ChemComm



COMMUNICATION

View Article Online



Cite this: Chem. Commun., 2016 **52**. 2023

Received 30th September 2015, Accepted 17th November 2015

DOI: 10.1039/c5cc08182c

www.rsc.org/chemcomm

Tetra-cationic imidazoliumyl-substituted phosphorus-sulfur heterocycles from a cationic organophosphorus sulfide†

Florian D. Henne, Fabian A. Watt, Kai Schwedtmann, Felix Hennersdorf, Malte Kokoschkabc and Jan J. Weigand*a

The reaction of imidazoliumyl-substituted P(III) cations of type $[L^{(R,Me)}PCl_2]^+$ (3a,b+; $L^{R,Me}$ = imidazolium-2-yl a: R = Me; b: R = iPr) with (Me₃Si)₂S leads to the formation of tetra-cationic, eight-membered phosphorus sulfur heterocycles [L^(R,Me)PS]₄⁴⁺ (9a,b⁴⁺), which can be explained by the tetramerization of the intermediately formed cationic phosphorus monosulfide [L^(R,Me)PS]⁺ (8a,b⁺). The P₄S₄ ring adopts a crown conformation as observed for cyclo-S₈. The Lewis base DMAP (4-dimethylaminopyridine) initiates a deoligomerization- and dismutation reaction of 9a,b⁴⁺ to give P^(I) centered cation [L^(R,Me)₂P]⁺ (12a,b+) and phosphorus disulfide [(DMAP)2PS2]+ (14+).

Organophosphorus-sulfur heterocycles with the general constitution $(RPS)_n$ (n = 2-4) and phosphorus in the oxidation state +III remain scarce, since their main access is from the reaction of a dichlorophosphane RPCl₂ (R = Aryl) and a source of sulfide (S^{2-} ; e.g. M_2S (M = Li, Na) or (Me₃Si)₂S). The formation of these compounds can formally be viewed as a combination of divalent RP: and S: units to give monomeric phosphorus mono-sulfides such as 1, which then can either yield oligomerization products (Fig. 1; path I) or ylidylphosphorus sulfide 2a (path II). 2a represents a rare example of a stable and structurally confirmed monomeric ylidylphosphorus monosulfide. Its stability is rationalized by a high contribution of the zwitterionic resonance formula 2b (path II).² Aiming at the synthesis of new cationic phosphorus species, we are investigating reactions of imidazoliumyl-substituted P-centered cations such as [L^(R,R/)PCl₂]⁺ 3⁺ $(L^{R,Me} = imidazolium-2-yl, R = Aryl, Alkyl; R' = H, Me, Cl)^3$ towards substitution^{3,4} (e.g. 4⁺,5⁺), coordination,⁵ oxidation⁶ or reduction⁷

Fig. 1 Formation of oligomeric phosphorus sulfides (RPS)_n (n = 2-4; R = Aryl, R' = Alkyl; path I) and phosphorus monosulfide **2a,b** (path II).

(e.g. $6^+,7^+$) and successfully isolated a series of novel cationic derivatives with intriguing bonding motives (Fig. 2). In this contribution we present the results of the attempted preparation of the imidazoliumyl-substituted $[L^{(R,Me)}PS]^+$ cations 8a,b⁺ (a: R = Me; b: R = iPr) from the reaction of $3a_1b^+$ with $(Me_3Si)_2S$ and the respective oligomerization to tetra-cations 9a,b4+ which can be isolated as triflate salts (Scheme 1). Compounds 3a,b[OTf] (ref. 3) were reacted with 1 eq. (Me₃Si)₂S in fluorobenzene for 5 h at ambient temperature, accompanied by the formation of colorless precipitates. After workup, compounds 9a,b[OTf]4 were isolated in excellent yields (>90%; Scheme 1). The ³¹P{¹H} NMR spectra of the dissolved compounds in d3-MeCN display one major resonance next to a

[†] Electronic supplementary information (ESI) available: For detailed experimental procedures and characterization details of new compounds, NMR spectra, crystallographic details and computational data. CCDC 1424341-1424343 and 1426199. For ESI and crystallographic data in CIF or other electronic format see DOI: 10.1039/c5cc08182c

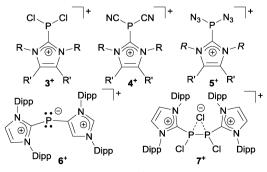


Fig. 2 Selected P-centered cations 3-7⁺ featuring imidazoliumyl-substituents (Dipp = 2,6-diisopropylphenyl)

R-P:∥ + :s path II path I $(RPS)_n (n = 2 - 4)$

^a Department of Chemistry and Food Chemistry, Technische Universität Dresden, 01062 Dresden, Germany. E-mail: jan.weigand@tu-dresden.de

^b Department of Computational Chemistry, Academy of Sciences of the Czech Republic, 16610 Praha 6. Czech Republic

^c Department of Physical Chemistry, Palacky University, 771 46 Olomouc,

Communication ChemComm

$$\begin{array}{c} \bigoplus \\ \mathsf{L}(\mathsf{R}/\mathsf{Me}) \\ \mathsf{P}-\mathsf{Cl} \\ \\ \mathsf{OI} \\ \mathbf{3a,b}[\mathsf{OTf}] \\ \mathbf{3a,b}[\mathsf{OTf}] \\ \oplus \\ \mathsf{L}(\mathsf{R}/\mathsf{Me}) \\ \mathsf{P}-\mathsf{S} \\ \\ \mathsf{I}(\mathsf{R}/\mathsf{Me}) \\ \mathsf{IOTf}]_4 \\ \oplus \\ \mathsf{P}-\mathsf{S} \\ \mathsf{I}_{\mathsf{L}(\mathsf{R}/\mathsf{Me})} \\ \mathsf{IOTf}]_4 \\ \mathsf{S}-\mathsf{P} \\ \mathsf{S}-\mathsf{P} \\ \mathsf{I}_{\mathsf{L}(\mathsf{R}/\mathsf{Me})} \\ \mathsf{P}-\mathsf{S} \\ \mathsf{I}_{\mathsf{L}(\mathsf{R}/\mathsf{Me})} \\ \mathsf{P}-\mathsf{S} \\ \mathsf{I}_{\mathsf{L}(\mathsf{R}/\mathsf{Me})} \\ \mathsf{P}-\mathsf{S} \\ \mathsf{I}_{\mathsf{L}(\mathsf{R}/\mathsf{Me})} \\ \mathsf{P}-\mathsf{S} \\ \mathsf{R} \\ \mathsf{R}$$

 $\begin{array}{lll} \textbf{Scheme 1} & \text{Preparation of tetrameric imidazoliumyl-substituted phosphorus-sulfur heterocycles} & \textbf{9a,b}[\text{OTf}]_4 & \text{from the intermediately formed cation} & \textbf{8a,b}^+ \text{ (a: } R = \text{Me; b: } R = \text{iPr); (i)} + (\text{Me}_3\text{Si})_2\text{S, } C_6\text{H}_5\text{F, rt, } -2\text{Me}_3\text{SiCl.} \\ \end{array}$

minor singlet in the typical region of tri-coordinate phosphorus derivatives ($9a^{4+}$: $\delta(P)_{major/minor} = 48.2$ ppm/48.0 ppm; $9b^{4+}$: $\delta(P)_{major/minor} = 50.5$ ppm/50.3) indicating the oligomerization of the intermediately formed cationic phosphorus monosulfide $8a,b^+$. However, no evidence for the formation of other ring sizes was found, showing a high selectivity of the oligomerization process. It can be assumed that, under these conditions, the formation of the P_4S_4 ring is thermodynamically (considering ring strain and steric effects) favored. The variable-temperature (VT) ^{31}P NMR spectra for $9b[OTf]_4$ are depicted in Fig. 3a, evidencing a dynamic behavior and the presence of two highly symmetric conformational isomers (crown (C_{4v}) vs. boat-chair (C_s) conformer) of the P_4S_4 ring in solution (Scheme 2). A significant broadening of the two resonances upon

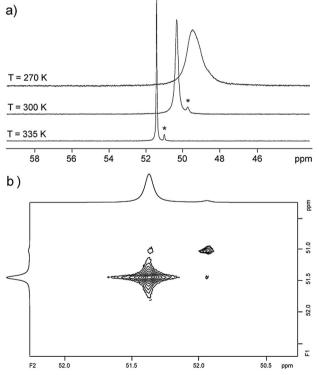


Fig. 3 (a) VT 31 P NMR spectra of **9b**[OTf]₄ recorded in CD₃CN (see ESI†) * indicates minor amounts of the conformational isomer of **9b***; (b) 31 P EXSY NMR spectrum of **9b**[OTf]₄ recorded at 335 K with a mixing time of $t_m = 0.55$ s.

Scheme 2 Interconversion process of cations $9a,b^{4+}$ from the conformational isomer with crown shape (C_{4v}) to the boat-chair (C_s) conformer without considering the imidazoliumyl substituents.

cooling is observed. The VT 1 H NMR spectra also show additional dynamic behavior of the iPr-groups. We thus confirmed the existence of two conformational isomers independently by 31 P EXSY NMR experiments (Fig. 3b), although quantitative accuracy (to determine kinetic processes or exchange rates) was limited by the narrow temperature range in which useful spectra could be measured. The 31 P EXSY NMR experiments suggest exchange of two conformers in which one of the sulfur-bridges reversibly changes its relative position, giving either the approximate C_{4v} or C_s symmetric cations $\mathbf{9a,b}^{4+}$ (Scheme 2). The cross peaks in the 2D spectrum demonstrate the exchange between the two symmetric conformers in solution, consistent with the observation of singlet resonances as expected for an A_4 spin-system for both isomers.

Satisfactory crystal structure analyses could be performed confirming the formation of the suggested eight-membered organophosphorus-sulfur heterocycles (Fig. 4). In the case of compound 9b[OTf]₄ the refinement of the X-ray data confirmed the crown-shaped P₄S₄ moiety, similarly to cation 9a⁴⁺, however, due to severe disorder caused by alternating ring orientation full refinement was only possible after treatment by an appropriate disordered model.8 The PIII-S bond lengths (av. 2.129 Å) in 9a4+ are in the typical range for PIII-S single bonds and compare well with those reported by Sheldrick et al. for the neutral derivative (MesPS)4 (av. 2.117 Å; Mes = 2,4,6-trimethylphenyl). The pyramidalization of the P atoms, as well as the lengths of the C-P bonds (av. 1.817 Å), together with the internal angle N1-C1-N2 of the imidazoliumyl moieties $(9a^{4+}$: av. 106.9° vs. $\sim 101^{\circ}$ in NHCs)⁹ are in agreement with the ability of the imidazoliumyl fragment to (a) delocalize the positive charge, (b) reduce the nucleophilicity of a directly bonded P atom and thus may account for the stability of these cations. 5,10,11

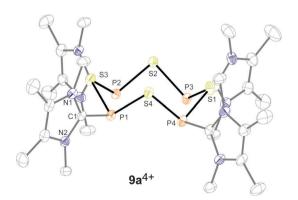


Fig. 4 Molecular structure of tetracation $9a^{4+}$ in $9a[OTf]_4$. All hydrogen atoms and triflate anions are omitted for clarity. Selected bond lengths in Å and angles in $^{\circ}$: P1–S1 2.1306(9), P1–S4 2.1364(9), P2–S1 2.1234(9), P1–C1 1.820(3), S1–P1–S4 101.99(4), S1–P1–C1 99.31(8), S4–P1–C1 101.26(9), N1–C1–N2 101.26(9).

ChemComm Communication

Scheme 3 Deoligomerization of 9b[OTf]₄ with DMAP and proposed intermediates; (i) +4 DMAP, MeCN, rt.

To confirm that the formation of tetracations 9a,b⁴⁺ proceeds *via* monomeric phosphorus mono-sulfides 8a,b⁺, we reacted 9a,b[OTf]₄ with DMAP in MeCN, since this Lewis base has been widely used to stabilize low-coordinate phosphorus species. ¹² The σ -donor strength of DMAP should be high enough to deoligomerize tetracations 9a,b4+ to cations 10a,b⁺ which represent DMAP adducts of the elusive cations 8a,b⁺ (Scheme 3). The reaction of 4 equivalents DMAP in MeCN proceeds comparably clean with 9b[OTf]4 at ambient temperature giving pale-yellow solutions. The ³¹P{¹H} NMR spectra of the reaction mixture of 9b[OTf]₄ and DMAP after reaction times of 10 min to 7d are depicted in Fig. 5. After 10 min a broad resonance at $\delta(P) = 147.1$ ppm is observed which splits into 2 singlets at low temperature ($\delta(P)$ = 140.3 ppm and $\delta(P)$ = 144.4 ppm; 253 K). We believe that the splitting of the resonances results from two rotational isomers caused by a restricted rotation of the iPr groups at low temperature.^{8,13} From the distinctive chemical shift a dimeric derivative with tetra-coordinate phosphorus atoms

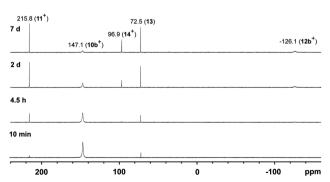


Fig. 5 ³¹P{¹H} NMR spectra of the 1:4 reaction of **9b**[OTf]₄ and DMAP in CD₃CN showing the scrambling reaction to cations 11⁺, 12b⁺, 14⁺ and adduct 13

(cf. $[(Et_2N)_2PS_2][AlCl_4]_2$: $\delta(P) = 21.0 \text{ ppm})^{14}$ can be excluded and we thus propose the formation of DMAP adduct 10b+ which is also supported by our NMR investigation.8 We were not able to isolate 10b[OTf], however, we assume that cation 10b⁺ readily dismutates to cations **11**⁺ (δ (P) = 215.8 ppm) and **12b**⁺ (δ (P) = -126.1 ppm) *via* an intermolecular scrambling reaction, i.e. an intermolecular exchange of imidazolium-2-yl and sulfur substituents. Related exchange reactions were discussed for the DMAP induced disproportionation of POCl₃¹⁵ and scrambling reactions of imidazoliumylsubstituted $[L^{(Me,Me)}PCl_2]^+$ cations. PI centered cation $13b^+$ $(\delta(P) = -126.1 \text{ ppm})$ was recently reported by Macdonald et al. and unambiguously confirmed by its characteristic chemical shift (cf. lit: $\delta(P) = -124.2$ ppm, CD_2Cl_2). Cations of type $12a^+$ are also known and reported by Schmidpeter et al. as ylidylphosphorusdisulfide containing a tri-coordinate R-PS₂ moiety. For these types of compounds the chemical shift strongly depends on the nature of the supporting substituent R and is typically observed in the range of $\delta(P) = 170-240 \text{ ppm}$ (cf. Ph₃PCMe-PS₂: $\delta(P)_{PS_2} = 243.4 \text{ ppm}$, d₈-THF).² In an equilibrium reaction of cation 11⁺ with the triflate anion the formation of 13 is explained and supported by the pronounced upfield shifted triplet resonance due to the coupling to the *ortho*-protons of the DMAP ligand (eqn (1); $\delta(P) = 72.5$ ppm, triplet, ${}^{3}J_{PH}$ = 9.0 Hz; cf. PyPS₂Br: $\delta(P)$ = 65.5 ppm, Py = pyridine; d₃-MeCN). The formation of cation 14⁺ results either from the equilibrium reaction of 11+ (eqn (2)) or 13 (eqn (3)) with DMAP which is liberated during the dismutation of cation **10b**⁺ (Scheme 3). The ³¹P NMR spectrum displays a quintet resonance which is indicative for the presence of two DMAP substituents consistent with the C_{2v} symmetry of cation 14⁺ ($\delta(P) = 96.9$ ppm; cf. $[Py_2PS_2]^+$: $\delta(P) = 104.7$ ppm, quintet, ${}^{3}J_{PH} = 9.6$ Hz; Py = pyridine; d₃-MeCN). Similar equilibria and cations have been observed by Meisel et al. who reported on the pyridine (Py) stabilized phosphorus disulfide [Py₂PS₂]⁺ cation. Two crystalline polymorphs of 14[OTf] were obtained after layering the reaction mixtures with Et₂O (Fig. 6). 19 The obtained structural parameters compare well with those reported for the related pyridine cation [Py2PS2]+ by Meisel et al. 18

$$11[OTf] \rightleftharpoons 13$$
 (1

$$11[OTf] + DMAP \Rightarrow 14[OTf] \tag{2}$$

$$13 + DMAP \rightleftharpoons 14[OTf] \tag{3}$$

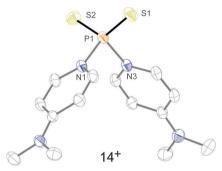


Fig. 6 Molecular structure of 14⁺ in 14[OTf]. All hydrogen atoms and the triflate anion are omitted for clarity. Selected bond lengths in Å and angles in °: P1-S1 1.9309(8), P1-S2 1.9321(8), P1-N1 1.782(2), P1-N2 1.798(2), S1-P1-S2 124.09(4), N1-P1-N2 96.77(8), S-P1-N av. 108.14.

Communication ChemComm

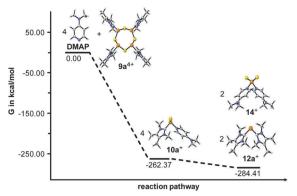


Fig. 7 Gibbs free energy in kcal mol⁻¹ of the observed and proposed phosphorus species.

In order to confirm our findings and support the suggested dismutation, quantum chemical calculations have been performed from the reaction of 9a4+ with 4 eq. DMAP to derive geometry and Gibbs free energy of the involved species as well as the suggested reaction intermediate 10a⁺. ²⁰ The density functional theory (DFT) hybrid model B3LYP21 was used in combination with Grimme's atom-pairwise dispersion correction (D3). 22 Fig. 7 illustrates the Gibbs free energy ΔG of educts (9a⁴⁺, DMAP), products (12b⁺, 14⁺) and the proposed intermediate (10a⁺) calculated at the B3LYP-D3/def-SVP level of theory. The whole reaction pathway is thermodynamically favored ($\Delta G = -284.4 \text{ kcal mol}^{-1}$). The proposed reaction intermediate 10a⁺ is energetically less favorable by 22 kcal mol⁻¹ compared to the final products, but 262 kcal mol⁻¹ lower in energy than the educt molecules ($\Delta G = -262.4 \text{ kcal mol}^{-1}$). This observation is perfectly in line with the assumption of **10a**⁺ being the main reaction intermediate.

In summary, we reported on the oligomerization reaction of cationic phosphorus monosulfides $\mathbf{8a,b}^+$ which were formed in situ from the reaction of $[\mathbf{L}^{(R,Me)}\mathbf{PCl_2}]^+$ cations $\mathbf{3a,b}^+$ ($\mathbf{L}^{R,Me}$ = imidazolium-2-yl a: $\mathbf{R} = \mathbf{Me}$; b: $\mathbf{R} = \mathbf{iPr}$) and ($\mathbf{Me_3Si)_2S}$. The obtained tetra-cationic, eight-membered phosphorus-sulfur heterocycles $[\mathbf{L}^{(R,Me)}\mathbf{PS}]_4^{4+}\mathbf{9a,b}^{4+}$ primarily exist as crown conformers similar to cyclo- $\mathbf{S_8}$, however, the boat-chair ($C_{\mathbf{s}}$) conformers of the $\mathbf{P_4S_4}$ rings also exist in solution according to 2D-EXSY $^{31}\mathbf{P}$ NMR experiments. Cations $\mathbf{9a,b}^{4+}$ can be deoligomerized by DMAP to yield adducts $\mathbf{10a,b}^+$ of the elusive cations $\mathbf{8a,b}^+$. Subsequent dismutation of $\mathbf{10a,b}^+$ gives cations $[\mathbf{L}^{(R,Me)}_{2}\mathbf{P}]^+$ ($\mathbf{12a,b}^+$) and $[(\mathbf{DMAP})_2\mathbf{PS_2}]^+$ ($\mathbf{14}^+$) as final products. The suggested reaction pathway was supported by DFT calculations.

This work was supported by the Fonds der Chemischen Industrie (FCI, Kekulé scholarship for F. H.), the German Science Foundation (DFG, WE 4621/2-1) and the ERC (SynPhos 307616). Financial support of M. K. by a POSTUP² grant (European social fund in the Czech Republic, European Union, Czech ministry of education and sports, operational program for the advancement of the competitive capacity) is gratefully acknowledged (CZ.1.07/2.3.00/30.0041). We thank the Center

for Information Services and High Performance Computing (ZIH) for the generous allocation of computation time.

References

- 1 (a) T. Chivers and I. Manners, *Inorganic Rings and Polymers of the p-Block Elements*, RSC Publishing, 2009; (b) C. Lensch and G. M. Sheldrick, *J. Chem. Soc., Dalton Trans.*, 1984, 2855–2857; (c) B. Cetinkaya, P. B. Hitchcock, M. F. Lappert, A. J. Thorne and H. Goldwhite, *J. Chem. Soc., Chem. Commun.*, 1982, 691–693; (d) M. Baudler, D. Koch, T. Vakratsas, E. Tolls and K. Kipker, *Z. Anorg. Allg. Chem.*, 1975, 413, 239–251.
- 2 G. Jochem, K. Karaghiosoff, S. Plank, S. Dick and A. Schmidpeter, Chem. Ber., 1995, 128, 1207–1219.
- 3 J. J. Weigand, K.-O. Feldmann and F. D. Henne, J. Am. Chem. Soc., 2010, 132, 16321–16323.
- 4 F. D. Henne, A. T. Dickschat, F. Hennersdorf, K. O. Feldmann and J. J. Weigand, *Inorg. Chem.*, 2015, 54, 6849–6861.
- 5 K. Schwedtmann, M. H. Holthausen, K.-O. Feldmann and J. J. Weigand, *Angew. Chem., Int. Ed.*, 2013, 52, 14204–14208.
- 6 K. Schwedtmann, S. Schulz, F. Hennersdorf, T. Strassner, E. Dmitrieva and J. J. Weigand, *Angew. Chem., Int. Ed.*, 2015, 54, 11054–11058.
- 7 F. D. Henne, E.-M. Schnöckelborg, K.-O. Feldmann, J. Grunenberg, R. Wolf and J. J. Weigand, *Organometallics*, 2013, **32**, 6674–6680.
- 8 See ESI†.
- 9 F. E. Hahn and M. C. Jahnke, Angew. Chem., Int. Ed., 2008, 47, 3122-3172.
- 10 M. H. Holthausen, S. K. Surmiak, P. Jerabek, G. Frenking and J. J. Weigand, Angew. Chem., Int. Ed., 2013, 52, 11078-11082.
- D. J. D. Wilson, S. A. Couchman and J. L. Dutton, *Inorg. Chem.*, 2012, 51, 7657–7668.
- 12 (a) R. J. Davidson, J. J. Weigand, N. Burford, T. S. Cameron, A. Decken and U. Werner-Zwanziger, Chem. Commun., 2007, 4671–4673;
 (b) J. J. Weigand, N. Burford, A. Decken and A. Schulz, Eur. J. Inorg. Chem., 2007, 4868–4872;
 (c) M. Blättner, M. Nieger, A. Ruban, W. W. Schoeller and E. Niecke, Angew. Chem., Int. Ed., 2000, 39, 2768–2771;
 (d) E. Rivard, K. Huynh, A. J. Lough and I. Manners, J. Am. Chem. Soc., 2004, 126, 2286–2287;
 (e) N. Burford, H. A. Spinney, M. J. Ferguson and R. McDonald, Chem. Commun., 2004, 2696–2697;
 (f) J. J. Weigand, N. Burford, D. Mahnke and A. Decken, Inorg. Chem., 2007, 46, 7689–7691.
- 13 H. Kessler, Angew. Chem., Int. Ed. Engl., 1970, 9, 219-235.
- 14 N. Burford, R. E. v. H. Spence and R. D. Rogers, J. Chem. Soc., Dalton Trans., 1990, 3611–3619.
- 15 P. Rovnaník, L. Kapička, J. Taraba and M. Černík, *Inorg. Chem.*, 2004. 43, 2435–2442.
- 16 B. D. Ellis, C. A. Dyker, A. Decken and C. L. B. Macdonald, *Chem. Commun.*, 2005, 1965–1967.
- 17 The low symmetry of 13 and the presence of the triflate anion encourage an effective quadrupole relaxation and prevents the observation of the ¹*J*(³¹P, ¹⁴N) coupling. The same accounts for the more symmetric cation 14⁺.
- 18 M. Meisel, P. Lönnecke, A.-R. Grimmer and D. Wulff-Molder, *Angew. Chem., Int. Ed.*, 1997, 36, 1869–1870.
- 19 Similarly to the highly reactive intermediate ${\bf 10b}^{\dagger}$, the tetramethyl substituted derivative ${\bf 10a}^{\dagger}$ was also observed in the reaction of ${\bf 9a[OTf]^4}$ and 4 eq. DMAP at $\delta(P)=144.7$ ppm. From the reaction spectra, chemical shifts as $\delta(P)=216.6$ ppm, 97.3 ppm, 70.9 ppm and -113.2 ppm can be assigned to ${\bf 11}^{\dagger}$, ${\bf 14}^{\dagger}$, ${\bf 13}$ and ${\bf 12a}^{\dagger}$, respectively. The reaction NMR is depicted in the supporting information; Details of the two polymorphs are given in the ESI † .
- 20 Cation 9a⁴⁺ was choosen as model system.
- 21 (a) A. D. Becke, J. Chem. Phys., 1993, 98, 5648–5652; (b) C. Lee, W. Yang and R. G. Parr, Phys. Rev. B: Condens. Matter Mater. Phys., 1988, 37, 785–789; (c) P. J. Stephens, E. J. Devlin, C. F. Chabalowski and M. J. Frisch, J. Phys. Chem., 1994, 98, 11623–11627; (d) S. H. Vosko, L. Wilk and M. Nusair, Can. J. Phys., 1980, 58, 1200–1211.
- 22 (a) T. Schwabe and S. Grimme, Phys. Chem. Chem. Phys., 2006, 8, 4398-4401; (b) S. Grimme, J. Antony, S. Ehrlich and H. Krieg, J. Chem. Phys., 2010, 132, 154104.