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Cite this: *RSC Adv.*, 2017, 7, 642

Spirooxazine molecular switches with nonlinear optical responses as selective cation sensors†

Jin-Ting Ye,^a Li Wang,^a Hong-Qiang Wang,^a Zhen-Zhen Chen,^a Yong-Qing Qiu^{*ab} and Hai-Ming Xie^{*ab}

Spirooxazine, a photochromic material, can transform into metallic open-form merocyanine by molecular switching, giving rise to large contrasts in its second-order nonlinear optical (NLO) properties. The switching properties are particularly large when various metal ions (Li^+ , Na^+ , K^+ , Mg^{2+} , Ca^{2+} , Fe^{2+} , Zn^{2+} , and Ag^+) are introduced, as evidenced by density functional theory calculations, which show that the spirooxazine undergoes a pronounced change in geometry accompanied by formation of a larger π -conjugated system. The resultant merocyanine derivatives have 10–21-fold higher static second-order NLO responses. Spirooxazine can therefore be used as a powerful and multi-use detection tool. The large first hyperpolarizability (β_{tot}) is shown to rely on the alkaline earth metal, causing β_{tot} values to increase nearly 21-fold, as evidenced by the larger charge distribution, lower transition energy, and separate distribution of first hyperpolarizability density. In contrast, variation of β_{tot} in the Fe^{2+} derivative is not obvious, owing to stronger complexation, a larger amount of charge transferred from the naphthoxazine moiety to the metal, and the reduction in N...O distance between the ligand heads. Therefore, spiropyran-to-merocyanine molecular switching can be used to distinguish alkaline earth metals and determine the efficiency of cation detection.

Received 20th October 2016
Accepted 14th November 2016

DOI: 10.1039/c6ra25478k

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1. Introduction

Cation detection techniques are of extensive interest because of their widespread application in various fields, including biology, chemistry, clinical biochemistry, and environmental sciences.^{1,2} Conventional cation detection techniques are based on changes in light absorption, which results in color changes or fluorescence induction/modification. Spirooxazine (SP) responds to different external stimuli, such as light,^{3,4} temperature,^{5,6} and metal ions, to undergo reversible structural interconversion accompanied by changes in its photophysical properties. Therefore, it is of interest in optoelectronic applications to optical memories with data storage,^{7–9} molecular switches,^{10–14} and metal ion detection.^{15–17} In particular, the introduction of different metal ions causes the closed-form spirooxazine to transform into the open-form metallic merocyanine (MC^*M^{n+}), which is always accompanied by a major change in geometric structure or π -electron conjugation, resulting in a significant switching effect in nonlinear optical response properties.¹⁸

Spirooxazines have been utilized extensively in the development of optical probes and molecular switches because their

molecular architecture is easily tuned. Previous studies, which focused on coupling the changes in electronic structure and open-ring reaction mechanism of spirooxazine, have allowed an in-depth understanding of its optical properties in metal ion detection. A systematic study of highly sensitive and selective metal ion detection through optical signals using a spirooxazine derivative has been reported.^{19–29} As spirooxazine and its derivatives have strong fluorescence signals, complexes of spirooxazine and transition metal cations (Fe^{2+} , Zn^{2+} , and Ag^+) have been fully reported at the molecular level.^{19,20} Recently, Huang *et al.* reported that spirooxazine combined with earth metal cations (Mg^{2+} and Ca^{2+}) can show the superior metalochromic properties.^{19,21} Using the same rationale, alkali metals (Li^+ , Na^+ , and K^+) with spirooxazine were calculated to produce similar molecular switches. In this work, we demonstrate that selective cation recognition can be performed using molecular NLO switches. Indeed, this property is associated with the important first hyperpolarizability (β_{tot}) contrast, when the merocyanine form complexes a series of alkaline, alkaline earth, and transition metal cations. In addition, the large NLO contrast is demonstrated to depend strongly on the nature of the metal, providing selective cation sensing.

2. Computational details

Geometry optimizations were carried out using the B3LYP^{30,31} functional as implemented in the Gaussian 09W³² program. The 6-31G(d) basis set and the LanL2DZ effective core potential

^aFaculty of Chemistry, Institute of Functional Material Chemistry, Northeast Normal University, Changchun, Jilin 130024, China. E-mail: qiyuq466@nenu.edu.cn; xiehm136@nenu.edu.cn; Fax: +86 431 85098768

^bNational & Local United Engineering Laboratory for Power Battery, Faculty of Chemistry, Northeast Normal University, Changchun, Jilin 130024, China

† Electronic supplementary information (ESI) available. See DOI: 10.1039/c6ra25478k



(ECP) basis set for transition metal cations (Fe^{2+} , Zn^{2+} , and Ag^+) were applied to the complexes studied. The B3LYP functional, a combination of Becke's three-parameter hybrid exchange functional and the Lee–Yang–Parr correlation functional, has been widely used in geometrical optimizations.^{33–35} Harmonic vibrational frequency calculations were used to confirm that the optimized structures were minima, as characterized by positive vibrational frequencies.

The total first hyperpolarizabilities, β_{tot} , for the studied complexes are defined as:

$$\beta_{\text{tot}} = \sqrt{(\beta_x^2 + \beta_y^2 + \beta_z^2)} \quad (1)$$

where β_i is defined as:

$$\beta_i = (1/3) \sum_j (\beta_{iji} + \beta_{jii} + \beta_{jij}) \quad i, j = \{x, y, z\} \quad (2)$$

Choosing an appropriate method for the evolution of hyperpolarizability is crucial for hyperpolarizability calculations. High-level *ab initio* methods, such as the second-order Møller–Plesset perturbation method (MP2), coupled cluster methods (CCSD, CCSD(T), or even higher CCSD(T)) are known to be generally reliable for calculating molecular system hyperpolarizabilities.³⁶ However, the high scaling order of the *ab initio* methods requires tremendous computational resources with increasing system size.³⁷ Therefore, density functional theory (DFT) offers an attractive alternative to the demanding high-level *ab initio* methods. Four functionals, the BHandHLYP hybrid exchange–correlation functional, the M06-2X functional with a high percentage of HF exchange, and two long-range corrected functionals, CAM-B3LYP and ω B97XD, were chosen to check that our calculations were consistent.^{38,39} Moreover, studies have shown that basis sets must be chosen with due consideration of the calculation of optical properties, especially in hyperpolarizability calculations.^{40,41} Therefore, five Pople's basis sets (6-31+G(d), 6-31++G(d), 6-31+G(d,p), 6-31++G(d,p), and 6-311++G(d,p)) were chosen to evaluate the effect of the basis set. Due to the high computational cost, $\text{MC}^*\text{Ca}^{2+}$ was chosen to assess the basis set effects at the CAM-B3LYP level in this work.

In order to further explain the second-order NLO behaviors of this series of complexes, time-dependent density functional theory (TD-DFT) is a useful tool for computing linear and

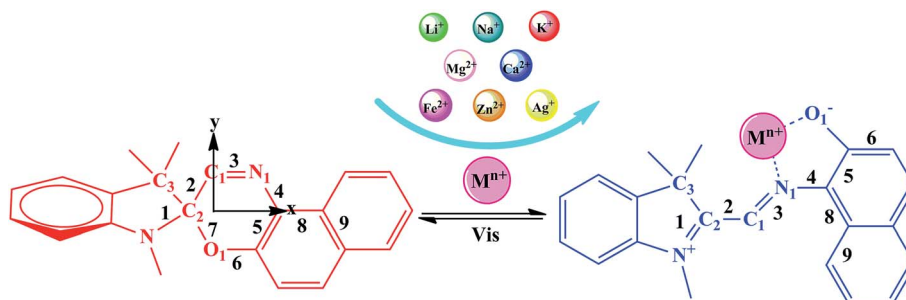
nonlinear molecular properties, because of its desirable compromise between computational efficiency and accuracy.^{42,43} The ω B97XD functional was found to be suitable for large π -systems.⁴⁴ Therefore, the absorption spectra of complexes were simulated using the ω B97XD functional with the 6-31+G(d) basis set (LanL2DZ ECP basis set for transition metal ions).

All DFT and TD-DFT calculations were carried out using the Gaussian 09W program package, with the results analyzed by Multiwfn 3.3.8 software.⁴⁵

3. Results and discussion

3.1 Molecular structures

The photochromic molecules in this study originate from the combination of metal ions with spirooxazine, which can be converted into the corresponding open-form merocyanine after the introduction of the metal ions (Scheme 1). The geometric structures of the studied complexes were optimized without any symmetry constraint at the B3LYP/6-31G(d)/LanL2DZ level. Typically, the closed spirooxazine consists of an indoline fragment and a naphthoxazine moiety, which are kept almost orthogonal by a chiral “spiro” carbon atom. When metal ions are added, two isolated π -conjugated portions in the spirooxazine become extensively conjugated as a large coplanar structure (MC^*M^{n+}). The $\text{O}_1\text{--N}_1\text{--C}_1\text{--C}_2$ dihedral angle of SP was shown to be 7.7° , while that of $\text{MC}^*\text{Ca}^{2+}$ was 92.6° . Unlike other derivatives, the Ca^{2+} cation lead to C_1 , C_2 , and C_3 atoms becoming out of the plane ($\text{C}_1\text{--C}_2\text{--C}_3\text{--Ca}^{2+}$ dihedral angle of 46.0°), suggesting that it caused the largest structural distortion. The $\text{O}_1\text{--C}_2$ bond length of the SP was 1.428 \AA , which was very close to the corresponding value (1.454 \AA) previously reported by Sahoo *et al.*,²⁰ suggesting that the geometrical calculations were reliable. Selected bond lengths and dihedral angles are listed in Table 1. The $\text{O}_1\text{--N}_1$ bond length of SP was found to be 2.825 \AA (Table 1). In the metal cation derivatives, the $\text{O}_1\text{--N}_1$ distances became smaller (ranging from 2.549 to 2.798 \AA), which was easily explained by the metal cations having strong interactions with naphthoxazine. Moreover, calculation results showed that metal ions were located near the center of the coplanar structure in the complexes, but slightly closer to the O side, probably because of the stronger interaction of $\text{O} \cdots \text{M}^{n+}$ relative to $\text{N} \cdots \text{M}^{n+}$. In these complexes, the distances between



Scheme 1 Equilibrium between the spiropyran form and the cation-complexed merocyanine form.



Table 1 Important geometrical parameters and NBO charges of metal cations at the B3LYP/6-31G(d)/LanL2DZ level

Compound	M ⁿ⁺ –O ₁ (Å)	M ⁿ⁺ –N ₁ (Å)	O ₁ –N ₁ (Å)	Angle ^a (°)	Angle ^b (°)	Q ^c (M)	BLA ^d (Å)
SP	—	—	2.825	–7.7	—	—	0.056
MC*Li ⁺	1.792	2.022	2.670	–37.4	4.2	0.78	0.013
MC*Na ⁺	2.123	2.482	2.752	–60.8	3.9	0.89	0.022
MC*K ⁺	2.422	3.886	2.706	–39.9	2.6	0.96	0.020
MC*Mg ²⁺	1.877	2.059	2.686	–32.9	6.9	1.59	0.001
MC*Ca ²⁺	2.179	2.449	2.701	–92.6	46.0	1.83	0.005
MC*Fe ²⁺	1.789	1.924	2.549	–37.1	–3.0	0.84	0.017
MC*Zn ²⁺	1.888	2.032	2.728	–37.9	6.5	1.47	0.003
MC*Ag ⁺	2.209	2.452	2.798	–70.3	4.3	0.77	0.017

^a O₁–N₁–C₁–C₂ dihedral angle. ^b C₁–C₂–C₃–M dihedral angle. ^c Natural bond orbital (NBO)^{46,47} charge on the metal atom in *e*. ^d Bond length alternation (BLA) in the conjugated bridge between the indoline and naphthoxazine rings, defined as BLA = |(R₁ + R₃ + R₈)/3 – (R₂ + R₄ + R₉)/3| (Scheme 1).

the different metal ions and the oxygen and nitrogen atoms were 1.792–2.422 Å and 1.924–3.886 Å, respectively. These data not only revealed strong O···Mⁿ⁺ and N···Mⁿ⁺ charge transfer interactions, but also indicated the metal ion location in the complexes. The bond length alternation (BLA) value, defined as the absolute value of the difference between the average length of single and double bonds, is a quantitative tool to evaluate the degree of π -conjugation in a molecule with conjugated bonds. Smaller BLA values imply greater π -conjugation in the system. Compared with monovalent cations, complexation with divalent cations sharply decreased the BLA value of the naphthoxazine moiety (~0.001 Å vs. ~0.056 Å, as shown in Table 1), indicating greater π -conjugation in the system and further demonstrating that the two isolated π -conjugated parts in spirooxazine can become extensively conjugated upon the introduction of metal ions, which is associated with large hyperpolarizability NLO responses.

3.2 NBO analysis

The NBO charges of the metal cations are listed in Table 1. For the alkali and alkaline-earth metal cation derivatives (Li⁺, Na⁺, K⁺, Mg²⁺, and Ca²⁺), the metal charges decreased slowly with respect to the free metal cations. However, for transition metal cation compounds, the metal charge decreased moderately for Zn²⁺ and Ag⁺, but significantly for Fe²⁺. This large decrease was attributed to stronger Fe²⁺ complexation with the naphthoxazine moiety, as evidenced by analysis of the NBO second-order interaction energies, which provide a further interpretation of the stabilizing effect of the metal ions, as calculated using the following equation:

$$E_2 = \Delta E_{ij} = q_i \frac{F^2(i, j)}{\epsilon_j - \epsilon_i} \quad (3)$$

where q_i is the donor orbital occupancy, ϵ_i and ϵ_j are the diagonal elements (orbital energies) of the Fock matrix, and $F_{(ij)}$ is the off-diagonal NBO Fock matrix element. The stabilization energy, E_2 , indicates the strength of donor–acceptor interactions, as summarized in Table S1.† The calculated results showed that the interaction energies, E_2 , of most MC*Mⁿ⁺ species were mainly attributed to the lone pair electrons (LP) of

oxygen atoms and partial nitrogen atoms, and the LP* (one-center valence antibonding lone pair) of the metal cations (Li⁺, Na⁺, K⁺, Mg²⁺, Ca²⁺, and Ag⁺). Interactions between the lone pair electrons of the electron-donating oxygen atom and the LP* orbitals of Mⁿ⁺ were much stronger than those between the nitrogen atom lone pairs and the Mⁿ⁺LP*, except for compounds containing metal cations with strong interactions with oxygen and nitrogen atoms (Fe²⁺ and Zn²⁺), as indicated by their stabilization energies, E_2 (Table S1†). Larger stabilization interaction energies, E_2 , are known to cause stronger interactions between the bonds.^{48–52} Therefore, the results suggested that Fe²⁺ complexation was stronger, which was in good agreement with the reduced N···O distance between the ligand heads (from 2.825 Å in uncomplexed merocyanine to 2.549 Å in the Fe²⁺ complex). Furthermore, the E_2 value would increase with decreasing metal center charge. As shown in Tables 1 and S1,† the calculated E_2 values increased in the order MC*K⁺ < MC*Na⁺ < MC*Li⁺ < MC*Ag⁺ for monovalent metal complexes and MC*Ca²⁺ < MC*Mg²⁺ < MC*Zn²⁺ < MC*Fe²⁺ for divalent metal complexes. Meanwhile, the charge on the metal was in the order MC*K⁺ < MC*Na⁺ < MC*Li⁺ < MC*Ag⁺ for monovalent

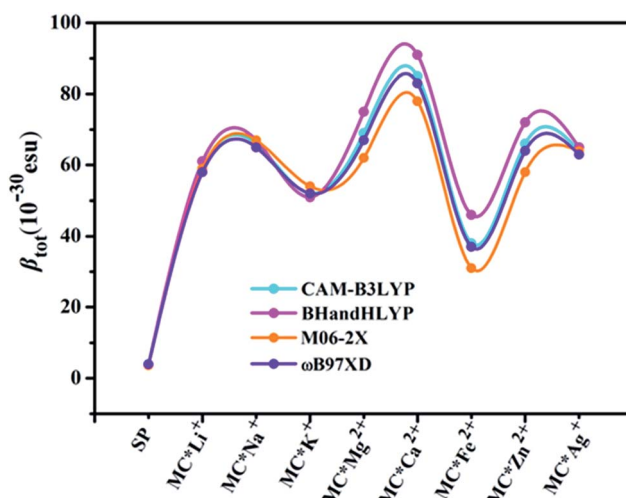


Fig. 1 Relationships between complex β_{tot} values computed at various levels of theory.



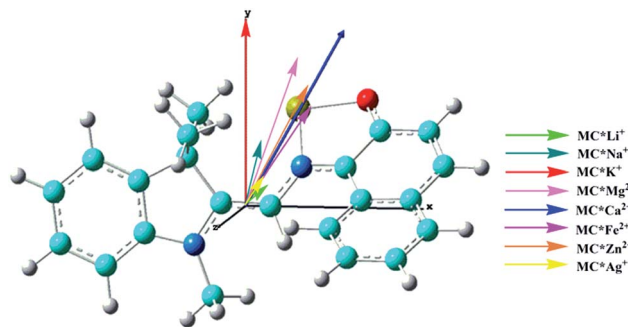


Fig. 2 Components of dipole moment (scale = 0.5) of the metal cation complexes MC^*M^{n+} . Carbon (light blue), hydrogen (white), nitrogen (blue), oxygen (red), and the cation (yellow).

metal complexes and $MC^*Ca^{2+} < MC^*Mg^{2+} < MC^*Zn^{2+} < MC^*Fe^{2+}$ for divalent metal complexes.

3.3 First hyperpolarizability

Quantum chemistry calculations can aid understanding of the relationship between molecular structure and NLO properties, and prescreen molecules with large NLO responses.^{53–55} As no experimental or theoretical β_{tot} values were available for the studied compounds, a comparative discussion of the results obtained using different DFT methods (see Table 3) was useful. Here, four DFT functionals (CAM-B3LYP, BHandHLYP, M06-2X, and ω B97XD), were used to assess the effect of DFT functionals on the first hyperpolarizability. Notably, the β value of the four functionals varied within a small margin for SP and the monovalent metal complexes (Table S2† and Fig. 1). However, BHandHLYP can give relatively large β values, while M06-2X underestimates β values, which seem to be comparable with the CAM-B3LYP result, providing a consistent first hyperpolarizability picture with respect to the method ω B97XD for divalent metal complexes. Moreover, recent studies show that the first hyperpolarizabilities predicted by CAM-B3LYP are similar to those obtained by MP2.^{56–58} Therefore, we used the CAM-B3LYP results as an example to assess the multistate second-order NLO behaviors of the complexes studied. Moreover, five Pople's basis sets (6-31+G(d), 6-31++G(d), 6-31+G(d,p), 6-31++G(d,p), and 6-311++G(d,p)) were chosen to evaluate the effect of the basis set at the CAM-B3LYP level for MC^*Ca^{2+} (Table S3†). Compared with the 6-31+G(d) basis set, using the slightly extended basis set with an added p polarization function led to a slight decrease in β_x , resulting in a smaller β_{tot} . Likewise, using the more diffuse 6-31++G(d) basis set, β_x decreased slightly, along with an increase in β_z values. However, for the triple split valence basis set 6-311++G(d,p), adding diffuse and polarization functions resulted in an overestimation of β_x , β_y , β_z , and β_{tot} values from their 6-31+G(d) values. Therefore, we used only the 6-31+G(d) basis set as an example to shed light on changes in the first hyperpolarizabilities of the complexes studied (except for transition metals). The solvent effect is known to be important for first hyperpolarizability calculations. As typical examples, β_{tot} values for SP, MC^*K^+ , MC^*Ca^{2+} , MC^*Fe^{2+} , and MC^*Zn^{2+} were calculated using the

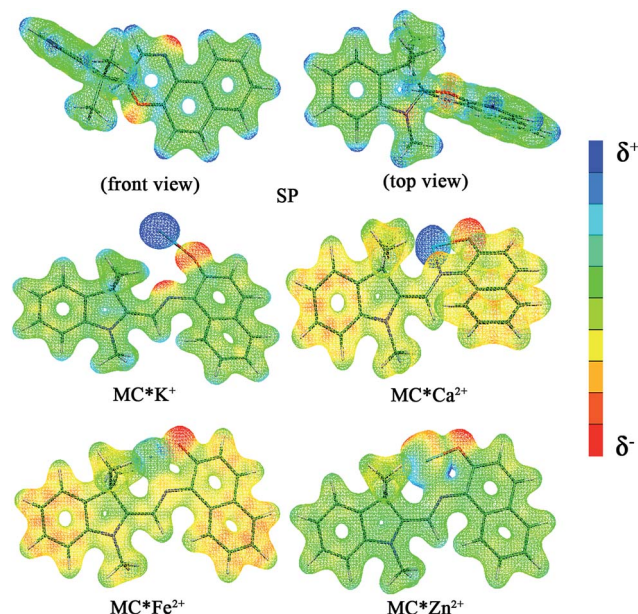


Fig. 3 Electrostatic potentials of SP, MC^*K^+ , MC^*Ca^{2+} , MC^*Fe^{2+} , and MC^*Zn^{2+} .

different functionals (CAM-B3LYP, BHandHLYP, M06-2X, and ω B97XD) and basis sets (6-31+G(d) and LanL2DZ), via the PCM model, which simulated the solvent effect (with methanol as the solvent). We chose methanol as the solvent because it was used in related experiments. The results are listed in Table S4,† and clearly show that the β_{tot} values in methanol solvent are larger than those in the gas phase, but variation tendencies remaining the same, with β_{tot} values 10–21 times higher after the metal ions were added. The regularity of the β_{tot} values remained the same in gas-phase and methanol-solvent conditions. The calculation in the gas phase can be proved to be reasonable. Therefore, we used the gas phase results to discuss the second-order NLO behaviors of the complexes studied.

The calculated first hyperpolarizability (β_{tot}) values of the studied compounds at the 6-31+G(d) (LanL2DZ basis set for the transition metal ion) level are given in Table 3. For these compounds, the origin of the Cartesian coordinate system was located in the middle of the C1–C2 bond in the metal complexes (Fig. 2), and in the xy -plane with the central C1–O1

Table 2 Dipole moments (Debye), individual components of first hyperpolarizabilities (a.u.), and total first hyperpolarizabilities (10^{-30} esu) computed at the CAM-B3LYP/6-31+G(d)/LanL2DZ level of theory

Compound	μ_x	μ_y	μ_{tot}	β_x	β_y	β_z	β_{tot}
SP	−0.26	−0.67	0.77	0.5	−3.9	−1.0	4.0
MC^*Li^+	1.25	1.03	1.62	−50.0	−31.9	1.4	59.3
MC^*Na^+	0.83	3.54	3.67	−58.2	−30.9	5.5	66.1
MC^*K^+	−0.07	10.56	10.57	−41.3	−31.8	3.1	52.3
MC^*Mg^{2+}	2.96	8.11	8.67	−55.9	−39.5	6.5	68.7
MC^*Ca^{2+}	4.39	8.64	12.11	−75.3	−33.8	18.9	84.6
MC^*Fe^{2+}	3.66	5.28	6.52	−20.0	−32.8	0.3	38.4
MC^*Zn^{2+}	3.60	6.52	7.45	−50.6	−41.6	6.1	65.8
MC^*Ag^+	1.07	1.68	2.14	−53.4	−34.0	4.6	63.5

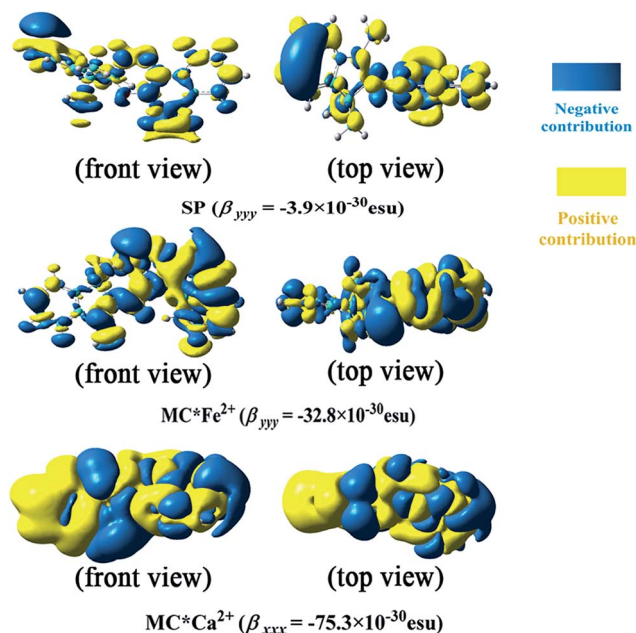


Fig. 4 Electronic density (isovalue = 7) of first hyperpolarizability at the CAM-B3LYP/6-31+G(d)/LanL2DZ level.

bonds, and x -axis along with naphthoxazine moiety in SP (Scheme 1). Before discussing the first hyperpolarizabilities, it is worth studying the dipole moments. The dipole moments of the metal cation complexes were obviously larger than that of SP. This meant that the complexation of SP with metal cations significantly enhanced the dipole moment, due to the strong positive charge of the metal cation. The principal component of dipole moment was μ_y for all the compounds studied

(except for MC^*Li^+ , for which it was μ_x) and its sign was positive. The orientation of the dipole moment remained in the positive direction of the y -axis and was aligned with the center of indoline and naphthoxazine in the metal axis (Fig. 2). The size of the dipole moment and the positive metal cation charge separation was clearly implied by the total electrostatic potentials. As typical examples, the total electrostatic potentials of SP, MC^*K^+ , $\text{MC}^*\text{Ca}^{2+}$, $\text{MC}^*\text{Fe}^{2+}$, and $\text{MC}^*\text{Zn}^{2+}$ are plotted in Fig. 3. As shown, the important region of positive charge is the metal cation fragment. In contrast, the net negative charge is mostly located on the oxygen atom of the naphthoxazine fragment. This charge distribution led to large dipole moments in the complexes studied.

As mentioned above, the separation of charges is large, inevitably leading to a large first hyperpolarizability. For SP, the calculated β_{tot} value was only 4.1×10^{-30} esu. With the introduction of metal ions, prominent reinforcement of second-order NLO responses was obtained with enhanced β_{tot} values (38.4×10^{-30} esu for $\text{MC}^*\text{Fe}^{2+}$ and 84.6×10^{-30} esu for $\text{MC}^*\text{Ca}^{2+}$), which were about 10–21 times larger than that of SP. Consequently, these improved β_{tot} values for MC^*M^{n+} were also due to the formation of larger π -conjugated system with the aid of metal ions, which, as is mentioned previously regarding BLA values, also play a vital and predominant role in the selection of metal cations. Therefore, SP can be used for selective sensing or NLO-based detection of cations.

For all compounds, the β_x component was dominant (except for SP and $\text{MC}^*\text{Fe}^{2+}$, for which β_y was dominant) in describing the β_{tot} responses, compared with β_y and β_z components, suggesting that, during polarization, electronic charge transfer is expected along the x -axis. However, intramolecular charge transfer of naphthoxazine along the y -axis occurs in SP, and

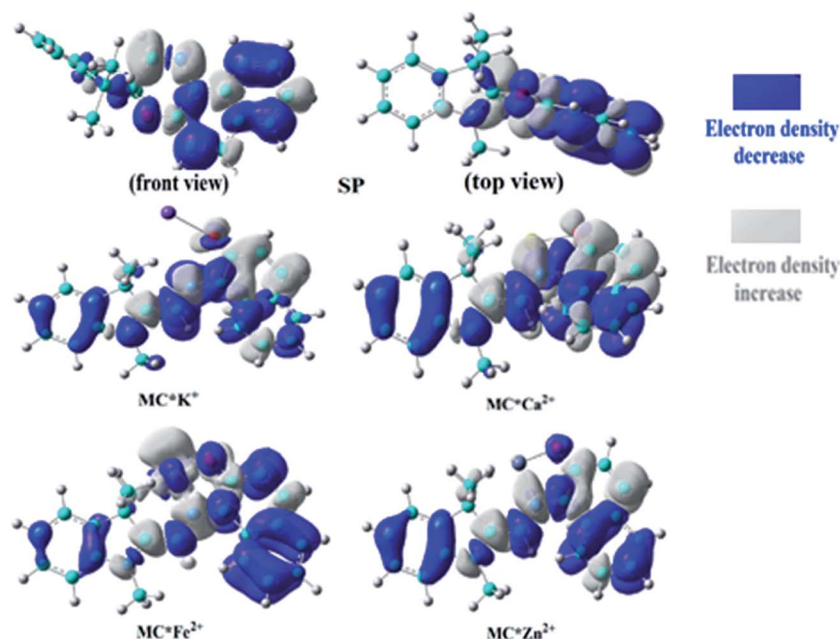


Fig. 5 Electron density differences in SP, MC^*K^+ , $\text{MC}^*\text{Ca}^{2+}$, $\text{MC}^*\text{Fe}^{2+}$, and $\text{MC}^*\text{Zn}^{2+}$ from the ground state to the crucial excited state, calculated at the $\omega\text{B97XD}/6-31+\text{G}(\text{d})/\text{LanL2DZ}$ level.



a small amount of charge transfer from the naphthoxazine fragment to metal remains in MC*Fe²⁺.

We also examined the spatial contributions of different molecular regions to the static first hyperpolarizability using the hyperpolarizability density^{59,60} in the finite field (FF). As is well known, the dipole moment $\mu(\vec{F})$ can be Taylor expanded in powers of the external field, \vec{F} , as

$$\mu(\vec{F}) = -\frac{\partial E}{\partial \vec{F}} = \mu_0 + \alpha \vec{F} + \frac{1}{2} \beta \vec{F}^2 + \frac{1}{6} \gamma \vec{F}^3 + \dots \quad (4)$$

Similarly, Taylor expansion of the electron density function $\rho(\vec{r}, \vec{F})$ can also be conducted as

$$\rho(\vec{r}, \vec{F}) = \rho^{(0)}(\vec{r}) + \rho^{(1)}(\vec{r})\vec{F} + \frac{1}{2}\rho^{(2)}(\vec{r})\vec{F}^2 + \frac{1}{6}\rho^{(3)}(\vec{r})\vec{F}^3 + \dots \quad (5)$$

From eqn (4) and (5), static β can thus be expressed as

$$\beta = \int -\rho^{(2)}(\vec{r}) \cdot \vec{r} d\vec{r} \quad (6)$$

where

$$\rho^{(2)}(\vec{r}) = \left. \frac{\partial^2 \rho(\vec{r})}{\partial \vec{F}^2} \right|_{\vec{F}=0} \quad (7)$$

This second-order derivative of electron density with respect to the applied electric field is referred to as the β density. In this study, we confine our attention to the β density $\rho^{(2)}(\vec{r})(\rho_{xx}^{(2)}(\vec{r}))$ corresponding to β_{xxx} , which is the most crucial component of β in the metal cation complexes, except for MC*Fe²⁺ (Table 2). In this section, we focus on the MC*Ca²⁺ complex because it has electronic distributions similar to those of MC*Li⁺, MC*Na⁺, MC*K⁺, MC*Mg²⁺, MC*Zn²⁺, and MC*Ag⁺ along the x-axis. Moreover, $\rho_{yy}^{(2)}(\vec{r})$ is related to β_{yyy} and is the most significant component for SP and MC*Fe²⁺. These $\rho_{xx}^{(2)}(\vec{r})$ and $\rho_{yy}^{(2)}(\vec{r})$ can be calculated at each spatial point in discretized space using the following second-order numerical differentiation formulas:

$$\rho_{xx}^{(2)}(\vec{r}) = \frac{\rho(\vec{r}, F^x) - 2\rho(\vec{r}, 0) + \rho(\vec{r}, -F^x)}{(F^x)^2} \quad (8)$$

$$\rho_{yy}^{(2)}(\vec{r}) = \frac{\rho(\vec{r}, F^y) - 2\rho(\vec{r}, 0) + \rho(\vec{r}, -F^y)}{(F^y)^2} \quad (9)$$

where $\rho(\vec{r}, F^x)$ or $\rho(\vec{r}, F^y)$ represent the electron density at spatial point \vec{r} in the presence of electric field F^x or F^y , respectively. The applied electric fields along the x-axis and y-axis were 0.003 a.u. The electron densities over a three-dimensional grid of points were evaluated using the CAM-B3LYP functional with 6-31+G(d) (LanL2DZ for transition metal ion) from the Gaussian 09 program package.

In this work, the visualized results of the $-x\rho_{xx}^{(2)}(\vec{r})$ function, together with β_{xxx} values of the studied MC*Ca²⁺ system, and the $-y\rho_{yy}^{(2)}(\vec{r})$ function, together with β_{yyy} values of the studied SP and MC*Fe²⁺ systems, at the CAM-B3LYP/6-31G(d)/LanL2DZ level, are illustrated in Fig. 4. The total magnitudes of β_{xxx} and β_{yyy} are decomposed into positive (yellow) and negative (blue) parts. For SP, negative contributions were primarily distributed on the indoline side, compared with the sparse positive contributions distributed on the naphthoxazine side. It was not surprising that SP provided a rather small negative β_{yyy} value (-3.9×10^{-30} esu). In contrast, relatively large negative contributions were present on the naphthoxazine side in MC*Fe²⁺. MC*Ca²⁺ contained remarkably large negative contributions, principally distributed in the naphthoxazine fragment and the inner regions of the indoline fragment, and, hence, gave a considerably large negative β_{xxx} value (-75.3×10^{-30} esu).

3.4 TDDFT studies

To understand the first hyperpolarizability values, TD-DFT calculations of the studied complexes were carried out at the ω B97XD/6-31+G(d)/LanL2DZ level. In SP, the naphthoxazine moiety serving as an electron donor contained the majority of

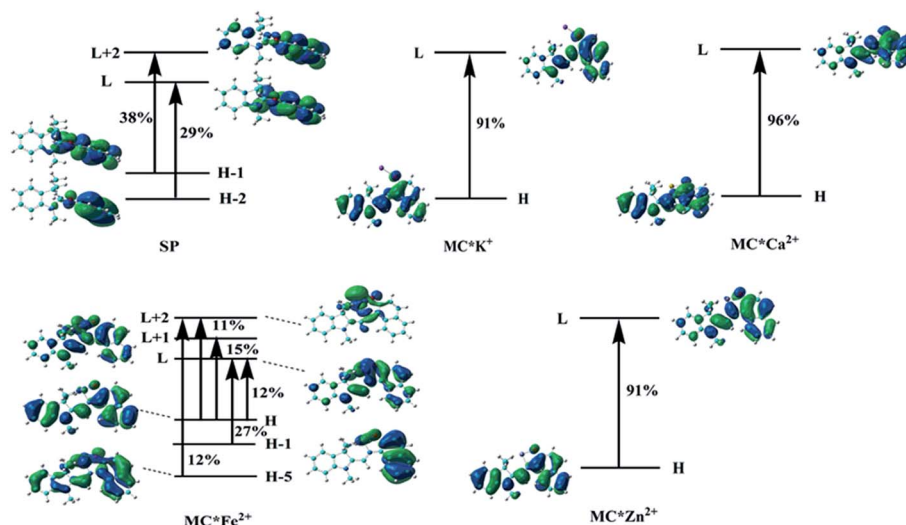


Fig. 6 Molecular orbitals involved in the main excited states contributing to the β_{tot} values.



Table 3 Energies, oscillator strengths, and major contributions of SP, MC*K⁺, MC*Ca²⁺, MC*Fe²⁺, and MC*Zn²⁺ at the ω B97XD/6-31+G(d)/LanL2DZ level

Compound	State	Wavelength (nm)	ΔE (eV)	Oscillator (f_{os})	MO transition
SP	S8	224	5.53	0.55	H ^a −2 → L (29%), H−1 → L+2 (38%)
MC*K ⁺	S1	490	2.53	0.64	H → L (91%)
MC*Ca ²⁺	S1	615	2.01	0.60	H → L (96%)
MC*Fe ²⁺	S7	523	2.37	0.26	H−5 → L+2 (12%) H−1 → L (27%) H → L (12%) H → L+1 (15%) H → L+2 (11%) H → L (91%)
MC*Zn ²⁺	S1	587	2.11	0.61	H → L (91%)

^a H = HOMO, H−1 = HOMO−1, L = LUMO, L+1 = LUMO+1, etc.

occupied molecular orbitals. The orthogonality of the indoline and naphthoxazine moieties led to little overlap between the orbital pairs, resulting in the generation of a weak CT transition between the naphthoxazine moieties. Meanwhile, the transition energy of SP was rather large (5.53 eV), as observed *via* electron density difference plots (Fig. 5). For MC*Fe²⁺, the crucial excited state was formed by the orbits of the HOMO−1 → LUMO and HOMO → LUMO+1 transitions. The HOMO and HOMO−1 were found to be localized on the whole merocyanine molecule and naphthoxazine unit, respectively, while the LUMO and LUMO+1 were localized on the metal center and naphthoxazine unit, respectively. A partial area of overlap between these transitions would generate a charge transfer from the naphthoxazine unit to the metal center, and thus this excited state contained the ligand-to-metal charge-transfer (LMCT) transition. From the electron density difference plot of MC*Fe²⁺, we also noted that there were some π − π^* and π −d contributions, and slightly weak CT transitions over the MC*Fe²⁺. However, for MC*K⁺, MC*Ca²⁺, and MC*Zn²⁺, there were no contributions from these molecular orbitals to the metal center. These first transitions were dominated by HOMO-to-LUMO singly excited electronic

configurations, and were assigned as π − π^* transitions displaying better charge transfer character from the indoline to the naphthoxazine moiety (see Fig. 6). It was also noted that the direction of charge transfer in the coplanar MC series (MC*K⁺, MC*Ca²⁺, and MC*Zn²⁺) was along the *x*-axis, inevitably resulting in negative β_x values. Furthermore, these complexes with larger π -conjugation, lower excited energy, and stronger oscillator strength might be promising for generating a large increase in static first hyperpolarizability.

Molecular NLO properties are closely related to electronic absorption characteristics. Therefore, the static first hyperpolarizability can be elucidated from the electronic absorption characteristics using the two-level model established by Oudar and Chemla,^{61,62} with relevant parameters shown in Table 3 and visualized in Fig. 7. The ΔE values of crucial transition states that made that largest contribution to the hyperpolarizabilities are listed in Table 3. The ΔE values increased in the order MC*Ca²⁺ (2.01 eV) < MC*Zn²⁺ (2.11 eV) < MC*Fe²⁺ (2.37 eV) < MC*K⁺ (2.53 eV) < SP (5.53 eV). However, the ΔE value of MC*K⁺ was larger than that of MC*Fe²⁺, indicating that the sequence of β_{tot} values could not be determined only in terms of ΔE values. Therefore, we focused on another factor controlling β_{tot} values, namely, oscillator strength. Intriguingly, the oscillator strength of MC*Fe²⁺ was particularly small, which was mainly attributed to charge transfer from the naphthoxazine unit to the metal center of HOMO−1 and LUMO (because the major CT at this state arises from HOMO−1-to-LUMO). The $f/\Delta E^3$ values of the SP and the metal cation complex varied after the introduction of metal ions, to give the following order SP (0.0032) < MC*Fe²⁺ (0.0196) < MC*K⁺ (0.0397) < MC*Zn²⁺ (0.0648) < MC*Ca²⁺ (0.0723). The β_{tot} values of these complexes were in good agreement.

4. Conclusions

Prototypical SP and MC complexes containing various metals (MC*Ca²⁺, MC*Mg²⁺, MC*Fe²⁺, MC*Zn²⁺, and MC*Ag⁺) were synthesized, and DFT calculations were employed, along with three additional reference MC compounds (MC*Li⁺, MC*Na⁺ and MC*K⁺), to theoretically investigate electronic absorption characteristics and predict static second-order NLO responses.

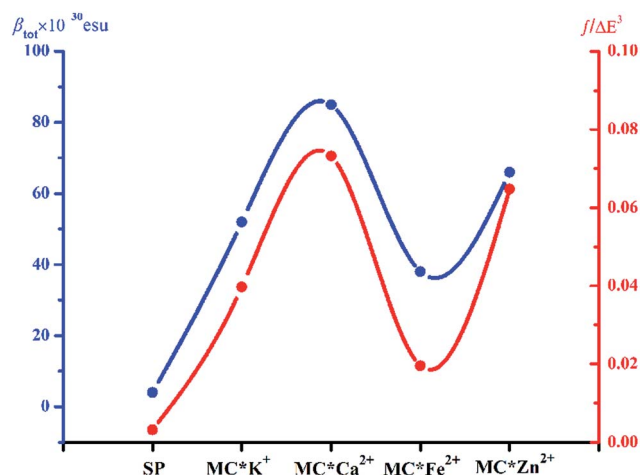


Fig. 7 Relationship between the β_{tot} values (blue curve) and corresponding $f/\Delta E^3$ values (red curve) of complexes SP, MC*K⁺, MC*Ca²⁺, MC*Fe²⁺, and MC*Zn²⁺.



Using various functionals, DFT calculations showed that the introduction of various metals into spirooxazine can drastically enhance second-order NLO switches. For the large conjugated MC*Ca²⁺ compound, the first hyperpolarizability (β_{tot}) increased significantly, due to the obvious charge transfer from the indoline unit to the naphthoxazine unit, large charge distribution, and lower transition energy. In contrast, the β_{tot} values of the Fe²⁺ derivative increased moderately due to the larger amount of charge transferred from the naphthoxazine unit to the metal and the shorter N...O distance between the ligand heads. Consequently, the performances of both prototypical and additional metal compounds in this study showed them to be excellent candidates for optical molecular switches, and further verified the ability of spirooxazine/merocyanine systems to selectively detect alkali, alkaline earth, and transition metal cations.

Acknowledgements

The authors gratefully acknowledge financial support from the "12th Five-Year" Science and Technology Research Project of the Education Department of Jilin Province ([2016] 494) and the National Natural Science Foundation of China (No. 21173035).

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