

Cite this: *RSC Adv.*, 2017, 7, 56266

Sol–gel synthesis of $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ nanoparticles dispersible in acrylates†

L. Schmidt, St. Mahn and E. Kemnitz *

A new approach to prepare nanoparticles in $\text{SrF}_2\text{--YbF}_3$ systems via the fluorolytic sol–gel synthesis is presented. A series of $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ ($0.12 < x < 0.62$) nanoparticles of nonstoichiometric fluorite phases obeying Vegard's law throughout the homogeneity area have been successfully prepared at room temperature. For all Yb concentrations XRD patterns show the formation of cubic phases. For higher Yb concentration (>50 mol%) crystallite sizes decrease abruptly in comparison to lower Yb concentrations (<50 mol%) as detected by XRD. The obtained sols are highly transparent. The investigations by DLS and TEM revealed the presence of monodisperse sol particles with sizes in the lower nm range (~ 5 nm). The nanoparticles are characterized by a wide range of homogeneity (up to approx. 60 mol% Yb) and show promise of a wide range of applicability in the areas of medicine, dentistry and optics.

Received 7th November 2017
Accepted 6th December 2017

DOI: 10.1039/c7ra12210a

rsc.li/rsc-advances

At present, there is great interest in luminescent lanthanide doped nanoparticles for efficient frequency conversion from infrared (IR) to visible (VIS) radiation. Particularly because a visible source pumped by a near infrared (NIR) laser is useful for high-capacity data storage optical devices.¹ This process can be obtained by upconversion mechanisms.² Upconversion nanoparticles emit detectable photons of higher energy in the short wavelength range upon irradiation with near-infrared (NIR) light. Several infrared photons can be absorbed by the material doped with rare earth ions (RE) in order to populate more energetic levels. The use of long lifetime and real ladder-like energy levels of trivalent lanthanide ions embedded in an appropriate inorganic host lattice can produce higher energy luminescence. In recent years, the application of rare earth doped alkaline earth metal fluoride nanoparticles ($\text{MF}_2\text{:RE}$, $\text{M} = \text{Ca, Sr, Ba}$) has attracted the interest of researchers for the possibility of using them as optical labels in medical diagnostics and imaging.² In order to be successfully employed in *in vivo* studies, however, the nanoparticles must be efficiently dispersible in physiological solutions.³ In many cases this is a challenging task, as nanoparticles in water have a higher tendency to agglomerate to a larger size and precipitate out of solution. The stability of colloidal dispersed particles depends on the relative magnitude of the forces of attraction and the forces of repulsion. A method to enhance the stabilization of nanoparticles and prevent the formation of precipitates that enhance the sedimentation is the functionalization of particles with hydrophilic capping agents in

order to reduce attractive forces between particle surfaces. The most popular methods described in the literature to prepare upconversion nanoparticles are the thermolysis strategy and the hydro(solvo)thermal synthesis with the assistance of surfactants.^{2,4} In some cases, hydrophilic ligands such as citric acid,³ ethylenediaminetetraacetic acid (EDTA) and (poly)acrylic acid⁵ are used providing good water solubility. Therefore only very few reports exist in the literature on upconverting nanoparticles directly dispersible in water solution.

Since rare earth doped particles ($\text{MF}_2\text{:RE}$) are known to emit VIS light under near infrared (NIR) excitation by an upconversion process, they are of great interest in light-curable polymers commonly used in restorative dentistry.⁶ Usually, light-curing dental filling materials consist of a dimethacrylate monomer, inorganic fillers and a photo-initiator. A blue visible light (420–470 nm) is required for initiating the polymerization process.⁷ However, despite their widespread application, polymerization shrinkage and a partly incomplete curing is a drawback of these materials. The curing in deep cavities is limited by the penetration depth of the blue light in the tooth structure and the composite itself. Since dental composites also contain a large amount of inorganic fillers (up to 50 vol%) transmittance of VIS, is scattered strongly resulting in shallow curing depths. For this reason, the multilayered technique for the restoration of deep cavities is required. This in turn often requires the destruction of healthy tooth structures. An efficient polymerization by deeply penetrating NIR light can be achieved by embedding upconversion nanoparticles in the monomer matrix.^{6,7} Furthermore, by using nanoscopic fluorides of alkaline earth metals and rare earth metals as fillers one can improve the cariostatic properties of dental composites and at the same time to provide an increase in X-ray efficiency of such materials. Therefore, nanoparticles of $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ solid-solutions in $\text{SrF}_2\text{--}$

Humboldt-Universität zu Berlin, Department of Chemistry, Brook-Taylor-Straße 2, 12489 Berlin, Germany. E-mail: erhard.kemnitz@chemie.hu-berlin.de

† Electronic supplementary information (ESI) available: Detailed experimental procedures, STEM image and hypermap of the elements, XRD pattern after treatment at 700 °C. See DOI: 10.1039/c7ra12210a



YbF₃ systems are promising materials in terms of dental applications due to their anticariogenic effect, the ability to provide radiopacity to the dental material as well as, doped with Er³⁺, to improve the polymerization of dental composites. Solid solutions and Sr_{1-x}Yb_xF_{2+x} nonstoichiometric fluorite phases have been known for decades.^{8–12} However, the syntheses were carried out at high temperatures resulting in single crystals which allows a thoroughly investigation of the materials. With continuously increasing interest in nanomaterials many synthetic strategies were developed to prepare nanoscopic particles of solid solutions according the requirements for the desired materials.^{13–17} A challenge represents the synthesis of monodisperse nanoparticles with particle sizes in the lower nanometer range, which are important for further processing.

In this study we present an elegant and easy approach to synthesize Sr_{1-x}Yb_xF_{2+x} solid-solution nanoparticles homogeneously dispersed in water, which makes them suitable for medical applications. A series of solid solution nanoparticles with various mean crystallite sizes were successfully prepared by the fluorolytic sol-gel route.^{18,19} X-ray powder diffraction (XRD), dynamic light scattering (DLS) and transmission electron microscopy (TEM) were used to characterize the particles according to their particle size, crystallite size as well as to study the ageing process and crystallite size dependency with increasing ytterbium concentration. The fluorolytic sol-gel synthesis was carried out dissolving acetates of Sr and Yb in water and adding non-aqueous methanolic HF solution (full experimental procedure is available in the ESI†). However, it has to be noted, that by using aqueous HF immediate sedimentation was observed. Apparently, by using alcoholic HF solution we influence the kinetics of fluorolysis and formation of particles and therefore their stability. Furthermore, the formed nanoparticles show a lower solubility in alcoholic solutions as compared to aqueous solutions which has an impact on their solubility product during the formation. The XRD pattern (Fig. 1) of Sr_{1-x}Yb_xF_{2+x} phases prepared *via* the fluorolytic sol-gel synthesis show significant reflections which can be clearly assigned to the crystallographic planes of cubic SrF₂. There is a slight shift in the XRD peaks towards higher angles. This shift is believed to result from the incorporation of Yb ions into the SrF₂ lattice, and the smaller ionic radius of Yb³⁺ (0.985 Å) as

compared to that of Sr²⁺ (1.26 Å).²⁰ The incorporation of the smaller cation leads to smaller lattice constants as compared to the pure SrF₂, which causes the shift to higher angles.¹⁷ A series of Sr_{1-x}Yb_xF_{2+x} nanoparticles with different Yb concentrations (0.12 < *x* < 0.62) was prepared and characterized by XRD. The results calculated from XRD patterns concerning lattice constants, crystallite sizes and Yb concentrations are given in Table 1. The calculation of the lattice constant *a* of the crystallographic unit cell in the cubic system for each sample was carried out using the Bragg equation:

$$d_{hkl} = \frac{a}{\sqrt{h^2 + k^2 + l^2}} \text{ and } \lambda = 2d_{hkl} \sin \theta$$

here, λ is the wavelength of X-ray radiation (Cu-K α 0.15406 nm), θ the diffraction angle, d_{hkl} is the lattice plane distance, wherein *hkl* are the Miller indices. According to Sobolev *et al.*⁸ the lattice constant *a* depends on the concentration of Ln³⁺ by the following equation:

$$A = a_0 + kx$$

where $a_0 = 5.800$ Å is the lattice constant of SrF₂ and $k = -0.3199$ for Yb.²¹

It can also be observed from Fig. 1 that there is a slight shift in the XRD peak position towards higher angles with increase in Yb concentration, resulting in change in the lattice constant. Broad diffraction peaks in the patterns are in agreement with the characteristics of nanosized materials. Fig. 2 shows the lattice constant *a* as a function of different Yb concentrations. Lattice constants decrease with increase in the Yb concentration perfectly obeying Vegard's law.²² Moreover, this also reflects that Yb³⁺ ions were substituted in the SrF₂ lattice without changing the symmetry of the cubic structure.

Crystallite sizes of the obtained samples were estimated from the full width at half maximum (FWHM) of the most distinct XRD reflections (111), (220) and (311) using the Scherrer equation.²³ Here, we found that for samples with Yb concentrations of <50 mol% the calculated mean crystallite size is approx. 10 nm. For samples with Yb concentrations of >50 mol% the mean crystallite size decreases abruptly to approx. 6 nm indicating the formation of smaller primary particles with increasing Yb concentration in the sample.

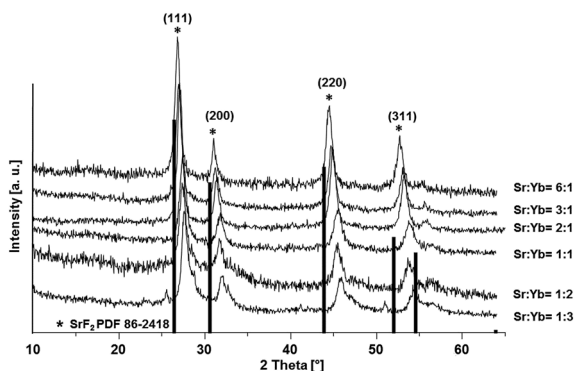


Fig. 1 XRD patterns of Sr_{1-x}Yb_xF_{2+x} (0.12 < *x* < 0.62) phases obtained *via* the fluorolytic sol-gel synthesis.

Table 1 Overview of calculated values for solid solutions in terms of Yb concentration, lattice constant and crystallite size

Sr : Yb	Yb concentration in Sr _{1-x} Yb _x F _{2+x} th. exp.	Lattice constant <i>a</i> [Å]	Crystallite size [nm]
6 : 1	14%	5.753	10
5 : 1	16%	5.737	9
4 : 1	20%	5.744	10
3 : 1	25%	5.726	10
2 : 1	33%	5.694	10
1 : 1	50%	5.630	7
1 : 2	—	5.625	6
1 : 3	—	5.595	—



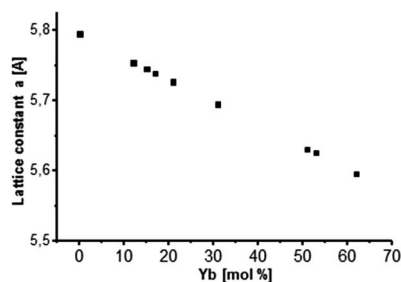


Fig. 2 Lattice constant a as a function of Yb concentration incorporated into the cubic SrF_2 lattice. A behavior according to Vegard's law is indicated.

A transparent sol was obtained at Sr-to-Yb molar ratio of 1 : 2. The determination of the hydrodynamic particle diameter by means of DLS (Fig. 3) shows for the 0.2 M sol with a dynamic viscosity of 1.1 mPa s a monodisperse particle size distribution with a maximum at about 30 nm. Since DLS only provides hydrodynamic diameters and the crystallite sizes according the Scherrer equation give only estimated values TEM was used in order to determine and to provide additional information with respect to the particle size, shape and morphology as well as to prove the crystallinity of the particles. Fig. 4 shows the high resolution TEM image (HRTEM) of a TEM grid dip-coated into a 0.2 M transparent $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ ($x = 0.53$) sol. It shows a certain degree of agglomeration of several primary particles. Lattice plane distances can be clearly recognized proving the crystallinity of the particles. The measured lattice plane distances are consistent with the calculated lattice spacings for

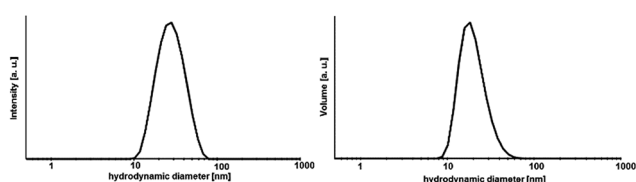


Fig. 3 Size distribution by DLS of a transparent 0.2 M $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ ($x = 0.53$) sol.

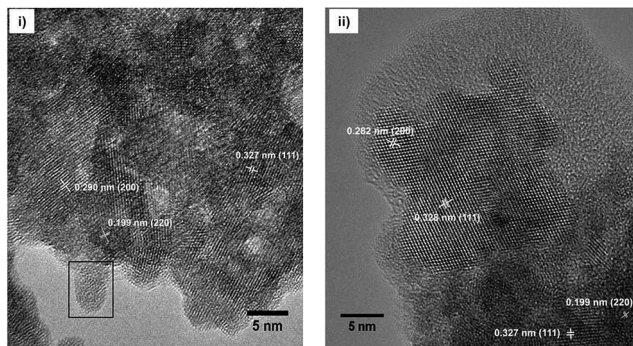


Fig. 4 HRTEM image of $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ ($x = 0.53$) nanoparticles obtained after (i) dip-coating the TEM grid into a 0.2 M sol and (ii) after calcining the particles at 300 °C.

the nonstoichiometric phase $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ with $x = 0.53$ confirming the formation of this phase. From the evaluation of an isolated particle the average particle size can be estimated to be ~ 5 nm. The formation of core-shell structured particles can be excluded as no amorphous shells or a difference by material contrast of isolated particles can be observed by TEM. The same sample was then treated at 300 °C in order to remove residual organic and investigated by TEM, subsequently. It seems that the particles have been undergoing a homogenization process at higher temperatures. In the HRTEM image large particles can be seen having the same orientation as well as an amorphous shell. The measured lattice space distances are in good agreement with the calculated lattice plane distances leading to the conclusion that the expected compound is formed. Overall, TEM revealed the presence of agglomerates with sizes of approx. 30 nm, consisting of smaller (~ 5 nm) and larger primary particles (~ 10 nm). To gain more information about the amorphous layer, STEM (scanning TEM) was used. The image of the particles in the STEM mode (Fig. S1, ESI†) shows the agglomeration of these larger units. The sample is very well structured. The element distribution was determined using EDXS in selected regions of the sample. A homogeneous distribution of the elements Sr, Yb and F was detected. The amorphous region of the sample consists exclusively of carbon and oxygen. No other elements were detected in this area. Since both carbon and oxygen are also detected in the crystalline region, it can be concluded that the sample still contains residual organics, which was supplied either during the synthesis or could not be removed in the course of preparation of the TEM grid. Therefore, the formation of core-shell particles cannot be assigned. However, utilizing TEM in combination with XRD and DLS, the formation of non-stoichiometric phase of the composition $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ ($x = 0.53$) as a highly transparent aqueous sol with particle sizes in the lower nanometer range was proven. Samples with different Yb concentrations are of nanocrystalline character but are obtained as nanopowders.

Furthermore, the ageing process of the sol was studied. The 0.2 M sol is highly stable over a period of at least two years and shows neither an increase in turbidity nor signs of ageing resulting in sedimentation or gelation. However, this sol is characterized by a high transparency. It also does not show any changes in the dynamic viscosity and size distribution of the hydrodynamic particle diameters. The 2 years aged sol has a monodisperse particle size distribution with a maximum at about 30 nm and a viscosity of 1.11 mPa s. Comparing the XRD patterns (Fig. 5) of xerogels obtained from 1 week old and 2 years old sol, the diffraction patterns remain unchanged in terms of reflection positions and reflection peak broadening of $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ ($x = 0.53$). Therefore, one can conclude that Ostwald ripening does not occur within a period of 2 years although the nanoparticles are present in the aqueous system. This could be explained suggesting the formation of sol particles with a very low solubility and uniform particle size. Ostwald ripening is the growth of the large particles on expense of the small ones. Small-sized particles are being dissolved and re-deposit on the surface of larger particles, reaching more stable thermodynamic state. So the driving force is the minimization of the surface



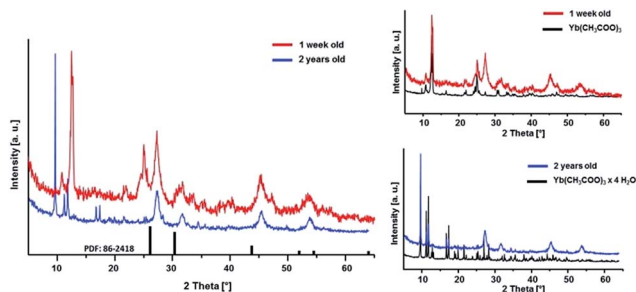


Fig. 5 XRD patterns of $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ ($x = 0.53$) xerogels obtained from sols of different ageing time.

energy. The risk of Ostwald ripening increases if nanoparticles have relatively high aqueous solubility. However, here, it seems not to be the case as the nanoparticles do not show an increase in crystallite size even after 2 years. On the one hand, Ostwald ripening requires to occur a certain solubility of nanoparticles in the solvent, on the other hand it requires a difference in particle size and therefore in solubility. However, DLS shows a very monodisperse size distribution leading to the conclusion that particles of similar hydrodynamic diameters are present. Therefore, Ostwald ripening plays a minor role in the ageing process of the sols. Merely recrystallization of the unreacted anhydrous ytterbium acetate to ytterbium acetate tetrahydrate is observed. Since both acetates are water-soluble, this process does not influence the transparency and stability of the sol. Nanoparticles have an extremely large surface area per unit volume of the particles. Because of the large surface area, nanoparticles tend to adsorb substances, such as water molecules and ions, from the surrounding water. The surface of a nanoparticle tends to acquire an electrostatic charge due to the ionization of surface groups and the adsorption of ions from the surrounding solution. The sol particles remain dispersed and stabilized in water for long periods of time (2 years) as a result of the electrostatic forces of the sol particle surfaces themselves. As no additives were added during the synthesis, the obtained sol particles are compatible with water solution.

As demonstrated by XRD patterns of the as-prepared $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ samples shown in Fig. 1, all the diffraction peaks of the cubic SrF_2 lattice are shifted towards higher angles, due to the increasing concentration of Yb in the SrF_2 lattice. The cubic

lattice constant decreases with increasing Yb content. In contrast, the samples treated at 700°C show reflections of the nonstoichiometric phases with almost identical reflection positions. It can also be observed from Fig. S2 (ESI†) that there is a shift in the diffraction peak position towards smaller angles as compared to Fig. 1, indicating a decrease in the Yb concentration in the solid solutions. That results in change in the lattice constant. The calculated lattice constants support this result (see Table 2). The lattice constants of samples calcined at 700°C show a nearly constant value for a as compared to the lattice constants of uncalcined samples which follow Vegard's law. Particularly $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ phases with higher Yb contents ($>20\text{ mol}\%$) show a significant difference in lattice constants at different temperatures. At the same time, XRD analysis shows the coexistence of Yb_2O_3 and YbOF at 700°C as shown in Fig. S2 (ESI†).

It has to be noted that the synthesis of composite materials where $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ nanoparticles are homogeneously dispersed in an organic polymer matrix is rather challenging. The initial solvent to prepare transparent $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ sols and nanoparticles is water. The problem is that hydrophobic resins such as Bis-GMA and TEGDMA commonly used in dental filling materials have poor water solubility. Therefore they are not

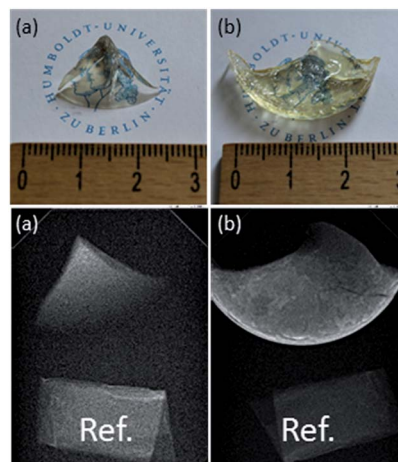


Fig. 6 Photo and radiograph of (a) pure plastic, (b) plastic containing 6 wt% $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$.

Table 2 Comparison between uncalcined solid solutions and solid solutions calcined at 700°C in terms of lattice constants and Yb concentrations

Sr : Yb	Yb concentration in $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$	Lattice constant a [\AA]	Lattice constant a [\AA] 700°C	Yb concentration in $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ at 700°C
6 : 1	12%	5.753	5.794	10%
5 : 1	17%	5.737	5.762	8%
4 : 1	15%	5.744	5.767	8%
3 : 1	21%	5.726	5.766	7%
2 : 1	31%	5.694	5.771	6%
1 : 1	51%	5.630	5.775	14%
1 : 2	53%	5.625	5.747	8%
1 : 3	62%	5.595	5.787	19%

miscible with water. By mixing transparent $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ sols with hydrophobic resins, upon mixing, they separate into two immiscible phases. Also, starting from nanoscopic $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ solid particles only turbid materials are obtained indicating inhomogeneous dispersion of the particles. This is, obviously larger agglomerates of nanoparticles in the organic matrix are formed. This problem can be overcome by replacing water during the synthesis or in the matrix with polar organic solvents such as ethanol or by modifying the nanoparticles formed with suitable complexing agents thus making them compatible to the organic monomers. Additionally, the hydrophilicity of the resins can be improved adding hydrophilic monomers, such as HEMA. A post modification of the particle surface by polyacrylic acid is also an elegant option to redisperse these particles in dimethacrylates. As seen in Fig. 6, after polymerization we obtained transparent plastics. Radiological experiments proved an increased radiopacity of the plastic with at least 6 wt% of particles inside (Fig. 6b), in comparison to the same reference.

Conclusions

In summary, we present the synthesis of $\text{SrF}_2\text{-YbF}_3$ nanoparticles via the fluorolytic sol-gel synthesis. The obtained particles are solid solutions of YbF_3 in the cubic lattice of SrF_2 , which can be described as nonstoichiometric $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ phases with Vegard behavior. The formation was confirmed by XRD and TEM analysis. The cubic lattice constant decreases with increasing Yb content. After thermal treatment of the solid solutions at 700 °C, however, an increase in the lattice constant is observed which is accompanied by the formation of a SrF_2 phase with lower ytterbium concentrations and the formation of YbOF phases. Smaller crystallite sizes (<6 nm) are stabilized with higher ytterbium concentrations in the SrF_2 lattice. Highly transparent monodisperse sols of $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ ($x = 0.53$) in water solution with hydrodynamic diameters of ~30 nm and crystallite sizes of ~6 nm are stable over a period of at least 2 years without facing loss of visual transparency and viscosity. The nanoparticles are characterized by a wide range of homogeneity (up to approx. 60 mol% Yb). Without further preparation steps, the as-prepared $\text{Sr}_{1-x}\text{Yb}_x\text{F}_{2+x}$ ($x = 0.53$) particles are homogeneously dispersible in water solution and therefore show promise of a wide range of applicability in the areas of medicine, dentistry and optics.

Conflicts of interest

There are no conflicts to declare.

Acknowledgements

The authors thank Holm Kirmse (Department of Physics) for TEM measurements. The financial support by DFG (Deutsche Forschungsgemeinschaft) in the framework of the graduate

school GRK 1582 ("Fluorine as a key element") is gratefully acknowledged.

Notes and references

- 1 P. P. Fedorov, A. a. Luginina, S. V. Kuznetsov and V. V. Osiko, *J. Fluorine Chem.*, 2011, **132**, 1012–1039.
- 2 G. Chen, H. Qiu, P. N. Prasad and X. Chen, *Chem. Rev.*, 2014, **114**, 5161–5214.
- 3 M. Pedroni, F. Piccinelli, T. Passuello, S. Polizzi, J. Ueda, P. Haro-Gonzalez, L. M. Maestro, D. Jaque, J. Garcia-Sole, M. Bettinelli and A. Speghini, *Cryst. Growth Des.*, 2013, **13**, 4906–4913.
- 4 Y.-P. Du, X. Sun, Y.-W. Zhang, Z.-G. Yan, L.-D. Sun and C.-H. Yan, *Cryst. Growth Des.*, 2009, **9**, 2013–2019.
- 5 H. Qiu, G. Chen, R. Fan, L. Yang, C. Liu, S. Hao, M. J. Sailor, H. Ågren, C. Yang and P. N. Prasad, *Nanoscale*, 2014, **6**, 753–757.
- 6 A. Stepuk, D. Mohn, R. N. Grass, M. Zehnder, K. W. Krämer, F. Pellé, A. Ferrier and W. J. Stark, *Dent. Mater.*, 2012, **28**, 304–311.
- 7 M. Uo, E. Kudo, A. Okada, K. Soga and Y. Kogo, *J. Photopolym. Sci. Technol.*, 2009, **22**, 551–554.
- 8 B. P. Sobolev, K. B. Seiranian, L. S. Garashina and P. P. Fedorov, *J. Solid State Chem.*, 1979, **28**, 51–58.
- 9 B. P. Sobolev and K. B. Seiranian, *J. Solid State Chem.*, 1981, **39**, 337–344.
- 10 B. P. Sobolev, D. N. Karimov, S. N. Sul'yanov and Z. I. Zhmurova, *Crystallogr. Rep.*, 2009, **54**, 122–130.
- 11 V. a. Chernyshev, a. E. Nikiforov and a. D. Nazemnikh, *J. Phys.: Conf. Ser.*, 2011, **324**, 012025.
- 12 V. a. Chernyshev, a. E. Nikiforov, V. P. Volodin and G. S. Slepukhin, *Phys. Solid State*, 2010, **52**, 1874–1879.
- 13 J. Chen and J. X. Zhao, *Sensors*, 2012, **12**, 2414–2435.
- 14 L. G. Jacobsohn, C. J. Kucera, T. L. James, K. B. Sprinkle, J. R. DiMaio, B. Kokuzov, B. Yazgan-Kukouz, T. a. DeVol and J. Ballato, *Materials*, 2010, **3**, 2053–2068.
- 15 J. Sun, J. Xian and H. Du, *Appl. Surf. Sci.*, 2011, **257**, 3592–3595.
- 16 S. V. Kuznetsov, I. V. Yarotskaya, P. P. Fedorov, V. V. Voronov, S. V. Lavrishchev, T. T. Basiev and V. V. Osiko, *Russ. J. Inorg. Chem.*, 2007, **52**, 315–320.
- 17 J. Sun, J. Xian, X. Zhang and H. Du, *J. Rare Earths*, 2011, **29**, 32–38.
- 18 E. Kemnitz, U. Gross, S. Rüdiger and C. S. Shekar, *Angew. Chem., Int. Ed. Engl.*, 2003, **42**, 4251–4254.
- 19 S. Rüdiger and E. Kemnitz, *Dalton Trans.*, 2008, **9226**, 1117–1127.
- 20 R. D. Shannon, *Acta Crystallogr.*, 1976, **32**, 751–767.
- 21 X. Qiao, X. Fan, M. Wang and X. Zhang, *J. Phys. D: Appl. Phys.*, 2009, **42**, 055103.
- 22 L. Vegard, *Zeitschrift für Physik*, 1921, **5**, 17–26.
- 23 A. L. Patterson, *Phys. Rev.*, 1939, **56**, 978–982.

