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Cite this: *RSC Adv.*, 2016, 6, 55499

# Broadband-sensitive Ni<sup>2+</sup>–Er<sup>3+</sup> based upconverters for crystalline silicon solar cells†

Hom N. Luitel,\* Shintaro Mizuno, Toshihiko Tani and Yasuhiko Takeda

We have developed Ni<sup>2+</sup>, Er<sup>3+</sup> codoped CaZrO<sub>3</sub> broadband-sensitive upconverters that significantly broaden the sensitive range, and hence overcome the shortcomings of conventional Er<sup>3+</sup> doped upconverters used for crystalline silicon (c-Si) solar cells that utilize only a small fraction of the solar spectrum around 1550 nm. We have designed the combination of sensitizers and host material to utilize photons that are not absorbed by c-Si itself or Er<sup>3+</sup> ions. Six coordinated Ni<sup>2+</sup> ions substituted at the Zr<sup>4+</sup> sites absorb (1060–1450) nm photons and transfer the energies to the Er<sup>3+</sup> ions, and the Er<sup>3+</sup> upconverts at 980 nm. Co-doping with monovalent charge compensators such as Li<sup>+</sup> for high Er<sup>3+</sup> solubilisation at the Ca<sup>2+</sup> sites and multivalent ions (Nb<sup>5+</sup>) for stabilization of Ni<sup>2+</sup> at the Zr<sup>4+</sup> sites is essential. In addition to 1450–1600 nm ( $\approx 2 \times 10^{20} \text{ m}^{-2} \text{ s}^{-1}$ ) photons directly absorbed by the Er<sup>3+</sup> ions, we have demonstrated upconversion of 1060–1450 nm ( $\approx 6 \times 10^{20} \text{ m}^{-2} \text{ s}^{-1}$ ) photons in the Ni<sup>2+</sup> absorption band to 980 nm photons using the CaZrO<sub>3</sub>:Ni<sup>2+</sup>,Er<sup>3+</sup> upconverters. Compared with the current density gain of present c-Si solar cells ( $\sim 40 \text{ mA cm}^{-2}$ ), the upconverted photons could increase this by  $\sim 7.3 \text{ mA cm}^{-2}$ , which is about 18% improvement. This architecture for broadband-sensitive upconversion may pave a new direction for the improvement in efficiency of the present c-Si solar cells to surpass the limiting conversion efficiency of single-junction solar cells.

Received 26th April 2016  
Accepted 27th May 2016

DOI: 10.1039/c6ra10713c

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## 1. Introduction

Incident solar radiation is energetically broad and poses challenges for efficient conversion to electricity using solar cells consisting of finite bandgap semiconductors.<sup>1</sup> Even with an optimized crystalline silicon (c-Si) semiconductor,  $\sim 30\%$  of the incident radiation is not absorbed and is simply transmitted through the present c-Si solar cells. Considering the maximum conversion efficiency of single-junction solar cells,  $\sim 33\%$  sunlight into electricity in the radiative limit,<sup>2</sup> the unused near-infrared (NIR) radiation provides an important opportunity for enhancing the efficiency of solar cells. Although the NIR photons have insufficient energy, combining two or more infrared photons to generate a single visible or ultraviolet photon, a process known as upconversion, enables these NIR photons to contribute to solar energy conversion.<sup>3,4</sup> An upconversion layer can be placed at the back of a solar cell and converts a part of the transmitted photons to wavelengths that can be absorbed; it is straightforward to demonstrate a positive contribution from the upconversion layer.

Upconversion in various materials in which rare-earth ions are doped have been reported.<sup>5–9</sup> Among them, upconverters

using Er<sup>3+</sup> ions that convert 1550 nm photons to 980 nm photons are applied to c-Si solar cells,<sup>10–12</sup> while those using a combination of Er<sup>3+</sup> and Yb<sup>3+</sup>, which converts 970 nm to the visible photons, to amorphous silicon (a-Si), organic, and dye-sensitized solar cells.<sup>13–17</sup> However, the absorption bands of rare-earth ions originating from f–f transitions in the NIR region (700–2100 nm) are narrow, and hence only a small fraction of the solar spectrum can be utilized.<sup>17–19</sup> Thus, to realize highly efficient solar cells, efficient upconverters with sufficiently wide absorption spectra are desired. One of the approaches is to use a combination of rare earth ions with sensitizers that absorb photons in a broadband range, which are not directly absorbed by the rare-earth ions, and transfer the absorbed energies to the rare-earth ions. There are reports on upconversion of 970 nm photons to the visible (550, 650 nm) using the Er<sup>3+</sup>–Yb<sup>3+</sup> pairs where organic dyes function as the sensitizers that absorb photons in a range of 700–850 nm and transfer the energies to the Yb<sup>3+</sup> (ref. 19) and similarly Cr<sup>3+</sup> for 600–650 nm.<sup>20</sup> On the other hand, upconversion with a rather broadband sensitivity and a high efficiency has been demonstrated using triplet–triplet annihilation of organic molecules but the absorption range is limited up to 800 nm at present and thus can have applications only for a-Si, organic, and dye-sensitized solar cells.<sup>21–23</sup>

## 2. Materials design

There are detailed reports on absorption spectra of transition-metal ions that extend up to the NIR range.<sup>24–31</sup> It has been

Toyota Central Research and Development Laboratories Inc., 41-1, Yokomichi, Nagakute, Aichi 480-1192, Japan. E-mail: e1698@mosk.tytlabs.co.jp; takeda@mosk.tytlabs.co.jp; Tel: +81 956 717134

† Electronic supplementary information (ESI) available. See DOI: 10.1039/c6ra10713c



demonstrated that six coordinated  $\text{Ni}^{2+}$  ions located at the centers of octahedrons have substantial absorption around 1100–1400 nm that can further be tuned in a wide range by manipulating the crystal field strength around the  $\text{Ni}^{2+}$  ions.<sup>26,30,32</sup> Accordingly, its NIR emission band is also wide ranging from 1200 nm to longer than 1700 nm with extremely high quantum yield reaching unity in some crystals such as  $\text{LiGa}_5\text{O}_8$ .<sup>33</sup> There are other reports of the  $\text{Ni}^{2+}$  emission bands in the NIR ranges<sup>25–27,34–37</sup> that sufficiently overlap with the  $\text{Er}^{3+}$  absorption bands making possibility of  $\text{Ni}^{2+} \rightarrow \text{Er}^{3+}$  resonance energy transfer (sensitization).<sup>32,38,39</sup> Zhang *et al.* has reported that  $\text{Ni}^{2+}$  to  $\text{Er}^{3+}$  energy transfer or *vice versa* in glass ceramics depending on the host matrix and  $\text{Ni}^{2+}$  to  $\text{Er}^{3+}$  physical separation to achieve NIR broadband Stokes emission for amplifier and lasers. Furthermore, a high concentration of the  $\text{Ni}^{2+}$  sensitizers is required, because it is equivalent to high excitation intensity for the  $\text{Er}^{3+}$  emitters. In the similar way, the optimum  $\text{Er}^{3+}$  concentration should also be high, 10–25% range, to promote energy transfer between two neighbouring excited  $\text{Er}^{3+}$  ions in addition to excited state absorption in a single  $\text{Er}^{3+}$  ion.<sup>34</sup>

Thus, the host materials to realize broadband-sensitive upconversion using  $\text{Er}^{3+}$  and  $\text{Ni}^{2+}$  dopants are selected according to the following three criteria: (1) the host material must include cations located at octahedron centers, and should not include tetrahedron or other symmetry sites that can be occupied by  $\text{Ni}^{2+}$  ions. Four co-ordinated  $\text{Ni}^{2+}$  ions located at tetrahedron centers and  $\text{Ni}^{3+}$  have lower energy levels<sup>26,30</sup> and hence rapid relaxation occur rather than energy transfer to the  $\text{Er}^{3+}$  emitters after photoexcitation. (2) The ionic radius of the cations located at the octahedron centers should be close to or at least not much smaller than that of  $\text{Ni}^{2+}$  (0.069 nm) to enable a high  $\text{Ni}^{2+}$  concentration, otherwise introduced  $\text{Ni}^{2+}$  ions would change to smaller  $\text{Ni}^{3+}$  ions (0.056 nm) or segregate. (3) The host material should include bigger ions (favourably isoivalent to  $\text{Er}^{3+}$ ) such that sufficient amount of  $\text{Er}^{3+}$  can be solubilised. Most widely used upconversion materials such as  $\text{NaYF}_4:\text{Er}^{3+}$ ,  $\text{Y}_2\text{O}_2\text{S}:\text{Er}^{3+}$ , or  $\text{YF}_3:\text{Er}^{3+}$  (ref. 10 and 40) do not contain octahedron centers for  $\text{Ni}^{2+}$  hosting thus not suitable for the present purpose. We have already found that  $\text{ABO}_3$  type perovskite structures such as the  $\text{LaGaO}_3$  structure fulfil these criteria, because Ga ions (B sites) are located at the octahedron centers and the ionic radius of  $\text{Ga}^{3+}$  (0.062 nm) is similar to that of  $\text{Ni}^{2+}$ .  $\text{La}^{3+}$  ions (A sites) are isoivalent to  $\text{Er}^{3+}$  ions with very similar ionic radii. Under such materials design, we have successfully demonstrated the broadband-sensitive upconversion utilizing the Ni–Er pairs in  $\text{La}(\text{Ga},\text{Sc})\text{O}_3$ , where the  $\text{Ni}^{2+}$  sensitizers absorb the photons around 1100–1400 nm and transfer the absorbed energies to the  $\text{Er}^{3+}$  ions, followed by  $\text{Er}^{3+}$  upconversion at around 980 nm, highly suitable for c-Si solar cells.<sup>41</sup> However, the Ni-sensitized Er-upconverter exhibited low efficiency, and La and Sc used in the  $\text{La}(\text{Ga},\text{Sc})\text{O}_3$  compounds are extremely expensive. For practical applications, inexpensive materials with high upconversion efficiency are desired.

It has been reported that alkaline earth perovskites such as  $\text{CaZrO}_3$  are good hosts for rare earth doped phosphors and can solubilize as high as 20% rare earth ions when proper charge

compensators are utilized.<sup>42</sup> The crystal structure of  $\text{CaZrO}_3$  consists of  $\text{ZrO}_6$  octahedra and  $\text{CaO}_{12}$  polyhedra as depicted in Fig. 1(c). The 6-coordinated  $\text{Zr}^{4+}$  ions occupy the centres of octahedra. The ionic radius of  $\text{Zr}^{4+}$  is 0.072 nm (6-coordination) while that of  $\text{Ca}^{2+}$  is 0.112 nm (12-coordination).<sup>43</sup> Thus, it is expected that codoped  $\text{Ni}^{2+}$  ions (0.069 nm) occupy  $\text{Zr}^{4+}$  sites while  $\text{Er}^{3+}$  ions (0.106 nm) occupy the  $\text{Ca}^{2+}$  sites. When the tetravalent  $\text{Zr}^{4+}$  ions are substituted with divalent  $\text{Ni}^{2+}$  ions, oxygen vacancies are created for charge neutrality, which would cause parasitic absorption and nonradiative relaxation of excited  $\text{Ni}^{2+}$  and  $\text{Er}^{3+}$  ions. Further,  $\text{Ni}^{2+}$  ions located at the higher valence sites ( $\text{Zr}^{4+}$ ) would change to  $\text{Ni}^{3+}$  ions and do not contribute to upconversion as described above.<sup>30</sup>  $\text{Nb}^{5+}$  ions seem suitable as the charge compensators because they are stable and the ionic radius ( $\text{Nb}^{5+} \approx 0.064$  nm) is close to that of  $\text{Zr}^{4+}$  (0.072 nm). Furthermore, it has been reported that the substitution of larger or smaller ions into host cation sites remarkably distorts the crystal field from the ideal symmetry and hence changes the crystal field splitting.<sup>44</sup> As a result, the f–f transition probabilities improve leading to increased absorption and upconversion. In the  $\text{CaZrO}_3:\text{Er}$  system, substitution of

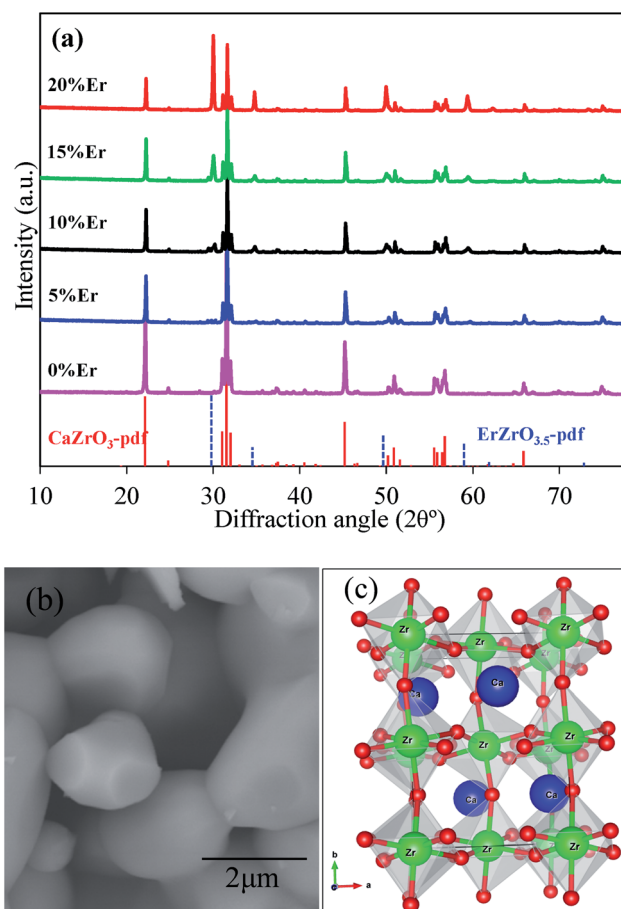


Fig. 1 (a) XRD patterns of  $\text{CaZrO}_3$  doped with 0.2 mol% Ni and different mol% Er. For comparison, standard pdf data of  $\text{CaZrO}_3$  (red solid lines) and  $\text{ErZrO}_{3.5}$  (blue dotted lines) are also shown. (b) SEM image of the typical sample and (c) crystal structure of  $\text{CaZrO}_3$  created by VESTA program.



**Table 1** Ionic radii of cations at different coordination environments<sup>31,43</sup>

Metal ions	Er <sup>3+</sup>	Ca <sup>2+</sup>	Li <sup>+</sup>	Na <sup>+</sup>	K <sup>+</sup>
Ionic radii (nm) (12 coordination)	0.106	0.112	0.092	0.118	0.151
Metal ions	Ni <sup>2+</sup>	Ni <sup>3+</sup>	Zr <sup>4+</sup>	Nb <sup>5+</sup>	
Ionic radii (nm) (6 coordination)	0.069	0.056	0.072	0.064	

a part of the Ca<sup>2+</sup> ions with smaller Er<sup>3+</sup> ions distorts the crystal structure and gives the possibility of improved upconversion. In addition, substitution of smaller (Li<sup>+</sup>) or bigger (K<sup>+</sup>) ions for the Ca<sup>2+</sup> ions further distorts the CaZrO<sub>3</sub> crystal, which can more remarkably increase the upconversion efficiency (Table 1).

Therefore, in the present study we have elaborately investigated the broadband-sensitive upconversion characteristics in the newly designed Ni<sup>2+</sup>-Er<sup>3+</sup> codoped CaZrO<sub>3</sub> that can significantly improve the conversion efficiency of present c-Si solar cells.

### 3. Experiments

#### 3.1. Synthesis of Er, Ni-codoped samples

We synthesized powder samples of CaZrO<sub>3</sub> codoped with Er<sup>3+</sup> and Ni<sup>2+</sup>. Equivalent amount of Li<sup>+</sup> ions (or Na<sup>+</sup>/K<sup>+</sup>) to that of Er<sup>3+</sup> ions and double amount of Nb<sup>5+</sup> ions to that of Ni<sup>2+</sup> ions were also co-doped for charge balance unless specified. Because Er<sup>3+</sup> occupy Ca<sup>2+</sup> sites and Ni<sup>2+</sup>, Nb<sup>5+</sup> substitute Zr<sup>4+</sup> sites, the compositions were determined as (Er<sub>x</sub>Li<sub>x</sub>Ca<sub>1-2x</sub>)(Zr<sub>1-3y</sub>Ni<sub>y</sub>Nb<sub>2y</sub>)O<sub>3</sub>. The compound oxide powders were synthesized using component metal-oxide or carbonate powders by the solid state reaction method. Predetermined amounts of the oxides/carbonates (Kojundo Kagaku, Japan) were well mixed with the help of small amount of ethanol and then dried at RT. Next the dry powders were again mixed well and heat-treated at 1400 °C for 6 h in air for reaction and crystallization. As synthesized powders might contain mixture of Ni<sup>2+</sup> and Ni<sup>3+</sup>, post annealing of the powder samples was carried out at 800 °C in N<sub>2</sub> gas flow to convert all the Ni<sup>3+</sup> ions to Ni<sup>2+</sup> ions.

The crystalline structures were identified by X-ray diffraction (XRD) using Cu-K $\alpha$  line in a range from 10 to 80 degree. Scanning electron microscope (SEM) observations were carried out using Hitachi SU3500.

#### 3.2. Optical measurements

Each powder sample was sandwiched between two glass plates with a 0.5 mm thick spacer. Absorption spectra were measured using an integrating sphere. To determine the photon flux at the Ni<sup>2+</sup> or Er<sup>3+</sup> absorption bands, we have integrated the standard AM1.5 spectral solar irradiation at earth surface<sup>45</sup> in the absorption range of Ni<sup>2+</sup> and Er<sup>3+</sup>, respectively. The reference spectrum is available in irradiance (W m<sup>-2</sup> nm<sup>-1</sup>) form, that was converted to the photon flux and current density forms. Continuous wave (CW) laser diodes of ~1 mW output power were used as excitation sources to acquire upconversion and Stokes emission spectra. Excitation beam intensity (mW cm<sup>-2</sup>) at the sample surface was obtained using a power meter and

a knife-edge and it was in the order of 10<sup>6</sup> mW cm<sup>-2</sup>. An optical parametric oscillator (OPO) pumped by the third harmonic of a Nd-YAG laser (7 ns pulse duration, 5–20 mW output power depending on output wavelengths) was employed for evaluation of wavelength dependent upconversion sensitivity and time-resolved measurements. Appropriate bandpass filters were used to receive emitted photons of desired wavelengths. Si and InGaAs photodiodes were used to detect the 980 nm and longer wavelength photons, respectively, and the output signal was accumulated using a storage oscilloscope.

## 4. Results and discussion

Fig. 1(a) shows XRD patterns of the CaZrO<sub>3</sub> doped with different mol% Er. The measured diffraction peaks of the powder samples matched well to those of the standard CaZrO<sub>3</sub> card data (PDF# 01-080-6213), and confirmed that the samples were well crystallized in the orthorhombic phase (oP20). The sharp peaks are indication of good crystallization of the particles. The SEM image presented in Fig. 1(b) with well determined facets further confirmed the highly crystallized particles. The particles dimension varied over a range of 1–5  $\mu$ m. The lattice constants calculated from the XRD result of the undoped CaZrO<sub>3</sub> sample are  $a = 5.5861$  Å,  $b = 8.012$  Å and  $c = 5.7568$  Å, which is in good agreement with the standard JCPDS card data (PDF# 01-080-6213). With increasing Er-doping concentration, the lattice constants ( $a$ ,  $b$ ,  $c$ ) and cell volume gradually decreased as summarised in the ESI S1† indicating smaller Er<sup>3+</sup> (0.106 nm) ions occupied the larger Ca<sup>2+</sup> (0.112 nm) sites. However, at/above 15 mol% Er addition, no further lattice contraction was observed indicating the limiting solid solubility of the Er<sup>3+</sup> ions in the CaZrO<sub>3</sub> host, which was confirmed by existence of distinct XRD peaks of Er<sub>2</sub>O<sub>3</sub> phase ( $\approx 2\theta = 30$  degree) in the XRD diagram in Fig. 1(a). On the other hand, no distinct lattice changes were observed by the Ni substitution at the Zr sites because the amount of Ni was very small (<0.5 mol%) in addition to the fact that the ionic size of Ni<sup>2+</sup> (0.069 nm) is very similar to that of Zr<sup>4+</sup> (0.072 nm). Further, because trivalent Er<sup>3+</sup> substituted divalent Ca<sup>2+</sup> ions, charge unbalance limited the solubility of Er<sup>3+</sup> in the CaZrO<sub>3</sub> matrix as observed by the existence of Er<sub>2</sub>O<sub>3</sub> peaks ( $2\theta = 29.4$  degree; PDF# 01-073-6274) in the Li free sample as shown in Fig. S2.† When equal amount of monovalent charge compensators such as Li<sup>+</sup>, Na<sup>+</sup>, K<sup>+</sup> were codoped together with Er<sup>3+</sup>, the solid solubility of Er<sup>3+</sup> in the CaZrO<sub>3</sub> host increased, and as a result the Er<sub>2</sub>O<sub>3</sub> phase disappeared (see ESI Fig. S2†). However, lower formation energy of pyrochlore structures (–3.88 eV) compared to the perovskite structures, CaZrO<sub>3</sub> (–3.66 eV), the ErZrO<sub>3.5</sub> pyrochlore phase was unavoidable at higher Er-doping concentration.<sup>46</sup> Reflecting the fact that codoped Li<sup>+</sup> (Na<sup>+</sup>/K<sup>+</sup>) occupied Ca<sup>2+</sup> sites, the lattice parameters and cell volume changed according to the ionic radii of these alkali ions (Fig. S2†).

The absorption spectra of the CaZrO<sub>3</sub> doped with 10 mol% Er and different mol% of Ni are presented in Fig. 2 and S3 (refer ESI S3† for visible absorption range). Sharp absorption peaks located at 970, 800, 660, 520, 490, 410, 380 nm and comparatively broad absorption band around (1450–1600) nm



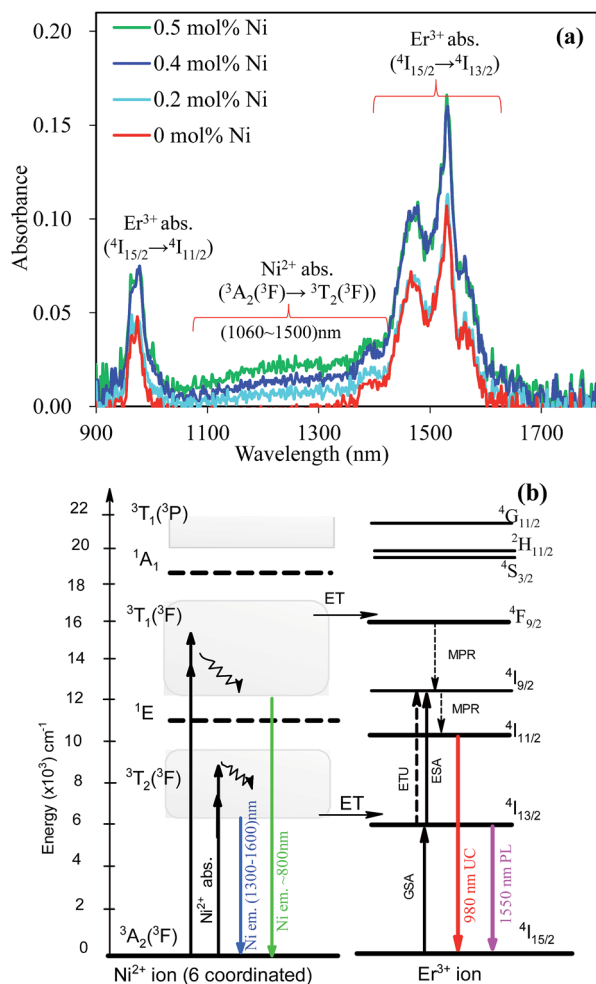


Fig. 2 (a) Absorption spectra of the  $\text{CaZrO}_3:10 \text{ mol}\% \text{ Er}$  codoped with different mol% of Ni exhibiting Er–Ni combined broadband absorption and (b) energy level diagram of the  $\text{Ni}^{2+}$  and  $\text{Er}^{3+}$  ions in the  $\text{CaZrO}_3$  host with possible transitions and Ni  $\rightarrow$  Er energy transfer.

were assigned to the f–f transitions of  $\text{Er}^{3+}$  ions,<sup>24,34</sup> while rather broad but comparatively weak absorption bands located around (1050–1500) nm, (680–860) nm and (390–460) nm were originated from the  ${}^3\text{A}_2({}^3\text{F})$  to  ${}^3\text{T}_2({}^3\text{F})$ ,  ${}^3\text{T}_1({}^3\text{F})$  and  ${}^3\text{T}_1({}^3\text{P})$  optically allowed transitions, respectively, of six coordinated  $\text{Ni}^{2+}$  ions.<sup>20,32</sup> No distinct  $\text{Ni}^{3+}$  absorption bands were identified indicating that most of the doped Ni stabilised as  $\text{Ni}^{2+}$  ions.<sup>25,33</sup> We used  $\text{Nb}^{5+}$  ions as charge compensator in double amount to that of doped Ni that might have stabilized the added Ni as  $\text{Ni}^{2+}$  ions. The relative locations of the energy levels of the  $\text{Er}^{3+}$  and  $\text{Ni}^{2+}$  ions are illustrated in Fig. 2(b). Furthermore, the  $\text{Ni}^{2+}$  absorption bands remarkably increased with increasing doped  $\text{Ni}^{2+}$  ion concentration. The extra broad  $\text{Ni}^{2+}$  absorption band (1060–1500 nm) in combination with the  $\text{Er}^{3+}$  absorption band (1450–1600 nm) covers the most of the NIR solar spectrum (1050–1600 nm) which is not absorbed by c-Si solar cells themselves and will have a great advantage for the spectral conversion purpose.

Fig. 3(a) and (b) show the upconversion spectra of the various mol% of Er (Li) doped  $\text{CaZrO}_3:0.2 \text{ mol}\% \text{ Ni}$  (Nb) samples when

excited at 1490 and 1300 nm, respectively. Under the 1490 nm excitation, corresponding to direct  $\text{Er}^{3+}$  excitation, clear upconverted emissions at around 980 nm were observed (Fig. 3(a)). In addition, very similar upconverted emissions appeared while excited at 1300 and 1180 nm (for 1180 nm excited UC see Fig. S5†) despite the excitation light was not absorbed by the  $\text{Er}^{3+}$  ions themselves. The maximal upconversion intensity was achieved at 15 mol% Er doping concentration under both the 1300 and 1490 nm excitations. Further, it has been confirmed that the upconverted emission at 980 nm was proportional to the square of the Er concentrations for both excitation wavelengths at lower concentrations as depicted in the insets of Fig. 3(a) and (b). The power dependent upconversion intensity measurements confirmed that the present upconversion is two photon processes under both the 1490 and 1300 nm excitations (Fig. 3(c)).

Fig. 4 compares the Stokes emissions of the Ni (Nb) only doped and Er, Ni (Li, Nb)-codoped samples excited at 1180 nm. For the Ni only doped (no Er) sample, broad emission band ranging from 1300 nm to 1600 nm originated from the  ${}^3\text{T}_2({}^3\text{F}) \rightarrow {}^3\text{A}_2({}^3\text{F})$  transition of  $\text{Ni}^{2+}$  was observed.<sup>26–33</sup> However, by introducing  $\text{Er}^{3+}$  ( $\text{Li}^+$ ) co-dopants, the  $\text{Ni}^{2+}$  emission almost disappeared and  $\text{Er}^{3+}$  emissions at around 1550 nm ( ${}^4\text{I}_{13/2} \rightarrow {}^4\text{I}_{15/2}$ ) and 980 nm ( ${}^4\text{I}_{11/2} \rightarrow {}^4\text{I}_{15/2}$ ) appeared (see Fig. S5† for 1180 nm excited UC at 980 nm). This suggests that the energies absorbed by the  $\text{Ni}^{2+}$  ions transferred to the  $\text{Er}^{3+}$  ions, followed by the  $\text{Er}^{3+}$  emissions *i.e.* the  $\text{Ni}^{2+}$  ions act as donors while  $\text{Er}^{3+}$  acceptors. Further, under sufficient  $\text{Er}^{3+}$  co-doping (15 mol% or higher), the  $\text{Ni}^{2+}$  emission was almost perfectly quenched and only the  $\text{Er}^{3+}$  emission appeared, indicating the Ni  $\rightarrow$  Er energy transfer efficiency was close to unity. The energy transfer efficiency estimated from the ratio of the  $\text{Ni}^{2+}$  emission intensities integrated over 1300–1450 nm in the Ni only doped sample (0.2 mol% Ni) and Ni–Er codoped sample (0.2 mol% Ni, 10 mol% Er) was as high as 84%. However, at lower  $\text{Er}^{3+}$  concentrations, the  $\text{Er}^{3+}$  ions were far apart from the  $\text{Ni}^{2+}$  ions and the Ni  $\rightarrow$  Er energy transfer was less efficient, as a result,  $\text{Ni}^{2+}$  emission was detected although it was weak. The energy transfer efficiency and subsequent excited  $\text{Er}^{3+}$  number should increase with the  $\text{Er}^{3+}$  concentration, and consequently the  $\text{Er}^{3+}$  Stokes emission intensity. In fact, the  $\text{Er}^{3+}$  Stokes emission, which is a one-photon process, was proportional to the Er concentration (see Fig. S4†). On the other hand,  $\text{Er}^{3+}$  upconversion (980 nm) is a two-photon process (Fig. 3(c)); it means two excited  $\text{Er}^{3+}$  ions are utilised to emit a single upconverted photon at a shorter wavelength. Thus, the upconversion emission intensity should be proportional to the square of the  $\text{Er}^{3+}$  ion concentration, which was obeyed at relatively lower  $\text{Er}^{3+}$  concentrations. However, at higher  $\text{Er}^{3+}$ -doping concentrations, the Ni  $\rightarrow$  Er energy transfer efficiency saturated and concentration quenching processes predominates, consequently the upconversion and Stokes emissions weakened.<sup>34</sup>

Effect of the  $\text{Ni}^{2+}$ -doping concentration on the upconversion spectra of  $\text{CaZrO}_3:15 \text{ mol}\% \text{ Er(Li)}$  are presented in Fig. 5. At the beginning, the upconversion intensity increased with increasing Ni-doping concentration that is due to increased Ni absorption as depicted in Fig. 2(a). However, at slightly higher



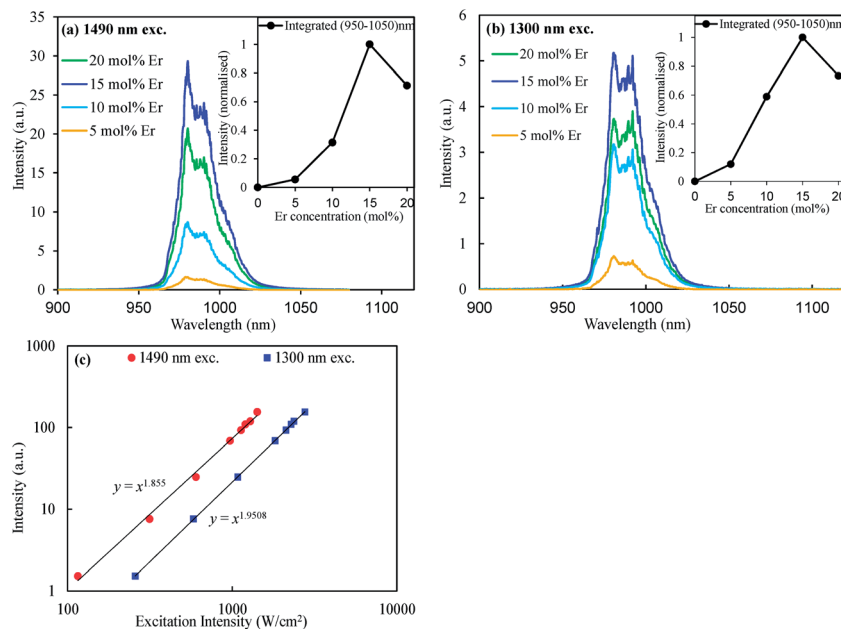


Fig. 3 Upconversion spectra of the  $\text{CaZrO}_3:0.2 \text{ mol\% Ni}$  codoped with different mol% of Er excited at (a) 1490 nm, and (b) 1300 nm. (c) Power-dependent UC intensity of the  $\text{CaZrO}_3:0.2 \text{ mol\% Ni}^{2+}, 15 \text{ mol\% Er}^{3+}$  under 1490 and 1300 nm excitations. Inset in the (a) and (b) are the dependence of the UC intensities integrated over 950–1050 nm with the  $\text{Er}^{3+}$  ion concentration.

Ni concentrations, the upconversion intensity decreased rapidly. The reason of the decrease would be due to remarkable non-radiative relaxation through concentration and defect-related quenching as oxygen vacancies may increase at higher Ni concentrations.<sup>41</sup> The energy transfer efficiency is expected to be independent of the  $\text{Ni}^{2+}$  concentrations because the  $\text{Ni}^{2+}$  concentration is very low compared to the  $\text{Er}^{3+}$  concentrations. Thus increased  $\text{Ni}^{2+}$  absorption enhanced the overall energy transfer and hence intensified the  $\text{Er}^{3+}$  upconversion. However, effects of high absorption and energy transfer efficiency were overcome by nonradiative loss at a relatively higher  $\text{Ni}^{2+}$

concentration as mentioned above and reduced the overall upconversion intensity. Inset in the Fig. 5 shows the effect of  $\text{Nb}^{5+}$  concentration on the upconverted emission integrated over 950–1050 nm. By introducing proper amount of  $\text{Nb}^{5+}$  ions (twice the amount of  $\text{Ni}^{2+}$ ) the upconverted emission intensity was almost doubled. Since,  $\text{Ni}^{2+}$  ions were introduced at the  $\text{Zr}^{4+}$  sites, charge imbalance reduced the solubility of  $\text{Ni}^{2+}$  ions into the  $\text{CaZrO}_3$  host (no Ni-phase was detected due to low doping

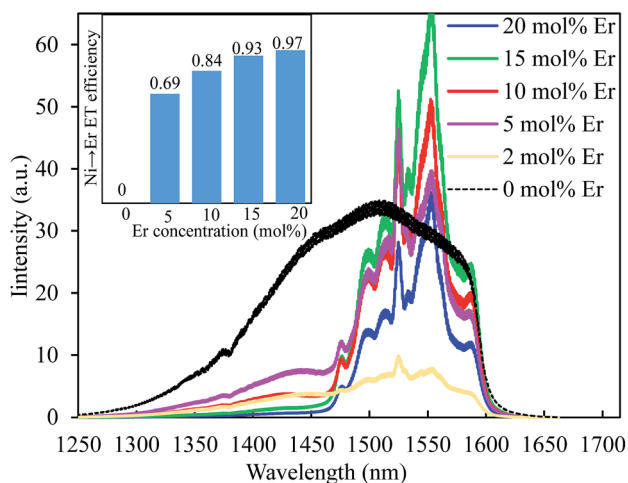


Fig. 4 Stokes emission spectra of the Ni (Nb) only doped (dotted line) and different mol% of Er (Li) codoped  $\text{CaZrO}_3$  samples excited at 1180 nm.

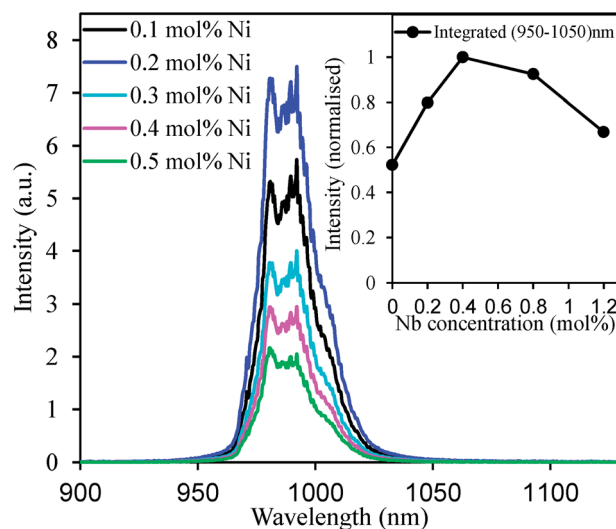


Fig. 5 Upconversion spectra of the  $\text{CaZrO}_3:15 \text{ mol\% Er}$  codoped with different mol% of Ni excited at 1300 nm. Inset is the effect of  $\text{Nb}^{5+}$  doping concentrations on the upconverted emission intensity (integrated over 950–1050 nm) of  $\text{CaZrO}_3:15 \text{ mol\% Er}^{3+}, 0.2 \text{ mol\% Ni}^{2+}$  samples.



concentration) or stabilised the Ni<sup>3+</sup> ions to reduce the stress of charge imbalance. Substitution of two Nb<sup>5+</sup> ions at Zr<sup>4+</sup> sites for each Ni<sup>2+</sup> addition balanced the total charge that might have increased the Ni-solubility as well as stabilize the Ni<sup>2+</sup>. As a result, improved upconverted emission intensity was detected.

To evaluate the Ni → Er energy transfer rate quantitatively, time-resolved decay profiles were recorded. Typically, the Ni<sup>2+</sup> emission at 1400 nm was recorded for the Ni only doped (no Er) and Ni, Er-codoped (0.2 mol% Ni, 10 mol% Er) samples under the 1180 nm pulsed excitation. The results are presented in Fig. 6. The time-dependent Ni<sup>2+</sup> emission intensity of the Ni only doped (no Er) sample  $I_{\text{Ni(no Er)}}(t)$  was well fitted using a double exponential eqn (1) mentioned below:<sup>39</sup>

$$I_{\text{Ni(no Er)}}(t) = a_{\text{Ni}} \exp[-t/\tau_{\text{Ni}}^{(1)}] + (1 - a_{\text{Ni}}) \exp[-t/\tau_{\text{Ni}}^{(2)}] \quad (1)$$

The Ni<sup>2+</sup> emission lifetimes  $\tau_{\text{Ni}}$  are determined by

$$\tau_{\text{Ni}} = (a_{\text{Ni}}\tau_{\text{Ni}}^{(1)^2} + (1 - a_{\text{Ni}})\tau_{\text{Ni}}^{(2)^2}) / (a_{\text{Ni}}\tau_{\text{Ni}}^{(1)} + (1 - a_{\text{Ni}})\tau_{\text{Ni}}^{(2)}) \quad (2)$$

From the fitting data,  $\tau_{\text{Ni}}$  was found to be ~0.6 ms for 0.2 mol% Ni (Nb) only doped CaZrO<sub>3</sub>, which is comparable with the previously reported values for other oxide hosts.<sup>47,48</sup>

When the Er<sup>3+</sup> acceptors were introduced, the Ni<sup>2+</sup> emission intensity decreased more rapidly, because of the energy transfer from the Ni<sup>2+</sup> donors to the Er<sup>3+</sup> acceptors. The effect of the energy transfer on the time evolution of the emission intensity of the Ni<sup>2+</sup> donors is expressed as  $\exp[-\gamma_{\text{Ni} \rightarrow \text{Er}} \sqrt{t}]$  when energy migration among the donors is negligibly weak,<sup>38,39</sup> whereas it is described by an exponential function  $\exp[-w_{\text{Ni} \rightarrow \text{Er}} t]$  for significant migration.<sup>49–51</sup> In the present case, the acquired data are fitted by the former better than the latter, *i.e.*,

$$I_{\text{Ni(Er co-doped)}}(t) = \exp[-\gamma_{\text{Ni} \rightarrow \text{Er}} \sqrt{t}] I_{\text{Ni(no Er)}}(t) \quad (3)$$

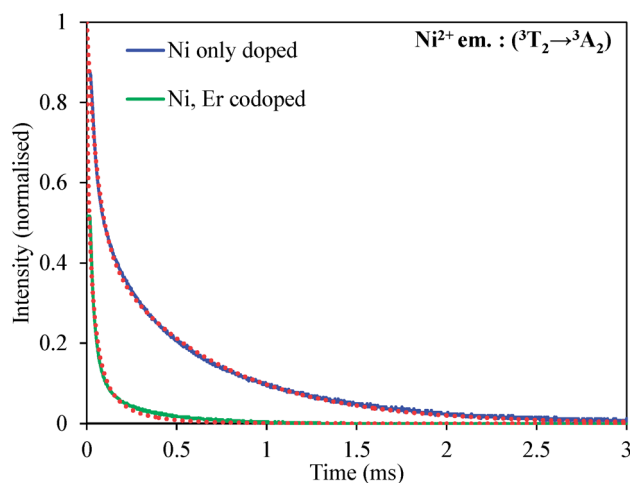


Fig. 6 Decay profiles of the Ni<sup>2+</sup> emission at 1400 nm for the Ni (Nb) only doped (no Er) and Ni, Er (Nb, Li) codoped CaZrO<sub>3</sub> samples under the 1180 nm pulsed excitation. Red dotted lines are the results of fitting.

This is consistent with the facts that the Ni concentration is as low as 0.2 mol% and the energy transfer is completed within sub-milliseconds. Using eqn (1) and (3), the energy transfer efficiency  $\eta_{\text{Ni} \rightarrow \text{Er}}$  is derived as follows,

$$\eta_{\text{Ni} \rightarrow \text{Er}} = 1 - \int_0^\infty dt I_{\text{Ni(Er co-doped)}}(t) / \int_0^\infty dt I_{\text{Ni(no Er)}}(t) \quad (4)$$

The efficiency obtained from the time-resolved data was about 86%, which is very close to the result obtained from the steady-state Ni-emission intensities as mentioned earlier.

Fig. 7 shows the effect of monovalent ions (Li<sup>+</sup>, Na<sup>+</sup>, K<sup>+</sup>) substitution on the upconversion intensity of the Er, Ni codoped CaZrO<sub>3</sub> upconverters. Addition of equivalent amount of alkali ions to that of doped Er<sup>3+</sup> ions remarkably increased the upconversion intensity. Because the Er<sup>3+</sup> ions (0.106 nm) were substituted for the Ca<sup>2+</sup> (0.112 nm) sites, there was imbalance of the total charge. As a result, stress was produced that limits the solubility of the Er<sup>3+</sup> ions in CaZrO<sub>3</sub> host, which was confirmed by the existence of segregated Er<sub>2</sub>O<sub>3</sub> impurity phase in the XRD patterns as stated previously (Fig. S2†). When the equivalent amount of monovalent ions such as Li<sup>+</sup>, Na<sup>+</sup>, K<sup>+</sup> *etc.* were added, the charge neutrality was maintained, and consequently the Er<sup>3+</sup> impurity phase was remarkably reduced (see Fig. S2†). There were no significant differences in the absorption peak positions of the Er<sup>3+</sup> and Ni<sup>2+</sup> but remarkable enhancement of the peak intensities around the Er<sup>3+</sup> and Ni<sup>2+</sup> absorption bands was observed (see Fig. S6†). The enhanced absorption of Er<sup>3+</sup> is obviously due to increased numbers of the Er<sup>3+</sup> ions inside the CaZrO<sub>3</sub> lattice, resulting in more intense upconversion. However, the upconversion intensity was found in the order of Li<sup>+</sup> >> K<sup>+</sup> > Na<sup>+</sup> > no alkali ions, and could not be explained by charge compensation only. The f–f electronic transitions of rare earth ions are partially forbidden. As a result, they exhibit low

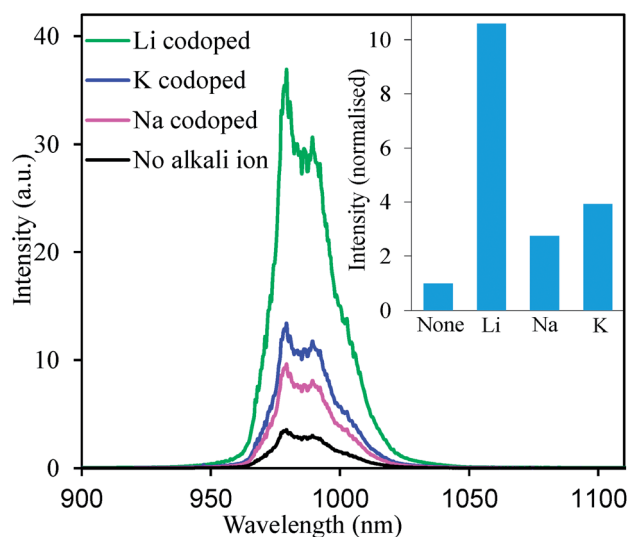


Fig. 7 Upconversion spectra of CaZrO<sub>3</sub>:Er<sup>3+</sup>, Ni<sup>2+</sup> codoped with alkali ions excited at 1180 nm. Inset is the variation of integrated upconversion intensity over 950–1050 nm with Li<sup>+</sup>, Na<sup>+</sup>, K<sup>+</sup> ions substitutions.



transition probabilities in presence of inversion symmetry.<sup>44</sup> It has been reported that substitution of larger or smaller ions into host cation sites remarkably distorts the crystal geometry from the ideal symmetry and hence changes the crystal field splitting.<sup>44</sup> As a result, the f-f transition probabilities increase and absorption originating from the  $\text{Er}^{3+}$  pronounce. The similar trend was observed in the present case too, where the  $\text{Er}^{3+}$  absorption bands were pronounced more by the substitution of the smaller  $\text{Li}^+$  ions (0.092 nm) at the  $\text{Ca}^{2+}$  sites (0.112 nm) than the similar sized  $\text{Na}^+$  ions (0.118 nm). Substitution with  $\text{K}^+$  ions (0.151 nm) is also expected to intensify the upconversion as with  $\text{Li}^+$  ions, however,  $\text{K}^+$  ions are much larger than  $\text{Ca}^{2+}$  ions and it is difficult to occupy the  $\text{Ca}^{2+}$  sites. Thus, some of the added  $\text{K}^+$  ions (hence the same number of the  $\text{Er}^{3+}$  ions) did not exist inside the  $\text{CaZrO}_3$  crystals and remained at the surfaces. Nonradiative transitions from surface ions (here  $\text{Er}^{3+}$  ions) will be pronounced due to rapid migration of excited energy to the surface defects.<sup>52</sup> Thus, lower  $\text{Er}^{3+}$  concentration inside the  $\text{CaZrO}_3$  lattice and existence of considerable amount of  $\text{Er}^{3+}$  ions at the surfaces made the  $\text{K}^+$ -substituted samples less efficient compared to the  $\text{Li}^+$ -substituted samples. Furthermore, the  $\text{K}^+$ -substituted sample exhibited lower crystallinity as seen by weaker XRD peak intensity depicted in Fig. S2.† It is well known that luminescence is crystallinity dependent; higher the crystallinity the better is the luminescence performance.

Fig. 8 shows the absorption, excitation and upconverted emission spectra of the  $\text{CaZrO}_3$ :15 mol%  $\text{Er}(\text{Li})$ , 0.2 mol%  $\text{Ni}(\text{Nb})$  sample. The excitation spectrum was obtained from the upconverted emission intensity normalized by the square of the excitation photon flux (due to two-photon process), namely, the emission intensity at a constant excitation photon flux. The upconverter developed here provides broadband sensitivity ranging from 1060 nm to longer than 1600 nm as seen from the excitation spectrum. It further suggests that quite strong upconversion was achieved at the  $\text{Er}$ -absorption band while

comparatively weak at the  $\text{Ni}$ -absorption band, which is in accordance to the absorbance at the corresponding wavelengths. We have compared the upconversion intensities of such a broadband sensitive upconverter developed here with the previously reported similar upconverter (see ESI S7†) and concluded that the upconversion emission of the  $\text{CaZrO}_3$ : $\text{Er}$ , $\text{Ni}$ -based upconverter is about 1.7 times stronger. Further, the new upconverter developed here can efficiently absorb 1350–1450 nm light even though the solar irradiation at these wavelengths is weak.

The photon flux in the solar spectrum integrated over the  $\text{Er}^{3+}$  absorption band (1450–1600 nm) is about  $2.0 \times 10^{20} \text{ m}^{-2} \text{ s}^{-1}$ , which is equivalent to  $\sim 1.93 \text{ mA cm}^{-2}$  current density gain for c-Si solar cells assuming perfect upconversion.<sup>45</sup> Introduction of the  $\text{Ni}^{2+}$  sensitizers increases the absorbed photon flux by  $6.0 \times 10^{20} \text{ m}^{-2} \text{ s}^{-1}$  (1060–1450 nm), leading to an additional gain of  $\sim 5.94 \text{ mA cm}^{-2}$  that is more than 3 times the gain originating from the  $\text{Er}^{3+}$  absorption alone. The optimum current density gain of present silicon solar cell is about  $40 \text{ mA cm}^{-2}$ .<sup>53</sup> Assuming perfect absorption and upconversion, the newly developed  $\text{CaZrO}_3$ : $\text{Ni}^{2+}$ , $\text{Er}^{3+}$  upconverter can contribute  $\sim 7.3 \text{ mA cm}^{-2}$  current density gain of present c-Si solar cells that corresponds to nearly  $\sim 18\%$  increase in gain. However, to realize such efficient broadband-sensitive upconverters, and hence higher c-Si solar cell efficiency, further improved  $\text{Ni}^{2+}$  and  $\text{Er}^{3+}$  absorption is essential and it can be achieved, for example, by coupling with plasmons at the desired wavelengths and such experiments will be conducted in near future.

## 5. Conclusions

To improve conversion efficiency of c-Si solar cells, we have developed a new class of broadband-sensitive upconverter,  $\text{CaZrO}_3$ : $\text{Ni}^{2+}$ , $\text{Er}^{3+}$  that absorbs photons in a broad wavelength range *viz.* 1060–1600 nm and emits photons at 980 nm to be efficiently absorbed by c-Si solar cells. We used 6-coordinated  $\text{Ni}^{2+}$  located at the octahedron centers ( $\text{Zr}^{4+}$ -sites) and 12-coordinated  $\text{Er}^{3+}$  located at the  $\text{Ca}^{2+}$  sites, such that efficient energy transfer from the  $\text{Ni}^{2+}$  to the  $\text{Er}^{3+}$  was achieved. Further, optimization of the  $\text{Ni}^{2+}$  and  $\text{Er}^{3+}$  concentrations and addition of charge compensators to reduce the stress caused by the  $\text{Er}^{3+}$  and  $\text{Ni}^{2+}$  doping significantly improved the upconversion efficiency. Assuming ideal upconversion, the newly developed  $\text{CaZrO}_3$ : $\text{Ni}^{2+}$ , $\text{Er}^{3+}$  upconverter can contribute  $\sim 7.3 \text{ mA cm}^{-2}$  current density gain of present c-Si solar cells ( $\sim 40 \text{ mA cm}^{-2}$ ) which corresponds to nearly  $\sim 18\%$  increase in gain. Such broadband-sensitive absorption of sub-bandgap photons above the absorption edge of c-Si solar cells and upconverting them to the most sensitive range (980 nm) of the cell offer a clear route towards surpassing the limiting conversion efficiency of single-junction solar cells, and further enable new applications in sub-bandgap detector sensitization and many more.

## Acknowledgements

This work was partially supported by Advanced Low Carbon Technology Research and Development Program (ALCA), Japan Science and Technology Agency.

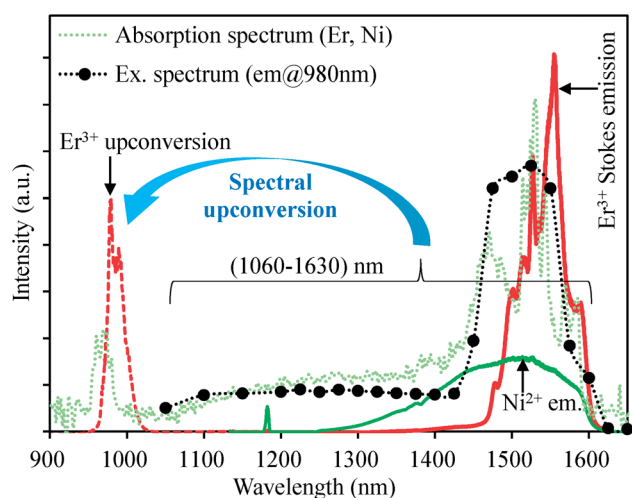


Fig. 8 Illustration of broadband-sensitive upconversion in the  $\text{CaZrO}_3$ : $\text{Ni}^{2+}$ , $\text{Er}^{3+}$  upconverter along with the  $\text{Ni}$  and  $\text{Er}$  Stokes emissions excited at 1180 nm.



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