High-mobility two-dimensional electron gas in SrGeO$_3^-$ and BaSnO$_3$-based perovskite oxide heterostructures: an ab initio study†

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We explored the possibility of producing a high-mobility two-dimensional electron gas (2DEG) in the LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ heterostructures using first-principles electronic structure calculations. Our results show that the 2DEG occurs at n-type LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ interfaces. Compared to the prototype LaAlO$_3$/SrTiO$_3$, LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ systems yield comparable total interfacial charge carrier density but much lower electron effective mass (nearly half the value of LaAlO$_3$/SrTiO$_3$), thus resulting in about twice larger electron mobility and enhanced interfacial conductivity. This work demonstrates that SrGeO$_3$ and BaSnO$_3$ can be potential substrate materials to achieve a high-mobility 2DEG in the perovskite-oxide heterostructures.

1 Introduction

The recent development of epitaxial technology has made it possible to achieve high-quality oxide heterostructures (HS) with novel interfacial material properties that are absent in the bulk materials.$^{1-3}$ A prominent example is a LaAlO$_3$/SrTiO$_3$ HS system that consists of two wide band gap insulators LaAlO$_3$ and SrTiO$_3$. This HS system has displayed some unique interfacial properties such as two-dimensional electron gases (2DEGs),$^1$ superconduction,$^2$ and ferromagnetism.$^3$ These interesting interfacial properties have attracted great attention not only because of its fundamental physics but also because of its promising applications in next-generation nanoelectronics.$^{1-3}$

Although the 2DEG at the LaAlO$_3$/SrTiO$_3$ interface shows an extremely high charge carrier density,$^4,5$ its relatively low mobility is still a critical problem and very sensitive to the growth conditions.$^6,7$ To maximize the function of a perovskite-oxide-based 2DEG for high-performance nanoelectronics, it is necessary to further improve its conductivity with higher charge density and electron mobility. To do this, some approaches such as defect engineering,$^6,9$ strain engineering,$^{10-14}$ and doping engineering$^{15-18}$ have been proposed to optimize the interfacial conductive property of perovskite-oxide HS systems. In addition, some experimental efforts have also been made to prepare novel perovskite-oxide-based HS systems such as NdAlO$_3$/SrTiO$_3$$^{19}$ and LaTiO$_3$/SrTiO$_3$$^{20}$ and to explore their interfacial conductive properties. However, all these perovskite-oxide-based HS systems still use SrTiO$_3$ as the substrate, and the interfacial conductivity is caused by the partially occupied Ti 3d orbitals. It is known that the localized Ti 3d orbital has an intrinsic low-dispersion character, which yields a large electron effective mass and relatively low charge carrier mobility. As a result, even though the charge carrier density could be effectively tuned in the SrTiO$_3$-based HS systems via various approaches mentioned above, the charge carrier mobility might not be significantly tuned.

To improve the 2DEG mobility in the perovskite-oxide-based HS systems, one approach is to replace the SrTiO$_3$ with other nonpolar perovskite oxides whose bottom conduction bands are comprised of s or p orbitals. This is because s and p orbitals are less localized than the d orbital, which can potentially lead to larger band dispersion and lower electron effective mass.$^{21}$ In terms of this hypothesis, BaSnO$_3$ and SrGeO$_3$ are two potential substrate materials for growing perovskite-oxide HS systems because of their s/p hybridization characters at the bottom of conduction bands.$^{22,23}$ Interestingly, several recent experimental studies have provided a solid support for this hypothesis.$^{24-28}$ The bulk single crystal of La-doped BaSnO$_3$ has a high room-temperature mobility of 320 cm$^2$ V$^{-1}$ s$^{-1}$, though the epitaxial films have relatively lower values in the range from 10 to 150 cm$^2$ V$^{-1}$ s$^{-1}$ in either doped BaSnO$_3$ films or BaSnO$_3$/LaAlO$_3$ (001) HSs using ex situ X-ray photoelectron spectroscopy (XPS) and spectroscopic ellipsometry (SE).$^{29}$ Correspondingly, a recent computational study revealed that there exists a conduction-band
offset of 1.14 eV at the BaSnO$_3$/SrTiO$_3$ interface. These experimental and computational studies both suggest that BaSnO$_3$ is an appropriate electron acceptor for LaAlO$_3$ and SrTiO$_3$. Nevertheless, the extremely large lattice mismatch between BaSnO$_3$ and LaAlO$_3$ (about 8%) is pernicious to minimize the defects at the interfacial region or to improve the electron mobility. Hence, it is quite necessary to find an alternative perovskite oxide material to match with the BaSnO$_3$ substrate or to find an alternative substrate material with equivalent or higher electron mobility as compared with that of BaSnO$_3$.

In this work, by using first-principles electronic structure calculations, we have modeled LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ HS systems in which SrGeO$_3$ and BaSnO$_3$ are used as substrate materials, and explored the possibility of producing a high-mobility 2DEG in these two HS systems, respectively. Our results show that these two perovskite-oxide HS systems are able to produce the interfacial metallic states due to the polar catastrophe mechanism, and they keep the comparable total charge carrier density with that of the LaAlO$_3$/SrTiO$_3$ system. Moreover, by calculating and analyzing electron effective masses, we show that the electron mobility of these two substrate materials is about two times larger than that of LaAlO$_3$/SrTiO$_3$. These results indicate that, with respect to the model LaAlO$_3$/SrTiO$_3$ system, an enhanced interfacial electron conductivity is expected in the LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ HS systems.

### 2 Computational and structural details

The density functional theory (DFT) calculations were performed using the Vienna Ab initio Simulation Package (VASP). The electron–ion interaction was treated by the projector augmented wave (PAW) potential, and the electron exchange–correlation interaction was described by the generalized-gradient approximation (GGA) parameterized by Perdew–Burke–Ernzerhof (PBE). A cutoff energy of 450 eV for the planewave basis set and a Monkhorst–Pack $k$-point mesh of $4 \times 4 \times 1$ were employed. To simulate the epitaxial film growth process in the experiments, the lattice parameters along the $ab$-plane were fixed while those along the $c$-axis and all the ions’ positions were fully relaxed until the force tolerance on each atom was smaller than 0.03 eV Å$^{-1}$. All the structural relaxations were carried out using the standard DFT calculations within the GGA-PBE framework. To reproduce the accurate experimental band gap of the parent compounds [BaSnO$_3$ and SrGeO$_3$], the Heyd–Scuseria–Ernzerhof (HSE06)$^{18}$ hybrid functional was employed in the single-point total energy calculations. The electronic energy convergence was set to $10^{-4}$ eV, and a Gaussian smearing of 0.08 eV was employed for density of states (DOS) calculations. Although not shown here, the calculated band gaps with varied percent HF exchange contributions show that a 33% HF exchange contribution can yield well the experimental band gaps of 2.7 eV for SrGeO$_3$ and 3.1 eV for BaSnO$_3$, which is exactly the same as the case of SnO$_2$. Thus, the same HF exchange was used for the following heterostructure calculations.

### Table 1

Experimental and calculated structural parameters within the standard DFT–PBE method and band gaps within the DFT–HSE method of cubic LaAlO$_3$, SrGeO$_3$, LaGaO$_3$ and BaSnO$_3$ along with the lattice mismatch ($f$) for the LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ HS models. "I" ("D") in the bracket stands for the indirect (direct) band gap type.

<table>
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<th>Compound</th>
<th>Experiment</th>
<th>DFT</th>
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<td>$a$ (Å)</td>
<td>$f$ (%)</td>
</tr>
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<td>LaAlO$_3$</td>
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<td>0</td>
</tr>
<tr>
<td>SrGeO$_3$</td>
<td>3.798$^{22}$</td>
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</tr>
<tr>
<td>LaGaO$_3$</td>
<td>3.860$^{12}$</td>
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</tr>
<tr>
<td>BaSnO$_3$</td>
<td>4.115$^{23}$</td>
<td>-6.2</td>
</tr>
</tbody>
</table>

A superlattice approach was used to model LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ HS systems that contain symmetrical n-type [LaO]/[SnO$_2$]$^0$ and [LaO]/[GeO$_2$]$^0$ interfaces. To model the HS, 7.5 unit cells of SrGeO$_3$ (LaGaO$_3$) were used as the substrate and 4.5 unit cells of LaAlO$_3$ (LaGaO$_3$) were stacked on the substrate. It is worth mentioning that the superlattice model could exhibit different materials properties from the HS-based slab model in which both the film and the substrate have a surface. The difference is mainly caused by the surface effects in the HS-based slab mode in which the film and the substrate both have a surface. For instance, for the well-known LaAlO$_3$/SrTiO$_3$ system, prior computational studies indicate that only a HS-based slab model can well depict the polarization behavior in the LaAlO$_3$ film though both models can reproduce the interfacial electron reconstruction phenomenon.

At room temperature, BaSnO$_3$ crystallizes in a cubic phase, and LaAlO$_3$ and LaGaO$_3$ crystallize in an orthorhombic phase. For SrGeO$_3$, under appropriate conditions such as high pressure and temperature, it can exhibit a cubic phase. For example, Mizoguchi et al. prepared the cubic SrGeO$_3$ with a typical perovskite structure upon high-pressure treatment at 1100 °C. Herein, by following the widely used approach, we built the HS models (1 × 1 in the $ab$-plane) by treating these non-cubic perovskite oxides as pseudo-cubic structures. In fact, to investigate the possible structural rotation in LaAlO$_3$/SrGeO$_3$, we also carried out test calculations for a larger HS model by using a $\sqrt{2} \times \sqrt{2}$ supercell in the $ab$-plane. Our calculated energy function versus the rotation angle indicates that the structural rotation of the GeO$_2$ cage is not energetically favorable in this model, see the ESL. Table 1 lists the experimental and calculated structural parameters and band gaps of LaAlO$_3$, SrGeO$_3$, LaGaO$_3$, and BaSnO$_3$ in their pseudo-cubic (cubic) phase. The lattice mismatch $f$, defined as $f = (a_l - a_s)/a_s$, for the LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ HS models is also listed. The negative values of $f$ indicate that the film materials experience a tensile strain from the substrate.

### 3 Results and discussion

#### 3.1 Cleavage energy

To evaluate the strength of interfacial cohesion for the LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ HS systems, we calculated their cleavage energies utilizing the following formula:$^{15,45}$
where $E_{HS}$ is the total energy of the HS system, $A$ is the interfacial area and the factor 2 accounts for two symmetrical interfaces. $E_{1\text{slab}}$ and $E_{2\text{slab}}$ are the total energies of the same supercell containing one material with the other one being replaced by a vacuum. As a proof of concept, we took the HS model $(LaAlO_3)_{4.5}/(SrGeO_3)_{7.5}$ as an example to discuss the procedure of cleavage energy calculations. By following the above notation, $E_{HS}$ refers to the total energy of $(LaAlO_3)_{4.5}/(SrGeO_3)_{7.5}$; $E_{1\text{slab}}$ and $E_{2\text{slab}}$ are the total energies of the LaAlO$_3$ and SrGeO$_3$ slabs, respectively. The LaAlO$_3$ slab was modeled by replacing SrGeO$_3$ with a vacuum in $(LaAlO_3)_{4.5}/(SrGeO_3)_{7.5}$, while the SrGeO$_3$ slab was modeled by replacing LaAlO$_3$ with a vacuum in the HS model. As a result, the vacuum in the two slab models are about 29 and 17 Å, respectively, which is sufficient to avoid artificial interactions between adjacent periodic images. Moreover, the HS model and two slab models share the same size of the supercell, which can cancel out the error to a maximum extent.

The cleavage energy is the energy needed to separate the HS system. That is, a larger cleavage energy indicates a stronger cohesion between the two materials at the interface. The calculated cleavage energies within standard DFT calculations are 0.230 eV Å$^{-2}$ for LaAlO$_3$/SrGeO$_3$ and 0.241 eV Å$^{-2}$ for LaGaO$_3$/BaSnO$_3$, respectively, slightly larger than that of the LaAlO$_3$/SrTiO$_3$ HS system (0.19 eV Å$^{-2}$, ref. 45). This indicates that the n-type $(LaO)/(GeO_2)$ and $(LaO)/(SnO_2)$ interfaces are more cohesive than $(LaO)/(TiO_2)$, and thus the LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ interfaces are thermodynamically more favorable than the LaAlO$_3$/SrTiO$_3$ interface.

### 3.2 Density of states

The calculated total DOS plots of LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ are shown in Fig. 1. It shows that the Fermi level is pinned to the bottom of conduction bands, indicating typical n-type conductivity. To understand the origin of the metallic electronic states in these two HS systems, we calculated the layer-resolved partial DOSs for LaGaO$_3$/BaSnO$_3$ and LaAlO$_3$/SrGeO$_3$ models and are shown in Fig. 2 and 3, respectively. For convenience, here we defined three consecutive SnO$_2$ (GeO$_2$) layers, i.e., the 1st, 3rd, and 5th BaSnO$_3$ (SrGeO$_3$) layers as IF-I, IF-III, and IF-V layers, respectively. Our calculations show that the O 2p states in the layers of the substrate materials shift toward high energy with layers moving from the interfacial layer to the deeper layer. The interfacial metallic states are mainly contributed by IF-I, IF-III, and IF-V SnO$_2$ (GeO$_2$) layers, and these metallic states are mostly composed of Sn 5s (Ge 4s) and O 2p orbitals, displaying a large energy dispersion within the band gap. The formation of the interfacial metallic states indicates that there exists a polar-catastrophe-driven charge transfer from LaGaO$_3$ to BaSnO$_3$ for the LaGaO$_3$/BaSnO$_3$ HS system, and from LaAlO$_3$ to SrGeO$_3$ for the LaAlO$_3$/SrGeO$_3$ system, similar to the case of the LaAlO$_3$/SrTiO$_3$ system. Interestingly, the
The largest charge densities for LaGaO$_3$/BaSnO$_3$ (LaAlO$_3$/SrGeO$_3$) HS systems occur in the IF-III SnO$_2$ (GeO$_2$) layer. This is mainly because the SnO$_6$ (GeO$_6$) octahedra in the IF-I layer have a larger structural distortion than that in the IF-III layer. The structural distortion produces a dipole moment towards the deep layers, leading to more charge transfer to the IF-III layer. This fact is different from the case of the LaAlO$_3$/SrTiO$_3$ HS system, in which the 2DEG mainly resides in the IF-I TiO$_2$ layer. In addition, in the LaGaO$_3$/BaSnO$_3$ system (see Fig. 2 and 4b), few electrons released from the interfacial (LaO)$^+$ layer are also transferred to La 5d orbitals in its adjacent (LaO)$^+$ layer, forming partially occupied La 5d states. As discussed below, the partially occupied La 5d states also increase the electron effective mass of the LaGaO$_3$/BaSnO$_3$ system. In contrast, interestingly, the LaAlO$_3$/SrGeO$_3$ system (see Fig. 3 and 4a) does not show a similar phenomenon. This implies that La 5d orbitals have much weaker ability to capture electrons compared to Ge 4s orbitals and Sn 5s orbitals either, but to a lesser extent for the later. Therefore, La 5d orbitals are partially occupied in the LaGaO$_3$/BaSnO$_3$ system.

### 3.3 Band structures and effective masses

Next, we calculated the electronic band structures for the LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ HS systems along the path $M\rightarrow\Gamma\rightarrow X$ of the interfacial Brillouin zone, along with that of the prototype LaAlO$_3$/SrTiO$_3$ HS system for a direct comparison (see Fig. 4c). As shown in the band structures, some electronic states reside below the Fermi level in all the three HS systems, indicating an n-type conductivity in the systems. For the LaAlO$_3$/SrGeO$_3$ HS system (non-spin-polarized calculation), the light band $d_{xy}$ around $\Gamma$ is parabolic and the heavy band extends along the $\Gamma\rightarrow X$ direction. In contrast, in the case of the LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ HS systems (see Fig. 4a and b), the hybridization between Ge 4s (Sn 5s) states and O 2p states leads to more delocalized conduction bands near the Fermi level than that of the LaAlO$_3$/SrTiO$_3$ system, and thus a smaller electron effective mass is expected.

To quantitatively verify this inference, we then calculated the electron effective mass, $m^*/m_e$, for the minimum conduction bands along the $\Gamma\rightarrow X$ and $\Gamma\rightarrow M$ directions, in which $m_e$ is the free electron rest mass. The effective mass $m^*$ was calculated using the parabolic approximation using the formula:

$$\frac{1}{m^*} = \frac{1}{h^2} \frac{\partial^2 E_{CB}}{\partial k^2}$$

where $h$ is the reduced Planck constant, $E_{CB}$ the energy of the minimum conduction band, and $k$ the wave vector corresponding to the conduction bands. The calculated effective masses along the $\Gamma\rightarrow X$ and $\Gamma\rightarrow M$ directions for the three HS systems are listed in Table 2. For the LaAlO$_3$/SrTiO$_3$ HS system, the calculated relative effective mass $m^*/m_e$ is 0.49 along the $\Gamma\rightarrow X$ direction, which is well consistent with previous calculation. For the LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ HS systems, the calculated $m^*/m_e$ along the $\Gamma\rightarrow X$ direction are 0.20 and 0.24, respectively, which are nearly half of the value for the LaAlO$_3$/SrTiO$_3$ HS system. This is because the minimum conduction bands of the LaAlO$_3$/SrGeO$_3$ (LaGaO$_3$/BaSnO$_3$) HS systems are comprised of Ge 4s (Sn 5s) and O 2p orbitals, while those of the LaAlO$_3$/SrTiO$_3$ HS system is comprised of Ti 3d orbitals, and the former are more delocalized than the latter. Since the electron mobility is inversely proportional to the electron effective mass, the LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ HS systems are expected to have a higher 2DEG mobility than the LaAlO$_3$/SrTiO$_3$. It is worth pointing out that the calculated $m^*/m_e$ for the LaAlO$_3$/SrTiO$_3$ and LaGaO$_3$/BaSnO$_3$ HS systems is in good agreement with that of the bulk SrTiO$_3$ (0.46$^{48}$) and BaSnO$_3$ (0.20–0.23$^{49,50}$), indicating that the interfacial 2DEG of the HS oxide systems inherits the bulk materials properties from their parent constituent materials.

### 3.4 Charge carrier density, mobility and conductivity

Besides the charge carrier mobility, the interfacial charge carrier density is also an important factor in determining the interfacial conductivity of the 2DEG. To have a quantitative comparison of the interfacial charge carrier density among the LaAlO$_3$/SrGeO$_3$, LaAlO$_3$/BaSnO$_3$, and LaAlO$_3$/SrTiO$_3$ HS systems, we calculated the total and layer charge carrier densities by integrating their total and layer-resolved partial DOSs for the conducting gap states below the Fermi level, see Fig. 5a. Our calculations show that these three HS systems nearly show a comparable total charge density of about $3.0–3.5 \times 10^{14}$ cm$^{-2}$, which corresponds to a charge transfer of 0.5e$^-$ from the polar LaAlO$_3$ (LaGaO$_3$) to the nonpolar SrTiO$_3$ (SrGeO$_3$ and BaSnO$_3$) substrate. This indicates that the polar catastrophe at the (AO)$^+/$(BO)$_3^-$ interface can drive about 0.5e$^-$ charge transfer, which is independent of the choice of the substrate. It is worth

<table>
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<th>Systems</th>
<th>$\Gamma\rightarrow X$</th>
<th>$\Gamma\rightarrow M$</th>
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<td>LaAlO$_3$/SrTiO$_3$</td>
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</table>
mentioning that the present calculations are based on the superlattice model, which leads to a higher charge carrier density than that of the HS-based slab model.41

To have a direct comparison of the interfacial conductivity among these three HS systems, we calculated the normalized charge carrier mobility ($\mu/\mu_0$) and conductivity ($\sigma/\sigma_0$) with respect to those of the LaAlO$_3$/SrTiO$_3$ system, see Fig. 5b. $\mu_0$ and $\sigma_0$ refer to the charge carrier mobility and conductivity of the LaAlO$_3$/SrTiO$_3$ HS system, respectively. The following two equations were used:43 $\mu = e\langle\tau\rangle/m^*\tau$ and $\sigma = ne\mu$, in which $\tau$, $\tau$, $\mu$, and $\sigma$ are the elementary charge, average scattering time (also called “relaxation time”),54,55 effective mass, charge carrier density, electron mobility, and electrical conductivity, respectively. The scattering time $\tau$ is determined by all the scattering events such as impurity scattering, electron–phonon scattering, and electron–electron scattering, and the inverse of $\tau$ can be expressed as the sum of rates associated with different scattering mechanisms according to Matthiessen’s rule.43 It has been extremely challenging to calculate the scattering time $\tau$ due to the complicated scattering mechanism. One common and simplified approach is to treat $\tau$ as a constant under the constant scattering (relaxation) time approximation,54,55 which has been validated in prior studies.46,56,57 In this work, by assuming that $\langle\tau\rangle$ is a constant, our calculations show that the electron mobility and the electrical conductivity of LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ HS systems are nearly 2.5 and 2.0 times larger than those of the LaAlO$_3$/SrTiO$_3$ HS system, respectively. This indicates that using BaSnO$_3$ and SrGeO$_3$ as the host substrates one can effectively improve the charge carrier mobility and conductivity of the 2DEG.

4 Conclusions

In conclusion, first-principles electronic structure calculations are employed to explore the possibility of producing a high-quality 2DEG in the LaAlO$_3$/SrGeO$_3$ and LaGaO$_3$/BaSnO$_3$ HS systems. Our results reveal that these two HS systems can form interfacial metallic states consisting of less localized Ge 4s and Sn 5s orbitals, respectively, which leads to smaller electron effective mass and higher charge carrier mobility compared to the well-known LaAlO$_3$/SrTiO$_3$ HS model. This work shows a feasible route to enhance the 2DEG mobility and interfacial conductivity using novel substrate materials such as SrGeO$_3$ and BaSnO$_3$.

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