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# First-principles investigation of a $\beta$ -MnO<sub>2</sub> and graphene composite as a promising cathode material for rechargeable Li-ion batteries

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In this investigation, we studied the effect of the synergistic mechanism on the stability and the electronic and Li diffusion performance of a  $\beta$ -MnO<sub>2</sub> and graphene composite. The C–O covalent bonds formed in the stable interface not only improved the hybrid structure stability (a stable C–O bond forms between the  $\beta$ -MnO<sub>2</sub> (110) plane and graphene) but also led to enhanced conductivity. The calculated results implied that a possible diffusion pathway with the lowest energy barrier was found along the hybrid structure interface.

## 1 Introduction

Manganese dioxide (MnO<sub>2</sub>) was the most promising material for low cost and environment-friendly battery systems for over a decade.<sup>1–3</sup> Recently, it has received more attention in the field of supercapacitors.<sup>4–11</sup> Several MnO<sub>2</sub> polymorphs have been studied for use in Li-ion batteries, such as  $\alpha$ -MnO<sub>2</sub>,  $\beta$ -MnO<sub>2</sub> and  $\gamma$ -MnO<sub>2</sub> (a mixture of  $\alpha$  and  $\beta$ ).<sup>12</sup> Among them, due to the rutile structure of  $\beta$ -MnO<sub>2</sub>, which contains common phases of oxides (such as TiO<sub>2</sub>), much attention has been paid to  $\beta$ -MnO<sub>2</sub>. Mesoporous  $\beta$ -MnO<sub>2</sub> exhibited high Li uptake.<sup>13</sup> Furthermore,  $\beta$ -MnO<sub>2</sub>, which could be easily fabricated by the pyrolysis of MnOOH and a hydrothermal reaction, was thermodynamically stable.<sup>14,15</sup> According to the literature, researchers have not paid more attention to crystallized  $\beta$ -MnO<sub>2</sub> due to its poor ion insertion performance.<sup>16,17</sup> To our excitement, the nanocomposite and mesoporous  $\beta$ -MnO<sub>2</sub> could further enhance the capacity of the Li ions, and the capacity could achieve values of 320 mA h g<sup>-1</sup>.<sup>18–20</sup> This implied that the compact tunnel structure of  $\beta$ -MnO<sub>2</sub> was conducive to accommodating the volume changes as well as charging and discharging.

Graphene has attracted more attention as electrically conductive reinforced composites, sensors, and electrodes due to its superior chemical and physical properties.<sup>21</sup> In particular, graphene has been treated as a potential electrode to recharge lithium ions due to its superior conductivity (electron mobility of  $2 \times 10^6$  cm<sup>2</sup> V<sup>-1</sup> s<sup>-1</sup>) and large surface area (2630 m<sup>2</sup> g<sup>-1</sup>).<sup>22–25</sup> Cao *et al.* found that the sandwich-type functionalized graphene sheet-sulfur nanocomposite tested as a cathode in lithium-sulfur batteries exhibited a high reversible capacity of about 960 mA h g<sup>-1</sup>.<sup>26</sup>

To our knowledge,  $\beta$ -MnO<sub>2</sub>/graphene composite as a promising cathode electrode and graphene as an anode electrode were expected to obtain high voltages, high energies, and high power densities in neutral aqueous electrolytes.<sup>27–30</sup> Wu *et al.* found that a MnO<sub>2</sub> nanowire/graphene and graphene asymmetric electrochemical capacitor could be cycled reversibly in a high-voltage region of 0–2.0 V and showed an excellent energy density of 30.4 W h kg<sup>-1</sup> and a high power density of 5000 W kg<sup>-1</sup> at 7.0 W h kg<sup>-1</sup>.<sup>30</sup>

But above all, not only graphene but also MnO<sub>2</sub> could have an important role as electrode materials to obtain a synergetic effect, leading to excellent cyclic properties and eventually higher reversible capacities.<sup>31,32</sup> However, previous work focused on experimental studies with MnO<sub>2</sub> and graphene as the cathode electrode of a lithium battery. The synergistic mechanism of MnO<sub>2</sub> and graphene and the intercalation or deintercalation of Li are still not well understood, and they are seldom systematically reported in theoretical studies. Additionally, the charge–discharge process is complex, and it is still rather difficult to directly characterize Li diffusion at the atomic level.<sup>33</sup> Therefore, the first-principles method was selected in this work in order to analyze the properties and mechanism of Li adsorption on MnO<sub>2</sub> and a graphene hybrid structure (a stable C–O bond forms between the  $\beta$ -MnO<sub>2</sub> (110) plane and graphene). We investigate the structural stability and the electronic and Li diffusion properties of the MnO<sub>2</sub> and graphene hybrid structure.

## 2 Method and model

The DFT calculations were performed with CASTEP code,<sup>34</sup> using the generalized gradient approximation (GGA) in the form of the Perdew–Burke–Ernzerh (PBE) of the exchange–correlation functional. A plane wave cutoff energy of 480 eV and a *k*-point mesh of  $2 \times 2 \times 1$  in the Monkhorst Pack sampling scheme were used in all calculations. The tolerance of the self-

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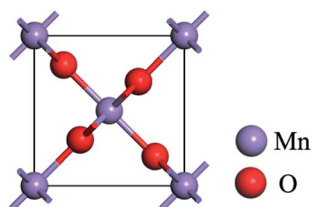


Fig. 1 Unit cell of the  $\beta$ - $\text{MnO}_2$  model used in the calculations.

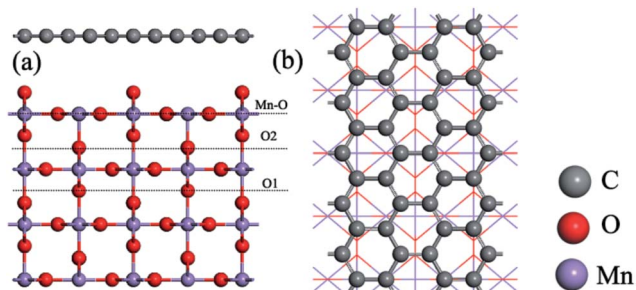


Fig. 2 (a) Three kinds of  $\beta$ - $\text{MnO}_2$  (110) surfaces: O1 surface, O2 surface, and Mn–O surface. (b) Top view of the G@O1 hybrid structure.

consistent field (SCF), and the energy, maximum force, maximum displacement and maximum stress were set as  $2.0 \times 10^{-5}$  eV per atom,  $2.0 \times 10^{-5}$  eV per atom,  $0.05 \text{ eV \AA}^{-1}$ ,  $2.0 \times 10^{-3}$  Å and 0.02 GPa, respectively. The structural relaxation was carried out with the Broyden–Fletcher–Goldfarb–Shannon (BFGS) algorithm.

Fig. 1 shows the rutile unit cell of  $\beta$ - $\text{MnO}_2$ . According to the experimental results of the  $\beta$ - $\text{MnO}_2$  nanoparticle and graphene nanosheet, the diameters of the  $\beta$ - $\text{MnO}_2$  nanoparticle and graphene nanosheet were set as 3–5 nm and a few layers with about 10–1000  $\mu\text{m}$  size, respectively.<sup>35,36</sup> Then the interface structure of the graphene and  $\beta$ - $\text{MnO}_2$  surface was built. The main effect on Li intercalation and deintercalation was believed to be contributed from the interaction at the interface. The (110) surface was the most stable surface of  $\beta$ - $\text{MnO}_2$ .<sup>37</sup> The  $\beta$ - $\text{MnO}_2$  (110) surfaces existed in three types: two O-terminated surfaces

(the O1 surface and O2 surface) and one Mn- and O-terminated surface (Mn–O surface) (Fig. 2a). Therefore, in this investigation, three kinds of  $\text{MnO}_2$ /graphene hybrid structure were well studied. We denoted these structures as G@O1, G@O2, and G@Mn–O. Based on the calculated results, G@O1 exhibited the most stable structure (Fig. 2b). We modeled the  $\text{MnO}_2$  (110) surface square lattice with a  $3 \times 2$  supercell ( $8.61 \text{ \AA} \times 12.44 \text{ \AA}$ ) and the graphene square lattice with a  $3 \times 3$  supercell ( $8.52 \text{ \AA} \times 12.33 \text{ \AA}$ ). The lattice mismatch was less than 1%. In order to obtain accurate results, the thicknesses of the vacuum (15 Å) and ten  $\text{MnO}_2$  (110) layers were enough for all calculations.

### 3 Results

First of all, the stability of the three interface structures (G@O1, G@O2, and G@Mn–O) is investigated. For the G@O2 and G@Mn–O structures, the distance between the  $\text{MnO}_2$  surface and graphene is 3.85 and 3.09 Å, respectively. It is worth noting that the graphene in the two structures is still flat, and  $\text{MnO}_2$  changes only a little compared to the original  $\text{MnO}_2$  (110) surface. However for the G@O1 interface structure, two carbon atoms bond to the surface oxygen atoms, as shown in Fig. 3a. The graphene and  $\text{MnO}_2$  surface is distorted. The nearest C–O distance is 1.48 Å (see Fig. 3b), which is close to the experimental value of the C–O bonding length (1.43 Å).<sup>38</sup> It can be concluded that the bonding between carbon and oxygen is covalent bonding. This is also verified by the charge transfer between the carbon and oxygen atoms (see Fig. 3c).

Subsequently, the density of states (DOS) is often used to measure the electronic conductivity of the structure.<sup>38,39</sup> Fig. 4a and b show that, besides a little gap difference, the total DOS is similar. The total DOS of the  $\text{MnO}_2$  surface and bulk  $\text{MnO}_2$  is plotted in Fig. 4a. The calculated band gap of bulk  $\text{MnO}_2$  is 0.23 eV, narrower than that of the experimental value (0.8 eV),<sup>40,41</sup> because DFT always underestimates the band gap. The higher band gap of the  $\text{MnO}_2$  (110) surface (0.73 eV) is due to the DOS peak being located near the Fermi level of the surface O atoms. It is noteworthy that the  $\text{MnO}_2$  surface and bulk  $\text{MnO}_2$  exhibit lower band gaps, which are helpful for the electron transport due to the exhibited semiconductor behavior. The

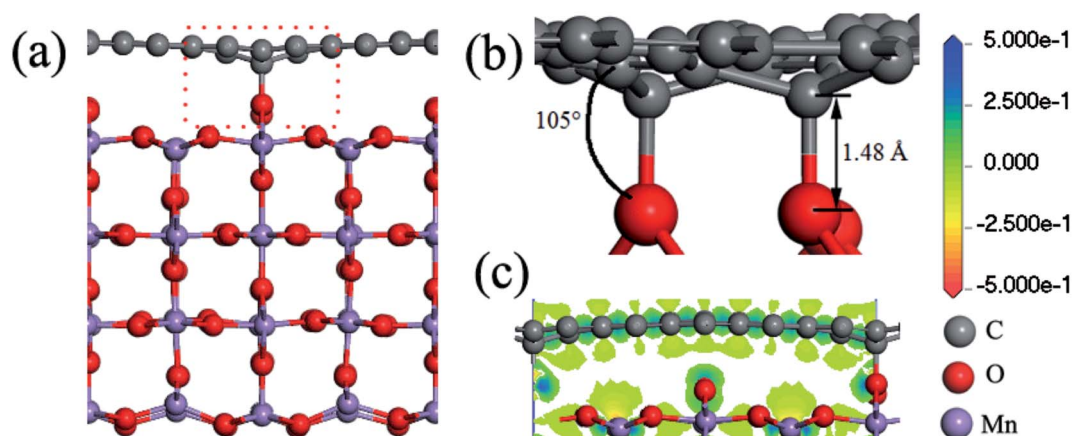


Fig. 3 (a) Side view of the G@O1 hybrid structure; (b) detailed view of the interface; (c) charge transfer of the bonded C and O atoms.



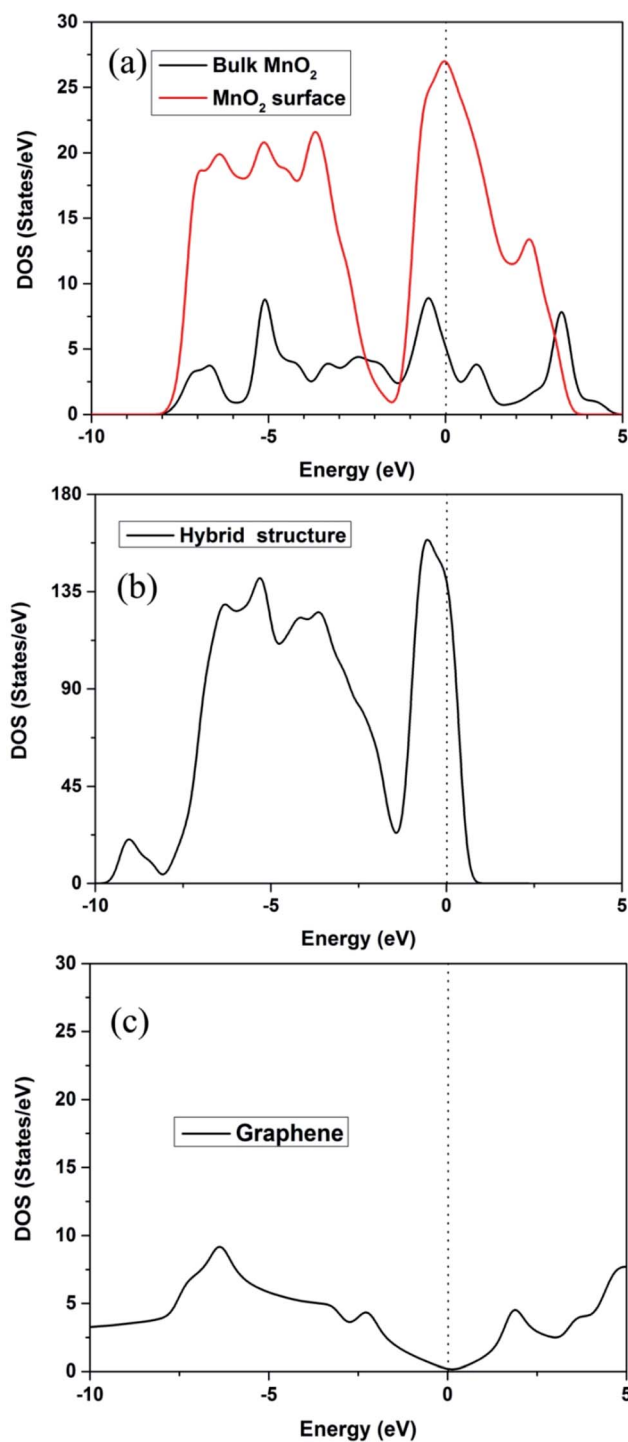


Fig. 4 (a) DOS of  $\beta$ -MnO<sub>2</sub> (110) surface and bulk; (b) DOS of the hybrid structure; (c) DOS of graphene.

total DOS of the hybrid structure in Fig. 4b, with zero band gap around the Fermi level, shows a conductor behavior. Fig. 4c is the DOS of graphene. The band gap of graphene is 0 eV.

Next, the Li adsorption on the hybrid structure is well investigated. The stability of Li adsorption can be examined by the binding energy, given as  $E_{\text{ad}} = E_{\text{h}} + E_{\text{Li}} - E_{\text{t}}$ .  $E_{\text{t}}$ ,  $E_{\text{h}}$ , and  $E_{\text{Li}}$  are the total energies of the hybrid structure after Li adsorption,

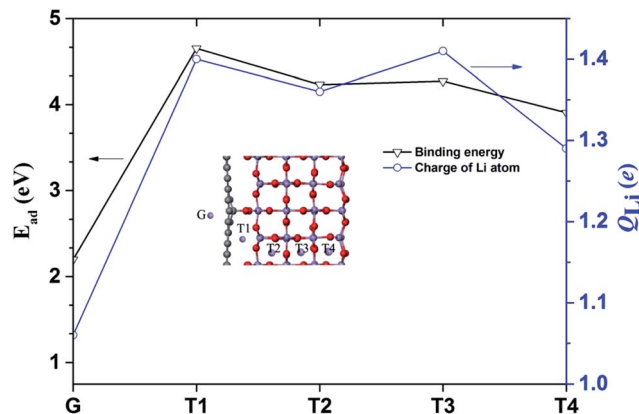


Fig. 5 Binding energy and charge of the Li atom at each site. The inset shows the adsorption sites of the Li atoms in a hybrid structure.

the hybrid structure and the isolated Li atom, respectively. The different adsorption position of the Li atom in the hybrid structure is plotted in the inset image of Fig. 5, and the binding energy  $E_{\text{ad}}$  and charge of the Li atom  $Q_{\text{Li}}$  are presented in Fig. 5.

The binding energies at the G, T1, T2, T3 and T4 sites in the hybrid structure are about 2.98, 4.65, 4.23, 4.27 and 3.91 eV, respectively. The larger binding energy at the T4 site (3.91 eV) could be attributed to surface adsorption.<sup>42</sup> Moreover, the binding energies at the T1, T2, and T3 sites at 4.65, 4.23 and 4.27 eV are due to the synergetic interaction of the MnO<sub>2</sub> surface and graphene. Specifically, based on the calculated binding energies at each site, the cathode of the hybrid structure is charged, and the Li atoms probably tend to occupy the interface sites. Mulliken population analysis is always used to analyze the average net charge.<sup>43,44</sup> The charge of the Li atom ( $Q_{\text{Li}}$ ) was calculated and is plotted in Fig. 5. The value of  $Q_{\text{Li}}$  has a maximum and minimum electron transfer of the Li atom at the T3 site (1.41 e) and the G site (1.06 e).

Next, the Li diffusion barriers are calculated in order to thoroughly probe the deintercalation properties of Li with high binding energy near the interface. At the beginning, the Li atom diffusion in bulk MnO<sub>2</sub> is investigated, as shown in Fig. 6a. According to the symmetry of bulk MnO<sub>2</sub>, path x is equivalent to path y. For bulk MnO<sub>2</sub>, the energy barriers of path x and path z (Fig. 6b and c) are 75.8 and 3.07 eV, respectively. This implies that path z is the main Li diffusion pathway. Fig. 6d shows the Li diffusion near the interface of the hybrid structure. There are three possible pathways (path x', path y' and path z'). Fig. 6e and f give the energy barriers of path x' and path y'. The energy barriers for these two pathways are 0.48 and 7.3 eV, respectively. The Li diffusion from path x' exhibits the lowest energy barrier. It is worth noting that the energy barrier of path x' is evidently reduced. Thereafter, the rapid Li diffusion along path x' in the hybrid structure is feasible.

## 4 Discussion

The Li diffusion behavior in the graphene and  $\beta$ -MnO<sub>2</sub> composite is well investigated using first-principles



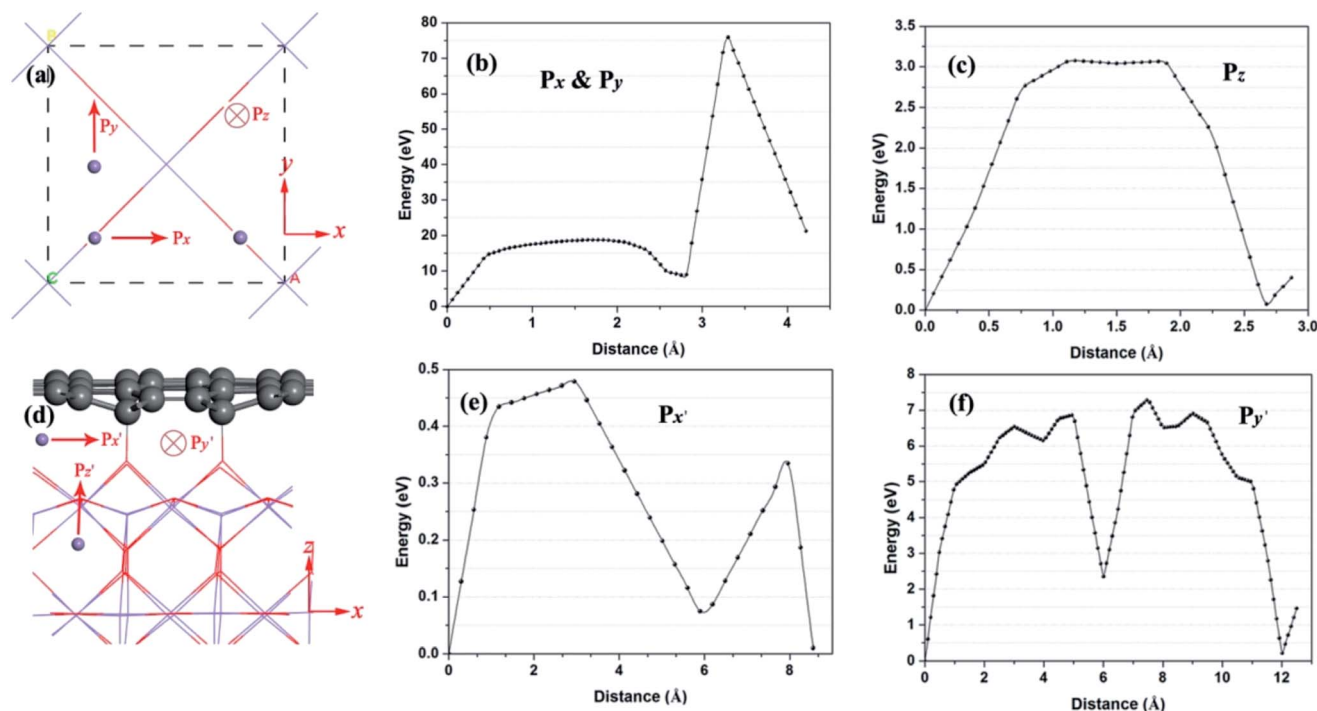


Fig. 6 (a) Li diffusion paths in bulk  $\beta$ -MnO<sub>2</sub>; (b) and (c) the energy barrier of lithium diffusion in bulk  $\beta$ -MnO<sub>2</sub>; (d) diffusion paths at the interface of the hybrid structure; (e) and (f) energy barrier of lithium diffusion in the hybrid structure.

calculations. As we know, the structure of the electrode materials has a significant effect on the Li diffusion behavior. Indeed, Yang *et al.* reported that the Mg diffusion pathway on the zigzag MoS<sub>2</sub> nanoribbon was identified as passing two adjacent T sites mediated by the nearest neighboring H site in between.<sup>45</sup> Therefore, we carefully investigated the interface structure of the graphene and  $\beta$ -MnO<sub>2</sub> composite in order to probe the synergistic mechanism of the intercalation or deintercalation of the Li atom.

To obtain high power in rechargeable Li ion batteries, it was reported that Li diffusion in or out of the electrode materials was fast enough to supply the electric current in a short time.<sup>46</sup> Although there existed many possible diffusion paths in the graphene and  $\beta$ -MnO<sub>2</sub> interface structure, it was primarily a one-dimensional channel along the interface, as was the case with Li diffusion in the graphene and SnO<sub>2</sub> composite.<sup>38</sup> With the combination of Fig. 3a and 6d, only one channel along the interface is observed, and the energy barrier is about 0.48 eV. This implies that the Li atom could easily diffuse through this diffusion path.

As reported in some experimental investigations, Cao *et al.* fabricated a sandwich-type functionalized graphene sheet-sulfur nanocomposite, and they pointed out that the interface of the nanocomposite had a significant effect on its cycling stability and capacity retention.<sup>26</sup> Wang *et al.* reported that the layer by layer assembly of sandwiched graphene/SnO<sub>2</sub> nanorod/carbon nanostructures exhibited ultrahigh lithium ion storage properties, which were attributed to a fast Li diffusion rate in the interfaces.<sup>47</sup> Especially, Zhang *et al.* compounded nitrogen-doped MnO/graphene nanosheets hybrid materials, and they

pointed out that the hybrid structure exhibited a reversible electrochemical Li storage capacity as high as 772 mA h g<sup>-1</sup> at 100 mA g<sup>-1</sup> after 90 cycles.<sup>48</sup> However, the diffusion path in bulk  $\beta$ -MnO<sub>2</sub> exhibits higher energy barriers for the Li atom, as shown in Fig. 6b and c.

Of course, a detailed diffusion process should take into account numerous variables such as the temperature, pressure and shape of the materials. Given that studying the effect of these factors on the diffusion process was beyond the scope of this investigation, here we just simply aimed to find the lowest possible energy barrier path in the hybrid structure. Indeed, the simulation method was a meaningful tool for providing insight into the Li diffusion in the hybrid structure. The calculated results implied that the pathway along the hybrid structure interface exhibited the lowest energy barrier for Li diffusion, which was consistent with the experimental results.<sup>22,42,43</sup> We expected that the simulation results could give positive guidance for experimental investigation.

## 5 Conclusions

In summary, the structural stability and the electronic and Li diffusion properties of the  $\beta$ -MnO<sub>2</sub> and graphene hybrid structure have been investigated in detail. The main findings were summarized as follows: (1) the structural stability and electronic conductivity of the hybrid structure (a stable C–O bond forms between the  $\beta$ -MnO<sub>2</sub> (110) plane and graphene) were better than that of  $\beta$ -MnO<sub>2</sub>. (2) The sites nearby the interface were more fit for Li insertion than other sites in the hybrid structure. (3) The diffusion pathway along the interface of the



hybrid structure was treated as a fast pathway for the Li atom. We proposed that the calculated results could give positive guidance for understanding the synergistic mechanism of  $\beta$ -MnO<sub>2</sub> and graphene as the cathode of a Li ion battery with high cycle stability and charge/discharge rate.

## Author contributions

The manuscript was written with contributions from all authors. All authors have given approval to the final version of the manuscript.

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## References

- 1 M. Manickam, P. Singh, T. B. Issa, S. Thurgate and R. De Marco, *J. Power Sources*, 2004, **130**, 254–259.
- 2 A. Biswal, B. Chandra Tripathy, K. Sanjay, T. Subbaiah and M. Minakshi, *RSC Adv.*, 2015, **5**, 58255–58283.
- 3 M. Minakshi Sundaram, A. Biswal, D. Mitchell, R. Jones and C. Fernandez, *Phys. Chem. Chem. Phys.*, 2016, **18**, 4711–4720.
- 4 M. V. Reddy, G. V. Subba Rao and B. V. R. Chowdari, *Chem. Rev.*, 2013, **113**, 5364–5457.
- 5 M. S. Whittingham, *Chem. Rev.*, 2004, **104**, 4271–4302.
- 6 A. L. M. Reddy, M. M. Shaijumon, S. R. Gowda and P. M. Ajayan, *Nano Lett.*, 2009, **9**, 1002–1006.
- 7 M. M. Thackeray, S.-H. Kang, C. S. Johnson, J. T. Vaughey, R. Benedek and S. A. Hackney, *J. Mater. Chem.*, 2007, **17**, 3112–3125.
- 8 K. Kang, Y. S. Meng, J. Bréger, C. P. Grey and G. Ceder, *Science*, 2006, **311**, 977–980.
- 9 Q. Qu, P. Zhang, B. Wang, Y. Chen, S. Tian, Y. Wu and R. Holze, *J. Phys. Chem. C*, 2009, **113**, 14020–14027.
- 10 C. Xu, B. Li, H. Du, F. Kang and Y. Zeng, *J. Power Sources*, 2008, **184**, 691–694.
- 11 T. Brousse, M. Toupin, R. Dugas, L. Athouël, O. Crosnier and D. Bélanger, *J. Electrochem. Soc.*, 2006, **153**, A2171–A2180.
- 12 M. M. Thackeray, *Prog. Solid State Chem.*, 1997, **25**, 1–71.
- 13 F. Jiao and P. G. Bruce, *Adv. Mater.*, 2007, **19**, 657–660.
- 14 B. Folch, J. Larionova, Y. Guari, C. Guérin and C. Reibel, *J. Solid State Chem.*, 2005, **178**, 2368–2375.
- 15 F. Cheng, J. Zhao, W. Song, C. Li, H. Ma, J. Chen and P. Shen, *Inorg. Chem.*, 2006, **45**, 2038–2044.
- 16 D. W. Murphy, F. J. Di Salvo, J. N. Carides and J. V. Waszczak, *Mater. Res. Bull.*, 1978, **13**, 1395–1402.
- 17 B. Zachau-Christiansen, K. West, T. Jacobsen and S. Skaarup, *Solid State Ionics*, 1994, **70**, 401–406.
- 18 W. Tang, X. Yang, Z. Liu and K. Ooi, *J. Mater. Chem.*, 2003, **13**, 2989–2995.
- 19 W.-M. Chen, L. Qie, Q.-G. Shao, L.-X. Yuan, W.-X. Zhang and Y.-H. Huang, *ACS Appl. Mater. Interfaces*, 2012, **4**, 3047–3053.
- 20 X. Wang and Y. Li, *J. Am. Chem. Soc.*, 2002, **124**, 2880–2881.
- 21 M. J. Allen, V. C. Tung and R. B. Kaner, *Chem. Rev.*, 2010, **110**, 132–145.
- 22 D. Wang, D. Choi, J. Li, Z. Yang, Z. Nie, R. Kou, D. Hu, C. Wang, L. V. Saraf, J. Zhang, I. A. Aksay and J. Liu, *ACS Nano*, 2009, **3**, 907–914.
- 23 D. Wang, R. Kou, D. Choi, Z. Yang, Z. Nie, J. Li, L. V. Saraf, D. Hu, J. Zhang, G. L. Graff, J. Liu, M. A. Pope and I. A. Aksay, *ACS Nano*, 2010, **4**, 1587–1595.
- 24 K. I. Bolotin, K. J. Sikes, Z. Jiang, M. Klima, G. Fudenberg, J. Hone, P. Kim and H. L. Stormer, *Solid State Commun.*, 2008, **146**, 351–355.
- 25 M. D. Stoller, S. Park, Y. Zhu, J. An and R. S. Ruoff, *Nano Lett.*, 2008, **8**, 3498–3502.
- 26 Y. Cao, X. Li, I. A. Aksay, J. Lemmon, Z. Nie, Z. Yang and J. Liu, *Phys. Chem. Chem. Phys.*, 2011, **13**, 7660–7665.
- 27 S. Zhu, H. Zhang, P. Chen, L.-H. Nie, C.-H. Li and S.-K. Li, *J. Mater. Chem. A*, 2015, **3**, 1540–1548.
- 28 J. Zhang, J. Jiang and X. S. Zhao, *J. Phys. Chem. C*, 2011, **115**, 6448–6454.
- 29 H. Wang, Q. Zhao, X. Wang, Y. Zhang, J. Gao, Y. Fu, X. Yang and H. Shu, *RSC Adv.*, 2014, **4**, 42910–42916.
- 30 Z.-S. Wu, W. Ren, D.-W. Wang, F. Li, B. Liu and H.-M. Cheng, *ACS Nano*, 2010, **4**, 5835–5842.
- 31 G. Yu, L. Hu, N. Liu, H. Wang, M. Vosgueritchian, Y. Yang, Y. Cui and Z. Bao, *Nano Lett.*, 2011, **11**, 4438–4442.
- 32 J. Kwon, S. H. Lee, K.-H. Park, D.-H. Seo, J. Lee, B.-S. Kong, K. Kang and S. Jeon, *Small*, 2011, **7**, 864–868.
- 33 J. Meurig Thomas and P. A. Midgley, *Chem. Commun.*, 2004, 1253–1267.
- 34 M. D. Segall, J. D. L. Philip, M. J. Probert, C. J. Pickard, P. J. Hasnip, S. J. Clark and M. C. Payne, *J. Phys.: Condens. Matter*, 2002, **14**, 2717.
- 35 S. Jana, S. Basu, S. Pande, S. K. Ghosh and T. Pal, *J. Phys. Chem. C*, 2007, **111**, 16272–16277.
- 36 M. L. Sushko, K. M. Rosso and J. Liu, *J. Phys. Chem. C*, 2010, **114**, 20277–20283.
- 37 T. A. Mellan, K. P. Maenetja, P. E. Ngoepe, S. M. Woodley, C. R. A. Catlow and R. Grau-Crespo, *J. Mater. Chem. A*, 2013, **1**, 14879–14887.
- 38 L. Miao, J. Wu, J. Jiang and P. Liang, *J. Phys. Chem. C*, 2013, **117**, 23–27.
- 39 M. Minakshi, D. Mitchell, R. Jones, F. Alenazey, T. Watcharatharapong, S. Chakraborty and R. Ahuja, *Nanoscale*, 2016, **8**, 11291–11305.
- 40 D. A. Tompsett, D. S. Middlemiss and M. S. Islam, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2012, **86**, 205126.
- 41 H. Sato, T. Enoki, M. Isobe and Y. Ueda, *Phys. Rev. B: Condens. Matter Mater. Phys.*, 2000, **61**, 3563–3569.
- 42 Q. Zhang, W. Zhang, W. Wan, Y. Cui and E. Wang, *Nano Lett.*, 2010, **10**, 3243–3249.
- 43 R. Zhang, Q. Wang, J. Liang, Q. Li, J. Dai and W. Li, *Phys. B*, 2012, **407**, 2709–2715.
- 44 R. Zhang, Q. Wang, Q. Li, J. Dai and D. Huang, *Phys. B*, 2011, **406**, 3417–3422.
- 45 S. Yang, D. Li, T. Zhang, Z. Tao and J. Chen, *J. Phys. Chem. C*, 2012, **116**, 1307–1312.



- 46 D. Wang, L.-M. Liu, S.-J. Zhao, B.-H. Li, H. Liu and X.-F. Lang, *Phys. Chem. Chem. Phys.*, 2013, **15**, 9075–9083.
- 47 D. Wang, J. Yang, X. Li, D. Geng, R. Li, M. Cai, T.-K. Sham and X. Sun, *Energy Environ. Sci.*, 2013, **6**, 2900–2906.
- 48 K. Zhang, P. Han, L. Gu, L. Zhang, Z. Liu, Q. Kong, C. Zhang, S. Dong, Z. Zhang, J. Yao, H. Xu, G. Cui and L. Chen, *ACS Appl. Mater. Interfaces*, 2012, **4**, 658–664.

