Thin film depth profiling by ion beam analysis

Chris Jeynes* and Julien L. Colaux†

The analysis of thin films is of central importance for functional materials, including the very large and active field of nanomaterials. Quantitative elemental depth profiling is basic to analysis, and many techniques exist, but all have limitations and quantitation is always an issue. We here review recent significant advances in ion beam analysis (IBA) which now merit it a standard place in the analyst’s toolbox. Rutherford backscattering spectrometry (RBS) has been in use for half a century to obtain elemental depth profiles non-destructively from the first fraction of a micron from the surface of materials: more generally, “IBA” refers to the cluster of methods including elastic scattering (RBS; elastic recoil detection, ERD, and non-Rutherford elastic backscattering, EBS), nuclear reaction analysis (NRA: including particle-induced gamma-ray emission, PIGE), and also particle-induced X-ray emission (PIXE). We have at last demonstrated what was long promised, that RBS can be used as a primary reference technique for the best traceable accuracy available for non-destructive model-free methods in thin films. Also, it has become clear over the last decade that we can effectively combine synergistically the quite different information available from the atomic (PIXE) and nuclear (RBS, EBS, ERD, NRA) methods. Although it is well known that RBS has severe limitations that curtail its usefulness for elemental depth profiling, these limitations are largely overcome when we make proper synergistic use of IBA methods. In this Tutorial Review we aim to briefly explain to analysts what IBA is and why it is now a general quantitative method of great power. Analysts have got used to the availability of the large synchrotron facilities for certain sorts of difficult problems, but there are many much more easily accessible mid-range IBA facilities also able to address (and often more quantitatively) a wide range of otherwise almost intractable thin film questions.

1 Historical introduction to IBA

What is Ion Beam Analysis (IBA)? We will answer this question implicitly by an historical survey, which will also shed light on the synergies that are central to our subject: modern IBA depth profiling of thin films. IBA has been used by analytical chemists for over half a century, ever since Rubin et al. published their landmark paper in 1957.1 Although in the 1990s IBA methods were rather overtaken by rapid developments in other techniques, in the last decade or so some dramatic developments in IBA have made it significantly more powerful, and it is these we aim to describe and explain here.

These developments gathered pace around the turn of the 21st century. Fig. 1 shows a profile through the depth of an antireflection coating which an optics company wished to reverse-engineer. It is an iconic image of far-reaching significance to which we will return repeatedly in this Review, here pointing out merely that the coating is complex and yields an intricate spectrum which we can nevertheless fit very precisely, meaning that very detailed information can be extracted from this single spectrum, non-destructively and with essentially no prior knowledge (it is a “model-free” analysis, although see discussion in §§3.9, 4.2).

Throughout this Review we will emphasise the importance of the proper use of complementary techniques. This importance is nothing new, but in today’s increasingly multidisciplinary science we are finding that even in routine work, for which twenty years ago we might have been satisfied with a single analytical method, we now use multiple complementary methods. It is informative to trace the history of IBA with this in mind, since the various atomic and nuclear excitations that underlie most of the complementary analytical techniques of relevance to thin film analysis (including IBA) were all discovered together at the birth of the new physics.

And central to this Review is the recognition that “IBA” is itself a cluster of complementary techniques that historically were handled separately but which we have recently learned to handle self-consistently in a synergistic way. To refer to this self-consistent use of multiple IBA methods we will use...
“Total-IBA”, a term proposed by Jeynes et al. in 2012, who also provide an annotated Glossary of the “acronym soup” for all the complementary techniques. In this Review we will highlight acronyms as they occur, for ease of reference, expanding them repeatedly as necessary for clarity.

High energy nuclear backscattering was first proposed by Ernest Rutherford in 1911 to account for the scattering of alpha particles by gold atoms. Also in 1911, Charles Barkla recognised that the mysterious effect generated by γ-rays striking matter, which he named “X-ray fluorescence” (XRF), was similar to the atomic emission already familiar to the spectroscopists for half a century. This was immediately followed by Niels Bohr’s modelling of the Rydberg equation: hence the first explanation of the characteristic elemental lines that the spectroscopists had never understood. It was Barkla in 1911 who established the “K, L, M” nomenclature for the X-ray lines from the atomic shells (before the “Bohr atom”); he started with “K” precisely because he had no reason to believe it was the first!

Atomic excitation by particles was immediately reported, first for alphas (by James Chadwick) and then for electrons (by Henry Moseley). Thus, Rutherford backscattering spectrometry (RBS) and particle-induced X-ray emission (PIXE) are classical techniques closely associated with the birth of the new physics. Electron-probe microanalysis (EPMA) eventually followed from Moseley’s observation, and he was present enough to remark: “The prevalence of [X-ray] lines due to impurities suggests that this may prove a powerful method of chemical analysis”. How right he was!

The first X-ray photoelectron spectra (XPS) were recorded by P. D. Innes in 1907, anticipating XRF. Of course, the photoelectric effect was discovered by Hertz in 1887 and interpreted by Einstein in 1905 but Innes was the first to unequivocally analyse the emitted electrons, interpreting them as due to ‘nuclear [actually atomic] disintegration’ processes. Pierre Auger observed the eponymous “Auger electron” spectra (AES) in 1925, by which time it was clearly understood that XPS was a primary atomic excitation process, and XRF together with AES were the two branches of the secondary relaxation process.

Nuclear (rather than atomic) processes were of great interest in the early 1920s: the transition from RBS to elastic (non-Rutherford) backscattering (EBS) as the Coulomb barrier is exceeded was first effectively demonstrated by Chadwick & Bieler in 1921 (for alphas on H). Of course, in this case the alphas cannot backscatter from H (it is kinematically forbidden) but they can scatter, and the H will recoil with a high energy: such recoils can be detected for analytical purposes and are known as elastic recoil detection (ERD).

Ernest Rutherford first understood that he had observed nuclear reactions in 1922, using the 4.87 MeV α particle from 228Ra on nitrogen gas: the 14N(α,p)17O reaction has a Q-value of −1.19 MeV, so that fast protons were visible. The so-called “Q-value” of the reaction is determined by the mass difference between the initial and final state (before and after the reaction), and can be readily calculated using Einstein’s $E = mc^2$ relation. Note that the rest mass of the electron is 511 keV. Also see Fig. 8 caption for explanation of this nuclear physics terminology.

Later, Cockcroft and Walton were the first to use an electrostatic ion accelerator to induce nuclear reactions, demonstrating the (exothermic) 7Li(p,α)4He reaction, for which the Q-value is an enormous 17.35 MeV, and which has a non-zero cross-section down to very low energies (at 430 keV this is 0.27 mb sr$^{-1}$). We can note here parenthetically that the proton capture reaction 11B(p,γ)12C has its first resonance at an even lower energy: only 163 keV [23–26] (useful both for calibrating ion implantation energies and also for depth profiling boron, with a very high depth resolution implied by the 7 keV resonance width; this is discussed below in §3.3 and Fig. 8). This capture reaction also has a huge Q-value of 16 MeV. These sorts of inelastic reactions are used in the so-called nuclear reaction analysis (NRA), which is known as particle-induced gamma emission (PIGE) when it is the resulting γ-rays that are detected. PIGE is the result of nuclear relaxation after an excitation event in exactly the same way that atomic fluorescence (XRF, PIXE, EPMA) is the result of the relaxation of an atom after it has been ionised.

Digressing a little, and to complete our whirlwind tour of quantum physics history from an elemental analysis point of view, the wave-mechanical interference between identical scattered and recoil nuclei due to their indistinguishability...
was pointed out (for electrons) by Nevill Mott in 1930 and immediately verified using magnetic spectrometers for proton–proton RBS and EBS (measurements and theory). This has a direct analytical use: extraordinary sensitivity for hydrogen (with a detection limit of $1.4 \times 10^{16}$ H cm$^{-3}$) was obtained in 2004 by Reichart et al. using proton–proton scattering with detection of the scattered and recoiled particles in coincidence (see Fig. 2). A 3-D analysis of polycrystalline diamond was made with micron-sized voxels using a 17 MeV proton beam focussed by superconducting magnetic lenses: this high energy was needed to penetrate the sample thickness (55 μm) with adequate spatial resolution. Most IBA labs do not have such high energy microbeams, but thinner samples can be measured equally well with lower energies using the same methods.

The dramatic advance in the understanding of nuclear processes achieved since Rutherford first directly observed atomic nuclei is beautifully exemplified by the extraordinary and seminal work of Burbidge, Burbidge, Fowler and Hoyle in 1957 on stellar nucleosynthesis (the famous “BBFH” paper). It is an astounding experience to realise for the first time that we are – literally! – stardust, and not only that but also to see that it is possible for us to grasp the whole of cosmic history, notwithstanding our manifest insignificance.

BBFH was a lifetime ago: huge strides have been made since then to obtain an understanding of cosmic chemistry, with increasingly well-informed speculations on the origin of life. Curiously, these also have an example using IBA: Howard et al. have recently demonstrated that organic molecules can survive a large meteor impact, implying that interstellar organics could possibly be carried intact to earth. This work was initiated from an unambiguous identification by IBA of carbonaceous inclusions in impact glass, completely against the expectations of the geologists. We will return to this interesting example below (§4.6 and Fig. 23).

2 Thin film depth profiling methods
The modern analyst is regularly confronted by a wide variety of analytical problems. Of course, in any particular project certain analysis methods become the routinely used workhorses, and in the majority of cases the routine workhorse is either the ideal method or at least well-suited to the problem.
But what to do when the routine method fails for the exceptional problems? How to specify appropriate methods for new projects? Which methods should we turn to when we really need absolute model-free fully quantitative analysis?

Standard methods for elemental depth profiling of thin films include secondary ion mass spectrometry (SIMS), cross-sectional transmission electron microscopy (XTEM), scanning Auger microscopy (SAM), glow discharge optical emission spectrometry (GD-OES), X-ray photoelectron spectrometry (XPS), and laser-ablation inductively coupled plasma mass spectrometry (LA-ICP-MS). All of these have very well developed instrumentation and a large analytical literature with very wide applicability, and they (with their variants) are all in widespread use in both industrial and research labs.

In this Review, and in the context of these complementary methods, we will be explaining the strengths and capabilities of ion beam analysis (IBA), which uses an MeV ion beam to probe the sample. Table 1 indicates some of the characteristics of these complementary methods. All analysis methods have strengths and weaknesses, and a wise analyst will have a sensitive appreciation of their complementarity, mixing and matching techniques appropriate to the current analytical problem. Some brief comments here will help the reader to place IBA correctly in context. The strength of one technique is not properly recognised unless the limitations of the others are also understood.

We first (§2.1) describe salient features of the complementary techniques, especially noting the great strengths of each method together with an indication of where alternative methods are needed. We then (§3) briefly sketch the IBA techniques. These will be very incomplete sketches, but should be sufficient for readers to grasp the points in this Review (perhaps with the help of Wikipedia) without being forced to look at other literature. The latter, as we have said before, is voluminous, and we will try to cite it helpfully.

### Table 1  Characteristics of complementary thin film depth profiling methods. Values given are indicative or typical “best” values. Different applications may have widely differing performances. Possible primary beam energies and types are indicated. A wide variety may be used (see text)

<table>
<thead>
<tr>
<th>Primary beam</th>
<th>SIMS</th>
<th>XTEM</th>
<th>SAM</th>
<th>GD-OES</th>
<th>XPS</th>
<th>LA-ICP-MS</th>
<th>IBA</th>
</tr>
</thead>
<tbody>
<tr>
<td>Detected signal</td>
<td>Sputtered ions</td>
<td>Primary electrons in phase contrast</td>
<td>Auger (^a) electrons</td>
<td>Visible photons (^a)</td>
<td>Photo-electrons</td>
<td>Evaporated ions</td>
<td>~3 MeV light ions</td>
</tr>
<tr>
<td>Destructive (^b)</td>
<td>Yes</td>
<td>Yes</td>
<td>No</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Depth resolution (^c)</td>
<td>2 nm</td>
<td>0.1 nm</td>
<td>2 nm</td>
<td>20 nm</td>
<td>2 nm</td>
<td>50 nm</td>
<td>2 nm</td>
</tr>
<tr>
<td>Information depth (^d)</td>
<td>500 nm</td>
<td>100 nm</td>
<td>500 nm</td>
<td>50 μm</td>
<td>500 nm</td>
<td>~5 μm</td>
<td>15 μm</td>
</tr>
<tr>
<td>Lateral resolution (^e)</td>
<td>50 nm</td>
<td>0.1 nm</td>
<td>2 nm</td>
<td>1 nm</td>
<td>3 μm</td>
<td>10 μm</td>
<td>500 nm</td>
</tr>
<tr>
<td>Elemental imaging</td>
<td>Yes</td>
<td>EELS, EDX (^f)</td>
<td>Yes</td>
<td>No</td>
<td>No</td>
<td>No</td>
<td>Yes</td>
</tr>
<tr>
<td>Molecular information</td>
<td>Yes</td>
<td>No (^g)</td>
<td>Yes</td>
<td>No</td>
<td>No</td>
<td>Yes</td>
<td>No</td>
</tr>
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<td>Ambient analysis</td>
<td>No</td>
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<td>No</td>
<td>No</td>
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<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Sample preparation</td>
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<td>Yes</td>
<td>UHV</td>
<td>No</td>
<td>UHV</td>
<td>No</td>
<td>No</td>
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<td>Quantitative</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
</tr>
<tr>
<td>Standards needed</td>
<td>Yes</td>
<td>—</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>No</td>
</tr>
<tr>
<td>Elemental sensitivity (^h)</td>
<td>10(^{-8})</td>
<td>10(^{-1})</td>
<td>10(^{-3})</td>
<td>10(^{-6})</td>
<td>10(^{-3})</td>
<td>10(^{-9})</td>
<td>10(^{-6})</td>
</tr>
<tr>
<td>Accuracy</td>
<td>—</td>
<td>—</td>
<td>10%</td>
<td>10%</td>
<td>5%</td>
<td>5%</td>
<td>1%</td>
</tr>
<tr>
<td>Traceability</td>
<td>—</td>
<td>—</td>
<td>—</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>primary</td>
</tr>
</tbody>
</table>

\(^a\) Auger electrons, photoelectrons and characteristic photons (X-rays or visible) are effects of atomic excitation, which can be by electrons (AES or SAM, EELS), photons (XPS, XRF) or ions (IBA). \(^b\) SIMS, SAM, XPS, GD-OES use sputtering to obtain depth profiles; XTEM requires special sample preparation. LA-ICP-MS uses laser ablation. IBA is not deliberately destructive, but the probe beam is energetic and may damage the sample.

\(^c\) For SIMS, SAM, XPS the depth resolution depends on control of the sputtering beam; for the LA-ICP-MS the depth resolution depends on control of the laser parameters; for GD-OES the sample is consumed by the plasma; the best IBA surface depth resolution for standard methods is given (rapidly degrades with depth). \(^d\) For SIMS, SAM, XPS, GD-OES the information depth depends on the sputter time; for IBA the information depth depends on the depth of the laser pulse at the same spot. \(^e\) For SIMS, SAM, XPS and IBA the lateral resolution is given by the spot size of the scanned probing beam: respectively keV ions, electrons, photons (X-rays), or MeV ions. \(^f\) Electron energy loss spectrometry (EELS) of the transmitted primary beam. Reliable elemental characterisation available as an attachment on many higher spec TEMs. See Fig. 23d. Energy-dispersive X-ray analysis (EDX) is usually rather low sensitivity in the TEM because of the very non-optimal geometry. \(^g\) SIMS is quantitative in particular well-characterised cases, and semi-quantitative in many other cases. Sample-matched standards are always needed. \(^h\) Elemental sensitivity is expressed in atomic fraction (not mass fraction) for all techniques. \(^i\) SIMS can be used with excellent relative accuracy but only in specific very well characterised cases. \(^j\) Three methods have been used as reference methods: only RBS is demonstrated as a primary method. \(^k\) TEM-EELS, GD-OES and LA-ICP-MS are usually used for elemental depth profiling although in principle all of them could be used to obtain chemical information. IBA is usually used only for elemental depth profiling, although PIXE-WDX and high energy resolution PIXE-EDX have both been used to obtain chemical information.
depends) is usually a strong function of the composition. The surface is also an important interface which is tricky to analyse reliably by sputtering methods.

- There are a variety of high-specification SIMS instruments capable of high throughput high reproducibility depth profiling, even at the sample surface. This is a standard workhorse in many labs. SIMS usually has a very high sensitivity, but its problem is that the ionisation probability for secondary ions may vary by orders of magnitude, and the matrix effect is usually huge. This means that quantification is always difficult, and that sample-matched standards are essential for accuracy. Seah et al. is a prominent example of an accurate comparison of SIMS and XPS.

- XPS uses useful 2-D high resolution (~0.1 eV) electron energy analysers which are easily good enough to detect chemical shifts in the electron binding energies. This is the reason for the name Kai Siegbahn gave the technique: electron spectroscopy for chemical analysis (ESCA), . The great value of the technique, apart from the ability to distinguish between (for example) oxidation states of metals, is that the electron mean free path (EMFP) in the sample being analysed is very short (~5 nm) so that photoelectrons only escape with their characteristic energy intact from the very near surface of the material. XPS is therefore a surface sensitive technique. To use it for depth profiling the sample must be sputtered away, with an XPS analysis for every sputtering increment.

Considering quantitative depth profiling, the weakness of the technique is that the EMFP is a strong function of the material and is not usually known very accurately. Therefore, standards are needed to determine EMFP (which IBA could provide ). Despite this, the method is classed as “traceable” and very considerable effort has gone into developing analysis protocols that allow accreditation of XPS labs to the ISO 17025 standard (Seah & Spencer ). However, the sensitivity of XPS is limited to a fraction of atomic% per layer: thus, it is insensitive to minor or trace elements not concentrated in layers.

XPS benchtop instruments use tube X-ray sources, which can be monochromated: all synchrotron light sources include XPS instrumentation: sy-XPS is very powerful.

- SAM uses the non-radiative atomic relaxation AES (Auger electron spectroscopy) process after excitation by an electron beam. The great advantage of AES is that it can be mounted into a (modified) scanning electron microscope (SEM), and the AES signal is used for imaging. Both XPS and AES (and therefore also SAM) are surface sensitive techniques, using the same electron energy analysers and getting depth profiles by sputtering.

- XTEM is an extraordinarily powerful technique, allowing atomic-level structural information by direct phase-contrast imaging of strings of atoms (so-called “high resolution”), and also using selected area diffraction (SAD) to identify the crystal structure, orientation and lattice parameter of nano-crystals. Crystalline defects (dislocations, twins etc.) can be imaged directly, using “dark field” imaging with the primary electron beam oriented crystallographically (but TEM is not sensitive to point defects, for which positron annihilation spectroscopy, PAS, is needed). Elemental sensitivity can be obtained either by including an energy dispersive X-ray detector (EDX), or by using the energy-analysed transmitted electrons, so-called electron energy-loss spectrometry (EELS), where the information derives from the effect of target atomic excitation on the primary beam. A recent example is of nano-structured CeO thin films, and we have discussed another example shown in Fig. 23d.

However, XTEM has a number of weaknesses. Sample preparation is laborious and time consuming, and can be very difficult; also, operating the instrument is very highly skilled and requires great intelligence, including the ability to think in reciprocal space: XTEM is not a fast method for routine use on many samples! The field of view of TEM samples is of the order of 100 nm, so that there is always the question of whether results are representative. Determining quantity of material (fully quantitative EELS or EDX) is usually impossible because sample thickness (on which the EELS or EDX signals depend) is a strong function of the sample preparation, is hard to control, and very difficult to measure. Even the phase contrast images are not entirely straightforward to interpret, so that “simple” film thickness measurements can have much larger errors than expected. This was very clearly demonstrated by Seah et al. in an extensive and important multi-technique Intercomparison exercise which established the use of XPS for the very accurate determination of native silicon oxide thicknesses.

- GD-OES is a completely different sort of analysis method with little or no lateral resolution, but rather good at profiling thick (>20 μm) layers. Again, considerable effort has gone into quantification, which always requires sample-matched standards (see the critical review by Winchester & Payling of NIST).

- LA-ICP-MS is also a completely different sort of analysis involving mass spectrometry where the sample that enters the spectrometer is created by a very well-controlled laser pulse. Even though the lateral and depth resolution of the technique is not usually very good, it can be used very effectively for accurate work (for exceptionally good spatial resolution see Gutiérrez-González et al. for a recent use in reference material certification, see Jochum et al.).

- Multitechnique examples: recently, the EMPIR programme (“European Metrology Programme for Innovation and Research”) has stimulated systematic analytical work on the chalcogenide glasses – in particular “CIGS”, Cu(In,Ga)Se, which have become important materials for thin film photovoltaics. These are complex materials, and the more powerful analytical methods usually need sample-matched standards for quantification. Abou-Ras et al. directly compare 18 techniques (including SIMS, XTEM, XPS, AES, GD-OES, EELS; also RBS, ERD). In a supplementary paper, Abou-Ras et al. add “laser-induced breakdown spectroscopy” (an OES variant of LA-ICP-MS) and grazing-incidence X-ray fluorescence (GI-XRF), which is a powerful depth-profiling method used with great delicacy by synchrotron groups for both layered and
implanted samples, and is an interference method analogous to variable-angle spectroscopic ellipsometry (VASE).

The photovoltaic (PV) efficiency of CIGS materials deposited on plastic (flexible) substrates have been significantly improved (to >20%) by the use of alternates to sodium passivation of grain boundaries. Materials aspects of this development have been described by Reinhard et al. (2015), who used SEM, XPS, ICP-MS, ERD, SIMS and PAS in a very thorough analysis. Heavy ion ToF-ERD (13 MeV I, see §3.5) was used to obtain quantitative depth profiles of all elements, including the important light elements.

- Sample charging: it is worth pointing out that the low energy techniques (particularly SIMS, XPS, SAM) cannot be used on insulating samples without very careful attention to charge compensation. As a high energy method IBA is much less sensitive to sample charging, but it is still sometimes a problem.57

2.2 Model-dependent thin film depth profiling methods

Atomic excitation methods (including XRF, PIXE etc.; see Jeynes & Grime for a general discussion) usually give integral signals, where depth information affects the signals but cannot usually be extracted from them unambiguously. Important and widely-used methods include X-ray fluorescence (XRF) and electron-induced XRF using a scanning electron microscope (SEM), either with energy-dispersive X-ray spectrometry (SEM-EDX) or with so-called electron-probe microanalysis (EPMA) which also uses wavelength dispersive X-ray spectrometry (WDX). Today the high specification SEMs can operate as EPMA, and here we will use “EPMA” to include “SEM-EDX”.

Both XRF and EPMA are now available commercially in very powerful desktop instruments supplied complete with advanced software based on “Fundamental Parameters” methods (see §3.2) which lead the operator through a proper instrument calibration procedure and is then able to validly interpret the spectra on the basis of sample structure information input by the operator without sample-matched standards. Thus, unwary users may think that XRF or EPMA can tell them layer thicknesses: indeed they can, but only if the layer existence and matrix composition are assumed. This is what is meant by “model-dependent” analysis.

Of course, in many cases the sample structure is known quite well in principle, and it is the details that need quantifying: there is no doubt that this sort of information from XRF and EPMA is highly valuable. But analysts need to be aware that the sample structure itself is assumed, and it is frequently difficult or even impossible to critically assess the validity of the assumed sample structure without recourse to other analytical techniques. Indeed, it is not always easy to remember the assumptions that underlie an analysis, and in §3.2 we give one interesting example where perhaps the power of sy-XRF has been rather overstated.

Depth information can be explicitly unfolded from X-ray data without sample structure assumptions using differential methods: the use of sputtering to reveal the depth information is clearly such a (destructive) differential method, and “angular resolved” XPS and the analogous “differential” PIXE are non-destructive differential methods. Karydas et al.61 explicitly compare reference-free sy-GIXRF with Total-IBA (PIXE + EBS/RBS), where again the application is to CIGS films.

IBA has an entirely different, and model-free, approach to extracting the depth information from the (integral) atomic excitation (PIXE) data: the commensurate methods (most often PIXE + EBS/RBS) mutually interpret each other. This synergy is central to this Review, and we explore it in §4 below.

3 Recent advances in IBA

Ion beam analysis (IBA) is usually done with light ions and quite small accelerators: for example, both Surrey and Namur have a 2 MV “tandem”, and similar machines are common.‡ Such machines inject a negative beam towards the central positively charged (say, 1 MV) terminal; at the terminal the 1 MeV particles are passed through a so-called “stripper” (usually nitrogen stripper gas channel but can be a thin carbon foil) which efficiently strips electrons from the atoms. The particles, now positively charged, are then accelerated away from the terminal. So 1 MV potential on the terminal will give us 2 MeV singly charged particles, 3 MeV doubly charged particles, and so on. A 2 MV machine can deliver 4 MeV protons, 6 MeV alphas, 8 MeV Li, etc.

Light ion beams (typically protons and alphas) generate backscattered ions (RBS for 1.5 MeV alphas, see §3.1; or EBS for higher energies and protons, see §3.3). They also generate PIXE (see §3.2), and the faster the ions the more X-rays you get. Particle-induced X-rays (PIXE) result from relaxation of inner-shell (core) electron excitations: of course the outer shells are also excited by ion impact but result in lower energy photons (so-called ion-beam-induced luminescence, IBIL) that are much less penetrating, harder to use and much harder to interpret. Still, IBIL is now attracting growing interest; although it is outside the scope of this Review we mention recent work on: damage centres in oxides, and demonstrating sub-30 nm imaging (of subcellular structures) using ion-beam-induced upconversion luminescence in lanthanide nano-crystals. The latter may prove complementary to (for example) stochastic optical reconstruction microscopy (STORM).

Light ions at these MeV energies sometimes produce strong nuclear reactions in certain isotopes: this is the basis of NRA and PIGE. The NRA methods are not emphasised in this Review since they have not significantly improved recently, although the IAEA has sponsored work which may yield dramatic improvements in PIGE quite soon.

These accelerators usually have versatile ion sources which can generate ion beams from essentially the whole Periodic Table.

† See https://nucleus.iaea.org/sites/accelerators/Pages/default.aspx the list of accelerator laboratories at the IAEA “Accelerator Knowledge Portal”.

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Table. So heavy ion beams are easy to produce, and are very well established for two main analytical uses: accelerator mass spectrometry (AMS) and elastic recoil detection (ERD). In AMS the sample is destroyed in the ion source, and its atoms are mass analysed, with isotope discrimination levels of $10^{-15}$ now routine in some cases. One important AMS centre is in Zurich, who have demonstrated outstanding performance with a 600 kV accelerator.67 But this is not a depth profiling method and is outside the scope of this Review. Heavy ion ERD on the other hand is a very important and versatile depth profiling method which has been dramatically improved recently (see §3.5).

IBA depth profiling is based on the energy loss of the probing beam in the target as well as the energy loss of the scattered or recoiled nuclei. It is not deliberately destructive – it does not sputter the sample away to mass-analyse the sputtered atoms as SIMS does, for example – so you get the sample back “intact” after the analysis (although there may still be damage induced by the energetic beam68). But of course there are also mass effects, easily calculated from kinematics. Thus the spectra always convolve mass and depth information and inverting the spectrum to recover the depth profile is a mathematically ill-posed problem: we return to this important issue repeatedly below.

Depth profiling of defects is a classical use of IBA when investigating crystalline materials and their response to various treatments. In particular, ion implantation in semiconductors is an enabling technology for modern electronics, and the implant always introduces crystalline damage (visible in Fig. 3) which must be healed by annealing to activate the impurities (“dopants”) electrically. Annealing is a complex materials problem in which there is still intense interest:69 the related problem of the lattice location of the implanted ion on annealing is also current.70 Channelling is a large and classical topic in its own right which we only mention here, because on the one hand there have not been significant recent advances and on the other hand it is mostly about the nature of the detected defects rather than their position in depth. But Fig. 3 indicates the power and versatility of the technique, showing the integrated damage as a function of lateral position introduced in single-crystal silicon by machining.71 At each point a quantified damage depth profile was obtained, including the contribution of both point and line defects. It is remarkable that silicon can behave plastically in some circumstances despite its extreme brittleness.

Finally we take up the issue of imaging and tomography. Depth profiling, the subject of this Review, involves 1-D spatial resolution in the direction of the probing beam, where imaging involves 2-D spatial resolution in the plane perpendicular to the probing beam. Focussed MeV ion beams with spot sizes of about 1 µm have been standard for over two decades, and it has proved remarkably difficult to improve on this because of the large off-axis aberrations of magnetic lenses. But recently some dramatic advances have been demonstrated, with spot sizes demonstrated down to 25 nm for very low beam currents. These can be used in scanning transmission ion microscopy (STIM) which is a direct ion analogue of EELS (see Table 1). STIM tomography is now a reality. 3-D imaging also becomes possible if the depth profiling can be put together with imaging. We explore all this in §3.8.

3.1 Accurate Rutherford backscattering spectrometry (RBS): ISO 17025

3.1.1 Understanding Rutherford backscattering. Among all the techniques mentioned so far, RBS is distinctive since the interaction cross-section is described analytically by considering point charges in a Coulomb field. Therefore in principle it is well suited to being a highly accurate primary reference method. This is why Anthony Turkevich claimed it was “1% accurate” in his report on the analysis of Moon rocks following the landing of Surveyor V in 1967.72 However, it turns out that this claim was hard to substantiate, and indeed transparent evidence for such accuracy has not been available until 2012, when Jeynes, Barradas & Szilágyi73 published a careful multi-laboratory analysis of the “quantity of material” (that is, the ion dose) in an ion implanted sample with a detailed account of uncertainties to the second and third order of accuracy. This paper is now the standard reference for RBS.

Stoichiometry is simpler than quantity of material to measure by RBS since only a relative measurement is needed. Even so, the first measurement at 1% accuracy which included a critical evaluation of the uncertainties was only published in 1997.74 This is a classical use of RBS which is still useful even for relatively inexact work where the uncertainty probably approaches only 5%. A recent example of such work is in ligand exchange chemistry (using nuclear magnetic resonance,
NMR) in which the power conversion efficiency of optical devices based on semiconductor CdSe nanocrystals was increased from ~1% to ~30%! RBS was used to determine the Cd : Se : Cl ratios where the ligands were chloride-terminated and the quantity of excess Cd was critical.75

Fig. 4 shows how the ‘quantity of material’ measurement works: the RBS spectrum shown is an energy spectrum, where “channel number” represents the detected energy of the backscattered particle, and the conservation of energy and momentum (kinematics) requires that heavy (or light) target atoms scatter the primary ion beam at high (or low) energies.

Fig. 4 is also an energy loss spectrum where the energy loss mechanism for energetic ions in material is now known fairly well, having been intensively studied since Bragg’s early work over a century ago. The energy loss is rather insensitive to chemical effects at the 5% level (although larger effects can be observed), and generally energy loss can be estimated for arbitrary materials from a linear combination of elemental energy losses (the so-called “Bragg’s rule”) for which a semi-empirical and very widely used database now exists (http://www.srim.org) and has recently been discussed by Ziegler et al.77 The database contains thousands of measurements, but is still sparse and inaccurate; new work is filling gaps,78 using new more efficient methods,79 and achieving very much better accuracy.80

It is the energy loss of the ion beam in material that directly gives depth profile information. The 80 keV arsenic implant in Fig. 4 has a range in silicon of 56 nm with a straggle of 17 nm, consistent with the observed peak and straggle of the As signal shown in the inset of Fig. 4, provided the instrumental function (essentially the detector resolution) is deconvoluted from the signal. This depth sensitivity is a classical use of RBS which remains important: in recent examples thorium diffusion in monazite (important in geochronology),81 the composition of reverse osmosis membranes,82 the stoichiometry of colloidal quantum dots,83 the composition of iron pyrite thin films (for photovoltaic applications),84 and the stoichiometry and thickness of SnO₂ thin films85 were all determined using RBS.

RBS spectra are energy spectra that convolve depth and compositional information in a complex way: Fig. 4 is a simple example where all the signals can readily be distinguished, although even in this case the implanted Ar signal partially overlaps the Si substrate signal. In the general case the signals for the various elements of the target mutually overlap (as in Fig. 1): mathematically this turns out to be an ill-posed problem (see Jeynes et al.), which we discuss further in §§3.4, 3.9.

3.1.2 “Quantity of Material” by RBS at 1% accuracy. Ion implantation has been an enabling technology for the entire semiconductor industry since the 1970s, and is now used as an important manufacturing technology in wide variety of industries (see Ghicov et al.86 as just one example of a novel application). Fig. 4 is an RBS spectrum of a typical ion implanted sample: arsenic is an n-type dopant which is implanted into p-type silicon to make an n–p junction.

![Fig. 4 Absolute determination of quantity of material by RBS. The sample is the “SPIRIT21” sample used by Jeynes et al.73 from which work this Figure was redrawn: Si nominally implanted with 5 × 10¹⁵ As cm⁻² at 80 keV (and 3 × 10¹⁵ Ar cm⁻² at 150 keV to amorphise). Elemental edges (highest backscattered energy) for As, Ar and Si, and the amorphisation depth in the silicon substrate are marked. The inset shows As signals from two RBS detectors plotted on a depth scale, uncorrected for straggle and detector energy resolution. The full energy spectrum is shown for one of these detectors. Note the background under the As signal, due to pulse pileup. Note the logarithmic scale of the ordinate axis. Reproduced from Fig. 1 of Colaux et al., Analyst, 201587 with permission from the Royal Society of Chemistry (RSC). The equations are rearranged from the same paper.](image-url)
In Fig. 4, eqn (1) shows the interpretation of the As yield from the measured area $A_{\text{AS}}$ of the As signal: $A_{\text{AS}}$ is proportional to the number of arsenic atoms $f_{\text{As}}$, the Rutherford cross-section $\sigma$ (known analytically), and the charge $\times$ solid-angle product $Q\Omega$, where $Q\Omega$ is given (eqn (2)) by the ratio of the (measured) amorphous Si yield $Y_{0,\text{Si}}$ and the gain of the spectrometer $\Delta$, provided the energy loss factor $[\varepsilon_{0,\text{Si}}]$ is known ($\Delta$ is discussed later with Fig. 6).

Using this method of determining implanted dose from RBS (treating the amorphised substrate signal as an internal reference) the Surrey ion implantation group have carried out a systematic quality assurance exercise to qualify the ion beam fluence, with the retained ion dose absolutely determined by RBS (see Colaux et al., 87 and Fig. 5). This work was a longitudinal study of implanter behaviour over three years, in which the RBS was demonstrated to be reproducible at 0.3% using an analysis of variance (ANOVA) method according to ISO Guide 35,88 and in which both the charge-collection measurement in the ion implanter and the post-implantation electrical characterisation of sheet resistance by four-point-probe (4pp) measurements were separately demonstrated accurate at, respectively, 1.1% and 1.3% (where all numerical error estimates are standard combined uncertainties). To make 4pp measurements the silicon must be annealed to activate the As atoms, that is, to make them substitutional in the Si lattice so they can act as electrical dopants. Thus, 4pp measurements involve further processing.

This is a remarkable result since three independent measurements of the same quantity (retained ion dose) are shown to be self-consistent, at an accuracy for each which is comparable to (or better than) current best practise. Two of the measurements (RBS and the charge collection in Faraday cups) have full traceability, with the Faraday cup measurements only equivocal because of the possibility of secondary and tertiary electrical currents disturbing the measurement. What we have demonstrated is that the Faraday cup design effectively suppresses these potential auxiliary currents. The third (4pp) shows an excellent relative consistency, with the absolute values depending on a calibration curve (converting sheet resistance to implanted dose: this is VIM terminology89) that is determined by our results. Thus, that the three datasets are demonstrably mutually consistent is itself a fact rich in information.

This accuracy for the 4pp and charge-collection are demonstrable only because both the reproducibility (0.3%) and the accuracy (1%) of the RBS are sufficiently good. The uncertainty of these RBS measurements is thoroughly evaluated through an uncertainty budget (“bottom-up” approach) which has been

Fig. 5  RBS repeatability. Repeated independent measurements of the retained $^{75}\text{As}$ dose in the sample measured by Jeynes, Barradas & Szilágyi. 73 25 independent fluence measurements of the same sample by RBS over a 31 months period using various incident beams: 9 MeV $^{12}\text{C}^{4+}$ (in orange); 4 MeV $^{7}\text{Li}^{2+}$ (in red); 2 MeV $^{7}\text{Li}^{2+}$ (in purple) and 1.5 MeV $^{4}\text{He}^{+}$ (in blue). The error bars are given for each measurement as the “Total combined standard uncertainty”. The weighted mean of the measurements (in green) has a precision (standard error on the mean) of 0.19%. The dataset has a standard deviation of 0.93%. ANOVA shows repeatability (the between-bottle variation, in ISO Guide 35 terms) of 0.33%. Reproduced from Fig. 7 of Colaux et al., Analyst, 2015 87 with permission from the Royal Society of Chemistry (RSC).
validated against an analysis of variance (ANOVA; “top-down” approach) of a longitudinal study. The RBS accuracy is traceable to an ion implanted certified reference material (CRM) manufactured and certified by IRMM and BAM through the use of the “stopping power factor” ([ε] in eqn (2) of Fig. 4) of the ion beam in silicon as an intrinsic measurement standard (again using VIM terminology) whose value was established separately (Colaux & Jeynes).

RBS is sensitive to the ion beam energy since the Rutherford cross-section goes as 1/E²; we also show how to directly measure this beam energy (at 0.03% accuracy), using the well-established nuclear resonance at 3038.1 keV of the 16O(a,α)16O elastic scattering cross-section function as another intrinsic measurement standard. See §3.3 for a discussion of the non-Rutherford scattering cross-sections.

3.1.3 Pitfalls for accurate RBS. Each input of the uncertainty budget ascribed to high accuracy RBS measurements has been discussed at length elsewhere. It is nevertheless worth noting that accurate RBS strongly depends on how well the experimental setup is under control. In particular, some parameters usually considered as trivial (and often overlooked) can significantly affect the final result of the measurement.

This is the case for the scattering angle of detection which is often (approximately) derived from the schematics of the analysis chamber. That is clearly not good enough for accurate RBS when an error of 0.5° gives a variation of about 1% in the RBS cross-section (σ in eqn (1) of Fig. 4) calculated at a backscattering angle of 150°. For non-Rutherford scattering the effect can be larger (see Fig. 10).

Another very good example is the linearization of the acquisition chain through the use of a proper model of the detector, which always has an entrance dead layer in which the particle loses some energy, with the energy loss being a function of the particle energy. Therefore, the detected pulse height is not a linear function of the incident particle energy: this effect is known as the pulse-height defect (PHD). This seems obvious but historically has only rarely been applied, precisely because RBS is very linear even neglecting this correction. Colaux & Jeynes have shown that in their conditions the linearization correction is about 1%, but also that the presence of such an error makes the determination of the spectrometer gain (Δ in eqn (2) of Fig. 4) effectively uncontrollable in detail, so that the precision may easily be worse than 2%. Thus, simple unlinearised RBS works perfectly well at 5% accuracy for a given beam energy, but much more care must be taken to take advantage of its intrinsically high precision (<0.5%). We do this systematically, following a detailed calibration procedure and using a very well characterised code (discussed below in §3.4).

For a given beam energy the non-linearity of the spectrometer is not so easy to detect, being rather a small effect; Fig. 6 shows an example where it is plainly visible in a simple case where the interpretation of the RBS spectrum is obvious.

The maximum scattered energy from Si and N atoms at the sample surface (channel numbers 300 & 160) is readily calculated from the kinematics: assuming linearity this immediately gives the apparent spectrometer gain (in keV per ch). It is then possible to include ISO Guide 34 certification of Reference Materials.

3.1.4 Future prospects for accurate RBS. The full procedure for accurate RBS summarised by Colaux et al. has been accredited as conforming to the ISO 17025 standard, and we intend to apply for an Extension of Scope for our accreditation to include ISO Guide 34 certification of Reference Materials. The Surrey Ion Beam Centre itself has a Quality Management System currently certified to conform to ISO 9001:2008.

At present, the accreditation is for the very limited case of heavy implants in silicon, since we depend on the stopping power factor [ε] given by the energy loss in silicon; [ε] is accurately known for 1.5 MeV He in Si from a measurement traceable to an Sb-CRM implant, where [ε] is used as an intrinsic measurement reference standard, thereby removing the need for the difficult measurement of the collected charge and the detector solid angle (QΩ in Fig. 4). However, we have shown that all the parameters of the measurement are well defined (and that the spectrometer is accurately linear when treated correctly), and therefore that the uncertainty budget is very well determined and robust. In particular, the beam energy and the spectrometer gain can now both be determined reliably at very high accuracy.
The case treated so far is rather restrictive, but is actually rather easy to generalise. This can be done at least two ways: by accurate charge measurement (giving $Q\Omega$ since the detector solid angle $\Omega$ is an apparatus constant), or by scanning the beam between the sample to be certified and a standard. Both of these are entirely feasible with present technology (even if the $Q\Omega$ determination remains notoriously difficult to achieve at better than 5%), and we expect to report high accuracy measurements of thin film foil thicknesses soon: this would be directly relevant for XPS and XRF communities that need reference standards certified at higher accuracy than is currently available to refine the current “Fundamental Parameters” values (see §3.2).

Note that such improvements in knowledge of the FP values would also be directly relevant for the IBA community since they are needed for validly interpreting the PIXE spectra complementary to (accurate) RBS (see Table 3 and §3.4.1) and are always available where an ion beam is used as a primary probe. The cross-sections for X-ray production nevertheless require one to use rather high incident beam energies for which the RBS formalism often breaks down. The knowledge of the (non-Rutherford) elastic backscattering (EBS) cross-sections therefore becomes essential for an accurate analysis of EBS spectra. This is discussed in §3.3.

3.2 EXSA’s “Fundamental Parameters Initiative” for XRF methods

Modern analytical methods depend on extensive and detailed knowledge of material parameters. Depth profiling by IBA depends on a single (large) semi-empirical electronic energy-loss database (see §3.1.1). In contrast, the XRF techniques (XRF, PIXE, EPMA) depend on (at least) three large and complex databases of the “Fundamental Parameters” (FP) that enable the accurate calculation of the ionisation, fluorescence and absorption cross-sections; these databases were originally established in the 1980s as a result of a huge quantity of first class work by both theoreticians and experimentalists.

But analytical requirements have become much more stringent than a generation ago, with the advent of a clutch of new and relatively complex functional materials (just as one class of examples). And it has become clear that the databases that have served us well for a generation now need revisiting: the European X-ray Spectrometry Association (EXSA) has perceived a “lack of recent reliable values with low associated uncertainties”, and since 2008 has been promoting its “FP Initiative” to address this lack. In this section we briefly introduce the necessity for an FP approach to XRF, and the new work that is improving and underpinning analytical accuracy.

Fig. 7 shows extraordinary data collected on Mars and analysed on Earth to determine Martian geochemistry. This is a tour de force of analysis which depends on very careful verification and handling of the X-ray data, summarised for the MSL team in a pair of recent Science papers,98,99 where the details of the calibration are explained by Campbell et al. in an important paper in 2012.100

It is worth noting here that there is an interesting philosophical difference between PIXE and RBS. The abscissa units for Fig. 1 are the instrumental “channel number”, where those for Fig. 7 are in absolute energy units (keV). This is because PIXE spectra show characteristic lines of the elements, where the line energies are natural constants (apart from tiny chemical shifts invisible at this energy resolution): the abscissa calibration is determined by the spectrum. But for the nuclear techniques the spectra show energy loss, and the interpretation of the spectrum depends on the spectrometer calibration, which must be done separately (see §3.1.3 and the discussion for Fig. 6). To give an RBS spectrum with the abscissa in keV interprets the data, whereas a PIXE spectrum in keV is still effectively raw data.

XRF has historically used sample-matched standards for accurate analysis but it was recognised very early that for homogeneous samples the composition could be unfolded from the XRF spectra – provided the appropriate fundamental parameters were known. The problem is that the calculation is complicated; moreover, not only the databases but also their interactions are intricate. A compromise was the use of the semi-empirical approach (the so-called “ZAF correction”, involving the atomic number, the self-absorption of the sample, and the self-fluorescence). In the presence of all these uncertainties, analysts always used sample-matched standards for accurate work: in the absence of such standards it is very difficult to be sure of the reliability of the estimates of uncertainty.

Therefore, this work on Mars data, where “sample-matched standards” are in principle not available, must use a pure
Fundamental Parameters (FP) method. And the MSL team are explicit that the data reduction is for unknown samples.

Recent FP work includes obtaining L-shell and K-shell parameters for germanium, mass attenuation coefficients for silicate minerals and aluminium, widths of energy levels, L-shell fluorescence yields, the K-shell fluorescence yield of Si, and the photo-ionisation cross-sections for light elements. Systematic K, L, & M-shell ionisation cross-sections for H and He beams are now available and much interesting new information is becoming available (using high energy resolution detectors) on chemical effects on line positions (WDX) or intra-shell branching ratios (HR-EDX). The latter uses the new transition-edge sensors operating at ~100 mK which are presently capable of an energy resolution of 2 eV at 6 keV but which give the full EDX spectrum. This means that it is easy to obtain good data on the intensity ratios of diagram lines, very difficult for WDX because of the limited energy range of each measurement. There is now intense development of this highly promising technology: see, recently, Palosaaari et al.

We mentioned above (§2.2) that depth information in XRF (or in PIXE by itself) cannot be obtained directly. Strictly speaking the same applies to determining Quantity of Material, since the ZAF correction must always be applied for good quantification, which cannot be done without knowledge of film thicknesses. So, regular EPMA work, or commercial XRF quantification using fused glasses assume homogeneous samples of infinite thickness. But recent sy-XRF work on biological samples (Turnbull et al.) makes tacit assumptions which very significantly reduce the information available relative to comparable recent IBA work (Jeynes et al.), especially since XRF data are not so rich as IBA data.

Turnbull et al. map the elemental distribution using sy-XRF in large numbers (204) of human cancer cells with the aim of counting the number of gold nanoparticles (GNPs) the cells have taken up under different irradiation conditions. Analytically, they identify cells through their Cu content and assign Au L counts per cell through this identification. Experimentally they obtain a high count rate by using the Maia detector, and quantify the XRF through standards in the usual way using the GeoPIXE code (for Maia and GeoPIXE, see §3.4.2: it is “trivial” to add an XRF module to a PIXE code, only the excitation mechanism is different), ignoring absorption effects which are assumed to be small for these relatively high energy X-rays. But because they only roughly determine the spatial extent of the cells, they have no reliable means of normalising the GNP content per cell to the cell size.

On the other hand, Jeynes et al. have made a more extensive study using Total-IBA (PIXE + EBS), also on (a different line of) human cancer cells. They map the elemental distribution in large numbers (332) of cells, but obtain a mass closure close to 100% since they measured the light elements (except H) directly. In particular, because C and P (and S) signals are clearly identifiable, they can weigh each cell individually as well as counting the GNPs per cell. They are therefore able to explore much more thoroughly the inhomogeneity in the GNP uptake that was of interest to Turnbull et al. (also obtaining the cell size inhomogeneity directly) and specifically, showing that it conforms to the Hill equation.

Turnbull et al. measure gold heterogeneity in the cells but this measurement takes no account of cell-size heterogeneity. They measured Cu as a proxy for cell size, but this may be a poor proxy, both because the signal is small (giving large counting statistics uncertainties) and because the Cu concentration in cells is also subject to a large variation (being regulated by external factors). In contrast, Jeynes et al. do not use a proxy for cell size, measuring C (and P + S) directly from the particle spectrum. Such a measurement is not available by XRF. In this case where the sample is known to be thin, the fact that XRF cannot correctly do the ZAF correction in the general case (because it is blind to sample thickness) is not important.

Interestingly, the sy-XRF and the IBA are analytically rather similar, with comparable detection limits for GNPs, and similar spatial resolution. The sy-XRF had much shorter counting times due to the much more sophisticated (and expensive) Maia detector which is so much faster than the standard lithium drifted silicon detector used by the IBA group. Critically, the XRF had neither light element nor depth sensitivity, and therefore could not have corrected for the absorption effects had they been significant. It is notable that Turnbull et al. emphasise the importance of single-cell measurements and therefore the advantage of spatially resolved analysis, but they appear unaware of the prior IBA work, comparing only to bulk analysis methods.

3.3 Evaluated elastic backscattering (EBS) cross-sections

In Rutherford’s 1911 treatment, the eponymous RBS assumes point charges in a Coulomb field. But as the beam energy increases, the distance of closest approach of the two nuclei decreases. What happens when this distance becomes comparable to the nuclear size? Clearly “RBS” is always an approximation: the questions are, how good is this approximation? and when does it completely break down? Parenthetically, it is interesting that of course Rutherford himself did a “classical” calculation, but the RBS cross-section also results from a quantum mechanical calculation of Coulomb potential scattering.

We mentioned above (§1) the large resonance in the 11B(p,γ)12C nuclear reaction at 163 keV: Fig. 8 shows that this resonance results in a non-zero reaction cross-section down to very low energies. The cross-section functions are given in terms of the astrophysical S factors (in keV-barn) which are effectively normalised to eliminate the exponential decrease of reaction rates at projectile energies below the Coulomb barrier as the beam energy decreases. This normalisation is needed since these reaction rates are dominated by the probability for barrier penetration. The differences between “Solution 1” and “Solution 2” in Fig. 8 are due to the detailed low energy effects of quantum mechanical interferences between higher energy states, and these effects are very sensitive to the details of the calculation, meaning that the low temperature behaviour is very difficult to determine.
Recall that the core temperature of the Sun (for example) is surprisingly low: \(16 \times 10^6\) K is only 1.4 keV! But even at this ridiculously low temperature nuclear reactions still proceed — very slowly! Of course, it is just as well that the reactions are slow, otherwise the Sun would not have been burning steadily without any noticeable change for 4 billion years. And we would not be here to talk about it!

Nevertheless, one might have thought (see §3.1) that it was valid to use Rutherford scattering cross-sections for 1.5 MeV \(^4\)He beams because the Coulomb barrier prevents nuclear effects on the cross-section. But this is not the reason, as is shown by Fig. 8 and many other data besides. RBS is valid simply because nuclear tunnelling effects are small. The question of how small they are, and where exactly the boundary lies between effectively Rutherford and measurably non-Rutherford elastic scattering, is still an open question even though much systematic work has been done on measuring the elastic backscattering (EBS) cross-sections in the last decade or so. This work was coordinated by the International Atomic Energy Agency (the IAEA), and was aimed at creating a reliable elastic scattering cross-section database.\(^{122}\)

Fig. 9 shows results of this IAEA-sponsored work for protons, and summarises the current rather incomplete knowledge of the Rutherford/non-Rutherford “boundary”. It shows that there remain substantial gaps in the data with some isotopes unmeasured and some measurements not extending to low enough energies. It also shows that there are no easy approximations (such as the “optical model”) that give reliable general estimates of the boundary position, not even for the apparently undemanding “4%” criterion — it is only in the...
absence of any other information that this “optical model” may sometimes be a useful indicator. The optical model almost always substantially overestimates the boundary energy since it ignores the effect of resonances on the scattering.

In Fig. 9 the “boundary” is defined as a 4% deviation from Rutherford. A comparable figure for a 1% deviation is not yet possible to draw since, as Fig. 8 shows, the effect of nuclear structure below the Coulomb barrier cannot yet be reliably modelled in the absence of experimental data. Thus, at present we cannot achieve “1% RBS” for a proton beam using the methods of §3.1 above.

Whereas Fig. 9 is for protons, for alphas (with a much higher Coulomb barrier) the Rutherford regime is both larger and better defined. But Fig. 10 shows that nuclear structure can also be probed with alphas at energies easily accessible with a 2 MV tandem accelerator. In particular, there is a very strong resonance at about 3.7 MeV for elastic scattering from nitrogen, where the cross-section is up to 9 times Rutherford: this is often used for extra sensitivity to N.

Fig. 10 shows that EBS cross-sections can be very strong – and apparently arbitrary – functions of both beam energy and scattering angle. As for the electron mean free path in XPS (see §2.1), these cannot be calculated sufficiently accurately for analytical purposes by the theoretical physicists, and there is at present no reasonable prospect that they will be calculable, even in the medium term. These data must be measured! But from an analytical point of view, measuring this sort of function is a nightmare since repeated measurements with slightly different parameters can give wildly different values, which are completely unpredictable in the absence of a model.

What has changed in this century is the steady increase in the availability of “evaluated” cross-section functions, now available on the “SigmaCalc” website (http://sigmacalc.iate. obnisk.ru/)125. Since there already exists a very well articulated theory of nuclear interactions it is “straightforward” (for skilled nuclear physicists) to specify a nuclear model accounting for the observed cross-sections. The nuclear model used for the evaluation shown in Fig. 10 is widely agreed (see Bailey et al.126): such models have many parameters, as can be seen from the case of $^{28}\text{Si}(\alpha,\alpha)^{28}\text{Si}$ reaction (involving the $^{28}\text{Si}$ compound nucleus, see Table 2).127 What is interesting is that constructing a detailed nuclear model sufficiently accurate for analytical purposes usually cannot be done from the existing, potential scattering was calculated by Gurbich (2014) with a Saxon-Woods real potential well requiring additional parameters; the “hard sphere” approximation was not used. The table shows only the parameters for the Breit-Wigner resonances. $E_{lab}$ is the energy of the resonance in the laboratory frame. $E_x$ is the excitation energy of the compound nucleus. $j^\pi$ is the spin quantum number and the parity. $\Gamma$ is the total resonance strength. NPA1990: Endt, Nuclear Physics A (1990);121 NDS2011: Ouellet & Singh, Nuclear Data Sheets (2011)122 relies entirely on Källman, Zeitschrift für Physik A (1996);123 Surrey: Gurbich & Jeynes, Nuclear Data Sheets (2014).127

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apparently comprehensive, compilations of nuclear data. In the $^{28}$Si + $\alpha$ case initial data taken from the literature (regarded as authoritative: see Table 2) were significantly changed quantitatively – and even qualitatively in the assignment of quantum numbers – in the effort to accurately fit the observed cross-section data.

Many nuclear model calculations of such low energy data are today done by the astrophysicists (see Fig. 8) who are interested only in estimates of total cross-sections (that is, integrated over all scattering angles). Analysts on the other hand, are interested in accurate values for differential cross-sections (that is, for specific scattering angles). Dramatic and continuing advances in the availability of evaluated cross-sections of sufficient accuracy for analytical purposes are well appreciated from the 2010 review of Gurbich,\textsuperscript{128} and the summary of the IAEA CRP.\textsuperscript{122,129}

It is clear from Fig. 8 that accuracy is needed for astrophysical calculations to allow extrapolation to the interesting low energy region where measurement is very difficult (since the cross-sections are so small). The “R-matrix” formalism for calculating the resonance part of the reaction cross-section can be adapted successfully to also account for the potential part (using the AZURE code\textsuperscript{130}) even though this is rather arbitrary from a physical point of view: AZURE was not used for Fig. 10 where the potential scattering was calculated in a physically realistic approach, and separately from the resonance scattering (for which a pure R-matrix model was used).

Since fluorine is ubiquitous but notoriously hard to analyse by other methods, the proton-fluorine nuclear reactions are important. But accurate IBA is difficult because so many channels are open at the same time, with $^{19}$F, $^{16}$O and $^{20}$Ne as potential final states. As a multi-channel code, AZURE has been found useful to calculate these cross-sections,\textsuperscript{134} although these preliminary calculations have so far served only to highlight experimental discrepancies.

Turning from the cross-sections in themselves to their use, Fig. 11 shows a far-reaching example of EBS. We indicated the importance of calibrations above (§3.1.3): this very simple sample can establish both the spectrometer gain (together with its non-linearity) and the accelerator terminal voltage. RBS spectra are exactly self-similar as the beam energy changes, provided the (slow) variation of energy-loss with energy and the spectrometer non-linearity are neglected – both rather small effects. But an EBS spectrum is very sensitive to beam energy where a sharp resonance is excited. In this case there is a strong resonance only 10 keV wide for the $^{16}$O$(\alpha,\alpha)^{16}$O reaction at 3038.1 ± 1.3 keV which we have used to determine the terminal voltage. We also have independently established this reference energy,\textsuperscript{93} and shown it is consistent with the nuclear physics compilations.\textsuperscript{135}

### 3.4 Spectrometry Software for IBA

#### 3.4.1 Atomic and nuclear IBA methods strongly complementary

It has always been clear that RBS and PIXE were strongly complementary (see Table 3). Nevertheless, IBA was historically split between the thin film (essentially RBS) and the chemistry (PIXE) communities. Partly this was because there were important subsets of samples which were adequately treated by the separate techniques. But mostly it was because the software for the atomic and nuclear techniques was completely different, based on different physics and used in a markedly different way. And integrated software was not available.

In this section we first explain the different codes, emphasising the startling improvements in the last few years. We then describe the – equally startling – recent advances in integrating the atomic and nuclear methods.

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**Table 3 Complementarity of RBS and PIXE**

<table>
<thead>
<tr>
<th>Quality</th>
<th>Strong</th>
<th>Weak</th>
</tr>
</thead>
<tbody>
<tr>
<td>Depth resolution</td>
<td>RBS: direct from energy loss</td>
<td>PIXE: weak indirect (integral) effect</td>
</tr>
<tr>
<td>Quantification</td>
<td>RBS: analytical, standard-less: readily traceable accuracy to 1%</td>
<td>PIXE: fundamental parameters (~10%), but best accuracy from sample-matched standards</td>
</tr>
<tr>
<td>Sensitivity</td>
<td>PIXE: typically a few mg kg(^{-1})</td>
<td>RBS: poor signal/noise due to overlaps</td>
</tr>
<tr>
<td>Mass resolution</td>
<td>PIXE: spectroscopic technique</td>
<td>RBS: smaller kinematical separation for higher masses, all signals overlap at depth</td>
</tr>
</tbody>
</table>
3.4.2 Atomic IBA codes (PIXE). There are two main production codes for PIXE used today, and both have been vigorously developed recently. GUPiX\textsuperscript{136} (the PIXE program from Guelph) was modified for use on Mars to handle joint PIXE/XRF data (see §3.2), underlining the commonality between these two techniques.

GeoPIXE\textsuperscript{137} (the PIXE program from Melbourne) is designed for mapping geological samples and is now also used not only for PIXE but also for sy-XRF (with “Maia”, a large-solid-angle detector array), again underlining the PIXE/XRF commonality. There are an important pair of recent papers on fluid inclusions (very important indicators of the richness of deposits to the economic geologists), the first by PIXE\textsuperscript{138} and the second by sy-XRF\textsuperscript{139} both using GeoPIXE.

Note that in the standard case IBA is richer (and therefore intrinsically superior) to XRF (see §3.2).

We should point out that the Monte Carlo GEANT\textsuperscript{140,141} (“GEometry ANd Tracking”) code developed by CERN is widely used, and not only in the accelerator community: this now also has a PIXE module.\textsuperscript{142}

We should also mention that there is also an entirely independent multilayer PIXE code from Lisbon\textsuperscript{143} that has now been incorporated in the nuclear IBA code DataFurnace (see §3.4.4) and is still under vigorous development.\textsuperscript{144}

3.4.3 Nuclear IBA codes (RBS, EBS, ERD, NRA, PIGE). Two analytical codes for nuclear reactions (including elastic scattering) were announced in 1997 and have since been continued in continuous development. SIMNRA\textsuperscript{145,146} is a well-supported\textsuperscript{147} simulation and fitting program (from München) and is very widely used, including in the Joint European Torus (JET) programme\textsuperscript{148,149}.

DataFurnace\textsuperscript{1,151} is a fitting and simulation program (from Guildford & Lisbon), also well-supported\textsuperscript{150} and with a very wide applicability, including to the JET programme\textsuperscript{149} (see §4.5 and Fig. 21, and also Fig. 1, 4, 6, 11 for other examples). These two independent codes (SIMNRA and DataFurnace) have been systematically validated against each other and against other IBA codes in an IAEA-sponsored Intercomparison exercise,\textsuperscript{152,153} which identifies these two as the “New Generation Codes”. In particular, they agree with each other to better than 0.2% for RBS, with this difference being largely due to rounding errors in the numerical integrations. This could be improved if further advances in the technique accuracy and precision (see §3.1) make it worthwhile. Note that this agreement is not trivial since even RBS, the simplest analytical method, has much subtlety at second and third order.\textsuperscript{7,92} This is exemplified by Fig. 12 which shows not only that excellent depth resolution is available in the surface 20 nm or so but also that even rather complicated spectra are understood in great detail (Fig. 1 tells the same story!)

Fig. 12 shows that it is a good approximation to assume single scattering: that is, the incident particle is assumed to travel unperturbed into the material to the reaction site where it scatters off a target atom, and then to travel back out of the material also unperturbed until it exits the material and enters the detector. Thus RBS is qualitatively different from electron backscattering which is used systematically on the SEM for Z-contrast, but which cannot be treated quantitatively due to the intractability of the multiple scattering. But for RBS, even in glancing incidence ($\theta = 5^\circ$ in Fig. 12), the single scattering approximation is fairly close to reality, with multiple and double scattering (MS & DS) being second order effects adequately accounted for by analytical approximations. On the other hand, single scattering is no longer a good first approximation for Heavy-Ion Elastic Recoil Detection (HI-ERD) since the MS and DS effects are now large. These can be effectively handled only by Monte Carlo codes, and HI-ERD is now well supported by such a code: CORTEO\textsuperscript{154} is a new code from Montréal with a good user interface, making HI-ERD accessible to analysts (see §3.5).

3.4.4 Synergistic codes. Table 3 underlines the strong complementarity of RBS & PIXE, but it is only quite recently that a single code integrated the nuclear and atomic methods: DataFurnace incorporated a full multilayer PIXE code in 2006,\textsuperscript{155} where it is the PIXE characteristic line areas (rather than the PIXE spectra themselves) that are fitted. The line areas are obtained from the energy spectra in a pre-processing step using GUPiX (or other convenient PIXE code). This demonstrated the first fully synergistic analysis.\textsuperscript{156} We will show several examples later (§4).

Fig. 1 shows a heavy contaminant in the optical multilayer: it is known that Hf is always present with Zr, and Hf fits the observed signal. But PIXE would have positively identified Hf spectroscopically. Again, in Fig. 11 the Ni signal looks strange: it cannot be fitted convincingly with pure Ni. But the PIXE shows that Cu is also present. In these cases we need only the element identification from PIXE, but the PIXE signal is also very well fitted, thus providing an independent confirmation.
that the interpretation of the data is correct. Grime’s OMDAQ code from Oxford157 did this in 1995, using GUPIX for the PIXE data with layer thickness information supplied to GUPIX from a simplified EBS code (see §4.4.2).

Of course, PIXE data on their own are always highly ambiguous for samples not homogeneous in depth (and the same applies to XRF, EPMA and comparable techniques). It should be easy to see that PIXE and RBS spectra can interpret each other so that the depth profile can be obtained from a synergistic analysis where the problem would be intractable if the data were treated separately. We demonstrate that in detail below (§4).

DataFurnace was designed to handle multiple spectra self-consistently, it was always used for multiple detectors, multiple beams and multiple techniques so it was easy to add a PIXE module. SIMNRA was designed to handle only single spectra so a self-consistent analysis of multiple spectra (of any sort) was always troublesome. But this problem has now started to be addressed in a fundamental way (“MultiSIMNRA” from Silva et al.158), although a PIXE module is not yet available.

We should also mention the very new open-source “Virtual IBA lab” (VIBA),159 which is a modular simulation program for PIXE, RBS and other techniques as more modules become available. MultiSIMNRA may well incorporate the PIXE module of VIBA in the future.

Lastly, we point out that with a scanning microbeam the lateral imaging has a spatial resolution given by the ion spot size (deep sub-micron160) and that consequently tomographic methods should give the full 3-D sample composition reconstruction. Tomography seems slightly outside our scope, but it is central in the use of the scanning microbeam and this will be discussed later (§3.8).

3.5 Heavy-ion elastic recoil detection (HI-ERD)

Detection of the elastic recoils in the scattering process has the great advantage that the mass overlaps intrinsic to RBS spectra can largely be avoided. This is because, where in RBS the detected backscattered particles are all necessarily scattered out of the primary incident beam and therefore distinguishable only by their energy (resulting in the mass-depth ambiguity discussed in §3.9), in ERD the detected particles are recoiled from the sample, and can therefore in principle be sorted by mass. Even though exactly the same scattering process is in view, ERD and RBS are qualitatively different since the purpose of the ERD detector is to distinguish the different atoms recoiled out of the sample (and to discriminate the primary scattered beam), where in contrast the RBS detector only sees backscattered primary ions.

Classical ERD uses a so-called “range foil” to stop the scattered (high intensity) primary beam161 while being transparent to high energy recoils; a single simple detector sufficed to energy-analyse the recoils. This arrangement has several disadvantages: the range foil necessarily degrades the available depth resolution; the various recoil signals for different masses usually overlap in the simple energy spectrum, degrad-

ing the signal/noise; and heavy recoils rapidly damage silicon detectors. However, it does have the enormous advantage of great simplicity, and if it is only sensitivity to hydrogen that is required a standard helium beam can be used (simultaneously with RBS162). In this case only hydrogen isotope recoils have the energy to penetrate the range foil, so the standard silicon detector may be used without damage and there is no signal/noise problem. This simple method remains important because hydrogen is otherwise difficult to depth profile quantitatively, and because it is very easy to combine with standard RBS.

However, over the last few years great advances have been made in the instrumentation of more complex detectors able to analyse recoils for mass as well as energy. Fig. 13 shows an example of Kr-ERD compared directly to He-RBS. This explains the dramatic contrast between ERD (Fig. 13a) and RBS (Fig. 13c) in the raw data collected: He-RBS is the energy spectrum of the backscattered ions where the Kr-ERD is a set of energy spectra for each of the recoiled masses, and in this case the (forward) scattered ion is also seen. Of course, there is no Mo recoil signal since it is kinematically forbidden into this recoil angle, but the Mo content is obtained from the scattered primary Kr signal just as for RBS.

The great virtues of time-of-flight ERD [ToF-ERD] are the high sensitivity to low-Z contaminants, and also, for relatively low energy primary beams, a very high depth resolution (~1 nm)163 which is improved for slower beams since it depends on time resolution. But it therefore depends on a reliable energy detector sensitive to these slow ions. The thin window gas ionisation chambers which have only recently become available (§3.6) are a notable detector breakthrough for this application.166

HI-ERD has a high depth resolution because a glancing geometry is used and because the energy loss for heavy ions is high. So ERD is valuable for atomic layer deposition (ALD) among many other applications. Uniform conformal films with excellent thickness controllability can be grown by ALD. As one example, iridium metal is used in optics (Fresnel zone and microchannel plates) and its oxide is biocompatible and also used as an electrode for pH measurement: Ir and IrO2 ALD films between 20 and 50 nm thick were characterised by 8.5 MeV Cl-ERD to directly obtain the Ir/O ratio and the C & H contamination.167 In another example, Nb2O5 (a wide bandgap dielectric material with high permittivity and high refractive index) is an interesting material with a wide range of potential applications: sufficiently high purity of ~40 nm ALD films of this oxide deposited from three different precursor materials was demonstrated by 6.8 MeV Cl-ERD168 where the required smoothness was determined by atomic force microscopy (AFM). In yet another example, efficient and manufacturable photocathode-chemical cells used a heterostucture of nickel and iron oxides that was depth profiled using XPS and 12 MeV I-ERD.169

3.6 Gas ionisation detectors of energetic particles

The energy loss methods such as RBS with proton or alpha beams have been so powerful because good energy resolution
was available using silicon diode detectors. Even cheap photodetector devices work very reliably with a pretty good performance. However, as soon as heavier ions are to be detected the energy resolution becomes quite poor, and the beam rapidly damages the detector, precluding routine analysis.

Gas ionisation chambers (GICs) are very well known and widely used as particle detectors: their limitation for the measurement of the energy of fast particles is that the particles have to enter the detector (with its special working gas) through a gas-tight window in which the particles cannot avoid losing energy. The great recent advance is that ultra-strong ultra-thin silicon nitride windows are now available, meaning that these detectors can now be used with high energy resolution for relatively low energy beams.\(^{170}\) And their enormous advantage is that there is no beam damage; this is already very valuable both for HI-ERD (see §3.5) and for STIM (see §3.8). They are also insensitive to light and can have fairly high counting rates which may prove valuable for operando methods (see §3.7).

GICs can be used with more or less complex internal electrode structures to obtain both the mass of the particle (from the spatial distribution of the ionisation) and its entrance position (from the ionisation asymmetry).\(^ {171}\) The former means that the GIC by itself can work effectively to discriminate particle mass (essential in a recoil measurement): time of flight (ToF) methods are not required. The latter means that large solid angle detectors can be used without degrading the energy resolution since internal kinematical corrections can be applied.

However, it turns out that for backscattering of particles with relatively low energies, the GICs can be heavily simplified by eliminating most of the internal electrode structure with almost no performance penalty.\(^ {172}\) For higher energy particles more attention must be paid to the flow of charge through the detector to the charge collection anode and a more complex electrode structure to shape the field is needed, together with a Frisch grid to improve the charge collection efficiency.\(^ {172}\) But the new methods have been used to demonstrate a large solid angle annular backscattering detector which works equally well for heavy and light ion backscattering.\(^ {174}\)

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**Fig. 13** Heavy-ion ERD analysis of a (Cr,Mo)O\(_2\) coating on Si. (a) Time-of-flight (ToF) ERD plot using 27.5 MeV \(^{84}\)Kr\(^{15+}\) primary beam incident at 15° grazing angle with the ToF telescope at a recoil (or scattering) angle of 30°. (b) Mass discriminated energy spectra from ToF ERD detector: the raw data (a) are projected onto the X-axis. (c) RBS spectrum with primary beam of 2 MeV \(^4\)He\(^{1+}\) in normal incidence, with the detector at 160° scattering angle. (d) Depth profile derived from the Hi-ERD data using CORTEO (§3.4.3). The (Cr,Mo)O\(_2\) film has thickness \(\sim2500\) TFU or \(\sim240\) nm. See Fig. 11 for “TFU”. Reprinted from Mater. Charact., 70 (Fig. 2, 4, 5, 7 of Khamlich et al., Compositional analysis and depth profiling of thin film CrO\(_2\) by heavy ion ERDA and standard RBS: a comparison, 42–47, ©2012),\(^ {164}\) with permission from Elsevier.
3.7 “Operando” methods and high volume quantitative analysis

Remarkable recent work that highlights novel and powerful ways of exploring systems with complex chemistry is shown in Fig. 14. Nickel silicides are widely used in making electrical contact to complementary metal–oxide–semiconductor (CMOS) devices in the advanced integrated circuits ubiquitous today. They have been the preferred contacting material since the 2006 "65 nm technology node", partly because of a self-aligned-silicide ("SALICIDE")\textsuperscript{175} process is available. However, their high temperature behaviour is complex and, crucially, improved by the presence of platinum.

Seminal information on the influence of the Pt in limiting the formation of the undesirable Ni$_3$Si phase during annealing was obtained kinetically in 2008 using real-time RBS\textsuperscript{176} (Fig. 14), where the very large quantity of data resulting is analysed in real-time by an artificial neural network (ANN)\textsuperscript{177}.

The Ni : Pt/Si system is very complex: the presence of Pt has intricate effects on the interplay between the two phases, Ni$_3$Si and NiSi, as is clear from the operando observation of the complete silicidation process (Fig. 14a), a single spectrum from which is shown in Fig. 14b where the segregation of Pt out of the di-nickel silicide and the onset of the formation of the monosilicide can be seen. Further work by Demeulemeester et al.\textsuperscript{178} on this important system has shown the sensitivity to the Pt content. They successfully applied real-time RBS (using ANNs) to disentangle the growth kinetics during the complex growth of Ni(Pt) silicides and showed that activation energies can be extracted from a single ramped real-time RBS measurement (see Fig. 14c).

Complementary work on the same system has included real-time X-ray diffraction\textsuperscript{179} (XRD) and atom probe tomography\textsuperscript{180} (APT). RBS allows the phase formation and the redistribution to be followed in situ and thus gives crucial information of the different steps of the redistribution. But RBS has relatively poor depth resolution and, for these nanocrystalline materials, effectively no lateral resolution. APT is a very high resolution (ex situ) tomographic method giving highly detailed structural information. Similar to the complementarity between RBS and TEM, operando RBS gives a (rather detailed) broad overview of the entire process, where APT follows inhomogeneities at the nano-crystalline level.

We should point out that although the spectra in Fig. 14 are fairly simple, they still have a number of intrincacies, including sample layer inhomogeneity (which are handled in quite a sophisticated way – see Fig. 12 or 16 for example). But the use of ANNs is not limited to these “simple” cases, or even to RBS. Energy-loss spectrometry (including RBS, EBS, ERD, NRA) is mathematically an “ill-posed” problem\textsuperscript{3} and this has meant that it has been remarkably difficult to automate. But this work shows that indeed certain sorts of problems can be automated, with the analytical difficulty now being transposed to constructing the proper training and test sets for the ANN. Barradas et al. long ago proposed “RBS without humans”\textsuperscript{181,182} policy makers should note that this proposal has now been very well substantiated and that, for a reasonably well-defined application, the marginal cost per analysed spectrum of high-volume IBA can be very low.

We should also point out parenthetically that this work is limited as it stands to only about 600 °C annealing temperatures since semiconductor detectors are light-sensitive, but much higher temperatures could be implemented directly with the gas ionisation detectors (see §3.6).

This is an important example, but only one of many quantitative operando RBS\textsuperscript{183} observations of diffusion and phase separation during annealing of multilayer samples. What is qualitatively different here is the use of ANNs to handle quantitatively the huge datasets produced. Operando measurements can be extraordinarily efficient; indeed, readily giving details of processes that are hard (or impossible) to obtain conventionally. In situ RBS is an obvious (and old!) technique: see

Fig. 14  Real-time RBS of silicidation of Ni(Pt) thin films. Left (2008 data): contour-plot representation of 125 He-RBS spectra acquired at 2 MeV from a 75 nm layer of Ni: 3%Pt sputter-deposited on Si and annealed at 2 °C min$^{-1}$ (colour coded counts per channel). For the thick black line at 375 °C, see Centre (2008 data): 2 minute spectrum obtained at 375 °C. Right (2013 data): Activation energy data for formation of the monosilicide for five initial Ni(Pt) film compositions. These data were obtained by single ramped anneals (2 °C min$^{-1}$) with operando RBS (2 min spectra reduced by artificial neural network) for each case. Below 2 atomic% Pt the activation energy is 1.5 eV, above it is 3 eV. The same values are obtained for ramp rates of 1 °C min$^{-1}$. Reprinted from Fig. 2 & 3 of Demeulemeester et al., Appl. Phys. Lett., 2008, 93\textsuperscript{176} and Fig. 6 of Demeulemeester et al., J. Appl. Phys., 2013, 113,\textsuperscript{178} with the permission of AIP Publishing.
for example Averback et al. on the radiation-induced segregation of nickel–silicon alloys, or Rennie et al. for the photodissolution of silver in chalcogenide glasses.

In situ IBA can even be used at the liquid–solid interface using an external beam (see §4.7 for cultural heritage applications of this). In situ electrochemical RBS was first published by Kötz et al. – both RBS and NRA still remain of interest and a general patent was published in 2014.

3.8 Imaging and tomography

We shall highlight the great value in fully quantitative analysis at a high lateral resolution (see §§4.6 and 4.7) and we have already mentioned this in the comparison of μ-XRF and μ-IBA above (§3.2). Le Trequesser et al. also make a similar point in their recent work on gold nanoparticles.

Tomography is now a very well-established technology with X-ray density tomography being widely available (an example is shown in Fig. 23g). Tomography is a 3-D technique that presupposes a 2-D imaging capability, which for the ion and electron beam techniques is usually determined by the probing beam spot size. For MeV ion beams the available ion sources are not very bright, and also the magnetic quadrupole lens aberrations are substantial: it has consequently proved difficult to reduce the spot size below the 1 μm achieved in the 1980s. However, in the last decade or so this had renewed attention and significant improvements in ion source brightness have been obtained.

Fig. 15 shows the best high resolution imaging currently possible with IBA methods. A cancer cell which has been cultured with gold nanoparticles (GNPs) is being imaged with scanning transmission ion microscopy (STIM) using a 1.6 MeV alpha particle (‘He’2+) beam focussed to 25 nm. “STIM” sounds similar to “STEM” (scanning transmission electron microscopy) but the image is formed entirely differently. It is more analogous to EELS (see Table 1) in that the energy loss of the ion through the material is being imaged, but EELS is a spectroscopy where the characteristic elemental edges are imaged (see Fig. 23d for an example) where STIM is a spectrometry with the energy loss being a proxy for density. This is exactly analogous to X-ray radiography, and the X-ray computed tomography techniques now standard and widespread are equally applicable to STIM. And indeed STIM tomography (STIM-T) has been used in earnest for fusion targets (on which see also §4.5).

STIM is almost entirely non-destructive: since it is a technique that analyses the energy loss of every transmitted par-

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**Fig. 15** 1.6 MeV He2+ STIM image of HeLa cell cultured with GNPs. STIM: “scanning transmission ion microscopy”; FSTIM: “forward (off-axis) STIM”; GNP: “gold nanoparticle”; HeLa: immortal cancer cell line cultured from Henrietta Lacks, who died in 1951. STIM beam is focussed to 25 nm. RBS beam is focussed to ~250 nm. See text. (a) (Top Left): STIM. Colour scale indicates energy loss. (b) (Bottom Left): FSTIM. Colour scale indicates probability of scattering into a large angle. (c) (Right): FSTIM with the GNPs colour coded for depth from the RBS signal. Reprinted from Biophys. J., 104 (Fig. 4b, 5b, 8 of Chen et al., High-resolution 3D imaging and quantification of gold nanoparticles in a whole cell using scanning transmission ion microscopy, 1419–1425, ©2013), with permission from Elsevier.
ticle only a very few particles are needed (a few thousand per second: \( \sim nA \)). But for microbeam RBS or PIXE a larger beam current is required (\( \sim nA \)), necessitating a larger object aperture which results in an order of magnitude larger spot size. For all focussed ion beams, a high imaging resolution will be controlled by the ion source brightness since a higher brightness allows a smaller object aperture for the same beam current.\(^{194}\)

In Fig. 15 we see a combination of techniques: Fig. 15a is classical STIM where the image contrast is most easily understood as representing thickness (with high energy loss due to large sample thickness). This is a well-known technique that was used long ago in conjunction with PIXE imaging in a study of Alzheimers neural plaques\(^{195} \) (as just one influential example). Fig. 15b is dark-field (‘off-axis’) STIM\(^{196} \) where the scattering (rather than merely the energy loss) is imaged. This is analogous to the backscattered electron detector in the SEM, which is sensitive to atomic number: Fig. 15b is imaging the GNPs in the cell. Trouble is, we need to distinguish between GNPs inside and outside the cell (the latter are also clearly seen in the top right of Fig. 15b). STIM cannot do this but RBS can: for STIM the energy loss is integrated along the particle path and there is no depth contrast whereas for the (large) RBS beam we look (at lower spatial resolution) for the depth of the GNPs in the cell, which is colour-coded in Fig. 15c.

In Fig. 15 the GNPs cannot unambiguously be identified as gold from the data unless the characteristic X-rays are also collected (PIXE). Clearly, where the RBS signal is collected the PIXE can be too: in this case the PIXE does not carry any information from the whole primary beam path and the whole X-ray path to the detector. To do the ZAF correction all of the elemental composition needs to be known, and they are not independent of each other! However, after much effort PIXE-T is now also a solved problem:\(^{199} \) it has been demonstrated for hair\(^{199} \) (and other targets too: see the useful review of STIM-T and PIXE-T by Michelet\(^ {200} \)).

The trouble with PIXE-T is that it is very damaging, and only rather robust samples can survive the many slices required.\(^ {201} \) We should mention that although simple tomography theory calls for a very large number of slices there are various mathematical ways of dramatically reducing this number and consequently reducing the analysis time (together with sample damage)\(^ {202} \) including maximum likelihood methods.\(^ {203} \) Again, Fig. 15 is interesting. The GNPs were located in depth not indirectly by the usual computed tomography methods but directly by RBS.

This example seems to imply a much more efficient method for Total-IBA tomography (Total-IBA-T: another example is discussed in §4.6 and elaborated in Jeynes et al.\(^ {1} \)). In such a method initial STIM-T would give the 3-D density non-destructively at high spatial resolution, and subsequent Total-IBA (PIXE + EBS) would give the (lower resolution) 3-D elemental composition with far fewer slices than required for PIXE alone since the backscattering signal relieves so much of the depth ambiguity of the PIXE. However, at present Total-IBA-T remains an unsolved problem.

Another approach to the damage problem has a different context. PIXE-T has also been demonstrated for an “animal-sized” model system by Bazalowa-Carter et al.\(^ {204} \) who use 200 MeV protons for penetration of large targets. They point out that sufficient contrast could be obtained for imaging of GNPs (for example) during clinical irradiations for proton radiotherapy, which has become topical.\(^ {205} \)

### 3.9 Estimating the uncertainty of IBA depth profiles

Depth profiling of a thin film sample by nuclear scattering methods depends on a depth scale given by the electronic energy loss of the incident and detected particles in the sample. Because sample composition information is convoluted with depth profile information in the energy spectra of the detected particles, the inversion of the data to yield the depth profile is an ill-posed mathematical problem. By contrast, the composition – but not the depth profile, which has to be assumed – can be extracted analytically from PIXE (or XRF) spectra.

There are general mathematical ways to directly solve such ill-posed problems, the IBA case was solved by Kogan et al.\(^ {206} \) using Pytev's\(^ {2} \) reduction method generalized for this nonlinear problem. Unfortunately, this promising approach has not yet been taken up by the community, but Bayesian methods have since been introduced systematically in different ways by both the leading codes (see §3.4.3), either of which allow a general approach to the estimation of uncertainties on the depth profiles extracted from the data.

Maximum Entropy (MaxEnt) methods were used by Fischer et al.\(^ {208} \) to improve the effective energy resolution by a factor of about 6 through deconvolving the instrumental function, comparable methods were subsequently used to obtain most probable depth profiles.\(^ {209} \) This approach has proved both very computationally intensive, and also cumbersome since it requires detailed knowledge of the instrumental function which is inconveniently unstable. However, Schmid & von Toussaint\(^ {210} \) have used similar methods to obtain statistically sound estimates of uncertainties of depth profiles for nuclear fusion applications\(^ {211} \) (see §4.3).

Simulated annealing\(^ {212} \) was introduced in 1997 \(^ {151} \) to obtain depth profiles by inverting the RBS spectra; this naturally introduces the Markov-chain Monte Carlo (MCMC) methods used in a Bayesian treatment that allow statistically robust estimates of the depth profile uncertainties to be obtained.\(^ {213} \) Dose\(^ {214} \) points out that Bayesian methods are useful for all spectrometries, although they are especially useful where the problem is mathematically ill-posed since there are few good alternatives. They have been extensively used: by James et al.\(^ {215} \) to determine the uncertainty of polymer diffusion coefficients (see §4.4); and by Jeynes et al.\(^ {2} \) (see Fig. 1) and Barradas et al.\(^ {216} \) (see §4.2) to determine layer
thickness uncertainties in respectively optical multilayers and SiGe superlattices. It is interesting to note that the same mathematical methods can be used on similar data to extract stopping power data or even differential scattering cross-sections.

IBA data can be ambiguous: this was discussed at length in the review by Jeynes et al. For RBS the ambiguity comes from the overlap of signals: any particular count could be from a heavy atom deep in the target or a light element close to the surface. There are standard ways of eliminating most (if not all) this ambiguity: in Fig. 1 for example we show only one spectrum with the primary beam normal to the sample, but a second was collected with the primary beam at 45° to the target resulting in a spectrum with a markedly different shape (see Jeynes et al.). Ambiguity is greatly reduced, but the remnant can be eliminated only by imposing chemical assumptions. In these data O is a small signal with a large background: we impose the assumption that the layer is fully oxidised (that is, it is a zirconia/silica multilayer). Of course, this assumption is fully justified by the optical behaviour of the film. In this early work the fits were only obtained by allowing intermixing of the layers (excluded by the optical properties!), but the same fit quality would be obtained by modelling roughness effects, as for Fig. 12 and 16.

Fitting data sets is done in most cases by simply minimising a \( \chi^2 \) function: multiple spectra each contribute a part of the value and these can be from different detectors (which may be using different techniques) or different data collection runs (different beam or beam energies or geometries). Energy loss spectra are well suited to this treatment since the spectra are histograms with Poisson statistics. However, any “objective function” that represents goodness of fit can be used, and in some cases this is desirable since the \( \chi^2 \) function has some problems. In particular it is unstable for poor fits (with large outlier values), and Dose & von Toussaint have pointed out that there are some rather elegant solutions to this.

Another standard statistical approach is to use “robustification” where the objective function morphs from \( \chi^2 \) to a \( \ln(\chi^2) \) function (for example) as the fit gets poorer. We have found this robustification approach useful for “Total-IBA” with PIXE data because the areas of the characteristic lines that are the input data are neither histogram data nor subject to Poisson statistics. In principle, treating the contribution to the \( \chi^2 \) function from the non-Poisson non-histogram PIXE data

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Fig. 16 High-resolution RBS of a (Re, Co) superlattice on glass. Glancing incidence RBS at 10°, 8°, 7°, 6° to surface, with detector (in “Cornell” geometry) at a backscattering angle of 160°. See text for red arrows. Sample: Glass substrate/Re(5 nm)/[Co(2.3 nm)/Re(0.5 nm)]15. The Co and Re elemental edges are labelled. Inset: 45° spectrum (courtesy of N. P. Barradas) showing the sample structure including the 5 nm Re interlayer. For the spectra collected at 7° and 6°, the simulated curves calculated for a deformed substrate (dotted line) or a rough substrate (solid line) are shown (see text for details). Reprinted from Nucl. Instrum. Methods Phys. Res., Sect. B, 190 (Fig. 1 of Barradas, Fitting of RBS data including roughness: application to Co/Re multilayers, 247–251, ©2002), with permission from Elsevier.
uniformly with that from the nuclear scattering data is not mathematically valid: in practice it usually works quite well. But it works better if a robustified $\chi^2$ function is used.

4 Quantitative depth profiling: IBA as a reference method

4.1 Introduction: synergy in IBA

In this section we draw together all the threads: many analysts have heard of RBS and many have heard of PIXE but this Review has the purpose of informing analysts of recent developments in Ion Beam Analysis, an effectively new method where the fast ion beam yields rich information when the various signals are treated synergistically. We refer to this “synergistic IBA”, the combining of multiple techniques, as “Total-IBA”, following Jeynes et al.\(^4\)

In Table 3 (§3.4.1) we pointed out that where the performance of PIXE was weak, that of RBS was strong, and vice versa: here we will elaborate on this, with several detailed examples none of which could have been given even a decade ago. These are selected arbitrarily from many possible examples, and demonstrate the great generality of IBA: it is valuable whenever thin films are depth profiled since it is quick, not deliberately destructive (and beam damage is usually limited), model-free and fully quantitative, and has near-100% mass closure.

The systematic use of PIXE is a key because the mass insensitivity (and ambiguity) of RBS is the very well-known drawback that has limited its use. Another important key is the realisation that even noisy spectra may be very informative. This is significant because PIXE typically has very high X-ray generation cross-sections and is often used (with large solid angle X-ray detectors) in imaging (microbeam) applications for which focussed beam currents are limited. For such analyses the backscattered particle signals are traditionally ignored because (a) the counting rates are usually very low, with very noisy spectra; and (b) the spectra usually look intractable anyway, with strongly non-Rutherford scattering cross-sections.

The massive recent work on evaluated cross-sections (summarised above in §3.3) has completely changed the situation: EBS spectra are now usually tractable. And Barradas et al.\(^213\) showed in 1999 that even very noisy RBS spectra can enable a qualitatively correct interpretation, allowing PIXE spectra of layered samples to be treated fully quantitatively. The PIXE by itself is blind to whether the films are 20, or 2, or 0.2 microns thick: in this case even a 10% uncertainty due to poor counting statistics of the RBS spectrum contributes negligibly to the PIXE uncertainty. This is something the XRF community knows very well: provided something is known about the sample, the XRF (or PIXE) can tell you much. More recent work has underlined that robust information is available even in the presence of 10% Poisson noise.\(^220\)

In this final section we will show a series of examples where the nuclear scattering and atomic excitation data, considered separately, are intractable, but where together they mutually interpret each other: self-consistent IBA (“Total-IBA”) is massively more powerful not only than any of the individual IBA techniques taken separately, but also than even the iterated sequential use of the individual IBA techniques, which even where it is successful is acknowledged to be long, clumsy, and uncertain.\(^221\)

It is now standard practise to collect RBS data with multiple detectors with different geometries to relieve the intrinsic mass-depth ambiguity in the energy-loss spectra. Analysing these multiple spectra self-consistently was first done by Barradas et al.\(^151\) and we have already referred to this (Fig. 1 and 4). Strictly, this is not “Total-IBA” since multiple techniques are not in use, but in practise the analysis code is modular and indifferent to which technique is in use for a particular spectrum. So “Total-IBA” was rapidly introduced in 1999 with RBS + ERD,\(^94\) RBS + NRA,\(^222\) and RBS + EBS + ERD + NRA,\(^223,224\)

It is clear that Total-IBA is an indispensable tool for quantifying the processes involved in creating novel advanced materials, which of course also need a battery of complementary analytical techniques. For example, Shaw et al.\(^225,226\) have synthesised novel porous high strength materials which are promising for energy storage, photovoltaics, and catalysis applications (characterised by nanoimplantation, XRD, SEM, TEM and IBA). They used a process that involved colloidal inorganic nanoparticles manipulated by functionalisation with organic ligands, where the organic material was finally “burnt off” by an oxygen plasma. In this case the IBA was essential to understanding the evolution of the structure during the plasma processing.

In the remainder of this chapter we will first underline how the self-consistent treatment of multiple RBS spectra can be highly informative (§4.2). Then (§4.3) we will explicitly demonstrate how IBA can be used to certify (potential) reference samples in cases that are difficult for alternative methods. §4.4 displays two interesting cases where modern IBA has proved valuable complementary to the big physics facilities: neutron reflectivity at spallation neutron sources and synchrotron X-ray crystallography. §4.5 is an example of an industrial scale analysis, showing that very large numbers of complex samples can be handled effectively with modern techniques. §4.6 shows a “blind” analysis informed by no prior knowledge: this situation is also very frequently found in processed samples where something has gone wrong and the prior knowledge the user thought he had has proven unreliable. We conclude (§4.7) with a celebration of IBA being non-destructive: it can also be used safely and very effectively on valuable and delicate layered samples (such as paintings) using an analysis at atmospheric pressure. Such samples may be rough, and IBA is sensitive to surface roughness – historically neglected but now tractable.

4.2 Self-consistent RBS for ∼1 nm depth resolution

In a Review of IBA depth profiling it would be strange not to underline the very high depth resolution available from rather simple equipment, and here we concentrate on this. However, we should first mention that ultra-high depth resolution is
available by RBS using magnetic spectrometers,\textsuperscript{227,228} which can even be used for liquids;\textsuperscript{229} liquid surfaces can also be analysed successfully by conventional RBS and grazing incidence geometry.\textsuperscript{230} Magnetic spectrometers have a rather small energy window (and consequently are often used in conjunction with other detectors – “Total-IBA” is normal for analysts). For example, to measure ultra-thin bilayers of HfO\(_2\) and Si oxynitride, Kimura et al.\textsuperscript{231} compare angular-resolved XPS with high resolution RBS (400 keV He) and HI-ERD (40 MeV Au), where (different) magnetic spectrometers were used for RBS and ERD.

Energy straggling of the beam degrades the depth resolution for the deeper layers whichever detector is used: this effect is now thoroughly understood\textsuperscript{233} and is obvious in Fig. 16, which shows extraordinary data collected by Barradas\textsuperscript{234} in 1994 but reanalysed in 2002\textsuperscript{232} with the advanced code that handles self-consistent RBS.\textsuperscript{216} In this analysis standard RBS with the usual silicon diode detector of about 15 keV energy resolution is used. The sample was a magnetic multilayer: the period of the superlattice is less than 3 nm and yet the signal from the top few layers is easily discriminated.

The questions to be answered were: (a) is the superlattice subject to substrate roughness, or not? and (b) is the roughness behaviour of a silicon substrate (not shown) different from that of the glass substrate (shown in Fig. 16)? Three models of roughness were considered: (i) random layer thickness non-uniformities (excluded by TEM); (ii) a deformed substrate or (iii) a rough substrate, both with conformal films. The difference between a deformed and a rough substrate (models (ii) and (iii)) is that there is correlation for (iii) but not for (ii). It turns out that in fact the datafavoured model (iii) since the best fit for model (ii) had misfits marked by the red arrows in Fig. 16. These data are fitted with model (iii) parameters of a correlation length \(L\) of the surface asperities and the standard deviation \(\delta x\) of the asperity height distribution.

The high depth resolution RBS data for the superlattices on the two substrates gave fitted roughness parameters of \(L = 38.2\) (39.3) nm and \(\delta x = 0.48\) (0.61) nm for glass (silicon) substrate. The result that the two substrates actually behave differently was confirmed by other data independently: it surely is amazing that standard RBS is capable of such exquisite sensitivity? The alert reader may object that the arrowed “misfits” are barely significant. But note the ordinate scale: a cold view of the Poisson statistics of the data confirms their significance. The various roughness models affect the energy straggling differently, and therefore we expect effects from the surface layer deeper in the sample (in the second and third layers), which is what we see.

We should point out that Fig. 16 is very remarkable: it is not at all trivial to fit four separate spectra simultaneously and so perfectly. All the experimental parameters have to be correct for this sort of accuracy, and moreover the calculation of the intrinsic energy straggling also has to be correct. We have already pointed to this excellent detailed understanding of RBS in the commentary on Fig. 12; this is another notable demonstration of it.

4.3 The reference sample problem

A leading author from one of Europe’s National Metrology Institutes has said: “The quantitation of XRF spectra is, in general, based on the use of appropriate reference materials that are as similar as possible to the sample to be analyzed as the interplay of many often unknown instrumental and fundamental atomic parameters determines the measured element-specific fluorescence countrates in a complex manner”.\textsuperscript{106} This statement is as true of PIXE as it is of XRF. The work of Beckho and co-workers in Berlin to develop and use reference-free XRF (see §3.2 above) is more difficult than for IBA since traceability for nuclear scattering is much easier to establish (see §3.1 above) than for the more complex atomic excitation methods. A recent direct example of this is the characterisation of olivine by IBA to calibrate the IR spectroscopy used in the study.\textsuperscript{235}

For validating routine analysis of course we always want comparisons to a reference sample, which should be similar to the sample set of interest: the question invariably is how to certify the reference? And today, with the explosion of interest in new and complex materials, this question is becoming increasingly acute.

The development of “Total-IBA” that we describe in this Review is complementary to reference-free XRF, and may be a better alternative, as we pointed out in §3.2. In particular, accurate RBS (see §3.1) may provide certified reference materials that can be used for establishing the fundamental parameters on which XRF and PIXE depend.

Accurate RBS may also establish reference materials for particular applications. Fig. 17 shows a case where depth profiling by XPS had produced equivocal results and independent validation was required. This is an interesting case since the RBS spectra have large overlaps of the elemental signals and are therefore not entirely trivial to interpret. Careful analysis of the RBS spectrum for the Cd, Zn and S content showed that the spectrum contained no evidence that the S was not a constant 50 atomic% through the depth profile. Therefore we imposed the chemical assumption that the film was a mixture of monosulfides, obtaining the profile shown in Fig. 17. Note that the similar assumption of full oxidation in Fig. 1 does not have independent support from the data (since the direct O signal is so small) but does have independent support from the optical behaviour (as an anti-reflection coating) of the film.

We used a 3070 keV alpha beam to look for surface oxidation, making use of the \(^{18}\text{O}(\alpha,\gamma)^{20}\text{O}\) resonance at 3038 keV (see §3.3) which gives strongly enhanced sensitivity to O (see Fig. 11). The higher energy beam was also convenient to see the whole film thickness. Oxygen is not detected, but had it been we could have looked for correlations in elemental signals which may have indicated oxidation of one or other of the species present.

There are several advantages of imposing chemical assumptions on the data. The heavy and light element signals
are correlated in the analysis, and also the number of free parameters is reduced: both standard noise-reduction techniques. Then, if the profiles are fitted in terms of compounds (sulfides) rather than elements a realistic linear depth scale (in nm) is readily available, using the bulk sulfide densities (in g cm\(^{-3}\)). Note that the natural thickness unit for energy loss methods is \(\text{TFU}\), since the units of energy loss are eV per \(\text{TFU}\): see Fig. 11 caption for “\(\text{TFU}\)”. This is valuable since the linear film thickness (in nm) can be measured directly with other methods, which then gives information on the actual film density.

Fig. 17 is a good example of a relatively simple coating which could in principle be used as a reference sample for applications work in this mixed sulfide system. The PIXE spectrum shown in Fig. 17 is similar to XRF or EPMA spectra, and is uninterpretable unless the profile is known. But we do know the profile! The RBS gives the profile not only unequivocally but also with rather small uncertainties. Therefore, this is one example where the sample could be certified by RBS, thereby becoming a standard sample for PIXE (or any other technique used), in which case the PIXE (or XRF, XPS, EPMA etc.) can inherit the accuracy of the RBS.

In this case the PIXE was not used to solve the sample structure so that the PIXE simply inherits the accuracy of the RBS. In other cases the PIXE may be needed to solve the structure, and then the RBS would inherit at least some of the uncertainty of the PIXE. In any case a set of detailed Uncertainty Budgets must be constructed separately for each certification analysis.

Fig. 18 is an example of a CIGS (CuInGaSe) sample grown on stainless steel with a Mo electrode (and a thin Cr buffer layer). Such samples are of great current interest for thin film photovoltaic (PV) applications. In this case the RBS is multiply ambiguous because of the systematic elemental overlaps: nevertheless the structure could be unambiguously solved with the addition of the PIXE data. In fact only a selection of the collected (and fitted) data is shown: 15 spectra were used including different beam settings, and different geometries. Bayesian (Markov chain Monte Carlo, \(\text{MCMC}\)) methods\(^{213}\) were used to explore the uncertainty of the results given the input assumptions.

What is interesting is that we can directly compare average IBA with integral XRF results. We obtain CIGS film thickness (assuming 5.8 g cm\(^{-3}\)) for IBA (XRF) of 1860 (1900) nm, and average film composition for IBA and XRF respectively of \((\text{Cu}, \text{In}, \text{Ga}, \text{Se}) = (262, 138, 77, 523)\) and \((219, 133, 90, 558)\). The purpose of the analysis was specifically to obtain the depth profile which of course is unavailable from XRF.

This analysis has fair agreement between XRF and PIXE. Both methods agree that the Se content is greater than 50 at%, but the Ga content (and profile) is determined from the X-ray data and will be sensitive to the details of the X-ray detector calibration: agreement of XRF and PIXE depend on a consistent calibration protocol. This underlines the point made for the mixed sulfide sample (Fig. 17): an IBA analysis that needs the self-consistent PIXE will have an uncertainty partly inherited from the PIXE.

On the other hand, IBA with accurately calibrated PIXE will yield reliable profile information comparable to that available from syn-Gi-XRF and entirely beyond desktop XRF. We therefore expect IBA to be used in future to certify reliable reference samples for desktop XRF.

### 4.4 Polymers and proteins: IBA as a complementary technique

In this section we show two examples of different complementary analysis methods which have made a significant impact in their fields. We will consider IBA used with neutron reflectivity (NR) for polymer interdiffusion measurements, and with synchrotron X-ray crystallography (\(\text{sy-XRX}\)) to determine the structure of proteins. In both cases the advances we sketched in §3 have proved crucial to the value of the IBA contribution.
4.4.1 Polymer mixing. IBA methods have been used systematically to understand the mixing and demixing behaviours of miscible and immiscible polymers; cheap and ubiquitous materials which can very easily be deposited as thin film coatings for an astonishing variety of purposes. Using this understanding, many novel and highly useful types of devices and materials can be made. Plastic electronics is now a huge market, as also is plastic packaging and coating, and we rely on plastic coatings for durability under very testing conditions: it is the polymer chemists who have to deliver this performance.

In all these cases, to understand the complex thermodynamics driving the development of the structure that gives the functional material its desired properties, a materials science approach following and accounting for this structure is required. Many methods are used, as usual in this multi-disciplinary field, but nuclear reaction analysis (NRA) using the \( d(\text{He},p)\alpha \) reaction\(^\text{237} \) together with deuteration of one of the mixing components has been found extraordinarily powerful in combination with neutron reflectivity. The NRA method is useful precisely because the isotopic effect due to deuteration is well understood.\(^\text{238} \)

Fig. 19 shows the depth profile of the deuterated component of a conjugated polymer blend which is successfully used in experimental light emitting diodes (LEDs). In this sort of material the exciton diffusion distance is very small (<10 nm) so that nanostructuring is essential to obtain electronic performance. The NRA depth resolution is about 10 nm, which is not good enough to understand the nanostructuring behaviour: for a high resolution measurement the chemists turn to neutron reflectivity, but NR spectra are multiply ambiguous and it is necessary to know the depth profile at low resolution to relieve this ambiguity. The same methods are used to follow depth profiles of surfactant and plasticiser additives in spin-cast polymer films,\(^\text{239} \) and even to follow nutrient uptake in mycobacteria.\(^\text{240} \)

In another recent example\(^\text{215} \) using the same methods as shown in Fig. 19 (but to understand completely different functional materials), parameters for the surface modification of polyester using incompatible blends of polystyrene additives were obtained. In such cases a surface bilayer is formed with an error function modelling each layer: there are two
characteristic lengths for each layer, the layer thickness and the interfacial width. These parameters are obtained directly from a parameterised fit of multiple NRA spectra collected for different glancing beam incident angles, where the absolute (model-free) depth resolution is comparable to about 10 nm and the information depth extends more than a quarter of a micron. Bayesian techniques (see §3.9) give reliable estimates of the uncertainty of these (parameterised) lengths: in this case the thickness of the surface enriched layer is obtained with a precision of about 1 nm, where the interface width between the surface enriched layer and the depleted layer immediately beneath it is obtained with a precision of about 3 Å.

Of course, the neutron reflectivity (NR) also used in this work has a much higher absolute depth resolution than this but a much lower sensitivity to slow changes in concentration. As before, NR and NRA complement each other almost perfectly.

Straightforward RBS is also powerful where one of the polymers is distinguished by a heavy component. In an example of self-assembled transistor structures, sulfur characterises one component. Another very recent example of self-assembled photonic structures follows the distribution of gold nanoparticles in polymer mixtures.

4.4.2 Protein structure. Structural biology is now central to very wide ranging investigations of gene function and drug discovery, and X-ray crystallography (XRX) is the main tool for determining protein structure. But XRX has some specific limitations: it relies on the electron density deduced from diffraction patterns taken from crystals to identify the presence of metal ions, but cannot in general unambiguously assign the atomic number of the metal or evaluate the stoichiometric ratio of the number of ions present per protein molecule. These metal ions often determine the function of the molecule so that accurate measurement of the trace elements using IBA on a liquid or crystalline sample of the protein is a rapid and convenient method to complement XRX, yielding the missing information and thus pivotaly contributing to a complete determination of the structure.

We should point out that neither the use of advanced computational methods nor complementary X-ray methods (such as X-ray absorption fine structure, XAFS) to follow the way the metals damage (oxidise) under the photon beam can do more than indicate the metal identification: Morshed et al. specifically underline the need for complementary methods to both quantify and also unambiguously identify the metals.

We also emphasise that the protein structure (including the location of the metal ions in the structure) is obtained by XRX, not by the IBA which only identifies and quantifies them.

Fig. 20 shows a protein which suppresses tumour growth, but mutations of which are (among other things) the cause of a genetic predisposition to “familial cylindromatosis”, a skin cancer affecting predominantly hair follicles and sweat glands of the head and neck. The main protein structure was determined by XRX but the two Zn atoms, located by XRX, were...
unambiguously identified by a “Total-IBA” measurement (using OMDAQ and GUPIX, see §3.4.4 and Garman243) using a 2.5 MeV proton beam and both PIXE and EBS, and a special protocol.247 This sort of structural work broadens and deepens our understanding of how cancer works: in this case the gene possessed a previously unknown (and unexpected) type of “B-box domain”. Further work (using sy-XRF) demonstrated that indeed the zinc was a physiological active ligand.

There are many other examples of examining important proteins using XRX + IBA, where the metal ligand is essential to the protein function. For example, to expand our understanding of catalysis by the alkaline phosphatase class of enzymes, Yong et al.247 determined the structure of the widely occurring microbial alkaline phosphatase PhoX. These enzymes play a crucial role in phosphate acquisition by microorganisms. The enzyme contains a complex active-site cofactor comprising two antiferromagnetically coupled ferric iron ions (Fe3+), three calcium ions (Ca2+), and an “oxo” group bridging three of the metal ions. These metal ions were identified and quantified by IBA. The presence of iron in PhoX raises the possibility that iron bioavailability limits microbial phosphate acquisition.

Again, Karkehabadi et al.249 solved the detailed structure of “Cel61A”, one of a significant class of the glycoside hydrolase (GH) “family 61” proteins found in the fungus Hypocrea jecorina. This was the first solution of any of the GH family 61 class. The authors identified a cluster of highly conserved residues on the surface of the Cel61B structure, finding a nickel ion bound within this conserved surface using IBA. The observation of bound Ni is expected to be important for Cel61B activity, stability or function.

In further work on the same fungus H. jecorina, Jacobson et al.250 identified and solved a previously unknown protein, denoted “cellulose induced protein 1” (Cip1) which is thought to be likely to function in biomass degradation. A calcium ion binding site was identified in a sequence-conserved region of Cip1: the presence of this ion was found to have a structural role. The calcium ion was unambiguously identified and quantified by IBA.

4.5 High throughput analysis
In §3.7 we described examples of real-time RBS. Clearly, such analyses generate very large datasets, counting as “high throughput analysis”. Also, at the end of §3.2 we compared a μ-IBA with a μ-XRF analysis: in this case the XRF used a multi-
segmented detector with a large solid angle capable of a very high total count rate; such a detector could just as easily be used for PIXE. Where the count rate is high the collection time may be small, and again the throughput may be high. So, in Florence the IBA (in this case PIXE) system has been improved to allow dataset collection times of only 30 s,

meaning that hourly resolved high sensitivity air pollution analyses over continuous periods of a week are easily feasible [and competitive with complementary methods]]. This system was used for a large and prominent study.

The problem of collecting enough data is solved by counting for longer; or counting faster, either by increasing the beam current or by increasing the number of detectors (which is equivalent to increasing the solid angle). Technically either is feasible, given appropriate investment. The problem of “high throughput analysis” therefore reduces to the feasibility of handling large datasets involving depth profiling. The air pollution example above is mathematically trivial since only PIXE spectra are handled: these can be inverted with simple minimisation methods. We have already given one example for the non-trivial depth profiling case in §3.7 where the depth profiles were given in real time by an artificial neural network. We give another substantial and interesting example below where the depth profiles are extracted in bulk by standard analytical software used off-line.

The Joint European Torus (JET) and its successor, the International Thermonuclear Experimental Reactor (ITER: this is a pun in Latin, it means the Way), depend on controlling very high temperature plasmas and understanding in detail their interaction with the walls of the reaction chamber. JET is continuing to host experiments aimed at the success of ITER, and these “campaigns” end with the reaction chamber lining tiles being removed for materials analysis. The results of these analyses are buried in the technical literature, but there are a large number of tiles with many analysis points needed per tile: the measurements are very extensive with very large datasets being generated. This is a continuing programme (for example, see Baron-Wiechec et al.

Fig. 21 shows just one such analysis. Four different analyses are used and many spectra are handled self-consistently per analysis point. This is an example where very large quantities of highly complex data are handled fully quantitatively and entirely automatically in support of an industrial-sized programme.

4.6 Blind analysis – Darwin glass

800 000 years ago a meteor struck Tasmania, creating a large impact crater (see Fig. 22), with impact glasses (see Fig. 23h) resulting from the condensation of the vapourised rock strewn over 400 km² around the crater. Some of these glasses have crystalline inclusions – rutile (see Fig. 23e and i) and silica have been detected – which is extraordinarily strange since the rapid quenching of impact glasses ought to have precluded any crystallisation. The geologist accordingly searched for the origin of these unexpected crystals, and found that they resided in inclusions in the glasses (see Fig. 23f). But the composition of these inclusions was completely unknown – standard methods remained equivocal.

Accordingly, we did IBA imaging of them (see PIXE maps of the Ti signal in Fig. 23a–c), which showed that they were extremely heterogeneous, but contained areas very rich indeed in Si as well as areas rich in Ti (and many other elements as well). Fig. 24 shows an analysis of one of these Si-rich areas, where we deliberately made use of the $^{12}\text{C}(p,p)^{12}\text{C}$ EBS resonance at 1734 keV. These resonances are just as characteristic of nuclear structure as characteristic X-rays are of atomic structure (see §3.2), so that the identification of the carbonaceous matrix of the inclusions was unequivocal, greatly surprising the geologists, for whom the observation of carbon in impact glasses was unprecedented.

Fig. 24 also shows how the carbon can be profiled by increasing the beam energy. Interestingly, the shape of the 1734 keV resonance appears not to be reproduced in the data, but this is due to the structural effect affecting the real energy straggling of the beam as a function of depth. This is a well-known effect that has been incorporated into the IBA code: it enables us to reliably model the depth profile in terms of silica inclusions in the carbonaceous matrix. Without this EBS resonance, the IBA would not be sensitive to the structure of the sample: it would only give us average elemental compositions. So the stereo pair for the Ti spatial distribution represented in Fig. 23a–c only localises Ti-rich regions, it does not identify the oxide.

As soon as the geologist understood the general structure of the sample he was able to persuade the microscopist that it was worth preparing a TEM sample to look specifically for the nanocrystals (rutile was positively identified, see Fig. 23e), and he also obtained the density tomograph of the sample (Fig. 23g is a still from the tomograph movie freely available in the supplementary material). He was then able to go on to make a detailed analysis of the chemical state of the carbon, finding a series of organic molecules, which again are unprecedented in impact glasses and indicates that we cannot rule out interstellar organic molecules being carried intact to Earth by meteorites.
4.7 Non-destructive analysis – cultural heritage

There are at least two European IBA labs dedicated to cultural heritage applications: LABEC in Florence and the AGLAE lab of the Louvre Museum. Calligaro & Dran have usefully reviewed this field recently. de Vigerie et al. have reviewed IBA for paintings. For cultural heritage the “samples” are frequently priceless treasures that must be treated very carefully: this does not include being cut up and stuffed into vacuum chambers by accelerator physicists. Accordingly, so-called “external beams” are usually used, where the samples to be analysed may be arbitrarily large and...
of any shape: they may also be wet or otherwise delicate. Typically, 3 MeV proton beams are used which can exit the vacuum system through a thin (200 nm) silicon nitride window (see §3.6) and travel tens of mm in air. For these applications the sample is brought as close to the exit window as possible to minimise absorption (for X-rays) and energy loss (for particles), and for the same reason a helium atmosphere is often used. The sample is held on a motorised stage, but the ion beam is usually focussed and scanned for fast and convenient imaging, as in the SEM: this is not possible for sy-XRF which is limited to mechanical scanning. The ion beam can be scanned over an area given by the exit window, which can be several nm in diameter.

Fig. 25 shows arguably the first photograph, an image of great importance almost 200 years old. It was apparently becoming corroded and was taken to AGLAE for investigation using both alpha and proton beams. Fig. 26 shows the results. In an analysis that would have been inconclusive using obsolete methods, Pascual-Izarra et al. were able to synergistically fit the He-RBS and the simultaneously collected H-EBS and H-PIXE to show quantitatively that the tin component of the heliograph was oxidising.

Another interesting example of a fully synergistic analysis is of a 19th century copy of *La Bohémienne* (Frans Hals, Fig. 25 View from the Window at Le Gras. Heliograph on pewter plate, 162 × 202 mm, by Joseph Niépce (1827). Figure credit: Wikimedia Commons.

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Fig. 26 IBA of a corroded spot on Niépce’s heliograph. RBS determines Pb/Sn at surface; EBS determines O/metal at surface; PIXE determines (total Pb)/(total Sn). Synergistic fitting of RBS + EBS + PIXE yields the depth profile. Reprinted from *Nucl. Instrum. Methods Phys. Res., Sect. B*, 261 (Fig. 2 and 3 of Pascual-Izarra et al., Towards truly simultaneous PIXE and RBS analysis of layered objects in cultural heritage, 426–429, ©2007), with permission from Elsevier.
5 Conclusions

Ion Beam Analysis is a collection of analytical techniques which individually have a long history, just as other spectrometries and spectroscopies do. And as for those other complementary methods, IBA has had a series of recent developments that have dramatically increased its power. In particular, we have at last found out how to take advantage of the very well-known synergies between the atomic and nuclear IBA methods. Where the performance of PIXE is weak that of EBS is strong, and vice versa (see Table 3 and §3.4.1).

This has resulted in what is effectively a new spectroscopic imaging technique (microbeam scanning “Total-IBA”) which is also fully quantitative (the spectrometries are very well developed). “Total-IBA” has a number of other features very attractive to analytical chemists: its depth resolution can reach ~1 nm near the sample surface and its lateral resolution depends on the focussed probe size which can be deep sub-micron; there are ways to use it for high-volume routine applications (which may themselves be very demanding); it can be used in real-time; and it requires little or no sample preparation.

The quantitation of “Total-IBA” (usually PIXE + EBS) is model-free in principle since its sensitivity extends from major (matrix) to trace elements; but there are also systematic and well-developed ways to introduce prior knowledge (including chemical information) into the analysis. It is non-destructive, although, as with other nominally “non-destructive” methods, there may be more or less beam damage.

We should emphasise that IBA includes RBS, which has very recently been shown to be a primary direct reference method (using the language of the metrologists), with an absolute traceable accuracy of about 1% easily surpassing any other model-free non-destructive thin film analytical method. We have shown how “Total-IBA” can inherit this new accuracy, and pointed out that it should enable the much easier production of thin film reference standards certified at high accuracy in a very wide variety of materials.

We have shown very varied examples of the power of these modern methods, as well as explaining nine completely different sorts of recent significant advances which together have had such a remarkable result, even if individually they may look incremental to the wider analytical community.

We have stressed the importance of complementary methods throughout this Review, and should now conclude with some observations. XRF and PIXE are competitive methods: they both do very similar things. But XRF and Total-IBA are complementary in that IBA has definite advantages over XRF in quantitation (a specific comparison between sy-XRF and IBA is given in §3.2) where sy-XRF has other advantages over IBA (in chemical imaging for example). GI-XRF is capable of a traceable measurement of quantity of material, just as RBS is: it is very valuable to have independent methods available. On the other hand RBS could certify the thickness of thin film reference samples used for SIMS (and XRF), and for determining Fundamental Parameters (see §3.2), at much higher accuracy than currently available. Such CRMs could also be valuable for determining electron mean free paths for XPS.

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