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# Hybrid silicon–carbon nanostructures for broadband optical absorption†

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Proper design of nanomaterials for broadband light absorption is a key factor for improving the conversion efficiency of solar cells. Here we present a hybrid design of silicon–carbon nanostructures with silicon clusters coated by carbon cages, *i.e.*,  $\text{Si}_m\text{@C}_{2n}$  for potential solar cell application. The optical properties of these hybrid nanostructures were calculated based on time dependent density function theory (TDDFT). The results show that the optical spectra of  $\text{Si}_m\text{@C}_{2n}$  are very different from those of pure  $\text{Si}_m$  and  $\text{C}_{2n}$  clusters. While the absorption spectra of pure carbon cages and  $\text{Si}_m$  clusters exhibit peaks in the UV region, those of the  $\text{Si}_m\text{@C}_{2n}$  nanostructures exhibit a significant red shift. Superposition of the optical spectra of various  $\text{Si}_m\text{@C}_{2n}$  nanostructures forms a broad-band absorption, which extends to the visible light and infrared regions. The broadband adsorption of the assembled  $\text{Si}_m\text{@C}_{2n}$  nanoclusters may provide a new approach for the design of high efficiency solar cell nanomaterials.

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## Introduction

As an important global problem, the potential energy shortage has attached a lot of attention. Solar energy is a clean, safe energy, and it is the largest source of sustainable energy. Making efficient utilization of solar energy is key to the development of modern economy and society. While solar cell technologies have been developing for many years, widespread use of solar cells to convert light into electricity is still limited by either high cost or low efficiency.<sup>1</sup> Reducing the cost and improving the efficiency of light-to-electricity conversion devices are highly desirable for effective utilization of solar energy.

Silicon-based nanomaterials have attracted a lot of attention due to their low reflectivity for light, high carrier collection efficiency, and potential low cost.<sup>2–10</sup> However, the optical properties and thus the efficiency of the photovoltaic devices can be strongly dependent on the shape and size of the nanostructures as well as the substrate materials on which the nanostructures are supported.<sup>11–18</sup>

In the past several years, considerable theoretical and experimental research have been devoted to enhancing the light absorption by designing difference Si-based nanostructures,

such as nanowires,<sup>3</sup> nanosphere,<sup>4,19–21</sup> nanocylinders,<sup>5,14</sup> nanocones,<sup>6,14</sup> nanodomains<sup>7</sup> and nanoholes,<sup>8,9</sup> *etc.* For example, silicon nanocylinder arrays were designed and fabricated,<sup>5</sup> total reflectance spectroscopy showed an average reflectivity of only 1.3% for light in the wavelength of 450–900 nm range. Wang *et al.* investigated the optical properties of Si nanocones arrays with various heights and diameters.<sup>14</sup> They showed that Si nanocones arrays can strongly interact with the incident light and the absorbance, and optical absorption over 95% for light in the wavelength of 300–2000 nm region can be achieved. Lin *et al.* designed the inverted nanopencils,<sup>22</sup> which can reduce the optical reflection below 5% over the 400–1000 nm range and a wide angle of incidence between 0° and 60°. A novel silicon nano-conical-frustum array structure were successfully fabricated by Lu *et al.*, which exhibits the absorbance of ~99% over 400–1100 nm range.<sup>23</sup> In addition, silicon nanosphere on a high-index substrate shows the a narrow-band antireflection properties in the visible spectral range.<sup>20,21</sup> Recently, Ramon *et al.* designed the all-dielectric metasurfaces composed of silicon nanodisks which exhibit a generalized Brewster's effect,<sup>24</sup> *i.e.* a zero of light reflection, at any angle of incidence light, frequency and polarization. These studies demonstrate that proper design of nanostructures is a key factor to improve the optical property, thus the conversion efficiency of solar cells.

Although Si nanoclusters have attracted a lot of theoretical and experimental interests due to their promising light emitting properties, it was shown that the optical properties of Si nanoclusters are strongly influenced by the surface passivation.<sup>25–35</sup> Li *et al.* reported that acrylic acid coated Si nanoclusters have good photo luminescent stability.<sup>31</sup> The molar extinction coefficient of Si nanoclusters is affected significantly by passivated alkyl and amine.<sup>32,33</sup> Oxidized surface of Si

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nanoclusters also affect the optical property, especially red shift phenomenon were observed after Si nanoclusters are exposed to air.<sup>34</sup> Zhou *et al.* studied the influence on luminescence from the hydrogen passivation on Si nanoclusters.<sup>35</sup> They found that blue luminescence can be attributed to strong quantum confinement in hydrogen passivated Si nanoclusters. On the other hand, using carbon cages as costing materials to protect clusters against external interference has been attracted a lot of attentions.<sup>36–41</sup> In particular, carbon cage encapsulating Si, Co, and Fe nanoparticles have been successfully synthesized by experiments, recently.<sup>36–40</sup> It has been shown that the carbon cage encapsulation not only acts as protective layer against cluster oxidation, the hybrid nanostructures formed by the carbon cage and the encapsulated nanoparticles can also exhibit interesting electronic structures and desirable properties for magnetic and battery applications.<sup>36–41</sup>

In the present paper, we propose a new design of Si-based nanostructures, *i.e.*, carbon fullerene coated Si nanoclusters for improving the light absorption efficiency. We show that the hybrid silicon–carbon nanostructures provide an interesting system to study the interplay between the electronic structures of Si clusters and carbon fullerenes and the unique optical properties arisen from such interplay. While pure carbon cages and pure Si clusters exhibit strong optical absorptions at the ultraviolet (UV) or far UV region, the optical spectra of the hybrid silicon–carbon nanostructures have substantial red shift. In particular, we found that assembly of the hybrid silicon–carbon nanostructures exhibit significant the optical absorption in the visible light and infrared regions. Our present study points to a promising direction for the design of high efficiency solar cell nanomaterials.

## Computational method

The hybrid silicon–carbon nanostructures were designed by enclosing silicon clusters into carbon cages, *i.e.*,  $\text{Si}_m@\text{C}_{2n}$ . The structure optimization and total energy calculations were performed within the first-principles density functional theory (DFT) framework by using Gaussian 09 package.<sup>42</sup> The lowest-energy structures of  $\text{Si}_{7-13}$  clusters were taken from ref. 43 and fully optimized at the B3LYP/6-31G(d) level. These structures have been demonstrated to be the ground-state structures of the free-standing  $\text{Si}_{7-13}$  clusters. The binding energy (per atom) and the HOMO–LUMO gaps of these free-standing clusters obtained from our calculations were summarized in Table S1 in the ESI.† The binding energy per atom is defined by  $E_b = [mE(\text{Si}) - E(\text{Si}_m)]/m$ , where  $E(\text{Si}_m)$  and  $E(\text{Si})$  are the energies of  $\text{Si}_m$  cluster and a single Si atom, respectively. It is clearly seen that  $\text{Si}_{10}$  cluster is most stable in the size range of  $m = 7-13$ , which agrees well with those reported in ref. 43. Four fullerenes, *i.e.*,  $\text{C}_{60}$ - $I_h$ ,  $\text{C}_{70}$ - $D_{5h}$ ,  $\text{C}_{76}$ - $D_2$  and  $\text{C}_{84}$ - $D_2$  cages, were chosen for the encapsulation of  $\text{Si}_m$  ( $m = 7-13$ ) clusters. These structures of  $\text{Si}_m@\text{C}_{2n}$  ( $m = 7-13$ ,  $2n = 60, 70, 76$ , and  $84$ ) have been fully relaxed by B3LYP/6-31G(d) calculations. The structures of the Si clusters inside cages have some distortions due to the interaction between the carbon atoms and the cages.

In order to see more clearly the effects on the electronic structures and optical properties from the carbon coating rather than from the distortions of the silicon clusters in the hybrid  $\text{Si}_m@\text{C}_{2n}$  structures, we also studied another type of structures where the Si clusters can maintain their structures inside the cages, although these structures may not be the ground-state structures in their free-standing forms.  $\text{Si}_7@\text{C}_{60}$ - $I_h$  belongs to both two types of structures. The lowest-energy  $\text{Si}_7$  cluster encapsulated into  $\text{C}_{60}$ - $I_h$  can also maintain the pentagonal bipyramid structure although the pentagonal ring was slightly buckled. Similarly,  $\text{Si}_{9-A}@\text{C}_{70}$ - $D_{5h}$ , and  $\text{Si}_{12-A}@\text{C}_{84}$ - $D_2$  discussed below also belong to both two types of structures.

The optical absorption properties of the nanostructures were studied by time-dependent density functional theory (TDDFT) using Gaussian 09 package. The absorption energy is determined by the energy difference between those of the final excited state and the initial occupied state of the electron, and the intensity of the absorption peak is proportional to the oscillator strength between the two states. In the TDDFT theory, the electronic excitations are calculated starting from the Kohn–Sham (KS) orbital and their eigenvalues. Then, electronic excitations were evaluated under the framework of linear response theory.<sup>44</sup> The Becke's three-parameters and Lee–Yang–Parr' gradient-corrected correlation hybrid functional (B3LYP) and 6-31G(d) basis sets were used for optical calculations. The oscillator strength is defined as  $f_{ij} = 4\pi m_e \omega_{ij} |D_{ij}|^2 / 3\hbar e^2$ , where  $m_e$ ,  $\hbar$  and  $e$  are electron mass, Planck constant, and electron charge, respectively,  $\omega_{ij}$  is angular frequency required to excite an electron from state  $i$  to state  $j$ , and  $D_{ij}$  is transition dipole from state  $i$  to  $j$ . The excitation states included in the optical absorption for  $\text{Si}_m$ ,  $\text{C}_{2n}$  and  $\text{Si}_m@\text{C}_{2n}$  are up to 6.2 eV, 5.48 eV and 4.30 eV from the HOMO, respectively.

We have assessed the accuracy of the TDDFT calculation for the optical properties of nanoclusters by comparing the results of optical gaps of the fullerenes from the TDDFT calculation with those from experimental measurement. The optical gaps of  $\text{C}_{60}$ - $I_h$ ,  $\text{C}_{70}$ - $D_{5h}$ ,  $\text{C}_{76}$ - $D_2$  and  $\text{C}_{84}$ - $D_2$  cages from our TDDFT calculations are 2.28, 2.10, 1.08, and 1.44 eV respectively, which are reasonably in good agreement with experimental values of 1.9–2.3 eV, 1.6–1.95 eV, 1.36–1.4 eV, and 1.24 eV respectively.<sup>45–52</sup> After the Si clusters have been inserted inside fullerenes, the HOMO–LUMO gaps of free  $\text{C}_{60}$ - $I_h$  (2.28 eV) and  $\text{C}_{70}$ - $D_{5h}$  (2.10 eV) cages decrease to 1.20 and 0.89–1.99 eV, respectively, and the gaps of free  $\text{C}_{76}$ - $D_2$  (1.08 eV) and  $\text{C}_{84}$ - $D_2$  (1.44 eV) cages change to 1.03–1.29 and 0.88–1.52 eV, respectively.

## Results and discussion

### Structures

The structures of the endohedral fullerene  $\text{Si}_m@\text{C}_{2n}$  ( $m = 7-13$ ,  $2n = 60, 70, 76$  and  $84$ ) after the optimization by DFT calculations are shown in Fig. 1. As one can see from Fig. 1, the fullerene cages are well preserved after the  $\text{Si}_m$  clusters encapsulation, although the shape of the cages has some small distortion. By contrast, the deformation of the  $\text{Si}_m$  clusters upon the encapsulation is more obvious. As shown in Fig. 1, free-standing  $\text{Si}_7$  cluster is a pentagonal bipyramid.  $\text{Si}_7$



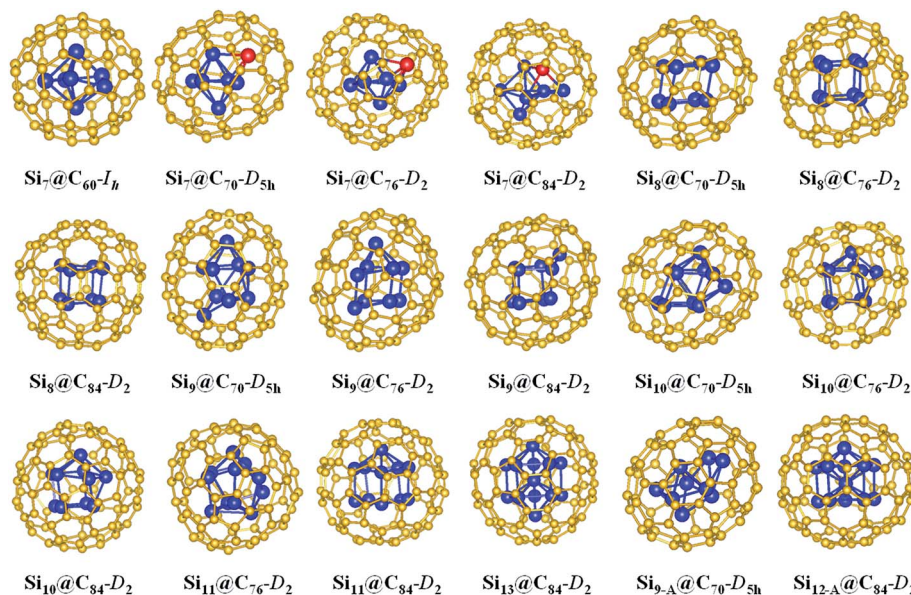


Fig. 1 Structures of hybrid silicon-carbon nanostructures  $\text{Si}_{7-13}@\text{C}_{2n}$  ( $2n = 60, 70, 76$ , and  $84$ ). The Si atoms were denoted by blue and red colors, C atom was denoted yellow color. The structures were optimized using B3LYP/6-31G(d) method.

encapsulated into  $\text{C}_{60}\text{-I}_h$  can still maintain the pentagonal bipyramid structure although the pentagonal ring is slightly buckled. As the size of the fullerene cage increases, more deformation in the encapsulated  $\text{Si}_7$  cluster can be seen. In particular, one of the Si atoms deviates substantially from the pentagonal plane, as indicated by red color in Fig. 1, making the encapsulated  $\text{Si}_7$  transformed into a tetragonal bipyramid structure. The ground-state structures of free-standing  $\text{Si}_8$  and  $\text{Si}_9$  clusters are the derivatives of tetragonal bipyramid and pentagonal bipyramid, respectively, while that of free-standing  $\text{Si}_{10}$  cluster is a tricapped-trigonal-prism (TTP). When these Si clusters are enclosed into the carbon fullerene cages, there are noticeable deformations but the structures inside the carbon cages still resemble those of free-standing clusters. The structures of free-standing  $\text{Si}_{11}$  and  $\text{Si}_{13}$  clusters are also the derivatives from the TTP  $\text{Si}_{10}$ . However, the encapsulated  $\text{Si}_{11}$  cluster transforms into a hollow cage while the  $\text{Si}_{13}$  cluster changes to an icosahedral structure similar to an  $\text{Al}_{13}$  cluster.<sup>53</sup> The ground-state structure of free-standing  $\text{Si}_{12}$  cluster<sup>43</sup> cannot be encapsulated into fullerene cage  $\text{C}_{2n}$  ( $2n = 60, 70, 76$ , and  $84$ ) without substantial deformation due to its prolate shape. Thus we did not consider it in our study.

In addition to the encapsulation of the ground-state free-standing clusters into the carbon cages, we have also searched for other Si clusters that can maintain their free-standing structures inside the cages so that effects of carbon cage can be seen more clearly. Two structures,  $\text{Si}_{9-A}@\text{C}_{70}\text{-D}_{5h}$  and  $\text{Si}_{12-A}@\text{C}_{84}\text{-D}_2$ , from our search are shown in Fig. 1. The structure of  $\text{Si}_7@\text{C}_{60}\text{-I}_h$  shown in Fig. 1 also belongs to this type of structure. As shown in Fig. 1, the  $\text{Si}_{9-A}$  cluster encapsulated by the fullerene cage  $\text{C}_{70}\text{-D}_{5h}$  can be viewed as a pentagonal bipyramid capped by two atoms on the same side, while the free-standing  $\text{Si}_9$  cluster is a pentagonal bipyramid capped by two atoms on both sides. For  $\text{Si}_{12-A}@\text{C}_{84}\text{-D}_2$ , the Si cluster takes an

icosahedral-like structure with one top atom missed from a 13-atom icosahedral cluster, similar to the geometry of the  $\text{Al}_{12}$  cluster,<sup>53</sup> different from the free-standing  $\text{Si}_{12}$  cluster with a prolate shape.

### Electronic properties

To better understand the electronic properties, we analyzed the density of states (DOS) for the free-standing  $\text{Si}_m$  and  $\text{Si}_m@\text{C}_{2n}$  clusters respectively. The electronic DOSs for the free-standing  $\text{Si}_7$  and  $\text{Si}_7@\text{C}_{2n}$  ( $2n = 60, 70, 76$ , and  $84$ ) clusters are shown in Fig. 2 (The DOSs of other free-standing and hybrid clusters are similar). The calculated DOSs were broadened by 0.2 eV using a Gaussian function. The Fermi energy level was set at 0.0 eV. The corresponding molecular energy levels of the nanostructures are also shown in Fig. 2. Compared with the DOS of free-standing  $\text{Si}_7$  cluster, obvious changes were observed in those of  $\text{Si}_7@\text{C}_{2n}$ . In particular, there are many energy levels located close to the Fermi energy level in the  $\text{Si}_7@\text{C}_{2n}$  as compared to that of  $\text{Si}_7$ . The calculation results show that the HOMO-LUMO gaps of  $\text{Si}_7@\text{C}_{60}\text{-I}_h$ ,  $\text{Si}_7@\text{C}_{70}\text{-D}_{5h}$ ,  $\text{Si}_7@\text{C}_{76}\text{-D}_2$  and  $\text{Si}_7@\text{C}_{84}\text{-D}_2$  are 1.10, 0.96, 1.39 and 1.40 eV, respectively, much smaller than the HOMO-LUMO gap of free-standing  $\text{Si}_7$  which is 3.18 eV. The red shift in the optical absorption spectra of the  $\text{Si}_m@\text{C}_{2n}$  cluster can be ascribed to the decrease of the energy gaps.

### Optical properties

The optical absorption spectra of the  $\text{Si}_m$  and  $\text{Si}_m@\text{C}_{2n}$  clusters obtained from the TDDFT calculations are displayed in Fig. 3. The principle excitation energies and oscillator strengths of the free-standing and encapsulated clusters were given in Tables S2 and S3,<sup>†</sup> respectively, where the contributions of orbital-to-orbital transitions of more than 20% were listed.





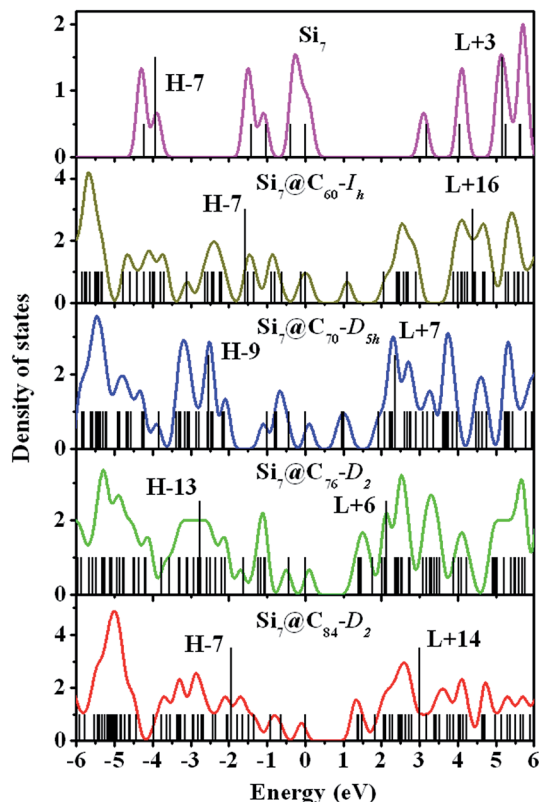


Fig. 2 Comparison of electron density-of-states (DOS) and the corresponding energy levels of  $\text{Si}_7$  and  $\text{Si}_7@\text{C}_{2n}$  ( $2n = 60, 70, 76$ , and  $84$ ).

As shown in Fig. 3, the optical absorption spectra of the  $\text{Si}_m@\text{C}_{2n}$  clusters exhibit a significant red shift in comparison with that of free-standing  $\text{Si}_m$  clusters. Absorptions of the free-standing  $\text{Si}_m$  clusters occur at 6.17–9.97 eV in the ultraviolet range, while those of the  $\text{Si}_m@\text{C}_{2n}$  occur at 1.90–5.34 eV. The structure of free-standing  $\text{Si}_7$  cluster has been well characterized by experiment and theory. As we can see from the insert in Fig. 3(a), the absorption spectrum of free-standing  $\text{Si}_7$  cluster shows a very sharp ultraviolet peak at the energy of 8.14 eV with an oscillation strength  $f = 2.302$ . The main contribution to this peak is from HOMO–7 to LUMO+3 transition. In comparison, the absorption intensity of the  $\text{Si}_7@\text{C}_{2n}$  clusters is reduced by a factor of 30 relative to that of the free-standing  $\text{Si}_7$  cluster. The absorption peaks in the  $\text{Si}_7@\text{C}_{2n}$  clusters is also dependent on the size of the fullerene cages, exhibiting significant red-shift as the size of the fullerene change from  $\text{C}_{60}\text{-I}_h$  to  $\text{C}_{70}\text{-D}_{5h}$ . However, in  $\text{Si}_7@\text{C}_{70}\text{-D}_{5h}$ ,  $\text{Si}_7@\text{C}_{76}\text{-D}_2$  and  $\text{Si}_7@\text{C}_{84}\text{-D}_2$ , their absorption spectra become similar with the strong peak almost at the same energies, which are about 4.33, 4.26 and 4.31 eV, respectively. Some dependence of absorption peaks on the size of fullerene is also seen for other  $\text{Si}_m@\text{C}_{2n}$  nanoparticles. Slight red-shift in the main adsorption peak as the size of the fullerene increase from 70 to 84 can also be seen for  $\text{Si}_8@\text{C}_{2n}$ ,  $\text{Si}_9@\text{C}_{2n}$  and  $\text{Si}_{10}@\text{C}_{2n}$  as shown in Fig. 3(b)–(d).

We have also analyzed the optical properties of  $\text{Si}_7@\text{C}_{60}\text{-I}_h$ ,  $\text{Si}_{9-A}@\text{C}_{70}\text{-D}_{5h}$  and  $\text{Si}_{12-A}@\text{C}_{84}\text{-D}_2$ . We found that in  $\text{Si}_7@\text{C}_{60}\text{-I}_h$ , two relatively sharp peaks at 3.76 eV and at 5.34 eV in the

ultraviolet region, respectively, are primarily contributed from the transitions HOMO–1  $\rightarrow$  LUMO+15 and HOMO–7  $\rightarrow$  LUMO+16. The optical absorption spectrum of  $\text{Si}_{9-A}@\text{C}_{70}\text{-D}_{5h}$  exhibits three peaks at 2.24 eV in the visible light region, and at 3.30 and 4.33 eV in the ultraviolet region, respectively. The absorption peak at 2.24 eV is dominated by the transitions HOMO–1  $\rightarrow$  LUMO+9 and HOMO  $\rightarrow$  LUMO+10, while that at 3.30 eV and 4.33 eV are dominated by the transition HOMO–8  $\rightarrow$  LUMO+10 and HOMO–4  $\rightarrow$  LUMO+19, respectively. The optical absorption spectrum of  $\text{Si}_{12-A}@\text{C}_{84}\text{-D}_2$  is shown in Fig. 3(h). The main absorption peaks is at 4.16 eV in the ultraviolet region, which is dominated by the transition HOMO–18  $\rightarrow$  LUMO+6.

To further understand the optical property, it is worthwhile to analyze main transitions in detail. For example, some main transitions of  $\text{Si}_7$  and  $\text{Si}_7@\text{C}_{2n}$  were marked by the arrows in Fig. 2. The primary absorption peak of the free-standing  $\text{Si}_7$  is from HOMO–7 to LUMO+3 (8.14 eV). In  $\text{Si}_7@\text{C}_{60}\text{-I}_h$ , the strong peak lies at 5.34 eV, which is ascribed to the transition HOMO–7  $\rightarrow$  LUMO+16. In  $\text{Si}_7@\text{C}_{70}\text{-D}_{5h}$ ,  $\text{Si}_7@\text{C}_{76}\text{-D}_2$  and  $\text{Si}_7@\text{C}_{84}\text{-D}_2$ , the strong peaks lie at 4.33, 4.26 and 4.31 eV, respectively, which are ascribed to HOMO–9  $\rightarrow$  LUMO+7, HOMO–13  $\rightarrow$  LUMO+6 and HOMO–7  $\rightarrow$  LUMO+14 transitions, respectively. The main features of optical excitations of  $\text{Si}_m$  and  $\text{Si}_m@\text{C}_{2n}$  ( $m = 8\text{--}13$ ,  $2n = 70, 76$  and  $84$ ) are similar to those of  $\text{Si}_7$  and  $\text{Si}_7@\text{C}_{2n}$  as shown in Fig. 2. These results show that the red shift of optical properties can be ascribed to the decrease of HOMO–LUMO gaps and the increase of the number of energy levels near Fermi level.

### Broadband optical absorption

Electromagnetic radiation from sun spreads over a wide range of continuous spectrum, and the sun radiation intensity is also different for different wavelengths, as shown in the bottom panel of Fig. 4. Most Si-based solar cells are effective only in certain energy range in the solar spectrum due to the narrow-band optical absorption features of the solar cells. In designing more efficient solar cell materials, it is desirable to improve their absorption spectra in conformity with the solar radiation spectrum in the visible light region. For the free-standing  $\text{Si}_m$  clusters, our TDDFT calculation results show that they are not efficient for solar cells because their optical absorptions have narrow peaks at the high-energy ultraviolet region as shown in the top panel of Fig. 4. In the experiment, it is shown that the absorption spectrum of fullerene cage  $\text{C}_{2n}$  also does not appear in the visible light region,<sup>52,54–56</sup> consistent with our calculated results for  $\text{C}_{60}\text{-I}_h$ ,  $\text{C}_{70}\text{-D}_{5h}$ ,  $\text{C}_{76}\text{-D}_2$  and  $\text{C}_{84}\text{-D}_2$  cages as one can see from the top panel of Fig. 4. However, the optical absorption spectra of the hybrid silicon–carbon structures are very different from that of pure silicon or carbon nanostructures. Our present calculation demonstrates that the main optical absorption peaks of  $\text{Si}_m@\text{C}_{2n}$  clusters are between 1.90 to 5.34 eV, which spread over the range of the visible light region. By superposition of all the optical spectra of the  $\text{Si}_m@\text{C}_{2n}$  cluster from the present study as shown in the middle panel of Fig. 4, we can obtain a broadband absorption with the



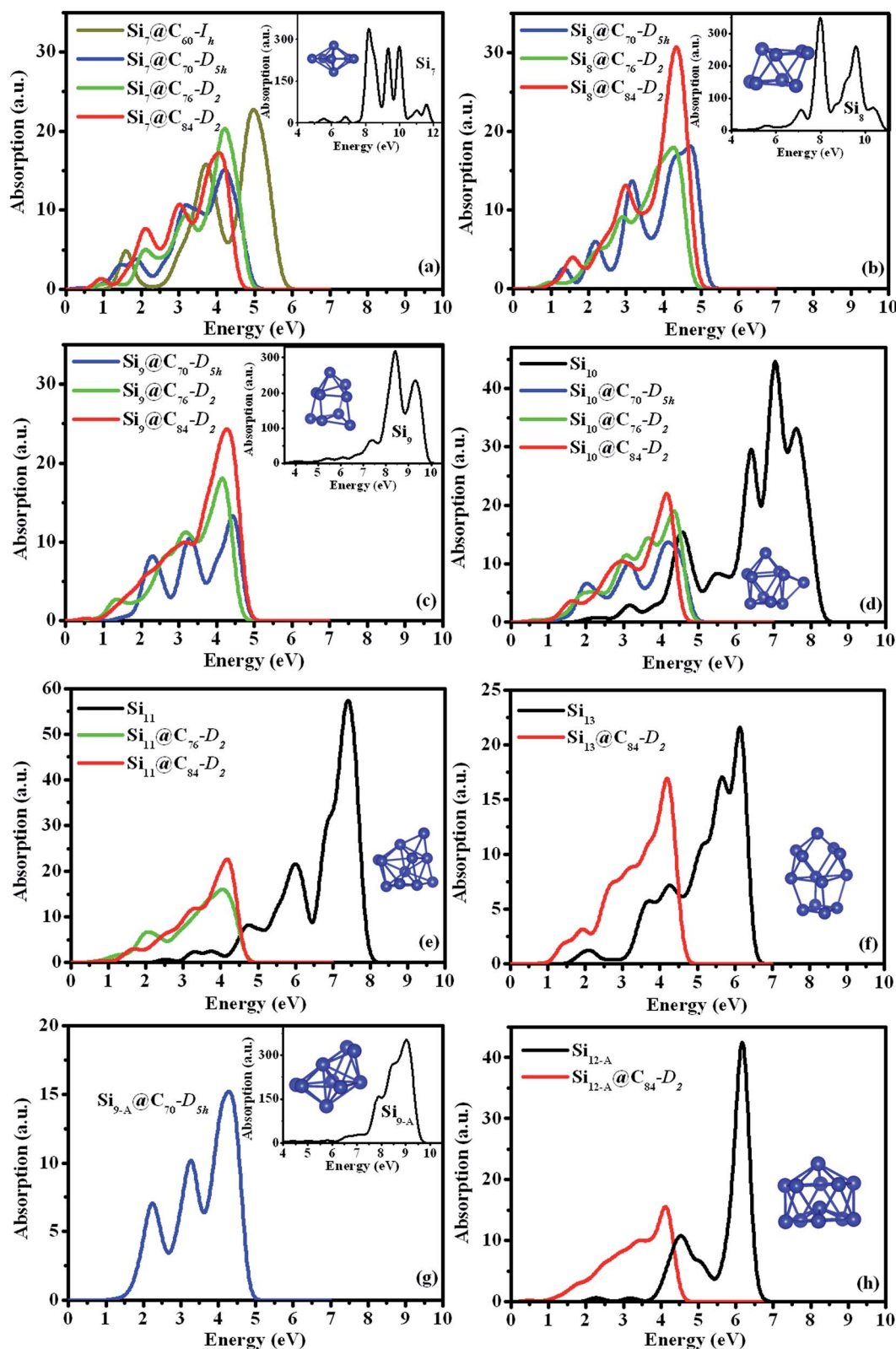


Fig. 3 Optical absorption spectra of free-standing silicon clusters (black lines) compared with those of hybrid silicon-carbon nanostructures  $\text{Si}_{7-13}@\text{C}_{2n}$  ( $2n = 60, 70, 76$ , and  $84$ ) from the TDDFT/B3LYP/6-31G(d) calculations. Substantial red shift in the hybrid structures compared to that of free-standing silicon clusters can be clearly seen.



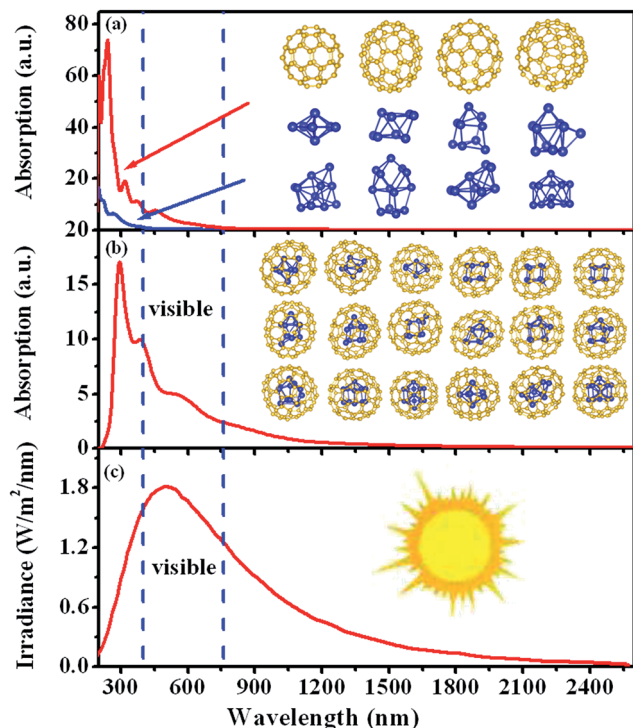


Fig. 4 (a) Superposition of the optical absorption spectra of free-standing  $\text{Si}_{7-13}$  clusters (blue) and that of  $\text{C}_{60} + \text{C}_{70} + \text{C}_{76} + \text{C}_{84}$  cages (red). (b) Superposition of the optical spectra of the assemble of  $\text{Si}_m@C_{2n}$  and the spectrum of solar radiation shown in (c).

intensity extends substantially into the visible light and infrared regions. Therefore, assembled  $\text{Si}_m@C_{2n}$  would provide a new direction for the design of more efficient solar cell nanomaterials.

## Conclusions

In summary, fullerenes  $C_{2n}$  ( $2n = 60, 70, 76$  and  $84$ ) were choose as coating materials, and free-standing  $\text{Si}_m$  ( $m = 7-13$ ) clusters were encapsulated in the hollow cages. Results from the DFT calculations using B3LYP/6-31G(d) show that the ground-state structures of the free-standing  $\text{Si}_m$  clusters exhibit substantial distortion when encapsulated in carbon fullerene cages. The optical properties of  $\text{Si}_m$  and  $\text{Si}_m@C_{2n}$  have been studied by means of TDDFT/B3LYP/6-31G(d). The calculated results show that the optical absorption spectra of  $\text{Si}_m$  occur in UV region, while significant red shifts occur for that of  $\text{Si}_m@C_{2n}$ . We also show that an assembly of  $\text{Si}_m@C_{2n}$  exhibits a broadband optical absorption, which extend to the visible light and infrared regions. This study may provide very useful insight into designing efficient solar cell nanomaterials.

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