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Atomic scale investigation of enhanced ferroelectricity in (Ba,Ca)TiO₃†

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The precise atomic positions and occupancies in (Ba,Ca)TiO₃ ceramics have been characterized by high angle annular dark field (HADDF)-scanning transmission electron microscopy (STEM), electron energy loss spectroscopy (EELS), and annular bright field (ABF)-STEM. EELS precisely determines the distribution of Ba, Ca, and Ti ions in the perovskite structure, confirming the occupancy of ~7% Ca content at B-site in (Ba_{0.75}Ca_{0.25})TiO₃, which is the first direct evidence of Ca occupancy at the B-site in (Ba,Ca)TiO₃ ceramics. ABF-STEM mapped the displacement of Ti ions and oxygen ions with respect to the center of Ba ions. By averaging the displacements of Ti and O ions in multiple single domains, it confirms the average Ti displacement of 0.263 Å, and large apical and equatorial oxygen displacement of 0.264 Å and 0.347 Å, respectively. Such great displacements in (Ba,Ca)TiO₃ compared to BaTiO₃ are direct evidence for the structure origin of the ferroelectric enhancement in Ca substituted BaTiO₃.

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Perovskite (ABO₃) ceramics are the most important materials for dielectric, piezoelectric, pyroelectric and ferroelectric applications.^{1,2} All these physical characteristics are primarily determined by the polarization. The dielectric constant is the oscillation of polarization under an AC electric field.³ The piezoelectric tensor is also determined in polar crystals and largely depends on polarization tensors. The pyroelectric property is the temperature dependence of polarization. The ferroelectric transition temperature, or Curie temperature is believed to increase with spontaneous polarization.⁴ As the critical role of so many important physical properties, polarization, is worthy to be understood deeply for great fundamental physical meaning and potential application significance. In ferroelectrics, the spontaneous polarization is indeed originated from the dipoles formed by displacements of charged ions inside the crystal unit cell. Numerous investigations of polarizations have been reported on the macro properties, while the report of atomic scale structure about the displacement of specific atoms is limited.⁵ The recently developed high-resolution transmission electron microscopy allow the determinations of atomic positions.^{6,7} With STEM EELS, specific atoms occupancies can be mapped⁸ and light element oxygen can be investigated by ABF-STEM.⁹ Combined with all the methods and techniques, the local polarization,¹⁰ ferroelectric

domain structure,^{11–13} interface effect¹⁴ and defects¹⁵ can be directly mapped across the investigated structure.

BaTiO₃, one of the most typical perovskite ferroelectric materials, is widely used in multilayer ceramic capacitors^{16,17} and many other applications.^{18,19} The spontaneous polarization in BaTiO₃ is originated from Ti off center displacement.²⁰ Ca ions has been an important chemical substitutions on Ba site for particular applications, such as lead free piezoelectric^{21,22} or multilayer capacitors.²³ Ca could intriguingly remain the Curie temperature and enhance its polarization.^{24,25} It rebels the common principle that smaller A-site ions substituted into BaTiO₃ matrix brings shrinkage of unit cell volume and suppresses the Ti displacement.²⁶ Laterly, Ca off centering was putted forward, proved to have some similarities to Pb off centering,²⁷ contributing to the polarization.²⁸ The structure-refinement gave instantaneous atomic positions supported the ferroelectric enhancement in (Ba,Ca)TiO₃.²⁹ However, the precise atomic position determination of Ti displacement in (Ba,Ca)TiO₃ materials at atomic scale is still lack.

Meanwhile, there is a remained controversy in (Ba,Ca)TiO₃ system for decades. Many researchers have stated that Ca ions could occupy B-site, especially in non-stoichiometric design, or prepared with special method.^{30,31} The site occupancy of Ca ions is believed to significantly influence the enhanced dielectric properties,^{32,33} and Curie temperature,³⁴ or even to induce double *P-E* loops.³⁵ To understand the local Ca site occupancy is of great importance for the drastically improvement of physical properties in Ca substituted BaTiO₃ materials.

In the present work, we located atom positions from unit-cell scale in BaTiO₃ and (Ba,Ca)TiO₃ using high angle annular dark field (HADDF)-scanning transmission electron microscopy (STEM), equipped with electron energy loss spectroscopy

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(EELS), and annular bright field (ABF)-STEM. The displacement of Ti atom and oxygen octahedral with respect to A-site are determined and averaged in one single domain. Both Ti ions and oxygen octahedrons shift stronger with increasing Ca content. Besides, EELS signal of Ca ions at B-site is the first direct structure evidence of the Ca ions' occupancy of Ti ions.

The (Ba,Ca)TiO₃ ceramics are prepared by a standard solid state reaction method. The reagent powders of CaCO₃ (99.99%), BaCO₃ (99.93%), and TiO₂ (99.99%) were mixed, and the mixtures were calcined at 1273 K in air for 3 h after drying. The calcined powders were pressed into the disks of 12 mm in diameter and 2 mm in thickness under a uniaxial pressure of 98 MPa. The green compacts were sintered at 1623 K in air for 3 h to yield the dense ceramics. TEM samples were prepared from the grinded powder from ceramics. The XRD patterns are shown in Fig. S1.† The selected two compositions in the present work: (Ba_{0.8}Ca_{0.2})TiO₃, (Ba_{0.75}Ca_{0.25})TiO₃ are confirmed to be tetragonal phase (PDF card 05-0626). With increasing Ca content, the unit cell volume decreases due to smaller ion radius of Ca²⁺ than Ba²⁺, lead to the peak shift to higher angle. The preparation method, dielectric, ferroelectric properties has been comprehensively improved by Ca²⁺ substitution.^{24,25} The remanent polarization *P_r* and dielectric strength *E_b* are significantly enhanced by Ca-substitution, and the best *P_r* (11.34 μC cm⁻²) and dielectric strength *E_b* (75 kV cm⁻¹) are obtained in the composition *x* = 0.25. Thus, here in the present work we choose these best two compositions to illustrate this enhancement in microstructure structure. Plan view specimens for HRTEM are prepared by disaggregating the ceramic followed by grinding in an agate mortar. The powder was then suspended in acetone and dispersed onto a holey carbon 200 mesh TEM grid. The high-resolution HAADF-STEM image was acquired using a G² 80-200 Chemi STEM FEI Titan microscope fitted with an aberration corrector for the probe-forming lens, operated at 200 kV, equipped with electron energy-loss spectroscopy (EELS). The STEM convergence semi-angle was approximately 21.4 mrad, providing a probe size of approximately 0.8 Å at 200 kV.

Fig. 1(a) shows the HAADF-STEM image of (Ba_{0.75}Ca_{0.25})TiO₃ ceramic in a projection along [010] axis, similar HAADF-STEM image of (Ba_{0.80}Ca_{0.20})TiO₃ ceramic is shown in Fig. S2.† We selected an area (the green rectangle) to do the EELS spectrum to observe the distribution of cations. By integrating the

intensity of ionization edges from the atomic-resolution EELS spectra where the peak intensity is related to the elemental content, the distribution of specific cation can be mapped (see Fig. 1(b–e)). Ba ions signal in EELS spectra only appears at A-site, and Ti ions signal only appears at B-site. However, the doped Ca atoms show EELS signal at both A- and B-sites (indicated as the arrowheads in Fig. 1(b)). With atomic EELS spectrum image, each single pixel can be corresponded to an EELS spectrum. Several pixels corresponding to A-site atoms in the spectrum image were selected and fitted to a linear combination of Ca²⁺ and Ba²⁺ reference spectra using EELS MODEL,³⁵ therefore, the average Ca/Ba ratio of A site was obtained. The detailed image simulations of EELS spectrum demonstrate that about 15 ± 2% of Ca atoms substitute A-site, the left 4 ± 1% Ca atoms are located at B-site in (Ba_{0.80}Ca_{0.20})TiO₃. Similarly, only 18 ± 2% Ca atoms substitute A-site, and 7 ± 1% occupy B-site in (Ba_{0.75}Ca_{0.25})TiO₃. This 7 ± 1% is a big portion that would influence the local strain field and build-in electric field, for the Ca ions radius and charge imbalance. It is confirmed here that the Ca ions could occupy B site with microstructure evidence for the first time. It is worth to notice that the large portion of Ca cations occupied B-site could influence lots of physical properties, such as lowering Curie temperature, and inducing double hysteresis loops. This is also the first demonstration of Ca occupancy at B-site in the composition near solid solution limit in (Ba,Ca)TiO₃, which means the multisite occupancy of Ca happens across the whole solid solution within the solid solution limit.

To make sure the reliability of the occupancy of specific atoms, the image intensity must be free of contributions arising from electron scattering at neighboring atomic columns. In order to guarantee that the Ca EELS intensity at B-site is not from the scattering of the A-site Ca ions, we used STEM sim software to simulate the HAADF STEM image and EELS STEM mapping image of Ba_{0.75}Ca_{0.25}TiO₃ along [010] zone axis which is presumably regarded only contains A-site Ca. The main parameters in Bloch wave modification are listed in Table S1.† The sample is regarded to keep at room temperature (295 K), with a thickness 20 nm, and occupy a tetragonal BaTiO₃ like phase. The crystal structure of the modification is shown in Fig. S3.† As shown in Fig. 2(a), the simulated HAADF-STEM image corroborates well to the experimental result in Fig. 1(a). Fig. 2(c–e) show the simulated STEM EELS image of Ba, Ca, and Ti atoms. It is worth noting that the simulated EELS image of Ca ions shows no signal at B-site (see Fig. 2(d)). As shown in Fig. 2(b), it compares the intensity profile of line scanning in Fig. 2(d) and the line intensity from experimental observed Ca EELS-STEM in Fig. 1(b). It is clearly that the simulated line intensity of Ca signal only shows a peak at A-site positions. However, the experimentally observed Ca EELS signal show intensity peak at B-site. This simulation excludes the possibility of Ca ions EELS signal at B-site due to the delocalization inelastic scattering of A-site Ca ions. That is to say, the experimental EELS signal of Ca ions at B-site shown in Fig. 1(b) is exactly due to the Ca ions occupied B-site, not the inelastic scattering from A-site Ca ions. Same simulation has also been performed in Ba_{0.80}Ca_{0.20}TiO₃, which can be found in Fig. S4.†

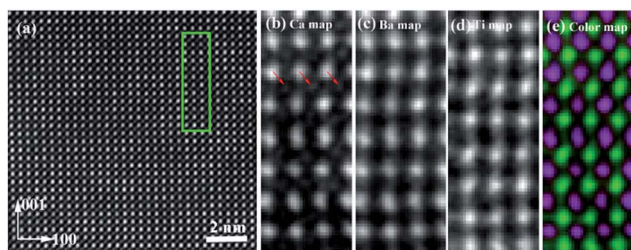


Fig. 1 (a) HAADF STEM image of Ba_{0.75}Ca_{0.25}TiO₃ ceramics including the survey region 3D EELS data is acquired from the region indicated by the green rectangle. The atomic resolution elemental maps of Ca (b), Ba (c) and Ti (d) are separately present. (e) Color map of the Ca (red), Ti (green) and Ba (blue) from the survey region.



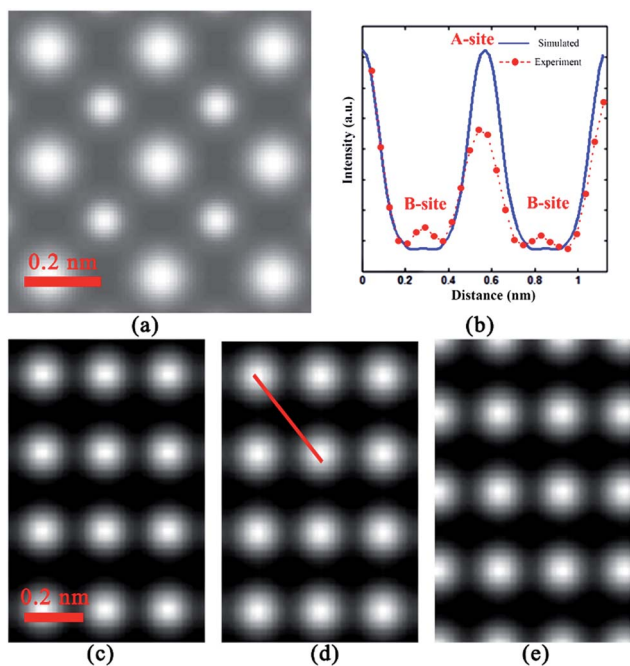


Fig. 2 Simulated results for $\text{Ba}_{0.75}\text{Ca}_{0.25}\text{TiO}_3$ sample of (a) atomic resolution HAADF STEM image viewed along [100] zone axis (b) intensity profile of simulated (blue line) and experimental (red dots) EELS spectrum image of Ca along the indicated line in (d). Simulated STEM EELS image of (c) Ba (d) Ca (e) Ti with Gaussian peak filter of 0.07 nm.

The displacements of dipole ions in displacement ferroelectrics is of great importance to understand their polarization. For $(\text{Ba,Ca})\text{TiO}_3$, the enhancement in polarization compared to BaTiO_3 has not been clarified from atomic displacements of its Ti–O dipoles, which should be most direct method to understand the enhancement. Here, the HAADF and ABF-STEM images have been combined to investigate the displacements of Ti–O dipoles (green HAADF image; red inverted ABF image), which are simultaneously obtained along [010] zone axis in $\text{Ba}_{0.75}\text{Ca}_{0.25}\text{TiO}_3$. As shown in Fig. 3, the structure (one projected unit cell) is indicated schematically (position of Ti, Ba/Ca, and O atomic columns are indicated by blue, green/yellow, and red circles, respectively). The position of Ti and O atoms displace along c axis by a distance d_1 and d_2 with respect to the position of the center of Ba sites. This shift means the unit cell is in a polarized state.

For a long time, the precise observation of oxygen has been difficult. In TEM analysis, therefore, more attention has been paid to the contribution of displacement of metal ions for ferroelectricity, such as Ti ions in BaTiO_3 and PbTiO_3 . Most of the local polarization has been calculated by the displacement of metal ions only. Oxygen octahedral displacement has been ignored or implied by empirical relation respect to Ti ions. However, oxygen octahedral usually has larger displacement than Ti ions in perovskites, and its direction dominantly determines the local polarization. In order to precisely determine the displacement of each atom, especially oxygen, annular bright field (ABF)-STEM was used to locate Ti–O dipoles. As

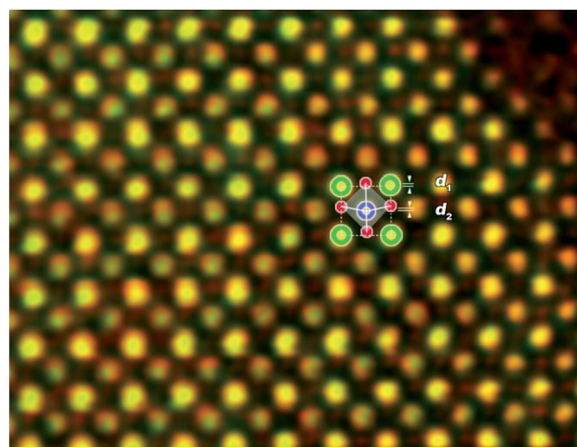


Fig. 3 Combined image of HAADF and simultaneously obtained ABF-STEM of the $\text{Ba}_{0.75}\text{Ca}_{0.25}\text{TiO}_3$ view along [010] zone axis. The schematic view of the crystals structure of the tetragonal $\text{Ba}_{0.75}\text{Ca}_{0.25}\text{TiO}_3$ is also shown. The d_1 and d_2 denote the displacement of Ti atoms (blue) and O atoms (red) along c axis from the centrosymmetry.

shown in Fig. 4, ABF-STEM images have been recorded along [010] zone axis. The darkest spots correspond to the mixture of heaviest Ba and Ca atoms, and the slightest spots refer to oxygen atoms. The atomic displacement map of Ti ions (Fig. 4(a)) and the center of oxygen octahedral (Fig. 4(b)) with respect to Ba ions center are modified, superimposed on the ABF-STEM image. The direction of the arrows indicates the polarization direction with respect to the center of Ba ions, and the color scale of arrows indicates the magnitude of polarization vector. The position of the contrast maxima in the images,

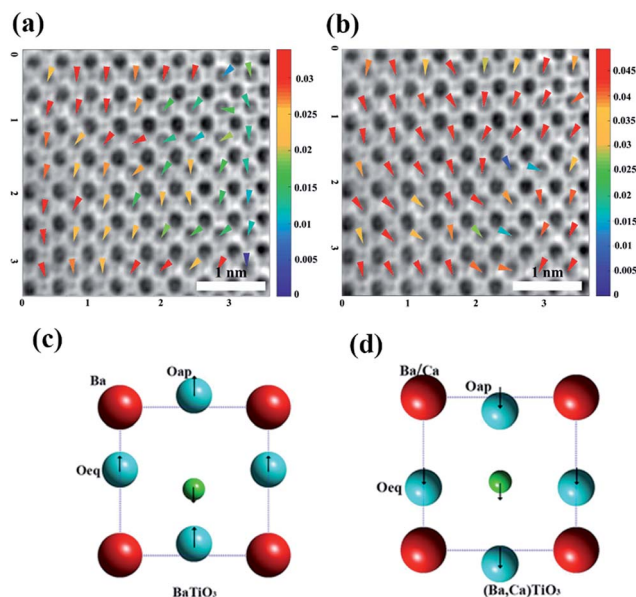


Fig. 4 Map of atomic displacement vectors showing the displacement of (a) Ti atoms (arrows), and (b) the center of oxygen octahedral (arrows) from the center of the projected Ba atoms superposed on the ABF-STEM images [010] zone axis of $\text{Ba}_{0.75}\text{Ca}_{0.25}\text{TiO}_3$. The plane view of BaTiO_3 (c) and $(\text{Ba,Ca})\text{TiO}_3$ (d) projected from a axis.



corresponding to the atomic positions, were determined by means of a least-squares fit of the intensity distribution using two-dimensional Gaussian profiles.

The Ti displacement map (Fig. 4(a)) superimposed on the ABF-STEM image illustrate a clear alignment of Ti upward along *c* axis, coincided with the direction of spontaneous polarization in tetragonal BaTiO₃. The oxygen octahedrons shift stronger in same direction compared to Ti ions. The average magnitude of the local Ti displacement in the present mono-domain is calculated as 0.263 ± 0.111 Å, whereas the oxygen octahedron has an average displacement of 0.268 ± 0.100 Å. The average displacement of Ti ions is much higher than that in the nano sized BaTiO₃ value (0.14 Å).³⁶

With further investigating the oxygen ions, we distinguish the three oxygen ions in one unit cell as one apical oxygen (O_{ap}) and two equatorial oxygen (O_{eq}). The average displacement of apical oxygen (O_{ap}) is 0.264 ± 0.110 Å, and the average displacement of equatorial oxygen (O_{eq}) is 0.347 ± 0.145 Å. This value is much higher than that in BaTiO₃ structure. According to the previous report of neutron diffraction in BaTiO₃ structure, the Ti ions move upward around 0.0904 Å, whereas the equatorial oxygen and apical oxygen moves downward 0.0424 Å and 0.0985 Å, respectively.³⁷ As shown in Fig. 4(c and d), it can be compared that the displacements of Ti and O ions shifts to the same direction in (Ba,Ca)TiO₃, whereas they shift to opposite direction in BaTiO₃. It is similar to that in PbTiO₃, wherein the Ti and O ions move to the same direction, and the displacements are much higher than that in BaTiO₃. In this respect, the Ti–O dipoles in (Ba,Ca)TiO₃ has similarity to that in PbTiO₃, and it should be the structure origin of the ferroelectric enhancement in (Ba,Ca)TiO₃ compared to BaTiO₃.

With these result, we can analysis the site contributions to the net polarizations using the equation below:³⁸

$$\delta P = \frac{e}{v} \sum_{m=1}^N Z_m^* \times \delta u_m$$

where, *N* is the number of atoms in the primitive unit cell, δu_m is position vector, and *v* is the volume of the unit cell. In the calculation, the center of Ba/Ca is fixed as zero point and the effective charges for oxygen atoms are distinguished as two equatorial atoms and one apical atom. Disregarding the distortion of oxygen octahedrons, and the difference of Born effective charge in Ba or Ca ions, the spontaneous polarization of one unit cell in (Ba,Ca)TiO₃ can be calculated as follow:

$$P_s = \frac{e}{v} (2\delta_{eq}Z_{eq} + \delta_{ap}Z_{ap} - \delta_{Ti}Z_{Ti})$$

where, *Z*_{eq}, *Z*_{ap}, and *Z*_{Ti} are the Born effective charge of equatorial oxygen and apical oxygen and Ti atom, respectively. The δ_{eq} , δ_{ap} , and δ_{Ti} are the displacement of atom from the positions of centrosymmetry, respectively. The *v* denotes the unit cell volume, which is refined from XRD result. The data are obtained from average displacements from multiple single domains. The local average polarization of the single domain is calculated as $27.6 \mu\text{C cm}^{-2}$, which is slightly higher than the macroscopic polarization measured in ceramic sample. It is due

to the defects and different polarization direction in multiple 90° and 180° domains in ceramic sample.

Conclusions

In summary, in (Ba_{0.75}Ca_{0.25})TiO₃ ceramic, a big portion of ~7% Ca content at B-site is confirmed by EELS-STEM, which is the first TEM evidence for Ca ions' B-site occupation. This founding is very important to understand the Curie temperature, dielectric constant and double ferroelectric hysteresis loops in (Ba,Ca)TiO₃ ceramics. More importantly, average Ti displacement of 0.263 Å, and large apical and equatorial oxygen displacement of 0.264 Å and 0.347 Å were confirmed using HADDF-STEM combined with ABF-STEM in (Ba_{0.75}Ca_{0.25})TiO₃ single domain, respectively. This great increase of magnitude of displacements in (Ba,Ca)TiO₃ compared to BaTiO₃ is the inherent structure origin of the ferroelectric enhancement in Ca substituted BaTiO₃.

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