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Anisotropic thermal motion in transition-metal carbonyls from experiments and *ab initio* theory†

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The thermal motion of atoms in crystals is quantified by aniso-tropic displacement parameters (ADPs). Here we show that dis-persion-corrected periodic density-functional theory can be used to compute accurate ADPs for transition metal carbonyls, which serve as model systems for crystalline organometallic and coordi-nation compounds.

Continuing work to synthesize new chemical compounds is giving rise to an ever-growing number of known structures. For organic and organometallic crystals, this knowledge is col-lected in the Cambridge Structural Database,[1] which is growing not only in size, but also regarding the quality and depth of information. Careful experiments yield reliable inten-sity data and trustworthy anisotropic displacement parameters (ADPs),[2] which allow refinements to be improved and subtle internal inconsistencies identified. ADPs can help to develop or even disprove a candidate structural model and are routinely requested for newly synthesized organometallic compounds. Physically meaningful ADPs convey information about struc-tural dynamics and translate this into instructive ellipsoid drawings; the Oak Ridge Thermal Ellipsoid Plot (ORTEP) program has just reached its 50th anniversary.[3]

Unfortunately, the most common method of quantifying ADPs – namely, X-ray diffraction (XRD) – has inherent limit-ations. The visibility of a scattering centre in XRD scales with its electron count. Improved XRD hardware and methodology

now available allow charge density studies to be carried out,[4] even on systems of lower suitability,[5] and accurate ADPs can be determined from XRD measurements for light atoms next to heavy atoms, although this requires a higher resolution.[6] For Mo Kα radiation, a recent study identified a minimum of $2\theta_{max} > 65°$ for determining reliable ADPs;[7] this target resolu-tion is currently out of experimental reach when using Cu Kα radiation for single-crystal XRD. We will address high-resolu-tion XRD and neutron diffraction as experimental solutions in the quest for reliable ADPs, but at the heart of this work is an emerging, alternative route of predicting ADPs from *ab initio* theory. Over recent years, quantum-chemical computations in general have proved to be valuable tools for molecular crystal-lographers in validating structures,[8] assisting with H atom localization[9] and in ranking or even predicting complex mole-cular crystal structures.[10] And likewise, it has very recently become possible to compute ADPs from first principles.[11–13]

We used dispersion-corrected density functional theory (DFT-D)[18] to compute ADPs for representative carbonyl com-pounds of transition metals (Table 1) and validated the results against experimental benchmarks. We discuss the compounds in sequence and use each example to address pertinent ques-tions regarding theoretical but also experimental aspects and limitations. This proof-of-concept study may open the way towards a more routine application of *ab initio* ADPs in organo-metallic chemistry.

We begin with chromium hexacarbonyl $Cr(CO)_6$ (**1**), a text-book example of a transition-metal carbonyl that has been widely studied from very early, almost historical, experi-ments[15,19] to more recent ones with higher accuracy.[20] We per-formed a separate high-resolution diffraction experiment on **1**. The displacement ellipsoids from our measurements and from DFT-D (Fig. 1) are in excellent agreement and practically no difference can be seen with the naked eye.

How close is this agreement numerically? To answer this question, we first inspected the equivalent isotropic displace-ment parameter, U_{eq}, for each symmetry-independent atom in **1** (Table 2). We compared the computed values with the experi-mental values, but before had to answer an even more funda-

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Table 1 Overview of the studied compounds with parameters for the respective experimental benchmarks, as well as the quality of the DFT-D structural description (RMS; see Methods section).[8,14] All RMS values are very low, which was a *conditio sine qua non* for this study

Compound	Cambridge structural database ref. code	Experimental parameters	RMS (Å)
1[a]	FOHCOU	X-rays, room temp. (ref. 15)	0.04
		X-rays, 100 K (this work)	0.02
2	BZCRCO	X-rays, 78 K (ref. 16)	0.11
		Neutrons, 78 K (ref. 16)	0.04
3	BOTTAF	Neutrons, 12 K (ref. 17)	0.05

[a] There are several previous reports of **1** (see text); for conciseness, we only list the results from an exemplary room-temperature experiment and our own low-temperature data.
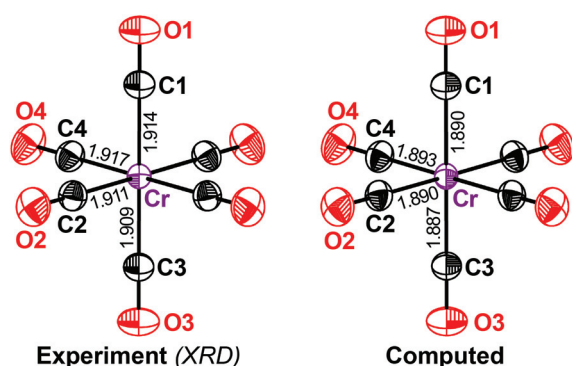

Fig. 1 Displacement ellipsoids for crystalline **1** at the 90% probability level, comparing XRD results (left-hand panel) with DFT-D based phonon computations (right-hand panel); both refer to a temperature of 100 K. Symmetry-inequivalent atom labels are given, together with the respective Cr–C distances (in Å).

Table 2 Equivalent displacement parameters[21] U_{eq} (10^{-4} Å²) for all symmetry-inequivalent atoms in crystalline **1**. For the experimental data based on Mo Kα radiation, we compared truncated ($2\theta \leq 90°$) and full high-resolution datasets; see text for details

	Single-crystal XRD		Computed results
	($2\theta \leq 90°$)	($2\theta \leq 110°$)	(DFT-D)
Cr	85.2(3)	92.8(3)	97.4
C(1)	129(1)	136(1)	135
C(2)	125(1)	132(1)	131
C(3)	127(1)	135(1)	133
C(4)	129(1)	136(1)	136
O(1)	196(1)	203(1)	201
O(2)	192(1)	199(1)	195
O(3)	199(1)	206(1)	206
O(4)	203(1)	209(1)	208

mental question: how accurate is our experimental benchmark?

For comparison, refinements of the structural model for **1** were carried out based on data with a resolution better than 1.15 Å⁻¹ (corresponding to an elevated maximum scattering angle of $2\theta = 110°$ with Mo Kα radiation) and also, in parallel, for a purposefully truncated dataset (up to 0.99 Å⁻¹ or 90°). In other words, we report here a "tailored" experiment on **1** in which we probed the effect of resolution. Note that even our truncated dataset exceeded that of most everyday laboratory experiments (usual resolution 0.6–0.7 Å⁻¹). Still, the value of U_{eq} and thus the ADPs at limited resolution are consistently smaller than those at high resolution (Table 2) and this difference is an order of magnitude larger than the standard uncertainties. This is important for any future benchmarking of computed ADPs.

Fundamentally, this effect is not surprising: X-rays interact with the electron cloud of an atom and hence XRD probes the electronic density. (The obvious alternative is neutron diffraction, to which we will come back when discussing **2**.) In XRD, low-order reflections also carry information about the valence electrons between the nuclei, whereas higher-resolution data emphasize the core electrons; the latter will thus better reproduce the properties dominated by nucleic positions, such as lattice vibrations. Experimental ADPs will therefore depend on the resolution and be better described by high-resolution data. This is precisely what is seen in Table 2.

Using higher-order diffraction data *only* will provide ADPs similar to those from the complete, high-resolution dataset; tentative high-order refinements confirmed this expectation for **1**. This is, however, not the norm in many routine laboratory experiments, where such high-order data will be simply unavailable and ADPs from standard refinements with spherical scattering factors will suffer from the limitations seen in Table 2. In principle, using aspherical scattering factors can improve the situation (even if the available resolution does not allow the deconvolution of deformation due to asphericity and thermal motion). Such aspherical scattering factors may be obtained *via* several approaches based on transferability[22] or from Hirshfeld atom refinement.[23] Notably, the computationally more demanding iterative Hirshfeld atom refinement has even allowed to refine ADPs for H atoms from XRD data at standard resolution.[24]

Returning to the computed values of U_{eq} in **1**, our results for the carbonyl ligands are almost without exception within the error range of the high-resolution experiment. Even more importantly for the present study, the value of U_{eq} for the transition-metal centre is also very well reproduced (Table 2). The DFT-D result for the Cr atom differs from the experimental value by *c.* 5%, which is less than the effect of resolution alone (*c.* 8%).

From this encouraging, but admittedly simple, example, we moved to a slightly more complex one: the "piano stool" molecule (η^6-benzene)-tricarbonyl-chromium (**2**), a representative of a half-sandwich compound with a hexahapto benzene ring bonded to the metal atom. It has been studied both by XRD
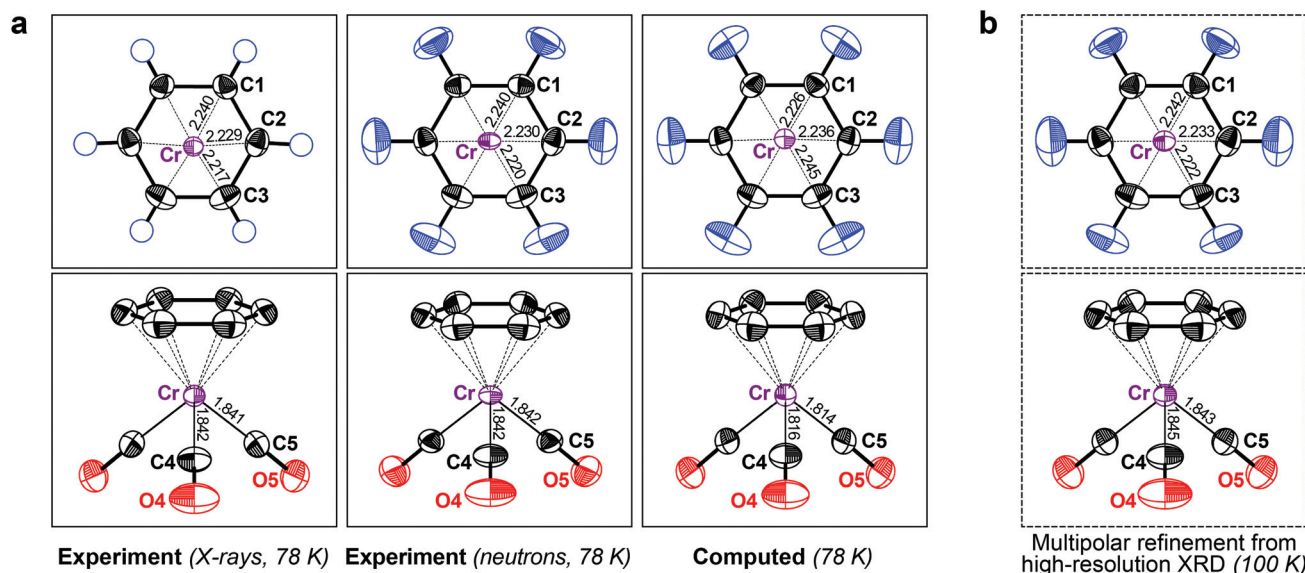
Fig. 2 (a) Displacement ellipsoids (90% probability at 78 K) for crystalline **2**, comparing X-ray (left) and neutron diffraction results (middle; both data-sets from ref. 16) with DFT-D based phonon computations (right). (b) Results of a multipolar refinement of high-resolution XRD data (at 100 K; data from ref. 25; see also ESI†).

and neutron diffraction experiments,[16] which allows for side-by-side comparison. Both previous results are compared with our DFT-D data in Fig. 2a.

We began by assessing the experimental benchmarks. The first difference between the two methods is obvious: no ADPs for H atoms are available from the 1973 XRD experiment. Although neutron diffraction did give hydrogen ADPs (Fig. 2a), its performance is otherwise not *a priori* better than that of XRD; the standard uncertainties of the neutron experiment by Rees and Coppens[16] are rather high and the authors reported a potential problem with the data. The neutron-derived ADPs for Cr are smaller in two axes and larger in the third and thus they are more anisotropic. This is, however, not inherent to the measurement technique: similar shapes for neutron and XRD derived ADPs have been confirmed in two independent experiments, but these studies also found significant differences in magnitude for both parameter sets. The reported discrepancies were 11% (ref. 26) and 5% (ref. 27), again orders of magnitude larger than the respective standard uncertainties.

In this light, the performance of the theoretical method for **2** is even more encouraging. DFT-D readily predicts the elusive hydrogen ADPs (Fig. 2a) in good agreement with the neutron benchmark, both with respect to size and anisotropy (the "rugby-ball-ness") of the ORTEPs. For further validation and to illustrate the capabilities of state-of-the-art high-resolution XRD, we also show the ADPs obtained from a charge density study at 100 K (Fig. 2b),[25] although we note that, in the latter work, the hydrogen ADPs had been re-scaled from the initial neutron study. A more detailed comparison (including theoretical results at the same temperature) is reported in the ESI.† The motion of the Cr atom in **2**, as described by DFT-D,

almost perfectly matches both XRD results and it is unclear whether the (slight) deviation between theory and neutron diffraction is a result of the former. No significant problem with the theoretical results is seen in either case.

Computed ADPs, if using the present theoretical machinery, inevitably begin to deviate from the experimental values at higher temperatures as anharmonic vibrational contributions come into play.[12,13] We previously carried out a temperature-dependent study and found that, for practical purposes, anharmonic contributions were not influential up to 100 K;[13] however, to (almost) fully rule them out, it would be interesting to look at a compound that has been studied at *very* low temperatures. Therefore we next turned to **3**, a dinuclear ethylene-bridged complex initially synthesized and routinely characterized by XRD.[28] The authors were aware of the contrast problem in their initial study and their experimental answer was neutron diffraction at 12 K.[17] Intuitively, this should provide us with an almost perfect benchmark because thermal effects are limited at such low temperatures and neutron diffraction can accurately localize the H atoms.

Fig. 3 shows that the motion of all the H atoms in **3** is well reproduced by computation. The same holds true for the carbonyl ligands, although, in this case, the ORTEPs are slightly underestimated by the theoretical method throughout. By contrast, strong deviations are seen for the metal atoms: both are predicted by theory to move significantly too little. The computed (measured) U_{eq} for Os(1) and Os(2) are 29 (47) $\times$ 10^{-4} and 28 (50) $\times$ 10^{-4} Å^2, respectively and so the theoretical method underestimates them by almost 50%. This is readily seen in Fig. 3.

How does this difference arise? A possible reason may be found in the higher mass of Os. The vibrations of the heavy
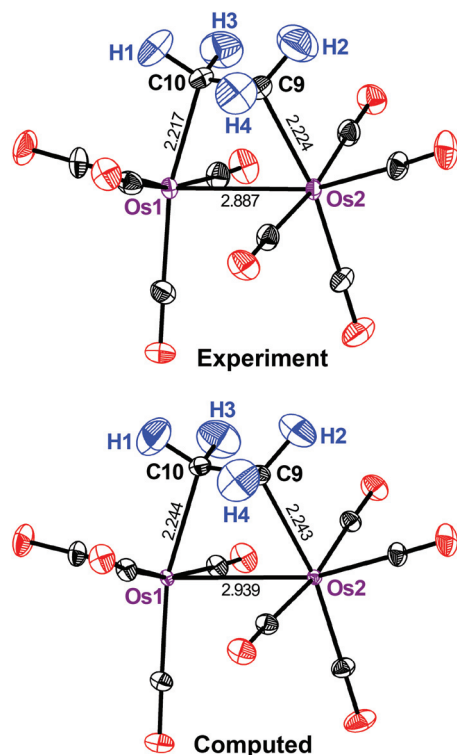
Fig. 3 Displacement ellipsoids (90% probability) as in Fig. 2, but for the ethylene-bridged osmium complex **3** at 12 K (experimental data from ref. 17).

Fig. 4 Experimental *vs.* computed ADPs for crystalline **1** (100 K; circles), **2** (78 K; triangles; experimental data from ref. 16) and **3** (12 K; squares; experimental data from ref. 17), given as main-axis displacement parameters U_1, U_2, U_3 and separately for (a) the metal atoms and (b) the light ligand atoms. For **2**, where both XRD and neutron data are available (see text), we benchmarked the computation against the XRD results for the metal atom and against neutron diffraction for the ligand atoms.

nuclei in **3** are strongly localized at low frequencies (ESI†), much more so than for the Cr compounds discussed earlier. As the expression for the *ab initio* ADPs contains a $1/\omega$ term, uncertainties at low frequencies are the most crucial. A possible solution may be a better description of the electronic structure, especially of the Os dimer species, within the DFT framework used.[29] However, we performed test computations for **3**, including the M06L functional,[30] but found no significant improvement (ESI†). Much validation work, including additional compounds and tailored experiments with improved accuracy, will be required for a definitive answer.

More generally, the theoretical method again emerges as complementary to experiments. In XRD, many-electron scattering centres are reliably localized, with small standard uncertainties for the coordinates and displacement parameters, whereas the light periphery atoms face problems. Theory, by contrast, describes the ligands (including H) with high confidence and could be useful even in those cases where the simulation underestimates the motion of the heavy metal atom(s), as seen in Fig. 3.

Fig. 4 summarizes the results of this study by comparing all the principal elements of the experimental and computed displacement tensors. Ideally, these would all reside on the identity (dashed lines), and the degree of deviation allows us to judge the quality of the DFT-D predictions. Regarding the metal atoms (Fig. 4a), the scatterplot readily exposes the underestimated A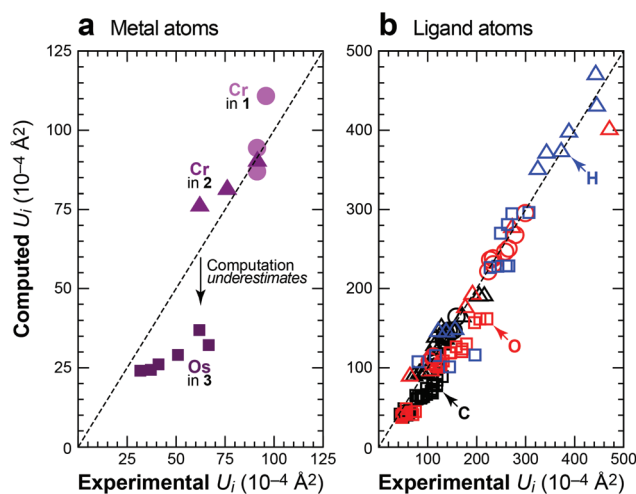DPs in **3**, but this trend is not general, as the metal atoms in **1** and **2** are well described by theory. The motion of the peripheral ligand atoms (Fig. 4b) is likewise reliably reproduced; this holds for the carbon, oxygen and hydrogen atoms alike and no systematic deviation is seen. We reiterate that some degree of scattering in the experimental benchmarks must be taken into account, no matter how well these experiments have been carried out. In this light, in particular, the results shown in Fig. 4 are highly encouraging.

Conclusions

DFT-D computations can be used to predict ADPs for organometallic and coordination compounds, which seems to be particularly useful for cases where routine experiments face (inevitable) difficulties. The method is both practical and economic, and predictive within its limits, which have been explored here for selected organometallic model compounds. Notably, theory might even be closer to reality than an experiment of limited resolution (*cf.* Table 2), as long as the electronic ground state can be correctly described by DFT. A further, much broader study is currently in progress in our laboratories. We note that *ab initio* ADP computations have now been interfaced with the popular SHADE server,[31] which underlines their significant potential for widespread future use.

Methods

High-quality crystals were available for **1**. The key quality indicators for data at full resolution were: $\sin(\theta_{max})/\lambda = 1.152$ Å^{-1};

47 979 reflections; 5016 independent observations; 67 variables; R_1 (all data) = 0.0448; wR_2 = 0.1054; and GOF = 1.055. Key quality indicators for data truncated at $\sin(\theta_{max})/\lambda$ = 0.995 Å^{-1}: 35 569 reflections; 3287 independent observations; 67 variables; R_1 (all data) = 0.0325; wR_2 = 0.0758; and GOF = 1.066. Details about data collection and the completeness and quality of diffraction data are given in the ESI.†

DFT-D computations were carried out using the projector augmented-wave method[32] implemented in VASP,[33] with a plane-wave cut-off of 500 eV. Reciprocal space was sampled on dense Γ-centred Monkhorst–Pack meshes.[34] Strict convergence criteria of $\Delta E < 10^{-8}$ (10^{-6}) eV per cell were applied for electronic (structural) optimization, respectively. Exchange and correlation were treated using the Perdew–Burke–Ernzerhof functional,[35] with dispersion corrections applied using the D3 scheme of Grimme *et al.* and Becke–Johnson damping.[18] This method has been thoroughly validated for molecular crystals[36] and for ADP computations.[13]

Crystal structures were taken from experiments and fully optimized, re-starting from scratch several times to ensure a well-converged minimum. The computed structures were assessed using the root mean square (RMS) displacement of atomic coordinates, which has been introduced to validate experiments,[8] but can also be used to check the quality of computations.[14]

ADPs were obtained from phonon computations[12,37] based on DFT-D and PHONOPY,[38] as detailed in the ESI.† The PHONOPY output was converted into crystallographic U_{ij} values using a custom-written MATLAB code.[13,39]

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