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The nature of the multicenter bonding in π -[TCNE]₂²⁻ dimer: 4c/2e, 12c/2e, or 20c/2e?

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The dianion dimer of tetracyanoethylene (TCNE), π -[TCNE] $_2^{2-}$, represents an unusual class of organic compounds, that possess exceptionally long C-C bonding interactions (~2.96 Å). It is twice that of conventional C-C bonds but shorter than the sum of the van der Waals radii. Experimental and computational studies best characterize the intradimer bonding as a multi-center C-C bond. A number of theoretical studies indicate that the π -[TCNE]₂²⁻ dimer exhibits long, four-centers/two-electron (4c/ 2e) C-C bonds. However, there is still some disputation about the number of centers involved in the multicenter bonding. This work focuses on quantitative understanding of the nature of the long, multicenter bonding in the π -[TCNE] $_2^{2-}$ dimer. By the chemical bonding analysis, it is found that \sim 68% of electrons in the long bond locate on the -CC- groups and the remaining locate on the -CN groups. The substituent effect is investigated by comparing the interaction energy curves of the $[C_2X_4]_2^{2-}$ dimer (X = H, Cl and CN). The deep local well at 3.0 Å for X = CN indicates a strong bonding interaction. However, there is no obvious local well in the curves for X = H and Cl, which indicates that the $[C_2Cl_4]_2^2$ and $[C_2H_4]_2^2$ dimer are unstable. Herein, the -CN plays an important role in the bonding of the π -[TCNE]₂²⁻ dimer, and it is more reasonable to take the long bond as 20c/2e (12 carbon plus 8 nitrogen). Moreover, we found an abnormal charge redistribution from TCNE to TCNE-, and the charge distribution of $[TCNE]_2^{2-}$ is very similar to that of $TCNE^-$, which benefits the formation of the dianion dimer.

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Introduction

The dianion dimer of tetracyanoethylene (TCNE), π -[TCNE]₂²⁻ have attracted reasonable interest both experimentally and theoretically over the past few years because of their exceptionally long C-C bonding interaction. 1-5 It is well known that chemical bonding is one of the most fundamental concepts in chemistry,6 organic chemistry has been exceptionally well served by the two-electron, two-center (2e/2c) bonding description and the concept of resonance. However, the study of electron-deficient boranes expanded bonding concepts to more than two centers. The $\pi\text{-}\!\left[\text{TCNE}\right]_2^{\,2-}$ dimer as a representative example of possessing long (~2.96 Å) multi-center C-C bonds have been focus of several recent studies. The 2.96 Å intradimer separation for the eclipsed π -[TCNE]₂²⁻ dimer was too long for a conventional C-C bond (≤1.54 Å), and too short for a van der Waals interaction (i.e., <3.4 Å). These long, multicenter C-C bonds within a dimer of neutral or charged radicals have been proved by spectroscopic (UV/Vis/NIR, IR, ESR, NMR and FITR-Rama) studies, structural (crystallographic) evidence, and theoretical support. The addition to π -[TCNE] $_2^{2-}$ other species

exhibit sub-van der Waals separations suggestive of the presence of long, multi-center C–C bonding. Examples include anionic species, e.g., 7,7,8,8-tetracyano-p-quinodimethanide ([TCNQ] $^-$), $^{13-15}$ 1,2,4,5-tetracyanobenzene ([TCNB] $^-$); 18 cationic species, e.g., tetrathia-fulvalenium ([TTF] $^+$), 19 tetramethylphenylenediaminium ([TMPD] $^+$), 20 and octamethylbiphenylenium; 21 as well as neutral radicals, e.g., substituted phenalenyl. $^{22-25}$ However, nature of the long C–C bonding in these π -dimer is still under discussion.

There have been a number of theoretical studies about the nature of such a long, multicenter bond.3,26-30 From the pictures of molecular orbitals (MOs), Novoa and co-workers1,2 thought that π -[TCNE]₂²⁻ dimer possess a 4c/2e long bond with two C···C components. By MO and atoms-in-molecules (AIM) analysis, Graham and co-workers3 think that there are a 6c/2e long bond in a non-eclipsed π -[TCNE] $_2^{2-}$ dimer. For some other systems, there are also arguments on the number of centers involved in the long, multicenter bonds.29,31,32 This piqued our curiosity as to the nature of the long, multicenter bond. Hence, we carried out a chemical bonding analysis for the π -[TCNE]₂²⁻ dimer about the number of centers involved in the long bond. It is found that \sim 68% electrons in the long bond locate on the -CC- groups and the remains locate on the -CN groups. Herein, the -CN group plays an important role in the bonding of π -[TCNE]₂²⁻ dimer. It is more reasonable to take the long bond as 20c/2e (12 carbon plus 8 nitrogen) in π -[TCNE]₂²⁻ dimer.

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Computational methods

Geometries of TCNE, TCNE⁻ and π -[TCNE]₂²⁻ are relaxed by density functional theory (DFT) calculations using the M06L functional³³ with 6-311+G* basis set,³⁴ which was proved to be reliable for such long bond systems.^{28,35-37} Potential energy curves were evaluated at M06-2X38/aug-cc-PVTZ which were corrected for basis set superposition error (BSSE) throughout. All DFT calculations are carried out using the GAUSSIAN 09 package.39 To give an alternative and vivid view on the chemical bonding of the π -[TCNE]₂²⁻, we employ the adaptive natural density partitioning (AdNDP)40 method as a tool for analysis, using long-range corrected functional (LC-M06L) which has been proved to be reliable in the study of electron delocalization in conjugated bonds over long distances. 41,42 Molecular orbital (MO) visualization is performed using MOLEKEL 5.4.43 Noncovalent interaction (NCI) plots are plotted using Multiwfn^{44,45} and VMD46 packages.

Results and discussion

A. Geometries and electronic properties

The optimized structure of TCNE₂²⁻ was shown in Fig. 1 with D_{2h} symmetry. The distance of the center C-C is 1.43 Å, the distance of TCNE dimer is 2.96 Å in good agreement with the experimental data.47 Meanwhile, we calculate the charge distribution between atoms of TCNE, TCNE and [TCNE]22-, respectively. As labeled in Fig. 1, we define the central carbon atom as C1, and the -CN carbon atom as C2. In TCNE, NPA charges on C1, C2 and N are -0.14|e|, +0.28|e| and -0.21|e|, respectively. With an additional electron, in TCNE⁻, negative charges on C1 (-0.31|e|) and N (-0.40|e|) increase. However, charge on C2 (+0.30|e|) becomes more positive in TCNE, which is abnormal. Moreover, the charge distribution of [TCNE]₂²⁻ dimer and TCNE⁻ are almost consistent. This indicates that the electronic structure does not change much in the formation of the dianion dimer, which may benefit the formation of the $[TCNE]_2^{2-}$ dimer.

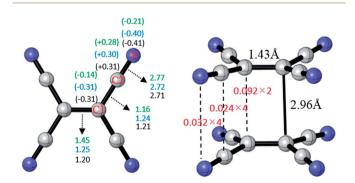


Fig. 1 Geometry of π -[TCNE]₂²⁻ dimer (right), of which the fuzzy bond orders between monomers are labeled in red. NPA charges of C1, C2, and N (in parentheses), fuzzy bond orders of C1–C1, C1–C2, and C2–N in neutral TCNE, TCNE⁻ anion, and the π -[TCNE]₂²⁻ dimer are shown in green, blue, and black, respectively (left).

Delocalization index (DI)48-51 is a quantitative measure of the number of electron pairs delocalized (or say shared) between two atomic spaces, which is also known as fuzzy bond order in fuzzy atomic space. In TCNE, the fuzzy bond order of C1=C1 is only 1.45 much less double bond order 2.0, the fuzzy bond order of C1-C2 is 1.16 slightly higher than single bond order 1.0, and the fuzzy bond order of C2≡N is 2.77 slightly less than triple bond order 3.0. This indicates certain delocalization of the π electrons, which weakens the double and triple bonds and strengthens the single bonds. With an additional electron, in TCNE⁻, the fuzzy bond orders of C1=C1 (1.45 to 1.25) and C2≡N (2.77 to 2.72) decrease, however, the fuzzy bond order of C1-C2 increases (1.16 to 1.24). This indicates that the extra electron enters the π^* -C1C1 and π^* -C2N anti-bonding orbitals, which weakens the C1=C1 and C2=N bonds. In π -[TCNE]₂²⁻ dimer, the fuzzy bond orders of C1=C1, C1-C2 and C2≡N (1.20, 1.21 and 2.71) decrease slightly compared to those in TCNE⁻, which may due to the delocalization of electrons between two monomers (bonding). Then, we calculated the fuzzy bond order between two monomers. The fuzzy bond orders between each pairs of C1, C2, and N in two monomers are 0.092, 0.024 and 0.032, respectively. There are two pairs of C1-C1, four pairs of C2-C2, and four pairs of N-N between two monomers, and so the total fuzzy bond order between the two monomers can be roughly calculated: $0.092 \times 2 + 0.024 \times 4 +$ $0.032 \times 4 = 0.41$. This indicates a fairly strong covalent interaction between two monomers in the π -[TCNE]₂²⁻ dimer.

B. Chemical bonding analysis

The fuzzy bond order gives indirect evidence of the covalent bond between two monomers in π -[TCNE] $_2^2$ dimer. To gain more direct insight into the nature of the bonding in π -[TCNE] $_2^2$, we apply adaptive natural density partitioning (AdNDP) method to obtain patterns of chemical bonding. The method was developed by Zubarev and Boldyrev, $_2^{52-54}$ which has been successfully applied in a number of systems. $_2^{55-60}$ AdNDP is based on the concept of the electron pair as the main element of chemical bonding models, which recovers both Lewis bonding elements (1c/2e and 2c/2e objects) and delocalized bonding elements (nc/2e). AdNDP is consistent with the recently developed Electron Density of Delocalized Bonds (EDDB) $_2^{61}$ method.

The geometric structure and the results of AdNDP analysis of neutral TCNE, TCNE $^-$ anion and π - $[TCNE]_2^{2-}$ dimer are shown in Fig. 2. For neutral TCNE, there are one lone pairs (LPs) in each N, twelve 2c/2e CN bonds (four C \equiv N triple bonds, including four σ and eight π bonds) and five 2c/2e CC σ bonds with nearly idealized occupy numbers (ONs = 1.97–2.00|e|). However, ON of the π -C1C1 bond is only 1.84|e|, indicating delocalization of the π bond (in consist with the low fuzzy bond order of C1 \equiv C1). If the π orbital is taken as delocalized 10c/2e bond, it has an idealized ON (2.00|e|), and the orbital shape is reasonable (delocalized over four π *-CN anti-bonding orbital). Thus it is more reasonable to take the π -C1C1 bond as a 10c/2e delocalized π bond (Fig. 2a).

AdNDP chemical bonding framework in TCNE⁻ is exactly same as that in TCNE. The extra electron occupies a 10c/1e

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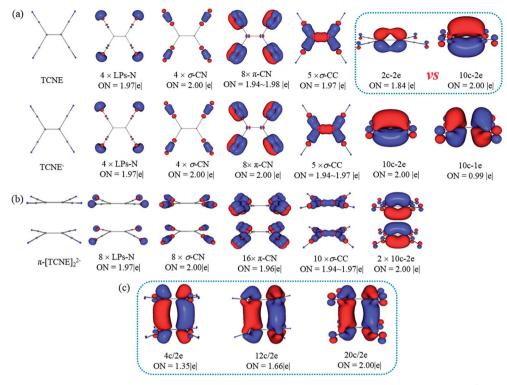


Fig. 2 Structures and AdNDP localized natural bonding orbitals of neutral TCNE, TCNE⁻ anion (a), and π -[TCNE]₂²⁻ dimer (b), where three patterns of the long distance bond are given (c). ON gives the occupancy number

delocalized bond, which is composed of π^* -C1C1 and π^* -C2N anti-bonding orbital from the symmetry (Fig. 2a).

As shown in Fig. 2b, for the π -[TCNE]₂²⁻ dimer, the chemical bonding framework of each monomer is also same as that of neutral TCNE. The extra two electrons occupy a 20c/2e bond (ON = 2.00|e|) delocalized over two monomers, which can be seen as a bonding orbital composed by the 10c/1e bonds as shown in TCNE⁻ from the symmetry. There are some disputes in literatures¹⁻³ about the number of centers involved in the π - $[TCNE]_2^{2-}$ dimer, so the situations of 4c/2e (4 × C1) and 12c/2e $(4 \times C1 + 8 \times C2)$ are also considered (Fig. 2c). Obvious, the 4c/ 2e (ON = 1.35|e|) and 12c/2e (1.66|e|) bonds can be seen as fragments of the 20c/2e bond from the orbital symmetry, and the ONs are obviously lower. Thus, it is more reasonable to take the long bond as 20c/2e (12 carbon plus 8 nitrogen) in the π -[TCNE]₂²⁻ dimer.

Previous studies think that the long distance bond is formed by two π^* -CC bonds, which is 4c/2e. However, it is more reasonable to take the long distance bond as a 20c/2e bond instead a 4c/2e one from AdNDP analysis. To give more clearly evidence from the composition of the bonding orbital, the AdNDP 20c/2e bonding orbital is enlarged in Fig. 3. As labeled, it is clearly seen that the orbital in each monomer is composed by one π^* -CC and four π^* -CN anti-bonding orbital. Moreover, contribution of each atom in the 20c/2e bond can also be roughly calculated from the ONs in AdNDP analysis. If only the four C1 atoms are involved in the long distance bond (4c/2e), ON is 1.35|e|, which indicates that the contribution of C1 atoms is 1.35|e|. When the eight C2 atoms are taken into accounts (12c/2e), the ON increases from 1.35|e| to 1.66|e|, which means that the contribution of eight C2 atoms is 0.31|e|(1.66|e| - 1.35|e|). Then ON reaches the standard 2.00|e|including the eight N atoms (20c/2e), and so the contribution of eight N atoms is 0.34|e| (2.00|e| - 1.66|e|). Thus, it can be educed that the partial electron numbers on C1, C2 and N are 1.35|e|, 0.31|e| and 0.34|e|, respectively. The ratio is 68% for π^* -CC and 32% for π^* -CN in the 20c/2e bond. Therefore, although the long distance bond is mainly formed by π^* -CC orbital, the π^* -CN anti-bonding orbitals also play an important role for the stability of the dimer, and the long distance bond should be 20c/2e.

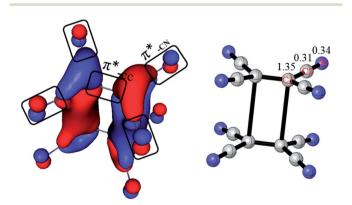


Fig. 3 Composition of the 20c-2e bonding orbital in π -[TCNE]₂²⁻ dimer (left, enlarged from Fig. 2c). Labeled are partial ONs on C1, C2 and N of the 20c-2e bond (right).

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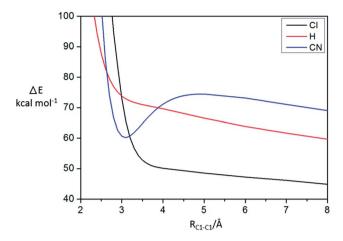


Fig. 4 BSSE-corrected M06-2X/aug-cc-pVTZ interaction potential curve for $[C_2H_4]_2^{2-}$ (red line), $[C_2Cl_4]_2^{2-}$ (black line), and π - $[TCNE]_2^{2-}$ (blue line). R_{C1-C1} gives the separation distance, Å.

C. Substituent effect

From the electronic properties and AdNDP analysis, it is shown that CN group plays an important role for the stability of the π -[TCNE]₂²⁻ dimer, and the long distance bond should be 20c/2e. To further verify the responsibility of CN in stabilizing π -[TCNE]₂²⁻, the substituent effect is investigated by comparing the interaction energy curves of $[C_2X_4]_2^{2-}$ dimer (X = H, Cl and CN). Fig. 4 plots the interaction energy (at the M06-2X/aug-cc-pVTZ level with BSSE corrections) of the dimer (X = H, Cl and CN) as a function of the separation distance ($R_{\text{C1-C1}}$). As expected, there is a deep local well at 3.0 Å for X = CN indicating strong bonding interaction. However, there is no obvious local well in the curves for X = H and Cl, which indicates that the $[C_2Cl_4]_2^{2-}$ and $[C_2H_4]_2^{2-}$ dimer are unstable. The substituent effect givers further evidence for the role of -CN group in the stability of π -[TCNE]₂²⁻ dimer.

D. NCI analysis

The long distance multicenter bond is not so strong, which has similar energy level with some secondary bonding, such as hydrogen bonding. As we know, π - π stacking can be rather strong in some cases. There are both long bonding and π - π stacking interactions in π -[TCNE]₂²⁻ dimer. However, there is only π - π stacking interaction in the triplet state.^{32,62} Herein, we use the non-covalent interaction (NCI) index approach to detect non-covalent interactions based on electron density and its derivatives, which has been successfully applied to investigate the weak interaction in a number of systems. 63-65 NCI index provides a rich representation of non-covalent interactions, such as, van der Waals interactions, hydrogen bonds, and steric repulsion. Besides the non-covalent interactions, NCI index can also provide representation for weak covalent interactions. Thus, we can use NCI analysis to compare the long distance multicenter bond and π - π stacking interactions. NCI involves the reduced density gradient (RDG) and the electron density (ρ). RDG is defined as:

$$s = \frac{1}{2(3\pi^2)^{1/3}} \frac{|\nabla \rho|}{\rho^{4/3}}$$

and the representation of *s versus* ρ shows characteristic peak sat low density values in the presence of non-covalent interactions. The sign of the second eigenvalue (λ_2) of the electron-density Hessian matrix is used to distinguish between bonded $(\lambda_2 < 0)$ and non-bonded $(\lambda_2 > 0)$ interactions. The visualization of the gradient isosurface can be seen in real space through VMD program. The gradient isosurfaces are colored according to the corresponding values of sign $(\lambda_2)\rho$, which is found to be a good indicator of interaction strength. A RGB (red-blue-green) scale is used.

Fig. 5a compares the scatter diagram of the singlet and triplet states (blue for singlet and red for triplet) of the π -[TCNE]₂²⁻ dimer. The singlet and triplet states have similar spikes at 0.02

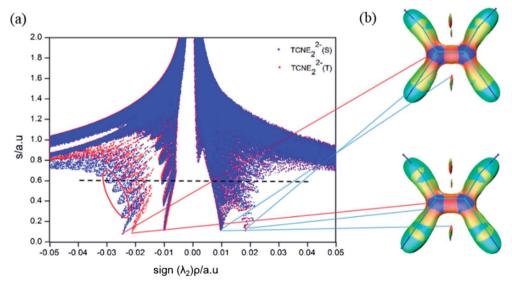


Fig. 5 (a) Plots of the reduced density gradient *versus* the electron density multiplied by the sign of the second Hessian eigenvalue, S-singlet; T-triplet, and (b) NCI isosurfaces (s = 0.60).

a.u. (coulomb repulsion), 0.01 a.u. (steric repulsion) and -0.01 a.u. (van der waals attraction). The spike at -0.02 a.u. in the triplet should be π - π stacking, and the spike at -0.025 a.u. in the singlet is bonding interaction. The isosurfaces (Fig. 5b) of the singlet and triplet states are also similar. NCI analysis directly shows the long distance bonding interaction, which is not so strong but is clearly stronger than π - π stacking.

Conclusion

In summary, the geometric structure and chemical bonding of the π -[TCNE]₂²⁻ dimer are investigated by using the DFT method, relying on M06L functional. The nature of the long multicenter bond in π -[TCNE]₂²⁻ dimer is studied by electronic properties, substituent effects and chemical bonding analysis with AdNDP method. The fuzzy bond order between the two monomers is 0.41, which indicates a fairly strong covalent bond between two monomers in the π -[TCNE]₂²⁻ dimer. As expected, AdNDP analysis locates all localized bonds in each TCNE monomer in the π -[TCNE]₂²⁻ dimer. The remaining two electrons tend to form 20c/2e delocalized bond between two monomers. It is clearly seen that the orbital in each monomer is composed by one π^* -CC and four π^* -CN anti-bonding orbital. Furthermore, the ratio is \sim 68% for π *-CC and \sim 32% for π *-CN in the 20c/2e bond from the partial electron numbers on C1, C2 and N. The substituent effect givers further evidence for the role of -CN group in the stability of π -[TCNE]₂²⁻ dimer. There is no obvious local well in the curves for X = H and Cl, however, there is a deep local well at 3.0 Å for X = CN. Hence, the π^* -CN orbitals also play an important role for the stability of the dimer, and the long distance bond should be 20c/2e.

Conflicts of interest

There are no conflicts to declare.

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