A new stable aqueous foam system was screened out by an orthogonal method and the effects of different factors on the rheological property of the foam were systematically investigated. The prepared aqueous foam has high stability. The foaming volume and half-life of 100 ml foam solution can reach 312 ml and 2274 min, respectively. The foam belongs to fine-celled foam, and the bubbles are wrapped by multilayered liquid films. The foam can maintain good stability even at high concentrations of salts and crude oil. For the foam rheology, with an increase in shear rate and salt concentration, the rheological model of the foam will change from power law model to Bingham model. Moreover, there exists optimum crude oil concentration and temperature to maximize the apparent viscosity of the foam. The apparent viscosity does not change significantly within several hours before and after foam drainage. In addition, a new wall slip correction method in foam rheology measurement is proposed.

Stability control is the key to research and application of foam properties. It is generally believed that the evolution of foam structure involves three mechanisms: foam drainage, film rupture and bubble coarsening. However, the high temperature and high pressure conditions in the formation of wellbore, as well as the crude oil itself and salts in oil, usually exacerbate foam decay. This requires that the prepared foam should have composite properties such as oil tolerance, salt resistance and temperature resistance in practical applications. It is often difficult for single surfactants to meet the above requirements. On changing the molecular structure of surfactants or surfactants compounding, some scholars have prepared different types of aqueous foams, which have composite properties of temperature and oil tolerance or temperature and salt resistance or acid and oil tolerance. These foams are mainly applied to oil or natural gas development underground.

As a potential and promising method, aqueous foam is likely to be used for reducing the pipeline drag in heavy oil transportation at normal temperature instead of water annulus technology. Specifically, aqueous foam is injected into the space between the heavy oil and pipe wall to form foam annulus, and the isolation and lubrication action of the foam annulus or foam drainage complex layer contributes to heavy oil flow drag reduction. First and foremost, a stable oil-tolerant and salt-resistant aqueous foam system needs to be recomposed. Lai synthesized a type of oil-tolerant and salt-resistant surfactant, which contains not only hydrophilic and lipophilic groups, but also hydrophobic and hydrophobic fluorinated side chains. However, this system has numerous synthetic steps, complex product structure and high difficulty in separation and
purification, which also make it difficult to apply this surfactant practically. There is still limited research on the study of this type of aqueous foam system and its rheological properties at present.

Herein, several oil-tolerant or salt-resistant surfactants were selected through previous studies, \(^{17,22-31}\) and we found that some of them have both oil and salt resistance, such as sodium lauryl polyoxyethylene ether sulfate (AES), sodium alpha-olefin sulfonate (AOS), xanthan gum (XG) and dodecanol (Dod). Based on the synergy of foaming agents and foam stabilizers, a new stable oil-tolerant and salt-resistant aqueous foam system was screened out and evaluated; moreover, the effect of different factors on the rheological properties of the foam was systematically investigated.

2. Experimental

2.1. Materials

The heavy crude oil sample, whose basic compositions and physical properties are listed in Table 1, was collected from Lvda (LD) oilfield in China. Two types of salts, NaCl with high purity (\(\geq 99.5\%\)) and CaCl\(_2\) with a purity of over 96.0\%, were bought from Chengdu Kelong Chemical Reagent Factory. Moreover, the water used in this study is tap water, which was from Chengdu water supply company. According to the company’s water analysis report, the pH value and salinity are 7.32 and 132 mg l\(^{-1}\), respectively.

The foaming volume and foam stability of aqueous foam were directly influenced by types and concentrations of foaming agents and foam stabilizers. There are four types of common foaming agents in industrial applications, i.e. the anionic, the cationic, the non-ionic and the amphoteric. Herein, based on the evaluation results of surfactants with oil or salt resistance in previous studies, four types of anionic surfactants, two types of non-ionic and amphoteric surfactants were selected as foaming agents, and two anionic and three non-ionic surfactants were selected as foam stabilizers, which are shown in Tables 2 and 3, respectively.

2.2. Apparatus

The XP-300C image analytical system (Shanghai, China) was used to capture and analyze foam micrographs. The Anton Paar Rheolab QC viscometer (Graz, Austria) and Haake Mars III (Haake, Germany) were adopted to test the rheological behaviors and viscoelasticity of foam solution and aqueous foam. The JJ2000B rotating drop interface tension measuring instrument (Shanghai, China) was used to measure the surface tension of surfactant solutions with different concentrations and the interface tension between oil and water or oil and foaming base solution. The GJ-1 homo-mixer with a maximum stirring rate of 13 000 rpm (Jiangyin, China) was used to prepare aqueous foam. The Shangping FA2104S electronic balance with an accuracy of 1/10 000 g (Shanghai, China) was used to weigh various samples. Some measuring cylinders (500 ml, 100 ml) and pipettes (100 ml) were used to evaluate the foam performance.

2.3. Experimental procedure

Based on the Waring Blender method, 100 ml water with the required proportion of surfactants was added to a stirring cup and mixed by a glass rod evenly to obtain the foaming fluid. Then, it was stirred by the GJ-1 homo-mixer for 1 min at room temperature (about 20 °C) under normal atmospheric pressure at a speed of 4500 rpm to prepare the aqueous foam. The foam volume \(V_o\) and the foam drainage half-life \(t_{1/2}\) reflect the different performance indicators of the foaming agents. To evaluate the comprehensive influences on the foamability of the foaming fluid, the foam composite index (FCI) is introduced, which can be calculated using the following formula:

\[
F\text{CI} = 0.75V_o t_{1/2}
\]

where \(V_o\) and \(t_{1/2}\) are expressed in milliliters (ml) and minutes (min) separately. The larger the FCI value, the stronger its comprehensive performance.

The liquid volume in foam \(V_l\) is the original volume of the foaming fluid. The foaming volume \(V_o\) is the sum of gas volume

| Table 1 Basic properties and compositions of LD crude oil |
|-----------------|-----------------|-----------------|-----------------|-----------------|
| Number          | Viscosity at 50 °C (mPa s) | Density at 20 °C (kg m\(^{-3}\)) | Asphaltene (wt%) | Wax (wt%) | Resin (wt%) |
| LD1             | 5.40             | 847.0           | 2.09             | 20.47      | 10.71       |
| LD2             | 134.90           | 918.40          | 1.12             | 8.45       | 16.40       |

<table>
<thead>
<tr>
<th>Table 2 Foaming agents used for foam preparation</th>
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<tr>
<td>Surfactant</td>
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<tr>
<td>Sodium benzenesulfonate</td>
</tr>
<tr>
<td>Sodium dodecyl sulfate</td>
</tr>
<tr>
<td>Sodium lauryl polyoxyethylene ether sulfate</td>
</tr>
<tr>
<td>Sodium alpha-olefin sulfonate</td>
</tr>
<tr>
<td>Coconut methyl monoethanolamide</td>
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<tr>
<td>Ocytphenol ethoxylate</td>
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<tr>
<td>Cocamidopropyl hydroxy sulfobetaine</td>
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<td>Disodium lauroamphodiacetate</td>
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</table>
$V_f$ and liquid volume $V_i$. Thus, the gas volume fraction in foam, namely foam quality $\Gamma$, can be calculated by eqn (2):

$$\Gamma = \frac{V_f}{V_f + V_i} \times 100\% = \frac{V_o - V_i}{V_o} \times 100\%$$  \hspace{1cm} (2)

3. Results and discussion

3.1. Composition of foaming solution

3.1.1. Evaluation of types of foaming agents. Eight different types of foaming agents were selected to determine the suitable formulations of foam by the Waring Blender method. The effect of different types of foaming agents on foaming capacity of 100 ml foaming solution is shown in Fig. 1. Overall, all the four types of anionic surfactants, i.e. sodium benzenesulfonate (ABS), sodium dodecyl sulfate (SDS), sodium lauryl polyoxyethylene ether sulfate (AES) and sodium alpha-olefin sulfonate (AOS), show great foaming capacity, the FCI values being maintained at around 3000 within the test concentration range. Relatively speaking, the foamability of ABS and AES is slightly better than that of SDS and AOS. The average foaming volumes and half-lives of ABS and AES exceed 450 ml and 8.8 min, respectively, at a concentration of 2 g l$^{-1}$ (optimum concentration), but for SDS and AOS, the concentration corresponding to optimum foaming performance appears around a slightly higher value of 3 g l$^{-1}$.

On the contrary, the foaming abilities of both the non-ionic surfactants octylphenol ethoxylate (OP-10) and coconut methyl monoethanolamide (CMMEA) are much lower than those of the above four anionic surfactants. All the FCI values for CMMEA are under 50 in the entire test surfactant concentration range. This may be due to the fact that its hydrophilic-lipophilic balance (HLB) value 7.6 is lower than the critical value (8) for surfactant foaming and defoaming. The smaller the HLB value, the stronger the defoaming performance. The foamability of OP-10 is poor when the surfactant concentration increases to 4 g l$^{-1}$, and the prepared foam rapidly decays in a short time. This may be attributed to its high critical micelle concentration (CMC).

3.1.2. Effect of foaming agent concentration. The four anionic surfactants cocamidopropyl hydroxy sulfobetaine (CHSB) and disodium lauroamphodiacetate (LAD-40) increase with increasing concentration, but they have better foaming ability only at higher concentrations, and the prices of the amphoteric surfactants are usually much higher than those of other surfactants. To have an integrative consideration of the foaming volume, half-life and dosage of foaming agents, the four types of anionic surfactants were used as the potential foaming agents in the following experiments.

3.1.3. Evaluation of type of foam stabilizers. The aqueous foam prepared with only foaming agents added generally has
very short half-life and cannot meet the actual engineering requirements. Different concentrations of five common foam stabilizers were added to 100 ml base solution and the foam stability was evaluated by the Waring Blender method. As shown in Fig. 3, all the foam stabilizers show different effects on the foam stability. Overall, when different types of foam stabilizers are added, the foam volumes decrease to varying degrees, but the half-lives are significantly improved instead. The most prominent step is the addition of xanthan gum (XG) and hydroxyethyl cellulose (HEC) that can greatly prolong the half-life of the foam; the average half-lives of the aqueous foam with these two foam stabilizers can increase to 1856.2 min and 106.8 min, respectively, at a concentration of 4 g l\(^{-1}\), which are far higher than the half-lives of the foam prepared with other three foam stabilizers. Therefore, XG and HEC are used as the foam stabilizers in the follow-up study.

### 3.1.4. Effect of foam stabilizer concentration.

The concentrations of XG and HEC required for stable aqueous foam were also investigated by the orthogonal method. It can be observed from Fig. 4 that all the foaming volumes of the prepared foam at different compound proportions of XG and HEC reduce to around 300 ml, but the half-lives and FCI values are improved significantly compared with the foam prepared without any foam stabilizer. Moreover, the XG is the leading factor that affects the foam performance. At same HEC concentration, the half-lives and FCI values increase almost linearly with the increasing XG concentration, and the increasing speed accelerates as the compound concentrations of XG and HEC continue to increase. Considering the effect of unit concentration of foam stabilizers on foam performance and the total usage in foam preparation comprehensively, the average FCI value can reach the maximum under unit concentration when 3 g l\(^{-1}\) XG and 4 g l\(^{-1}\) HEC were added to 100 ml foaming base solution. Moreover, the average foam volume and the half-life of this foam are up to 312 ml and 2274 min, respectively. Therefore, 3 g l\(^{-1}\) XG and 4 g l\(^{-1}\) HEC are

<p>| Table 4 Determination of the type of foaming agent by orthogonal test |
|------------------|------------------|------------------|------------------|------------------|------------------|</p>
<table>
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<tr>
<th>Test number</th>
<th>SDS (g l(^{-1}))</th>
<th>ABS (g l(^{-1}))</th>
<th>AES (g l(^{-1}))</th>
<th>AOS (g l(^{-1}))</th>
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</table>
considered as the most appropriate compound proportion for stable foam preparation.

3.2. Basic properties

Based on the synergistic effects of foaming agents and foam stabilizers, an orthogonal combination of 1 g l\(^{-1}\) AES + 3 g l\(^{-1}\) AOS + 3 g l\(^{-1}\) XG + 4 g l\(^{-1}\) HEC was screened out as the optimum compound proportion for preparing stable aqueous foam. The molecular structures of the four surfactants are shown in Fig. 5.

Their critical micelle concentrations (CMC) measured at 50 °C and 5000 rpm min\(^{-1}\) are 2, 3, 3 and 4 g l\(^{-1}\), and the corresponding surface tensions are 30.651, 28.954, 49.523 and 55.651 mN m\(^{-1}\), respectively. Its density is 0.3205 g cm\(^{3}\) at 25 °C and normal pressure. Both rheological curves of the foaming solution and aqueous foam were measured by the CC39 test system (38.88 mm i.d., 60 mm long and 1.56 mm gap) of the Rheolab QC rheometer under a shear rate ranging from 0 to 300 s\(^{-1}\), which shows the rheological behavior of a non-Newtonian fluid and can be well described by the power law model. The apparent viscosities of the foaming solution and foam at 300 s\(^{-1}\) are 101.33 and 291.23 mPa s, respectively. The foam quality is 0.679, which is in the Mitchell quality range (between 0.5236 and 0.9999) and shows a homogenous mixture with uniform bubble sizes.

3.3. Salt and oil sensitivity

The prepared foam has strong oil-tolerant and salt-resistant abilities. In this study, the comprehensive performance of the foam will gradually reduce with the increase in salt concentration, but the FCI values can still remain above 50 000 even if the concentration of sodium chloride (NaCl), sodium calcification (CaCl\(_2\)) and the mixed salt (NaCl + CaCl\(_2\)) increases to 100, 20 and 80 + 8 g l\(^{-1}\), respectively. This is because double bonds and hydroxyl groups exist in AES and AOS molecules, and they show a chelating effect on metal ions together with sulfonic acid groups; therefore, the foam system shows good salt resistance. Moreover, as the oil concentration increases, the foam FCI value first increases and then decreases gradually, i.e. the FCI value of the foam can reach a maximum with 30 g l\(^{-1}\) of LD1 crude oil and with 50 g l\(^{-1}\) of LD2 heavy oil, respectively. The corresponding half-lives of both of them can be maintained above 1200 min. This shows that the greater the viscosity of crude oil, the weaker its ability to enter the foam and spread, and the smaller the damage to the foam, which also proves the feasibility of applying the foam to the drag reduction of heavy oil transportation.

3.4. Microstructure

The microstructures of the aqueous foam were captured using the XP-300C image analytical system, and the micrographs under different magnifications are shown in Fig. 6. We can see that the foams are small and uniform and demonstrate dispersive spherical bubbles, which belong to fine-celled foam. Bubbles are formed by multilayered liquid films wrapping air cores. The shells of the bubbles are hard and different types of
Surfactants are evenly distributed in them. Owing to the existence of repulsion of surfactant molecules and Marangoni effect,33 each bubble is squeezed and repelled by other bubbles around them whether or not the bubbles contact each other. This is also the underlying cause for the stability of this foam system.

3.5. Bubble size distribution

Two-dimensional diameters and areas of the bubbles in pictures were collected using the MiVnt image analysis system (144 sets of data), and then the equivalent three-dimensional average diameter and number of bubbles could be calculated (Fig. 7).44 The bubble size is in accordance with the partial normal distribution and the bubble diameter is basically between 45 and 310 μm. The liquid film thickness is equivalent to the bubble size even more than the bubble diameter. This may also be another internal factor for the good stability of the foam prepared in this study. Most of the bubbles have a diameter of about 70 μm, while the probability of bubble emergence reaches the highest value of 0.275. The total probability of bubble emergence for bubble sizes ranging from 45 to 100 μm exceeds 0.60.

3.6. Rheological properties

3.6.1. Effect of shear rates. Aqueous foam is a thermodynamically unstable system, and it is significantly affected by shear rate. In this section, aqueous foam was prepared with the optimum proportion of 1 g l\(^{-1}\) AES + 3 g l\(^{-1}\) AOS + 3 g l\(^{-1}\) XG + 4 g l\(^{-1}\) HEC first, and then the rheological curves were measured under a shear rate ranging from 0–10 s\(^{-1}\) to 0–1500 s\(^{-1}\). New foam is required to be re-prepared in each set of tests. As shown in Fig. 8(a), all the shear stress vs. shear rate curves measured under 500 s\(^{-1}\) can be well described as the power law model, and all the correlation coefficients are larger than 0.99. In particularly, the rheological curves are almost completely coincident when the shear rate is below 50 s\(^{-1}\). With the increase in shear rate, the flow pattern index \(n\) has a gradually increasing trend, but the change laws of consistency coefficient \(k\) are not significant. The apparent viscosity decreases with the increasing shear rate, but the increasing speed then decreases gradually. This shows that the foam prepared in this study has a shear thinning property, but the extent of shear thinning gradually decreases.

However, when the shear rate increases to 600 s\(^{-1}\) (critical shear rate), the rheological properties of foam change essentially. The foam demonstrates Bingham fluid at a shear rate ranging from 0–600 s\(^{-1}\) to 0–1500 s\(^{-1}\) (Fig. 8(b)). This phenomenon is similar to what Wendorff and Ainley found,45 but the critical shear rate is higher than the value they measured. With the increase in shear rate, the structural viscosity \(\eta_s\) gradually decreases from 125.4 to 95.0 mPa s, but the ultimate shear stress \(\tau_u\) shows a slight increase from 55.202 to 67.352 Pa. In general, the rheological curves overlap approximately. This indicates that when the shear rate
increases to a certain extent, its effect on foam rheology will reduce, and moreover, the apparent viscosities are very close at a constant shear rate, and the standard deviation is only 0.0055. Based on the constitutive equation of Bingham fluid, the apparent viscosity of the foam is mainly affected by its structural viscosity at high shear rate.

3.6.2. Effect of temperature. Fig. 9 shows the effect of temperature on the apparent viscosity of the aqueous foam. The foam still belongs to power law fluid from 10 °C to 80 °C. With the increase in temperature, the apparent viscosity increases to a maximum at 30 °C first and then gradually decreases. This is probably because the increase in temperature results in the expansion of bubble volume and the increase in surface area at the low temperature stage, and then, the increase in surface tension causes the foam’s apparent viscosity to increase. After the apparent viscosity reaches the maximum value, the increase in temperature makes the increasing speed of kinetic energy of the liquid molecules greater than the increasing speed of the surface energy, thus the apparent viscosity will decrease as the temperature continues to increase.

3.6.3. Effect of salt concentration. The salts mainly include NaCl and CaCl₂. Hence, the individual and mixed effects of these two salts on the rheological property of the aqueous foam are illustrated in Fig. 10. The apparent viscosities of the foam are significantly affected by the presence of salts.

Fig. 9 Effect of temperature on the apparent viscosity of foam.

Fig. 10 Effect of salt concentration of rheological property of foam: (a) CaCl₂ concentration, (b) NaCl concentration, (c) Mixed salt concentration.
were studied. As can be seen from Fig. 10, when the concentration of CaCl$_2$ increases from 1 to 20 g l$^{-1}$, all the rheological curves can be described as the power law model and the apparent viscosities decrease slightly with the increase in CaCl$_2$ concentration at different shear rates (Fig. 10(a)), which indicates that low salt concentration has less influence on foam rheology. In addition, different concentrations of NaCl were also added to the foam base solution to prepare foam. We can see from Fig. 10(b) that the rheological model of the foam changes from the power law model to the Bingham model when the NaCl concentration exceeds 160 g l$^{-1}$. The apparent viscosity fluctuates greatly with the increasing concentration and reduces to the minimum at 200 g l$^{-1}$. This shows that the rheological properties of foam will begin to change when the salt concentration increases to a certain extent.

Moreover, the addition of mixed salts (salinity) causes a greater impact on the foam rheological property (Fig. 10(c)). The rheological model of foam begins to change to the Bingham model even at a compound concentration of 120 + 12 g l$^{-1}$ mixed salts. The apparent viscosity rapidly drops from above 140 mPa s to around 50 mPa s. This is because excessive salt content will compress the double adsorption layer of surfactant at the gas-liquid interface, which results in aggregation and precipitation of surfactants and a decrease in bubble surface tension and foam viscosity.

**3.6.4. Effect of oil concentration.** With the increase in crude oil concentration, the apparent viscosity of the foam increases until it reaches the maximum and then levels off (Fig. 11). The crude oil concentration corresponding to the maximum apparent viscosity is 30 g l$^{-1}$ for LD1 oil and 50 g l$^{-1}$ for LD2 oil, respectively, which is consistent with the crude oil concentration corresponding to the aforementioned maximum bubble FCI values. The reason for this may be that an appropriate amount of crude oil will be emulsified when stirred by the homo-mixer at high speed and the emulsified oil can increase the viscosity and stability of the foam. When the oil content reaches the saturation value, the apparent viscosity of foam remains basically stable. In addition, the apparent viscosity of the foam with low-viscosity crude oil (LD1) added is lower than that of the foam with high-viscosity oil (LD2) added. Generally, the higher the apparent viscosity, the greater the stability of the foam. Therefore, this shows that the stability of foam in the presence of heavy crude oil is higher than that in the presence of light crude oil.

**3.6.5. Effect of drainage time.** The rheological behaviors of the foam at 20 °C before and after drainage can also be described as the power law model. As time increases, the apparent viscosity of the foam shows some fluctuation at different shear rates (Fig. 12). However, what needs special mention here is that the apparent viscosities of the foam after draining for several hours can be restored to the initial values before drainage. The interval drainage time is 8 hours at 200 s$^{-1}$ and 300 s$^{-1}$, and 4 hours at 100 s$^{-1}$. The higher the shear rate, the longer the corresponding interval drainage time. On the whole, the apparent viscosity begins to reduce after 8 hours. This trend shows that the changes in the foam apparent viscosity are not very noticeable for several hours, and at the same time, the foam has a more stable structure.

**3.6.6. Viscoelasticity.** The viscoelasticity behaviors of the foam and foam solution were measured at 20 °C and 1 Hz using the Haake Mars III rheometer. As shown in Fig. 13, the steady length of the elastic modulus $G'$ and viscous modulus $G''$ curves with shear stress reflects the stability of the foam, i.e. the longer the steady length, the stronger the anti-shear ability. We can see that both $G'$ and $G''$ begin to decline when the shear stresses acting on the foam and foam solution reach 19.88 and 5.70 Pa, respectively, which means that the composite structures of the foam and foam solution begin to be destroyed by the external stress. This indicates that foam has higher stability and stronger anti-shear ability than the foam solution, which is also
one of the reasons for reducing the pipeline drag of heavy oil by injecting aqueous foam instead of using water annulus technology in this study.

### 3.6.7. Wall slip correction of rotational viscometer

When using the rotational viscometer to measure the rheological property of the aqueous foam, usually foam drainage easily reaches the wall of flow channel under shear stress and causes wall slip. Yoshimura et al. first proposed the wall slip correction method just considering the effect of shear stress, which requires only two measurements on geometries with different gaps but equal ratios of radii. However, from the experiments, we found that the greater the shear stress, the greater the differences in the results measured by CC27 and CC39 systems. Moreover, the wall slip caused by the CC27 system is more remarkable than that caused by the CC39 system at the same shear stress. This shows that the wall slip is a function of shear stress and geometries of the test system at the same time.

Considering the relationship between slip velocity and shear stress, cylinder radius and width of the annular gap simultaneously, we propose an improved wall slip correction method. The parameters of the rheometer are listed in Table 5.

Considering the wall slip phenomenon, the coaxial viscometer geometry to be considered and the velocity profile of the foam flowing in the annular gap are shown in Fig. 14. The inner cylinder is rotated at angular velocity \( \Omega \) relative to the cup.

In the rheological test system, the shear stress at the radius \( R \) of the cylinder is calculated using eqn (3) and the flow of foam in the annular gap using eqn (4).

\[
\tau = \frac{T}{2\pi HR^2} \tag{3}
\]

\[
\Omega = \int_{\omega_0}^{\omega_1} d\omega + \frac{\int_{\tau_i}^{\tau_o} \gamma(t) d\tau}{2\pi} \tag{4}
\]

where \( \omega_i \) and \( \omega_o \) are the rotational angular velocities at the inner and outer walls of the cylinder, \( \tau \) is the shear stress, \( \tau_i \) and \( \tau_o \) are the shear stresses at the inner and outer walls of the cylinder, \( T \) is the applied torque, \( \gamma(t) \) is the shear rate and \( R \) is the distance from the center of the cylinder axis.

The integral of eqn (4) from the inner wall to the outer wall of the cylinder can be obtained as follows:

\[
\Omega = \Omega_s + \Omega_f \tag{5}
\]

It can also be expressed as follows:

\[
\Omega_s = \left( \frac{v_i(\tau_i, R_i, \Delta)}{R_i} + \frac{v_o(\tau_o, R_o, \Delta)}{R_o} \right) + \int_{\tau_i}^{\tau_o} \frac{\gamma(t)}{2\pi} d\tau \tag{6}
\]

\[
\Omega_f = \int_{\tau_i}^{\tau_o} \frac{\gamma(t)}{2\pi} d\tau \tag{7}
\]

where \( \Omega \) is the rotational angular velocity of the inner cylinder, \( \Omega_s \) is the wall slip contribution to the angular velocity, while \( \Omega_f \) is the contribution from the aqueous foam deformation, \( R_i \) and \( R_o \) are the radii of the inner and outer cylinders, and \( v_i \) and \( v_o \) are slip velocities of the foam at the wall of the inner and outer cylinders.

Assume that the slip velocity is directly proportional to the shear stress and inversely proportional to the width of the annular gap and the radius of the rotor, i.e.

\[
v_i = \frac{\beta_i \tau_i}{R_i \Delta}, \quad v_o = \frac{\beta_o \tau_o}{R_o \Delta} \tag{8}
\]

where \( \beta_i \) and \( \beta_o \) are constants, and \( \Delta \) is the width of the annular gap.

This method involves two measurements taken on a Rheolab QC viscometer of difference radii but with the same ratio of cup and inner cylinder. Thus if the inner cylinders have radii of \( R_i \) and \( R_o \),

\[
\begin{align*}
\frac{v_i(\tau_i, R_i, \Delta)}{R_i} + \frac{v_o(\tau_o, R_o, \Delta)}{R_o} &= \frac{\beta_i \tau_i}{R_i \Delta} + \frac{\beta_o \tau_o}{R_o \Delta} \\
&= \frac{\beta_i \tau_i + \beta_o \tau_o}{R \Delta}
\end{align*}
\]

### Table 5 Geometric parameters of the rheometer testing system

<table>
<thead>
<tr>
<th>Rotor type</th>
<th>( R_i ) (mm)</th>
<th>( R_o ) (mm)</th>
<th>( H ) (mm)</th>
<th>( \Delta ) (mm)</th>
<th>( \kappa )</th>
</tr>
</thead>
<tbody>
<tr>
<td>CC27</td>
<td>13.38</td>
<td>14.46</td>
<td>40.03</td>
<td>1.06</td>
<td>1.08</td>
</tr>
<tr>
<td>CC39</td>
<td>19.44</td>
<td>21.00</td>
<td>60.00</td>
<td>1.56</td>
<td>1.08</td>
</tr>
</tbody>
</table>

*Where \( R_i \) is the outer diameter of the inner rotor, \( R_o \) is the inner diameter of outer rotor, \( H \) is the height of the inner rotor, \( \Delta \) is the difference between \( R_o \) and \( R_i \) and \( \kappa \) is the ratio of \( R_o \) to \( R_i \).
and $R_2$, the corresponding cups must have radii of $kr_1$ and $kr_2$ respectively, where $k$ is a constant. Therefore, the torques of the two test systems, $T_2$ and $T_1$, can satisfy the eqn (9),

$$\frac{T_1}{T_2} = \frac{H_1r_1^2}{H_2r_2^2}$$

(9)

where $H_1$ and $H_2$ are the cylinder heights of the CC27 and CC39 test systems.

The stress that is produced on each cylinder can be written as follows:

$$\Omega_1 = \frac{1}{R_1^2 \Delta_1} \left( \beta_1 \tau_1 + \frac{\beta_0 \tau_0}{k} \right) + \int_0^{\infty} \frac{\gamma(\tau)}{2\tau} \mathrm{d}\tau$$

(10)

$$\Omega_2 = \frac{1}{R_2^2 \Delta_2} \left( \beta_2 \tau_2 + \frac{\beta_0 \tau_0}{k} \right) + \int_0^{\infty} \frac{\gamma(\tau)}{2\tau} \mathrm{d}\tau$$

(11)

where $\Delta_1$ and $\Delta_2$ are the widths of the annular gap of the CC27 and CC39 test systems.

Combining eqn (8) through (11), the real rotational angular velocity inside the aqueous foam can be derived as:

$$\Omega_f = \frac{\Omega_2 R_2^2 \Delta_2 - \Omega_1 R_1^2 \Delta_1}{R_2^2 \Delta_2 - R_1^2 \Delta_1}$$

(12)

According to eqn (12), the rotational angular velocity of slip elimination can be obtained and then the real shear rate can be calculated.

The correction results of wall slip of the foam are shown in Fig. 15. We can find that corrected shear stresses are generally higher than the values tested by the CC27 and CC39 systems, which also verifies the effectiveness of this method. Furthermore, the rheological parameters of the foam before and after wall slip correction are also listed in Table 6. The consistency coefficients increase and the flow pattern indexes decrease, respectively, at the same temperature after correction, which shows much difference from the results tested using the coaxial rotational viscometer. Therefore, much importance should be

**Table 6** Rheological parameters of the foam before and after wall slip correction

<table>
<thead>
<tr>
<th>Temperature (°C)</th>
<th>Consistency coefficient ($\kappa$)</th>
<th>Flow pattern index ($n$)</th>
<th>Consistency coefficient ($\kappa$)</th>
<th>Flow pattern index ($n$)</th>
<th>Consistency coefficient ($\kappa$)</th>
<th>Flow pattern index ($n$)</th>
</tr>
</thead>
<tbody>
<tr>
<td>10</td>
<td>10.238</td>
<td>0.3288</td>
<td>17.289</td>
<td>0.2779</td>
<td>20.758</td>
<td>0.2758</td>
</tr>
<tr>
<td>20</td>
<td>15.485</td>
<td>0.2613</td>
<td>16.241</td>
<td>0.295</td>
<td>19.016</td>
<td>0.2775</td>
</tr>
<tr>
<td>30</td>
<td>11.485</td>
<td>0.3358</td>
<td>14.665</td>
<td>0.3224</td>
<td>18.312</td>
<td>0.2944</td>
</tr>
<tr>
<td>40</td>
<td>12.883</td>
<td>0.2806</td>
<td>15.546</td>
<td>0.2991</td>
<td>18.312</td>
<td>0.3011</td>
</tr>
</tbody>
</table>
attached to this characteristic of the foam in laboratory experiments and practical applications.

4. Conclusions

A stable aqueous foam system was prepared with 1 g l\(^{-1}\) sodium lauryl polyoxyethylene ether sulfate (AES) + 3 g l\(^{-1}\) sodium alpha-olefin sulfonate + 3 g l\(^{-1}\) xanthan gum (XG) + 4 g l\(^{-1}\) hydroxyethyl cellulose (HEC) at 20 °C by the Waring Blender and orthogonal method. The foaming volume and half-life of 100 ml foam solution can reach 312 ml and 2274 min, respectively. The foam quality is 0.679, which is in the Mitchell quality range of 0.5–0.8. The foaming volume and half-life of 100 ml foam solution can reach 312 ml and 2274 min, respectively. The apparent viscosity of the foam is 600 s\(^{-1}\), and changes to Bingham/C0 = 1.5 and changes to Bingham/C0 = 1.5.

The rheological property of the foam was also given much importance in this study. The foam demonstrates power law fluid at a shear rate of 500 s\(^{-1}\), and changes to Bingham fluid at a shear rate ranging from 0–600 s\(^{-1}\) to 0–1500 s\(^{-1}\). The apparent viscosity reaches the maximum at 30 °C. Moreover, the increase in salt concentration will essentially change the rheological model of the foam. There also exists optimum crude oil concentration to maximize the apparent viscosity of the foam. Moreover, one interesting phenomenon is that the apparent viscosity of the foam after draining for several hours can be almost equal to that of the foam before drainage. Finally, a new wall slip correction method was proposed.

Acknowledgements

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