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# Quasiparticle energies, exciton level structures and optical absorption spectra of ultra-narrow ZSiCNRs†

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The hydrogen-passivated  $N$  chain zigzag silicon carbide nanoribbons ( $N$ -ZSiCNRs) are indexed by their width  $N$  (the number of zigzag Si–C chains across the nanoribbon). Based on first-principles  $GW$  and Bethe–Salpeter equation (BSE) approaches, we investigated the quasiparticle band structures, exciton level structures and optical absorption spectra of the ultra-narrow  $N$ -ZSiCNRs with  $N = 2–3$ . It is found that the  $GW$  band gap of 3-ZSiCNR is 0.804 eV, which is more than two times larger than the HSE06 band gap (0.401 eV). The  $GW$  band gap of 2-ZSiCNR is 2.911 eV, which is also almost more than two times larger than the HSE06 band gap (1.621 eV). These results indicate that for 1-dimensional structure materials, HSE06 approaches underestimate the band gap of the system. The  $GW + BSE$  calculations demonstrate that the optical absorption spectra of the  $N$ -ZSiCNRs are dominated by edge-state-derived excitons with large binding energy, composed of a characteristic series of exciton states. It is found that the edge-state excitons of  $N$ -ZSiCNR belong to charge-transfer excitons, where the excited electron is confined to a Si edge while the hole is located on a C edge. The exciton binding energy increases with decreasing width  $N$ , which indicates that the quantum confinement effect enhances with decreasing width  $N$ . The excitons in 2-ZSiCNR can have a binding energy up to 1.78 eV. In addition, the exciton level structure and wave function are classified. It is very interesting to find a relationship between the node of the exciton wave functions and the incoming polarization light exciton excitation. For example, in the longitudinal optical absorption spectra, if the exciton whose wave function possesses an odd number of nodes is optically active, then the exciton whose wave function possesses an even number of nodes is optically inactive. In contrast, in the transverse optical absorption spectra, the exciton whose wave function possesses an odd number of nodes is optically inactive, while the exciton whose wave function possesses an even number of nodes is optically active.

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## 1 Introduction

It is known that double edge hydrogenation armchair edge graphene nanoribbons (ARGNRs) belong to nonmagnetic semiconductors; but double edge hydrogenation zigzag edge graphene nanoribbons (ZGNRs) belong to antiferromagnetic (AF) semiconductors, where each zigzag edge exists in the ferromagnetic (FM) order, while the magnetic moments at

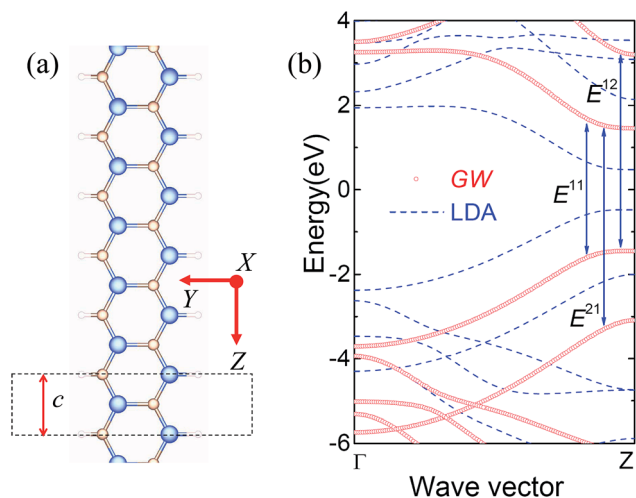
opposite edge carbon atoms exist as AF coupling.<sup>1–4</sup> Son *et al.* studied the transverse electric field effect on ZGNRs.<sup>5</sup> Kim *et al.*<sup>6</sup> studied the spin valve of ZGNRs. It is found that in non-straight edges of graphene nanoribbons, the edge magnetic coupling can be FM coupling.<sup>7–9</sup> Yu *et al.* found a unified geometric rule for designing the magnetic nanostructures of graphene-based nanoribbons.<sup>8</sup> In addition, studies reveal that ZGNRs made by functionalization of edges, such as by functional groups or by various atoms, can show various electronic and magnetic properties.<sup>10–14</sup> Recently, Chen *et al.* studied the room-temperature spin caloritronics effect of sawtooth ZGNRs.<sup>15</sup> Krepel *et al.* demonstrated that AGNRs can be used as ultra-sensitive chemical detectors.<sup>16</sup>

Unlike graphene,<sup>17</sup> which is a zero-band-gap semiconductor, SiC sheet, a new SiC lower dimensional structure material, is a wide-band-gap semiconductor.<sup>18–20</sup> SiC sheet nanoribbons (SiCNRs) are shown in Fig. 1(a) and 2(a), where the edge silicon and carbon atoms are referred to as edge Si and edge C atoms, whereas the corresponding edges are called Si-edge and C-edge, respectively. Spin-polarized first-principles calculations show

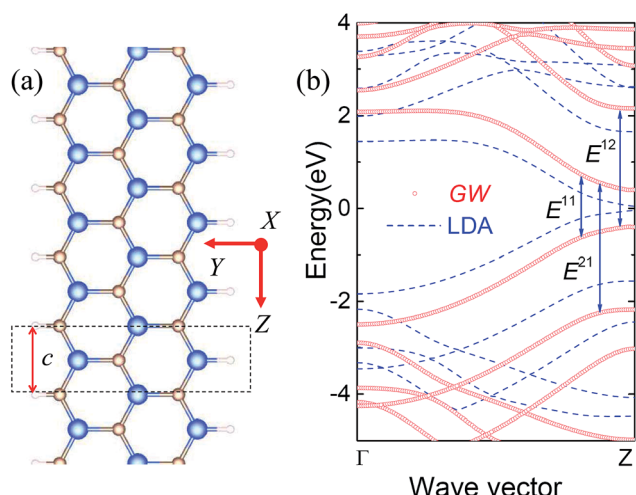
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† Electronic supplementary information (ESI) available: ESI Fig. 1 and 2 show the optical absorption spectra, where different Gaussian broadening  $\delta$  has been used. ESI Table 1 lists the special analysis for exciton wave functions of the degeneracy energy levels of 2-ZSiCNR associated with the interband transitions  $E_{ij}^{\delta}$ ; ESI Table 2 lists the special analysis for exciton wave functions of the degeneracy energy levels of 3-ZSiCNR associated with the interband transitions  $E_{ij}^{\delta}$ ; ESI Table 3 lists the convergence of band gap energies  $E_g$  calculated by  $GW$  of  $N$ -SiCNRs with respect to the  $k$ -grid. ESI Fig. 3–6 show convergence of the optical absorption spectrum with respect to the  $k$ -grid. ESI Fig. 7 and 8 show the optical spectra in the polarizability per unit area. See DOI: 10.1039/c7ra09993b





**Fig. 1** (a) Geometry structure of 2-ZSiCNR. The dark yellow, blue and white balls represent C atoms, Si atoms and H atoms, respectively. The system is periodic along the Z-direction.  $c$  is the lattice constant (3.116 Å) along the periodic direction. (b) Electronic band structures in the first Brillouin zone along the ribbon. The red open circles indicate the GW band structures while the blue dashed lines indicate the LDA band structures. The Fermi level is set to zero. The vertical blue arrows represent the interband transitions.  $E^{ij}$  denotes the interband transition energy from the  $i$ th valence band to the  $j$ th conduction band, with the band indices counted from the Fermi level.



**Fig. 2** (a) Geometry structure of 3-ZSiCNR. The dark yellow, blue and white balls represent C atoms, Si atoms and H atoms, respectively. The system is periodic along the Z-direction.  $c$  is the lattice constant (3.116 Å) along the periodic direction. (b) Electronic band structures in the first Brillouin zone along the ribbon. The red open circles indicate the GW band structures while the blue dashed lines indicate the LDA band structures. The Fermi level is set to zero. The vertical blue arrows denote the interband transitions.  $E^{ij}$  denotes the interband transition energy from the  $i$ th valence band to the  $j$ th conduction band, with the band indices counted from the Fermi level.

that armchair SiCNRs (ASiCNRs) are nonmagnetic semiconductors,<sup>18,19</sup> while  $N$  chain zigzag SiCNRs ( $N$ -ZSiCNRs) are magnetic metals.<sup>18</sup> A further study by Lou and Lee revealed that the  $N$ -ZSiCNRs ( $3 \leq N \leq 6$ ) are ferrimagnetic semiconductors of

which the spin-up and spin-down channels have different direct band gaps, but 2-ZSiCNR has only a nonmagnetic semiconducting state with a direct band gap.<sup>21</sup> Moreover, they found that by applying an external transverse electric field<sup>22</sup> or carrier (hole and electron) doping,<sup>23,24</sup> the  $N$ -ZSiCNRs can be utilized for manipulating the magnetization. Recently, Zheng *et al.*<sup>25</sup> found that the band-gap of SiCNRs can be modulated by transverse electric fields. In addition, the edge reconstruction effect,<sup>26</sup> edge hydrogenation,<sup>28</sup> NM impurity chemistry substitution,<sup>27,29</sup> Stone–Wales defects,<sup>30</sup> edge-modification,<sup>31,32</sup> as well as molecular surface-adsorbing<sup>33,34</sup> on the electrical and magnetic properties of  $N$ -ZSiCNRs have also been investigated. Recently, Wu *et al.* studied the spin caloritronics effect of the  $N$ -ZSiCNR heterostructure.<sup>35</sup>

More recently, the electronic and magnetic properties of  $N$ -ZSiCNRs have been investigated using the Heyd–Scuseria–Ernzerhof screened hybrid functional (HSE06) with a plane-wave basis set,<sup>36</sup> which confirm that 2-ZSiCNR and 3-ZSiCNR are new direct band gap semiconductors. The HSE06 band gap is 1.517 eV and 0.401 eV for the 2-ZSiCNR and 3-ZSiCNR,<sup>36</sup> respectively, which may be quite interesting from the perspective of photochemical catalysis and solar cells. Thus, it is highly required to understand the excited-state properties of  $N$ -ZSiCNRs. However, so far research is focused on the ground state properties of  $N$ -ZSiCNRs. The fundamental excited-state properties of  $N$ -ZSiCNRs, such as quasiparticle (QP) band structures, exciton structures and optical absorption spectra, have not been paid enough attention, although recently Alaál *et al.* studied the QP band structure and optical absorption spectrum of  $N$ -ZSiCNRs. Moreover, Alaál *et al.* revealed that the GW band gap of 2-ZSiCNR was 2.4 eV,<sup>37</sup> which is larger than the HSE06 band gap (1.517 eV).<sup>36</sup> However, they found that the GW band gap of 3-ZSiCNR was 0.45 eV,<sup>37</sup> which is almost equal to the HSE06 band gap (0.401 eV).<sup>36</sup>

On the other hand, it is known that in low dimensional structure materials, such as graphene, carbon nanotubes, GNRs, as well as SiC sheets and single-walled SiC nanotubes, the electron–electron (e–e) correlations and electron–hole (e–h) interactions play a very important role in the electronic band structure and optical properties.<sup>38–48</sup> This is due to the fact that there are two key effects in low dimensional structure materials: one is the quantum confinement effect, another is the less efficient electronic screening effect. These two key effects will not only give rise to the enhancement of the electron–electron (e–e) correlations, where the enhanced electron–electron (e–e) correlations will lead to a large QP energy gap, but also the quantum confinement effect leads to a large overlap between the electron and hole wave functions resulting in reduced screening between e–h excitations, as a result, this leads to the formation of strongly bound excitons. Since ultra-narrow  $N$ -ZSiCNRs are a one-dimensional structure semiconductor, one can expect that there is a strong exciton effect in such a system. However, Alaál *et al.* show that 2-ZSiCNR has only one strongly bound exciton, originating from optical transition between the first valence band and the first conduction band around the Brillouin zone (BZ) Z-point.<sup>37</sup> What is even more surprising is that unlike 2-ZSiCNR, 3-ZSiCNR does not have any strongly bound excitons.<sup>37</sup> Why? Is that really so? To answer these questions, it is naturally needed to further study the quasiparticle



band structures and optical absorption spectra of the 2-ZSiCNRs and 3-ZSiCNRs.

Motivated by the above issues, we perform first-principles  $GW$ <sup>49,50</sup> and Bethe–Salpeter equation (BSE)<sup>50,51</sup> approaches to study the QP band structures, exciton level structures and optical absorption spectra of the 2-ZSiCNRs and 3-ZSiCNRs. It is excitingly found that the  $GW$  band gap of 3-ZSiCNR is 0.804 eV, which is almost more than two times larger than the Alaal *et al.*<sup>37</sup>  $GW$  band gap (0.45 eV). The  $GW$  band gap of 2-ZSiCNR is 2.911 eV, which is also larger than the Alaal *et al.*<sup>37</sup>  $GW$  band gap (2.4 eV). Moreover, it is found that the optical absorption spectra of the 2-ZSiCNRs are dominated by edge-state-derived excitons with large binding energy, composed of a characteristic series of exciton states, instead of only one exciton state. Even more excitingly, just like 2-ZSiCNR, the optical absorption spectra of the 3-ZSiCNRs are also dominated by edge-state-derived excitons with large binding energy, composed of a characteristic series of exciton states. The edge-state excitons of  $N$ -ZSiCNR belong to charge-transfer excitons, where the excited electron is confined to the Si edge, while the hole is confined to the C edge. The exciton binding energy increases with decreasing width  $N$ , which indicates that the quantum confinement effect enhances with decreasing width  $N$ . The excitons in 2-ZSiCNR can have a binding energy up to 1.78 eV. In addition, the exciton level structure and wave function characteristics are classified. It is very interesting to find a relationship between the node of the exciton wave functions and the incoming polarization light exciton excitation; for example when the incoming polarization light is parallel to the ribbon axis, the exciton whose wave function possesses an odd number of nodes is optically active, while the exciton whose wave function possesses an even number of nodes is optically inactive. However, when changing the light polarization from parallel to perpendicular to the ribbon axis, the exciton whose wave function possesses an odd number of nodes will become optically inactive, while the exciton whose wave function possesses an even number of nodes will become optically active. Lastly, the results that Alaal *et al.* recently studied are discussed.

## 2 Computational methods and model system

### 2.1 Model system

Regarding the model system, as shown in Fig. 1(a) and 2(a), we adopted a super cell geometry where the length of a vacuum region along the non-periodic direction ( $X$ - and  $Y$ -directions) was 28 Å. The lattice constant ( $c$ ) along the periodic direction ( $Z$ -direction) was 3.116 Å,<sup>36</sup> which is in agreement with the findings of other researchers.<sup>18,37</sup> A zigzag silicon carbon nanoribbon that is hydrogen-terminated ( $N$ -ZSiCNR) can be indexed by a width  $N$ , where  $N$  is the number of parallel zigzag chains across the ribbon width, such as that shown in Fig. 1(a) for  $N = 2$  and shown in Fig. 2(a) for  $N = 3$ .

### 2.2 Electronic ground state

Standard density functional theory (DFT) with a local density approximation (LDA) functional (DFT-LDA) is used for treating

all the electronic ground states of the systems, and is performed using the Quantum-ESPRESSO package.<sup>52</sup> The plane-wave cutoff was set as 60 Ry with a norm-conserving pseudopotential. The BZ integration has been performed with  $1 \times 1 \times 64$   $\mathbf{k}$ -point sampling points in the calculations. The structures were fully relaxed until an energy convergence of  $10^{-9}$  Ry and a force convergence on atoms of  $0.01 \text{ eV \AA}^{-1}$  were reached.

### 2.3 GW approximation

From the DFT-LDA wave functions and corresponding eigenvalues calculated above, the many-body effects on the QP band structure are calculated within the  $GW$  approximation, which is performed using the BerkeleyGW package.<sup>50</sup> In detail, starting from the DFT-LDA wave functions and Coulomb screening, the QP energies ( $E_{nk}$ ) are obtained by solving the Dyson's equation:<sup>49,50</sup>

$$[H_0 + \sum(E_{nk})]\psi_{nk} = E_{nk}\psi_{nk} \quad (1)$$

where  $H_0$  is the Hamiltonian in the Hartree approximation, and  $\psi_{nk}$  represents the QP wavefunction of energy  $E_{nk}$  within one-particle Green's function method. The equation is solved non-self-consistently, *i.e.*, within the  $G^0W^0$  approximation. The QP self-energy operator is given by  $\Sigma = iG^0W^0$ .  $G^0$  is the mean field one-particle Green's function and  $W^0$  is the screened Coulomb potential, which are constructed by the ground-state DFT-LDA wave functions and corresponding eigenvalues. To speak specifically, the vertex correction is approximated by a delta function and the irreducible polarizability  $P^0$  is given by  $P^0 = -iG^0G^0$ , which gives rise to a dynamical dielectric matrix within the random phase approximation (RPA) scheme and a generalized plasmon-pole (GPP) model.<sup>49</sup> After that, the screened Coulomb potential  $W^0$  is obtained from the bare Coulomb interaction  $v$  through the equation  $W^0 = v/[1 - vP^0]$ . In calculating the QP energies, a  $1 \times 1 \times 64$   $\mathbf{k}$ -point grid, a 12.0 Ry energy cutoff, and 320 unoccupied bands are used for computing the dielectric function and self-energy  $\Sigma$ , and the Coulomb truncation scheme has been adopted.<sup>39,44,45</sup>

### 2.4 Excitonic effects and exciton

The excitonic effects (electron–hole interactions), which are not included in  $GW$  itself, are included by solving the BSE in terms of two-particle Green's function, which is also performed using the BerkeleyGW package.<sup>50</sup> In detail, in the quasi-electron state  $|\mathbf{c}\mathbf{k}\rangle$  and quasi-hole state  $|\mathbf{v}\mathbf{k}\rangle$  direct product space  $|\mathbf{v}\mathbf{c}\mathbf{k}\rangle$  ( $|\mathbf{v}\mathbf{c}\mathbf{k}\rangle = |\mathbf{v}\mathbf{k}\rangle|\mathbf{c}\mathbf{k}\rangle$ ), the electron–hole excited state ( $|S\rangle$ ) is represented by the expansion<sup>50,51</sup>

$$|S\rangle = \sum_{\mathbf{k}} \sum_{c,v} A_{\mathbf{v}\mathbf{c}\mathbf{k}}^S |\mathbf{v}\mathbf{c}\mathbf{k}\rangle. \quad (2)$$

The amplitude  $A_{\mathbf{v}\mathbf{c}\mathbf{k}}^S$  is the excitonic wave function of the  $S$ th exciton in  $\mathbf{k}$ -space, which is obtained by solving the BSE<sup>50,51</sup>

$$(E_{\mathbf{c}\mathbf{k}} - E_{\mathbf{v}\mathbf{k}})A_{\mathbf{v}\mathbf{c}\mathbf{k}}^S + \sum_{\mathbf{k}'} \sum_{c',v'} \langle \mathbf{v}\mathbf{c}\mathbf{k} | K^{\text{eh}} | \mathbf{v}'\mathbf{c}'\mathbf{k}' \rangle A_{\mathbf{v}'\mathbf{c}'\mathbf{k}'}^S = \Omega^S A_{\mathbf{v}\mathbf{c}\mathbf{k}}^S. \quad (3)$$



The eigenvalue  $\Omega^S$  is the excitonic energy of the  $S$ th exciton.  $E_{\nu\mathbf{k}}$  and  $E_{c\mathbf{k}}$  indicate quasiparticle energies for the valence band state  $|\nu\mathbf{k}\rangle$  and conduction band state  $|c\mathbf{k}\rangle$  at a specific  $\mathbf{k}$  point, respectively.  $K^{eh}$  is the kernel, which describes the interaction between excited electrons and holes. For calculating, the kernel  $K^{eh}$  of the  $N$ -SiCNRs is computed on a coarse  $\mathbf{k}$ -point grid of  $1 \times 1 \times 64$  and then interpolated onto a fine  $\mathbf{k}$ -point grid of  $1 \times 1 \times 256$  to get converged exciton states,<sup>50,51</sup> and the Coulomb truncation scheme has been adopted.<sup>39,44,45</sup>

On the other hand, in  $\mathbf{r}_e$  and  $\mathbf{r}_h$  coordinate representation,  $\phi_{c\mathbf{k}}(\mathbf{r}_e) = \langle \mathbf{r}_e | c\mathbf{k} \rangle$ ,  $\phi_{\nu\mathbf{k}}(\mathbf{r}_h) = \langle \mathbf{r}_h | \nu\mathbf{k} \rangle$ , and  $\Phi_S(\mathbf{r}_e, \mathbf{r}_h) = \langle \mathbf{r}_e, \mathbf{r}_h | S \rangle$ , and then by eqn (2), the excitonic wave function in real space can be expressed as<sup>50,51</sup>

$$\Phi_S(\mathbf{r}_e, \mathbf{r}_h) = \sum_{\mathbf{k}} \sum_{c,\nu} A_{\nu\mathbf{k}}^S \phi_{c\mathbf{k}}(\mathbf{r}_e) \phi_{\nu\mathbf{k}}(\mathbf{r}_h) \quad (4)$$

where  $\phi_{c\mathbf{k}}(\mathbf{r}_e)$  and  $\phi_{\nu\mathbf{k}}(\mathbf{r}_h)$  are wave functions of the quasi-electron and quasi-hole in real space, respectively.  $\mathbf{r}_e$  and  $\mathbf{r}_h$  represent the positions of the quasi-electron and quasi-hole, and thus, the corresponding exciton states can be visualized in real space. For example, a simpler distribution of the electron amplitude square with the hole position fixed, *i.e.*,  $|\Phi_S(\mathbf{r}_e, \mathbf{r}_h = 0)|^2$ , can be used to reveal how the quasi-electron and quasi-hole in the photoexcited state are correlated in real space.<sup>50,51</sup>

## 2.5 Exciton energy level and binding energy

By solving eqn (3) we can get the exciton energy  $\Omega^S$ , *i.e.*, the excitonic energy of the  $S$  exciton. It is noted that  $S$  is an index mark in all excitons. In order to more clearly describe which quasi-electron and quasi-hole interaction leads to  $\Omega^S$ , we define the exciton energy level  $E_n^{ij}$ , *i.e.*, the excitonic energy of the  $n$ th exciton that the  $i$ th quasi-hole and  $j$ th quasi-electron interactions result in.

The exciton binding energy  $E_b^{ij}(n)$  is defined as

$$E_b^{ij}(n) = E^{ij} - E_n^{ij}, \quad (5)$$

namely, the energy difference between the interband transition energy  $E^{ij}$  (see vertical blue arrows in Fig. 1(b) and 2(b)) and the corresponding exciton energy level  $E_n^{ij}$ . The magnitude of  $E_b^{ij}(n)$  reflects the strength of the Coulomb attraction between the electron and the hole in the exciton, *i.e.*, the larger exciton binding energy stems from the stronger electron-hole interaction in the system.

## 2.6 Excitation optical absorption spectra

It is known that the excitation optical absorption spectra, one of the most fundamental techniques for directly probing electronic transitions in materials, are determined by the imaginary part of the macroscopic dielectric function  $\varepsilon_2(\omega)$ , which can be expressed as:<sup>50,51</sup>

$$\varepsilon_2(\omega) = \frac{16\pi^2 e^2}{\omega^2} \sum_S |\mathbf{e} \cdot \langle 0 | \mathbf{v} | S \rangle|^2 \delta(\omega - \Omega^S) \quad (6)$$

where  $\langle 0 | \mathbf{v} | S \rangle$  is the velocity matrix element.  $\mathbf{e}$  is the unit vector that indicates the direction of the polarization of light.  $\Omega^S$  is

given by eqn (3). When  $K^{eh} \neq 0$ , such a result includes the e-h interactions, labelled as “with e-h” in the following.

In contrast, when  $K^{eh} = 0$ ,  $\Omega^S = E_{c\mathbf{k}} - E_{\nu\mathbf{k}}$ , and then eqn (6) is reduced to

$$\varepsilon_2(\omega) = \frac{16\pi^2 e^2}{\omega^2} \sum_{\nu\mathbf{k}} |\mathbf{e} \cdot \langle \nu\mathbf{k} | \mathbf{v} | c\mathbf{k} \rangle|^2 \delta(\omega - E_{c\mathbf{k}} + E_{\nu\mathbf{k}}). \quad (7)$$

Such a result ignores the e-h interactions, marked as “without e-h” in the following.

It should be mentioned that the optical absorption spectra have a relationship with the incoming light polarization direction  $\mathbf{e}$ . In this paper, we research two different kinds of incoming light polarization direction  $\mathbf{e}$ , namely, (a) the  $\mathbf{e}$  that is parallel to the  $Z$ -axis, *i.e.*, along the  $N$ -ZSiCNr axis, called the longitudinal optical absorption spectrum and (b) the  $\mathbf{e}$  that is perpendicular to the  $Z$ -axis and is parallel to the  $Y$ -axis, called the transverse absorption spectrum. Of course, compared with the longitudinal optical absorption spectrum, the transverse absorption spectrum should be strongly suppressed owing to the ribbon geometrical anisotropy and the depolarization effect it produces.<sup>53</sup>

More details concerning the  $GW$  and BSE methods can be found in ref. 49–51.

## 3 Results and discussion

### 3.1 QP band structure

The  $GW$  and LDA band structures of 2-ZSiCNr and 3-ZSiCNr in the ground state are shown in Fig. 1(b) and 2(b), respectively. The blue dashed lines display the LDA band structures exhibiting a direct band gap at the  $Z$  point (0.957 eV for 2-ZSiCNr and 0.093 eV for 2-ZSiCNr), which is in good agreement with the recent PBE results.<sup>21</sup> The red open circles show the  $GW$  band structures. It is clear that when the e-e self-energy effects are included using the  $GW$  approximation, the band structure is strongly modified, except the direct band gap located at the  $Z$  point. As shown in Fig. 1(b) in the red open circles, the  $GW$  band gap of 2-ZSiCNr is 2.911 eV, which is more than three times larger than the LDA band gap (0.927 eV) and is also larger than a recent  $GW$  band gap (2.4 eV).<sup>37</sup> As shown in Fig. 2(b) in the red open circles, the  $GW$  band gap of 3-ZSiCNr is 0.804 eV, which is more than 9 times larger than the LDA band gap (0.093 eV) and is also almost more than two times larger than the recent  $GW$  band gap (0.45 eV).<sup>37</sup> Such large  $GW$  QP corrections to the LDA band gap originate from the enhance of e-e interactions owing to the enhanced quantum confinement and less efficient electronic screening in 1-dimensional structure semiconducting

**Table 1** The band gap energies  $E_g$  calculated by LDA, HSE06 and  $GW$  of  $N$ -SiCNrs. All values are in eV

$N$ -SiCNr	LDA	HSE06	$GW$
$N = 2$	0.957	1.621	2.911
$N = 3$	0.093	0.401	0.804





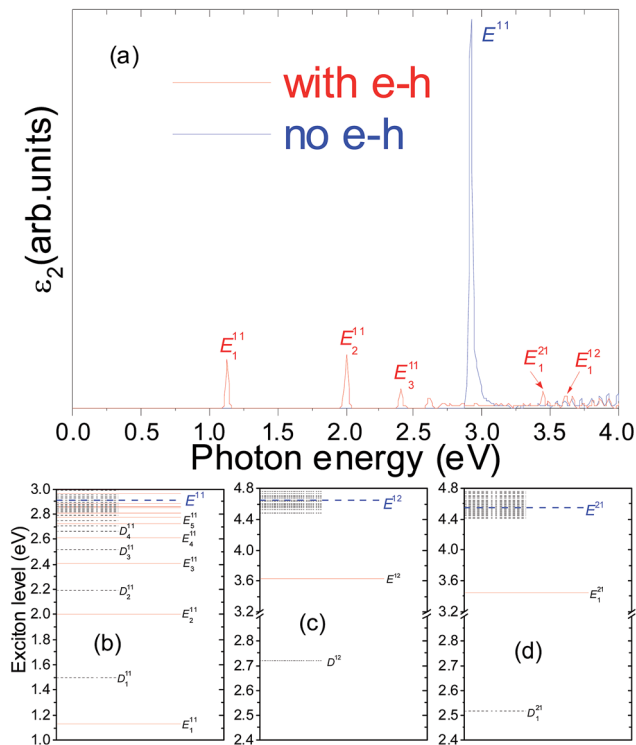


Fig. 4 (a) The transverse optical absorption spectra of 2-ZSiCNR with (red lines) and without (blue lines) including the effect of the electron–hole (e–h) interaction. (b), (c) and (d) are the schematic drawings of the energy levels of the excitons associated with the interband transitions  $E_n^{ij}$ , where  $E_n^{ij}$  and  $D_n^{ij}$  denote the  $n$ th bright and dark exciton states, respectively. The black dashed lines denote the dark exciton levels. The red solid lines show the bright exciton levels. The blue dashed lines denote the energy levels of the interband transitions.

which is located at 2.911 eV. After including the electron–hole interaction, the entire absorption spectrum of the 2-SiCNR changes dramatically, namely, the continuum interband transition peaks vanish, accompanying the appearance of new peaks below the onset of  $E^{11}$ . These dominating new peaks in the absorption spectrum are associated not only with the  $E_n^{12}$  series of bound excitons but also with the  $E_n^{21}$  and  $E_n^{21}$  series of bound excitons, such as  $E_1^{11}$  and  $E_2^{11}$  resulting from optical transition between the first valence band and the first conduction band around the Z-point,  $E_1^{12}$  resulting from optical transition between the first valence band and the second conduction band around the Z-point, and  $E_1^{21}$  resulting from optical transition between the second valence band and the first conduction band around the Z-point. It is clear that compared with the without electron–hole results, the absorption spectrum including the electron–hole interaction has a red shift with a change in the relative position of the peaks, *i.e.*, the first prominent peak  $E_1^{11}$  is located at 1.496 eV, which is in the visible light region, whereas the second strongest peak  $E_1^{12}$  is located at 2.71 eV, which is also in the visible light region. On the other hand, due to the fact that these excitons take off nearly all the continuum transition oscillator strengths, they will possess extraordinarily large electron hole binding energies. As expected, the  $E_1^{11}$  exciton binding energy  $E_b^{11}(1)$  is 1.48 eV. The

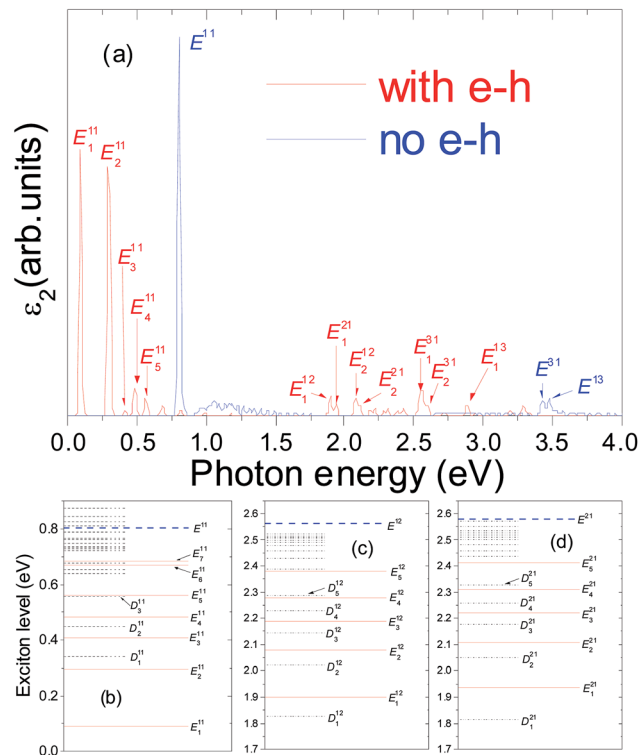


Fig. 5 (a) The longitudinal optical absorption spectra of 3-ZSiCNR with (red lines) and without (blue lines) including the effect of the electron–hole (e–h) interaction. (b), (c) and (d) are the schematic drawings of the energy levels of the excitons associated with the interband transitions  $E_n^{ij}$ , where  $E_n^{ij}$  and  $D_n^{ij}$  denote the  $n$ th bright and dark exciton states, respectively. The black dashed lines denote the dark exciton levels. The red solid lines show the bright exciton levels. The blue dashed lines denote the energy levels of the interband transitions.

$E_1^{12}$  exciton binding energy  $E_b^{12}(1)$  is 1.95 eV. It should be pointed out that  $E_1^{11}$  is not the lowest energy level of an exciton in the 2-SiCNR. As shown in Fig. 3(b), the lowest energy level of an exciton in the system belongs to  $D_1^{11}$ , which is a dark exciton state. More detailed discussions of the exciton state and level structure are referred to in Section 3.3.

For the longitudinal optical absorption spectrum of the 3-SiCNR, new peaks below the onset of  $E^{11}$  are associated only with the  $E_n^{11}$  series of bound excitons. However, new peaks associated with the  $E_n^{12}$  and  $E_n^{21}$  series of bound excitons (such as  $E_1^{12}$  and  $E_1^{21}$ ) are located above the  $E^{11}$  continuum, which is different compared to the 2-SiCNR. It is noted that the first strongest absorption peak  $E_1^{11}$  (see Fig. 5(a)) is located at 0.09 eV, which corresponds to an exciton binding energy  $E_b^{11}(1)$  of 0.714 eV. Moreover, as shown in Fig. 5(b),  $E_1^{11}$  is the lowest energy level of an exciton in the 3-SiCNR. Meanwhile the second strongest peak  $E_2^{11}$ , still resulting from optical transition between the first valence band and the second conduction band, is located at 0.29 eV, which corresponds to an exciton binding energy  $E_b^{11}(2)$  of 0.514 eV. In addition, the visible light peaks of the 3-SiCNR result from optical transitions between the first valence band and the second conduction band, between the second valence band and the first conduction band,



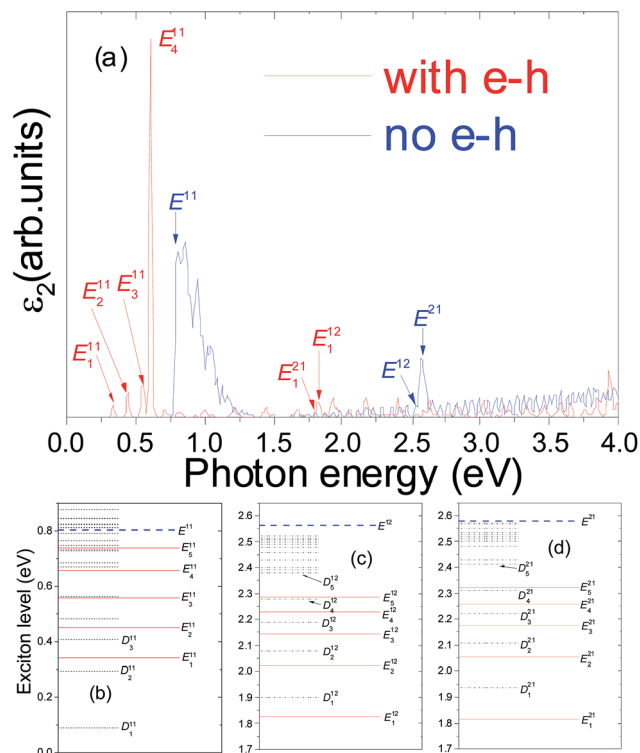


Fig. 6 (a) The transverse optical absorption spectra of 3-ZSiCNR with (red lines) and without (blue lines) including the effect of the electron–hole (e–h) interaction. (b), (c) and (d) are the schematic drawings of the energy levels of the excitons associated with the interband transitions  $E_n^{ij}$ , where  $E_n^{ij}$  and  $D_n^{ij}$  denote the  $n$ th bright and dark exciton states, respectively. The black dashed lines denote the dark exciton levels. The red solid lines show the bright exciton levels. The blue dashed lines denote the energy levels of the interband transitions.

between the first valence band and the third conduction band, and between the third valence band and the first conduction band, such as  $E_1^{12}$ ,  $E_1^{21}$  and  $E_1^{13}$ , as well as  $E_1^{31}$ .

As for the transverse absorption spectra of the 2-SiCNR and 3-SiCNR, compared with the corresponding longitudinal absorption spectra, the absorption peak positions and line shapes change obviously. For example, the lowest-energy absorption peak position of the 2-SiCNR (see Fig. 4(a) red  $E_1^{11}$ ) now moves downward to 1.128 eV, which is the position of the  $D_1^{11}$  dark exciton state in the longitudinal optical absorption spectrum. Now, as shown in Fig. 4(b),  $E_1^{11}$  is the lowest energy level of an exciton in the 2-SiCNR. The binding energy of the corresponding exciton  $E_b^{11}(1)$  is 1.78 eV. Moreover, unlike the longitudinal optical absorption spectrum, where the first prominent peak is  $E_1^{11}$ , we find that the first prominent peak of the transverse absorption spectrum is  $E_2^{11}$ .

For the transverse absorption spectrum of the 3-SiCNR, in contrast to the absorption peak red shift of the 2-SiCNR, the absorption peak of the 3-SiCNR appears to blue shift, *i.e.*, the lowest-energy absorption peak  $E_1^{11}$  (see Fig. 6(a)) now moves upward to 0.34 eV, which is the position of the  $D_1^{11}$  dark exciton state in the longitudinal optical absorption spectrum. As a result, as shown in Fig. 6(b),  $E_1^{11}$  is no longer the lowest energy

level of an exciton in the 3-SiCNR. Now, the lowest energy level of an exciton in the system belongs to  $D_1^{11}$ , which is the dark exciton. The binding energy of the corresponding exciton  $E_b^{11}(1)$  is 0.464 eV. In addition, unlike the longitudinal optical absorption spectrum, where the first prominent peak is  $E_1^{11}$ , we find that the first prominent peak of the transverse absorption spectrum is  $E_4^{11}$ .

In addition, it should be mentioned that for lower dimensional systems,<sup>54,55</sup> the supercell calculation will lead to an artificial size effect on the dielectric function. In order to eliminate such an artificial size effect, for the  $N$ -ZSiCNR, the optical spectrum in the polarizability per unit area is defined as  $\alpha_2(\omega) = A_{\perp} \varepsilon_2(\omega)/4\pi$ , where  $A_{\perp}$  is the cross-sectional area of the supercell perpendicular to the  $N$ -ZSiCNR axis. The optical spectra in the polarizability per unit area are shown in ESI Fig. S7 and S8.† Clearly, there is no difference between Fig. 3(a), 4(a), 5(a) and 6(a) and the corresponding Fig. S7(a) and (b) and S8(a) and (b),† except for the unit. This is due to the fact that for a given supercell,  $A_{\perp}$  is a constant.

### 3.3 Exciton level structure and wave functions

In order to gain further insight into the above results, the exciton level structure and the corresponding exciton wave functions are plotted. The exciton level structure of the 2-ZSiCNR and 3-ZSiCNR are shown in (b), (c) and (d) of Fig. 3, 4, 5, and 6. It should be pointed out that from solving eqn (3) to obtain the excitonic energy, we know that the exciton level structure is the intrinsic property of the system. However, in order to mark whether the excitons are excited in the optical absorption spectrum or not, the excitons are classified into bright excitons ( $E$ ) and dark excitons ( $D$ ). In addition, from solving eqn (3) and (6) to obtain the optical absorption spectrum, we know that  $\mathbf{e} \cdot \langle 0|\mathbf{v}|S\rangle$  of eqn (6) represents the  $S$ th exciton contribution to the optical absorption spectrum, namely,  $\mathbf{e} \cdot \langle 0|\mathbf{v}|S\rangle$  will give rise to the  $S$ th exciton peak in the optical absorption spectrum under the  $\mathbf{e}$  direction polarization light. In general, for the  $S$ th exciton there are two possible results: one is  $\mathbf{e} \cdot \langle 0|\mathbf{v}|S\rangle \neq 0$ , namely the peak of the  $S$ th exciton will appear in the optical absorption spectrum, which is labelled the bright exciton, *i.e.*, optically active exciton; the other is  $\langle 0|\mathbf{v}|S\rangle \neq 0$  but  $\mathbf{e} \cdot \langle 0|\mathbf{v}|S\rangle = 0$ , *i.e.*,  $\mathbf{e} \perp \langle 0|\mathbf{v}|S\rangle$ , namely, although there exists an  $S$ th exciton, the peak of the  $S$ th exciton does not appear in the optical absorption spectrum, which is labelled the dark exciton, *i.e.*, optically inactive exciton.

For example, (b), (c) and (d) of Fig. 3 show the exciton level structure associated with the interband transitions  $E_n^{ij}$  in 2-SiCNR for light polarized along the ribbon axis ( $\mathbf{e}||Z$ ), where  $E_n^{ij}$  and  $D_n^{ij}$  denote the  $n$ th bright and dark exciton states, respectively. Superscript  $ij$  denotes the excitation originated from optical transition between the  $i$ th valence band and the  $j$ th conduction band, counted from the band gap. In order to describe the exciton level structure more clearly,  $E_n^{ij}$  and  $D_n^{ij}$  associated with the interband transitions  $E_n^{ij}$  are called as the  $E_n^{ij}$  series of excitons. In the  $E_n^{ij}$  series of excitons, the exciton of the lowest energy level is called the “ground state” exciton. For example, as shown in Fig. 3(b),  $D_1^{11}$ ,  $E_1^{11}$ ,  $D_2^{11}$ ,  $E_2^{11}$ ,  $D_3^{11}$ , and



**Table 2** Excitonic energy (in eV) of the first three lowest bright and dark excitons in 2-SiCNR, when  $\mathbf{e}||Z$  and  $\mathbf{e}||Y$ 

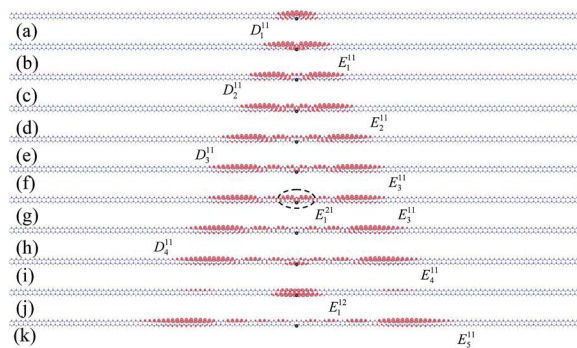
$\mathbf{e}  Z$	$D_1^{11}$	$E_1^{11}$	$D_2^{11}$	$E_2^{11}$	$D_3^{11}$	$E_1^{21}, E_3^{11}$
	1.128	1.496	2.005	2.191	2.407	2.489
$\mathbf{e}  Y$	$E_1^{11}$	$D_1^{11}$	$E_2^{11}$	$D_2^{11}$	$E_3^{11}$	$D_1^{21}, D_3^{11}$

**Table 3** Excitonic energy (in eV) of the first three lowest bright and dark excitons in 3-SiCNR, when  $\mathbf{e}||Z$  and  $\mathbf{e}||Y$ 

$\mathbf{e}  Z$	$E_1^{11}$	$E_2^{11}$	$D_1^{11}$	$E_3^{11}$	$D_2^{11}$	$D_3^{11}$
	0.09	0.294	0.342	0.408	0.45	0.558
$\mathbf{e}  Y$	$D_1^{11}$	$D_2^{11}$	$E_1^{11}$	$D_3^{11}$	$E_2^{11}$	$E_3^{11}$

$E_3^{11}$  belong to the  $E^{11}$  series of excitons. Clearly,  $D_1^{11}$  is the ground state exciton, which is the dark exciton state. However, when changing the light polarization from parallel ( $\mathbf{e}||Z$ ) to perpendicular to the ribbon axis ( $\mathbf{e}||Y$ ), as shown in Fig. 4(b), the ground state exciton turns into  $E_1^{11}$ , *i.e.*, the bright exciton state. For the  $E^{12}$  series of excitons, as shown in Fig. 3(c), the ground state exciton is  $E_1^{12}$ , which is the bright exciton state. However, when changing the light polarization from parallel ( $\mathbf{e}||Z$ ) to perpendicular to the ribbon axis ( $\mathbf{e}||Y$ ), as shown in Fig. 4(c), the ground state exciton turns into  $D_1^{12}$ , *i.e.*, the dark exciton state. Similarly, for the  $E^{21}$  series of excitons, as shown in Fig. 3(d), the ground state exciton is  $E_1^{21}$ , which is the bright exciton state. However, when changing the light polarization from parallel ( $\mathbf{e}||Z$ ) to perpendicular to the ribbon axis ( $\mathbf{e}||Y$ ), as shown in Fig. 4(d), the ground state exciton turns into  $D_1^{21}$ , *i.e.*, the dark exciton state. The excitonic energies of the first three lowest bright and dark excitons in the 2-SiCNR and 3-SiCNR, when  $\mathbf{e}||Z$  and  $\mathbf{e}||Y$ , are respectively summarized in Tables 2 and 3, which clearly show that whether an exciton is a bright exciton (optically active exciton) or a dark exciton (optically inactive exciton) is strongly dependent on the incoming light polarization direction  $\mathbf{e}$ .

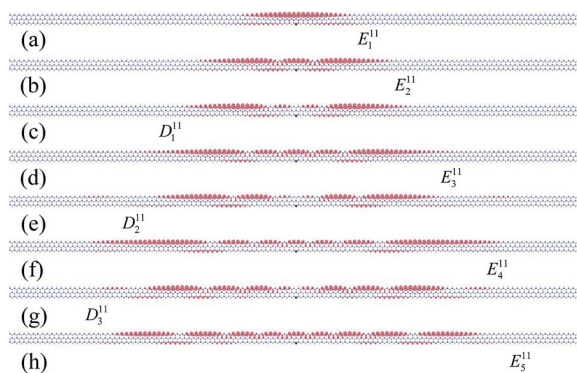
In order to further investigate the exciton properties of the 2-ZSiCNR and 3-ZSiCNR, the electron amplitude squared ( $|\Phi_S(\mathbf{r}_e, \mathbf{r}_h = 0)|^2$ ), the real-space charge distribution of the excitons at a fixed hole position (black dot on top of a C atom), is plotted in Fig. 7, 8, 9 and 10. It should be pointed out that from solving eqn (3) and (2) to obtain the exciton wave function, we know that the exciton wave function is the intrinsic property of the system, while the bright and dark marks of the exciton wave function originate from the corresponding exciton marks. Thus, just like the bright and dark marks of the exciton, the bright and dark marks of the exciton wave function are strongly dependent on the incoming light polarization direction  $\mathbf{e}$ . The bright and dark marks in Fig. 7–10 are linked with the longitudinal optical absorption spectra, *i.e.*, the incoming light polarization direction  $\mathbf{e}$  parallel to the ribbon axis ( $\mathbf{e}||Z$ ). Taking the optical absorption spectra of 2-ZSiCNR as an example, as shown in Fig. 7(a) and (b), the exciton wave function of Fig. 7(a) is marked as  $D_1^{11}$ , while the exciton wave function of Fig. 7(b) is marked as  $E_1^{11}$ . However, when changing the light polarization from



**Fig. 7** Exciton wave functions of 2-ZSiCNR for the first 10 lowest bright and dark excitons associated with the interband transitions  $E^{11}$ ,  $E^{21}$ , and  $E^{12}$ . (a)  $D_1^{11}$ , (b)  $E_1^{11}$ , (c)  $D_2^{11}$ , (d)  $E_2^{11}$ , (e)  $D_3^{11}$ , (f)  $E_3^{11}$ , (g)  $E_2^{21}$  and  $E_3^{11}$ , (h)  $D_4^{11}$ , (i)  $E_4^{11}$ , (j)  $E_1^{12}$ , and (k)  $E_5^{11}$ . The bright and dark marks are under the incoming light polarization direction  $\mathbf{e}||Z$ . The hole (black spot) is fixed on top of a C atom (dark yellow spheres). The electron amplitude squared  $|\Phi_S(\mathbf{r}_e, \mathbf{r}_h = 0)|^2$  in arbitrary units (a.u.) is shown by a red.

parallel ( $\mathbf{e}||Z$ ) to perpendicular to the ribbon axis ( $\mathbf{e}||Y$ ), the exciton wave function of Fig. 7(a) should be marked as  $E_1^{11}$  owing to the corresponding exciton turning into a bright exciton, while the exciton wave function of Fig. 7(b) should be marked as  $D_1^{11}$  owing to the corresponding exciton turning into a dark exciton.

It is clear that the wave functions plotted in Fig. 7–10 display a common feature of the exciton wave function, namely the spatial extent of the exciton wave function. The spatial extents of the excitons are closely related to their corresponding binding energies, *i.e.*, the smaller the spatial extent of the exciton, the larger the exciton binding energy. Therefore, in the  $E^{ij}$  series, the spatial extent of  $E_n^{ij}$ , as well as that of  $D_n^{ij}$ , increases with  $n$  increasing. Taking Fig. 9 as an example, in the  $E^{12}$  series, the spatial extent of  $D_1^{12}$  is the smallest, which is the ground-state exciton, while the spatial extent of  $E_5^{12}$  is the largest. Therefore,



**Fig. 8** Exciton wave functions of 3-ZSiCNR for the first 8 lowest bright and dark excitons associated with the interband transitions  $E^{11}$ . (a)  $E_1^{11}$ , (b)  $E_2^{11}$ , (c)  $D_1^{11}$ , (d)  $E_3^{11}$ , (e)  $D_2^{11}$ , (f)  $E_4^{11}$ , (g)  $D_3^{11}$ , and (h)  $E_5^{11}$ . The bright and dark marks are under the incoming light polarization direction  $\mathbf{e}||Z$ . The hole (black spot) is fixed on top of a C atom (dark yellow spheres). The electron amplitude squared  $|\Phi_S(\mathbf{r}_e, \mathbf{r}_h = 0)|^2$  in arbitrary units (a.u.) is shown by a red.



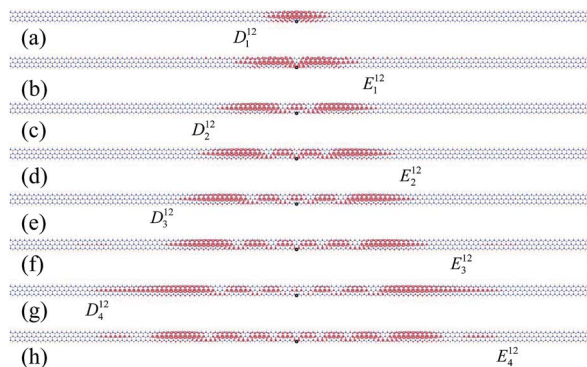


Fig. 9 Exciton wave functions of 3-ZSiCNR for the first 8 lowest bright and dark excitons associated with the interband transitions  $E^{12}$ . (a)  $D_1^{12}$ , (b)  $E_1^{12}$ , (c)  $D_2^{12}$ , (d)  $E_2^{12}$ , (e)  $D_3^{12}$ , (f)  $E_3^{12}$ , (g)  $D_4^{12}$ , and (h)  $E_4^{12}$ . The bright and dark marks are under the incoming light polarization direction  $\mathbf{e} \parallel Z$ . The hole (black spot) is fixed on top of a C atom (dark yellow spheres). The electron amplitude squared  $|\phi_5(\mathbf{r}_e, \mathbf{r}_h = 0)|^2$  in arbitrary units (a.u.) is shown by a red.

the binding energy of the ground-state exciton is the largest in the same series of excitons, for example, the binding energy of  $D_1^{12}$  is the largest in the  $E^{12}$  series. Note that each 2-ZSiCNR in Fig. 7, as well as each 3-ZSiCNR Fig. 8–10, consists of 128 unit cells. It is clear that the extent of  $D_1^{11}$  of 2-ZSiCNR is smaller than that of  $E_1^{11}$  of 3-ZSiCNR, which indicates that the binding energy of  $D_1^{11}$  of 2-ZSiCNR is larger than that of  $E_1^{11}$  of 3-ZSiCNR. On the other hand, in the excitons of 3-ZSiCNR, the spatial extent of  $E_1^{21}$  is the smallest, then the extent of exciton  $E_1^{12}$  is smaller than that of exciton  $E_1^{11}$ . Thus, the binding energy of exciton  $E_1^{21}$  is the maximum (0.786 eV), and the binding energy of exciton  $E_1^{12}$  (0.744 eV) is larger than that of exciton  $E_1^{11}$  (0.715 eV).

However, the exciton wave functions of  $N$ -ZSiCNR also display several unique characteristics. As shown in Fig. 7, 8, and 10, for the  $E^{11}$  and  $E^{21}$  series of excitons, one of the most striking characteristics is that the electron is confined to the Si edge

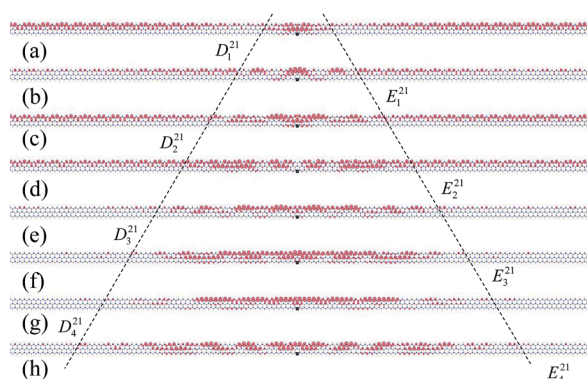


Fig. 10 Exciton wave functions of 3-ZSiCNR for the first 8 lowest bright and dark excitons associated with the interband transitions  $E^{21}$ . (a)  $D_1^{21}$ , (b)  $E_1^{21}$ , (c)  $D_2^{21}$ , (d)  $E_2^{21}$ , (e)  $D_3^{21}$ , (f)  $E_3^{21}$ , (g)  $D_4^{21}$ , and (h)  $E_4^{21}$ . The bright and dark marks are under the incoming light polarization direction  $\mathbf{e} \parallel Z$ . The hole (black spot) is fixed on top of a C atom (dark yellow spheres). The electron amplitude squared  $|\phi_5(\mathbf{r}_e, \mathbf{r}_h = 0)|^2$  in arbitrary units (a.u.) is shown by a red.

while the hole is confined to the C edge, namely, the electrons and holes are separated spatially onto different edges. Such a kind of electron and hole spatial separation means that any of these excitons being formed gives rise to the fact that a charge transfer occurs in the system. Finally, such a charge transfer will affect the recombination time and diffusion processes of the electron–hole pairs. In contrast, the  $E^{12}$  series of excitons shows a different charge distribution. As shown in Fig. 9 and 7(j) ( $E_1^{12}$ ), the electron distribution of the  $E^{12}$  series of excitons is extended over the width of the ribbon, instead of being confined to one edge. What is the origin of such characteristics of electron distribution? From a previous study,<sup>21</sup> we know that near the  $Z$ -point of the Brillouin zone, the first valence band originates from the  $p_z$  atomic orbitals of the edge C atoms and the first conduction band originates from the  $p_z$  atomic orbitals of the edge Si atoms, which are called the edge states. It is clear that  $E_n^{12}$  involving the electron state is the second conduction band, which does not belong to the edge state. In contrast, both  $E^{11}$  and  $E^{21}$  involving electron states are the first conduction band (Si edge), which is the edge state. As a result, the electron distribution of the  $E^{12}$  series of excitons is extended over the width of the ribbon, while for both the  $E^{11}$  and  $E^{21}$  series of excitons, the excited electron locates on the Si edge and the hole locates on the C edge. The  $E^{11}$  series of excitons are called the edge-state excitons, owing to the fact that the excited electron and hole result from edge states. Moreover, the edge-state excitons of  $N$ -ZSiCNR belong to charge-transfer excitons, owing to the fact that the excited electron and hole are confined to opposite edges.

It is very interesting to find a relationship between the node of the exciton wave functions and the incoming polarization light exciton excitation. We note that all exciton wave functions have symmetrical characteristics. In general, the wave functions of the excitons have nodes (zeros). In the  $E^{ij}$  series, the nodes of the wave function of  $E_n^{ij}$ , as well as those of  $D_n^{ij}$ , increase with  $n$  increasing. For example, as shown in Fig. 9,  $D_1^{12}$  is the ground state, and thus the wave function of  $D_1^{12}$  has no node. However,  $E_1^{12}$  is the first excited state, and thus the wave function has one node.  $D_2^{12}$  is the second excited state, and thus the wave function has two nodes, *etc.* On the other hand, under incoming light polarization direction  $\mathbf{e}$ , whether an exciton is excited in the optical absorption spectrum or not is simply dependent on the odd or even number nodes of its wave function. If the exciton whose wave function possesses an even number of nodes is optically active, the exciton whose wave function possesses an odd number of nodes must be optically inactive and *vice versa*. For example, as shown in Fig. 9, the excitons whose wave functions possess an odd number of nodes are optically active, such as  $E_1^{12}$ ,  $E_2^{12}$ , and  $E_3^{12}$ , while the excitons whose wave functions possess an even number of nodes are optically inactive, such as  $D_1^{12}$ ,  $D_2^{12}$ , and  $D_3^{12}$ , *etc.* However, when changing the light polarization from parallel ( $\mathbf{e} \parallel Z$ ) to perpendicular to the ribbon axis ( $\mathbf{e} \parallel Y$ ), the excitons whose wave functions possess an odd number of nodes are optically inactive, while the excitons whose wave functions possess an even number of nodes are optically active (refer to the marks of Fig. 6(c)).



The above relationship between the node of the exciton wave functions and the incoming polarization light exciton excitation can be understood further using an electric dipole moment model. It is noted that in eqn (6),  $\langle 0|\mathbf{v}|S\rangle \neq 0$  is the electric dipole moment of the  $S$ th exciton. That is to say, each exciton possesses a definitive electric dipole moment. On the other hand, due to its quasio-one-dimensional ribbon structure, there are two symmetrical directions in  $N$ -ZSiCNR; one is the longitudinal direction and another is the transverse direction. Thus, the dipole polar moment direction of the exciton is either transverse or longitudinal. Moreover, the electric dipole moment direction has a relationship with the node of the exciton wave function. For example, if the dipole polar direction of the wave function with an odd number of nodes is along the longitudinal direction, then the dipole moment direction of the wave function with an even number of nodes is perpendicular to the longitudinal direction (along the transverse direction). Therefore, in the longitudinal optical absorption spectra, the exciton of the wave function with an odd number of nodes is optically active (bright), while the exciton of the wave function with an even number of nodes is optically inactive (dark, dipole forbidden). In contrast, in the transverse absorption spectra, the exciton of the wave function with an odd number of nodes is optically inactive (dark, dipole forbidden), while the exciton of the wave function with an even number of nodes is optically active (bright).

It is noted that there is a dotted ellipse in Fig. 7(g), which marks out the region of the  $E_1^{21}$  wave function. From Table 2, we can see that the energy levels of  $E_1^{21}$  and  $E_3^{11}$  are 2.489 eV (see (b) and (d) of Fig. 3 and 4), namely, the degeneracy of the energy levels of  $E_1^{21}$  and  $E_3^{11}$ . In order to compare the  $E_1^{21} + E_3^{11}$  wave function with the  $E_3^{11}$  wave function, as shown in Fig. 7(f), we also plot the  $E_3^{11}$  wave function. It is clear that the  $E_1^{21} + E_3^{11}$  wave function is different from the  $E_3^{11}$  wave function. Moreover, the binding energy of  $E_3^{11}$  is 0.422 eV, while the binding energy of  $E_1^{21}$  is 2.0586 (eV). However, both the  $E_1^{21} + E_3^{11}$  wave function and  $E_3^{11}$  wave function possess the same type of nodes, *i.e.*, both  $E_3^{11}$  and  $E_1^{21} + E_3^{11}$  have an odd number of nodes. The  $E_3^{11}$  wave function has 5 nodes,  $E_1^{21} + E_3^{11}$  also has 5 nodes, and  $E_1^{21}$  has one node. Thus, when the incoming light polarization is parallel to the  $Z$ -axis, both  $E_3^{11}$  and  $E_1^{21}$  are optically active (bright exciton, refer to the marks of Fig. 3(b) and (d)). When changing the light polarization from parallel ( $\mathbf{e}\parallel Z$ ) to perpendicular to the ribbon axis ( $\mathbf{e}\parallel Y$ ),  $E_3^{11}$  becomes the optically inactive  $D_3^{11}$  (dark exciton, refer to the marks of Fig. 4(b)) and  $E_1^{21}$  becomes the optically inactive  $D_1^{21}$  (dark exciton, refer to the marks of Fig. 4(d)). As for the weight of the wave functions for  $E_1^{21}$  and  $E_3^{11}$  in Fig. 7(g), refer to ESI Table 1.†

Moreover, the degeneracy of the energy levels also occurs in the excitons of 3-ZSiCNR. It is noted that there are two auxiliary lines (drawn with dashed lines) in Fig. 10, which mark out the region of the  $E^{21}$  series exciton wave functions. As listed in ESI Table 2,† it is clear that there is energy level degeneracy between the  $E^{21}$  series excitons and the  $E^{11}$  series excitons. It is this degeneracy that give rise to the overlap between the  $E^{21}$  series exciton wave functions and the  $E^{11}$  series exciton wave functions. The weight of the wave functions for  $E^{21}$  and  $E^{11}$  in Fig. 10

are referred to in ESI Table 2.† For example, for Fig. 10(a), the weight of the wave function of the  $E^{11}$  series exciton (75th exciton) is 0.62481, while the weight of the wave function of the  $E^{21}$  series exciton (first exciton, *i.e.*,  $D_1^{21}$ ) is 0.34912.

Lastly, we discuss the results that Alaal *et al.* recently obtained. It is noted that they found that the  $GW$  band gap of 2-ZSiCNR was 2.4 eV, which is larger than the HSE06 band gap (1.517 eV)<sup>36</sup> but smaller than our obtained  $GW$  band gap (2.911 eV). For 3-ZSiCNR, their obtained  $GW$  band gap was 0.45 eV, which is almost equal to the HSE06 band gap (0.401 eV)<sup>36</sup> and is almost half of our  $GW$  band gap (0.804 eV). Clearly their obtained  $GW$  band gaps are smaller than our obtained  $GW$  band gaps, particularly the  $GW$  band gap of 3-ZSiCNR. The differences between their results and our results originate from two facts. It is well known that the quasiparticle band gap from the  $GW$  calculations with or without the Coulomb truncation scheme can differ significantly. The Coulomb truncation scheme can remove image effects directly and leads to well converged results for modest-sized periodic cells, while in the scheme without Coulomb truncation, owing to the computational constraints, it is impossible to obtain a fully converged band gap simply by expanding the length of a vacuum region along the non-periodic direction.<sup>39,44,45</sup> One fact is that in calculating the QP energies, we adopted the Coulomb truncation scheme, while Alaal *et al.* do not adopt the Coulomb truncation scheme. Another fact is that in calculating the QP energies, we adopted a  $1 \times 1 \times 64$   $\mathbf{k}$ -point grid, while Alaal *et al.* adopted a  $1 \times 1 \times 32$   $\mathbf{k}$ -point grid. Speaking specifically for the  $GW$  band gap of 3-ZSiCNR, the difference between our calculation results and the results from Alaal *et al.* originates from the above two facts. As for the  $GW$  band gap of 2-ZSiCNR, the difference between our calculation result and the results from mainly originates from the use of the Coulomb truncation scheme, because the  $GW$  band gap of 2-ZSiCNR with respect to a  $1 \times 1 \times 32$   $\mathbf{k}$ -point grid has been converged, while the  $GW$  band gap of 3-ZSiCNR does not (refer to ESI Table 3†).

On the other hand, as for the transverse absorption spectra, they found only one strongly bound exciton absorption peak in the transverse absorption spectra of the 2-ZSiCNR. Moreover, they fail to find any strongly bound exciton absorption peak in the transverse absorption spectra of the 3-ZSiCNR. However, we find that the optical absorption spectra of the 2-ZSiCNR and 3-ZSiCNR are dominated by edge-state-derived excitons with large binding energy, composed of a characteristic series of exciton states. The differences between the results from Alaal *et al.* and our results originate from three facts. The first fact is that in calculating the QP energies, we adopted the Coulomb truncation scheme, while Alaal *et al.* do not adopt the Coulomb truncation scheme. The second fact is that in calculating the QP energies, we adopted a  $1 \times 1 \times 64$   $\mathbf{k}$ -point grid, while Alaal *et al.* adopted a  $1 \times 1 \times 32$   $\mathbf{k}$ -point grid. These lead to the difference in the  $GW$  band gap, and therefore lead to the transverse absorption spectra difference. The third fact is that in calculating the kernel  $K^{\text{eh}}$ , we not only adopted the Coulomb truncation scheme, but also adopted a coarse  $\mathbf{k}$ -point grid of  $1 \times 1 \times 64$  and then interpolated onto a fine  $\mathbf{k}$ -point grid of  $1 \times 1 \times 256$  to get converged exciton states,<sup>50,51</sup> while Alaal *et al.* only



adopted a  $1 \times 1 \times 32$  **k**-point grid. This directly leads to the transverse absorption spectra difference. Speaking specifically for the optical absorption spectra of the 3-ZSiCNR, that they fail to find any strongly bound exciton absorption peak in the transverse absorption spectra originates from the above three facts. As for 2-ZSiCNR, that they found only one strongly bound exciton absorption peak in the transverse absorption spectra mainly originates from the fact that they do not adopt the Coulomb truncation scheme, and the optical absorption spectra of the 2-ZSiCNR with respect to the  $1 \times 1 \times 32$  **k**-point grid has been converged, while the optical absorption spectra of the 3-ZSiCNR does not (referring to ESI Fig. 3–6†).

## 4 Conclusions

In summary, the electronic and optical properties of the 2-ZSiCNR and 3-ZSiCNR have been studied by means of first principles *GW* + BSE calculations. Quasi-particle *GW* self-energy corrections remarkably widened the corresponding Kohn-Sham band gaps: namely, the *GW* band gap of 2-ZSiCNR is 2.911 eV, which is more than three times larger than the Kohn-Sham band gap (0.957 eV), and the *GW* band gap of 3-ZSiCNR is 0.804 eV, which is more than nine times larger than the Kohn-Sham band gap (0.093 eV). By solving the BSE on top of the *GW* approximation, we demonstrated that the optical absorption spectra of the 2-ZSiCNR and 3-ZSiCNR are dominated by strong excitonic effects with the formation of strongly bound excitons. In the longitudinal optical absorption spectra, the binding energy of the first absorption peak exciton is 1.5 eV for 2-ZSiCNR and 0.8 eV for 3-ZSiCNR. However, in the transverse optical absorption spectra, the binding energy of the first absorption peak exciton of 2-ZSiCNR increases to 1.78 eV owing to the first absorption peak red shift, while the binding energy of the first absorption peak exciton of 3-ZSiCNR decreases to 0.464 eV owing to the first absorption peak blue shift. It is very interesting to find a relationship between the node of the exciton wave functions and the incoming polarization light exciton excitation. In the longitudinal optical absorption spectra, the exciton whose wave function possesses an odd number of nodes is optically active, while the exciton whose wave function possesses an even number of nodes is optically inactive. However, when changing the light polarization from parallel ( $\mathbf{e} \parallel Z$ ) to perpendicular to the ribbon axis ( $\mathbf{e} \parallel Y$ ), the exciton whose wave function possesses an odd number of nodes becomes optically inactive, while the exciton whose wave function possesses an even number of nodes becomes optically active. The rich physical properties of the 2-ZSiCNR and 3-ZSiCNR make them promising materials for photochemical catalysis, as well as for nanoscale photonic and optoelectronic devices. In addition, the above results may also provide valuable information for understanding the physical properties of other low-dimensional materials.

## Conflicts of interest

There are no conflicts to declare.

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## References

- 1 Y.-W. Son, M. L. Cohen and S. G. Louie, *Phys. Rev. Lett.*, 2006, **97**, 216803.
- 2 K. Nakada, M. Fujita, G. Dresselhaus and M. S. Dresselhaus, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 1996, **54**, 17954.
- 3 M. Fujita, K. Wakabayashi, K. Nakada and K. Kusakabe, *Peculiar, J. Phys. Soc. Jpn.*, 1996, **65**, 1920–1923.
- 4 H. Lee, Y.-W. Son, N. Park, S. Han and J. Yu, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2005, **72**, 174431.
- 5 Y.-W. Son, M. L. Cohen and S. G. Louie, *Nature*, 2006, **444**, 347–349.
- 6 W. Y. Kim and K. S. Kim, *Nat. Nanotechnol.*, 2008, **3**, 408–412.
- 7 D. Yu, E. M. Lupton, M. Liu, W. Liu and F. Liu, *Nano Res.*, 2008, **1**, 56–62.
- 8 D. Yu, E. M. Lupton, H. J. Gao, C. Zhang and F. Liu, *Nano Res.*, 2008, **1**, 497–501.
- 9 Z. F. Wang, S. Jin and F. Liu, *Phys. Rev. Lett.*, 2013, **111**, 096803.
- 10 O. Hod, V. Barone, J. E. Peralta and G. E. Scueria, *Nano Lett.*, 2007, **7**, 2295–2299.
- 11 E.-J. Kan, Z. Li, J.-L. Yang and J. G. Hou, *J. Am. Chem. Soc.*, 2008, **130**, 4224–4225.
- 12 M. H. Wu, X. J. Wu and X. C. Zeng, *J. Phys. Chem. C*, 2010, **114**, 3937–3944.
- 13 D. Gunlycke, J. Li, J. W. Mintmire and C. T. White, *Appl. Phys. Lett.*, 2007, **91**, 112108.
- 14 M. H. Wu, Y. Pei and X. C. Zeng, *J. Am. Chem. Soc.*, 2010, **132**, 5554–5555.
- 15 X. Chen, Y. Liu, B.-L. Gu, W. Duan and F. Liu, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2014, **90**, 121403(R).
- 16 D. Krepel, J. E. Peralta, G. E. Scuseria and O. Hod, *J. Phys. Chem. C*, 2016, **120**, 3791–3797.
- 17 A. H. CastroNeto, F. Guinea, N. M. R. Peres, K. S. Novoselov and A. K. Geim, *Rev. Mod. Phys.*, 2009, **81**, 109–162.
- 18 L. Sun, Y. Li, Z. Li, Q. Li, Z. Zhou, Z. Chen, J. Yang and J. G. Hou, *J. Chem. Phys.*, 2008, **129**, 174114.
- 19 E. Bekaroglu, M. Topsakal, S. Cahangirov and S. Ciraci, *Phys. Rev. B: Condens. Matter*, 2010, **81**, 075433.
- 20 J. M. Zhang, F. L. Zheng, Y. Zhang and V. Ji, *J. Mater. Sci.*, 2010, **45**, 3259–3265.
- 21 P. Lou and J. Y. Lee, *J. Phys. Chem. C*, 2009, **113**, 12637–12640.
- 22 P. Lou and J. Y. Lee, *J. Phys. Chem. C*, 2009, **113**, 21213–21217.
- 23 P. Lou and J. Y. Lee, *J. Phys. Chem. C*, 2010, **114**, 10947–10951.
- 24 P. Lou and J. Y. Lee, *Bull. Korean Chem. Soc.*, 2012, **33**, 763–769.
- 25 F.-L. Zheng, Y. Zhang, J.-M. Zhang and K.-W. Xu, *Phys. Status Solidi B*, 2011, **248**, 1676–1681.



- 26 P. Lou, *Phys. Chem. Chem. Phys.*, 2011, **13**, 17194–17204.
- 27 P. Lou, *Phys. Status Solidi B*, 2012, **249**, 91–98.
- 28 P. Lou, *J. Mater. Chem. C*, 2013, **1**, 2996–3003.
- 29 P. Lou, *Phys. Status Solidi B*, 2014, **251**, 423–434.
- 30 J. Guan, G. Yu, X. Ding, W. Chen, Z. Shi, X. Huang and C. Sun, *ChemPhysChem*, 2013, **14**, 2841–2852.
- 31 X. Ding, G. Yu, X. Huang and W. Chen, *Phys. Chem. Chem. Phys.*, 2013, **15**, 18039–18047.
- 32 W. Chen, H. Zhang, X. Ding, G. Yu, D. Liu and X. Huang, *J. Mater. Chem. C*, 2014, **2**, 7836–7850.
- 33 D. Liu, G. Yu, Y. Sun, X. Huang, J. Guan, H. Zhang, H. Li and W. Chen, *Phys. Chem. Chem. Phys.*, 2015, **17**, 941–950.
- 34 H. Li, W. Chen, Y. Sun, X. Huang and G. Yu, *Phys. Chem. Chem. Phys.*, 2015, **17**, 24038–24047.
- 35 D. D. Wu, H. H. Fu, L. Gu, Y. Ni, F. X. Zu and K. L. Yao, *Phys. Chem. Chem. Phys.*, 2014, **16**, 17493–17498.
- 36 P. Lou, *Phys. Status Solidi B*, 2013, **250**, 1265–1277.
- 37 N. Alaal, V. Loganathan, N. Medhekar and A. Shukla, *Phys. Rev. Appl.*, 2017, **7**, 064009.
- 38 D. Y. Qiu, F. H. da Jornada and S. G. Louie, *Phys. Rev. Lett.*, 2013, **111**, 216805.
- 39 H. C. Hsueh, G. Y. Guo and S. G. Louie, *Phys. Rev. B: Condens. Matter*, 2011, **84**, 85404.
- 40 L. Yang, *Nano Lett.*, 2011, **11**, 3844–3847.
- 41 P. Cudazzo, C. Attaccalite, I. V. Tokatly and A. Rubio, *Phys. Rev. Lett.*, 2010, **104**, 226804.
- 42 J. Deslippe, M. Dipoppa, D. Prendergast, M. V. O. Moutinho, R. B. Capaz and S. G. Louie, *Nano Lett.*, 2009, **9**, 1330–1334.
- 43 L. Yang, J. Deslippe, C.-H. Park, M. L. Cohen and S. G. Louie, *Phys. Rev. Lett.*, 2009, **103**, 186802.
- 44 L. Yang, M. L. Cohen and S. G. Louie, *Phys. Rev. Lett.*, 2008, **101**, 186401.
- 45 L. Yang, M. L. Cohen and S. G. Louie, *Nano Lett.*, 2007, **7**, 3112–3115.
- 46 B. Arnaud, S. Lebègue, P. Rabiller and M. Alouani, *Phys. Rev. Lett.*, 2006, **96**, 026402.
- 47 V. Tran, R. Soklaski, Y. Liang and L. Yang, *Phys. Rev. B: Condens. Matter*, 2014, **89**, 235319–235324.
- 48 H. Shu, Y. Li, S. Wang and J. Wang, *J. Phys. Chem. C*, 2015, **119**, 15526–15531.
- 49 M. S. Hybertsen and S. G. Louie, *Phys. Rev. B: Condens. Matter*, 1986, **34**, 5390.
- 50 J. Deslippe, G. Samsonidze, D. A. Strubbe, M. Jain, M. L. Cohen and S. G. Louie, *Comput. Phys. Commun.*, 2012, **183**, 1269–1289.
- 51 M. Rohlfing and S. G. Louie, *Phys. Rev. B: Condens. Matter*, 2000, **62**, 4927.
- 52 P. Giannozzi, S. Baroni, N. Bonini, M. Calandra, R. Car, C. Cavazzoni, D. Ceresoli, G. L. Chiarotti, M. Cococcioni, I. Dabo, A. Dal Corso, S. Fabris, G. Fratesi, S. de Gironcoli, R. Gebauer, U. Gerstmann, C. Gougoussis, A. Kokalj, M. Lazzeri, L. Martin-Samos, N. Marzari, F. Mauri, R. Mazzarello, S. Paolini, A. Pasquarello, L. Paulatto, C. Sbraccia, S. Scandolo, G. Sclauzero, A. P. Seitsonen, A. Smogunov, P. Umari and R. M. Wentzcovitch, *J. Phys.: Condens. Matter*, 2009, **21**, 395502.
- 53 H. Ajiki and T. Ando, *Jpn. J. Appl. Phys.*, 1995, **34**(Suppl. 1), 107–109.
- 54 C.-H. Park, C. D. Spataru and S. G. Louie, *Phys. Rev. Lett.*, 2006, **96**, 126105.
- 55 L. Yang, *Phys. Rev. B: Condens. Matter*, 2010, **81**, 155445.

