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Formation mechanism of hafnium oxide nanoparticles by a hydrothermal route

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Hafnium oxide nanoparticles (NPs) were synthesized by a hydrothermal route, using hafnium tetrachloride (HfCl_4) as the starting material and sodium hydroxide (NaOH) to adjust the pH. Through changing the aging temperature, concentration of NaOH and reaction time, both pure tetragonal hafnium oxide (t-HfO_2) and pure monoclinic hafnium oxide (m-HfO_2) were obtained. X-ray diffraction (XRD) spectra and transmission electron microscopy (TEM) images indicated that the shapes of t-HfO_2 NPs and m-HfO_2 NPs were near-spherical and spindle-like, respectively. The formation of t-HfO_2 NPs or m-HfO_2 NPs is probably related to their crystal cell structure, thermodynamic and kinetic stabilities. Tetragonal HfO_2 is produced originally in the process of the formation of monoclinic HfO_2 . A higher temperature, lower concentration of NaOH , longer reaction time and addition of m-HfO_2 seeds are beneficial for the formation of m-HfO_2 NPs. By analysis and calculation of the equilibrium constants involving hydrolysis of hafnium ions, the changes in the mole fractions of hafnium hydro-complexes with pH were determined. The $\text{Hf}(\text{OH})_6^{2-}$ ion is assigned to the precursory hydro-complex for the formation of HfO_2 nanoparticles transformed from $\text{Hf}(\text{OH})_4$ gel according to a comparison between the influences of pH on the equilibrium and the formation of HfO_2 particles. Moreover, the formation of HfO_2 NPs was obviously promoted and the size was reduced by addition of seeds, suggesting that the formation of HfO_2 NPs is controlled by the surface-deposition reaction. The above results are of great importance for studying nano-inorganic solution chemistry.

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Introduction

Nanostructured materials have a lot of important applications in various fields because of their unique properties.^{1–3} Hafnium is known as the “little brother” of titanium and zirconium. Its dioxide (HfO_2) is a material with a number of technologically attractive properties such as high melting point (2758 °C), high dielectric constant (≈ 30), high chemical stability, a wide band gap (>5.0 eV), and high neutron absorption cross section.^{4,5} It often plays an important role in the continuous down-scaling of integrated circuits since new insulating materials with a high dielectric constant are being researched to replace SiO_2 as a gate dielectric.^{6,7} In terms of structural characteristics, hafnium oxide exists in three polymorphic structures, namely monoclinic (m-HfO_2) at low temperature, tetragonal (t-HfO_2) above 2050 K, and cubic (c-HfO_2) at around 2803 K.^{8–10} Each structure has different applications.

The optical, electrical and other properties of HfO_2 nanoparticles (NPs) are strongly affected by their size, morphology, and surface characteristics.^{11,12} Therefore, it is necessary to consider the required specifications of HfO_2 NPs before

choosing the synthesis method. Up to now, researchers have developed some synthesis approaches such as gel-sol method,¹³ microemulsion processes¹⁴ and precipitation.^{10,15} However, these methods have some drawbacks, such as complicated operation, low yield and agglomerated products. In addition, all these ways only can obtain the m-HfO_2 NPs. Preparation of t-HfO_2 NPs has been rarely reported so far. More importantly, the formation mechanism and crystal form or morphology control of HfO_2 NPs are less reported.

Recently, many efforts have been undertaken to improve the synthesis method. As a promising approach, hydrothermal synthesis^{16–18} is widely used to synthesize nanocrystalline oxide materials due to the mild reaction condition, simple operation and no roasting. A. Sahraneshin¹⁶ synthesized three differently shaped HfO_2 NPs *via* a surfactant-assisted hydrothermal reaction in highly alkaline media. The products obtained were flower-like nanostructures (20.0 nm in diameter), polycrystalline nanoagglomerates (25.0 nm in diameter), and water-dispersible single nanoparticles (4.0 nm in diameter). In addition, S. A. Elizario⁸ successfully obtained the HfO_2 NPs by the microwave hydrothermal method. The temperature chosen was 140 °C and these nanostructures exhibited an average width in the range from 15.0 to 75.0 nm as well as an average height between 85.0 and 105.0 nm. The hydrothermal method allows to control size, morphology and the composition of the

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products, and to obtain homogeneous and dispersed nanoparticles, through varying parameters such as temperature, pressure, duration of the process, concentration and acidity (pH).^{19–21} The control of particle size and morphology is the result of processes of coarsening and redissolution–recrystallization which takes place under conditions of high pressure and temperature. The main advantages of hydrothermal method are simplicity and convenience.

In common, hydrothermal method still needs improvement in terms of yield, monodispersity, structural perfection, and size control. For synthesizing some nanoparticles, seeding is a very effective way to control particle size, to determine the crystal form²² and even to study the nucleation and growth mechanisms. Some researchers have made in-depth studies on this technology. Our previous studies reported that the addition of seeds has been able to systematically control the particle morphology and studied the nucleation and growth mechanisms of ZrO₂ (ref. 22) and TiO₂.²³ The seeds inhibit aggregation and the formation of secondary particles, so as to obtain the product wanted. Generally, the surface-deposition of monomers is not often the rate-determining step for the formation of nanoparticles unless the formation is accelerated and the particle size is controlled by seeding. Also, in this case, the size-distribution of nanoparticles is commonly narrowed.

In this paper, we used a hydrothermal route to prepare hafnium oxide nanoparticles. Effects of temperature, NaOH concentration, duration and crystal form of seeds were investigated to study the formation mechanisms of HfO₂ NPs from aspects of precursory complexes, thermodynamic and kinetic stabilities.

Experimental

Materials

HfCl₄ (AR, 99.0%), sodium hydroxide (AR, 96.0%), sodium dodecyl-benzenesulfonate (AR, 88.0%), dodecylamine (CP) were all purchased from Sinopharm Chemical Reagent Co., Ltd.

Synthesis

Preparation of HfO₂ nanoparticles. The HfO₂ nanoparticles (NPs) were synthesized by the hydrothermal route. The standard experimental procedure is described as follows. The hafnium hydroxide chloride (Hf(OH)₂Cl₂) solution was firstly prepared by dissolving 0.160 g of HfCl₄ in 10.0 mL of de-ionized water. NaOH aqueous solution (3.0 M, 10.0 mL) was added dropwise to the solution above, causing the reaction with Hf(OH)₂Cl₂ to form hafnium hydroxide (Hf(OH)₄). After that, the solution was transferred into a 100 mL Teflon-lined autoclave with inner diameter of ca. 4.2 cm, and the sealed autoclave was heated to 120 °C and maintained for 24 h. The products were purified by centrifugation for three cycles with alcohol and de-ionized water alternately after the autoclave was cooled down. Finally the precipitate was dried at 50 °C for 24 h. The procedure is summarized in Scheme 1.

Preparation of tetragonal and monoclinic HfO₂ seeds. The synthesis procedure of monoclinic HfO₂ (m-HfO₂) seeds is

Scheme 1 Preparation of HfO₂ NPs.

described as follows. To the solution prepared by dissolving 0.160 g of HfCl₄ in 8.0 mL of de-ionized water, 10.0 mL NaOH was added in order to make 0.1 M NaOH in aqueous phase, and 2.0 mL of 0.1 M dodecylamine solution was mixed with the solution above by stirring for 2–3 h. Hereafter, the resulting mixture was transferred into a 100 mL Teflon-lined autoclave with inner diameter of ca. 4.2 cm and maintained for 24 h after heated to 160 °C. On the other hand, to obtain tetragonal HfO₂ (t-HfO₂) seeds, 5.0 mL of de-ionized water including 0.160 g of HfCl₄ was added to 10 mL of 0.1 M sodium dodecylbenzenesulfonate solution, along with agitation of 2–3 h. Then the mixture was transferred into a 100 mL Teflon-lined autoclave with addition of 5.0 mL NaOH solution to make 3.0 M NaOH in aqueous phase. Afterwards, the autoclave was sealed and maintained for 24 h after heated to 100 °C.

The products were purified by centrifugation for three cycles with alcohol and de-ionized water alternately after the autoclave was cooled down. Finally the precipitate was dried at 50 °C for 24 h. The procedures are summarized in Scheme 2.

Characterization

The different morphologies and phases presenting in the solids were measured using X-ray powder diffraction (XRD, D/max, Rigaku, Tokyo, Japan) with Cu-K α radiation ($\lambda = 1.5418$ Å) in a 2θ – θ setup, the 2θ angle was scanned from 0 to 90°. JADE software (MDI JADE 7 Materials Data XRD Pattern Processing, Identification, and Quantification) was used to evaluate/analyze the XRD patterns. The JCPDS card no. 06-0318 and the JCPDS card no. 53-0550 were used as the XRD standard files of m-HfO₂ and t-HfO₂, respectively. The pH was measured by Sartorius PB-10.

Transmission electron microscopy (TEM) images were recorded with a JEOL JEM 2100F transmission electron-microscope, to analyze the product size and morphology. The samples used for TEM observations were prepared by dispersing the NPs in ethanol followed by ultrasonic vibration

Scheme 2 Preparation of HfO₂ seeds.

for 30 min, and then placing a drop of this dispersion onto a copper grid before loading into the instrument.

Results and discussion

Preparation of HfO₂

Fig. 1 shows the XRD spectra of both tetragonal hafnium oxide nanoparticles (t-HfO₂ NPs) and monoclinic hafnium oxide nanoparticles (m-HfO₂ NPs) prepared. The tetragonal phase of HfO₂ was obtained under otherwise the standard conditions at 100 °C, the monoclinic phase of HfO₂ was obtained at 160 °C. In Fig. 1(a), the major characteristics peaks found at 30.48°, 35.30°, 50.68°, 60.26° on the 2θ scale correspond to the {111}, {200}, {220} and {311} planes respectively, in good agreements

with the standard PDF card of t-HfO₂ (JCPDS: no. 53-0550). The corresponding TEM image of near-spherical t-HfO₂ particles (4.0 nm) is presented in Fig. 2(a). In Fig. 1(b), the major characteristics peaks found at 24.64°, 28.30°, 31.76°, 50.46° on the 2θ scale correspond to the {011}, {−111}, {111}, {220} planes respectively, in good agreements with the standard PDF card of m-HfO₂ (JCPDS: no. 06-0318). The corresponding TEM images of spindle-like m-HfO₂ particles (*ca.* 100 nm × 50 nm) with a high aspect ratio is presented in Fig. 2(b). These nanoparticles are uniform, but some particles gather together.

The high-resolution TEM images shown in Fig. 2(a1) indicates high crystallinity of the structure, the *d* spacing of lattice fringes of 0.25 nm and 0.29 nm are indexed to the (200) and (111) plane of t-HfO₂, respectively. In Fig. 2(b1), the *d* spacing of lattice fringes of 0.28 nm and 0.32 nm are indexed to the (111) and (−111) plane of m-HfO₂, respectively. All the *d* spacing values are in close agreement with those from t-HfO₂ (JCPDS: no. 53-0550) and m-HfO₂ (JCPDS: no. 06-0318).

Effects of reaction conditions on the formation of HfO₂ nanoparticles

Reaction time. Fig. 3 and 4 present XRD spectra and TEM images of the products obtained with different aging time at 120 °C under the otherwise conditions. After aging for 3 h, fine near-spherical particles of 4 nm in diameter were found in Fig. 4(a) and proved to be tetragonal phase by the XRD spectrum in Fig. 3. Shown as the white circle in Fig. 4(a), the particles grew and aggregated with the time going and the spindle-like particles began to appear after aging for 24 h, as displayed in Fig. 4(b) in the white circle. Virtually, at this time the product has been a mixture of t-HfO₂ and m-HfO₂ NPs, as exhibited in the XRD spectrum in Fig. 3. After aging for 72 h, from XRD spectrum in Fig. 3, the nanoparticles have been transformed into spindle-like m-HfO₂ (*ca.* 120 nm × 52 nm) completely, as also being confirmed by that in Fig. 4(c).

Fig. 1 XRD spectra of HfO₂ NPs prepared under otherwise the standard conditions (3.0 M NaOH and 24 h) at different temperatures: (a) 100 °C, (b) 160 °C.

Fig. 2 HRTEM images (1) and TEM images (2) of HfO_2 NPs prepared under otherwise the standard conditions (3.0 M NaOH and 24 h) at different temperatures: (a) 100 °C, (b) 160 °C.

Fig. 3 XRD spectra of HfO_2 NPs prepared under otherwise the standard conditions (3.0 M NaOH and 120 °C) with different reaction time.

Fig. 4 TEM images of HfO₂ NPs prepared under otherwise the standard conditions (3.0 M NaOH and 120 °C) with different reaction time: (a) 3 h, (b) 24 h, (c) 72 h.

Fig. 5 XRD spectra of HfO₂ NPs prepared under otherwise the standard conditions (120 °C and 24 h) with different concentrations of NaOH.

The above analysis reflected a phenomenon that the m-HfO₂ was not formed at beginning, but transformed from the t-HfO₂. In the early stage of reaction, the t-HfO₂ NPs were firstly generated and then aggregated to form large secondary particles, which subsequently re-crystallized to produce m-HfO₂ NPs. This fact indicates that m-HfO₂ NPs probably have lower kinetic stability and higher thermodynamic stability in comparison to t-HfO₂ NPs.

Concentration of NaOH. XRD spectra in Fig. 5 show the diffraction peaks associated with m-HfO₂ and t-HfO₂ forms at different concentrations of NaOH. The main peaks of t-HfO₂ appeared in the presence of 5.0 M NaOH (pH = 14.0), the corresponding TEM image of near-spherical HfO₂ particles (3.0 nm) is presented in Fig. 6(a). It was clearly observed that with decreasing concentration of NaOH to 3.0 M (pH = 12.5), the low peaks in Fig. 5 and the spindle-like particles in Fig. 6(b) indicated the generation of m-HfO₂. Further decreasing led to the decline of peaks of t-HfO₂ and the enhancement of the peaks of m-HfO₂ in Fig. 5. Meantime, from Fig. 6(b), the mixture of the near-spherical and spindle-like HfO₂ particles was found.

Fig. 6 TEM images of HfO₂ NPs prepared under otherwise the standard conditions (120 °C and 24 h) with different concentrations of NaOH: (a) 5.0 M, (b) 3.0 M, (c) 0 M.

Decreasing NaOH concentration from 5.0 M to 0 resulted in the formation of m-HfO₂ (ca. 115 nm × 70 nm), indicated in Fig. 6(c).

Carefully considering the influence of pH or alkaline concentration on the formation of metal oxide from metal hydroxide, some metal hydro-complexes usually play a key role to the formation of metal oxide like TiO₂ (ref. 24 and 25) and ZrO₂.^{22,26} Jia *et al.*²⁷ suggested that the pH of the reaction mixture can control the dissociation rate of the precursor, which significantly affects the supply of metal ions or metal hydro-complexes in the reaction environment and thus the growth rate of the metal-oxide nanocrystals. For HfO₂ particles, precursory complex Hf(OH)_x^{4-x} ($x \geq 5$), has been suggested²⁸ from its influence on the particle size. On the other hand, A. Sahraneshin¹⁶ proposed that the concentration of alkali can affect the growth of (111) plane of HfO₂ which was unstable with higher surface energy. For the current synthesis of HfO₂, with no doubt, the high concentration of NaOH is of benefit to the

formation of primary t-HfO₂ NPs, this may be related to the effects of NaOH concentration on the precursor complex, which will be discussed in details in the latter section.

Reaction temperature. Undoubtedly, temperature is a key factor for the control of crystal forms. From the XRD spectra displayed in Fig. 7, the tetragonal phase of HfO₂ (4.0 nm) obtained at 100 °C under otherwise the standard conditions, the corresponding TEM image of near-spherical t-HfO₂ particles is presented in Fig. 8(a). The main peaks of t-HfO₂ became more obvious and the near-spherical particles began to accumulate as the temperature rose. Hereafter, the weak peak of M (-111) of m-HfO₂ appeared at 120 °C indicated the trend of formation of m-HfO₂ as also revealed from that some tiny embryos of spindle-like m-HfO₂ NPs were discernible in Fig. 8(b). Indeed, all the nanocrystals were fully transformed into monoclinic phase in the temperature range of 140–160 °C. The well crystallized monoclinic phase of HfO₂ was obtained under the standard conditions at 160 °C, the corresponding TEM image of spindle-like m-HfO₂ particles (ca. 100 nm × 50 nm) is presented in Fig. 8(c).

Based on the XRD and TEM observation in Fig. 7 and 8, the reaction temperature is also the key factor that influences particle morphology under the fixed alkaline concentration and reaction time. It has been reported that with the increase of temperature, the particles are more likely to collide to form a large particle even with different form at enough high temperature.^{23–25} In this work, t-HfO₂ NPs may collide mutually and transform to m-HfO₂ NPs with the increase of temperature. Therefore, higher temperature, lower concentration of NaOH, and longer reaction time are beneficial for the formation of monoclinic hafnium oxide nanoparticles.

Seeding. Fig. 9 exhibits XRD spectra of HfO₂ nanocrystals prepared at 120 °C for 24 h with 3.0 M NaOH in the presence and the absence of HfO₂ seeds. It was found that without seeds, both the main peaks of m-HfO₂ and t-HfO₂ appeared simultaneously, indicating that the product was a mixture of t-HfO₂ and m-HfO₂ particles, but in the presence of t-HfO₂ seeds, the main peaks were associated with t-HfO₂. Due to the addition of

Fig. 7 XRD spectra of HfO₂ NPs prepared under otherwise the standard conditions (3.0 M NaOH and 24 h) at different temperatures.

Fig. 8 TEM images of HfO₂ NPs prepared under otherwise the standard conditions (3.0 M NaOH and 24 h) at different temperatures: (a) 100 °C, (b) 120 °C, (c) 160 °C.

Fig. 9 XRD spectra of HfO₂ NPs prepared with different seeds.

tetragonal seeds, the solute monomers deposited on the pre-existing t-HfO₂ seeds and the size of the formed t-HfO₂ NPs became larger and larger, inhibiting aggregation and the formation of secondary particles, and preventing the production of m-HfO₂ NPs. Obviously, the t-HfO₂ seeds promoted the growth of t-HfO₂ and inhibited the formation of m-HfO₂. This is a strong evidence for the fact that the growth and phase transformation of t-HfO₂ NPs follow the non-aggregation and surface-deposition growth model.^{23,29} The seeding technique is undoubtedly useful for preparing the t-HfO₂ NPs, in spite of the difficulty to obtain the t-HfO₂ NPs. Interestingly, in the presence of m-HfO₂ seeds, the main peaks are associated with m-HfO₂. Due to the addition of monoclinic seeds, the solute monomers deposited on the pre-existing m-HfO₂ seeds, promoting the formation of m-HfO₂ and inhibiting the formation of t-HfO₂. In

a word, the product was t-HfO₂ in the presence of t-HfO₂ seeds, and that was m-HfO₂ in the presence of m-HfO₂ seeds. That means, crystal form of seeds determines that of the product. It is a very interesting and significant result, as the saying goes "You must reap what you have sown".

Formation mechanisms of HfO₂ by a hydrothermal route

Formation of m-HfO₂ NPs from t-HfO₂ NPs. Three cell types of HfO₂ forms are monoclinic (M), tetragonal (T) and cubic (C) as shown in Fig. 10. The coordination numbers of Hf⁴⁺ both in cubic and tetragonal cells are 8 to form Hf–O₈^{2–} structure, while that of monoclinic cell is 7 to form Hf–O₇^{2–} structure. The structure of m-HfO₂ can be viewed that the t-HfO₂ deflects a certain angle, along the β axis. Usually, structures with coordination number of 8 have better geometric symmetry and are easier to form, but monoclinic cell with coordination number of 7 is stable thermodynamically indeed. Under normal temperatures, the m-HfO₂ is the most stable, which is a reason for obtaining t-HfO₂ NPs with difficulty.

In terms of structures of t-HfO₂ and m-HfO₂, t-HfO₂ has better geometric symmetry compared with m-HfO₂, and a rule of thumb is that better symmetry products usually have good kinetic stability and are easy to be produced preferentially. Generally, the occurrence of any reaction or variance is comprehensively selected or controlled by both factors of thermodynamics and kinetics, and the reaction in the initial stage is controlled mainly by factor of kinetics.

In our experiment, t-HfO₂ NPs are easier to form compared with m-HfO₂ NPs and then the t-HfO₂ gradually transforms to m-HfO₂ with temperature rising or time going. In our previous work,²⁸ the m-HfO₂ NPs were obtained at 160 °C with 3.0 M NaOH for 24 h, but in the early stage of this reaction (1 h and 3 h), the products were t-HfO₂ NPs. It can be deduced that generally t-HfO₂ is produced originally and m-HfO₂ will be

Fig. 10 Structures of different HfO₂ crystal cells.

obtained by transformation from t-HfO₂. We have mentioned that under adequate temperature and concentration of NaOH, the products were a mixture of t-HfO₂ and m-HfO₂. Moreover, based on the influence of temperature and concentration of NaOH on products, it is confirmed that t-HfO₂ is produced originally and m-HfO₂ is obtained by transformation from t-HfO₂. Therefore, it can be concluded that t-HfO₂ is stable kinetically and m-HfO₂ is stable thermodynamically.

To further confirm it above, the aging time of the reaction at 100 °C with 3.0 M NaOH was extended from 24 h to 168 h, the XRD spectra are shown in Fig. 11. Obviously, the products were mainly t-HfO₂ NPs after 24 h, but after 168 h, the products were mainly m-HfO₂ NPs. Passage of time led to the weakening of peaks of t-HfO₂ and the appearance of the peaks of m-HfO₂ in Fig. 11. After 168 h, it was surprising to see that all of t-HfO₂ NPs was transformed to m-HfO₂ NPs. The result offers a clear proof that the m-HfO₂ is stable thermodynamically and the m-HfO₂ is commonly transformed from t-HfO₂.

The formation of t-HfO₂ with high geometric symmetry becomes more possible in alkaline circumstance. Contrarily, the formation of m-HfO₂ is probably inhibited when the concentration of NaOH in solution is enough high. It is reasonable that high concentration of NaOH can inhibit transformation from t-HfO₂ to m-HfO₂, because high concentration of NaOH can offer more coordinating oxygen ions and then more oxygen ions are beneficial for formation of oxides with high coordination number. These oxygen ions increase the possibility of the occurrence of the structure with high coordination number and high symmetry, and reduce that of the occurrence of distortion, leading to the formation of t-HfO₂ NPs. In a word, high concentration of NaOH is beneficial for formation of t-HfO₂ and inhibits the formation of m-HfO₂, this has been confirmed by our previous report.²⁸ More interestingly, it is also found that with the increased concentration of NaOH, the size of the obtained t-HfO₂ decreased in the concentrated NaOH aqueous solution.

Fig. 11 XRD spectra of HfO₂ NPs prepared under otherwise the standard conditions (3.0 M NaOH and 100 °C) with different reaction time.

On the other hand, temperature is often an important factor to determine the reaction direction and even to determine the crystal form of products. In this work, it has been found that the high temperature is beneficial for the formation of m-HfO₂. It could be caused by particles annealing and the difference in the structures of the two forms of HfO₂. Generally, large crystals can be formed by annealing of small crystals, along with the change in the crystal forms in some cases. Therefore, with the rise in temperature, the transformation of t-HfO₂ to m-HfO₂ can be explained in terms of the collision and the distortion in the process of the annealing. It has been reported that with the increase of temperature, the particles are more likely to collide, resulting in the reduction of coordination number, thus forming a large particle.^{23–25} As a result, these small t-HfO₂ crystals were transformed to large m-HfO₂ crystals due to the reduction of coordination number.

Formation process of HfO₂ NPs with and without seeds.

Generally, the meta-stable t-HfO₂ NPs are formed firstly due to their high formation rate. Then, with the passage of time, the particles change from t-HfO₂ to m-HfO₂ with thermodynamic stability. Based on the significant analyses in the former parts, the formation process of HfO₂ by the hydrothermal route is illustrated as follows.

In Fig. 12, after accomplishment of reaction between hafnium hydroxide chlorides and OH[−] in the water, the precursory complex Hf(OH)_x^{4−x} ($x \geq 5$) gather and react in the water. Through nucleation of solute monomers without seeds, the meta-stable t-HfO₂ NPs appear. Under appropriate conditions, the product is a mixture of t-HfO₂ NPs and m-HfO₂ NPs because some t-HfO₂ NPs transform to m-HfO₂ NPs. However, the main product is m-HfO₂ NPs under higher temperature and lower alkali, whereas the product under the opposite conditions is t-HfO₂ NPs. In other words, higher temperature and lower alkali concentration are beneficial for the formation of m-HfO₂. For better control of crystal forms, the seeds are added. When the adequate t-HfO₂ seeds exist, the solute monomers will deposit on t-HfO₂ seeds and the size of formed t-HfO₂ NPs become larger and larger, inhibiting aggregation and the formation of secondary particles, and then preventing the production of m-HfO₂ NPs. Obviously, the t-HfO₂ seeds promote the growth of t-HfO₂ and inhibit the formation of m-HfO₂. In the other hand, when the m-HfO₂ seeds are added, the solute monomers will deposit on the pre-existing m-HfO₂ seeds, promoting the formation of m-HfO₂ and inhibiting the formation of t-HfO₂. In a word, the product is t-HfO₂ in the presence of t-HfO₂ seeds, and that is m-HfO₂ in the presence of m-HfO₂ seeds.

For nucleation, the overall Gibbs free energy change,³⁰ ΔG , should be considered. ΔG , is the sum of the free energy due to the formation of the cluster and that due to the new surface created. In Fig. 13(b), ΔG has a positive maximum at a critical size, r^* . This maximum free energy change is the activation energy for nucleation. Nuclei or clusters larger than the critical size will further decrease their free energy for growth and become stable ones that grow to form particles.

Usually, it is somewhat hard to make $\Delta G < 0$ in the absence of seeds. However, once the seeds preformed stably are added,

Fig. 12 Formation and transformation processes of HfO_2 NPs with and without seeds.

Fig. 13 (a) LaMer model schematic diagram³² and (b) illustration of the overall free energy ΔG as a function of the growth particle size r .³⁰

spontaneous nucleation is inhibited, and then they grow by deposition of monomers on their surfaces to become large particles. At this time, the overall free energy change ΔG , could be much lowered even to less than 0. That means, the formation process of stable solute clusters or particles is skipped (Fig. 13(a)) and the reaction is accelerated. Therefore, the resulting final nanoparticles are smaller in size and more evenly dispersed. Undoubtedly, the seeding technique is useful for the systematic control of crystal form and for the study of the growth and nucleation mechanisms.³¹

Reaction and precursor species for formation of HfO_2 NPs.

Generally, in aqueous solution, pH affects the concentration of hydro-complexes. By analysis and calculation of the equilibrium constants involving hydrolysis of hafnium ions from D. Rai's report,³³ the changes of mole fractions of the four main hydro-complex species with pH are summarized and shown in Fig. 14. In our work, we measured the yield of t- HfO_2 NPs under different pH. These t- HfO_2 NPs were prepared at 100 °C

Fig. 14 Mole fractions of Hf(OH)^{3+} , Hf(OH)_4 , Hf(OH)_5^- , Hf(OH)_6^{2-} complexes as a function of pH at 25 °C.

Fig. 15 Formation of HfO₂ from Hf(OH)₆²⁻ and Hf(OH)₄.

with 3.0 M NaOH for 24 h. Respectively, when pH was 11.5, 12.5 and 13.5, the yields of t-HfO₂ were 70.8%, 82.1% and 90.5%, respectively. Obviously, the yield of t-HfO₂ increases with the increase of pH in this pH range. In our previous study, the high concentration of NaOH not only promotes the formation of t-HfO₂, but also declines particle size of t-HfO₂. Clearly, the pH dependence on the nucleation rate of t-HfO₂ reveals that some specific complex is responsible for the nucleation of t-HfO₂ as a precursor intermediate. The increase of the formation rate, or nucleation rate, with the increase of pH from 10.0 to 14.0 may be closely related to the increase in the equilibrium concentration of Hf(OH)₆²⁻ in Fig. 14. The high concentration of precursors usually results in the rapid nucleation, leading to the production of more nuclei, and then decreasing the particle size. Therefore, the Hf(OH)₆²⁻ species is assigned to the precursory complex to form t-HfO₂ in the hydrothermal system.

If we take into account that the overall reaction for the transformation from Hf(OH)₄ gel to HfO₂ sol is Hf(OH)₄ → HfO₂ + 2H₂O, the precursory complex must only be a catalyst or an intermediate, and thus Hf(OH)₄ complex, constantly furnished from the Hf(OH)₄ gel with the progress of the reaction, may also contribute to the poly-condensation reaction in the formation of HfO₂ particles. The transformation is similar to production of TiO₂ from Ti(OH)₄,²⁴ CeO₂ from Ce(OH)₄ (ref. 34) and ZrO₂ from Zr(OH)₄.^{22,35} The following elementary processes

may be involved in the overall reaction shown in Fig. 15(a and b), deduced from those of TiO₂ (ref. 24) and CeO₂.³⁴

Conclusions

The HfO₂ nanoparticles (NPs) were prepared successfully by a hydrothermal route. The phase transformation of HfO₂ occurs through changing the reaction temperature, the concentration of NaOH, aging time and crystal form of seeds. XRD spectra and TEM images revealed the near-spherical particles belonged to tetragonal HfO₂ (t-HfO₂), and the spindle-like particles belonged to monoclinic HfO₂ (m-HfO₂). Based on the kinetic and thermodynamic analyses, it can be induced that higher temperature, lower concentration of NaOH and longer reaction time are beneficial for the formation of m-HfO₂ nanoparticles. Moreover, it is confirmed that t-HfO₂ generally produces originally and m-HfO₂ is obtained by transformation from t-HfO₂.

In the standard conditions at 120 °C with 3.0 M NaOH for 24 h, the product is a mixture of t-HfO₂ and m-HfO₂ NPs in the absence of seeds. When m-HfO₂ seeds are added, the resultant is pure m-HfO₂ NPs, while t-HfO₂ seeds are added, under the same conditions the particles are pure t-HfO₂ NPs, proving the non-aggregation growth of nanoparticles. Not only the crystal form of HfO₂ can be well controlled, but also the particles size can be altered. The addition of HfO₂ seeds decreases the size of

nanoparticles. In the presence of seeds, the declined activated energy for the reaction is due to the decrease of ΔG , resulting from the skipping of spontaneous nucleation stage, and then causing separation of nucleation from growth.

The effect of solution pH on the formation of HfO_2 NPs was learned by the analysis above. Meantime, the high concentration of NaOH promoted the formation of t- HfO_2 NPs. Therefore, the hydro-complex $\text{Hf}(\text{OH})_6^{2-}$ has been confirmed as the precursor complex to form HfO_2 particles.

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Notes and references

- 1 C. A. Mirkin, R. L. Letsinger, R. C. Mucic and J. J. Storhoff, *Nature*, 1996, **382**, 607–609.
- 2 D. L. Feldheim and C. D. Keating, *Chem. Soc. Rev.*, 1998, **27**, 1–12.
- 3 S. Saito, *Science*, 1997, **278**, 77–78.
- 4 J. Robertson, *Rep. Prog. Phys.*, 2006, **69**, 327–396.
- 5 J. De Roo, K. De Keukeleere, J. Feys, P. Lommens, Z. Hens and I. Van Driessche, *J. Nanopart. Res.*, 2013, **15**, 1778.
- 6 G. D. Wilk, R. M. Wallace and J. M. Anthony, *J. Appl. Phys.*, 2001, **89**, 5243–5275.
- 7 J. Molina, R. Ortega, W. Calleja, P. Rosales, C. Zuniga and A. Torres, *Mater. Sci. Eng., B*, 2012, **177**, 1501–1508.
- 8 S. A. Eliziario, L. S. Cavalcante, J. C. Sczancoski, P. S. Pizani, J. A. Varela, J. W. M. Espinosa and E. Longo, *Nanoscale Res. Lett.*, 2009, **4**, 1371–1379.
- 9 R. Terki, G. Bertrand, H. Aourag and C. Coddet, *Mater. Lett.*, 2008, **62**, 1484–1486.
- 10 V. Jayaraman, G. Bhavesh, S. Chinnathambi, S. Ganesan and P. Aruna, *Mater. Express*, 2014, **4**, 375–383.
- 11 W. E. Buhro and V. L. Colvin, *Nat. Mater.*, 2003, **2**, 138–139.
- 12 H. B. Yao, M. R. Gao and S. H. Yu, *Nanoscale*, 2010, **2**, 323–334.
- 13 E. Tirosh and G. Markovich, *Adv. Mater.*, 2007, **19**, 2608–2612.
- 14 J. S. Quintero-Garcia, B. A. Puente-Urbina, L. A. Garcia-Cerda, O. S. Rodriguez-Fernandez and E. Mendoza-Mendoza, *Mater. Lett.*, 2015, **159**, 520–524.
- 15 A. Ramadoss, K. Krishnamoorthy and S. J. Kim, *Mater. Lett.*, 2012, **75**, 215–217.
- 16 A. Sahraneshin, S. Asahina, T. Togashi, V. Singh, S. Takami, D. Hojo, T. Arita, K. Minami and T. Adschiri, *Cryst. Growth Des.*, 2012, **12**, 5219–5226.
- 17 P. E. Meskin, F. Y. Sharikov, V. K. Ivanov, B. R. Churagulov and Y. D. Tretyakov, *Mater. Chem. Phys.*, 2007, **104**, 439–443.
- 18 E. Montes, P. Ceron, T. R. Montalvo, J. Guzman, M. Garcia-Hipolito, A. B. Soto-Guzman, R. Garcia-Salcedo and C. Falcony, *Appl. Radiat. Isot.*, 2014, **83**, 196–199.
- 19 L. Xiang, Y. P. Yin and Y. Jin, *J. Mater. Sci.*, 2002, **37**, 349–352.
- 20 H. B. Yin, Y. Wada, T. Kitamura, S. Kambe, S. Murasawa, H. Mori, T. Sakata and S. Yanagida, *J. Mater. Chem.*, 2001, **11**, 1694–1703.
- 21 Y. Q. Zheng, E. R. Shi, Z. Z. Chen, W. J. Li and X. F. Hu, *J. Mater. Chem.*, 2001, **11**, 1547–1551.
- 22 T. T. Shi, Y. T. Cai, L. Liu and X. P. Zhou, *Colloids Surf., A*, 2015, **469**, 83–92.
- 23 T. Sugimoto, X. P. Zhou and A. Muramatsu, *J. Colloid Interface Sci.*, 2003, **259**, 43–52.
- 24 T. Sugimoto, X. P. Zhou and A. Muramatsu, *J. Colloid Interface Sci.*, 2002, **252**, 339–346.
- 25 T. Sugimoto and X. P. Zhou, *J. Colloid Interface Sci.*, 2002, **252**, 347–353.
- 26 L. Liu, J. C. Xue and X. P. Zhou, *Nanosci. Nanotechnol. Lett.*, 2014, **6**, 346–352.
- 27 C. Jia, Y. Cheng, F. Bao, D. Chen and Y. Wang, *J. Cryst. Growth*, 2006, **294**, 353–357.
- 28 J. J. Qi and X. P. Zhou, *Colloids Surf., A*, 2015, **487**, 26–34.
- 29 X. P. Zhou, S. S. Li, X. L. Chen, Q. Zhu, Z. Q. Wang and J. Zhang, *J. Nanosci. Nanotechnol.*, 2008, **8**, 1392–1397.
- 30 I. V. Markov, *Crystal growth for beginners: fundamentals of nucleation, crystal growth and epitaxy*, World Scientific, 2003.
- 31 S. Taotao, C. Yutian, L. Li and Z. Xingping, *Colloids Surf., A*, 2015, **469**, 83–92.
- 32 C. Burda, X. Chen, R. Narayanan and M. A. El-Sayed, *Chem. Rev.*, 2005, **105**, 1025–1102.
- 33 D. Rai, Y. X. Xia, N. J. Hess, D. M. Strachan and B. P. McGrail, *J. Solution Chem.*, 2001, **30**, 949–967.
- 34 X. S. Zheng, L. Liu and X. P. Zhou, *Colloid J.*, 2014, **76**, 558–563.
- 35 R. R. Piticescu, C. Monty, D. Taloi, A. Motoc and S. Axinte, *J. Eur. Ceram. Soc.*, 2001, **21**, 2057–2060.