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Atomic structure, electronic properties and generalized stacking fault energy of diamond/c-BN multilayer

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The atomic structures, electronic properties and generalized stacking fault (GSF) energies of the diamond/c-BN multilayer are investigated systematically with first-principles calculations. A total of twelve interfacial structures are considered, encompassing two c-BN terminations, each of which involves two diamond terminations and three stacking sequences. We identify two stable interfacial structures, where the stacking sequence near the interface is identical to that in bulk diamond, implying a smooth transition across the interface. By using several analytical techniques, we find that the interfacial bonds are primarily of a mixed covalent-ionic nature, and the covalency stems from the sp^3 hybridization between interfacial C sp states and B sp states. The shapes of the GSF energy curves for the interfaces are similar to those for bulk diamond and c-BN, albeit that the unstable GSF energies for the former are smaller than those for the latter. The GSF energies of the slip planes near the interface alter remarkably due to the interfacial effect, meaning that they are dependent on the slip systems.

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1. Introduction

Ultra-hard materials have been widely used in many fields, such as cutting and polishing tools, aerospace structural components, high power and high frequency electronic devices.¹ Diamond is currently the hardest material, but its application may be limited by some of its inherent shortcomings.² Compared with diamond, cubic boron nitride (c-BN) possesses a higher thermal and chemical stability and is considered as an ideal coating material for cutting tools. However, c-BN has a lower Vickers hardness than diamond.³

Searching for materials that are harder and more stable than diamond for practical needs has attracted increasing attention in past years, and several methods have already been reported for this purpose.^{4,5} It is known that boron, carbon, and nitrogen atoms have a similar ionic radii and they can form sp^3 hybridized bonds, indicating that the superhard B–C–N ternary and binary materials can be considered as promising alternative candidates for diamond and c-BN. Both theoretical and experimental studies have indicated many of such materials with high hardness and excellent thermal stability, including BC_2N , BC_4N , BC_6N , β - C_3N_4 , BC_3 and BC_5 .^{6–10} However, in terms of the Hall–Petch relation, the hardness of a nanocrystalline material increases with the decrease

of its grain size. In particular, the nanoscale twin boundaries can act as regular grain boundaries.¹¹ For example, it has been reported that nanotwinned (nt) diamond and c-BN possess an ultrahigh Vickers indentation hardness, exceeding 200 and 100 GPa (twice that of single-crystal structure), respectively, as their twin thicknesses are reduced to a few nanometers (~ 3.8 nm for nt c-BN and ~ 5 nm for nt diamond).^{12,13} Theoretically, Li *et al.*¹⁴ found that bond rearrangement at twin boundary can remarkably enhance indentation shear strength in nt c-BN under indentation compression and shear strains. Huang *et al.*¹⁵ applied molecular dynamics simulations for the responses of c-BN films under nanoindentation, and found that during the indentation, plastic deformation of c-BN is can mainly be attributed to stress-induced slips of dislocations along $\{111\}\langle 110 \rangle$ orientations. In addition, Wang *et al.*¹⁶ reported the synthesis and characterization of transparent bulk diamond/c-BN alloy, and showed that the alloy has a superior chemical inertness over the polycrystalline diamond and a higher hardness than a single crystal.

By introducing layered interfaces into multilayer composites, mechanical properties of materials could be greatly improved, especially as the layer thickness reaches nanometer level.¹⁷ For instance, hardness of diamond(111)/c-BN(111) nanomultilayer composites can be increased to over 80 GPa while maintaining low compressibility, high thermal stability, and p -type semi-conductivity.¹⁸ Recently, an epitaxial diamond/c-BN heterojunction has been produced using a temperature gradient method, and a kind of heterointerface was found to be accommodated by a lattice mismatch, which consists of a network with continuous stacking fault arranged by hexagonal dislocation loops.¹⁹ For such composites, although their interfacial structure can be

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experimentally observed, it remains difficult to make clear the effects of the interfaces on mechanical properties of the composites due to the variety of interfacial structures formed in practical deposition and to the complex atomic structures and their interactions. In addition, it is known that plastic deformation and its associated nucleation, glide and transmission of dislocations are affected by interfaces,²⁰ rendering a systematic atomistic investigation of the diamond/c-BN interface in the multilayered composites timely and important.

First-principles calculation can serve as an effective means to investigate mechanical properties and atomic and electronic structures of an interface.^{21–23} In this article we apply first-principles calculations to study the possible interfaces in diamond and c-BN multilayers with a special focus on atomic stacking sequences and electronic states at the interfaces. The generalized stacking fault (GSF) energies of the likely slip systems are also calculated to probe the interfacial effects on mechanical properties of the multilayer composites.

2. Calculation details

Vienna *ab initio* simulation package (VASP) within the framework of density functional theory (DFT) was applied in our calculation. The generalized gradient approximation by Perdew and Wang (GGA-PW91)²⁴ was adopted to describe the exchange-correlation functional. The electron-ion core interactions were described using the pseudo-potentials of carbon, boron and nitrogen atoms with the electronic configurations of $2s^2 2p^2$, $2s^2 2p^1$, and $2s^2 2p^3$, respectively. Single-particle Kohn–Sham wave function^{25,26} was extended using the plane waves with a cut-off energy of 500 eV and sampling of irreducible edge of Brillouin zone was performed with a regular Monkhorst–Pack scheme²⁷ for all calculations. We used $11 \times 11 \times 11$ *k*-point meshes for bulk calculations and $9 \times 9 \times 1$ *k*-point meshes for calculations of adhesion or GSF energies. A vacuum of 15 Å was embedded into the supercell to avoid the interaction between the slab and its periodic images in the calculation of GSF energies. In all relaxations, total energy was converged to less than 10^{-5} eV and the Hellmann–Feynman force on each atom was set as 0.05 eV \AA^{-1} .

Adhesion energy (W_{ad}) depended sensitively on atomic species and electronic structure of the atoms at an interface, which is the key to predict mechanical properties of an interface. W_{ad} was defined as the energy required to break down the interfacial bonds and separate the interface into two free surfaces, which could be calculated by²⁸

$$W_{\text{ad}} = (E_{\text{diamond}} + E_{\text{c-BN}} - E_{\text{slab}})/A, \quad (1)$$

where E_{diamond} , $E_{\text{c-BN}}$, and E_{slab} were the total energy of the isolated relaxed diamond, c-BN and diamond/c-BN slab with interface, respectively, and A was the interface area. The GSF energy, which was considered a perfect crystal cutting across a plane into two parts and subjected to a relative displacement f and then rejoined, was usually used to measure nonelastic deformation, especially for dislocation glide and twinning. The GSF energy could be calculated by²²

$$\gamma_{\text{SFE}} = (E_f - E_0)/A, \quad (2)$$

where E_f and E_0 were the total energy of the supercell with and without a stacking fault. A was the stacking fault area. To obtain the total energy with a stacking fault (E_f), the atomic positions perpendicular to the shear displacement plane were fully relaxed, while those in the direction parallel to the slip plane were fixed to maintain stacking fault during relaxation after a relative displacement.

3. Results and discussion

3.1 Structures and properties of interfaces

3.1.1 Adhesion energy. Table 1 compares our calculated results with the published works for both bulk diamond and c-BN, where a good consistency is achieved,^{29–31} validating the use of our calculation methodology to describe this system. Since the orientation relationship between diamond and c-BN is $(111)_{\text{diamond}} \parallel (111)_{\text{c-BN}}$ and $[1\bar{1}0]_{\text{diamond}} \parallel [1\bar{1}0]_{\text{c-BN}}$ ¹⁹ and the B–C bonds are observed at the diamond/c-BN interfaces,^{19,32} we consider the B-terminated c-BN only here. On the other hand, there are two types of stacking pattern in diamond structures, shuffle- and glide-set. Hence, two types of terminations of c-BN at (111) interfaces are established, denoted with B1 (Fig. 1(b)) and B2 (Fig. 1(c)). Similarly, two stacking modes in diamond (111) are also taken into consideration, as denoted with C1

Table 1 Comparison of our predicted structural parameters with the experimental and other reported results^a

Parameters	Diamond			c-BN		
	This work	Exp. ²⁹	Others ³¹	This work	Exp. ³⁰	Others ³¹
a (Å)	3.575	3.567	3.567	3.625	3.615	3.627
C_{11} (GPa)	1052	1079	1055	791	820	783
C_{12} (GPa)	125	124	120	173	190	172
C_{44} (GPa)	556	578	559	447	480	444
K (GPa)	434	443	431	379	382	376

^a a : lattice constant; C_{11} , C_{12} , C_{44} : elastic constants; and K : bulk modulus.

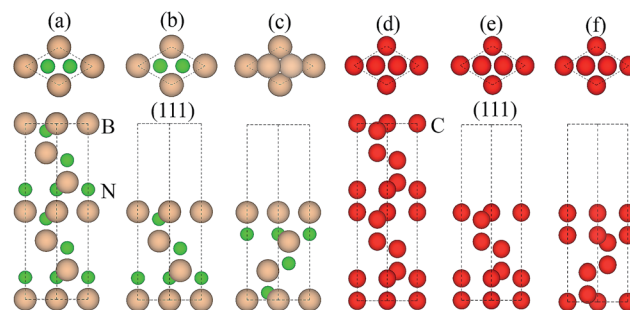


Fig. 1 Atomic structures: (a) bulk c-BN, (b) B1, (c) B2, (d) bulk diamond, (e) C1, and (f) C2. The upper parts are top views and the lower ones are side views. Only the top seven of thirteen symmetric layers are presented for each termination.



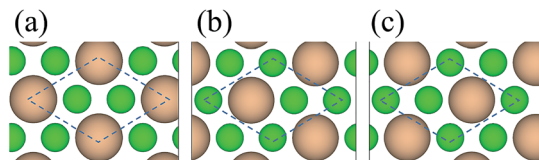


Fig. 2 Stacking sequences between diamond and c-BN: (a) OS site, (b) HS site, and (c) SS site. The c-BN proximal to interface is presented only for clarity. Dotted parallelogram outlines denote the projection of unit diamond cell in [111] direction.

Table 2 W_{ad} (J m^{-2}) for the twelve interfacial structures, including two terminated structures B1 and B2 and three possible stacking sequences OS, HS and SS site

Termination		Stacking sequences		
c-BN	Diamond	OS	HS	SS
B1	C1	11.325	4.907	2.122
	C2	11.085	6.507	4.356
B2	C1	7.285	1.049	0.043
	C2	5.789	18.301	18.211

(Fig. 1(e)) and C2 (Fig. 1(f)). In addition, there are three stacking sequences: interfacial C atoms of diamond are located (i) on the top surface atoms (OS) of c-BN (Fig. 2(a)), (ii) above the hollow site (HS) (Fig. 2(b)), and (iii) above the second-layer atoms (SS) (Fig. 2(c)). As a consequence, a total of 12 interfacial geometries are considered, which can be divided into two groups: B1 and B2. To satisfy the need of periodic boundary conditions, lattice constant of c-BN is shrunk by 1.20% to match that of diamond.

Table 2 lists adhesion energies of all the interfaces. In the B1 case, the adhesion energy for the OS stacking sequence is larger than that for the HS and SS, and the largest $W_{\text{ad}} = 11.325 \text{ J m}^{-2}$ appears in the case of C1/B1 with OS, the atomic structure of which is shown in Fig. 3(a). The stacking sequence at the interface with the largest W_{ad} is identical to that of bulk diamond structure. In the B2 case, the C2/B2 with HS possesses the largest W_{ad} of 18.301 J m^{-2} , and the corresponding atomic structure is shown in Fig. 3(b). The atomic stacking sequence at this interface also retains that in the bulk diamond (or c-BN). Such stacking sequence provides a smooth transition from c-BN to diamond. It is worthy of noting that the C2/B2 with SS has an adhesion energy of 18.211 J m^{-2} , very close to that of C2/B2 with HS. By comparing the adhesion energies of the 12 interfacial structures, we find the most stable interfaces in the B1 (Fig. 3(a)) and B2 (Fig. 3(b)) cases.

3.1.2 Local atomic structure. As shown in Fig. 3, there is a significant difference between the two types of interfaces, B1 and B2 (e.g. bond length at interface), which accounts for their distinct W_{ad} (B2 is greater than B1 in W_{ad}). For B1, the interfacial B–C distance is calculated as 1.655 \AA , strikingly larger than 1.544 \AA for bulk diamond and 1.563 \AA for c-BN. The lengths of C–C and B–N bonds near to the interface are 1.551 and 1.562 \AA , respectively, which deviate by 0.11 \AA from that of bulk diamond and 0.09 \AA from that of bulk c-BN. Such deviation is screened to

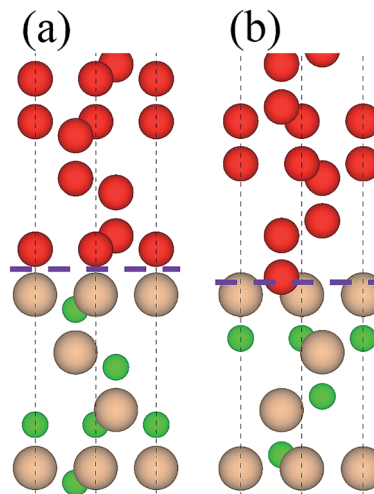


Fig. 3 Two stable interfacial atomic configurations: (a) B1 and (b) B2. Upper parts are diamond and lower parts are c-BN. Interface is denoted by dotted lines.

less than 0.06 \AA in the following layers, implying that the effect of B1 interface is rather confined. For B2, the interfacial B–C distance is 1.614 \AA , smaller than that of B1. The lengths of sub-interfacial C–C and B–N bond lengths are 1.502 \AA and 1.549 \AA , respectively, which deviate by 0.07 \AA from that of bulk diamond and 0.05 \AA from that of bulk c-BN. This deviation is screened to less than 0.03 \AA in the following layers, implying that the interfacial effect is localized.

3.1.3 Electronic properties. Fig. 4 shows density of states (DOS) projected onto selected atomic layers of the two interfaces. A key feature in Fig. 4 is that the partial densities of states (PDOSs) of the interfacial C and B layers show states at Fermi level (E_{F}) (Fig. 4(a) and (b)), indicating metallic nature at the interfaces, which vanishes in bulk diamond or c-BN (Fig. 4(c)). Such metallic behavior at the interface can be attributed to the fact that boron atoms can serve as dopants on the surface of pure diamond.³³ In addition, a significant sp^3 hybridization can be observed between interfacial sp states of C and sp states of B, indicating that the covalent bonds emerge at interface. It is worthwhile noting that the p_z state of the entire interfacial atoms suffers a significant change in the energy range between -10 and 0 eV , which is ascribed to the hybridization between the interfacial atoms.

To identify the type of chemical bond at interface, the charge density distribution and its difference are calculated, as shown in Fig. 5, in which the difference of charge density is calculated by subtracting the sum of the isolated diamond and c-BN slabs from the total interface charge density. There is a significant feature in Fig. 5(a) and (b) between the charge density of bulk c-BN and that of diamond. Charge distribution around N of c-BN is approximately spherically symmetric and distorted toward the neighboring B, indicating that c-BN has mixed ionic and covalent nature. It can be seen in Fig. 5(a) and (b) that charge in diamond region is located in the bridge section between C atoms, indicative of covalent bonds only in bulk diamond. Most of charges are located along B–N bonds in the region of c-BN



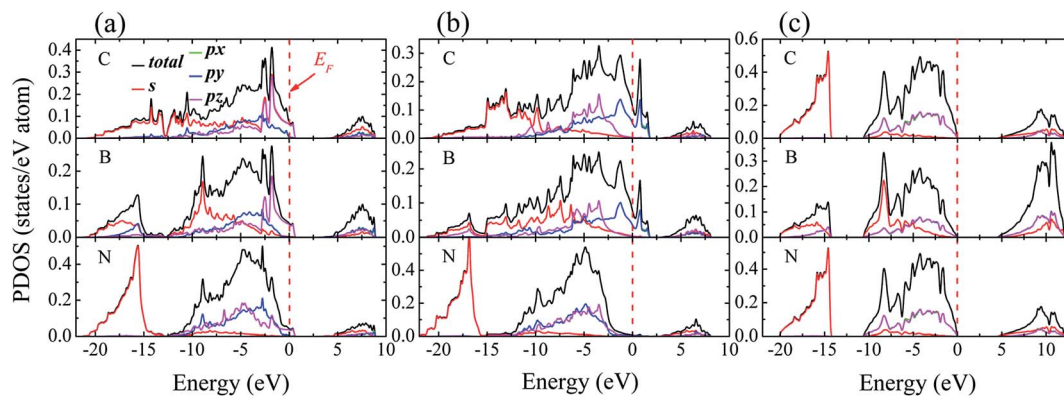


Fig. 4 Density of state (DOS) for (a) B1, (b) B2, and (c) bulk diamond and c-BN. For the multilayer, the PDOS of the first C layer in diamond part, first B layer and second N layer in c-BN part are present. The Fermi level is set to zero and represented with vertical dotted lines.

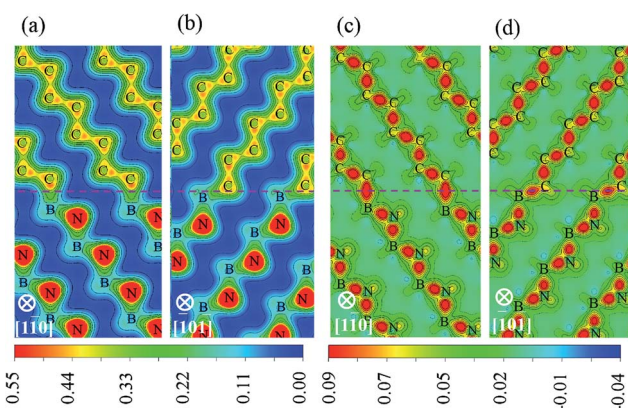


Fig. 5 Distribution of charge densities and charge density differences: charge density of (a) B1 and (b) B2, charge density difference of (c) B1 and (d) B2. The interfaces are represented with horizontal dotted lines.

and along C–C bonds in the diamond area, as shown in Fig. 5(c) and (d). Interfacial C–B bonds exhibit the following characters: (i) most charges are located around C atoms, and (ii) charges around C atoms are distorted toward the neighboring B atoms and remarkably accumulated along the interfacial B–C bonds.

These two observations suggest that the interfacial bonds are primarily of mixed covalent-ionic nature, which explains why the interfaces show a metallic character.

3.2 GSF energies of interfaces

3.2.1 GSF energies of interfaces. For a crystal of diamond-structure, there exist two patterns of stacking faults on the $\{111\}$ plane, glide- and shuffle-set, each of which has two types of slip directions, $\langle 110 \rangle$ and $\langle 112 \rangle$, as shown in Fig. 6(c). It can be found that the B1 interface is of shuffle-set pattern (Fig. 6(a)), while the B2 interface can only form glide-set dislocation (Fig. 6(b)). There are two common intrinsic energy barriers, the unstable stacking fault energy (γ_{USF}) and stable stacking fault energy (γ_{SF}), which are formally defined as maximum and minimum energies in GSF energy curves, respectively. The values of the γ_{USF} for all the slip systems are listed in Table 3. These energy barriers are related to many factors, such as phase transition, crystal growth, plastic deformation, dislocation glides and twin interactions.^{34–36}

Fig. 7 shows the GSF energies of the two kinds of interfaces with displacements along $\langle 110 \rangle$ and $\langle 112 \rangle$ directions, in which the GSF energies of bulk diamond and c-BN are also presented

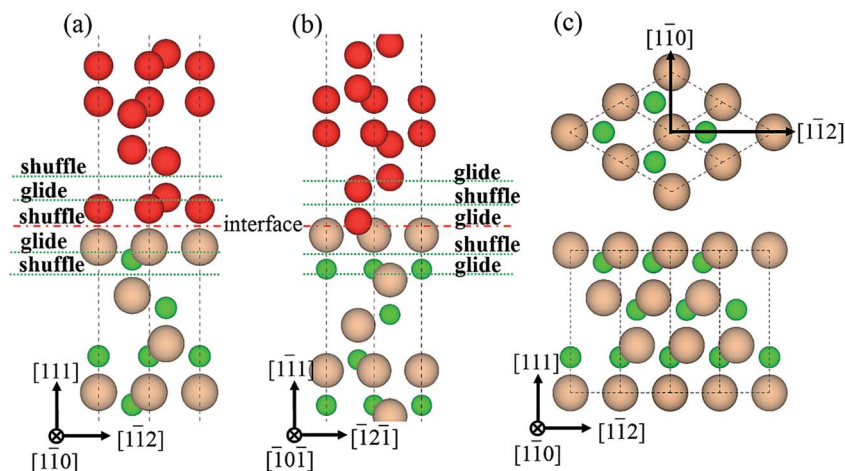


Fig. 6 Dislocations patterns, glide- and shuffle-set. (a) B1, (b) B2, and (c) two slip directions, $\langle 110 \rangle$ and $\langle 112 \rangle$.



Table 3 The γ_{USF} for the interfaces in B1 and B2, and for the bulk c-BN and diamond

Slip systems	B1 interface		B2 interface		Bulk c-BN		Bulk diamond	
{111}<110> shuffle	6.995	—	—	—	7.218	—	8.825	—
{111}<112> shuffle	9.123	—	—	—	9.325	—	10.303	—
{111}<110> glide	—	—	10.080	—	11.166	—	13.546	—
{111}<112> glide	—	—	1.893	12.346	3.413	13.171	5.285	13.588

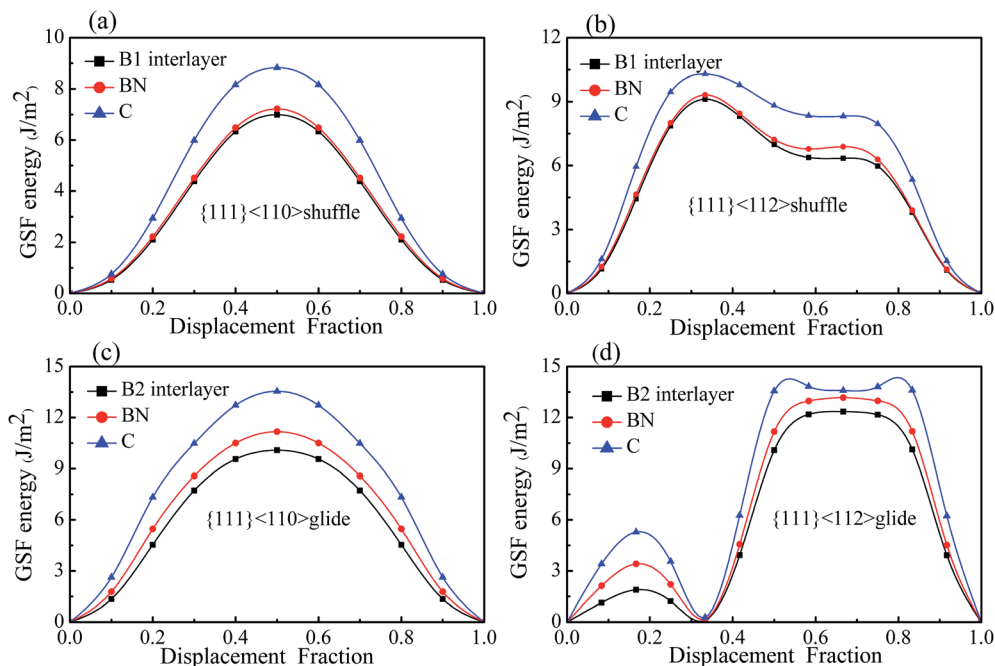


Fig. 7 The GSF energies of the interfaces B1 and B2, and of bulk C and c-BN: (a) and (b) are the B1 interface, (c) and (d) are B2 interface.

for comparison. It can be seen that the GSF energy curves of the interfaces have a shape similar to that of bulk diamond and c-BN. For all the slip systems, the γ_{USF} of the interfaces are almost equal to that of bulk c-BN, especially in case of shuffle-set dislocation. The shuffle-set dislocation in <110> direction possesses the minimum γ_{USF} of 6.995 J m⁻² (Fig. 7(a)), indicating that {111}<110> is the easiest direction for dislocation glide. The {111}<112> slip system for the glide-set dislocation has two values of γ_{USF} (1.893 and 12.346 J m⁻²), as shown in Fig. 7(d). The existence of the lower γ_{USF} (1.893 J m⁻²) indicates that resistance to the formation of twin structure in this slip system is much lower than that in bulk diamond (5.286 J m⁻²) and c-BN (3.413 J m⁻²). This also suggests that the {111}<112> slip system is easier to form partial dislocations.

3.2.2 Effect of interfaces. Since the interfacial effects are localized in terms of atomic structure and the GSF energies of the layer far away from interface is insignificantly affected by interface, we therefore only calculate the GSF energy curves for some layers near interface in all systems, as shown in Fig. 8. The slip systems include two types of stacking pattern, glide- and shuffle-set (Fig. 6(a) and (b)), and two slip directions, <110> and <112> (Fig. 6(c)). The GSF energies of bulk diamond and c-BN

are also presented for comparison. The γ_{USF} for all the slip systems are listed Table 4. The GSF energy curves for B1 and B2 show the same trend as those for bulk materials.

For the c-BN layers in {111}<110> glide-set and {111}<112> glide-set slip systems, the GSF energies of B2 are somewhat higher than those in bulk c-BN, and the B1 has the lowest γ_{USF} . As shown in Fig. 8(a) and (c), both B1 and B2 have a low γ_{SF} in {111}<112> glide-set slip system. For the c-BN layers in {111}<110> shuffle-set and {111}<112> shuffle-set slip systems, the GSF energies of B1 are slightly smaller than those in bulk c-BN (Fig. 8(e) and (f)), the trend of which reverses as compared to the former slip systems. The B2 in {111}<110> shuffle-set slip system has the lowest γ_{USF} of 6.277 J m⁻², indicating that perfect dislocation is easy to form in this slip system. In general, for the c-BN layers, little change is found in the GSF energies between B2 in {111}<110> and {111}<112> glide-set slip systems and of B2 in {111}<110> and {111}<112> shuffle-set slip systems.

For the diamond layers in {111}<110> glide-set and {111}<112> glide-set slip systems, the GSF energies for B1 and B2 are significantly lower than that in bulk diamond, as shown in Fig. 8(b) and (d). The B2 has the lowest γ_{USF} , and the B1 and B2 almost have the same γ_{USF} in {111}<112> glide-set slip



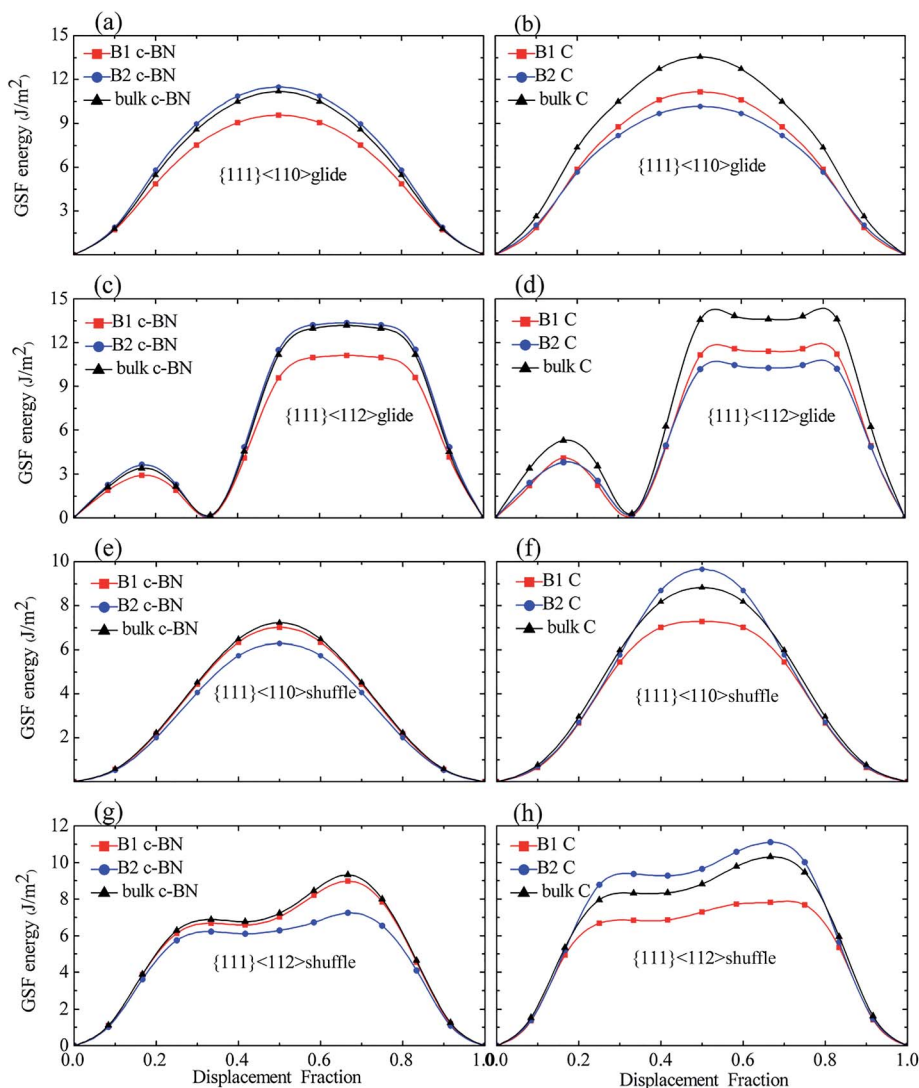


Fig. 8 The GSF energies of slip planes near the interfaces and of bulk diamond and c-BN: (a and b) $\{111\}\langle 110\rangle$ glide, (c and d) $\{111\}\langle 112\rangle$ glide, (e and f) $\{111\}\langle 110\rangle$ shuffle, and (g and h) $\{111\}\langle 112\rangle$ shuffle dislocations. The GSF energies of c-BN and diamond layer are shown on the left and right panel, respectively.

Table 4 The γ_{USF} of slip layers near the interfaces in B1 and B2, and of bulk c-BN and diamond

Slip systems	c-BN			Diamond		
	B1	B2	Bulk	B1	B2	Bulk
$\{111\}\langle 110\rangle$ glide	9.566	11.489	11.158	11.143	10.173	13.546
$\{111\}\langle 112\rangle$ glide	11.120	13.353	13.163	11.411	10.254	13.588
$\{111\}\langle 110\rangle$ shuffle	7.012	6.277	7.218	7.285	9.652	8.825
$\{111\}\langle 112\rangle$ shuffle	8.987	7.256	9.325	7.807	11.112	10.303

system. For the diamond layers in $\{111\}\langle 110\rangle$ shuffle-set and $\{111\}\langle 112\rangle$ shuffle-set slip systems (Fig. 8(f) and (h)), the GSF energies of B2 is higher than that of B1 and bulk diamond, while the GSF energies of B1 is less than that of bulk diamond, which differs from the former slip system in the diamond layers. For the diamond layers, the GSF energies of B2 in $\{111\}$

$\langle 110\rangle$ shuffle-set and $\{111\}\langle 112\rangle$ shuffle-set slip systems increases significantly, while that for the rest decreases. Therefore, we conclude that the GSF energies of the slip planes near interface behaves differently due to the interface, meaning that they are dependent on the slip systems.

4. Conclusions

We have investigated the atomic structure, electronic properties, and generalized stacking fault energy of the diamond/c-BN multilayer systematically with first-principles calculation. A total of twelve interfacial structures are considered, encompassing two c-BN terminations, each of which involves two diamond terminations and three stacking sequences. By comparing adhesion energy, we identify two stable interfacial configurations, where stacking sequences near the interfaces are identical to those in bulk diamond, implying a smooth



atomic transition across interface. Several analytic methods are applied to characterize the nature of the interfaces. The interfacial bonds are primarily of mixed covalent-ionic nature, and the covalency of interfacial bonds stems from the sp^3 hybridization between the sp states of C and of B. Most charges are located around C atoms, which are distorted toward the neighboring B atoms and remarkably accumulated along the interfacial B–C bonds. Further calculation of GSF energy reveals that the shape of the GSF energy curves for the interfaces is similar to that of bulk diamond and c-BN, despite that the unstable stacking fault energies for the former are smaller than those for the latter. The GSF energies of the slip planes near interface alter differently due to interfacial effect, meaning that they rely on the slip systems.

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