

Cite this: *Chem. Sci.*, 2017, 8, 7528

# Nb<sub>2</sub>@Au<sub>6</sub>: a molecular wheel with a short Nb≡Nb triple bond coordinated by an Au<sub>6</sub> ring and reinforced by $\sigma$ aromaticity†

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We report a photoelectron spectroscopy and high-resolution photoelectron imaging study of a bimetallic Nb<sub>2</sub>Au<sub>6</sub><sup>-</sup> cluster. Theoretical calculations, in conjunction with the experimental data, reveal that Nb<sub>2</sub>Au<sub>6</sub><sup>-/0</sup> possess high-symmetry D<sub>6h</sub> structures featuring a Nb–Nb axis coordinated equatorially by an Au<sub>6</sub> ring. Chemical bonding analyses show that there are two  $\pi$  bonds and one  $\sigma$  bond in the Nb<sub>2</sub> moiety in Nb<sub>2</sub>@Au<sub>6</sub>, as well as five totally delocalized  $\sigma$  bonds. The Nb≡Nb triple bond is strengthened significantly by the delocalized  $\sigma$  bonds, resulting in an extremely short Nb–Nb bond length comparable to the quintuple bond in gaseous Nb<sub>2</sub>. The totally delocalized  $\sigma$  bonding in Nb<sub>2</sub>@Au<sub>6</sub> is reminiscent of  $\sigma$  aromaticity, representing a new bonding mode in metal–ligand systems. The unusually short Nb–Nb bond length in Nb<sub>2</sub>@Au<sub>6</sub> shows that the Au<sub>6</sub> ring can serve as a bridging ligand to facilitate multiple bonding in transition metal dimers *via* delocalized  $\sigma$  bonding.

Received 30th June 2017  
Accepted 13th September 2017

DOI: 10.1039/c7sc02881d

rsc.li/chemical-science

## 1. Introduction

Due to the strong relativistic effects,<sup>1</sup> negatively charged gold clusters can be planar up to a surprisingly large size.<sup>2</sup> The Au<sub>6</sub> cluster is very special with a huge energy gap between its highest occupied (HOMO) and lowest unoccupied molecular orbitals (LUMO), as revealed in the photoelectron spectra of Au<sub>6</sub><sup>-</sup>.<sup>2a,3</sup> On the basis of vibrationally-resolved photodetachment spectroscopy, Au<sub>6</sub> was initially deduced to have a D<sub>6h</sub> ring structure,<sup>3b</sup> but was later confirmed to have a D<sub>3h</sub> triangular structure.<sup>2</sup> The high electronic stability of Au<sub>6</sub> is due to  $\sigma$  aromaticity from its delocalized  $\sigma$  electrons,<sup>4</sup> as is also found in the isoelectronic Au<sub>5</sub>Zn<sup>+</sup> cluster.<sup>5</sup> Photoelectron spectroscopy (PES) of MAu<sub>6</sub><sup>-</sup> (M = Ti, V,

Cr) along with density functional theory (DFT) calculations found these doped-clusters to have planar structures featuring an Au<sub>6</sub> ring with a central transition metal atom (M@Au<sub>6</sub><sup>-</sup>) with variable magnetic moments.<sup>6</sup> It was shown that, while the out-of-plane 3d orbitals of the transition-metal atoms do not participate in bonding with Au, the in-plane  $d_{xy}$  and  $d_{x^2-y^2}$  orbitals are important to maintain the disk structure due to bonding interactions with the Au<sub>6</sub> ring. Subsequent DFT calculations found that Au<sub>6</sub> doped with 3d transition metals all have similar M@Au<sub>6</sub> disk structures for M = Sc–Ni,<sup>7</sup> whose electronic structures were also rationalized using an electron shell model.<sup>8</sup> Thus, the Au<sub>6</sub> ring provides a good host for a central transition metal atom with tunable magnetic properties.

In the current study, we report the observation of Nb<sub>2</sub>@Au<sub>6</sub><sup>-/0</sup> molecular wheels, in which an Au<sub>6</sub> ring is hosting a Nb≡Nb triple bond equatorially. The first report in 1965 by Cotton *et al.* of K<sub>2</sub>[Re<sub>2</sub>Cl<sub>8</sub>]·2H<sub>2</sub>O with a quadruple bond ( $\sigma^2\pi^4\delta^2$ ) between the two Re atoms opened the field of metal–metal multiple bonds.<sup>9</sup> The  $\sigma$ ,  $\pi$ , and  $\delta$  bonds between two transition metal atoms (M<sub>2</sub>) are mainly formed by the overlap of their d orbitals with the same symmetry. Employing bulky or bridging ligands, Cr<sub>2</sub> complexes containing a quintuple bond ( $\sigma^2\pi^4\delta^4$ ) have also been successfully synthesized.<sup>10</sup> The quintuple bonded complexes synthesized so far are mainly related to group VI metals.<sup>11</sup> Although gaseous Nb<sub>2</sub> is characterized to possess a quintuple Nb–Nb bond with a  $1\pi^4_1\sigma^2_g2\sigma^2_g1\delta^2_g$  electron configuration,<sup>12</sup> synthesized diniobium complexes usually contain a Nb<sub>2</sub><sup>4+</sup> core and maintain a Nb–Nb triple bond at the most.<sup>9b,13</sup> To surpass the Nb–Nb triple bond, a Nb<sub>2</sub> complex needs to free more d electrons from metal–ligand bonding to participate metal–metal  $\delta$  bonding.

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† Electronic supplementary information (ESI) available: Photoelectron spectra of Nb<sub>2</sub>Au<sub>6</sub><sup>-</sup> at (a) 616.86 nm, (b) 610.55 nm, (c) 603.38 nm, and (d) 589.58 nm; relative energies of low-lying isomers of Nb<sub>2</sub>Au<sub>6</sub><sup>-</sup> within 1.5 eV at the PW91, PBE0 (in square brackets), CCSD (in braces) and CCSD(T) (in angle brackets) levels; the four lowest-lying isomers of Nb<sub>2</sub>Au<sub>6</sub> at the levels of PW91 and PBE0; valence canonical molecular orbital contours for the D<sub>6h</sub> Nb<sub>2</sub>Au<sub>6</sub><sup>-</sup> at the PBE0 level; comparison between the 193 nm spectrum of Nb<sub>2</sub>Au<sub>6</sub><sup>-</sup> with the simulated spectra of isomers I and II at the PW91/Def2-TZVPPD and BP86/Def2-TZVPPD levels; comparison between the 193 nm spectrum of Nb<sub>2</sub>Au<sub>6</sub><sup>-</sup> with the simulated spectra of isomer I at PBE0/Def2-TZVPPD and TPSSh/Def2-TZVPPD levels; the energy difference between isomers I and II of Nb<sub>2</sub>Au<sub>6</sub><sup>-</sup> calculated at various levels of theory; the first VDEs of isomers I, II, III, IV and V of Nb<sub>2</sub>Au<sub>6</sub><sup>-</sup> computed at the PW91 and PBE0 levels; calculated vibrational frequencies for the D<sub>6h</sub> global minimum of Nb<sub>2</sub>Au<sub>6</sub> at PW91 and PBE0 levels; calculated bond orders and charges of D<sub>∞h</sub> Nb<sub>2</sub>, D<sub>6h</sub> Au<sub>6</sub>, and D<sub>6h</sub> Nb<sub>2</sub>Au<sub>6</sub> at the PBE0/Def2-TZVP level. See DOI: 10.1039/c7sc02881d



The  $\text{Nb}_2\text{Au}_6^-$  cluster anions were produced by a laser vaporization supersonic cluster source and characterized by a magnetic-bottle PES analyzer,<sup>14</sup> as well as high-resolution velocity-map imaging (VMI).<sup>15</sup> Global minimum searches along with high-level quantum calculations reveal that the  $D_{6h}$   $\text{Nb}_2\text{Au}_6^{-/0}$  molecular wheels are the most stable structures. Chemical bonding analyses show that there are one  $\sigma$  bond and two  $\pi$  bonds in the  $\text{Nb}_2$  moiety, and five totally delocalized  $\sigma$  bonds in  $\text{Nb}_2\text{Au}_6$ . An extremely short Nb–Nb bond length is observed, showing that the  $\text{Au}_6$  ring can serve as a bridging ligand to facilitate multiple bonding in  $\text{Nb}_2$  *via* delocalized  $\sigma$  bonding.

## 2. Experimental methods

The  $\text{Nb}_2\text{Au}_6^-$  cluster was studied using two different PES apparatuses. The experiment was first carried out using a magnetic-bottle PES apparatus equipped with a laser vaporization supersonic cluster source, details of which has been published elsewhere.<sup>14</sup> The second harmonic radiation (532 nm) from a Nd:YAG laser was used to vaporize a disk target compressed from niobium and gold powders. A helium carrier gas seeded with 5% argon was used to quench the plasma, initiating nucleation and cluster formation. Clusters formed in the nozzle were entrained in the carrier gas and underwent a supersonic expansion. The anionic clusters were extracted from the collimated cluster beam and analyzed by a time-of-flight (TOF) mass spectrometer. The  $\text{Nb}_2\text{Au}_6^-$  anion of interest was mass-selected, decelerated and photodetached by a laser beam at 193 nm from an ArF excimer laser, and 266 nm from a Nd:YAG laser. Photoelectrons were collected at nearly 100% efficiency and analyzed in a 3.5 meter long electron flight tube. The photoelectron spectra were calibrated by the known spectra of  $\text{Au}^-$  or  $\text{Bi}^-$ . The energy resolution of the apparatus was  $\Delta E_k/E_k \approx 2.5\%$ , that is,  $\sim 25$  meV for 1 eV electrons.

High-resolution PES experiment was then performed using a VMI apparatus, which has been previously described in detail.<sup>15</sup> The cluster source and TOF mass spectrometer are similar to the magnetic-bottle PES apparatus. The  $\text{Nb}_2\text{Au}_6^-$  cluster was mass selected before entering the imaging detector. A laser beam from a 355 nm pumped Deyang dye laser was used to detach electrons from the cluster anions. A voltage of  $-300$  V was used on the repeller of the imaging lens.<sup>15</sup> The electrons were focused onto a microchannel plate (MCP) coupled with a phosphorus screen and charged-coupled device (CCD) camera for detection. The experiments required between 30 000 and 200 000 laser shots to achieve a satisfactory signal-to-noise ratio. Images were analyzed with the maximum entropy concept using the MEVELER program.<sup>16</sup> The detector was calibrated using the well-known detachment energy of  $\text{Au}^-$  at various photon energies.

## 3. Theoretical methods

Global minimum searches were carried out for  $\text{Nb}_2\text{Au}_6^-$  using the simulated annealing algorithm<sup>17</sup> coupled with density functional theory (DFT) geometric optimization. The PW91 (ref.

18) functional with the Los Alamos basis set and effective core potential (LANL2DZ)<sup>19</sup> on both Au and Nb atom was used in the initial structure searches. Low-lying isomers from the initial searches were refined at PW91 and PBE0 (ref. 20) levels of theory using the Def2-TZVPPD basis set<sup>21</sup> and the Stuttgart–Dresden (SDD) relativistic pseudopotentials (ECP28MDF for Nb and ECP60MDF for Au).<sup>22</sup> Vibrational frequencies of the low-lying isomers were calculated to ensure they are true energy minima. All the DFT calculations were carried out using Gaussian 09.<sup>23</sup> Single-point energies of the five lowest isomers were calculated using the coupled-cluster theory with single, double and perturbative triple excitations [CCSD(T)]<sup>24</sup> implemented in Molpro 2015.1.<sup>25</sup>

The first vertical detachment energy (VDE) was computed as the energy difference between the neutral and the anion at the optimized geometry of the anion. The first adiabatic detachment energy (ADE) was computed as the energy difference between the optimized anion and the neutral. Further VDEs were approximated by adding excitation energies from the time-dependent density functional theory (TDDFT)<sup>26</sup> calculations to the first vertical detachment energy. The simulated spectrum was obtained by fitting a unit-area Gaussian function of 0.03 eV width to each VDE. The ezSpectrum program was employed to calculate Franck–Condon factors, which were fitted with a unit-area Gaussian function of 2 meV width (FWHM) to simulate the vibrational features.<sup>27</sup> Natural population analyses (NPA) were carried out to illustrate the charge distribution on the neutral  $\text{Nb}_2\text{Au}_6$  cluster.<sup>28</sup> A charge decomposition analysis (CDA)<sup>29</sup> was done using the Multiwfn program<sup>30</sup> to describe the interaction between the  $\text{Au}_6$  ring and the  $\text{Nb}_2$  axis. Chemical bonding analyses were done using the adaptive natural density partitioning (AdNDP)<sup>31</sup> method at the PBE0/Def2-TZVP level of theory. The structural and chemical bonding pictures were visualized by GaussView<sup>32</sup> and Molekel.<sup>33</sup>

## 4. Experimental results

Fig. 1 displays the photoelectron spectra of  $\text{Nb}_2\text{Au}_6^-$  at 266 nm and 193 nm from the magnetic-bottle PES apparatus, which are compared with the simulated spectrum. The PES bands are labeled as X, A, B... which denote detachment transitions from the ground electronic state of the anion to the ground (X) and excited electronic states (A, B...) of neutral  $\text{Nb}_2\text{Au}_6$ . The VDEs of the electronic transitions are measured from the peak maxima and summarized in Table 1, where they are compared with theoretical calculations. The high-resolution spectra shown in Fig. 2 and S1† are taken from the VMI apparatus. The peaks labeled in lower case letters (a, b, c...) represent the vibrational levels resolved for the ground electronic state of neutral  $\text{Nb}_2\text{Au}_6$ . The binding energies and the corresponding assignments for the vibrational features are summarized in Table 2.

The 266 nm spectrum (Fig. 1a) displays a sharp ground-state band X around 2.0 eV. Following a large energy gap of  $\sim 1.25$  eV, a relatively broad band A at 3.25 eV is observed, as well as three more bands (B, C, D) at VDEs of 3.48, 3.79, and 4.11 eV, respectively. Following another energy gap after band D, more congested features are observed above 5 eV in the 193 nm



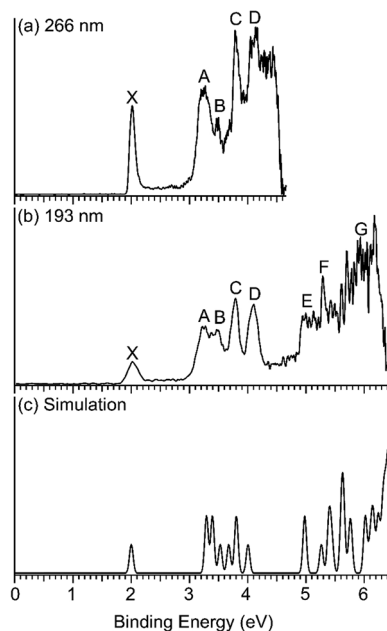


Fig. 1 Photoelectron spectra of  $\text{Nb}_2\text{Au}_6^-$  at (a) 266 nm (4.661 eV) and (b) 193 nm (6.424 eV) obtained from the magnetic-bottle PES apparatus, and (c) comparison with the simulated spectrum of the  $D_{6h}$  global minimum at PBE0/Def2-TZVPPD. The theoretical first VDE is shifted to align with the experimental first VDE, while the higher theoretical VDEs are shifted accordingly (see Table 1).

spectrum (Fig. 1b). The labels E, F, and G are given tentatively for the sake of discussion. The large gap between the X and A bands suggests that neutral  $\text{Nb}_2\text{Au}_6$  is closed shell with a large

HOMO–LUMO gap, indication of a very stable electronic system. A series of high-resolution spectra were obtained using the VMI PES apparatus to resolve vibrational structures for the ground-state transition. Three are shown in Fig. 2 and three more are given in Fig. S1.† The 589.58 nm spectrum (Fig. 2c) yields two main vibrational progressions with frequencies of 408 and  $128\text{ cm}^{-1}$ . The short vibrational progressions suggest a minimal geometry change between the anionic and neutral ground states and high symmetries for  $\text{Nb}_2\text{Au}_6^{-/0}$ . More weak vibrational features are resolved in the spectra at even lower photon energies (Fig. 2a and b). The 618.11 nm spectrum (Fig. 2a) defines the most accurate 0–0 transition at  $1.9969 \pm 0.0004\text{ eV}$ , which represents the first VDE and ADE, as well as the electron affinity (EA) of neutral  $\text{Nb}_2\text{Au}_6$ . The peak *d* resolved in Fig. S1a† has a line width of  $2\text{ cm}^{-1}$ , which is the narrowest peak resolved in PE imaging for any molecular systems.<sup>34</sup>

## 5. Theoretical results

The optimized low-lying isomers of  $\text{Nb}_2\text{Au}_6^-$  within 1.5 eV of the global minimum are given in Fig. S2.† All the low-lying isomers were found to have the six Au atoms arranged around a  $\text{Nb}_2$  moiety. Structures with two separated Nb atoms were all much higher in energy. At the PW91/Def2-TZVPPD level, the top five isomers are within 0.1 eV of each other with isomer II ( $D_{3d}$ ,  $^2A_{2u}$ ) being the lowest in energy. Isomer I ( $D_{6h}$ ,  $^2A_{2u}$ ) is a close-lying isomer, but shows a small imaginary frequency ( $16.5i\text{ cm}^{-1}$ ) at PW91/Def2-TZVPPD level. Distortion along this mode of imaginary frequency led to the  $D_{3d}$  isomer II. At the PBE0/Def2-TZVPPD level, isomer I was found to be the most stable

Table 1 Observed photodetachment transitions and their vertical detachment energies (VDE) for  $\text{Nb}_2\text{Au}_6^-$  in comparison with theoretical calculations at the TD-PBE0/Def2-TZVPPD level and the final electronic states and electron configurations. All energies are in eV

	VDE(exp) <sup>a</sup>	Final states and electronic configuration <sup>b</sup>	PBE0 <sup>c</sup>
X	1.9969(4)	$^1A_{1g} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^0$	2.00
A	3.25(3)	$^3E_{1g} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	3.29
		$^3A_{2u} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{1g}^4 5e_{1u}^4 2a_{2u}^1$	3.39
		$^1E_{1g} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	3.53
C	3.79(3)	$^1A_{2u} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{1g}^4 5e_{1u}^4 2a_{2u}^1$	3.67
		$^3E_{2u} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	3.80
D	4.11(5)	$^1E_{2u} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	4.00
E	~5.0	$^3E_{1g} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{1g}^4 5e_{1u}^4 2a_{2u}^1$	4.98
F	~5.3	$^1E_{1g} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	5.26
		$^3A_{1u} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	5.40
		$^1A_{1u} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	5.45
		$^3B_{2g} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{1g}^4 5e_{1u}^4 2a_{2u}^1$	5.61
		$^3A_{2g} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	5.64
		$^1A_{2g} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	5.75
G	~5.9	$^1B_{2g} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{1g}^4 5e_{1u}^4 2a_{2u}^1$	5.77
		$^3E_{1u} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	6.02
		$^1E_{1u} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{1g}^4 5e_{1u}^4 2a_{2u}^1$	6.10
		$^3E_{2u} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	6.15
		$^3B_{1u} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	6.24
		$^3B_{2g} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{1g}^4 5e_{1u}^4 2a_{2u}^1$	6.32
		$^3E_{2g} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	6.36
$^3E_{1g} \dots 2e_{2u}^4 3e_{1u}^4 3e_{2g}^4 1b_{1u}^2 1b_{2g}^2 2e_{1g}^4 1a_{1u}^2 2b_{1u}^2 1a_{2g}^2 4e_{1u}^4 4e_{2g}^4 4a_{2g}^4 5e_{1u}^4 2a_{2u}^1$	6.40		

<sup>a</sup> Numbers in the parentheses are the uncertainty in the last digit. <sup>b</sup> The orbitals shown in bold face indicate the major electron detachment channels. <sup>c</sup> The first VDE was computed to be 1.79 eV (see Table S2), but shifted to align with the experimental value. All higher VDEs are shifted accordingly to better compare with the experimental data.



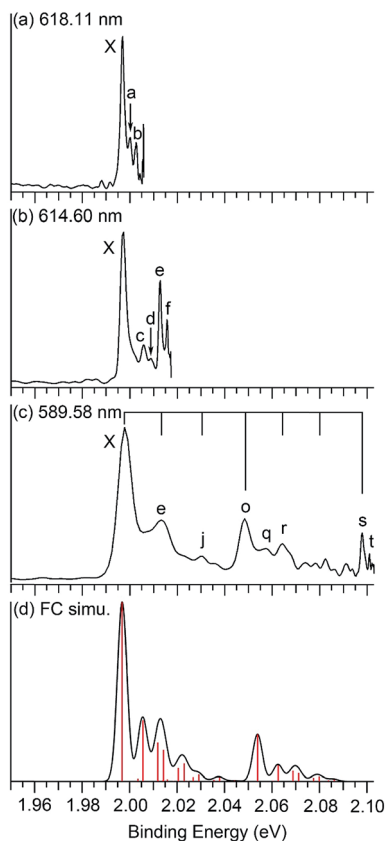


Fig. 2 Photoelectron spectra of  $\text{Nb}_2\text{Au}_6^-$  at (a) 618.11 nm (2.0059 eV), (b) 614.60 nm (2.0173 eV), and (c) 589.58 nm (2.1029 eV) obtained from the VMI PES apparatus, and (d) the Franck–Condon simulation. The black vertical lines in (c) indicate the vibrational progressions of the two totally symmetric modes,  $\nu_8$  (short lines) and  $\nu_{12}$  (long lines) (see Fig. 4 and Table 2). The red vertical lines in (d) represent the calculated Franck–Condon factors.

structure, while isomers II and III optimized to isomer I. The energy difference between isomers I and II was also calculated using different density functionals, which are summarized in Table S1.† Isomer II was calculated to be slightly more stable at PW91, PBE0, BP86, B3PB6, and TPSS levels, while isomer I was calculated to be more stable at PBE0, TPSSh, and LC- $\omega$ PBE levels.<sup>35</sup> This discrepancy in relative energies and imaginary frequency suggests that the choice of density functional is important to describe the potential energy surface correctly. To establish a better relative energy order, we calculated single-point energies at the CCSD/Def2-TZVPPD and CCSD(T)/Def2-TZVPPD levels for isomers I–V at the PW91/Def2-TZVPPD structures. At the CCSD and CCSD(T) levels, we found isomer I was most stable, while the second lowest-lying isomer II was 0.029 eV and 0.066 eV higher in energy, respectively. The imaginary frequency of isomer I at PW91/Def2-TZVPPD level is likely to be a result of computational artifact. The optimized neutral structures are shown in Fig. S3,† where the  $D_{6h}$  structure is found to be appreciably more stable at both the PW91/Def2-TZVPPD and PBE0/Def2-TZVPPD levels of theory. The optimized structures of  $\text{Nb}_2\text{Au}_6^-$  and  $\text{Nb}_2\text{Au}_6$  are nearly identical with only minor bond length changes, as shown in Fig. 3.

## 6. Comparison between experiment and theory

To compare with the experimental data, we computed the first ADE and VDE of isomers I–V at the PW91 and PBE0 levels, as given in Table S2.† It was shown previously that the PW91 functional was excellent in predicting the first ADE and VDE for the  $\text{M}@\text{Au}_6^-$  clusters.<sup>6a</sup> Indeed, we found that the calculated first ADE (2.01 eV) and VDE (2.02 eV) of isomer I at PW91 are in good agreement with the experimental ADE and VDE of 1.9969 eV, whereas the first VDEs computed for isomers II–V at PW91 are much larger. Furthermore, the large differences between the first ADE and VDE predicted for isomers II–V at PW91 are also inconsistent with the observed sharp band X. The first calculated VDE (1.79 eV) and ADE (1.77 eV) at the PBE0 level for isomer I are slightly lower than the experimental values. These results are consistent with previous observations that the PBE0 functional tends to underestimate the first VDEs of gold clusters by 0.1–0.3 eV.<sup>36</sup> Since isomers II–IV are not stable at the PBE0 level (Fig. S2†), their first VDE and ADE could not be computed at this level of theory. The calculated first ADE and VDE of isomer V are much larger than the experimental value at the PBE0 level. At both PW91 and PBE0 levels, only the calculated first VDE and ADE of isomer I are consistent with the observed band X.

We further computed the vibrational frequencies for the neutral  $D_{6h}$  global minimum at the PW91 and PBE0 levels, as given in Table S3.† There are only two totally symmetric fundamental modes (Fig. 4) for the  $D_{6h}$  structure, the ring breathing ( $\nu_8$ : 121  $\text{cm}^{-1}$  at both PW91 and PBE0) and the Nb–Nb stretching ( $\nu_{12}$ : 423  $\text{cm}^{-1}$  at PW91 and 460  $\text{cm}^{-1}$  at PBE0). To better compare with the vibrationally-resolved spectra in Fig. 2 and S1,† we also calculated the Franck–Condon factors for the detachment transition from the ground state of the  $D_{6h}$  anion ( $^2A_{2u}$ ) to that of the  $D_{6h}$  neutral ( $^1A_{1g}$ ) using output files at the PBE0 level.<sup>27</sup> The Franck–Condon simulated spectrum of isomer I is shown in Fig. 2d. Apart from the two totally symmetric fundamental modes, the totally symmetric overtone of the out-of-plane bending mode ( $\nu_2$ : 32  $\text{cm}^{-1}$  at PW91 and 35  $\text{cm}^{-1}$  at PBE0) also gives a significant Franck–Condon factor. Most of the observed vibrational features can be assigned to the combination/overtone of these three modes ( $2\nu_2$ ,  $\nu_8$ , and  $\nu_{12}$ ), as shown in Table 2. Several low frequency modes involving ring distortions are also observed (Fig. 2 and S1†) and the observed frequencies for these weak vibrational features are also in good agreement with the calculated frequencies (Table 2). The Franck–Condon factors of the transition from the ground state of the  $D_{3d}$  anion ( $^2A_{2u}$ ) to that of the  $D_{6h}$  neutral ( $^1A_{1g}$ ) are negligible, ruling out the possibility of contributions from isomer II to the observed vibrational features. The excellent agreement between the computed first detachment energies and Franck–Condon factors for isomer I and the experimental data confirms firmly the  $D_{6h}$  global minimum for both  $\text{Nb}_2\text{Au}_6^-$  and  $\text{Nb}_2\text{Au}_6$ . The observation of the weak vibrational features involving the ring distortion modes indicate that the  $\text{Au}_6$  ring is somewhat floppy in the anion.



**Table 2** Observed vibrational peaks, binding energies (BEs), and the corresponding assignments. Vibrational levels from the totally symmetric vibrational modes are in boldface

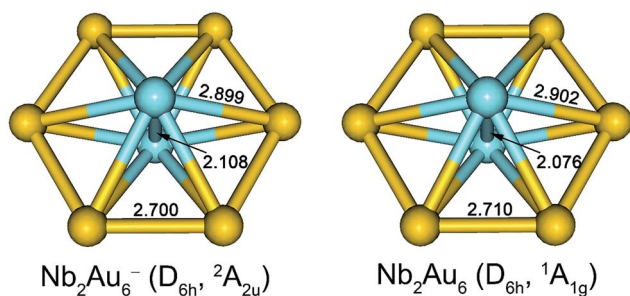
Peak	BE (eV)	$\Delta E$ (cm <sup>-1</sup> )	Assignment	Symmetry	Calculated <sup>a</sup>
X	1.9969 ± 0.0004	0.0			
a	2.0001 ± 0.0006	26 ± 5	$\nu_1$	E <sub>2u</sub>	24 (26)
b	2.0027 ± 0.0003	47 ± 2	$\nu_3$	E <sub>1g</sub>	48 (68)
<b>c</b>	<b>2.0067 ± 0.0003</b>	<b>79 ± 2</b>	<b>2</b> $\nu_2$	<b>A<sub>1g</sub></b>	<b>64 (70)</b>
d	2.0092 ± 0.0002	99 ± 2	$\nu_7$	E <sub>1u</sub>	81 (83)
<b>e</b>	<b>2.0128 ± 0.0003</b>	<b>128 ± 2</b>	<b><math>\nu_8</math></b>	<b>A<sub>1g</sub></b>	<b>121 (121)</b>
<b>f</b>	<b>2.0157 ± 0.0002</b>	<b>152 ± 2</b>	<b>4</b> $\nu_2$	<b>A<sub>1g</sub></b>	<b>128 (140)</b>
g	2.0190 ± 0.0005	178 ± 3	$\nu_8 + \nu_3$	E <sub>1g</sub>	169 (189)
<b>h</b>	<b>2.0215 ± 0.0013</b>	<b>198 ± 5</b>	<b><math>\nu_8 + 2\nu_2</math></b>	<b>A<sub>1g</sub></b>	<b>185 (191)</b>
<b>i</b>	<b>2.0250 ± 0.0008</b>	<b>227 ± 3</b>	<b>6</b> $\nu_2$	<b>A<sub>1g</sub></b>	<b>192 (210)</b>
<b>j</b>	<b>2.0285 ± 0.0004</b>	<b>255 ± 2</b>	<b>2</b> $\nu_8$	<b>A<sub>1g</sub></b>	<b>242 (242)</b>
<b>k</b>	<b>2.0349 ± 0.0003</b>	<b>306 ± 2</b>	<b><math>\nu_8 + 4\nu_2</math></b>	<b>A<sub>1g</sub></b>	<b>249 (261)</b>
<b>l</b>	<b>2.0375 ± 0.0004</b>	<b>328 ± 2</b>	<b>2</b> $\nu_8 + 2\nu_2$	<b>A<sub>1g</sub></b>	<b>306 (312)</b>
<b>m</b>	<b>2.0391 ± 0.0004</b>	<b>340 ± 2</b>	<b><math>\nu_8 + 6\nu_2</math></b>	<b>A<sub>1g</sub></b>	<b>313 (331)</b>
<b>n</b>	<b>2.0444 ± 0.0004</b>	<b>383 ± 2</b>	<b>2</b> $\nu_8 + 4\nu_2$	<b>A<sub>1g</sub></b>	<b>370 (382)</b>
<b>o</b>	<b>2.0475 ± 0.0003</b>	<b>408 ± 2</b>	<b><math>\nu_{12}</math></b>	<b>A<sub>1g</sub></b>	<b>423 (460)</b>
p	2.0509 ± 0.0002	436 ± 2	$\nu_{12} + \nu_1$	E <sub>2u</sub>	447 (486)
<b>q</b>	<b>2.0575 ± 0.0014</b>	<b>489 ± 6</b>	<b><math>\nu_{12} + 2\nu_2</math></b>	<b>A<sub>1g</sub></b>	<b>487 (530)</b>
<b>r</b>	<b>2.0643 ± 0.0011</b>	<b>544 ± 5</b>	<b><math>\nu_{12} + \nu_8</math></b>	<b>A<sub>1g</sub></b>	<b>544 (581)</b>
<b>s</b>	<b>2.0979 ± 0.0005</b>	<b>815 ± 3</b>	<b>2</b> $\nu_{12}$	<b>A<sub>1g</sub></b>	<b>846 (920)</b>
t	2.1010 ± 0.0002	840 ± 2	2 $\nu_{12} + \nu_1$	E <sub>2u</sub>	870 (946)

<sup>a</sup> The values without and with parentheses are from the PW91/Def2-TZVPPD and PBE0/Def2-TZVPPD calculations, respectively.

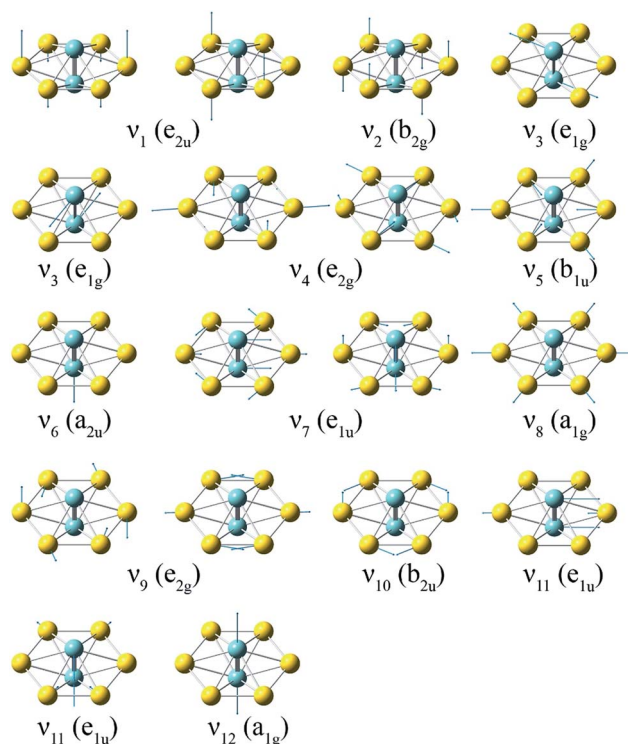
The valence canonical molecular orbital (CMO) contours of isomer I are shown in Fig. S4.† The first PES band X corresponds to electron detachment from the singly occupied molecular orbital (SOMO) ( $a_{2u}$ ), which involves weak antibonding interactions between the two Nb atoms and weak bonding interactions between Nb and Au. Thus, the removal of the SOMO electron should lead to a slight decrease of the Nb–Nb bond length and a slight increase of the Nb–Au bond length in the Nb<sub>2</sub>Au<sub>6</sub> neutral, consistent with the optimized structures (Fig. 3) and the Franck–Condon activities observed for the Au<sub>6</sub> ring breathing and Nb–Nb stretching modes (Fig. 2).

To help assign the PE spectra at the high photon energies (Fig. 1), we calculated higher VDEs of the  $D_{6h}$  global minimum of Nb<sub>2</sub>Au<sub>6</sub><sup>-</sup> using TDDFT at the PBE0/Def2-TZVPPD level, which are compared with the experimental VDEs in Table 1 and plotted in Fig. 1c by fitting each VDE with a unit-area Gaussian function of 0.03 eV width. The calculated VDEs from deeper

orbitals are consistent with the observed bands at the higher binding energy side. We also performed TDDFT calculations for isomers I and II using different functionals and plotted the simulated spectra in the ESI (Fig. S5–S7†). Overall, only the



**Fig. 3** The optimized structures for the global minimum  $D_{6h}$  Nb<sub>2</sub>Au<sub>6</sub><sup>-</sup> and Nb<sub>2</sub>Au<sub>6</sub> at the PBE0/Def2-TZVPPD level. Bond lengths are given in Å.



**Fig. 4** The normal modes and their symmetries for the  $D_{6h}$  Nb<sub>2</sub>Au<sub>6</sub> cluster at the PBE0/Def2-TZVPPD level.



simulated spectral pattern of isomer I is in good agreement with the experimental PE spectra (Fig. 1), lending further credence to the established  $D_{6h}$  global minimum for  $Nb_2Au_6^-$ .

## 7. Discussion

### 7.1. The extremely short Nb–Nb bond length in $Nb_2Au_6$

The optimized structures for the global minima of  $Nb_2Au_6^-$  and  $Nb_2Au_6$  at the PBE0/Def2-TZVPPD level are shown in Fig. 3. Both  $Nb_2Au_6^-$  and  $Nb_2Au_6$  possess  $D_{6h}$  symmetry featuring an  $Au_6$  ring building around the Nb–Nb axis. The slight bond length variations between  $Nb_2Au_6^-$  and  $Nb_2Au_6$  are consistent with the nature of the SOMO of the anion (or the LUMO of the neutral), as discussed above. Interestingly, the size of the  $D_{6h}$   $Au_6$  ring in  $Nb_2Au_6^-$  is almost identical to that in the  $M@Au_6^-$  ( $M = Ti, V, Cr$ ) clusters,<sup>6a</sup> suggesting the  $Au_6$  ring is a robust host to accommodate a dopant from a single atom to a dimer. The Nb–Nb bond lengths in  $Nb_2Au_6^-$  and  $Nb_2Au_6$  are 2.108 Å and 2.076 Å, respectively. These short Nb–Nb bond lengths are similar to the observed bond length of 2.078 Å in gaseous  $Nb_2$ , which possesses a  $^3\Sigma_g^-$  ground state with a  $1\pi_u^4 1\sigma_g^2 2\sigma_g^2 1\delta_g^2$  electron configuration.<sup>12</sup> With two unpaired

weakly bonding electrons in the two degenerate  $\delta$  orbitals, the bare  $Nb_2$  dimer can be approximately viewed to possess a quintuple bond. The Nb–Nb bond lengths in  $Nb_2Au_6^{-/0}$  are much shorter than the Nb–Nb triple bond length (2.32 Å) from Pyykkö's self-consistent covalent radii.<sup>37</sup> Indeed, the calculated Mayer bond orders<sup>38</sup> between Nb–Nb in  $Nb_2$  and  $Nb_2Au_6$  are 5.07 and 3.61 at the PBE0/Def2-TZVP level, respectively. This implies that the Nb–Nb bond strength in  $Nb_2Au_6$  is beyond a triple bond. How does the  $Au_6$  ring accommodate the  $Nb_2$  dimer and facilitate the multiple bonding of  $Nb_2$  in  $Nb_2Au_6$ ?

### 7.2. Chemical bonding in $Nb_2Au_6$

The binding energy between  $Nb_2$  and  $Au_6$  is calculated to be 8.71 eV at the PBE0/Def2-TZVPPD level based on  $Nb_2Au_6$  ( $D_{6h}, ^1A_{1g}$ )  $\rightarrow$   $Nb_2$  ( $D_{\infty h}, ^3\Sigma_g^-$ ) +  $Au_6$  ( $D_{6h}, ^1A_{1g}$ ), indicating strong guest–host interactions. The charge distribution on each atom in  $Nb_2Au_6$  is shown in Table S4.† Although the Au atom is more electronegative than the Nb atom, the charge distribution shows each Nb atom actually draws electron (NPA charge:  $-0.195|e|$ ; Mulliken charge:  $-0.457|e|$ ) from the Au atoms in  $Nb_2Au_6$ . Using the results from the CDA analysis, we made an

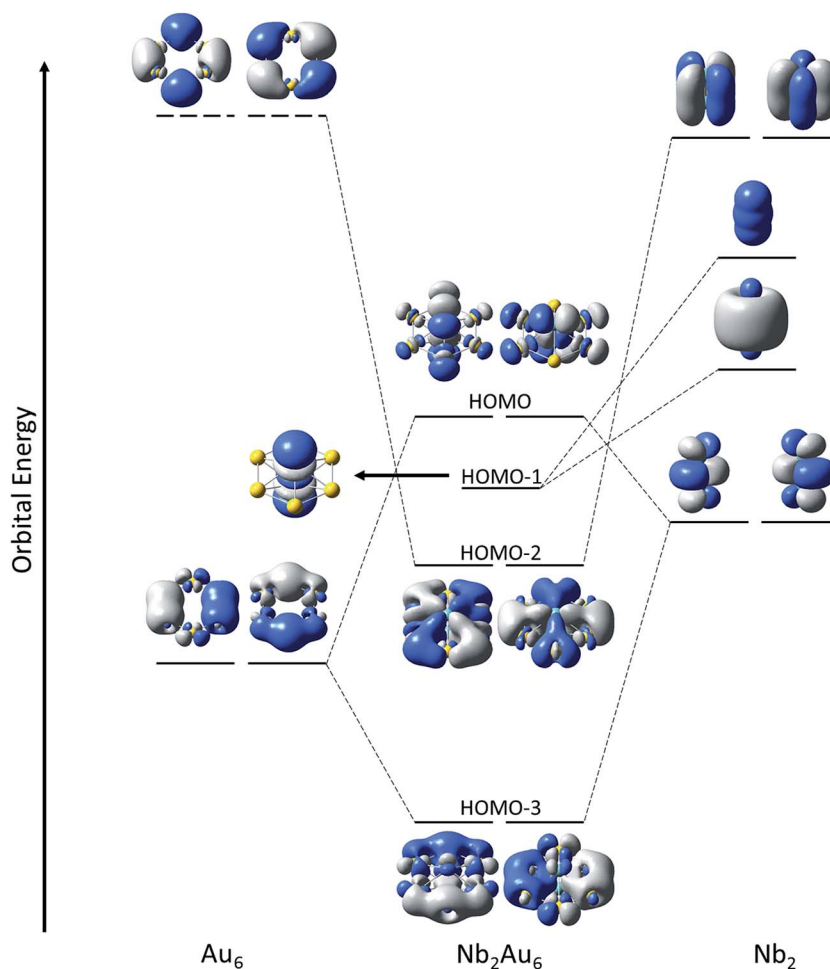


Fig. 5 Qualitative orbital correlation diagram of the interactions between the  $D_{\infty h}$   $Nb_2$  fragment and the  $D_{6h}$   $Au_6$  fragment in the  $D_{6h}$   $Nb_2Au_6$ . The horizontal dashed and solid lines represent virtual and occupied molecular orbitals, respectively.



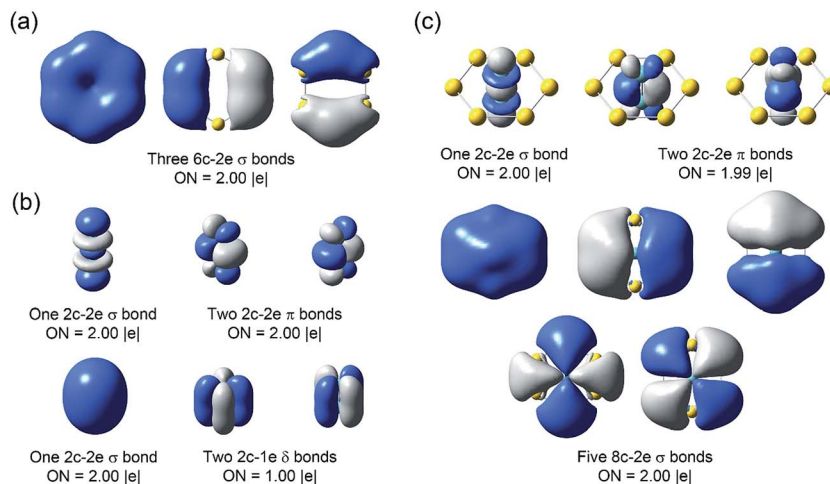


Fig. 6 The AdNDP chemical bonding analyses of (a)  $D_{6h}$   $Au_6$ , (b)  $D_{\infty h}$   $Nb_2$ , and (c)  $D_{6h}$   $Nb_2Au_6$  at the PBE0/Def2-TZVP level. ON stands for occupation number.

orbital correlation diagram about the interactions between the  $Nb_2$  and the  $Au_6$  fragments in  $Nb_2Au_6$ , as shown in Fig. 5. The HOMO ( $e_{1u}$ ) and HOMO-1 ( $a_{1g}$ ) of  $Nb_2Au_6$  are mainly from the  $Nb_2$  fragment, representing two  $\pi$  bonds and one  $\sigma$  bond formed by the overlap of 4d orbitals. The HOMO-2 ( $e_{2g}$ ) of  $Nb_2Au_6$  results from symmetric overlap between the SOMO ( $1\delta_g$ ) of  $Nb_2$  and the LUMO ( $e_{2g}$ ) of the  $Au_6$  ring, providing the key factor to stabilize the ring structure and facilitate the multiple bonding of  $Nb_2$  in  $Nb_2Au_6$ .

However, it is difficult to establish a clear bonding picture between  $Nb_2$  and  $Au_6$  in the deeper CMOs due to strong hybridization. We further analyzed the bonding in  $Nb_2$ ,  $Au_6$ , and  $Nb_2Au_6$  using the AdNDP method at the PBE0/Def2-TZVPPD level. The AdNDP analysis can yield a chemically intuitive bonding picture, displaying not only localized but also delocalized bonds in complicated molecular and cluster systems.<sup>31,39</sup> The results of the AdNDP analyses are shown in Fig. 6. For the  $Au_6$  ring, there are three totally delocalized  $\sigma$  bonds mainly from the 6s orbitals. For the isolated  $Nb_2$ , there are one 4d $\sigma$  bond, two 4d $\pi$  bonds, one 5s $\sigma$  bond, and two two-center one-electron (2c-1e) 5d $\delta$  bonds. In  $Nb_2Au_6$ , the one 4d $\sigma$  bond and two 4d $\pi$  bonds are preserved, defining a triple bond in the  $Nb_2$  moiety. In addition, there are five totally delocalized  $\sigma$  bonds, describing bonding within the  $Au_6$  ring and the  $Nb_2$ - $Au_6$  guest-host bonding. These five delocalized 8c-2e bonds are remarkable, reminiscent of  $\sigma$ -aromaticity. The first three 8c-2e  $\sigma$  bonds in  $Nb_2Au_6$  are similar to those in the  $Au_6$  ring but contain extra contributions from 5s/5p orbitals of Nb. The first and following two 8c-2e  $\sigma$  bonds show the overlap between the bonding orbitals of  $Au_6$  with the 5s $\sigma$  orbital and the 5p $\pi$  orbitals of  $Nb_2$ , respectively. The last two 8c-2e bonds mainly represent interactions between the  $\delta$  MOs of  $Nb_2$  and the antibonding orbitals of  $Au_6$ . The totally delocalized bonding between  $Nb_2$  and  $Au_6$  represents a new mode of guest-host interactions, reinforcing the  $Nb\equiv Nb$  triple bond and giving rise to the extraordinarily short Nb-Nb bond length.

### 7.3. The $Au_6$ ring as a bridging ligand to facilitate metal-metal multiple bonding

It is a well-established strategy to use bridging ligands to facilitate metal-metal multiple bonding.<sup>9b</sup> In fact, using 1,3,4,6,7,8-hexahydropyrimido[1,2-*a*]pyrimidinate (hpp) as bridging ligands, Cotton *et al.* synthesized the  $Nb_2(hpp)_4$  complex, which contains the shortest Nb-Nb triple bond ( $\sigma^2\pi^4$ ) with a bond length of 2.204 Å.<sup>13</sup> This kind of complexes require four electrons of  $Nb_2$  for metal-ligand bonding, restricting the Nb-Nb bond order to be no more than three. Note that the Nb-Nb bond length in  $Nb_2Au_6$  is significantly shorter than that in  $Nb_2(hpp)_4$ . The  $\delta$  orbitals in  $Nb_2$  can interact with the antibonding orbitals of the equatorial  $Au_6$  ring by symmetry, providing the key mechanism for reinforcing the  $Nb\equiv Nb$  triple bond. Thus, the  $Au_6$  ring acts as a new type of bridging ligand and provides a new strategy to facilitate stronger multiple bonding in transition metal dimers.

## 8. Conclusions

In summary, we report the observation of highly symmetric  $Nb_2@Au_6^{-10}$  molecular wheels, in which an extremely short  $Nb\equiv Nb$  triple bond is coordinated equatorially by an  $Au_6$  ring and stabilized by  $\sigma$  aromaticity. A large HOMO-LUMO gap is observed in the photoelectron spectra, suggesting the neutral  $Nb_2Au_6$  cluster is a highly stable electronic system. High-resolution photoelectron spectra from velocity map imaging indicate that neutral  $Nb_2Au_6$  is highly symmetric. Global minimum searches coupled with high-level quantum calculations show that the most stable structures of  $Nb_2Au_6^{-10}$  consist of a  $D_{6h}$   $Au_6$  ring building around a short  $Nb_2$  axis. Chemical bonding analyses reveal one  $\sigma$  bond and two  $\pi$  bonds in the  $Nb_2$  axis, and five totally delocalized  $\sigma$  bonds in  $Nb_2Au_6$ . The antibonding orbitals of the  $Au_6$  ring can interact with the  $\delta$  orbitals in  $Nb_2$  by symmetry, which is critical for strengthening the  $Nb\equiv Nb$  triple bond. The  $Au_6$  ring acts as a novel bridging ligand, providing a new strategy to facilitate stronger multiple



bonding in transition metal dimers. A whole class of  $M_2@Au_6$  type molecular wheels containing a strengthened M–M multiple bond may be possible.

## Conflicts of interest

There are no conflicts to declare.

## Acknowledgements

This work was supported by the National Science Foundation (CHE-1263745). We are indebted to Prof. Xueming Yang and Dr Tao Wang for supplying us the Deyang (德扬) dye laser system, which is critical for the high-resolution PE imaging experiment. The calculations were performed using resources at the Center for Computation and Visualization (CCV) of Brown University. T. J. wishes to thank the Chemistry Department of Brown University for the Vince Wernig Fellowship.

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