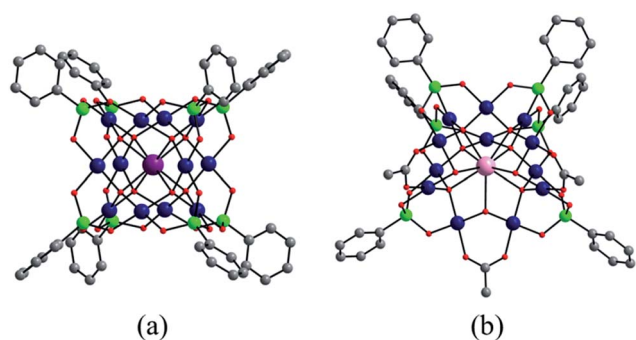


Fig. 5 Ball-and-stick representation of (a) the cuboid-shaped  $\{\text{MPd}_{12}(\text{AsPh})_8\}$  ( $\text{M} = \text{La}^{3+}$ ,  $\text{Ga}^{3+}$ ,  $\text{In}^{3+}$ ) and (b) the open-nanocube **LaPd<sub>12</sub>-open**. Colour code: M (violet), La (pink), Pd (blue), As (green), O (red), C (grey). Hydrogen atoms omitted for clarity.





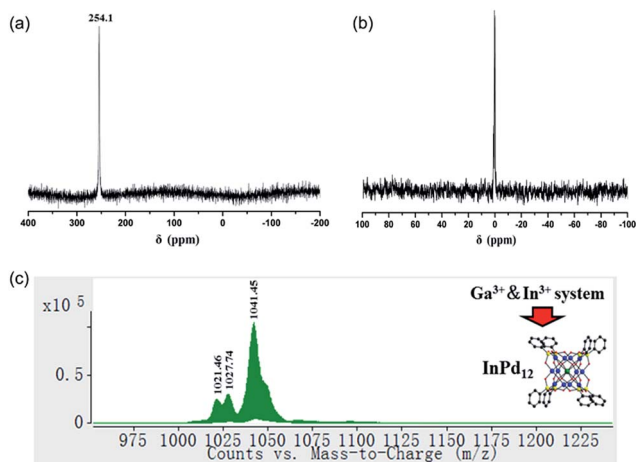


Fig. 6 (a)  $^{115}\text{In}$  NMR spectrum ( $\text{H}_2\text{O}$ , room temperature, pH = 5.5) of a reaction solution for  $\{\text{MPd}_{12}(\text{AsPh})_8\}$  with  $\text{Ga}^{3+}$  and  $\text{In}^{3+}$  ions being present in equimolar amounts; (b)  $^{71}\text{Ga}$  NMR spectrum ( $\text{H}_2\text{O}$ , room temperature, pH = 5.5) of the same reaction solution after being acidified to pH 1; (c) negative ion ESI mass spectrum of  $\{\text{MPd}_{12}(\text{AsPh})_8\}$  crystals collected from the  $\text{Ga}^{3+}$  and  $\text{In}^{3+}$  systems in aqueous solution.

and  $\{\text{Na}[\text{InPd}_{12}\text{O}_8(\text{C}_6\text{H}_5\text{AsO}_3)_7(\text{AsO}_3)](\text{H}_2\text{O})\}^{3-}$ , which may form from the plenary  $\text{InPd}_{12}$  cluster by losing one  $(\text{C}_6\text{H}_5)^-$  fragment, perhaps during the electrospray ionization processes.

We also performed additional competition experiments, for example for the template pairs  $\text{Ga}^{3+}/\text{Sc}^{3+}$  and  $\text{In}^{3+}/\text{Sc}^{3+}$ , respectively. Both  $^{71}\text{Ga}$  and  $^{45}\text{Sc}$  NMR signals could be detected for the  $\text{Ga}^{3+}/\text{Sc}^{3+}$  system after the reaction, indicating that  $\text{GaPd}_{12}$  and  $\text{ScPd}_{12}$  are both formed and coexist in solution (Fig. S10 and S11 $^\dagger$ ). For the  $\text{In}^{3+}/\text{Sc}^{3+}$  system, the  $^{115}\text{In}$  NMR signal for  $\text{InPd}_{12}$

could be detected after a few seconds; whereas the  $^{45}\text{Sc}$  signal for  $\text{ScPd}_{12}$  could only be obtained overnight. These results indicate that selective encapsulation features exist for the central cation guest  $M$  of the  $\text{Pd}_{12}$  nanocube, which fit well with the trends of the computed complexation energies shown in Fig. 4. Combining the theoretical and experimental results, we obtain a selectivity order of  $\text{In}^{3+} > \text{Ga}^{3+} \approx \text{Sc}^{3+}$ . The apparent  $E_{\text{com}}$  difference between  $\text{In}^{3+}$  ( $-137.1 \text{ kcal mol}^{-1}$ ) and  $\text{Ga}^{3+}/\text{Sc}^{3+}$  ( $-116.2/-115.8 \text{ kcal mol}^{-1}$ ) leads indeed to a pronounced encapsulation selectivity for  $\text{In}^{3+}$ , whereas  $\text{Sc}^{3+}$  and  $\text{Ga}^{3+}$  are more difficult to be separated by polyoxopalladate formation, due to similar complexation energies.

### 3.6 Factors governing encapsulation of metal ion templates in different polyoxopalladate shells

In the above mentioned theoretical and experimental studies, we have mainly addressed the two main factors that control incorporation of metal ion guests in the polyoxopalladate nanocube shell  $\text{Pd}_{12}$ : (i) the energy associated with the complexation of a given cation by the empty  $\text{Pd}_{12}$  cage ( $E_{\text{com}}$ ) and (ii) how the guest fits inside the host cage. In order to gain a deeper understanding of the intrinsic factors governing formation of  $\{\text{MPd}_{12}\text{L}_8\}$ , we decided to perform an energy decomposition analysis for  $E_{\text{com}}$ . From an energetic point of view, we can subdivide the encapsulation process of the cation guest in three steps: (i) dehydration of the cation, (ii) deformation of the  $\text{Pd}_{12}$  host shell, and (iii) binding between the cation and the  $\text{Pd}_{12}$  host. Thus,  $E_{\text{com}}$  can be expressed as the sum of  $\Delta E_{\text{def}} + \Delta E_{\text{dehyd}} + \Delta E_{\text{bind}}$ . In Fig. 7, the values computed for  $\Delta E_{\text{def}}$ ,  $\Delta E_{\text{dehyd}}$ , and  $\Delta E_{\text{bind}}$  for a series of cation guests are

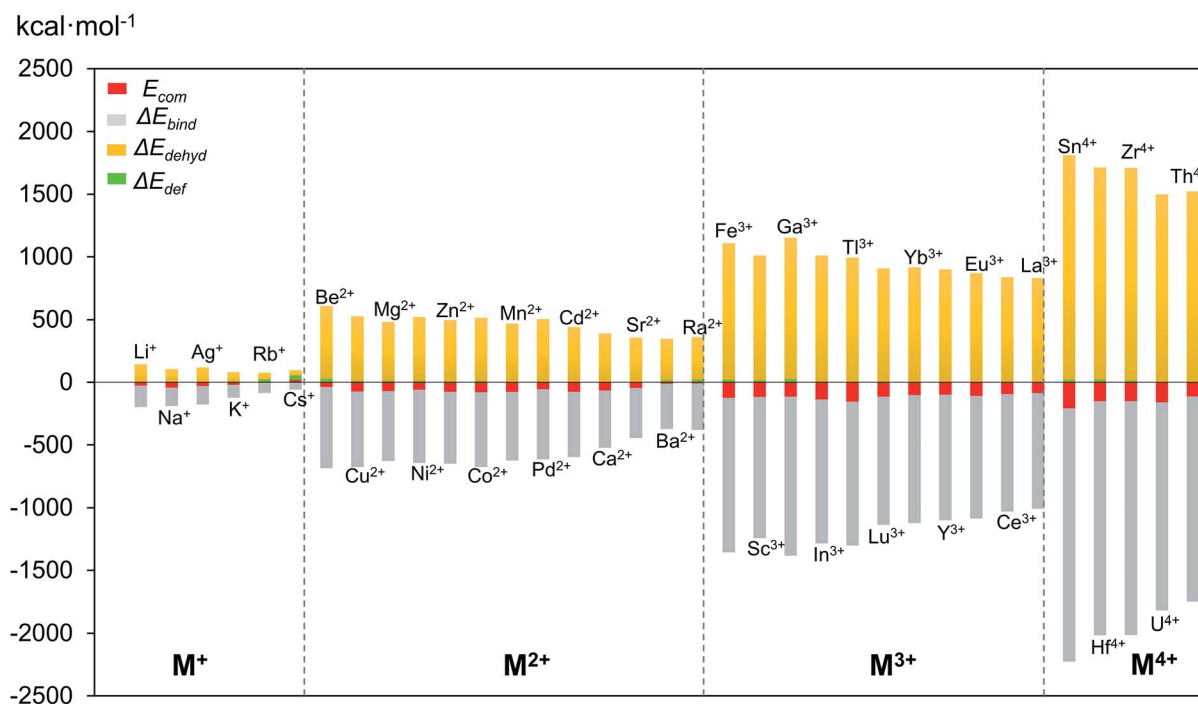


Fig. 7 Complexation energy  $E_{\text{com}}$  (in  $\text{kcal mol}^{-1}$ ) of  $M^{n+}$  encapsulated in  $\text{Pd}_{12}\text{L}_8$  ( $L = \text{PhAs}$ ) host shell and its decomposition terms  $\Delta E_{\text{dehyd}}$ ,  $\Delta E_{\text{bind}}$  and  $\Delta E_{\text{def}}$ .





classified according to the cation charge. It becomes apparent that in absolute values  $\Delta E_{\text{def}}$  is much smaller than  $\Delta E_{\text{dehyd}}$  and  $\Delta E_{\text{bind}}$ , and that these two latter terms are very dependent on the cation charge. The complexation energy for di- and trivalent cation guests is respectively two or three times more exothermic than for monovalent cations, due to increasing charge-dipole and charge-charge interactions.

The dehydration energy ( $\Delta E_{\text{dehyd}}$ ) of the cation guest  $M$  and the electrostatic interaction ( $\Delta E_{\text{bind}}$ ) between  $M$  and the  $\text{Pd}_{12}$  nanocage exhibit large values, and in all cases  $\Delta E_{\text{bind}}$  is larger than the sum  $\Delta E_{\text{dehyd}} + \Delta E_{\text{def}}$ , consequently, the  $E_{\text{com}}$  term is always negative and hence exothermic. However, this does not mean that  $\Delta E_{\text{bind}}$  alone is sufficient to describe the  $E_{\text{com}}$  trend. In Table 2 three examples are shown indicating that in absolute value  $\Delta E_{\text{bind}}$  is indeed dominant, but this term alone does not allow predicting the correct trend for  $E_{\text{com}}$ . For example, let us consider the cation guest pair  $\text{Ga}^{3+}/\text{In}^{3+}$ , for which experiments clearly demonstrated that  $\text{In}^{3+}$  is captured preferentially over  $\text{Ga}^{3+}$ . The more negative value for  $E_{\text{com}}$  for  $\text{In}^{3+}$  originates essentially from the large deformation energy of  $25.7 \text{ kcal mol}^{-1}$  for  $\text{Ga}^{3+}$  (vs.  $8.4 \text{ kcal mol}^{-1}$  for  $\text{In}^{3+}$ ). The other two energy terms ( $\Delta E_{\text{bind}}$  and  $\Delta E_{\text{dehyd}}$ ) are significantly larger in absolute terms for  $\text{Ga}^{3+}$  than  $\text{In}^{3+}$ , but they cancel each other out. Notice that the  $\text{Pd}_{12}$  host cage deforms significantly more for  $\text{Ga}^{3+}$  than  $\text{In}^{3+}$ , because the former is rather small.

For the  $\text{Lu}^{3+}/\text{Yb}^{3+}$  pair, it can be noticed from the values in Table 2 that  $\text{Lu}^{3+}$  has a more negative complexation energy by  $12 \text{ kcal mol}^{-1}$ . The radii of both ions are virtually identical and the deformation and binding energies are rather similar, and so it can be concluded that the dehydration energy is the critical term in this case.

Finally, the third ion pair  $\text{Ce}^{3+}/\text{La}^{3+}$  allows to identify the relevance of electronic structure. The  $\text{La}^{3+}$  and  $\text{Ce}^{3+}$  ions have the same charge and essentially identical ionic radii, but the larger atomic number for  $\text{Ce}^{3+}$  leads to a higher effective nuclear charge and due to the low shielding of  $f$  electrons  $\text{Ce}^{3+}$  has a larger (more negative) binding energy than  $\text{La}^{3+}$ , which in turn leads to a higher (more negative) complexation energy for the former.

In summary,  $E_{\text{com}}$  depends mainly on the following four properties of the metal ion guest: (i) effective ionic radius, (ii) valence state, (iii) dehydration ability, and (iv) electronic configuration and resulting charge-accepting ability. The selectivity for a given cation guest is the result of a delicate

balance between the cation-polyoxopalladate and the cation-solvent interactions.

## 4. Conclusions

In host-guest or template-based chemistry, one of the challenges is to know the exact role that ions or small fragments play in the formation of a given species. Ever since the discovery in 2008 of the archetypal polyoxopalladate  $[\text{H}_6\text{Pd}_{12}\text{O}_8(\text{As}^{\text{V}}\text{O}_4)_8]^{8-}$  ( $\text{Pd}_{13}$ ), which can be described as a  $\{\text{Pd}_{12}\text{O}_8(\text{AsO}_4)_8\}$  nanocube encapsulating a central  $\text{Pd}^{2+}$  ion with square-planar coordination geometry, about 50 more polyoxopalladate nanocubes  $\{\text{MPd}_{12}\text{L}_8\}$  with different central metal ion guests  $M$  and capping groups  $L$  have been reported. However, the main factors that govern the experimental formation of a particular polyoxopalladate (and the non-formation of others) are not well understood. Here, combining experimental and computational chemistry, we have been able to rationalize why a polyoxopalladate shell self-assembles around a particular cation template guest more preferentially than others.

The prototype  $\text{Pd}_{13}$  is formed by condensation of  $[\text{Pd}(\text{H}_2\text{O})_4]^{2+}$  complex cations in the presence of arsenate anion heterogroups. Nevertheless, if the solution contains other cations  $M^{n+}$ , then in principle  $\{\text{MPd}_{12}\text{L}_8\}$  type species may also be formed, determined by the favourable complexation energy and the relative competition with respect to  $\text{Pd}^{2+}$  ions. After an exhaustive computational analysis of complexation and dehydration energies for a series of cation guests we were able to identify the most promising cations to be encapsulated inside the  $\text{Pd}_{12}$  nanocube shell. Trivalent and tetravalent cations are easily trapped inside  $\text{Pd}_{12}$ , whereas monovalent cations are largely elusive. As based on the calculations, we also performed target-oriented synthetic studies and we were able to isolate four novel polyoxopalladates: (i) the  $\text{La}^{3+}$ -centered nanocube  $[\text{LaPd}_{12}\text{O}_8(\text{PhAsO}_3)_8]^{5-}$  (**LaPd<sub>12</sub>-closed**), the  $\text{La}^{3+}$ -centered "open" nanocube  $[\text{LaPd}_{12}\text{O}_6(\text{OH})_3(\text{PhAsO}_3)_6(\text{OAc})_3]^{3-}$  (**LaPd<sub>12</sub>-open**), the  $\text{Ga}^{3+}$ -centered  $[\text{GaPd}_{12}\text{O}_8(\text{PhAsO}_3)_8]^{5-}$  (**GaPd<sub>12</sub>**), and the  $\text{In}^{3+}$ -analogue  $[\text{InPd}_{12}\text{O}_8(\text{PhAsO}_3)_8]^{5-}$  (**InPd<sub>12</sub>**). All four compounds were fully characterized in the solid state, in solution, and in the gas phase. In particular  $^{115}\text{In}$  and  $^{75}\text{Ga}$  NMR combined with mass spectrometry were very useful, as these techniques allowed to perform speciation studies. We demonstrated that in solutions containing  $\text{In}^{3+}$  and  $\text{Ga}^{3+}$  ions only the former is incorporated in the  $\text{Pd}_{12}$  shell, due to its more suitable size and higher complexation energy. DFT method also predicted that the large  $\text{La}^{3+}$  ion should fit in the  $\text{Pd}_{12}$  host shell. The experimental work following the computations indeed resulted in the successful synthesis of the regular nanocube **LaPd<sub>12</sub>-closed** as well as the open-shell structure **LaPd<sub>12</sub>-open**. These results reemphasize that size and dehydration energy of the cation guest are the key driving forces in the formation mechanism of nanocuboid polyoxopalladates of the type  $\{\text{MPd}_{12}\text{L}_8\}$ . Our work has demonstrated how powerful the interplay between theory and experiment can be. We predict that other cations such as  $\text{Cd}^{2+}$ ,  $\text{Tl}^{3+}$ ,  $\text{Sn}^{4+}$ ,  $\text{Zr}^{4+}$ ,  $\text{Hf}^{4+}$ ,  $\text{U}^{4+}$ , and  $\text{Th}^{4+}$  amongst others are potential candidates for encapsulation inside the  $\text{Pd}_{12}$  host and our efforts are geared in this direction.

**Table 2** Complexation energy and decomposition analysis terms (all in units of  $\text{kcal mol}^{-1}$ ) for three groups of cation guests encapsulated in  $\text{Pd}_{12}\text{L}_8$  ( $L = \text{PhAs}$ ) host shell

$M^{n+}$	$E_{\text{com}}$	$\Delta E_{\text{def}}$	$\Delta E_{\text{bind}}$	$\Delta E_{\text{dehyd}}$	Ionic radius	Critical energy term
$\text{Ga}^{3+}$	−115.8	25.7	−1267.1	1125.5	0.92	$\Delta E_{\text{def}}$
$\text{In}^{3+}$	−137.1	8.4	−1146.9	1001.5	1.06	
$\text{Lu}^{3+}$	−115.0	5.7	−1021.2	900.5	1.12	$\Delta E_{\text{dehyd}}$
$\text{Yb}^{3+}$	−103.0	4.9	−1018.4	910.5	1.13	
$\text{Ce}^{3+}$	−95.5	5.8	−935.2	833.9	1.28	$\Delta E_{\text{bind}}$
$\text{La}^{3+}$	−86.3	3.9	−920.6	830.4	1.30	



## Conflicts of interest

There are no conflicts to declare.

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