Ligand-core NLO-phores: a combined experimental and theoretical approach to the two-photon absorption and two-photon excited emission properties of small-ligated silver nanoclusters†

Isabelle Russier-Antoine,a Franck Bertorelle,a Nathalie Calin,b Željka Sanader,c,d Marjan Krstič,c Clothilde Comby-Zerbino,a Philippe Dugourd,a Pierre-François Brevet,a Vlasta Bonačić-Koutecký*c,e and Rodolphe Antoine*a

We report a combined experimental and theoretical study of the two-photon absorption and excited emission properties of monodisperse ligand stabilized Ag11, Ag15, and Ag31 nanoclusters in aqueous solutions. The nanoclusters were synthesized using a cyclic reduction under oxidative conditions and separated by vertical gel electrophoresis. The two-photon absorption cross-sections of these protected noble metal nanoclusters measured within the biologically attractive 750–900 nm window are several orders of magnitude larger than that reported for commercially available standard organic dyes. The two-photon excited fluorescence spectra are also presented for excitation wavelengths within the same excitation spectral window. They exhibit size-tunability. Because the fundamental photophysical mechanisms underlying these multiphoton processes in ligand protected clusters with only a few metal atoms are not fully understood yet, a theoretical model is proposed to identify the key driving elements. Elements that regulate the dipole moments and the nonlinear optical properties are the nanocluster size, its structure and the charge distribution on both the metal core and the bound ligands. We coined this new class of NLO materials as "Ligand-Core" NLO-phores.

Introduction

Two-photon absorption (TPA) defined as the electronic excitation of a molecular system induced by the simultaneous absorption of a pair of photons was first proposed theoretically by M. Göppert-Mayer in 1931.1 TPA was then only demonstrated experimentally in 1961, soon after the invention of the laser.2 TPA is obtained with photons at a frequency half of the actual energy gap between the ground and excited states. As a result, for transitions in the visible to blue side of the optical spectrum, TPA is readily accessible with the femtosecond pulses delivered by standard femtosecond oscillators with a wavelength tunability in the 700–1300 nm range. This is therefore a definite advantage to access a deeper penetration depth into the heavily scattering biological tissue media. TPA has thus gained a widespread popularity in the biology community especially in the development of microscopy. Other applications like photodynamic therapy with in situ photon conversion have also been recently proposed as an alternative method to the more conventional one-photon absorption (OPA) one. Besides the deeper penetration depth of long wavelength irradiation into tissues, a gain in the spatial resolution is also observed owing to the multiphoton character of the interaction of light with the medium.3 Similarly, the technique of two-photon excited fluorescence (TPEF), that entails a TPA process in the first stage before emission of the fluorescence...
photon, is also gaining a widespread popularity within the same community. Here, the advantages not only lie in the increased penetration depth in tissues but also in the reduced background fluorescence of the images collected.

Within this context, considerable efforts have been made to engineer molecular systems or nanoparticles with the largest TPA and TPEF cross-sections. Interestingly, it is also attractive to compare these cross-sections with their molecular first hyperpolarizability. The latter is the cross-section for the process of frequency doubling better known as Second Harmonic Generation (SHG). SHG relies on the quadratic or first hyperpolarizability whereas TPA and TPEF rely on the cubic nonlinearity or second hyperpolarizability. In the case of SHG for instance, the standard class of molecular systems is known as asymmetric push–pull chromophores whereas for the TPEF process it is rather customary to have centrosymmetric systems. Push–pull chromophore systems consist of donor and acceptor end-groups connected by a charge conjugation path. The latter introduces the possibility of a large charge transfer along the conjugated molecular axis upon excitation. Recently, Ågren and collaborators have proposed a simple relationship between the metric of the charge transfer excitation \( \Delta r \) of a bright \( \pi-\pi^* \) state, involved in the first hyperpolarizability, and the two-photon absorption cross-section for two families of push–pull \( \pi \)-conjugated systems. \(^8\) The change in the dipole moment upon excitation \( \Delta \mu \) can also be viewed as a measure of the average hole–electron distance upon excitation and can therefore be used to link hyperpolarizability values to the conjugated chain length of push–pull systems. While extremely appealing as efficient chromophores, for quadratic and cubic nonlinear processes, such push–pull \( \pi \)-conjugated systems. \(^8\) The change in the dipole moment upon excitation \( \Delta \mu \) can also be viewed as a measure of the average hole–electron distance upon excitation and can therefore be used to link hyperpolarizability values to the conjugated chain length of push–pull systems. While extremely appealing as efficient chromophores, for quadratic and cubic nonlinear processes, such push–pull \( \pi \)-conjugated systems.

Noble metal nanoclusters constitute another route to provide efficient linear optical (LO)\(^9\) and NLO-phores. \(^10\) The search for ultra-bright emitting metal nanoclusters has been developed over the last 12 years or so using the concept of a ligand shell protected metal core. The latter core is however composed of only a few metal atoms in order to avoid developing a surface plasmon resonance. \(^11\) Different ligand shell templates have been proposed, from small organic compounds \(^13,14\) to larger proteins, \(^15\) DNA \(^16\) and dendrimers for example. \(^17\) Such nanoclusters then display intense luminescence with long Stokes shifts and long lifetimes along with good photostability. \(^18\) In addition, the use of peptides or proteins as templates brings a good biocompatibility and low cytotoxicity, rendering these nanoclusters highly appealing for bioimaging applications. \(^19\) Moreover, these nanoclusters display giant TPA cross sections in the NIR region as shown by Goodson and collaborators \(^20\) and more recently by our group. \(^21,22\) In particular, biocompatible glutathione capped gold nanoclusters are excellent one- and two-photon excited fluorescence (OPEF and TPEF) contrast agents for live cell imaging, as proposed by Polavarapu et al. \(^23\)

However, predicting the emission properties upon one- and two-photon excitation in these nanoclusters remains a difficult task. Radiative de-excitation pathways involving either metal–metal transitions within the metal core or ligand-to-metal and ligand-to-metal–metal charge transfer (LMCT and LMMCT, respectively) transitions are rather efficient. \(^24\) It is the purpose of this contribution to propose through a combined experimental and theoretical study of concepts to design ligand protected nanoclusters with large cross-sections for quadratic and cubic nonlinear processes based on the interplay between the ligand role and the non-uniform delocalisation of electrons within the metal core.

In a recent communication, we have reported theoretical results on the TPA cross section of small thiolated silver nanoclusters \( \text{Ag}_{15} \) where \( L \) stands for the –SH ligand. This system exhibits an extremely large TPA cross-section on the red side of the visible spectrum. \(^26\) Such large TPA cross-sections at long wavelengths are indeed expected when a resonance between a TPA and an OA process to the final excited state occurs. Also, the leading excitations in states yielding large TPA cross-sections always involve ligands and not just the metal core. The TPA process is accompanied by a large charge transfer upon excitation. In the present work, we have adapted our size-focusing separation method to produce glutathione (SG) ligand protected \( \text{Ag}_{11}, \text{Ag}_{15} \) and \( \text{Ag}_{31} \) nanoclusters. This achievement allows us to explore the size effect on the TPA and TPEF cross-sections. The size influences the optical band gap and then both the resonance effects and the charge transfer effects. Both result from a change in the metal core charge distribution, including the confinement of core electrons. A thorough comparison of the experimental findings with DFT and TDDFT calculations therefore allowed us to reveal the structural and electronic properties of these low nuclearity liganded silver nanoclusters constituting the new class of non-linear nanomaterials termed “Ligand-Core” NLO-phores.

### Results and discussion

#### Linear optical properties

Three of the smallest silver nanoclusters, previously denoted as bands 1, 2, and 6 in the synthesized mixtures obtained by Bigioni and collaborators\(^27\) were produced in a “size-focusing” way using a cyclic reduction under oxidative conditions. \(^28,29\) Two of these species have been formally identified previously using electrospray-ionization (ESI) mass spectrometry (MS) as \( \text{Ag}_{15}(\text{SG})_{10} \) (band 6) and \( \text{Ag}_{15}(\text{SG})_{11} \) (band 2). \(^29\) The smallest size (band 1) has been identified as the \( \text{Ag}_{15}(\text{SG})_2 \) species in a recent study. \(^10\) PAGE and ESI-Time-Of-Flight (TOF) MS analysis on band 1 in water/methanol (50/50 v/v) are shown for this band in Fig. S1 and S2. \(^1\) Two charge states for \( \text{Ag}_{15}(\text{SG})_2 \) were observed, namely \( [M - 2H^+]^{2+} \) and \( [M - 3H^+]^{3+} \), in the mass spectra. In addition to \( \text{Ag}_{15}(\text{SG})_7 \), minor \( \text{Ag}_{14}(\text{SG})_1 \) species along with fragmented species were also present in the ESI-MS spectra, see in Fig. S2. \(^1\) In an effort to structurally better characterize our cluster species, we also performed X-ray...
Powder Diffraction [see Fig. S3†]. For Ag$_{31}$(SG)$_{19}$, the peak positions correspond to the fcc lattice arrangement for silver. The “metal core” sizes of the silver nanoclusters were estimated according to the broadening of the full width at half-maximum of the (111) diffraction peak by the Debye–Scherrer formula. These sizes are in reasonable agreement with the ones obtained using the DFT structures reported in this work (see Fig. 3 and Table S1 in the ESI†).

Optical absorption and fluorescence spectra for the three nanocluster sizes, namely Ag$_{11}$(SG)$_{7}$, Ag$_{15}$(SG)$_{11}$ and Ag$_{31}$(SG)$_{19}$, were then recorded, as shown in Fig. S4.† The Ag$_{15}$(SG)$_{11}$ and Ag$_{11}$(SG)$_{7}$ absorption spectra are rather similar. They do not exhibit prominent features, only a monotonous increase of the absorption at wavelengths below 600 nm with a plateau between 400 and 500 nm. In contrast, the Ag$_{31}$(SG)$_{19}$ absorption spectrum shows a large characteristic peak centered at about 490 nm with an absorption onset near 700 nm. This band is attributed to a core-to-core excitation within the metal core, from the P-cluster-core orbital to the D-cluster-core-orbital. The fluorescence spectra for these nanoclusters were also recorded, as shown in Fig. S4b.† All solutions were excited at 450 nm. Ag$_{15}$(SG)$_{11}$ and Ag$_{11}$(SG)$_{7}$ display similar fluorescence spectra with a broad emission band centred at about 700 nm. Ag$_{31}$(SG)$_{19}$ though presents a small blue-shift of its emission band as compared to Ag$_{11}$(SG)$_{7}$ and Ag$_{15}$(SG)$_{11}$, respectively, using DCM dye as the reference. Ag$_{31}$(SG)$_{19}$ is found to be extremely weakly fluorescent upon one-photon excitation at 450 nm. A slowly rising onset of fluorescence appears though in the NIR region but remains very low. While the present spectra for Ag$_{15}$(SG)$_{11}$ and Ag$_{11}$(SG)$_{7}$ are in qualitative agreement with those reported by Bigioni and collaborators, they clearly disagree for band 6. Indeed, Ag$_{31}$(SG)$_{19}$ is here found to be non-fluorescent whereas clusters in band 6 were previously found to be fluorescent in ref. 34 with a behaviour very similar to those of Ag$_{15}$(SG)$_{11}$ and Ag$_{11}$(SG)$_{7}$. We speculate that this discrepancy may arise from the synthesis as band 6 was previously attributed to the Ag$_{12}$(SG)$_{19}$ stoichiometry. One may therefore argue that the Ag$_{31}$ and Ag$_{12}$ metal cores introduce very different absorption and fluorescence properties. Note also that two small peaks at 335 and 635 nm were reported in the Ag$_{12}$ absorption spectra, peaks that we do not observe in our synthesis, see Fig. S4.†

**Two-photon excited fluorescence spectra**

TPEF spectra with an excitation at 800 nm were recorded for the Ag$_{11}$(SG)$_{7}$, Ag$_{15}$(SG)$_{11}$ and Ag$_{31}$(SG)$_{19}$ nanoclusters, see Fig. 1. A broad band in the visible range between 400 and 650 nm with a large characteristic peak centered at about 530 nm is observed for Ag$_{31}$(SG)$_{19}$, whereas the TPEF spectra are red-shifted between 550 and 750 nm for Ag$_{11}$(SG)$_{7}$ and Ag$_{15}$(SG)$_{11}$. Also, while the TPEF and OPEF spectra are closely related for Ag$_{11}$(SG)$_{7}$ and Ag$_{15}$(SG)$_{11}$, the TPEF spectrum for Ag$_{31}$(SG)$_{19}$ is dramatically contrasted as compared to its linear OPEF counterpart where only an extremely weak emission in the NIR is observed, see Fig. 1. This Ag$_{31}$(SG)$_{19}$ TPEF spectrum though bears some similarity with the corresponding absorption spectrum. Fig. S5† reports the same TPEF spectrum albeit with an excitation at 780 nm but no change as compared to an excitation at 800 nm is observed. Such a difference between the emission spectra resulting from one or two photon excitation has already been reported for Ag$_{29}$ silver nanoclusters in a previously reported study. One reason for this difference stems from a high symmetry dependence of the fluorescence spectra because OPEF and TPEF processes do not obey the same selection rules. The differences observed between the OPEF and TPEF spectra may therefore be accounted for by the different electronic distributions in the states involved in the metal-to-metal excitation within the silver nanocluster core and the LMCT and LMMCT excitations. We attempted to determine the TPA and TPEF cross-sections for these silver nanoclusters, using the methods reported in our previous studies. Experimentally, we found that the TPEF cross-sections at 800 nm excitation are $3.3 \times 10^{-4}$, 0.00169 and 0.066 GM for the Ag$_{11}$(SG)$_{7}$, Ag$_{15}$(SG)$_{11}$ and Ag$_{31}$(SG)$_{19}$ nanoclusters, respectively, see Table 1. These experimental TPEF cross-sections are related to the TPA ones through the quantum yield (QY),
namely \( QY = \frac{\sigma_{TPEF}}{\sigma_{TPA}} \), see also Table 1. For the silver nanoclusters, this quantum yield is therefore found to be roughly constant at about \( 5 \times 10^{-3} \% \). Similarly to gold nanoclusters, ligand protected silver nanoclusters are therefore excellent two-photon absorbers but present a limited two-photon emission cross-section due to a rather low quantum yield. Yet, the two-photon quantum yields for these small silver nanoclusters remain about two orders of magnitude higher than that of the gold nanoclusters.

**Two-photon absorption cross section**

In parallel to the two-photon excited emission properties, we also investigated the TPA cross-section as a function of the laser excitation wavelength. Fig. 2 displays the cross-section for different wavelengths for the three nanocluster stoichiometries. Clearly, two trends emerge. First, the larger the nanocluster size, or more precisely the higher the number of silver atoms’ content, the larger is the TPA cross-section. Second, the TPA cross-section increases as the excitation wavelength shortens. Here, it must be emphasized that the TPA cross-sections are reported on a logarithmic scale. The observed effects are therefore large. TPA cross-sections are derived from the imaginary part of the second hyperpolarizability. A simple three-state model, involving a ground, an intermediate and a final state was proposed to qualitatively describe the TPA cross-sections for push–pull organic dye molecules. In this model, the TPA cross-sections depend on the transition energy between the ground to the intermediate and the intermediate to the final state and the related transition dipole moments. The resonance effect describes the possibility to have an excitation resonant at one or two photons between the three states involved. In ligated clusters, the transition dipole moment effect is related to the geometry taken by the core metal atoms and the ligands. These two effects have been further investigated with a theoretical approach.

**Structural, electronic and nonlinear optical properties of small ligand protected silver nanoclusters**

**Insight from theory.** Theoretical investigations of the nonlinear optical properties for the lowest energy structures of the Ag\(_{11}\), Ag\(_{15}\), and Ag\(_{31}\) nanoclusters, where L stands for the \( \text{SCH}_3 \) group, were performed. Although the ligand is different from the \( \text{–SG} \) one used in the experimental work, this study is a first step in confirming that the two effects introduced above are mainly responsible for the amplitude of the TPA, TPEF and first hyperpolarizability of these small clusters. It is obvious that the full computation involving SG ligands would be highly desirable but such a computation is not within reach at the present time due to the resources required. Time dependent density functional theory (TDDFT) calculations were thus performed for the 3 above mentioned nanoclusters. They contain 4, 8 and 12 delocalized electrons within the core as reported in Fig. 3(d–f). Several factors influencing the TPA cross-sections have been identified: (i) the excitation between ligands and the metal core are characteristic of the nonlinear transitions, (ii) the resonance between states involved in the OPA and TPA processes is required to obtain large TPA cross-sections, (iii) large dipole transition moments are related to a non-uniform electron distribution within the metal core. The role of the structural properties, i.e. of the geometry of the metal core in determining this electron distribution, is therefore crucial.

All the above listed factors are illustrated in Fig. 3 and 4. In the case of the Ag\(_{11}\) nanoclusters, the resonance between the OPA process with an excited \( S_1 \) state localised at a wavelength of about 450 nm (see Fig. S4†) cannot be achieved considering a manifold increase of about 100 states within the calculation. The ELF representing delocalized electrons within the core in Ag\(_{11}\) nanoclusters (see Fig. 3d) shows an electron delocalization distributed between all core atoms. This induces low values for the transition dipole moments through LMMCT excitations. For this stoichiometry, the central metal core is formed with one central Ag atom and two symmetrical Ag subunits. In contrast, for the Ag\(_{15}\) and Ag\(_{31}\) nanoclusters, the situation is strikingly different, as illustrated in Fig. 3b and c. First, there is a resonance between the low lying states accessible through OPA and TPA in the spectral range around 500 nm (in the case of Ag\(_{15}\)) and 730 nm (in the case of Ag\(_{31}\)). Second, in both cases, the delocalised electron distributions within the core are non-uniform as shown by the electron localization function (ELF) in the lower part of Fig. 3(e and f). This is a prerequisite for large transition dipole moments of LMMCT excitations involving ligands and the metal core. Notice that in the case of Ag\(_{15}\) with L = \( \text{SCH}_3 \),

Table 1  Two-photon cross sections and quantum yields for Ag nanoclusters excited at 800 nm

<table>
<thead>
<tr>
<th>Silver nanoclusters</th>
<th>TPA cross section (in GM units)</th>
<th>TPEF cross section (in GM units)</th>
<th>Two photon QY (in %)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ag(_{11})(SG)(_7)</td>
<td>6.6</td>
<td>3.3 ( \times 10^{-4} )</td>
<td>4.9 ( \times 10^{-3} )</td>
</tr>
<tr>
<td>Ag(<em>{15})(SG)(</em>{11})</td>
<td>63.5</td>
<td>0.00169</td>
<td>2.7 ( \times 10^{-3} )</td>
</tr>
<tr>
<td>Ag(<em>{31})(SG)(</em>{19})</td>
<td>950</td>
<td>0.066</td>
<td>6.9 ( \times 10^{-3} )</td>
</tr>
</tbody>
</table>

Fig. 2  TPA cross-sections as a function of wavelength for the Ag\(_{11}\)(SG)\(_7\), Ag\(_{15}\)(SG)\(_{11}\), and Ag\(_{31}\)(SG)\(_{19}\) nanoclusters.
the wavelength of the largest cross-sections is blue shifted by 56 nm with respect to the previously published result for Ag15L11 with L = SH,26 thus the structure of the ligands influences the results quantitatively but not qualitatively. Of course, an increase in the size of the metal core induces a red shift of the resonance between OPA and TPA and therefore plays an important role in the context of applications where the excitation wavelength lies in the NIR window.

The influence of changing the charge distribution from uniform to non-uniform on the values of cross-sections is illustrated in Ag11L7 by introducing a positive external charge on the central Ag atom of the metal core. This pushes the electron distribution from the Ag3 group towards the central part of the core. The redistribution of electron density causes the increase of transition dipole moments through LMMCT excitations and induces an increase in TPA, as shown in Fig. 4a and b. However, this underlines that not only the size of the core but also the structure of the metal core responsible for the distribution of the charge might be important for giving rise to large TPA.

Altogether, despite the simplification of the nanocluster ligand nature, our findings suggest that, in addition to the role of ligands as acceptors or donors, the structural properties of the core, responsible for charge distribution of the delocalized electrons, play an important role in the design of large TPA cross-section systems.

The experimental and theoretical values for the TPA cross-sections are in acceptable agreement considering the simplification introduced. However, the wavelengths predicted with the theoretical calculations to yield very high TPA cross-sections are not yet experimentally accessible. From the application point of view, the design of NLO-phores with large TPA cross-sections in the NIR spectral window is desirable and can be realised according to the above proposed criteria.
Concluding remarks

As already observed for Ag29 nanoclusters, it appears that the different selection rules involved for one- and two-photon excitations are indeed playing a critical role in determining cross-sections for TPA, TPEF and SHG processes. In the case of the TPA cross-sections which we have investigated based also on theoretical contributions, a resonance between TPA and OPA is essential. Large transition dipole moments are due to ligand-to-core or inversely core-to-ligand excitations, and are reinforced by a non-uniform electronic distribution in the metal core. Therefore, large dipoles are a consequence of both the structural properties of the metal core and its size. Besides this analysis, the optical band gap decreases as the size of the silver nanoclusters increases, shifting the spectra towards the NIR spectral region, a feature useful for bio-imaging applications. Altogether, an understanding of leading factors governing non-linear properties of ligated small silver nanoclusters presented in this communication allows us to propose novel ligand-core NLO-phores with potential for different applications.

Materials and methods

Experimental

Synthesis and characterization. Glutathione protected Ag (Ag(SG)) nanoclusters were formed by reducing silver nitrate in the presence of excess glutathione, using a method that was similar to that previously reported. For band 1 (Ag12(SG)2) cluster synthesis: 90 mg of glutathione is dissolved in methanol (50 ml) and triethylamine (3 ml). Then 0.5 ml of silver trifluoroacetate solution is added (64 mg ml−1 in methanol) and the mixture is left undisturbed at 50 °C overnight. After 12 hours later, the mixture is cooled to −10 °C and irradiated with a commercial UV lamp (“black light” lamp type, 365 nm, 25 W). 50 mg (powder) of tetrabutylammonium borohydride is quickly added under agitation. After one hour, 20 mg (powder) of tetrabutylammonium borohydride is added and the solution is agitated for one more hour. Then, clusters are precipitated (and centrifuged) by adding 0.5 ml of 1 M NaOH (or KOH) solution. After being redissolved in water (∼1 ml), 20 ml of methanol is added. The precipitate is centrifuged again. This cycle (dissolution/precipitation/centrifugation) is repeated one more time before drying the powder under vacuum.

For characterization, PAGE separation was carried out by using a vertical gel electrophoresis unit with a size of 0.2 cm × 20 cm × 20 cm. The separating and stacking gels were prepared by acrylamide/bis-(acrylamide) monomers with the total content of 35 wt% (acrylamide/bis-(acrylamide) 94:6). The eluting buffer consisted of 192 mM glycine and 25 mM tris (hydroxymethyl)aminoethane. The as-prepared Ag(SG) clusters were dissolved in a 15% (v/v) glycerol/water solution (6 mg in 100 μl). The sample solutions were loaded onto the stacking gel (10 μl per well) and eluted for 7 h at a constant voltage (150 V) to achieve sufficient separation. After gel separation, our synthesis led to a major band closely located near “band 1”, “band 2” and “band 6” of the Bigioni synthesis.27

X-ray powder diffraction experiments were carried out using a PANalytical EMPYREAN diffractometer with a PIXcel 3D detector using Cu-Kα monochromatic radiation and a High resolution Theta-Theta goniometer. XRD patterns were measured between 12 and 80° in 2θ at room temperature (with a step size of 0.026° and a time per step of 600 s).

NLO experiments. The light source for the present two-photon absorption and emission experiments was a mode-locked femtosecond Ti:sapphire laser delivering at the fundamental wavelength of 800 nm pulses with a duration of about 140 femtoseconds at a repetition rate of 76 MHz. The beam was gently focused by a 5 cm focal length lens to a waist of 10 μm and sent in transmission into a 0.5 cm path length spectrophotometric cuvette. The transmitted light was detected with a large aperture photodiode. The incident power was controlled with a half-wave plate and a polarizing cube. The sample absorption, the concentration of which was set to 1 mM, was then determined as a function of the incident power. Nonlinear absorption was probed using the P-scan (or Power-scan) technique during which the incident power is directly varied and the induced changes in the sample transmission are measured.28 For small nonlinear effects, the absorption coefficient expansion can be reduced to \( a = a_0 + \delta I \) (where \( I \) is the intensity of the incident optical field and \( a_0 \) and \( \delta \) are, respectively, the linear absorption and third order non-linear absorption coefficients). The transmission factor \( T \) of the sample can then be expressed as a function of the intensity using the standard Beer–Lambert law:

\[
T = C e^{−αL} = C e^{−(α + \delta L)} I
\]

where \( C \) is a constant. If the factor \( δL_{\text{eff}} \) (with \( L_{\text{eff}} = \frac{1}{a} \frac{e^{−αL}}{I} \)) is small compared to unity, it is possible to approximate the transmission with the following expression:

\[
T(I) ≈ T(0) − T(0)δL_{\text{eff}} I
\]

where \( T(0) \) is a constant depending on \( C \) and on the linear transmission \( e^{−αL} \). The beam on-axis intensity is expressed as a function of the pulse peak power \( P_c \) measured before the sample:

\[
I = \frac{(1 − R)P_c}{πω_0^2}
\]

where \( R \) is the sample front interface reflection coefficient and \( ω_0 \) is the beam waist. Thus, the transmission can be calculated as a function of the measured power as

\[
T(I) ≈ T(0) − T(0)δL_{\text{eff}} \frac{(1 − R)P_c}{πω_0^2}
\]

indicating a linear dependence between the measured power and the sample transmission. It is possible to extract \( δ \) from the slope of the \( T(P_c) \) vs. \( P_c \) dependence. Typical nonlinear absorption plots are shown in Fig. S6† for silver nanoclusters. As expected, in the absence of the clusters, the plot exhibits a
linear behavior with a slope of unity whereas in the presence of the clusters, a decrease of the transmitted intensity is observed as the absorption increases due to a nonlinear contribution. The calibration of the photodiode signal was obtained prior to the experiment by removing the cuvette and varying the incident power. The TPEF light was collected at an angle of 90° from the incident direction by a 2.5 cm focal length lens. A short pass filter with a cut-off wavelength at 750 nm was placed before the monochromator to minimize the light scattering from the excitation beam at 800 nm. The laser source could be tuned around 800 nm to record similar spectra at a different excitation wavelength. Fig. S7 in the ESI† shows the different pump-powers for Ag(SG) nanoclusters and the pump-power dependence of the fluorescence after an excitation at 800 nm which gave a slope of ~2 suggesting that it is indeed a two-photon excited emission.

Computational. The structural, one- and two-photon (OPA and TPA) absorption properties of ligated silver nanoclusters with \( L = \text{SCH}_2 \) were determined using density functional theory (DFT), time dependent version (TDDFT)\(^{29,37}\) and a quadratic response approach.

For the silver atoms (Ag\(_n\), \( n = 11, 15, 31 \)), the 19-e-relativistic effective core potential (19-e-RECP) from the Stuttgart group\(^{38}\) taking into account scalar relativistic effects has been employed. For all atoms, triple zeta plus polarisation atomic basis sets (TZVP) have been used.\(^{38,39}\) The Perdew–Burke–Ernzerhof (PBE)\(^{40}\) functional and Coulomb-attenuated version of Becke’s three-parameter non-local exchange functional together with the Lee–Yang–Parr gradient-corrected correlation functional (CAM-B3LYP)\(^{41}\) have been employed to determine the structural and optical properties.

For the calculation of the TPA cross section (\( \sigma \))\(^{42}\), the two-photon absorption probability (\( \delta \)) is needed which can be obtained from two-photon absorption transition matrices from the ground to the excited state using either a single residue\(^{8,43}\) or a double residue quadratic response procedure. In the latter case, the sum-over-states (SOS) approach can be used which also contains the dumping factor \( f \) serving to prevent the TPA cross-sections from blowing up near the one-photon resonances. This allowed TPA cross-sections to be adequately corrected when necessary as well as the inclusion of manifold states, usually 20 to 30 excited states. In some cases the “few states” model was used as a simplified version in which only the dominating terms in the two-photon absorption transition amplitude tensor are accounted for.\(^{44}\) For calculations the DALTON\(^{42,43}\) program and its modified version were used.

References


