1. Introduction

Poly(vinyl butyral) (PVB) is a random ter-polymer of vinyl butyral, vinyl alcohol and vinyl acetate (Fig. 1). The random structure of PVB results in an amorphous polymer showing excellent optical clarity, adhesive properties, toughness, and flexibility. Thanks to these properties, PVB is widely employed as an interlayer material in the manufacture of safety glass laminates, particularly in automotive and architectural glass. It is also used in solar photovoltaic modules and as a binder in various coatings, enamels, adhesives, and inks.1–3

In spite of a large number of industrial applications, the microstructural and dynamic properties of PVB have not been thoroughly characterized. In particular, chemical composition, molecular weight, and glass transition temperature of commercial PVB films were investigated using standard analytical techniques.4,5 Viscoelastic studies were recently performed on PVB films containing additives6–8 and on neat PVB,9 the latter study providing a rather low average molecular weight between entanglements ($M_e = 2670 \text{ g mol}^{-1}$). As far as the dynamic properties of PVB are concerned, dielectric spectroscopy (DS) investigations were reported quite long ago, sometimes in combination with mechanical measurements.10–13 However, the results shown in the different publications seem incoherent, possibly because of the different, often unspecified, PVB composition and/or the different sample treatments. More recently, DS data were reported only at a few temperatures above the PVB glass transition in comparative studies of pristine PVB and PVB either UV irradiated14 or loaded with alumina particles.15

Dielectric Spectroscopy (DS) and $^1$H Fast Field-Cycling (FFC) NMR relaxometry were applied for understanding the dynamic behavior of the amorphous ter-polymer poly(vinyl butyral) (PVB) across the glass transition temperature ($T_g \approx 70 \text{ °C}$ by Differential Scanning Calorimetry). Above $T_g$, main chain segmental motions ($\alpha$ relaxation) were detected and characterized using both DS and FFC NMR relaxometry. The correlation times extracted by the analysis of DS and FFC NMR relaxometry data agreed within a factor of three and showed a Vogel–Fulcher–Tammann temperature dependence, with an associated $T_g$ of 69 °C and a fragility of 155 for PVB glass. Below $T_g$, a secondary process ($\beta$ relaxation) was revealed by DS, and was ascribed to reorientations of the vinyl alcohol dipoles due to local twisting motions with an associated activation barrier of 11 kcal mol$^{-1}$. The $\beta$ process was also found to contribute to $^1$H NMR relaxation above $T_g$.

Fig. 1 Chemical structure of PVB. For the sample investigated in this work, the molar fractions of vinyl butyral ($x$), vinyl alcohol ($y$), and vinyl acetate ($z$) units are $0.55–0.57, 0.41–0.45$, and $0–0.02$, respectively.

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reorientation of side groups and segmental dynamics of polymeric systems over a broad frequency range. In particular, DS can be used to investigate motions associated with orientation rearrangements of permanent electric dipoles with characteristic frequency scales ranging from about $10^{-3}$ to $10^{10}$ Hz. This is achieved by measuring the polarization current induced by dipole reorientation after the application of an alternating electric field. Motions of lateral chains and cooperative segmental motions are usually indicated as $\beta$ and $\gamma$ relaxation processes and they dominate DS spectra at low and high temperatures, respectively. $^1$H FFC NMR relaxometry allows polymer dynamics to be investigated by measuring the dependence (dispersion) of the proton spin–lattice relaxation time $T_1$ on the Larmor frequency. $^1$H relaxation originates from fluctuations of dipole–dipole interactions between proton pairs due to polymer motions. With commercial FFC relaxometers the frequency range from 0.01 to 40 MHz is covered, this range being further extendable to lower frequencies with home-made relaxometers and to higher frequencies with high field superconducting spectrometers.

Dynamics of melt-like polymer chains can be depicted as a hierarchy of processes starting from very fast and local conformational rearrangements (i.e. isomeric motions in side chains and local reorientations of the chains within the so-called Kuhn segment) and extending to slow, diffusive and collective motions of the polymer chains.23–25 Local dynamics (also referred to as glassy dynamics), which is related to the glass transition phenomenon, usually dominates $^1$H NMR longitudinal relaxation at low temperature and high frequency, while polymer chain dynamics prevails at high temperature and low frequency.20,21 In recent papers, it was shown that the combination of DS and $^1$H FFC NMR relaxometry can give detailed information on the dynamics of melt polymers, not attainable when a single method is used.21,26,27

In the present work, DS and $^1$H FFC NMR were applied to investigate the dynamic properties of a PVB film, with a composition representative of that used for interlayer films in the safety glass industry, both below and above the glass transition ($T_g = 70 \, ^\circ \text{C}$, as determined using Differential Scanning Calorimetry, DSC). In particular, dynamic processes occurring in the glassy state were studied using DS, reaching temperatures as low as 130 K below $T_g$, while both DS and $^1$H FFC NMR were applied to investigate the polymer dynamics above $T_g$. However, due to the technical limitations and the necessity to ensure polymer stability, we could reach temperatures only up to 120 °C, that is only 50 K above $T_g$; this limited the investigation to chain segmental dynamics. The obtained results were discussed taking into account motions of different polymer moieties that, given the quite complex structure of PVB, may contribute to dielectric relaxation and/or $^1$H longitudinal relaxation at the investigated frequencies and temperatures. In fact, reorientations of permanent dipoles present in both butyral and vinyl alcohol moieties contribute to dielectric relaxation, with butyral dipoles being unable to reorient independently of the main chain and vinyl alcohol dipoles reorienting because of both backbone segmental motions and local motions. On the other hand, contributions to $^1$H $T_1$'s may arise from reorientations of both main chain segments and side groups, in particular propyl chains of butyral monomers.

2. Experimental

2.1 Sample preparation

PVB (trade name Butvar B98) was purchased from Sigma-Aldrich. The molecular weight, $M_w$, determined using size exclusion chromatography, was 79 kg mol$^{-1}$ with a polydispersity of 2.4. The molar fractions of the vinyl butyral, vinyl alcohol, and vinyl acetate units, verified by means of $^1$H NMR in CDCl$_3$ according to ref. 28, were 0.55–0.57, 0.41–0.45 and 0–0.02, respectively.

For DSC and NMR measurements, a film was prepared by dissolving PVB in ethanol at 75 °C at a concentration of about 4 wt% and stirring for 30 min. Then the solution was transferred into a teflon Petri dish and let dry in air until complete evaporation of the alcohol, which occurred after several days. The thickness of the obtained film was about 200 μm, as measured by means of a caliper. Before measurements, the film was heated at 70 °C at a pressure of $10^{-2}$ Torr for 12 hours and afterwards kept under a nitrogen atmosphere.

For the dielectric spectroscopy measurements, a film of PVB was cast from an ethanol solution (about 8 wt%) onto a steel plate, obtaining a 50 μm thick film. The sample was heated at 70 °C under vacuum for 60 hours. Before measurements, the film was capped by an indium coated upper plate to form a parallel plate capacitor.

The heat treatment under reduced pressure ensured the removal of residual water and ethanol. No signal was detected for mobile water or ethanol in $^1$H Free Induction Decay (FID) analyses of the PVB film.29 On the other hand, no evidence of constrained ethanol was present in the $^{13}$C Cross Polarization Magic Angle Spinning NMR spectra (see Fig. S1 in the ESI†). Moreover, residual ethanol was found to be 4.2 ± 0.5 mg per kg of the polymer using headspace solid-phase microextraction coupled with gas chromatography, mass spectrometry (HS-SPME-GCMS) performed on the PVB film after heating at 80 °C for 1 hour.

2.2 Molecular weight determination

$M_w$ and polydispersity were determined by size exclusion chromatography using an Agilent Technologies 1200 Series instrument equipped with two PLgel 5 μm MiniMIX-D columns (flux 0.3 mL min$^{-1}$) and a refractive index detector. Monodisperse poly(styrene) samples were used as calibration standards. The analysis was performed on a PVB solution in chloroform (2 mg mL$^{-1}$) filtered through a 0.2 μm filter prior to the measurement.

2.3 Differential scanning calorimetry

The glass transition temperature of the film was determined by means of DSC, performed on a Seiko SH ExstarDSC7020 calorimeter using the following thermal protocol: first cooling from 20 to 0 °C; 0 °C for 2 min; first heating from 0 to 110 °C; 110 °C for 2 min; second cooling from 110 to 0 °C; 0 °C for 2 min; second heating from 0 to 110 °C; 110 °C for 2 min; third cooling
from 110 to 20 °C. The cooling/heating rate was always 10 K min⁻¹ except for the last cooling process, when it was fixed to 30 K min⁻¹. The sample amount was ~5 mg.

2.4 Dielectric spectroscopy

Dielectric relaxation spectra were recorded using an Alpha Analyzer from Novocontrol (frequency interval 10⁻²–10⁷ Hz). The temperature was controlled through a heated flow of nitrogen gas by means of a Quatro Cryosystem integrated to the spectrometer. During the whole measurement period the sample was kept in a pure nitrogen atmosphere. Measurements were performed upon cooling in the interval from 86 to ~60 °C and subsequently upon heating from 70 to 116 °C. The spectra acquired between 70 and ~60 °C upon either heating or cooling were reproducible. Different measurement sessions were performed showing good agreement among measurements at different dates.

DS data were fitted using the software Grafity, version 0.4.5.

2.5 ¹H FFC NMR relaxometry

The ¹H longitudinal relaxation times T₁ were measured at different Larmor frequency values over the range 10 kHz–30 MHz using a Spinnmaster FFC-2000 (Stelar srl, Mede, Italy) relaxometer. The measurements were performed using the prepolared (PP) and nonpolarized (NP) pulse sequences below and above 10 MHz, respectively. In the former case, a polarizing field of 0.7 T, corresponding to a ¹H Larmor frequency of 30.0 MHz, was used. The detection field was 0.5 T, corresponding to a ¹H Larmor frequency of 21.5 MHz and the switching time was 3 ms. The 90° pulse duration was 9.7 μs and 2 scans were accumulated. All the other experimental parameters were optimized for each experiment. Each relaxation trend was acquired with at least 16 values of the variable delay t and was then fitted to the following equation

\[ M(t) = M_{\text{relax}} + (M_{\text{pol}} - M_{\text{relax}}) \exp(-t/T_1) \] (1)

using the SpinMaster fitting procedure. In this equation, \( M_{\text{pol}} \) and \( M_{\text{relax}} \) represent the magnetization values in the polarizing and relaxation fields, respectively, with \( M_{\text{pol}} = 0 \) for the NP experiments. In all cases, the experimental trends were well reproduced by this equation, with errors on \( T_1 \) values lower than 5%. Experiments were performed upon heating in the 70–120 °C temperature range and letting the sample temperature equilibrate for 10 minutes. The temperature of the sample was controlled within ±0.1 K with a Stelar VTC90 unit. Air was used as the heating gas.

The analysis of the experimental ¹H FFC NMR data in terms of models for longitudinal relaxation was performed using the least-squares minimization procedure implemented in the Fitteia environment.32,33

3. Results and discussion

3.1 Dielectric spectroscopy

Dielectric spectra were acquired on the PVB film as a function of frequency at different temperatures from -60 to 116 °C. The frequency dependence of the dielectric loss, \( \varepsilon'' \), is shown in Fig. 2a and b for selected temperatures below and above the glass transition, respectively. Below \( T_g \) a peak attributed to a secondary (β) relaxation process was observed, with the peak maximum moving towards higher frequencies upon heating (Fig. 2a). Around the glass transition, another more intense peak appeared in the spectra due to cooperative segmental motions of the main chain (α relaxation); the trend of this peak upon heating is similar to those reported in ref. 10 and 15. In the 50 to 70 °C temperature range, motions responsible for β relaxation were so fast that the peak maxima occurred above the available frequency range and motions associated with α relaxation contributed to the spectra in a frequency range where the effect of conductivity is dominant (Fig. 2a). Indeed a conductivity contribution to the signal was observed starting from 40 °C; this contribution, showing the usual \( \nu^{-1} \) dependence, was subtracted from the spectra shown in Fig. 2b to highlight the α process.

Frequency-temperature superposition (FTS) applied for the α process, as shown in Fig. 2c, indicating that the DS spectral shape of the structural relaxation only slightly changes with temperature in the rubbery state, as observed for other polymers.21

Quantitative information on the α and β relaxation processes was obtained analyzing the \( \varepsilon''(\nu) \) data using the imaginary part of the empirical Havriliak–Negami (HN) function.34-36 \( \varepsilon''(\nu) \) can be expressed in terms of the relaxation strength of the process, \( \Delta \varepsilon \), and the HN spectral density, \( j_{\text{HN}}(\nu) \), by the following equation:

\[ \varepsilon''(\nu) = \Delta \varepsilon \pi j_{\text{HN}}(\nu) \] (2)

where

\[ j_{\text{HN}}(\nu) = \frac{1}{\pi} \left\{ \frac{b \cdot \arctan \left[ \frac{(2\pi\nu\tau_{\text{HN}})^c \sin \left( \frac{\pi}{2} \right)}{1 + (2\pi\nu\tau_{\text{HN}})^c \cos \left( \frac{\pi}{2} \right)} \right]}{1 + [2(2\pi\nu\tau_{\text{HN}})^c \cos \left( \frac{\pi}{2} \right) + (2\pi\nu\tau_{\text{HN}})^c]^2} \right\} \] (3)

This function is particularly suitable for the description of the dynamics of polymeric systems since it takes into account the presence of both the distribution of correlation times and correlation between motions.19,37 The HN parameters are the characteristic correlation time \( \tau_{\text{DS}} \), the symmetric and asymmetric broadening of the distribution of correlation times, a and b, respectively. The parameter a can span from 0 to 1, while b from 0 to 1/a. The HN expression reduces to the Cole–Cole, Davidson–Cole or Debye ones if \( b = 1 \), a = 1, or a = b = 1, respectively. Representative examples of the fitting of \( \varepsilon'' \) curves below and above \( T_g \) are given in Fig. 2a and b, respectively.

The parameter a of the β process, \( a_{\beta} \), was found to be 0.30 ± 0.04 in the temperature range from -60 to 40 °C, whereas \( b_{\beta} \) was ~0.4 below -10 °C and was fixed to 1 at temperatures ≥ -10 °C. Low values of \( a_{\beta} \) indicate that the β relaxation is characterized by a broad distribution of correlation times, typically attributed to the existence of a large variety of environments experienced by the reorienting dipoles. \( \Delta \varepsilon_{\beta} \) did not depend significantly on temperature, as commonly observed for β processes below \( T_g \) and showed values scattered around 0.4. In order to facilitate the comparison with the literature data for similar systems, the correlation time, \( \tau_{\text{HNmax}} \), equal to the inverse angular frequency...
at the HN function maximum \( \tau_{HN_{\text{max}}} = 1/(2\pi \tau_{\text{HN}}) \), was derived from the parameter \( \tau_{\text{HN}} \) according to the following formula\(^{39,40} \)

\[
\tau_{HN_{\text{max}}} = \tau_{HN} \left( \frac{\sin \left( \frac{\pi a \cdot b}{2(1 + b)} \right)}{\sin \left( \frac{\pi a}{2(1 + b)} \right)} \right)^{-1/2}
\] (4)

The temperature dependence of \( \tau_{HN_{\text{max}}} \) (in the following referred to as \( \tau_{\text{DS}}_{HN_{\text{max}}} \)) indicates that it was determined by DS and that it is relative to the \( \beta \) process could be formally reproduced by an Arrhenius equation (Fig. 3) with an activation energy of \( 11.1 \pm 0.2 \text{ kcal mol}^{-1} \), which is close to the values previously derived from dielectric data for PVB\(^{10} \) (12 kcal mol\(^{-1} \)) and for poly(vinyl alcohol) (PVA)\(^{31,42} \) (~13 kcal mol\(^{-1} \)). A value of the activation energy of 13 kcal mol\(^{-1} \) was also reported for \( \beta \) relaxation in PVB by Mehendru et al.,\(^{13} \) but the motional correlation times were considerably lower than those found by us and other authors.\(^{10} \) On the other hand, the correlation times here determined are in agreement with those reported for \( \beta \) relaxation in amorphous PVA.\(^{43} \) By also considering that the permanent dipoles present in the vinyl butyral units are unable to reorient independently of the main chain, the \( \beta \) process can be essentially ascribed to local twisting of the chains inducing reorientations of the vinyl alcohol dipoles.

Fig. 2  Frequency dependence of the dielectric loss, \( \epsilon'' \), for PVB at the indicated temperatures (expressed in °C) below (a) and above (b) the glass transition temperature (\( T_g = 70 °C \)). The spectra shown in (b) were obtained after subtraction of the conductivity contribution. For the spectra at ~10 and 100 °C, the curves obtained by data fitting are shown as examples. At ~10 °C, the solid line represents the HN function (eqn (2) and (3), see the text) describing the \( \beta \) relaxation. The fitting parameters are \( \tau_{\text{DS}}_{HN_{\beta}} = (0.1 \pm 0.7) \times 10^{-6} \text{ s}, \Delta_{\text{DS}_{\beta}} = 0.33 \pm 0.04, a_{\beta} = 0.29 \pm 0.03 \) (\( b_{\beta} \) was fixed to 1). At 100 °C, the solid line represents the HN function pertaining to the \( \alpha \) relaxation. The fitting parameters are \( \tau_{\text{DS}}_{HN_{\alpha}} = (4.8 \pm 2.0) \times 10^{-6} \text{ s}, \Delta_{\text{DS}_{\alpha}} = 1.80 \pm 0.06, a_{\alpha} = 0.66 \pm 0.04, b_{\alpha} = 0.51 \pm 0.09 \).

(b) Expansion of (a) for temperatures above \( T_g \). The black line represents an extrapolation of \( \tau_{\text{DS}}_{HN_{\text{max}} \beta} \) to temperatures above \( T_g \).

Fig. 3  (a) Temperature dependence of: \( \tau_{\text{DS}}_{HN_{\text{max}} \alpha} \) (red triangles) and \( \tau_{\text{DS}}_{HN_{\text{max}} \beta} \) (black circles) derived from DS data; \( \tau_{\text{NMR}}_{\text{min}} \) (blue squares) extracted from FFC NMR data represented in Fig. 4b exploiting the condition \( 2\pi \tau_{\text{NMR}}_{\text{min}} = 0.616 \); \( \tau_{\text{NMR}}_{HN_{\text{max}}} \) extracted from the analysis of \( \omega_{00} \) NMR shown in Fig. 5 considering two (blue empty squares) and one (blue crossed empty squares) processes, as described in the text. The solid lines represent the best fitting curves for each data set: \( \tau_{\text{DS}}_{HN_{\text{max}}} \) and \( \tau_{\text{NMR}}_{HN_{\text{max}}} \) are described by the VFT equation (\( D = 2.6 \pm 0.4, T_g = 41 \pm 3 °C \)), whereas an Arrhenius equation fits \( \tau_{\text{DS}}_{HN_{\text{max}}} \) (\( E_{\text{act}} = 11.1 \pm 0.2 \text{ kcal mol}^{-1} \)). The vertical line marks the glass transition temperature. (b) Expansion of (a) for temperatures above \( T_g \). The black line represents an extrapolation of \( \tau_{\text{DS}}_{HN_{\text{max}} \beta} \) to temperatures above \( T_g \).
For the $z$ process, investigated between 76 and 116 °C, the parameter $a$ increased upon heating from 0.65 to 0.75, whereas $b$ was scattered in the range 0.45–0.60, and $\Delta c$ tended to decrease from 1.9 to 1.7. Deviations of the DS peaks from the Debye behavior, that is peak broadening and asymmetry, were also observed by Funt in a PVB sample containing 12–13% of vinyl alcohol.11 The temperature dependence of $\tau_{\text{DS}}$max,as derived from $\tau_{\text{HN}}$ using eqn (4),36,40 was fitted according to the Vogel–Fulcher–Tammann (VFT) equation

$$\tau(\text{DS})_{\text{HNmax},a} = \tau_\infty \exp \left( \frac{D T_0}{T - T_0} \right)$$

(5)

usually adopted for the $z$ relaxation. For the best fitting function, reported in Fig. 3, the strength parameter $D$ was found to be $2.6 \pm 0.4$, while $T_0 = 41 \pm 3$ °C. Using eqn (5), we determined the DS glass transition temperature, $T_{\text{gDS}}$, as the temperature where $\tau(\text{DS})_{\text{HNmax},a}$ is equal to 100 s, according to a common convention.19 We found $T_{\text{gDS}} = 69 \pm 3$ °C, a value quite close to that determined using DSC. Dynamic fragility $m$ was calculated using the equation44,45

$$m = \frac{D T_0 T_{\text{gDS}}}{(T_{\text{gDS}} - T_0)2\ln 10}$$

(6)

and resulted to be 155 ($\pm 10\%$). This value indicates that PVB forms a fragile glass, as expected for polymers with long rigid backbones.45

### 3.2 $^1$H FFC NMR relaxometry

Fig. 4a shows the $^1$H $T_1$ dispersions acquired on the PVB film in the temperature range from 70 to 120 °C. At all temperatures and frequencies a single $T_1$ value was obtained, as usually found for amorphous melt polymers, indicating that spin diffusion was effective. At Larmor frequencies $>10^4$ Hz, $T_1$ values were strongly dependent on frequency and decreased with increasing temperature,46 while at frequencies $<10^5$ Hz and for temperatures above 90 °C, the $T_1$ values reached a plateau, suggesting that the motions entered the extreme narrowing regime.

$T_1$ trends as a function of the inverse absolute temperature (Fig. 4b) allowed the presence of dynamic processes contributing to proton relaxation in the investigated frequency range to be better identified. At frequencies $<0.5$ MHz, a minimum was clearly observed between 100 and 120 °C, which shifted to higher temperatures as the frequency was increased; at frequencies $>0.5$ MHz, only the “low” temperature side of the trend was observed. An estimate of the motional correlation time at the temperature corresponding to the minimum, $\tau_{\text{NMR}}$min, was obtained by the relationship $2\pi \nu_{\text{min}}\tau_{\text{NMR}}$min, $\approx 0.616$, where $\nu_{\text{min}}$ indicates the frequency at which the minimum is observed. The derived $\tau_{\text{NMR}}$min values are reported in Fig. 3. Considering the DS findings, we can infer that the $z$ process is responsible for the NMR minima, although the $\tau(\text{NMR})_{\text{min},a}$ values are systematically shorter than the corresponding $\tau(\text{DS})_{\text{HNmax},a}$ by a factor of about 3. This difference, also observed by other authors,26 may be ascribed to a diffusional process for which $\tau_{\text{DS}} = 3\tau_{\text{NMR}}$ is theoretically predicted.44 It should be noticed that the $\tau(\text{NMR})_{\text{min},a}$ values showed the same temperature dependence as $\tau(\text{DS})_{\text{HNmax},a}$.

In order to directly compare $^1$H FFC NMR and DS data, dispersions of “NMR susceptibility”, defined as $\chi_{\text{NMR}} = \nu/T_1$,21 were used (Fig. 4c). In this representation the presence of peaks is related to the occurrence of dynamic processes governing relaxation in the investigated frequency range. For temperatures between 100 and 120 °C, the $\chi_{\text{NMR}}$ curves showed a distinct maximum ascribable to the $z$ process which shifted to higher frequencies upon heating.

The amplitude of $\chi_{\text{NMR}}$ decreased with decreasing temperature, indicating that FTS did not apply rigorously, and the high
frequency side of the peaks was rather flat with respect to DS data (see Fig. S2 in the ESI† where the shapes of $g'$ and $N_{\text{HN}}$ curves acquired above $T_g$ are directly compared after scaling the amplitude and the time scale). The amplitude decrease could be due to: (i) a broadening of the $a$ relaxation peak upon cooling; (ii) the emergence of a secondary process associated with local motions of the main and/or side chains, such as the $b$ relaxation process identified by DS measurements; 26 (iii) a decrease in the proton fraction involved in the $a$ relaxation with decreasing temperature (vide infra). The possible contribution of secondary relaxation processes could also account for the shape of the $N_{\text{HN}}$ peaks on the high frequency side.

In order to elucidate the role of the factors determining the shape of $N_{\text{HN}}$ curves, these curves were analyzed on the basis of relaxation theory. Following Bloembergen, Purcell and Pound, $N_{\text{HN}}$ can be associated with the spectral densities of motion, $J(v)$, by the equation:

$$N_{\text{HN}} = \frac{\nu}{T_1} = A^* \cdot \nu \cdot [J(v) + 4J(2v)]$$

In the motional narrowing regime, $A^* = \frac{1}{3} g^2 \Delta M_2$, with $g$ representing the proton gyromagnetic ratio and $\Delta M_2$ the reduction of the second moment caused by the motion. 50,51 We considered conformational and segmental reorientation dynamics of proton pairs on the same segment, disregarding contributions arising from interactions between different segments on the same macromolecule, which are of lower magnitude, 52 and used the HN function, $J_{\text{HN}}(v)$ (eqn (3)), to express the associated spectral density. 37 For PVB, $^1H$ longitudinal relaxation is mainly determined by the reorientations of the inter-proton CH$_2$ vector and, assuming isotropic motion, $A^* = 2.5 \times 10^9$ s$^{-2}$.

The experimental curves at 110 and 120 °C could be satisfactorily reproduced with a single HN function (see Fig. 5a and b), with $a \sim 1$, $b = 0.15$, and $A^*$ equal to $2.0 \times 10^9$ s$^{-2}$ and $2.4 \times 10^9$ s$^{-2}$, respectively. The $\tau_{\text{HN}}^{\text{NMR}}$ values, derived from the best fit $\tau_{\text{HN}}^{\text{NMR}}$ using eqn (4), are in good agreement with the $\tau_{\text{HN}}^{\text{NMR}}$ values (Fig. 3). For $a = 1$, the HN equation reduces to the Davidson–Cole one, a function usually employed to model glassy dynamics of polymers. Departures of $N_{\text{HN}}$ trends from this function, observed at temperatures much higher than $T_g$, have been ascribed to contributions to relaxation arising from slower collective polymer dynamics. 21,52–56 Hence, in our case the obtained values of $a$ indicate that the collective dynamics does not significantly contribute to relaxation, most probably because the measurements were performed only up to 50 K above the glass transition. Since glassy dynamics is not influenced by the chain length, 21 the polymer polydispersity is expected to play a minor role. The value of $b$ was quite small and much smaller than those found by DS for the $a$ process. Moreover, a single HN function could not satisfactorily reproduce the $N_{\text{HN}}$ curve at 100 °C.

The introduction of a second faster relaxation process, besides accounting for the observed FTS inapplicability, might also allow the $N_{\text{HN}}$ vs. frequency trends between 100 and 120 °C to be well reproduced with larger values of the $b$ parameter for the HN function describing the $a$ process. In this case, the NMR susceptibility can be written as:

$$N_{\text{HN}} = f_a \cdot N_{\text{HN},a} + f_b \cdot N_{\text{HN},b}$$

where $f_a$ represents the fraction of “mobile” protons involved in the $a$ process described by the susceptibility function $N_{\text{HN},a}$ introduced in eqn (7). In eqn (8), the contribution of methyl protons to $N_{\text{HN}}$ can be neglected since, at the investigated temperatures, the rotation about the $C_3$ axis certainly occurs at frequencies much higher than those explored here (see the ESI†). The contribution of protons in “slow” segments, related to the occurrence of dynamic heterogeneity and revealed by us through FID analysis, 29 can be safely neglected given their much longer $T_1$. Indeed, dynamic heterogeneity has been reported for amorphous polymers up to a few tens of degrees above $T_g$. 59,60

Since the $N_{\text{HN}}$ dispersions did not show features suitable for a univocal quantitative analysis in terms of two dynamic processes, we tentatively assumed that the secondary process was the $b$ relaxation process detected by DS measurements. In particular, this process was modeled with the Cole–Cole function ($b_0 = 1$) and the correlation times ($\tau_{\text{HN},b}$) were fixed to values extrapolated at the temperatures of interest according to the temperature dependence of $\tau_{\text{DS}}^{\text{HN},b}$ (see the black line in Fig. 3b). On the basis of the preliminary fittings of the curves at 110 and 120 °C mentioned above, the $a$ process was modeled with the Davidson–Cole function ($a_0 = 1$). With these assumptions, we could fit the experimental curves between 100 and 120 °C (Fig. 5c, d and e) with the parameters reported in Table 1. It must be noted that the fitting parameter $a_i$ is equal to $f_i A^*$. Interestingly, a combination of the $a$ and $b$ relaxation processes with the same assumptions on the parameters allowed the $N_{\text{HN}}$ curves at 80 and 90 °C to be well reproduced (Fig. 5e and h); the curve at 70 °C could be satisfactorily described considering the sole $b$ process (Fig. 5g). The best fit correlation times for the $a$ process were converted to the corresponding $\tau_{\text{HN}}^{\text{NMR}}$ values (shown in Fig. 3), in agreement with those derived from the $T_g$ minima.

Throughout the temperature range examined, no significant changes were found for the shape parameters $b_i$ and $a_i$. For the $b$ process, the $A_b$ factor initially slightly increased with increasing temperature, reaching a constant value at 90 °C. The low limiting value compared to that expected for a methylene isotropic motion indicates that the $b$ motion covers a restricted solid angle range, a feature expected for local motions. In the case of the $a$ process, $A_a$ increased in the whole temperature range, tending to a plateau at the highest temperatures. This trend can be accounted for considering that the fraction of protons involved in the $a$ process, $f_{a a}$, increases with the temperature up to a limit value. In fact, the fraction of the “mobile” protons progressively increases with temperature above $T_g$ at the expense of the rigid fraction. Dynamic heterogeneity with residual slow segments in an increasing rubbery matrix, with chain segments hierarchically entering the motional averaging regime, has been highlighted in other studies for temperatures up to $T_g + 40$ K. 60 The same phenomenon may involve the protons subject to the $b$ process,
thus justifying the initial increase of $A_b$. The limiting value of $A_a$ is compatible with an isotropic motion involving the CH$_2$ groups on
the main chain, for which a molar fraction of about 0.6 is estimated on the basis of the polymer composition.

Fig. 5 Experimental (circles) and calculated (black lines) $\chi''_{\text{NMR}}$ at the indicated temperatures. In (a and b) the $\chi''_{\text{NMR}}$ curves are fitted with a single HN function with the parameter values reported in the text. In (c–h) the fitting functions result from the sum of the HN contributions associated with the $\beta$ (blue line) and $\alpha$ (red line) relaxation processes. The fitting parameters are reported in Table 1.
The dynamics of PVB, including motions of the main chain and of the side groups, was studied across the glass transition acquiring information from both DS and FFC relaxation.

Above $T_g$, a primary process (α relaxation) due to segmental motions of the polymer chain was quantitatively characterized by DS measurements, covering wide temperature and frequency ranges on which FTS was found to apply. The analysis of DS data provided information on the change of the dynamic properties at the glass transition and, therefore, on the fragility of glassy PVB, exploiting the VFT equation. The α process was also detected using $^1$H FFC NMR, which provided correlation times in agreement with those determined using DS data analysis.

In the glassy state, a secondary process (β relaxation) associated with local motions of the chains inducing reorientations of the vinyl alcohol dipoles was clearly observed using DS, with an energy barrier of $11.1 \pm 0.2 \text{ kcal mol}^{-1}$. $^1$H FFC NMR relaxation data, acquired above $T_g$, were consistent with the occurrence of this β process, contributing to relaxation in the high frequency side of the investigated range. Nevertheless, propyl side chain motions, to which DS is not sensitive, could also concur to relaxation in the same frequency region. We safely excluded the relevance of the methyl motion for relaxation at the investigated temperatures and frequencies.

From a methodological point of view, we can state that, for PVB, characterized by a complex structure and a rather high $T_g$, DS has revealed to provide dynamic information more straightforwardly with respect to $^1$H FFC NMR. In fact, at temperatures close to $T_g$, the interpretation of $^1$H FFC data may be complicated by incomplete motional narrowing and by spin diffusion between protons in dynamically different domains. Nonetheless, $^1$H FFC NMR could grant additional information if suitable strategies are adopted. In particular, the use of instrumentation allowing measurements at temperatures higher than 120 °C could give access to detailed information on segmental and collective motions. Furthermore, the investigation of PVB samples selectively labeled with deuterium on different methylene groups, planned in our laboratory, is expected to allow the different contributions of main and side chains to the relaxation to be unraveled.

Conflicts of interest
There are no conflicts of interest to declare.

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References
31 The software is freely available at http://grafitylabs.com/.