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# Vibrational nonlinear optical properties of spatially confined weakly bound complexes†

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This study focuses on the theoretical description of the influence of spatial confinement on the electronic and vibrational contributions to (hyper)polarizabilities of two dimeric hydrogen bonded systems, namely  $\text{HCN} \cdots \text{HCN}$  and  $\text{HCN} \cdots \text{HNC}$ . A two-dimensional analytical potential is employed to render the confining environment (e.g. carbon nanotube). Based on the results of the state-of-the-art calculations, performed at the CCSD(T)/aug-cc-pVTZ level of theory, we established that: (i) the influence of spatial confinement increases with increasing order of the electrical properties, (ii) the effect of spatial confinement is much larger in the case of the electronic than vibrational contribution (this holds for each order of the electrical properties) and (iii) the decrease in the static nuclear relaxation first hyperpolarizability upon the increase of confinement strength is mainly due to changes in the harmonic term, however, in the case of nuclear relaxation second hyperpolarizability the anharmonic terms contribute more to the drop of this property.

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## 1 Introduction

The interaction between the electric field and spatially confined quantum objects is intensively investigated in recent years, due to its importance for both fundamental science and the prospects of applications. Great achievements in new technologies for the synthesis of low-dimensional semiconductor structures (e.g. quantum dots, quantum wires or more complicated nanometric semiconductors like quantum rings), whose properties seem to be suitable for optoelectronic devices,<sup>1–3</sup> can be considered as some of the important motivating factors for the development of theoretical models able to cope with the spatial confinement phenomena. The reports from experimental studies on more extended molecular systems, which indicate the possibility of tuning the optical response of molecules encapsulated in different chemical cages, might also be considered as encouraging. For instance, it has been shown quite recently that the second harmonic generation (SHG) efficiencies of push–pull aminopyridine derivatives intercalated into inorganic layered materials are larger than those measured for the pure chromophores.<sup>4</sup> Likewise, the materials consisting of a dye encapsulated inside

metal–organic-framework (MOF) structures are also promising to exhibit large SHG activity.<sup>5</sup> Last but not least, the confinement of organic molecules in two-dimensional nanospace has been reported as an effective strategy to enlarge their two-photon absorption strength.<sup>6–8</sup>

The promising conclusions from experimental works are accompanied by the growing interest in theoretical analyses of the linear and nonlinear optical (L&NLO) properties of confined quantum objects. Usually, in order to describe the behaviour of such systems, the various kinds of analytical potentials are employed. One of the simplest and earliest ideas dates back to 1937, when Michels *et al.* proposed an enclosing of the hydrogen atom inside an impenetrable sphere in order to explore the pressure influence on hydrogen dipole polarizability.<sup>9</sup> Over the years this methodology has been reported in a number of studies allowing us to gain insights into the effect of the confining environment on the dipole moment ( $\mu$ ), polarizability ( $\alpha$ ), first and second hyperpolarizability ( $\beta$  and  $\gamma$ ) of various molecular systems (e.g. H, He, Li, Be, B, C, N, O, F, Ne, Br,  $\text{H}^-$ ,  $\text{F}^-$ ,  $\text{Cl}^-$ ,  $\text{O}^{2-}$ ,  $\text{S}^{2-}$ ,  $\text{H}_2^+$ ,  $\text{H}_2$ , HeH, LiH, LiF, HCl, HF,  $\text{HArF}$ , OCS, HCN,  $\text{CO}_2$ ,  $\text{HCCl}$ ,  $\text{HCCN}$ ,  $\text{HCN} \cdots \text{HCN}_m$ , CO, BF).<sup>10–26</sup>

Even though the list of spatially restricted quantum objects whose L&NLO response has already been investigated is quite long, it is mainly limited to atoms or simple molecules. Besides, in the vast majority of cases, only the purely electronic contributions to the static electric properties of these systems were analysed. In contrast, the studies on vibrational (hyper)polarizabilities of the spatially limited molecular systems are rare,<sup>23,24</sup> although the prominent role of molecular vibrations in various NLO processes

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is quite well recognized for the unconfined molecules (see for example ref. 27–30). The importance of this issue has been revealed only recently, in our study performed on the model linear molecules (HCN, HCCH and CO<sub>2</sub>).<sup>24</sup> As has been demonstrated the electronic contributions can prevail over the vibrational terms for unconfined molecules. However, the spatial confinement modifies the electronic contribution to hyperpolarizabilities to a larger extent than the vibrational one. Thus both counterparts should be considered in the interpretation of the nonlinear optical properties of spatially confined molecules.

Aiming at verifying this conclusion for molecular complexes, in this work we report on the effect of orbital compression on the electronic and vibrational contributions to  $\alpha$ ,  $\beta$  and  $\gamma$  of two dimeric hydrogen bonded (HB) systems, composed of the HCN molecule or its tautomeric form, *i.e.* HCN $\cdots$ HCN and HCN $\cdots$ HNC. Due to the presence of hydrogen bonds, these systems are expected to exhibit significant vibrational hyperpolarizabilities. Hence, it is interesting to shed light on confinement-induced relative changes in the electronic and vibrational properties. Until now, the confinement of HB complexes inside chemical cages was studied mostly in a broader context of physical chemistry, as it allows for temporary isolation (from milliseconds to hours) of the complexes by mechanical barriers in very small spaces,<sup>31–34</sup> providing a ‘snapshot’ of what goes on with the individual donor and acceptor hydrogen bond pairs. Simultaneously, the influence of the confining environments on the structural and energetic properties of HB complexes exposed to the high pressure or encapsulated inside various chemical cages has also been widely studied.<sup>25,34–44</sup> Among others, based on the results of NMR measurements obtained for the hydrogen bonded carboxylic acid dimers embedded in different molecular capsules it was shown that the orbital compression leads to the shortening of the hydrogen bond length.<sup>34,37</sup> Likewise, the data obtained from the Raman scattering study performed on the crystalline deuterated formic acid indicate that under the influence of high pressure the strength of deuterium bonds has been enhanced.<sup>38</sup> Similar findings emerged from the recent theoretical studies concerning the impact of spatial restriction, represented by the cylindrical harmonic potential, on the properties of linear hydrogen bonded complexes.<sup>25,43</sup> It should be highlighted that previous studies on the L&NLO properties of the spatially limited hydrogen bonded complexes are scarce in the literature. In fact, the only report analysing the influence of the orbital compression on the electric properties of HB molecular complexes is that by Róztoczyńska *et al.*,<sup>25</sup> who found that the effect of the analytical confining potential leads to the decrease of both the dipole moment and dipole polarizability of the linear HCN chains. Thus, to the best of our knowledge, the present study is a pioneering exploration of confinement-induced changes in the electronic and vibrational nonlinear optical properties for weakly bound systems. It is also worth mentioning that this is a significant extension of our earlier systematic research focusing on the influence of a chemical confining environment on the vibrational contributions to molecular polarizabilities.<sup>23,24</sup>

## 2 Computational methods

Under the assumption of the validity of the clamped nuclei approximation, the molecular (non)linear optical properties ( $P = \alpha, \beta, \gamma$ ) may be separated into pure electronic, nuclear relaxation ( $P^{\text{nr}}$ ) and curvature ( $P^{\text{curv}}$ ) contributions:<sup>45,46</sup>

$$P = P^e + P^{\text{nr}} + P^{\text{curv}} \quad (1)$$

The  $P^{\text{nr}}$  contributions usually prevail over  $P^{\text{curv}}$  terms. In order to treat the effect of molecular vibration on the electric properties, Bishop and Kirtman proposed a double (electrical and mechanical) perturbation theory (BKPT) treatment.<sup>47</sup> The  $P^{\text{nr}}$  contributions are given by leading terms of each type of ‘‘square bracket’’ terms of BKPT pure vibrational contributions.<sup>48</sup> Within this approach, the static nuclear relaxation (hyper)polarizabilities, which are central to this study, may be expressed using the ‘‘square bracket’’ notation as:

$$\alpha^{\text{nr}}(0;0) = [\mu^2]_{\omega=0}^{(0,0)} \quad (2)$$

$$\beta^{\text{nr}}(0;0,0) = [\mu\alpha]_{\omega=0}^{(0,0)} + [\mu^3]_{\omega=0}^{(1,0)} + [\mu^3]_{\omega=0}^{(0,1)} \quad (3)$$

$$\gamma^{\text{nr}}(0;0,0,0) = [\alpha^2]_{\omega=0}^{(0,0)} + [\mu\beta]_{\omega=0}^{(0,0)} + [\mu^2\alpha]_{\omega=0}^{(1,0)} + [\mu^2\alpha]_{\omega=0}^{(0,1)} + [\mu^4]_{\omega=0}^{(2,0)} + [\mu^4]_{\omega=0}^{(0,2)} + [\mu^4]_{\omega=0}^{(1,1)} \quad (4)$$

Each square bracket involves the products of normal coordinate derivatives of the electronic electrical properties indicated, as well as harmonic vibrational frequencies and anharmonic force constants. Each term is identified by a pair of superscripts ( $n, m$ ) denoting the order in electrical and mechanical anharmonicities, respectively. For the sake of brevity, the tensor indices were omitted in the above equations.

Alternatively, the nuclear relaxation contributions can be calculated from finite-field derivatives of the electronic properties computed at the field-relaxed equilibrium geometries (FF-NR method).<sup>49,50</sup> In general, during FF-NR calculations it should be ensured that the geometry relaxation must not result from rotations of the molecule through alignment of the permanent and/or induced dipole moment in the field direction. For that reason, the field-dependent optimization should be performed while strictly maintaining the Eckart conditions.<sup>51</sup> Such optimizations can be carried out with the aid of the procedure developed by Luis *et al.*<sup>50</sup>

Moreover, in order to reduce the numerical differentiation error in the FF-NR approach, in this study we follow the Romberg–Rutishauser scheme.<sup>52,53</sup> The correction of order  $p$  to the derivative  $P$  is determined iteratively according to the formula:

$$P^{p,k} = \frac{4^p \cdot P^{p-1,k} - P^{p-1,k+1}}{4^p - 1} \quad (5)$$

where  $k$  is related to the strength of the field used in the FF-NR calculations (see below). The value of  $P^{0,k}$  is determined from the finite-difference expression for the derivative of the energy ( $E$ ) with respect to the electric field ( $F$ ). The electric field amplitude  $F_i$  was equal to 0.0002 a.u. In all calculations employing the Romberg–Rutishauser scheme we used the following sequence of fields  $\pm F_i, \pm 2F_i, \dots, \pm 2^k F_i$ , where  $k = 7$ . Moreover, the Romberg–Rutishauser approach was also used to determine the energy gradient during field-dependent geometry optimizations.



In doing so, we used the step  $\Delta = 0.01$  Bohr, for the following sequence of displacements  $\pm\Delta, \pm2\Delta, \dots, \pm2^k\Delta$ , where  $k = 2$ .

The double harmonic square bracket terms are sufficient to compute the nuclear relaxation contribution to some dynamic NLO properties within the infinite optical frequency approximation. These include, *inter alia*, the electro-optical Pockels effect (EOPE), the intensity-dependent refractive index (IDRI) and electric field induced second harmonic generation (ESHG). In square bracket notation the properties were determined as:<sup>30</sup>

$$\beta_{\text{EOPE}}^{\text{nr}}(-\omega; \omega, 0)_{\omega \rightarrow \infty} = \frac{1}{3}[\mu\alpha]_{\omega=0}^{(0,0)} \quad (6)$$

$$\gamma_{\text{IDRI}}^{\text{nr}}(-\omega; \omega, -\omega, \omega)_{\omega \rightarrow \infty} = \frac{2}{3}[\alpha^2]_{\omega=0}^{(0,0)} \quad (7)$$

$$\gamma_{\text{ESHG}}^{\text{nr}}(-2\omega; \omega, \omega, 0)_{\omega \rightarrow \infty} = \frac{1}{4}[\mu\beta]_{\omega=0}^{(0,0)} \quad (8)$$

These equations hold for the diagonal components of the properties. In addition, the dynamic  $\alpha^{\text{nr}}$  vanishes in the infinite optical frequency approximation. In the case of vibrational properties reported herein, the temperature dependence is omitted since the nuclear-relaxation contributions do not depend on the temperature. The temperature dependence of the vibrational NLOP is given by the curvature contributions to NLOP, which are not computed here. Nevertheless, taking into account that the curvature contributions to the nonlinear optical properties are usually much smaller than the corresponding nuclear relaxation terms, the overall temperature effect on the total vibrational properties is not expected to be substantial.<sup>54</sup>

In this work, the effect of spatial confinement was modelled by applying the harmonic oscillator potential of cylindrical symmetry, centred at the nucleus and represented by the sum of one-electron contributions:

$$\hat{V}_{\text{conf}} = \sum_i \frac{1}{2} \phi^2 (x_i^2 + y_i^2) \quad (9)$$

The potential in such a form was added to the Hamiltonian. In eqn (9) the  $\phi$  parameter corresponds to the strength of spatial confinement. In the present study, in order to analyse the behaviour of  $\alpha$ ,  $\beta$  and  $\gamma$  as a function of confinement strength, the  $\phi$  values between 0 and 0.2 a.u. were considered. It is worth mentioning that this range might be connected with the repulsive interaction energy between studied complexes and carbon nanotubes. As an example of this relation, we have compared the Hartree–Fock interaction energies of both studied complexes and the (4,4) carbon nanotube with the results obtained using our analytic confining potential. The results presented in Table S1 (ESI†) show that the HF interaction energy between the (4,4) nanotube and HCN $\cdots$ HCN (HCN $\cdots$ HNC) is 133 kcal mol<sup>-1</sup> (134 kcal mol<sup>-1</sup>), so the interaction is clearly repulsive. The strength of the confining potential ( $\phi$ ) can be adjusted to represent this repulsive interaction:

$$\Delta E_{\text{int}}^{\text{HF}} \approx E(\phi) - E(\phi = 0.0)$$

One of two amplitudes of confining potential employed in this work is 0.1 a.u. and  $E(\phi = 0.1) - E(\phi = 0.0)$  roughly corresponds

to Hartree–Fock interaction energy of HCN $\cdots$ HCN and HCN $\cdots$ HNC complexes trapped inside the (4,4) carbon nanotube. The model analytic potential is even able to reproduce the small increase in the repulsion energy when the HCN $\cdots$ HCN dimer is replaced by the HCN $\cdots$ HNC dimer. Moreover, to shed light on the role of different interaction energy terms, we decomposed the Hartree–Fock interaction energy using the lowest-order of symmetry-adapted perturbation theory. The results of calculations for the studied complexes trapped inside the (4,4) nanotube show that the exchange repulsion contribution is much higher than the attractive electrostatic and delocalization terms (Table S1, ESI†). Noteworthy, these contributions show a very small dependence on the geometries of the HCN $\cdots$ HCN and HCN $\cdots$ HNC complexes trapped inside the nanotube (*cf.* Table S1, ESI†).

In the present study we employed the CCSD(T) method combined with the aug-cc-pVTZ basis set. As demonstrated in our earlier study this basis set delivers 1% accuracy in electronic and nuclear relaxation (hyper)polarizabilities of small molecules.<sup>55</sup> Tight convergence criteria during the optimization of coupled cluster wavefunction were imposed (energy convergence criterion was set to 10<sup>-12</sup> hartree). The latter and the large number of electric field amplitudes are the main factors contributing to very high computational expenses of the BKPT and FF-NR calculations performed in this study. The state-of-the-art results presented herein encouraged us to carry out the assessment of the MP2 method in computing both electronic and vibrational hyperpolarizabilities of confined molecules. The results are presented in the ESI† and show that the MP2 method reproduces the correct trends, although the errors may reach up to 15%.

FF-NR and BKPT calculations were performed using custom computer routines based on the energies computed using the GAUSSIAN 2009 package.<sup>56</sup>

### 3 Results and discussion

In order to analyze the confinement-induced changes in the electric properties of molecular aggregates, two model hydrogen-bonded systems were chosen, namely: HCN $\cdots$ HCN and HCN $\cdots$ HNC. For the sake of brevity, in what follows we will also refer to these systems as A and B, respectively. These strongly bonded bimolecular complexes were studied by Heikkilä and Lundell<sup>57</sup> who determined the interaction energy. The results of calculations, performed at the CCSD(T)/6-311++G(2d,2p) level of theory, indicate that HCN $\cdots$ HNC is much more strongly bonded than HCN $\cdots$ HCN and the corresponding interaction energies are -17.947 and -27.650 kJ mol<sup>-1</sup>. This is reflected in shortening of the N $\cdots$ H bond length from 2.207 Å to 1.946 Å (results obtained at the MP2/6-311++G(2d,2p) level by Heikkilä and Lundell).<sup>57</sup> This is in line with the results of calculations obtained in this work, *i.e.* the shortening of the N $\cdots$ H bond length from 2.204 Å to 1.967 Å on passing from HCN $\cdots$ HCN to HCN $\cdots$ HNC. Despite these significant differences in the equilibrium structure and interaction strength for isolated complexes, the patterns of confinement-induced changes in geometrical parameters for both systems are similar (see Fig. 1).



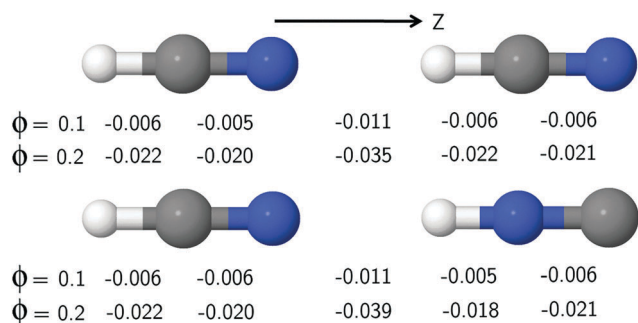


Fig. 1 Bond-length changes (given in Å) in the presence of confining potential ( $\phi$ , given in a.u.). Shown is also the orientation of studied complexes in the Cartesian coordinate system.

For  $\phi = 0.1$  a.u. one observes the shortening of all covalent bonds in A and B roughly by 0.006 Å, while the N··H bond length is shorter by 0.011 Å. Larger strength of confinement, *i.e.*  $\phi = 0.2$  a.u., leads to further shortening of covalent bonds in both complexes (from 0.020 to 0.022 Å with respect to the unconfined systems) and yet there is a significant decrease in the N··H bond length ranging from 0.035 Å (HCN··HCN) to 0.039 Å (HCN··HNC). The results presented herein for molecular complexes are consistent with what was reported for molecules, *e.g.* the confinement-induced shortening of covalent bonds was also observed for CO<sub>2</sub>, C<sub>2</sub>H<sub>2</sub>, HCN and HCCCN.<sup>23,24</sup> An analogous behavior has also been noted for the hydrogen bond length in several theoretical as well as experimental works concerning the effect of spatial confinement on the HB complexes.<sup>25,37,43,58</sup> As pointed out by Cammi *et al.* the shortening of the interatomic distances upon confinement is directly connected with the deformation of the molecular electronic charge density, due to the Pauli repulsive interaction with the environment.<sup>59,60</sup> According to the authors, such an interaction causes an increase of electron density in the interatomic regions of the molecule, which leads to a reduction of bond lengths. In some measure, these findings are in line with those emerging from the extensive quantum-chemical calculations conducted for the spatially limited HB dimers.<sup>43</sup> In particular, based on the results obtained using quantum theory of atoms in molecules, it has been shown that upon increasing the strength of the orbital compression the electron density at the hydrogen bond critical point becomes

larger, which might be directly related to the shortening of the hydrogen bond length.

The significant difference in the N··H bond length for both complexes is expected to have an impact on the electric dipole properties. Indeed, the data presented in Table 1 for unconfined complexes demonstrate that, by and large, (hyper)polarizabilities of HCN··HNC are higher than those for HCN··HCN. Similar observation has been made by Brandão *et al.*, who studied how the isomeric change affects the magnitude of electronic contributions to the electric properties.<sup>61</sup> As has been demonstrated such an effect has a notable influence on the values of  $\mu$ ,  $\alpha$  and, in particular,  $\beta$  of linear chains of HCN and HNC molecules.

We will now turn to the discussion of confinement-induced changes in the diagonal electronic contributions to  $\alpha$ ,  $\beta$  and  $\gamma$  based on the data compiled in Table 1 and Fig. 2. Note that all the NLO properties were calculated using geometries optimized for the indicated amplitudes of the confining potential ( $\phi$ ). In the case of electronic polarizability there is a similar decrease upon increasing the confinement strength from  $\phi = 0.0$  to  $\phi = 0.2$  a.u. (13.29% for A and 13.19% for B). This result was quite expected, as a direct consequence of the electron density compression due to the presence of the confinement effect.<sup>18,19,21,22</sup> The corresponding changes in electronic first hyperpolarizability are more pronounced, *i.e.* there is a 17.86% and 28.38% drop in this property for A and B, respectively. The largest effect of spatial confinement is observed in the case of  $\gamma^e$ : when increasing the confinement strength from  $\phi = 0.0$  to  $\phi = 0.2$  a.u. there is an accompanying decrease in this property as large as 44.62% and 50.00%, for A and B, respectively. Based on these results one can conclude that even moderate changes in the strength of confinement can lead to quite large changes in electronic hyperpolarizabilities. Moreover, as it can be noticed, the influence of orbital compression on the magnitude of (hyper)polarizabilities increases with the increasing order of the electrical properties. A similar remark has been made previously in several theoretical studies concerning the electric properties of molecular systems embedded in the model confining potentials.<sup>19,21–23</sup> Note that the electronic properties discussed thus far were calculated at geometries optimized for the indicated amplitudes of confining potential ( $\phi$ ). In order to address the importance of the effect of confinement-induced structural relaxation on  $\alpha^e$ ,  $\beta^e$  and  $\gamma^e$  we have performed

**Table 1** Electronic and vibrational contributions to (hyper)polarizabilities as a function of confinement strength ( $\phi$ ). The properties are given in atomic units and were computed at the CCSD(T)/aug-cc-pVTZ level of theory. Except three terms corresponding to the dynamic properties (see eqn (6)–(8)), all remaining ones are static. Note that all the NLO properties were calculated using geometries optimized for the indicated amplitudes of confining potential ( $\phi$ )

$\phi$	$\alpha^e$	$\alpha^{\text{nr}}$	$\beta^e$	$\beta^{\text{nr}}_{\text{EOPE}}$	$\beta^{\text{nr}}$	$\gamma^e$	$\gamma^{\text{nr}}_{\text{IDRI}}$	$\gamma^{\text{nr}}_{\text{ESHG}}$	$\gamma^{\text{nr}}$
<b>HCN··HCN</b>									
0.0	49.88	4.75	−28	−56	−225	$6.5 \times 10^3$	$2.6 \times 10^3$	$0.2 \times 10^3$	$11.3 \times 10^3$
0.1	47.65	4.59	−25	−52	−211	$5.2 \times 10^3$	$2.3 \times 10^3$	$0.2 \times 10^3$	$10.0 \times 10^3$
0.2	43.25	4.19	−23	−46	−185	$3.6 \times 10^3$	$1.8 \times 10^3$	$0.1 \times 10^3$	$7.5 \times 10^3$
<b>HCN··HNC</b>									
0.0	52.39	8.12	−74	−61	−301	$9.0 \times 10^3$	$2.8 \times 10^3$	$<0.1 \times 10^3$	$22.2 \times 10^3$
0.1	50.01	7.79	−62	−56	−282	$6.8 \times 10^3$	$2.5 \times 10^3$	$<0.1 \times 10^3$	$19.6 \times 10^3$
0.2	45.48	7.15	−53	−49	−250	$4.5 \times 10^3$	$2.0 \times 10^3$	$<-0.1 \times 10^3$	$16.2 \times 10^3$





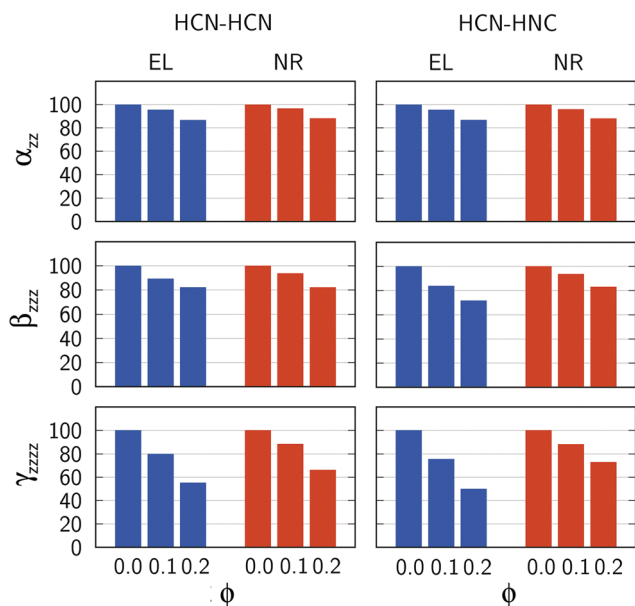


Fig. 2 Relative percentage changes of electronic (EL) and nuclear-relaxation (NR) (hyper)polarizabilities as a function of the confinement strength ( $\phi$ , given in a.u.).

property calculations at a set of frozen geometries (for  $\phi = 0$  and  $\phi \neq 0$ ). Based on the results shown in Table S2 in the ESI,<sup>†</sup> it can be concluded that the geometry relaxation makes only a minor contribution to the overall confinement-induced changes in electronic (hyper)polarizabilities.

In what follows we will seek to establish if the conclusion presented above also holds for the vibrational nonlinear optical properties of weakly bound HCN isomers. In doing so, we will analyse the confinement-induced changes in the vibrational properties of both complexes. The relevant data are presented in Table 1 and Fig. 2. As above, we will discuss the percentage changes between the properties computed for unconfined and confined complexes (where  $\phi = 0.2$  a.u.). Similar to electronic polarizability, a drop in the  $\alpha^{\text{nr}}$  value occurs for both systems upon increasing confinement and the corresponding change equals to 11.79% (A) and 11.95% (B). Note that the obtained decrease in the  $\alpha^{\text{nr}}$  values is slightly smaller than the corresponding changes in  $\alpha^{\text{e}}$ . The orbital compression has, again, almost an identical influence on nuclear-relaxation static first hyperpolarizability of both complexes and reduces its magnitude by 17.78% and 16.94% for A and B, respectively. As one can notice, in the case of the HCN  $\cdots$  HCN complex the degree of the confinement-induced change in  $\beta^{\text{nr}}$  is virtually the same as for  $\beta^{\text{e}}$ . In contrast,  $\beta$  of HCN  $\cdots$  HNC behaves differently and the drop in the nuclear relaxation contribution is roughly 10% smaller than that for  $\beta^{\text{e}}$ . Finally, we find that  $\gamma^{\text{nr}}$  for both systems is much less susceptible to spatial confinement and the corresponding changes are 33.63% (A) and 27.03% (B). It should not be overlooked that these changes are much smaller than those observed for electronic second hyperpolarizability. Table 1 also contains the values of dynamic vibrational hyperpolarizabilities. The confinement-induced change in  $\beta_{\text{EOPE}}^{\text{nr}}(-\omega; \omega, 0)$ ,

on passing from  $\phi = 0.0$  to  $\phi = 0.2$  a.u., is 17.86% and 19.67% for A and B, respectively. However, a much larger effect is found for  $\gamma_{\text{IDRI}}^{\text{nr}}$ , i.e. the change in this property is 30.77% (A) and 28.57% (B). We may thus conclude that in terms of magnitude the effect of confinement is similar for the static and dynamic vibrational properties.

In order to rationalize the changes in the static nuclear-relaxation hyperpolarizabilities upon confinement, we performed their breakdown into harmonic and net anharmonic contributions. The results are presented in Fig. 3 and 4 and all numerical data are presented in the ESI.<sup>†</sup> As shown by the latter figure, the above discussed confinement-induced changes in  $\beta^{\text{nr}}$  can be mainly associated with the decrease of the harmonic contribution (75.00% and 68.63% of total  $\beta^{\text{nr}}$  drop for A and B, respectively). However, in the case of  $\gamma^{\text{nr}}$  the anharmonic terms become far more important and they are responsible for the confinement-induced decrease of this property, i.e. the drop in  $\gamma^{\text{nr}}$  is 65.78% and 73.33% due to a decrease of anharmonic terms for A and B, respectively.

In an attempt to shed more light on the confinement-induced changes in the vibrational properties, we employed the BKPT formalism which allows for the analysis of the normal mode contributions to individual square bracket terms appearing in eqn (3) and (4). In order to unravel the connection between the changes in harmonic terms and the changes in the vibrational structure, we performed an exemplary analysis of individual normal modes contributing to the harmonic part of  $\beta^{\text{nr}}$ . The results for the  $[\mu\alpha]^{(0,0)}$  term are presented in Fig. 5 (for other terms we refer to the ESI<sup>†</sup>). The plots present the individual normal mode contributions (vertical bars) together with the total value (bold dotted line). As seen, in the case of studied molecular systems, only two modes have major contribution to the confinement-induced decrease in  $[\mu\alpha]^{(0,0)}$ . For both complexes these two modes correspond to: (i) the intermolecular stretching vibration ( $n = 1$ ), (ii) the stretching vibration of hydrogen involved in the hydrogen bond ( $n = 12$  (A) and  $n = 13$  (B)). The same conclusions hold for  $[\mu^2]^{(0,0)}$  and  $[\mu\beta]^{(0,0)}$  terms. Besides the modes  $n = 1$  and  $n = 12$  ( $n = 13$ ), the modes  $n = 10$  and  $n = 11$ , which correspond to C–N stretching and play a minor role in the

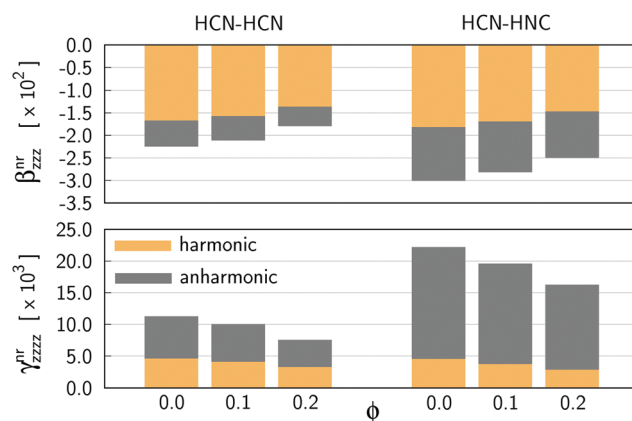


Fig. 3 Breakdown of nuclear-relaxation hyperpolarizabilities into harmonic and anharmonic contributions as a function of the confinement strength ( $\phi$ ). All values are given in atomic units.



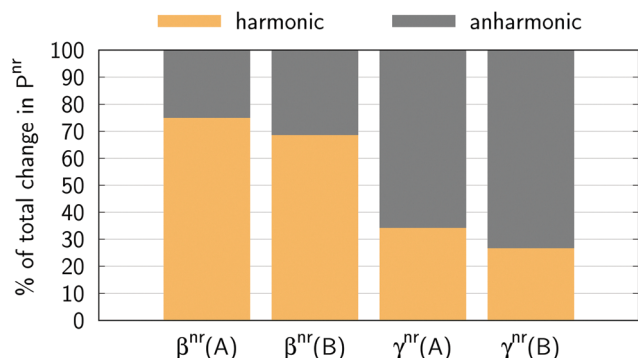


Fig. 4 Percentage contributions of harmonic and anharmonic terms to the total confinement-induced change ( $\phi = 0 \rightarrow \phi = 0.2$ ) in  $\beta^{nr}$  and  $\gamma^{nr}$  for HCN...HCN (A) and HCN...HNC (B).

BK terms that contain a normal mode derivative of  $\mu$ , also have a major contribution to  $[\alpha^{(0,0)}]$ .

In the case of  $\gamma^{nr}$ , as shown in Fig. 4, the anharmonic terms play a major role in confinement-induced changes of this property. In order to connect these changes with a particular mode of vibration, we evaluated the  $\left[\frac{1}{\omega_i^2} \frac{\partial \mu_z}{\partial Q_i}\right]^n$  term, up to  $n = 4$  for each normal mode  $i$  (the data are presented in the ESI†). Anharmonic contributions to  $\beta^{nr}$  and  $\gamma^{nr}$  are proportional to the second ( $[\mu^3]^{(1,0)}$ ,  $[\mu^2\alpha]^{(1,0)}$ ,  $[\mu^2\alpha]^{(0,1)}$ ), third ( $[\mu^3]^{(1,0)}$ ,  $[\mu^4]^{(1,1)}$ ,  $[\mu^4]^{(2,0)}$ ) and fourth ( $[\mu^4]^{(0,2)}$ ) power of this term.<sup>62</sup> Based on the data presented in the ESI† it is possible to link, albeit with some uncertainty, the pivotal role of intermolecular stretching vibration ( $n = 1$ ) with confinement-induced changes in anharmonic contributions.

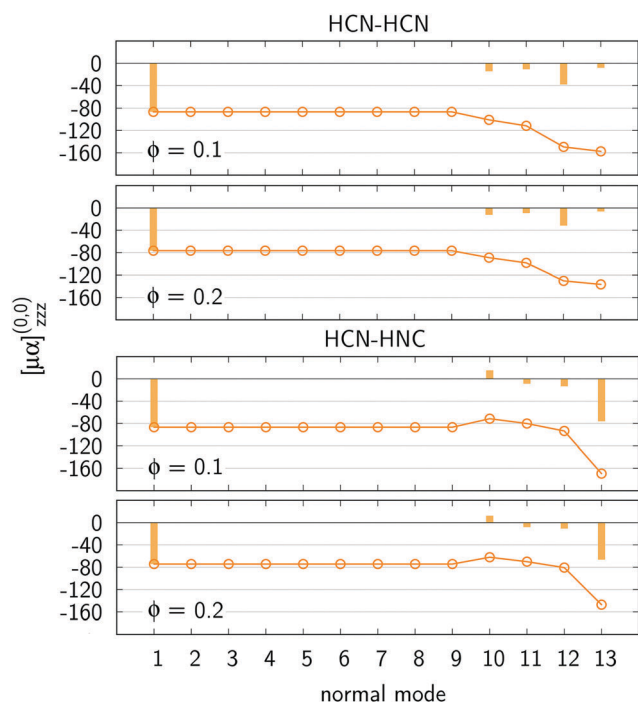


Fig. 5 The convergence of the  $[\mu\alpha]_{zzz}^{(0,0)}$  term as a function of normal modes for  $\phi = 0.1$  a.u. and  $\phi = 0.2$  a.u. All values are given in atomic units.

## 4 Conclusions

In this theoretical study we presented the analysis of the effect of spatial confinement on the electronic and vibrational contributions to longitudinal (hyper)polarizabilities of two dimeric hydrogen bonded systems, namely HCN...HCN and HCN...HNC. All the properties in question were calculated at the CCSD(T)/aug-cc-pVTZ level of theory. A two-dimensional analytical potential of cylindrical symmetry was applied to model the effect of the confining environment (e.g. carbon nanotube). The vibrational contributions to the static and dynamic properties were evaluated employing the perturbation method of Bishop and Kirtman together with the finite-field nuclear relaxation method. The results obtained in this study made possible drawing several new observations regarding the effect of confinement on the properties of molecular complexes. The most important ones can be summarized as follows:

- The influence of spatial confinement increases with increasing order of the electrical properties, both for electronic and vibrational contributions.
- The effect of spatial confinement is much larger in the case of electronic than vibrational contributions and this holds for each order of the electrical properties.
- The decrease in the static  $\beta^{nr}$  upon the increase of confinement strength is mainly due to changes in the harmonic term, however, in the case of  $\gamma^{nr}$  the anharmonic terms contribute more to the drop of this property.

Finally, it should be underlined that this is the first study analysing the effect of spatial confinement on static and dynamic (hyper)polarizabilities of weakly-bound systems. Authors would like to express their hope that more studies will follow, so it will be possible to generalize the conclusions presented herein.

## Conflicts of interest

There are no conflicts to declare.

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