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## Plasmon enhanced light absorption in aluminium@Hematite core shell hybrid nanocylinders: the critical role of length

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The light absorption as well as the near field enhancements properties of Al@ $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> core shell hybrid nanocylinders (HNs) have been systematically studied by means of Discrete Dipole Approximation simulations. The Al@ $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> HNs consist of a right circular cylinder Al core, wrapped by a circular section of an  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell, both having the same finite length  $L$ . A general and useful methodology has been implemented to assess separately the partial contributions to the absorption spectrum of each component of the Al@ $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> HN. The employed methodology can be applied not only to those HNs studied here but also to any other nanostructure with arbitrary geometry and several components providing relevant information not accessible through standard spectroscopic techniques. The absorption spectra have been employed to calculate the absorbed photon flux  $\phi$  within the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell. According to the HN size, plasmon enhanced light absorption in the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell of the Al@ $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> HNs is evidenced, which is attributed to a plasmon-induced energy transfer mechanism based on near field enhancements. The effect of the HN length on the absorbed photon flux  $\phi$  is an important issue that has not been addressed yet, as only infinitely long HN has been considered in previous studies. It is demonstrated that the HN length  $L$  has a crucial influence on the absorbed photon flux  $\phi$ , as it is the main structural parameter that allows us to tune the dipole plasmon resonance of the Al core into the visible region. Furthermore, it is shown that Al cores lead to larger  $\phi$  values than the typical plasmonic metals Ag and Au. The results presented in this work point out that the HN length should be explicitly taken into account for an optimum design of core shell hybrid cylindrical nanostructures with enhanced or improved photoactive properties.

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## Introduction

Nanostructures composed of semiconductor metal oxides have attracted great attention during the last few decades due to their applications as photoactive materials capable to transform light energy into electric or chemical energy.<sup>1–3</sup> Although solar radiation is the biggest source for clean, sustainable, abundant and easily accessible light energy, its broad utilization to satisfy the energy demand has been retarded by the high cost and low efficiency of the available photoconversion materials and devices.<sup>4,5</sup> The efficiency of the most widely used semiconductors materials in photocatalytic and photovoltaic devices is limited mainly due to their inability to use visible light and to the fast recombination of photogenerated electron–hole pairs before they migrate to the surface.<sup>6</sup> Among the several strategies implemented to overcome these limitations and to enhance the photoconversion efficiencies, stands out the combination of plasmonic metals and semiconductor metal oxides into single hybrid nanostructures.<sup>7–12</sup> In recent years, progress has been

made in understanding the plasmonic metal–semiconductor interactions, which lead to the identification of at least three different mechanisms that contribute to enhance the photoconversion efficiency: light trapping based on scattering, hot electron/hole transfer and plasmon-induced energy transfer based on near field.<sup>13–16</sup>

Hematite ( $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>) is one of the most thermodynamically stable iron oxides, it is abundant, inexpensive, non-toxic and stable in aqueous environment.<sup>17</sup> Its optical bandgap energy is reported to be between 1.9 and 2.2 eV (corresponding to 650 and 560 nm wavelengths respectively) depending on the sample preparation technique, which results in a theoretical maximum photocurrent density under AM 1.5 G illumination conditions of 12.6 mA cm<sup>–2</sup>, corresponding to a maximum solar to hydrogen (STH) conversion efficiency of about 15%.<sup>18,19</sup> In addition, it has been proposed that its valence band alignment is ideal to catalyze the oxygen evolution reaction.<sup>20</sup> These properties make  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> a promising material for the construction of photoanodes useful for photoelectrochemical water splitting.<sup>21,22</sup> However,  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> photoanodes exhibits low internal quantum efficiency, a feature that has been attributed to their slow water oxidation kinetics and short diffusion length of the photogenerated minority charge carriers (holes),

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resulting in significant losses due to electron/hole recombination.<sup>23</sup> Besides, the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> conduction band edge is lower than the reduction potential of water, therefore a large overpotential is required to drive the hydrogen evolution.<sup>24,25</sup> The incorporation of plasmonic materials in this structures could greatly overcome this shortcoming. Plasmonic metal nanoparticles are recognized for supporting localized surface plasmon resonances (LSPRs), which originate large absorption and scattering cross sections as well as near field enhancements.<sup>26</sup> Gold (Au) and silver (Ag) are the plasmonic metals most widely studied, whereas their nanoparticles have been employed along with photoelectrodes made of  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> in order to increase their STH and photocatalytic activity efficiencies.<sup>27–29</sup> For instance, Ian-dolo *et al.* have measured a considerable improvement of photoactivity under solar simulator illumination of  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> photoanodes functionalized with Au nanodisk, comparing reference samples consisting of bare  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>, an issue attributed to the plasmonic activity of Au nanodisks deposited on the electrode surface.<sup>30</sup> More recently, Archana *et al.* have reported enhanced photoelectrochemical performance of a smooth chemical vapor deposited  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> film embedded with Au nanoparticles.<sup>31</sup> These authors obtained about 3 times higher light absorption and photocurrent enhancement from thin  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> films containing Au nanoparticles than with pristine  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> films. Moreover, it has been proposed aluminium (Al) as an alternative plasmonic material, which exhibits plasmon resonances from the UV to the visible regions of the spectrum and extends the optically tunable range of plasmonic nanostructures beyond that of Au and Ag.<sup>32,33</sup> Some of the attractive features of Al include its low cost, high natural abundance<sup>34</sup> and compatibility with complementary metal–oxide–semiconductor (CMOS) technology,<sup>35</sup> whereas its plasmonics applications comprise optical antennas<sup>36</sup> and plasmon-enhanced spectroscopy,<sup>37</sup> among others. Therefore, bringing together these materials, that is,  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> and Al, into a single hybrid nanostructure provides a reasonable strategy to design materials with enhanced photoactivity taking advantage of the properties of their individual components in a synergic way as well as to expand our current understanding on the plasmonic metal–semiconductors interactions.

The nanowire geometry is particularly relevant due to its excellent charge extraction and large absorption cross sections.<sup>38</sup> Moreover, this geometry allow us to use Mie-formalism to obtain rigorous solutions to Maxwell's equations.<sup>39</sup> In this respect, the absorption properties of infinitely long core shell hybrid nanowires of different compositions have been theoretically investigated by several authors in order to determine the conditions that lead to photoactive materials with a strongly enhanced (solar) light absorption, and consequently to an improved STH efficiency.<sup>40–43</sup> Importantly, convenient methodologies to calculate separately the contributions to absorption from the different components of the hybrid nanowires, that is, the core and the shell, have been applied in these studies. For instance, Mann *et al.* have shown extreme light absorption in amorphous silicon thin films wrapped around silver nanowires, and suggested that metal nanowires with semiconductor shells might be ideal building blocks for

photovoltaic and solar fuel.<sup>44</sup> Recently, studies on the optical properties of infinite right circular cylindrical core–multishell hybrid nanostructures with several different compositions ( $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>–Al, Si– $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>–Al,  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>–Ag, Si– $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>–Ag, among others) have been reported.<sup>45</sup> In that work it has been shown that Al could be an excellent alternative plasmonic material to precious metals in core–multishell hybrid nanostructures with infinite length. In addition, it has been found that the maximum photocurrent density, calculated assuming ideal conditions, within the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell of a Si(40 nm diameter)–Al(50 nm) $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>(40 nm) nanowire reaches approximately 11.8 mA cm<sup>−2</sup> (*i.e.*, STH efficiency of 14.5%), whereas the absorption efficiency within the 40 nm  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell is about 93% of the theoretical maximum for bulk  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>.<sup>46</sup>

In this work, we have studied the absorption as well as the near field enhancement properties of Al@ $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> core shell hybrid nanocylinders (HNs) by means of systematic Discrete Dipole Approximation (DDA) simulations.<sup>47–50</sup> The Al@ $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> HNs consist of a right circular cylinder Al core, wrapped by a circular section  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell, both having the same finite length  $L$ . In order to perform this study a useful modification on the freely available DDSCAT 7.3 code<sup>51</sup> has been implemented, that allow us to examine separately the absorption spectrum of each component of the Al@ $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> HN. This strategy implemented in this work, has the important feature to be general and that can be applied not only to those HNs studied here but also to any other nanostructure with arbitrary geometry and several components. In addition, it gives information not available by means of standard experimental techniques. The geometrical parameters of the HNs have been varied systematically in a broad range, whereas the absorption spectra obtained have been used to calculate the absorbed photon flux within the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell  $\phi$ . Note that  $\phi$  is a relevant quantity as it greatly determines the photoconversion efficiency of photoelectrochemical cells.<sup>19</sup> It is shown that the length of the HNs has a crucial influence on  $\phi$ , as by tailoring the former it is possible to switch between size regimes where  $\phi$  can be either enhanced or suppressed. Moreover, the performance of Al as core material is compared with that of the typical plasmonics metals Ag and Au. It is important to note that this work aims to investigate the conditions that improve light absorption in the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell, whereas issues related with phenomena subsequent to light absorption (kinetics of chemical reactions, diffusion length of charge carriers, overpotential requirements) are not addressed. To the best of our knowledge, the effect of the length of the HN on  $\phi$  is an issue that has not been addressed yet, as only *infinitely* long HN has been previously considered. Thus, the present work aim to demonstrate that the HN length should be explicitly taken into account in the design of core–shell hybrid cylindrical nanostructures with improved photoactive properties.

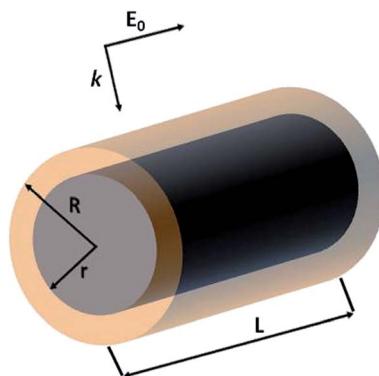
## Theoretical methods

The optical properties of Al@ $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> HNs as well as of  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shells with empty internal cavity were simulated using the DDSCAT 7.3 code, which implements the DDA method.<sup>51</sup>



Detailed reports about this approximation can be found elsewhere.<sup>47–50</sup> In this method, the nanostructure under study is represented by a cubic array of  $N$  dipoles at positions  $r_i$  with dipole polarizabilities  $\alpha_i$ . As there are no restrictions in the way to locate the dipoles within the cubic array, it is possible to simulate the optical properties of arbitrarily shaped nanostructures. The dipole polarizability  $\alpha_i$  value assigned to each dipole at position  $r_i$  is determined based on the dielectric constant of the composition material at position  $r_i$ , which is introduced externally as input, and the lattice dispersion relation.<sup>52</sup> In this work, the wavelength dependent complex dielectric constant of  $\alpha\text{-Fe}_2\text{O}_3$  and Al were obtained from ref. 53 and 54, respectively. Therefore, the method is able to simulate the optical properties of nanostructures with domains having different compositions. Probably, the above mentioned features constitute the most relevant characteristic of this powerful and versatile methodology able to simulate far and near field optical properties. It is important to note that the number of dipoles  $N$  used to represent a given nanostructure is a key parameter, as both the accuracy of the simulation and the computational time, increase with  $N$ . Thus,  $N$  should be chosen in such a way as to reach acceptable error tolerance. All the simulations have been performed using a lattice spacing (inter dipole distance) of 1.5 nm and  $N$  was varied from  $1 \times 10^5$  to  $3 \times 10^6$  according to the nanostructure dimensions. The length  $L$  of the cylindrical nanostructures, the external radius  $R$  and the internal radius  $r$  has been varied in the range 50–500 nm, 50–80 nm and 30–50 nm, respectively. Besides, all the nanostructures studied were located in vacuum, therefore we set the refractive index of ambient medium equal to 1. The core shell HNs, along with its geometrical parameters  $L$ ,  $R$  and  $r$ , are graphically depicted in Scheme 1, along with the orientations of the electric field  $E_0$  and wave vector  $k$  of the incident light relative to the HN. In all the computations,  $E_0$  is parallel whereas  $k$  is perpendicular to the major axis of the HN.

In order to obtain the absorption efficiency  $Q_{\text{abs},i}$  for each component  $i$  of the HN, that is, the Al core and the  $\alpha\text{-Fe}_2\text{O}_3$  shell,



**Scheme 1** Graphical representation of the  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  core shell hybrid nanocylinders studied in this work, along with their geometrical parameters: length  $L$ , internal and external radius of the  $\alpha\text{-Fe}_2\text{O}_3$  shell  $r$  and  $R$ , respectively. The Al core has also a radius  $r$ , while both components have the same length  $L$ . The orientations of the electric field  $E_0$  and wave vector  $k$  of the incident light are also shown.

the electric field values calculated at each dipole position  $r_i$ ,  $|E(r_i)|$ , were used into the following expression:<sup>19</sup>

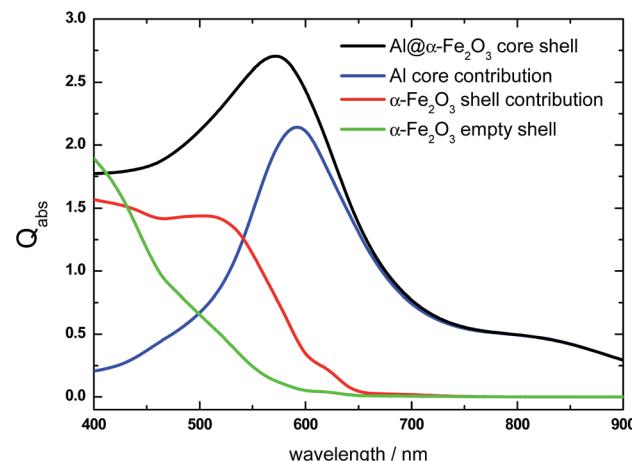
$$Q_{\text{abs},i} = \frac{\mathbf{k} \text{Im}(\varepsilon(\lambda))}{C_{\text{geom}} |E_0|^2} \int_{V_i} |E(r_i)|^2 dr, \quad (1)$$

where  $\text{Im}(\varepsilon(\lambda))$  is the value of the wavelength  $\lambda$  dependent imaginary part of the dielectric constant of the material at position  $r_i$ , and  $C_{\text{geom}}$  is the projected area of the HN perpendicular to  $\mathbf{k}$ . The integral is performed over the volume  $V_i$  occupied by material  $i$ , that is, by the Al core or the  $\alpha\text{-Fe}_2\text{O}_3$  shell, for each wavelength of interest. Therefore, the partial contribution of each component of the HN structure could be computed in the presence of the other component material. In all cases it has been checked that the sum of both contributions equals the total absorption efficiency of the  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  core shell HN, so that the relation  $Q_{\text{abs}} = Q_{\text{abs},\text{Al}} + Q_{\text{abs},\alpha\text{-Fe}_2\text{O}_3}$  is fulfilled.

## Results and discussion

### Contributions to $Q_{\text{abs}}$ from each component of the core shell hybrid nanocylinder

We will first examine the relative contribution to the absorption efficiency  $Q_{\text{abs}}$  from either the core or the shell component of two HNs with different length as typical examples to have a physical insight of the changes induced in  $Q_{\text{abs}}$  due to a change in the HN size. The  $Q_{\text{abs}}$  spectrum of a  $L = 100$  nm,  $R = 70$  nm,  $r = 50$  nm  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN is shown in Fig. 1 (black curve). It can be appreciated that its main feature is an asymmetric absorption peak centered at  $\lambda = 570$  nm, where the  $Q_{\text{abs}}$  values decrease more rapidly for long than for short wavelengths. As mentioned above, the  $Q_{\text{abs}}$  spectrum of HNs can be thought as the result of the contributions from each one of its constituent materials, that is, the core and shell components,



**Fig. 1** Absorption efficiency  $Q_{\text{abs}}$  spectrum of a  $L = 100$  nm,  $R = 70$  nm,  $r = 50$  nm  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN (black curve), along with its respective contributions from the Al core (blue curve) and the  $\alpha\text{-Fe}_2\text{O}_3$  shell (red curve). For comparison, the  $Q_{\text{abs}}$  spectrum of a  $L = 100$  nm,  $R = 70$  nm,  $r = 50$  nm  $\alpha\text{-Fe}_2\text{O}_3$  shell with empty internal cavity it is also shown (green curve).



respectively. The absorption spectrum of the Al cylindrical core ( $L = 100$  nm,  $r = 50$  nm) is characterized by an absorption peak at  $\lambda = 600$  nm, which is attributed to the dipole LSPR (blue curve). On the one hand, it is known that due to its dielectric properties, Al nanoparticles exhibits LSPR in the UV region.<sup>55-57</sup> However, the large redshift of the LSPR found in this case is a consequence of the relatively large size of the Al core as well as of the high refractive index local environment provided by the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell.<sup>58,59</sup>

On the other hand, the absorption contribution of the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell is significant in the range  $400 \text{ nm} < \lambda < 650 \text{ nm}$  (red curve). It resembles the typical absorption spectra of pure  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> and explains the asymmetry of the overall absorption peak.<sup>60,61</sup> In addition, note that for  $\lambda > 650$  nm, the Al core absorption overlaps with the overall absorption spectrum, indicating that the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell absorption is negligible for such  $\lambda$  values. The absorption spectrum of the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell with empty internal cavity and same dimensions ( $L = 100$  nm,  $R = 70$  nm,  $r = 50$  nm) is also shown in Fig. 1 for comparison purposes (green curve). The  $Q_{\text{abs}}$  values of the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell with empty internal cavity noticeably decrease in contrast with the  $Q_{\text{abs}}$  values obtained for the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell with its internal cavity occupied by the Al core, that is, when it constitutes the HN. This enhanced light absorption effect experienced by the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell is attributed to a plasmon-induced energy transfer mechanism, that is, to the near field enhancement generated by the excitation of the dipole LSPR in the Al core, as it will be further analyzed below. As it is becoming evident, the decomposition of the  $Q_{\text{abs}}$  spectrum into their respective contributions constitutes a useful theoretical tool to investigate the optical properties of nanostructures with domains having different compositions. Particularly for Al@ $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> HNs, it allows us to achieve a greater comprehension on the phenomena involved and somehow hidden in the overall absorption spectrum.

The near field enhancement at several incident wavelengths has also been calculated for both the HN as well as for the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell with empty internal cavity to further understand the observed difference between the respective  $Q_{\text{abs}}$  values. Fig. 2 shows 2D plots of the near field enhancement ( $|E|^2/|E_0|^2$ ) on a plane that contains the  $E_0$  and  $k$  vectors and cuts the HN (panels a-d) or the shell with empty internal cavity (panels e-h) in two halves (see Scheme 1).

The same color scale has been used in all panels. The central part of panels a-d represents the Al core, while the lateral bars correspond to the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell. Panels a-c show that the electric field values generated within the oxide shell increase as the incident wavelength is increased from 460 to 600 nm, as a result of the excitation of the dipole LSPR in the Al core (see Fig. 1, blue curve). Note that for  $\lambda = 860$  nm (panel d), which for this structure represents an off resonance wavelength, the electric field enhancement generated within the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell is lower than for the shorter wavelengths. Panels e-h (Fig. 2) show 2D plots of the near field enhancement in the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell with empty internal cavity, the calculations show that these values are considerably smaller than those obtained for the case of the HN. These results clearly indicates that the near field enhancement within the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell arises as a consequence of the dipole LSPR excitation produced by the Al core placed inside it.

According to eqn (1), the  $Q_{\text{abs}}$  value at a given incident wavelength is determined by the electric field values,  $|E(r_i)|$ , as well as by the value of the imaginary part of the dielectric constant for such wavelength  $\text{Im}(\epsilon(\lambda))$ . Based on this expression, it is possible to interpret the dependence of  $Q_{\text{abs}}$  of the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell in the HN with the incident wavelength, but also to make comparisons with the empty  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell. The variations of the bulk  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> dielectric constant with  $\lambda$  is shown in Fig. 3.<sup>53</sup>

The imaginary part of the dielectric constant,  $\text{Im}(\epsilon(\lambda))$ , decreases as the wavelength is increased from 400 to 650 nm, being negligible for larger wavelengths. This trend should be taken into account along with the electric field values, in order to rationalize the variation of the  $Q_{\text{abs}}$  values with the incident wavelength. Apart from a proportionality factor, the  $Q_{\text{abs}}$  spectrum for the empty  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell (green curve, Fig. 1) follows nearly the same dependence with  $\lambda$  than the  $\text{Im}(\epsilon(\lambda))$  of  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub>. This observation indicates that the electric field in the empty  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell has approximately the same value whatever the incident wavelength, in agreement with panels e-h shown in Fig. 2. On the other hand, considering that for a given wavelength  $\text{Im}(\epsilon(\lambda))$  of  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> has the same value irrespective the Al core is inside it or not, the larger  $Q_{\text{abs}}$  values for the  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell when it wraps the Al core (red curve, Fig. 1) in comparison with the empty  $\alpha$ -Fe<sub>2</sub>O<sub>3</sub> shell (green curve, Fig. 1), is attributed to the larger electric field within it (panels a-d, Fig. 2), which in

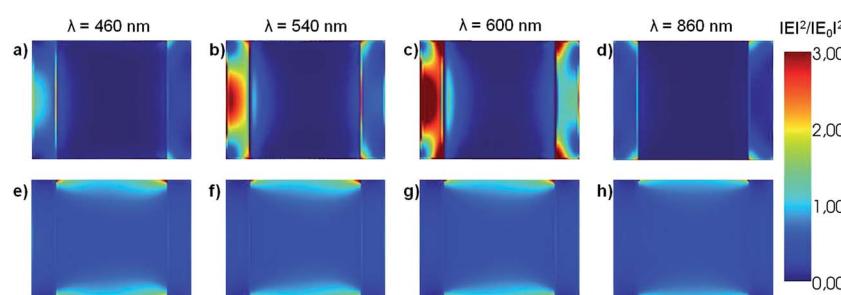


Fig. 2 2D plots of the near field enhancement ( $|E|^2/|E_0|^2$ ) on a plane that contains the  $E_0$  and  $k$  vectors and cuts the HN (panels a-d) or the shell with empty internal cavity (e-h) in two halves. Both nanostructures have the same dimensions ( $L = 100$  nm,  $R = 70$  nm,  $r = 50$  nm). The incident wavelength is indicated above each panel.

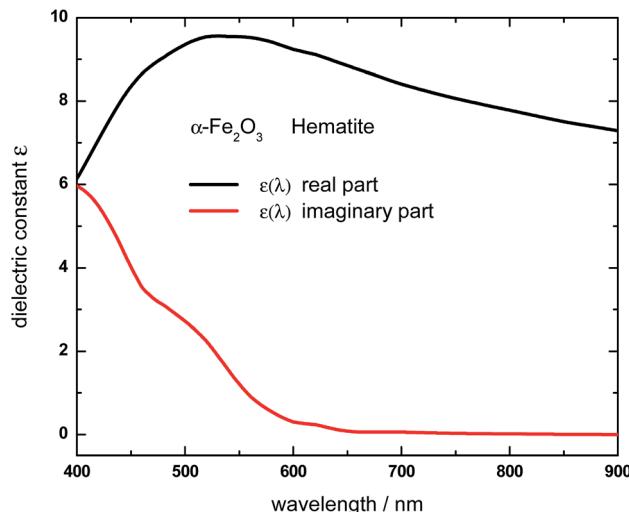


Fig. 3 Real (black curve) and imaginary (red curve) part of the wavelength-dependent dielectric constant of Hematite ( $\alpha\text{-Fe}_2\text{O}_3$ ). Data were obtained based on the complex refractive index values reported in ref. 53.

turn is associated to the excitation of the dipole LSPR. These results explicitly show the essence of the plasmon enhanced light absorption in  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HNs. Note that, even  $\text{Im}(\epsilon(\lambda))$  of  $\alpha\text{-Fe}_2\text{O}_3$  is quite small for  $\lambda$  around 600 nm, the  $Q_{\text{abs}}$  values for the HN case are significant, due to the fact that at this wavelength the plasmon excitation is on resonance (panel c Fig. 2), leading to the largest electric field enhancement within the shell. This result constitutes a clear example where the dipole moment of the LSPR, spectrally located near to the band edge of a semiconductor material, can be used to extend the effective absorption range of the latter.

Let us now analyze another representative HN. It is well known that the LSPR redshifts by increasing the aspect ratio of the nanocylinder.<sup>62,63</sup> Therefore, by increasing the nanocylinder length, keeping its radius constant, should significantly modify the absorption spectrum. Fig. 4 shows the  $Q_{\text{abs}}$  spectrum of a longer  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN ( $L = 200$  nm,  $R = 70$  nm,  $r = 50$  nm) (black curve) than that shown in the previous example along with the contributions from the Al core and the  $\alpha\text{-Fe}_2\text{O}_3$  shell. The overall spectrum shows important differences with respect to that analyzed previously for a shorter HN (black curve, Fig. 1) particularly a noticeable redshift of the absorption peak. The Al core absorption contribution presents a broad absorption peak centered at  $\lambda = 850$  nm which is assigned to the dipole LSPR excitation that overlaps with the total  $Q_{\text{abs}}$  spectrum for  $\lambda > 650$  nm (blue curve, Fig. 4). It is also important to note that the almost 250 nm redshift of the dipole LSPR by increasing 100 nm the nanocylinder length is also favored by the high dielectric constant of the local environment and the contribution to absorption from the  $\alpha\text{-Fe}_2\text{O}_3$  shell is relevant for  $\lambda < 650$  nm (red curve, Fig. 4). Another feature to be remarked is that the  $Q_{\text{abs}}$  values for the  $L = 200$  nm  $\alpha\text{-Fe}_2\text{O}_3$  shell are significantly smaller than the respective values for the  $L = 100$  nm shell (Fig. 1, red curve). At first glance, this effect is directly related with the redshift of the dipole LSPR toward  $\lambda > 650$  nm, where the  $\alpha\text{-Fe}_2\text{O}_3$  shell material does not absorb light. In addition, the  $Q_{\text{abs}}$  values of the  $\alpha\text{-Fe}_2\text{O}_3$  shell in the HN are smaller than the respective values of the  $\alpha\text{-Fe}_2\text{O}_3$  shell with empty internal cavity (green curve, Fig. 4).

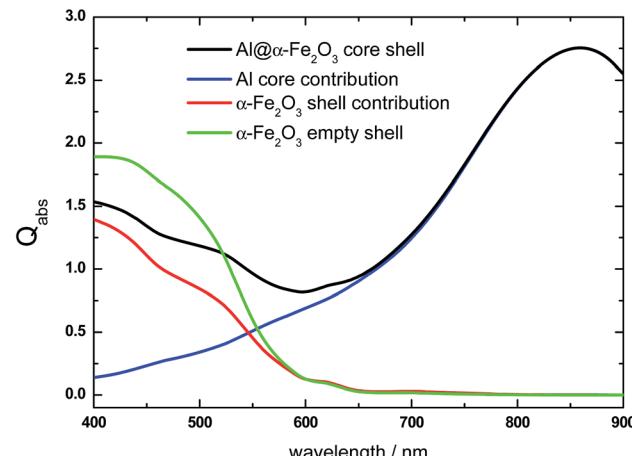


Fig. 4 Absorption efficiency  $Q_{\text{abs}}$  spectrum of a  $L = 200$  nm,  $R = 70$  nm,  $r = 50$  nm  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN (black curve), along with its respective contributions from the Al core (blue curve) and the  $\alpha\text{-Fe}_2\text{O}_3$  shell (red curve). For comparison, the  $Q_{\text{abs}}$  spectrum of a  $L = 200$  nm,  $R = 70$  nm,  $r = 50$  nm  $\alpha\text{-Fe}_2\text{O}_3$  shell with empty internal cavity it is also shown (green curve).

According to eqn (1), for a given incident wavelength, this difference should be attributed to the differences in the respective  $|E(r_i)|^2$ . Fig. 5 shows 2D plots of the near field enhancement ( $|E|^2/|E_0|^2$ ) on a plane that contains the  $E_0$  and  $k$  vectors and cuts the ( $L = 200$  nm,  $R = 70$  nm,  $r = 50$  nm) HN (panels a-d) or the  $\alpha\text{-Fe}_2\text{O}_3$  shell with empty internal cavity (panels e-h) in two halves (see Scheme 1), for several incident wavelengths. It can be observed that for  $\lambda = 460$  and  $\lambda = 540$  nm, the  $|E|^2/|E_0|^2$  values for the  $\alpha\text{-Fe}_2\text{O}_3$  shell in the HN (panels a and b, respectively, Fig. 5) are in general smaller than those for the  $\alpha\text{-Fe}_2\text{O}_3$  shell with empty internal cavity (panels e and f, respectively, Fig. 5), while for  $\lambda = 600$  nm the  $|E|^2/|E_0|^2$  values are almost similar for the  $\alpha\text{-Fe}_2\text{O}_3$  shell filled with Al (panel c, Fig. 5) or empty (panel g, Fig. 5). These observations explain the differences between the  $Q_{\text{abs}}$  spectrum for the  $\alpha\text{-Fe}_2\text{O}_3$  shell in the HN and the spectrum corresponding to the  $\alpha\text{-Fe}_2\text{O}_3$  shell with empty internal cavity, in the spectral region  $\lambda \leq 600$  nm (see Fig. 4, red and green curves respectively). For an incident  $\lambda = 860$  nm, the dipole LSPR is on resonance in the HN and produce large  $|E|^2/|E_0|^2$  values in the  $\alpha\text{-Fe}_2\text{O}_3$  shell (panel d, Fig. 5), in clear contrast with the empty shell case (panel h, Fig. 5).

However, although the near field enhancement is relatively high in the HN, the value of  $\text{Im}(\epsilon(\lambda = 860 \text{ nm}))$  is almost negligible, and consequently  $Q_{\text{abs}}$  is practically zero. This analysis clearly shows the possibility to modulate the plasmon enhanced light absorption effect in  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HNs by controlling the size of the nanostructure. Therefore, regarding light harvesting applications of this type of nanostructured materials, it is relevant to determine the set of  $L$ ,  $R$  and  $r$  values that give place to the largest light absorption within the  $\alpha\text{-Fe}_2\text{O}_3$  shell.



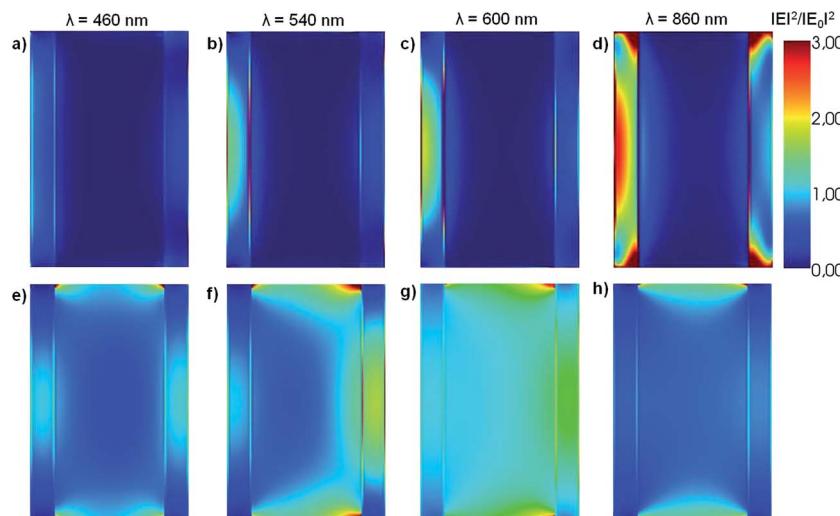


Fig. 5 2D plots of the near field enhancement ( $|E|^2/|E_0|^2$ ) on a plane that contains the  $E_0$  and  $k$  vectors and cuts the HN (panels a–d) or the shell with empty internal cavity (e–h) in two halves. Both nanostructures have the same dimensions ( $L = 200$  nm,  $R = 70$  nm,  $r = 50$  nm). The incident wavelength is indicated above each panel.

### Dependence of $Q_{\text{abs}}$ on the geometrical parameters $L$ , $R$ and $r$

Fig. 6 shows the effect of varying the length  $L$ , keeping fixed the  $R$  and  $r$  values, on the  $Q_{\text{abs}}$  spectrum of the  $\alpha\text{-Fe}_2\text{O}_3$  shell, when it constitutes a  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN. Fig. 6a shows this effect for  $\alpha\text{-Fe}_2\text{O}_3$  shells with fixed  $R$  and  $r$  values at 70 and 50 nm, respectively. An increase of  $L$  from 50 to 100 nm gives rise to a marked increase of  $Q_{\text{abs}}$ , whereas as  $L$  is further increased from 100 to 300 nm  $Q_{\text{abs}}$  decreases. Changing significantly  $R$  and  $r$  to 60 and 40 nm, respectively, produces similar variations in the  $Q_{\text{abs}}$  spectrum of the  $\alpha\text{-Fe}_2\text{O}_3$  shell (Fig. 6b).  $Q_{\text{abs}}$  increases as  $L$  is increased from 50 to 100 nm, and then decreases as  $L$  is further increased from 100 to 300 nm. The same trends are qualitatively observed for the  $\alpha\text{-Fe}_2\text{O}_3$  shell absorption in the  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN with  $R = 50$  nm and  $r = 30$  nm (Fig. 6c). These variations are a consequence of the plasmon enhanced light absorption effect, which in turn is directly associated to the spectral position of the plasmon resonance in the Al core. As the length of the HN is increased from 50 nm to 100 nm, the plasmon resonance wavelength red-shifts gradually from 400 nm to 650 nm, which, in turn, produces an increase in the  $|E|^2$  values within the  $\alpha\text{-Fe}_2\text{O}_3$  shell. According to eqn (1), this phenomenon leads to an increase in the  $Q_{\text{abs}}$  values of the  $\alpha\text{-Fe}_2\text{O}_3$  shell. Note that in the range  $400 \text{ nm} < \lambda < 650 \text{ nm}$ , the  $\text{Im}(\epsilon(\lambda))$  values of  $\alpha\text{-Fe}_2\text{O}_3$  are significantly larger than zero (see Fig. 3, red curve). By increasing the HN length beyond 100 nm, the plasmon resonance wavelength red-shifts toward values larger than 650 nm. As a consequence, enhanced  $|E|^2$  values within the  $\alpha\text{-Fe}_2\text{O}_3$  shell are produced for  $\lambda > 650$  nm. However, in this wavelength range, the  $\text{Im}(\epsilon(\lambda))$  of  $\alpha\text{-Fe}_2\text{O}_3 \rightarrow 0$ . Therefore, according to eqn (1), the enhanced  $|E|^2$  values do not contribute to increase the  $Q_{\text{abs}}$  values of the  $\alpha\text{-Fe}_2\text{O}_3$  shell. These results clearly show that, within the range of  $R$  and  $r$  values studied, the larger absorption efficiencies for the  $\alpha\text{-Fe}_2\text{O}_3$  shell is achieved for  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HNs with lengths  $L$  around 100 nm.

### Absorbed photon flux in the $\alpha\text{-Fe}_2\text{O}_3$ shell

Photoelectrochemical cells employing photoelectrodes made of  $\alpha\text{-Fe}_2\text{O}_3$  offer an inexpensive and clean route for the production of hydrogen from water.<sup>21–24</sup> In order to evaluate the effectiveness of  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN as component of devices based on light harvesting, for instance as photoelectrodes for water splitting, we have used the  $Q_{\text{abs}}$  spectra obtained based on DDA simulations to calculate the absorbed photon flux  $\phi$  within the  $\alpha\text{-Fe}_2\text{O}_3$  shell according to the following expression:<sup>19</sup>

$$\phi = \int_{\lambda=400 \text{ nm}}^{\lambda=900 \text{ nm}} I(\lambda) Q_{\text{abs}}(\lambda) d\lambda, \quad (2)$$

where the incident spectral photon flux  $I(\lambda)$  is given by  $I(\lambda) = \lambda I_{\text{AM1.5G}}/hc$ ,  $I_{\text{AM1.5G}}$  is the solar spectrum at AM1.5 G conditions,  $h$  is Planck's constant and  $c$  is the speed of light in vacuum. Fig. 7 shows the dependence of the absorbed photon flux  $\phi$  (obtained via eqn (2)) on the length  $L$  of both the  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN (solid lines) as well as of the  $\alpha\text{-Fe}_2\text{O}_3$  shell with empty cavity (dashed lines). Note that the results shown correspond to HNs with several different combinations of external  $R$  and internal  $r$  radius values, as indicated in the respective insets. The results presented in Fig. 7a–c correspond to nanostructures with  $\alpha\text{-Fe}_2\text{O}_3$  shell thicknesses  $S = R - r$  of 10, 20 and 30 nm, respectively. The set of results in Fig. 7 for both the  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HNs and the  $\alpha\text{-Fe}_2\text{O}_3$  shells with empty internal cavity follow qualitatively the same trend, whereas quantitative differences can also be clearly appreciated. In general, as the length  $L$  of the  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN is increased, the absorbed photon flux  $\phi$  increases up to a maximum value for  $L \approx 90$  nm, then decreases and finally goes to an asymptotic value as  $L$  is further increased ( $L \rightarrow 500$  nm). The asymptotic  $\phi$  value depends mainly on the  $\alpha\text{-Fe}_2\text{O}_3$  shell thickness  $S$ . In fact, the asymptotic  $\phi$  varies almost linearly with  $S$ , given that it increases roughly from  $3 \times 10^{16}$  to  $8 \times 10^{16}$  photons per  $\text{cm}^2$  per s when  $S$  increases from 10 to 30 nm. In addition, the maximum of  $\phi$ ,  $\phi_{\text{max}}$ , emerges as an



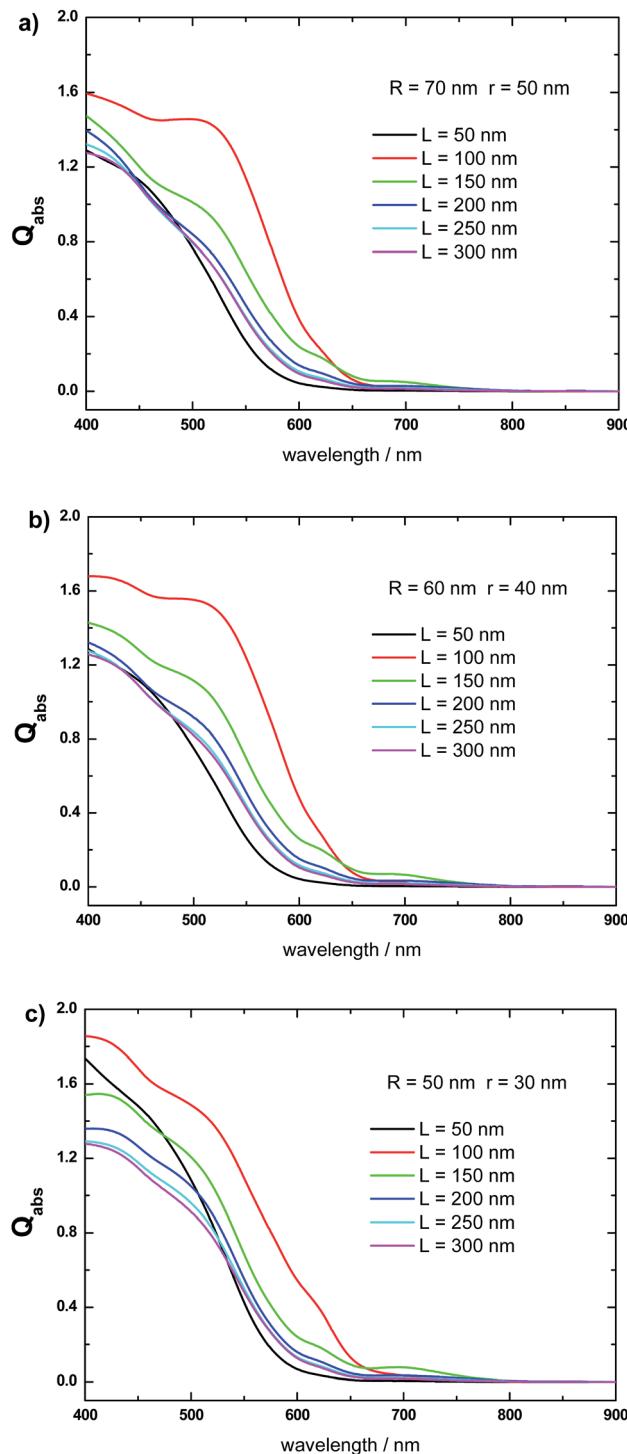


Fig. 6 Effect of the  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN length  $L$  on the absorption efficiency  $Q_{\text{abs}}$  spectrum of the  $\alpha\text{-Fe}_2\text{O}_3$  shell, for different values of its external and internal radius,  $R$  and  $r$ , respectively. (a)  $R = 70$  nm and  $r = 50$  nm. (b)  $R = 60$  nm and  $r = 40$  nm. (c)  $R = 50$  nm and  $r = 30$  nm.

important quantity which might be thought as a figure of merit to address the capability of these HNs in light harvesting devices.  $\phi_{\text{max}}$  does not show a clear trend with  $S$ , and seems to depend on the individual  $R$  and  $r$  values instead on their difference ( $S = R - r$ ). However, it can be noted that the highest

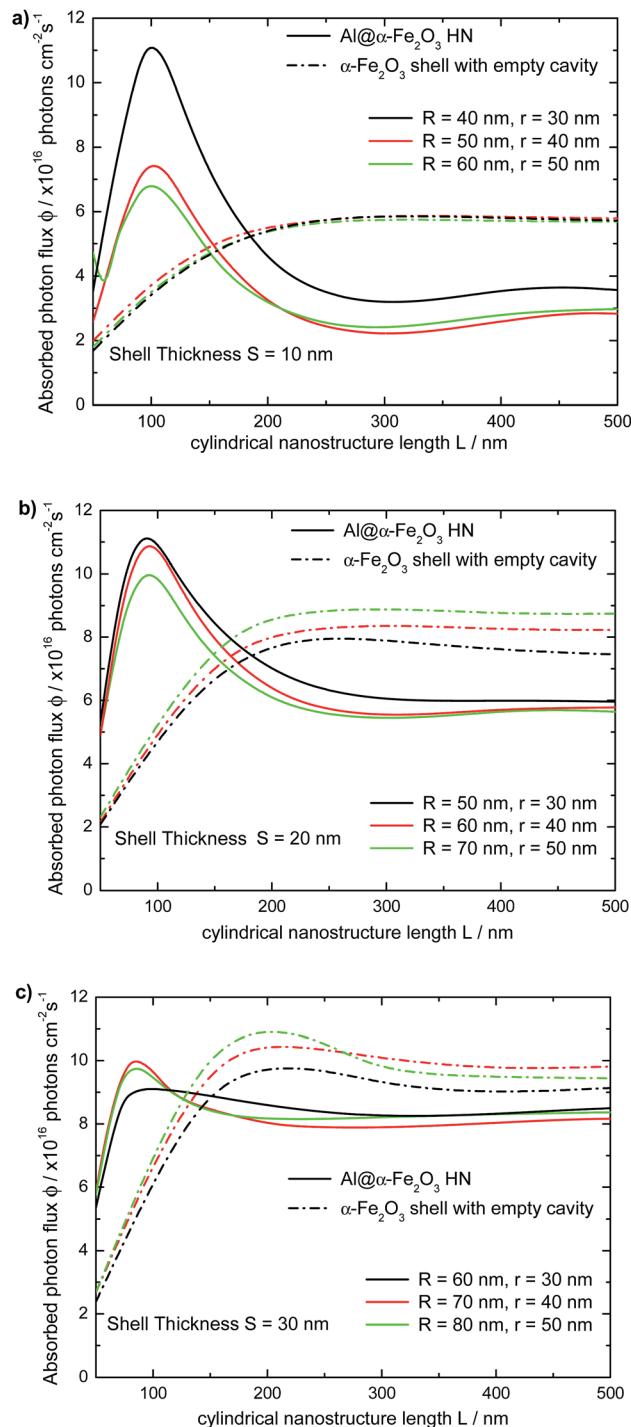


Fig. 7 Dependence of the absorbed photon flux  $\phi$  within the  $\alpha\text{-Fe}_2\text{O}_3$  shell on the length  $L$  of the  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN, for several external and internal radius,  $R$  and  $r$ , respectively (solid lines). For comparison, the dependence of the absorbed photon flux  $\phi$  on the length  $L$  of  $\alpha\text{-Fe}_2\text{O}_3$  shell with empty cavity it is also shown (dashed lines).

value of  $\phi_{\text{max}}$  are found for HNs with  $r = 30$  nm Al core. Indeed, the largest  $\phi_{\text{max}}$  value ( $11.2 \times 10^{16}$  photons per  $\text{cm}^2$  per s) is reached by the  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN with  $L = 100$ ,  $R = 40$  and  $r = 30$  nm (black solid line, Fig. 7a). The variation of  $\phi$  with  $L$  arises as a direct consequence of the plasmon enhanced light

absorption. By increasing either the aspect ratio AR of the Al core ( $AR = L/2r$ ) or the  $\alpha\text{-Fe}_2\text{O}_3$  shell thickness  $S$ , the Al core LSPR redshifts towards longer wavelengths. As the spectral position of the LSPR redshifts from  $\lambda = 400$  nm to approximately  $\lambda = 650$  nm, that is, in the wavelength range where  $\text{Im}(\varepsilon(\lambda))$  of hematite is greater than zero,  $\phi$  increases with  $L$ .

On the contrary, as the LSPR redshifts to wavelengths where  $\text{Im}(\varepsilon(\lambda))$  of hematite is nearly zero, typically for  $\lambda$  larger than 650 nm,  $\phi$  decreases with  $L$ . Therefore, to achieve large  $\phi_{\max}$  values a fine tuning of the geometrical parameters of the HN,  $L$ ,  $R$  and  $r$ , is required, in such a way to maximize the integral in eqn (2). For comparison, the dependence of the absorbed photon flux  $\phi$  on the length  $L$  of the  $\alpha\text{-Fe}_2\text{O}_3$  shell with empty cavity is also shown in Fig. 7 (dotted lines). It can be appreciated that the variation of  $\phi$  with  $L$  follows the same general trend:  $\phi$  increases rapidly from  $L = 50$  nm up to  $L \approx 200$  nm, and then it keeps almost constant as  $L \rightarrow 500$  nm, being the overall behavior described by a nearly sigmoidal curve. The limiting  $\phi$  value of the  $\alpha\text{-Fe}_2\text{O}_3$  shell with empty cavity as  $L \rightarrow 500$  nm also increases roughly linearly with  $S$ . A salient feature in Fig. 7 is the crossing point between the respective curves for the  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HNs and the  $\alpha\text{-Fe}_2\text{O}_3$  shells with empty cavity. This crossing point, whose position on the  $L$  axis varies between  $120 \text{ nm} < L < 190 \text{ nm}$  depending on the specific  $R$  and  $r$  values, delimits the length ranges where the absorbed photon flux  $\phi$  is enhanced or reduced within the  $\alpha\text{-Fe}_2\text{O}_3$  shell in a given  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN in comparison to the  $\alpha\text{-Fe}_2\text{O}_3$  shell with empty cavity. For instance,  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HNs with  $R = 40$ ,  $r = 30$  nm and  $L < 185$  nm present  $\phi$  values larger than the respective values of the  $\alpha\text{-Fe}_2\text{O}_3$  shell with identical dimensions. On the contrary, the relationship between the  $\phi$  values is quite the opposite for  $L > 185$  nm (solid and dashed black curves, Fig. 7a). This observation clearly exemplifies the plasmon enhanced light absorption effect and illustrates, in view of a given application, under which length range it is favorable or not to fill the  $\alpha\text{-Fe}_2\text{O}_3$  shell with an Al core.

### Effect of the plasmonic metallic core on the absorbed photon flux

The absorption spectra of  $\text{Ag}@\alpha\text{-Fe}_2\text{O}_3$  and  $\text{Au}@\alpha\text{-Fe}_2\text{O}_3$  HNs have also been simulated in order to analyze the effect of the nature of the plasmonic metallic core on the optical response of the HNs (the wavelength dependent complex refractive indexes for Au and Ag were obtained from ref. 64). Fig. 8 shows the variation of the LSPR wavelength peak on the length  $L$  of HNs with different core composition ( $R = 40$  nm and  $r = 30$  nm in all cases). In general, whatever the metallic core, a nearly linear dependence between the LSPR wavelength peak and the length  $L$  is found. However, for a given  $L$  value, the LSPR wavelength peak for Ag (red curve) and Au (green curve) is by far significantly redshifted with respect to the Al LSPR peak (black curve), a phenomena that can be explained in terms of the differences in the respective dielectric constant for each metal. For instance, for  $L = 100$  nm, the LSPR wavelength peaks are located at  $\lambda = 555$ , 710 and 750 nm for Al, Ag and Au, respectively. This example illustrates the following general trend: the LSPR

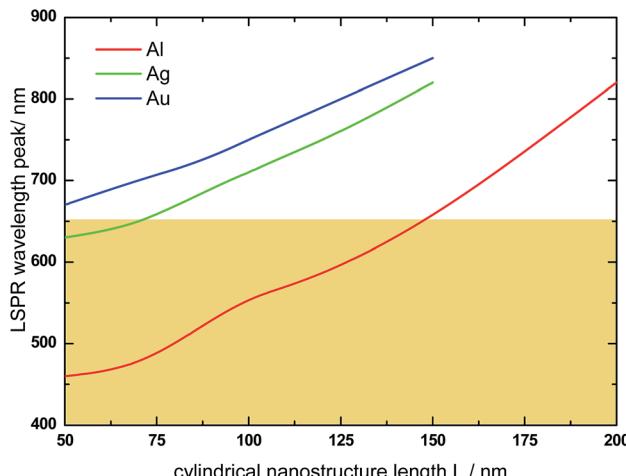


Fig. 8 Variation of the LSPR wavelength peak with the length  $L$  of HNs with different core composition.  $R = 40$  nm and  $r = 30$  nm in all cases. Al (red curve), Ag (green curve), Au (blue curve). The colored area schematically indicates the spectral range where  $\alpha\text{-Fe}_2\text{O}_3$  absorbs, that is, where the imaginary part of its dielectric constant is greater than zero,  $\text{Im}(\varepsilon(\lambda)) > 0$ .

excitation wavelengths for Ag and Au are larger than 650 nm and, therefore, do not overlap within the spectral range in which  $\alpha\text{-Fe}_2\text{O}_3$  absorbs, that is, in the spectral range where  $\text{Im}(\varepsilon(\lambda)) > 0$  (see Fig. 3, red curve). The spectral range in which  $\alpha\text{-Fe}_2\text{O}_3$  absorbs is schematically indicated in Fig. 8 by the colored area. Therefore, these results suggest that Al presents higher capabilities to enhance light absorption in  $\alpha\text{-Fe}_2\text{O}_3$  than Ag and Au.

Fig. 9 shows the variation of the absorbed photon flux  $\phi$  within the  $\alpha\text{-Fe}_2\text{O}_3$  shell with the length  $L$  of  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  (red curve),  $\text{Ag}@\alpha\text{-Fe}_2\text{O}_3$  (green curve) and  $\text{Au}@\alpha\text{-Fe}_2\text{O}_3$  (blue curve) HNs ( $R = 40$  nm and  $r = 30$  nm, in all cases). The variation of  $\phi$  with  $L$  for  $\alpha\text{-Fe}_2\text{O}_3$  shells with empty cavity and identical  $R$  and  $r$  values, is also shown (black curve). The main point to be remarked here is that, for this particular set of  $R$  and  $r$  values, the largest  $\phi$  is achieved for the HN with Al core and  $L = 100$  nm, whereas the typical plasmonics metals Ag and Au produce significantly smaller  $\phi$  values. This phenomena is directly related to the fact that, for Ag and Au, the plasmon resonances are substantially redshifted in comparison to Al, being as mentioned above located at  $\lambda > 650$  nm, where the imaginary part of the dielectric constant of  $\alpha\text{-Fe}_2\text{O}_3$  is negligible. Therefore, according to eqn (1) and (2), the plasmon enhanced light absorption effect produced by Ag and Au cores is rather poor and lower than that produced by an Al core.

### Comparison with infinitely long core shell HNs

To further address the reliability of the theoretical methodology implemented in this work, it is meaningful to contrast the results already presented with those recently reported by Ramadurgam *et al.*<sup>45</sup> In that work, the  $\phi$  values for core@ $\alpha\text{-Fe}_2\text{O}_3$  HNs (core = Ag, Si, Si-Ag, Si-Au, Si-Al) have been calculated based on rigorous solutions to the Maxwell's equations using



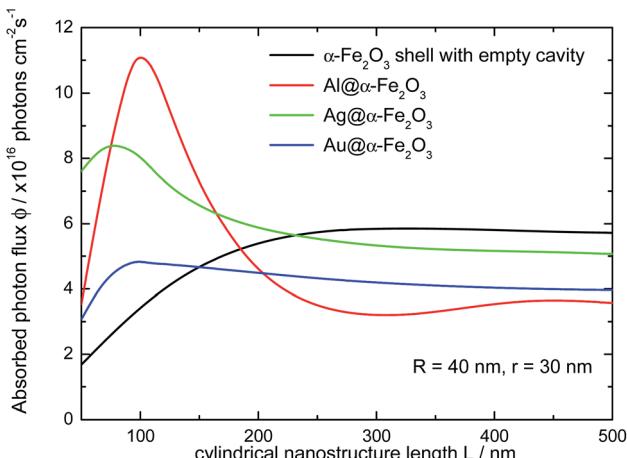


Fig. 9 Dependence of the absorbed photon flux  $\phi$  within the  $\alpha\text{-Fe}_2\text{O}_3$  shell with the length  $L$  of  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  (red curve)  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  (green curve) and  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  (blue curve) HNs. For comparison, the dependence of the absorbed photon flux  $\phi$  on the length  $L$  of  $\alpha\text{-Fe}_2\text{O}_3$  shell with empty cavity it is also shown (black curve).  $R = 40$  nm and  $r = 30$  nm in all cases.

Mie-formalism for  $L \gg r$  (infinite) right circular cylinders. Therefore, the proposed comparison makes sense for  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HNs with  $L = 500$  nm, where the  $L \gg r$  condition is roughly satisfied according to the length size studied in the current work. Table 1 shows the  $\phi$  values for  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HNs studied in the present work as well as for  $\text{Si}@\alpha\text{-Fe}_2\text{O}_3$  and  $\text{Ag}@\alpha\text{-Fe}_2\text{O}_3$  HNs studied by Ramadurgan *et al.* The comparison is performed between HNs with the same internal  $r$  and external  $R$  radius and different core composition (Al, Si and Ag). In addition, the length  $L$  is 500 nm for the  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HNs, whereas for the  $\text{Si}@\alpha\text{-Fe}_2\text{O}_3$  and  $\text{Ag}@\alpha\text{-Fe}_2\text{O}_3$  HNs,  $L > r$ . The  $\phi$  values for  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HNs are larger than those for  $\text{Si}@\alpha\text{-Fe}_2\text{O}_3$ , in turn, the  $\phi$  values for  $\text{Ag}@\alpha\text{-Fe}_2\text{O}_3$  HNs are just slightly larger than those for  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$ . These relationships highlight the effect of the nature of the core material. Given that the near field enhancements in Ag are larger than in Al nanostructures, it should be expected that Ag cores give rise to much larger  $\phi$  values in comparison to Al cores.<sup>33</sup> However, the dipole plasmon

Table 1 Absorbed photon flux  $\phi$  values for  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HNs and for other core shell HNs reported in ref. 45

$r/\text{nm}$	$R/\text{nm}$	$\phi/\text{photons} \times 10^{16} \text{ cm}^{-2} \text{ s}^{-1}$		
		$\text{Al}@\alpha\text{-Fe}_2\text{O}_3^a$ , $L = 500 \text{ nm}$	$\text{Si}@\alpha\text{-Fe}_2\text{O}_3^b$ , $L \gg r$	$\text{Ag}@\alpha\text{-Fe}_2\text{O}_3^b$ , $L \gg r$
30	40	3.6	2.0	
	50	5.9	3.9	
	60	8.5	5.6	
40	50	2.8		3.6
	60	5.8		6.8
	70	8.2		8.4

<sup>a</sup> This work. <sup>b</sup> Ref. 45.

resonance for the HNs analyzed in Table 1 ( $L \geq 500$  nm), which presents larger near field enhancements than higher order modes, is located beyond the visible region of the spectrum.

As a consequence, the effect of the nature of the plasmonic core on the  $\phi$  values is attenuated for these  $L$  values. For shorter lengths, the dipole LSPR blueshifts toward the visible region, and the near field enhancement generated within the shell produces an enhancement of  $\phi$  (see Fig. 7). Furthermore, this phenomenon should be the main mechanism that explains why the NHs studied in the present work exhibits larger  $\phi_{\text{max}}$  values in comparison to those reported previously. For instance, the largest  $\phi$  value ( $7.4 \text{ photons} \times 10^{16} \text{ cm}^{-2} \text{ s}^{-1}$ ) reported for  $\text{Si}@\alpha\text{-Fe}_2\text{O}_3$  HN has been found for  $\text{Si}(40 \text{ nm diameter})\text{-Al}(50 \text{ nm})\alpha\text{-Fe}_2\text{O}_3(40 \text{ nm})$  HN, whereas the highest  $\phi$  value found in this work ( $11.2 \text{ photons} \times 10^{16} \text{ cm}^{-2} \text{ s}^{-1}$ ) occurs for a  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN with  $R = 40$ ,  $r = 30$  and  $L = 100$  nm. This comparison with the results reported previously for similar HNs further support the consistence of the data presented in this work and emphasizes the relevance of considering not only  $r$  and  $R$ , that is, the 2D geometry of the HN, but also the length  $L$  for an optimum design of HNs potentially useful for harvesting applications.

## Conclusions

In this work, the absorption and near field properties of  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  core shell HNs has been theoretically studied by means of Discrete Dipole Approximation simulations, whereas the partial contribution to the absorption spectrum of each component of the HN has been evaluated by implementing a general methodology. The effect of varying the geometrical parameters of the HNs, that is, the length  $L$ , the internal  $r$  and the external  $R$  radius, on the respective absorption spectrum and absorbed photon flux  $\phi$  has been examined systematically. It has been found that, for a given set of  $r$  and  $R$  values, there exist an  $L$  value that gives place to the largest  $\phi$  value. This phenomena results as a compromise between the near enhancements within the  $\alpha\text{-Fe}_2\text{O}_3$  shell, which in turn depends on the resonance wavelength of the plasmonic excitations in the Al core, and the value of the wavelength dependent imaginary part of the dielectric constant of  $\alpha\text{-Fe}_2\text{O}_3$  ( $\text{Im}[\epsilon(\lambda)]$ ). The plasmon enhanced light absorption phenomena observed in the  $\alpha\text{-Fe}_2\text{O}_3$  shell of the  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HNs studied can be explained in terms of a plasmon-induced energy transfer mechanism based on the near field enhancement. Within the size range studied, the highest  $\phi$  value ( $11.2 \times 10^{16} \text{ photons per cm}^2 \text{ per s}$ ) is reached by the  $\text{Al}@\alpha\text{-Fe}_2\text{O}_3$  HN with  $L = 100$ ,  $R = 40$  and  $r = 30$  nm, a  $\phi$  value substantially larger those recently reported for infinitely long HNs with a similar composition. Furthermore, it has been shown that Al leads to greater light absorption in the  $\alpha\text{-Fe}_2\text{O}_3$  shell than conventional Ag and Au plasmonic materials, as the dipole plasmon resonance for Ag and Au are spectrally located well beyond the visible regime, where the  $\alpha\text{-Fe}_2\text{O}_3$  shell does not absorb. Importantly, in contrast with previous studies, the results presented here demonstrate that the dipole plasmon resonance of the Al core can be tuned into the visible region by adjusting properly the

HN length  $L$ . Consequently, the HN length  $L$  has a crucial role in determining the absorbed photon flux  $\phi$  values, therefore, a smart design of core–shell cylindrical HNs with improved photoactive properties should include the 3D geometry that takes into account the length  $L$  of the HN.

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