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## 1 Introduction

Water molecules are ubiquitous in nature and play a crucial role in many processes in biology and chemistry. The ability to form a strong three-dimensional hydrogen bond network determines many of water's often unusual properties such as the high melting point and the lower density of the solid ice phase than the liquid one. Numerous crystalline phases of ice are known,<sup>1,2</sup> where the  $I_h$  phase is the dominant natural form on Earth as it is formed at atmospheric pressure, while most other ices are formed at much higher pressure. In general crystalline ices exist in either highly ordered forms, where both the oxygen and hydrogen atoms are ordered in a crystalline way or in hydrogen disordered forms, where the oxygen atoms form an ordered crystal, but the hydrogen bonds form a random disordered network. Ice  $I_h$  belongs to the hydrogen disordered ice crystals (see Fig. 1). The understanding of ices is important for the understanding of the hydrogen bond properties of water in general.<sup>3–11</sup> Still the interpretation of the vibrational spectra of ice  $I_h$  has been subject to a long standing debate.<sup>9,12–23</sup> It has, for example, been suggested that the lowest frequency peak in the Raman spectrum should be assigned to globally in-phase symmetric stretch, while the rest should be interpreted in terms of out-of-phase symmetric and antisymmetric stretches with

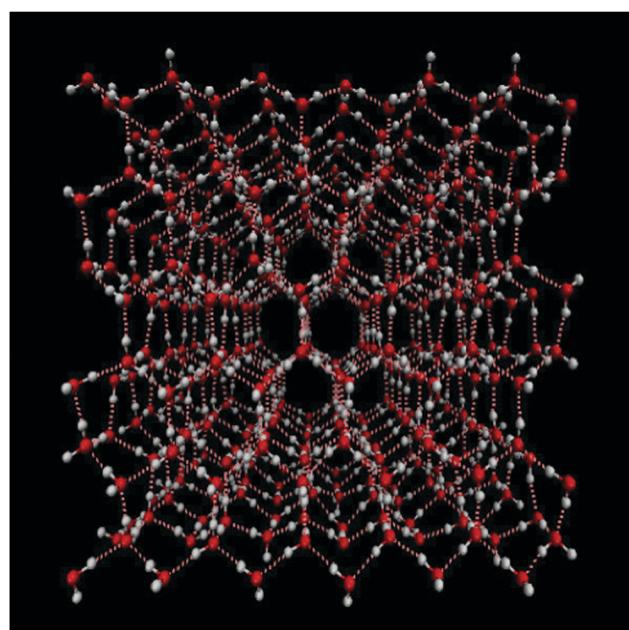


Fig. 1 View of the ice  $I_h$  water structure. Oxygen is represented in red, hydrogen in white and hydrogen bonds are highlighted in pink dashed lines. The plot was generated using VMD.<sup>28</sup>

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longitudinal and transverse optical (LO-TO) phonon splitting.<sup>15</sup> Others have concluded that the spectral features arise from an interplay between intra- and intermolecular coupling, that an interpretation in terms of the molecular symmetric and asymmetric stretch modes is meaningless, and that the LO-TO splitting had negligible effect on the spectral line shape.<sup>24,25</sup>



Recently, two-dimensional infrared spectroscopy (2DIR) was applied to help resolve some of the open questions.<sup>26,27</sup> These experiments provide new insights, but also give rise to new questions. Furthermore, the interpretation is complicated by finite pulse effects and contributions from a thermal signal. In this paper, we have applied a recently developed model for the OH-stretch (OD-stretch) vibrations of H<sub>2</sub>O (D<sub>2</sub>O) with the goal to provide new insights in the nature of the stretch vibrations in ice I<sub>h</sub> and their dynamics.

Two-dimensional infrared spectroscopy<sup>29,30</sup> is a powerful technique for studying vibrational dynamics. In this technique a combination of femtosecond laser pulses are applied to a sample essentially first exciting vibrational states and then after a waiting time probing the effect of the initial excitation. The two-dimensional spectrum consists of two frequency axes, one depicting the frequency of the excitation and another providing the frequency of detection, often denoted  $\omega_1$  and  $\omega_3$ , respectively. The waiting time, which is fixed for each experiment is denoted  $t_2$  and can be varied to study dynamics. This provides a combination of structural and temporal sensitivity. The method has been applied to neat liquid water,<sup>31–37</sup> liquid water under confined conditions,<sup>38–40</sup> water in dilute solutions,<sup>41–43</sup> amorphous ice,<sup>44–46</sup> and the supercooled state.<sup>47</sup> Diagonal peaks arising from exciting one vibration and probing it again at a later time reveal information about spectral diffusion.<sup>48–50</sup> Induced absorption peaks appear to the left of the diagonal ones as the initial excitation enables a subsequent transition of the excited molecules to doubly excited states. These induced absorption peaks are typically at lower frequencies due to the anharmonicity of the vibrations resulting in lower values of  $\omega_3$ . Furthermore, as these peaks originate from induced absorption they have the opposite sign of the diagonal bleach and stimulated emission peaks.<sup>30</sup> Off-diagonal peaks unmask vibrational couplings that may provide structural information<sup>51</sup> as well as information on excitation transfer.<sup>31,52</sup> By varying the polarization of the laser pulses used for excitation and detection additional information on relative orientation of vibrational modes can be extracted,<sup>51</sup> reorientational motion can be studied,<sup>53,54</sup> and excitation transfer changing the transition dipole orientation can be followed.<sup>31–33,55</sup>

The main experimental findings from the 2DIR spectroscopy of H<sub>2</sub>O and D<sub>2</sub>O ice I<sub>h</sub><sup>27</sup> were that the spectra of H<sub>2</sub>O are dominated by the two fundamental transitions, while the D<sub>2</sub>O spectra reveal signals from three of them. The isotropic spectra exhibited clear cross peaks between the fundamental vibrations, while cross peaks were absent in the anisotropic spectra. The cross peaks in the isotropic spectra were taken to solely originate from an isotropic thermal signal. The authors concluded that the observed bands are not related to excitonic splitting.<sup>27</sup> This conclusion contradicts the observation that the excitation is randomized on a very fast timescale. The isotropic signal was found to decay faster for H<sub>2</sub>O than for D<sub>2</sub>O, while the opposite was found for the anisotropic signal decay. In the isotropic signals a component rising on a picosecond timescale related to heating effects was observed very much like in water.<sup>31</sup>

Here we will demonstrate that the isotropic spectra do contain cross peaks of excitonic origin and we will discuss why these cross peaks are essentially absent in the anisotropic signal, which is unusual compared to other systems with vibrational excitons.<sup>42,43,52</sup> The remainder of this paper is organized as follows. In Section 2 the modeling approach is outlined. In Section 3 the results are presented and the conclusions are presented in Section 4.

## 2 Modeling

The two-dimensional infrared spectra were calculated using the vibrational Hamiltonian obtained in ref. 23. In short, MD simulations were performed with the E3B force field for water<sup>7</sup> using an ice I<sub>h</sub> lattice with 432 water molecules at 80 K. The production trajectory was 100 ps long with snapshots stored every 5 fs resulting in a trajectory of 20 000 snapshots. The vibrational Hamiltonian for the OH/OD-stretch vibrations of the form:

$$H(t) = \sum_i \left( \omega_i(t) B_i^\dagger B_i - \frac{\Delta_i(t)}{2} B_i^\dagger B_i^\dagger B_i B_i \right) + \sum_{i,j} J_{ij}(t) (B_i^\dagger B_j + B_j^\dagger B_i) \\ + \sum_i (\vec{\mu}_i(t) \cdot \vec{E}(t) (B_i^\dagger + B_i)) \\ + \sum_i (\vec{\mu}_i^{12}(t) \cdot \vec{E}(t) (B_i^\dagger B_i^\dagger B_i + B_i^\dagger B_i B_i)), \quad (1)$$

was extracted from the MD trajectories using electrostatic mappings.<sup>23,56</sup> The bosonic creation and annihilation operators are denoted  $B_i^\dagger$  and  $B_i$ , respectively. The OH/OD stretch modes are numbered with the indices  $i$  and  $j$ . The fundamental frequency,  $\omega_i(t)$ , and the anharmonicity,  $\Delta_i(t)$ , for each OH/OD stretch are determined using an electrostatic mapping procedure.<sup>23</sup> The coupling  $J_{ij}$  is determined by an intramolecular coupling model when  $i$  and  $j$  belong to the same water molecule, while a transition dipole coupling model is used for intermolecular couplings.<sup>23</sup> The transition dipole for the fundamental excitations,  $\vec{\mu}_i(t)$ , and the correction to the transition dipole for the sequence transition  $\vec{\mu}_i^{12}(t)$ <sup>33</sup> are obtained using electrostatic mappings like for the fundamental frequency and anharmonicity.<sup>56</sup>  $\vec{E}(t)$  is the applied laser field. Previously, the FTIR spectra of neat ice I<sub>h</sub><sup>22</sup> and the two-dimensional infrared spectra for isotope edited ice I<sub>h</sub><sup>23</sup> were simulated with the identical Hamiltonian.

The two-dimensional infrared spectra were simulated for neat H<sub>2</sub>O and D<sub>2</sub>O ice I<sub>h</sub> using the Hamiltonian described above using a computationally efficient version of the NISE approach.<sup>57</sup> In this method time-domain response functions (as given in eqn (11) of ref. 58) are calculated by solving the time-dependent Schrödinger equation using propagation of short (5 fs) intervals during which the Hamiltonian is assumed to be constant.<sup>58–60</sup> The response functions were evaluated for coherence times, usually denoted  $t_1$  and  $t_3$ , from 0 to 750 fs. For the waiting times denoted  $t_2$  the values 0, 150, 200, 300, and 1000 fs were used. The spectra were calculated by adding response functions obtained at 5 ps intervals along the Hamiltonian



trajectory and Fourier transforming the coherence times. For  $\text{H}_2\text{O}$  a lifetime of 300 fs was used while 700 fs was used for  $\text{D}_2\text{O}$ <sup>27</sup> following the procedure of ref. 59, where the lifetimes were estimated from ref. 21 and 61.

### 3 Results and discussion

The linear absorption spectra of  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$  are presented in Fig. 2. The simulated spectra closely resemble those found with identical simulation methods performed at 100 K<sup>22</sup> opposed to the 80 K used here and in the experiments.<sup>27</sup> The  $\text{H}_2\text{O}$  spectrum is dominated by a sharp peak at  $3250 \text{ cm}^{-1}$  and has a shoulder at  $3200 \text{ cm}^{-1}$ , while a weaker tail protrudes on the blue side of the spectrum. In the experimental spectrum the main peak and the shoulder at the red side of the spectrum are both about  $25 \text{ cm}^{-1}$  lower in frequency than in the simulations, while the shoulder on the blue side is considerably more pronounced than in the simulations.<sup>†</sup> The slight underestimation of the solvent shift in the simulations has been discussed previously.<sup>8</sup> For  $\text{D}_2\text{O}$  the spectral features are similar to  $\text{H}_2\text{O}$ , but much more pronounced. In the simulations two clear peaks are observed at  $2425 \text{ cm}^{-1}$  and  $2350 \text{ cm}^{-1}$ , while small shoulders are observed on the blue side of the spectrum. In the experimental spectrum the first two mentioned peaks are observed at  $2420 \text{ cm}^{-1}$  and  $2325 \text{ cm}^{-1}$ , respectively.<sup>27</sup> In addition a clear peak is observed at  $2480 \text{ cm}^{-1}$  close to the shoulders observed in the simulation. Overall, the experimental linear absorption spectra as at 100 K<sup>22</sup> are reproduced well by the theory with the largest discrepancy in the blue wing, where theory gives too low intensity both for  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$ .

In Fig. 3 the experimental<sup>27</sup> and theoretical 2DIR spectra are presented for a number of different waiting times. Both the isotropic ( $S_{ZZZZ} + S_{ZZXX} + S_{ZZYY}$ ) and the anisotropic components ( $S_{ZZZZ} - 0.5(S_{ZZXX} + S_{ZZYY})$ ) are presented. The shape of the isotropic spectra changes very little with time and is dominated by two vertically elongated bleach/stimulated emission peaks. These peaks correspond to the initial excitation in the range of the two main transitions and the subsequent detection of a bleach and stimulated emission from both these transitions. This indicates that excitations in these two regions communicate very rapidly with each other. For detection frequencies below  $3100 \text{ cm}^{-1}$  and above  $3250 \text{ cm}^{-1}$  excited state absorption is observed in the experimental spectra, while this is only detected at low frequencies in the simulation. This supports the conclusion that the high frequency excited state absorption has an origin from heating as the heating processes are not included in the simulations. In the anisotropic spectra a rapid decay of the signal is observed both in experiment and theory. Both lack the strong cross peaks between the two main transitions that are so prominent in the isotropic spectra, and only weak features may be recognised on close inspection. In the

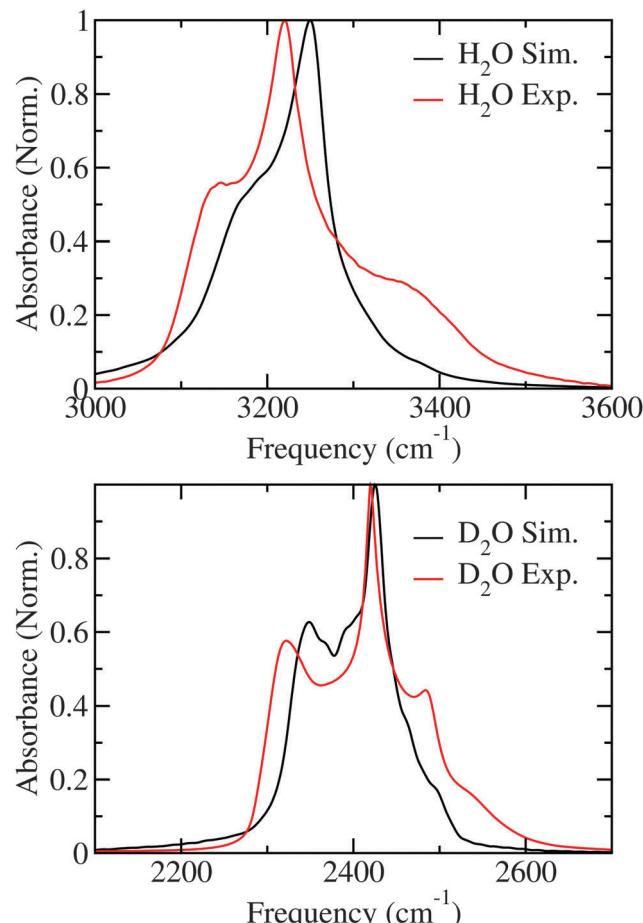


Fig. 2 Simulated and experimental (from ref. 27) linear absorption spectra for  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$  ice.

theoretical spectra the diagonal peak corresponding to the lowest frequency transition is much weaker than in experiment, while the high frequency peak persists longer.

In Fig. 4 the 2DIR spectra are presented for  $\text{D}_2\text{O}$  ice. In the isotropic spectra three vertical bleach/stimulated emission features are observed. At early times a fourth one is observed in the experiment above  $2500 \text{ cm}^{-1}$ . These peaks correspond well with the peaks observed in the linear absorption and as for  $\text{H}_2\text{O}$  clear cross peaks are observed in the isotropic signal. The excited state absorption peak below  $2300 \text{ cm}^{-1}$  is more pronounced than for  $\text{H}_2\text{O}$  water and weak absorption features are observed between the other peaks. As for  $\text{H}_2\text{O}$  the absorption feature growing in at 300 fs in the experiment is not present in the simulation confirming the origin as a heating process. The features in the anisotropic spectra are more complex than for  $\text{H}_2\text{O}$ . The simulated peaks are narrower than the experimental ones. This may be related to the lifetime of 700 fs used here based on previous estimations,<sup>21,61</sup> while recent experimental data suggested a lifetime of the OD-stretch as low as 480 fs.<sup>62</sup> As the lifetime affects the anisotropies very little and the lifetime used in the simulations is mainly included as an apodization function<sup>30,63</sup> to get smooth spectra we chose the lifetime used in the previous simulations of the absorption spectra.<sup>22</sup>

<sup>†</sup> The  $\text{H}_2\text{O}$  FTIR spectrum presented in ref. 27 was obtained under slightly saturated conditions. The spectrum presented here was provided by the authors of ref. 27, does not suffer from this artefact, and agrees well with previous studies as ref. 13 and 14.



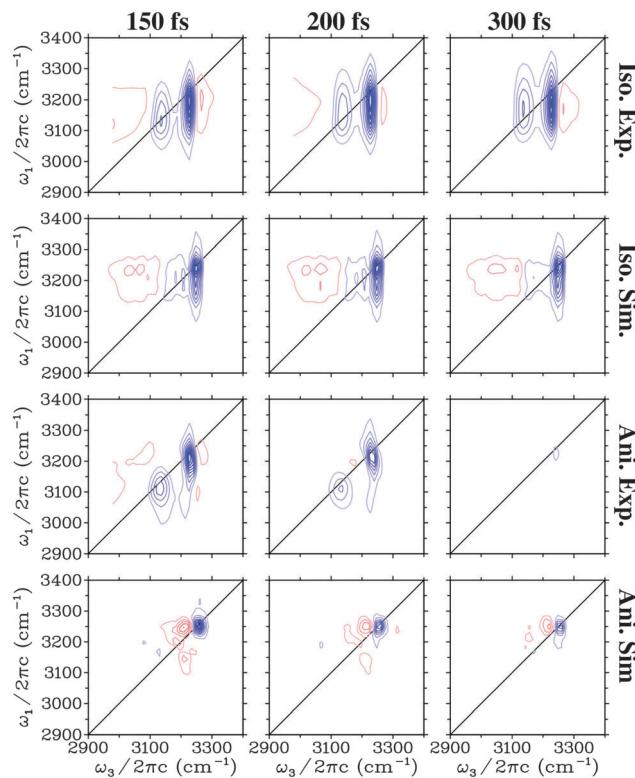


Fig. 3 Simulated and experimental (from ref. 27) two-dimensional spectra for the  $\text{H}_2\text{O}$  ice. Identical equidistant contours are used for all plots. Blue contour lines represent bleach signals, while red contour lines represent induced absorption.

The two dominant bleach/stimulated emission peaks exhibit the same trend in theory and experiment that the high frequency one is narrower in particular along the detection axis than the low frequency peak.

The anisotropy decay was calculated by setting  $t_1 = t_3 = 0$ , effectively providing the anisotropy decay of the integrated spectrum.<sup>33,64</sup> In Fig. 5 this is presented showing that the anisotropy for  $\text{D}_2\text{O}$  decay is slower than for  $\text{H}_2\text{O}$ . The results are very similar to those previously reported for anisotropies for ice  $\text{I}_h$  at higher temperatures.<sup>65,66</sup> However, it is in contrast with the experimental result extracted through an exponential fit at the position of the lower diagonal peak. As the calculations of the spectra are very expensive we only have data for three waiting times and a direct comparison by extracting points from these data would not give enough data for a reasonable comparison. From the experimental analysis exponential decay times of 85 fs and 65 fs were extracted for  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$ , respectively.<sup>27</sup> The experimental data are at least at short times also affected by the finite pulse duration of the laser pulses estimated to be 65 fs,<sup>27</sup> resulting in large error bars on these numbers. The origin of this discrepancy is still unclear, and further experimental and theoretical works are required. While the simulated results are for the integrated total spectrum and the experimentally reported numbers are extracted from the low frequency diagonal peaks, the dependence of the timescale was reported to be rather independent for the location of extraction in the experiment.<sup>27</sup>

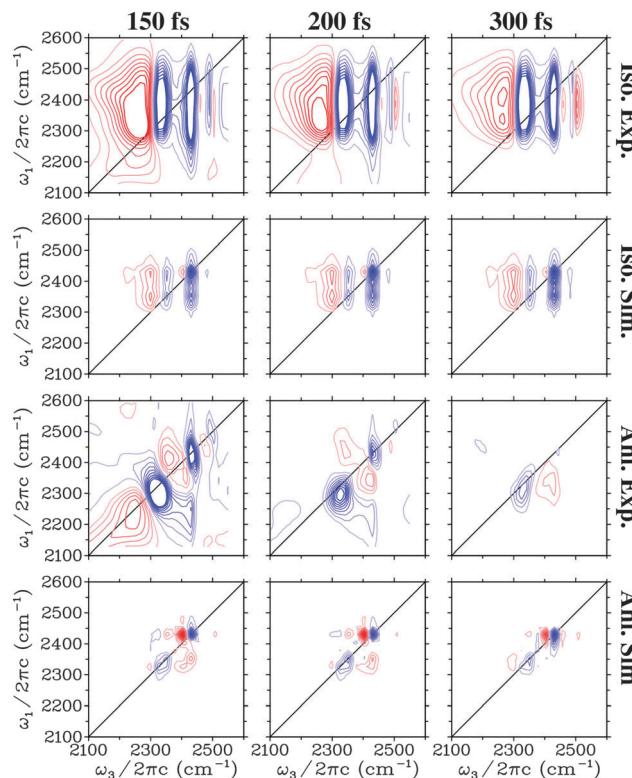


Fig. 4 Simulated and experimental (from ref. 27) two-dimensional spectra for the  $\text{D}_2\text{O}$  ice. Identical equidistant contours are used for all plots. Blue contour lines represent bleach signals, while red contour lines represent induced absorption.

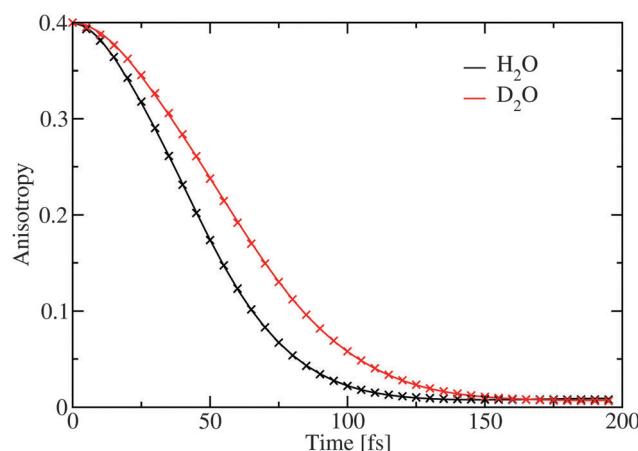


Fig. 5 The simulated anisotropy decay averaged over the complete spectral range. The crosses represent the fit given in Table 1.

The theoretical time dependence of the anisotropy was found to be non-exponential and it was fitted to a sum of gaussian and exponential decays with a very small offset. The choice of this functional form is pragmatic as the initial time-dependence is parabolic, reflecting coherent dynamics.<sup>66</sup> The fit parameters are provided in Table 1. The gaussian component dominates and is the slowest. The decay times are considerably faster than the 1/e time of 114 fs as reported for comparable simulations of water.<sup>33</sup>

**Table 1** Fit parameters for the fit of the averaged anisotropy decay to the function  $r(t) = \frac{2}{5}(A_1 \exp(-t/T_1) + A_2 \exp(-t^2/2T_2^2)) + (1 - A_1 - A_2)$

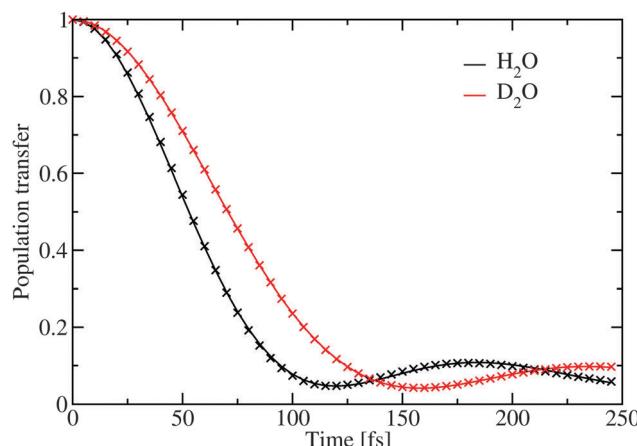
Site	$A_1$	$T_1$ (fs)	$A_2$	$T_2$ (fs)
$\text{H}_2\text{O}$	0.052	25.0	0.929	39.0
$\text{D}_2\text{O}$	0.048	31.3	0.937	50.1

The population transfer was calculated in the site basis by averaging over all sites according to the formula

$$P(t) = \frac{1}{N} \sum_{i=1}^N \left\langle \left| \langle \phi_i | U(t, 0) | \phi_i \rangle \right|^2 \right\rangle, \quad (2)$$

where the index  $i$  labels the local OH-stretch modes,  $\phi_i$  is the wave function where the  $i$ th site is excited,  $U(t, 0)$  is the time-evolution operator obtained according to the NISE approximation,<sup>33</sup> and the outer brackets  $\langle \dots \rangle$  indicate the average over 20 equidistant positions along the simulation trajectory used for ensemble averaging. This quantity essentially tells what the probability is that a site is still excited at the time  $t$  after an initial excitation of the site. The population transfer dynamics is presented in Fig. 6 and the parameters for a fit are presented in Table 2. As for the anisotropy decay the slow initial behaviour is due to coherent vibrational energy transfer as are the recurrences at 175 fs and 225 fs for  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$ , respectively. These coherent effects were previously observed for ice  $\text{I}_h$  at 245 K,<sup>66</sup> where the recurrences are less pronounced. The longer period of the oscillation in  $\text{D}_2\text{O}$  as compared to  $\text{H}_2\text{O}$  reflects the narrower line width in  $\text{D}_2\text{O}$  giving smaller energy gaps between the states involved in the transfer. Due to the coherent nature of the transfer the use of Förster transfer-like models does not apply to vibrational dynamics in ice and ice-like structures.<sup>65–67</sup> Similar observations were previously made in simulations of small ice clusters.<sup>68,69</sup>

The inverse participation ratio<sup>70</sup> was used to estimate the excitation delocalization size. Averaged over the complete OH-stretch band it was found to be 146 and 162 for  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$  respectively. This is in good agreement with previous simulations of ice at 1 K,<sup>21</sup> where a somewhat larger delocalization number of about 250 was reported for  $\text{H}_2\text{O}$ . It should be



**Fig. 6** The simulated population transfer using eqn (2). The crosses represent the fit given in Table 2.

**Table 2** Fit parameters for the fit of the averaged population transfer to the function  $P(t) = B \cos^2(t/\tau_1) \exp(-t^2/\tau_2^2) + (1 - B) \exp(-t/\tau_3)$

Site	$B$	$\tau_1$ (fs)	$\tau_2$ (fs)	$\tau_3$ (fs)
$\text{H}_2\text{O}$	0.946	74.6	123.9	798.9
$\text{D}_2\text{O}$	0.923	99.1	167.8	255.2

noted that the delocalization number is strongly frequency dependent and as previously demonstrated it is significantly lower at the wings of the OH-stretch band and in a region in the middle, where the density of states is lower.<sup>21</sup> In liquid  $\text{H}_2\text{O}$  water the delocalization number is 12.<sup>71</sup> The reported delocalization number is likely to be system size dependent as reported for the 1 K ice.<sup>21</sup> However, it remains interesting that while the delocalization in  $\text{D}_2\text{O}$  is larger than in  $\text{H}_2\text{O}$  the calculated dynamics is slower. One explanation for these differences may be that the intramolecular coupling in  $\text{D}_2\text{O}$  is significantly larger than in  $\text{H}_2\text{O}$ .<sup>22</sup> The extra delocalization in  $\text{D}_2\text{O}$  may, thus, mainly be due to coherent delocalization inside the water molecules, which is not efficient in transferring the excitation through the hydrogen-bond network.

The lack of cross peaks in the anisotropic spectra can be explained by two possible scenarios. First, if the angle between the transition dipoles of the two involved excitation states is always equal to the magic angle ( $\Theta_m = 54.7^\circ$ ) the cross peak should only appear in the isotropic response.<sup>30,51</sup> The second possible explanation is that there is essentially no correlation between the direction of the two involved transition dipoles. In Fig. 7 the transition dipole weighted densities of states are presented. It is clear that one can roughly understand the infrared spectra by considering three regions. At low frequencies there is a shoulder on the IR ( $\mu^2$ ) and 2DIR ( $\mu^4$ ) weighted densities, which gives rise to the lowest frequency peak in the spectra. The main peak is in the middle of the spectra, while at the high frequency range the unweighted density of states is the highest. The high frequency states, however, have very small transition dipoles leading to the very weak spectral shoulder in this region. A more elaborate analysis of the states is previously presented.<sup>21,22</sup> In Fig. 8 the IR weighted density of states is further separated in the components stemming from the components of the transition dipole in different directions of the unit cell. The difference between the different directions is quite small suggesting that there is little or no correlation between the directions of the transition dipoles for the different eigenstates and their location in the band. This unusual property likely stems from the fact that the hydrogen positions are disordered in the  $\text{I}_h$  structure. As the hydrogen positions do not switch during the simulation of the 432 water molecules, the 864 involved hydrogen positions represent a somewhat limited description of the hydrogen disorder in macroscopic ice  $\text{I}_h$ .

To examine the correlation between transition dipole directions the states with the largest transition dipole in the frequency regions corresponding to the low frequency shoulder ( $\omega < 3200 \text{ cm}^{-1}$  for  $\text{H}_2\text{O}$  and  $\omega < 2375 \text{ cm}^{-1}$  for  $\text{D}_2\text{O}$ ), the high frequency shoulder ( $\omega > 3300 \text{ cm}^{-1}$  for  $\text{H}_2\text{O}$  and  $\omega > 2450 \text{ cm}^{-1}$  for  $\text{D}_2\text{O}$ ), and the strong peak in the middle of the frequency range



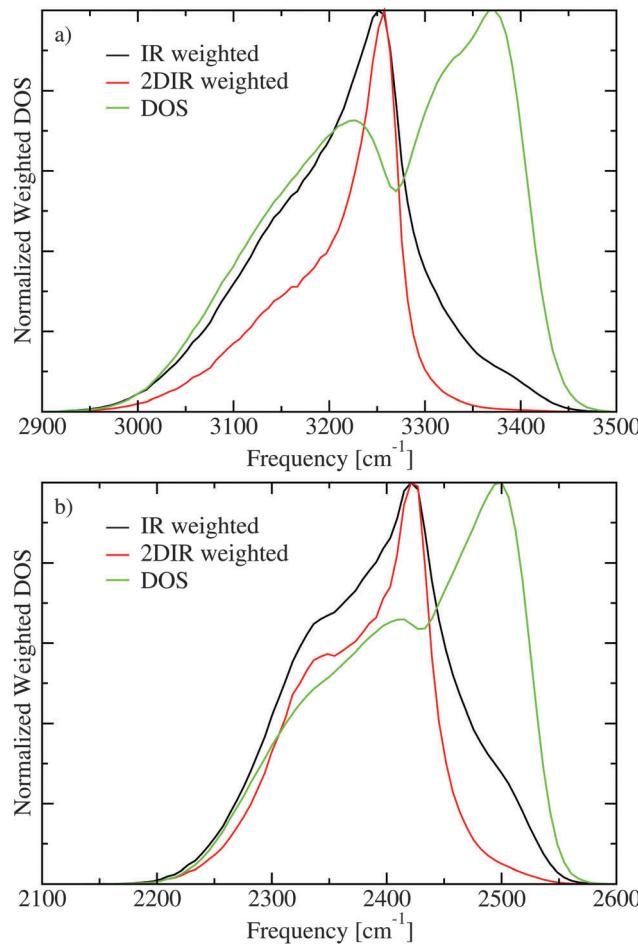


Fig. 7 The densities of states (DOS) without weighting and including weights with the transition dipole squared (IR) and to the fourth power (2DIR) for H<sub>2</sub>O (a) and D<sub>2</sub>O (b).

was identified for each snapshot along the trajectory. The angles between these transition dipoles of three states were determined for every 10th snapshot and histograms of these angles are presented in Fig. 9. The distribution of these angles are quite similar for H<sub>2</sub>O and D<sub>2</sub>O and little variation is seen for different combinations of frequency regions. For a completely isotropic distribution a sine dependence on the angle will be observed. The observed distributions are quite close to the isotropic one revealing the lack of correlation between the transition-dipole directions as the correct explanation for the lack of cross peaks in the anisotropic 2DIR spectrum. However, the cross peaks in the 2DIR spectra likely do not originate from the eigenstates with the largest transition dipoles only and the contribution from multiple other eigenstate combinations are likely contributing to the cross peaks in the anisotropic spectra as well.

The pulse duration in the experiment was 65 fs.<sup>27</sup> Therefore, the experiments are insensitive to dynamics faster than this and one should be cautious drawing too strong conclusions on dynamical times close to the pulse duration. The quantum-classical simulation method does not account for the relaxation of the excitation out of the OH-stretch (OD-stretch) manifold and the heating resulting from this relaxation. Accounting for

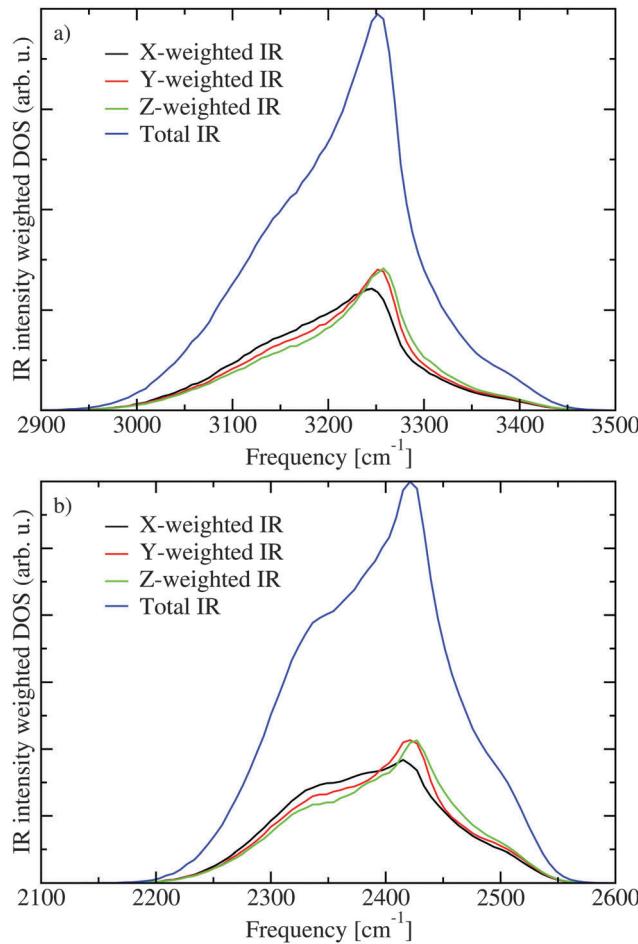


Fig. 8 The contribution to the IR weighted density of states for transition dipole components along the three axes of the unit cell for H<sub>2</sub>O (a) and D<sub>2</sub>O (b).

this relaxation is computationally expensive and was so far only achieved for very small system sizes.<sup>72</sup> Another drawback of the employed method is that correct thermalization within the studied band is not achieved, which may affect the shape of the 2DIR spectra at long waiting times as the band width (including infrared dark states) is larger than  $k_B T$ .<sup>73,74</sup> Considering the significant delocalization number one can further expect that the limited simulation box size may have some effects on the simulated spectra. Finally, we did not include Fermi resonances between the stretch vibrations and the bend overtones, which is stronger in D<sub>2</sub>O than in H<sub>2</sub>O<sup>22</sup> and may affect the spectra.

The reason for the lack of intensity on the high frequency side of the FTIR and 2DIR spectra is not clear and can have several reasons. For D<sub>2</sub>O it was argued that Fermi resonances contribute to the high frequency shoulder.<sup>22,24</sup> However, the spectral region, where the shoulders are located has a high spectral density both for D<sub>2</sub>O and H<sub>2</sub>O (see Fig. 7), which may suggest that the intensity of these states is underestimated by the present model. This could be due to some of the assumptions made in the present study. For example, we assume that the transition dipole is always exactly along the OH bond,<sup>23,56</sup> and we neglect nuclear quantum effects, which should be

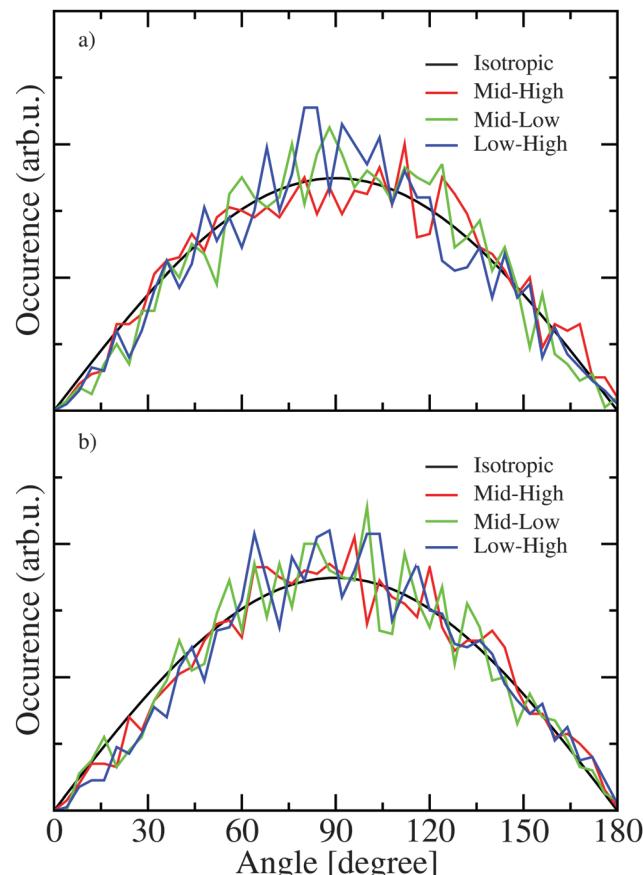


Fig. 9 The distribution of the angles between the strongest transitions from three spectral regions in  $\text{H}_2\text{O}$  (a) and  $\text{D}_2\text{O}$  (b).

important for light nuclei as hydrogen and deuterium.<sup>75</sup> Both for the high frequency librational degrees of freedom as well as the lower frequency translational degrees of freedom the classical approximation is not really well justified considering low temperature of the ice corresponding to about  $56\text{ cm}^{-1}$ , which is lower than the frequencies connected with these modes. We assume the transition-dipole coupling model for the intermolecular couplings, which may introduce discrepancies for hydrogen bonded pairs, where the distance between the oscillators become comparable in size to the vibrating OH bonds, and multipole corrections may be appropriate.<sup>24,76,77</sup> Finally, if real ice is slightly less ordered than predicted by our MD simulations this would likely also result in more intensity in these high frequency modes. Further refinement of the model will, thus, be needed to explain the higher infrared intensity observed experimentally on the blue side of the main peak. Nonetheless, the current model is sufficient to explain the main features of the 2DIR spectra and in particular the polarization dependence in these.

## 4 Conclusions

In this paper, we presented the first quantum-classical simulations of the two-dimensional infrared spectra of  $\text{H}_2\text{O}$  and  $\text{D}_2\text{O}$  ice  $\text{I}_{\text{h}}$ . We found that using the recently developed E3B force

field including three-body interactions, and the spectroscopic mapping approach, the key features of the two-dimensional infrared spectra are reproduced. In particular the presence of cross peaks in the isotropic spectra and their absence in the anisotropic spectra was confirmed in the spectral simulations. In contrast to the original experimental interpretation we conclude that the isotropic signal does contain excitonic cross-peaks on top of possible cross-peaks with a thermal origin. The reason that these peaks are essentially absent in the anisotropic signal is that the angle between dominant exciton states are almost isotropically distributed, which most likely is related to the fact that ice  $\text{I}_{\text{h}}$  is proton disordered. It was confirmed that the exciton dynamics in ice  $\text{I}_{\text{h}}$  is faster than the dynamics observed in liquid water. Furthermore, the simulations suggest that this relaxation is not exponential, reflecting coherent vibrational dynamics.

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