Synthesis and super-resolution imaging performance of a refractive-index-controllable microsphere superlens

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Microspheres can function as optical superlenses for nanoscale super-resolution imaging. The imaging performance is mainly affected by the size and refractive index of the microsphere. Precise control of these parameters is a challenging task but of fundamental importance to the further development of the technique. In this study, we demonstrate for the first time a nanoparticle-hybrid suspension polymerization approach to chemically synthesize high-quality microspheres (ZrO2/polystyrene) with optical properties that are highly controllable. Microspheres of different sizes (d: 2–20 μm) and refractive indexes (n: 1.590–1.685) were synthesized and their super-resolution imaging performances were evaluated and compared. Our results show that continuously increasing the refractive index of microspheres can enhance the imaging resolution and quality. A 60 nm resolution has been obtained in the wide-field imaging mode and a 50 nm resolution has been obtained in the confocal mode imaging of semiconductor chip samples. The obtained 50–60 nm resolutions have significantly gone beyond the conventional 200 nm resolution limit for visible light optical microscopes; the super-resolution mechanism has been discussed. The synthesized microsphere superlenses may find applications in many other areas as well, including nanolithography, nano-sensing, nano-diagnosis, nano-spectroscopy and ultra-high density optical data storage.

Introduction

Optical microscopes are indispensable tools for studying microscale features, especially for imaging of live biological samples. Compared with electron microscopy, optical microscopy is non-invasive and does not require a high vacuum. However, optical microscopy resolution is often limited at 200 nm, which is considerably inferior compared to the resolution of electron microscopes of about 10 nm. The limited optical resolution, known as the Abbe diffraction limit, stems from the wave nature of light and is caused by the loss of evanescent waves in the far-field, which contains high spatial frequency subwavelength information of an object. It shall be noted, however, the recent Nobel Prize awarded to super-resolution fluorescence microscopy techniques do not rely on the recovery of evanescent waves in the far-field. These techniques use strategies of patterned light excitation or single molecule localization of fluorescent molecules. In other words, the improvement of resolution in fluorescence super-resolution techniques is achieved through material response instead of optical system itself. Other super-resolution techniques, such as metamaterials superlenses, super-oscillatory lenses, plasmon gratings, and nanoscale solid immersion lenses (SILs) have the root connection with the transformation of evanescent waves into propagating waves. These techniques, however, have one drawback or another in optical super-resolution imaging. For example, metamaterial lenses, super-oscillatory lenses and plasmon gratings are very difficult to manufacture and can operate only in a narrow range of wavelengths. SILs operate by coupling of hemispherical or super-hemispherical dielectric lenses or microlens arrays with optical microscopy. The SILs could be fabricated by a self-assembly method, thermal reshaping method or the “top-down” fabrication approaches such as femtosecond laser direct writing, and highly ordered three dimensional microlens arrays even with dynamically tunable biopolymers have already been fabricated. However, it still remains a great challenge to resolve structures below 100 nm due to the low refractive index of the lens materials or the nanoscale separation between the surfaces of the SILs and the investigated substrates.

Recently, super-resolution imaging through coupling of dielectric microspheres with white-light optical microscopy have proven to be a simple and superior way to achieve sub-diffraction resolution. Compared with SILs, the contact region for a
hard microsphere is a single point, which is significantly smaller, thus making sure that the lower surface of microspheres is located within the extent of evanescent field produced by the underlying nano-patterned substrate. Thus, the microsphere can convert the high frequency spatial harmonics of the evanescent field into propagating waves to form a magnified virtual image below the substrate surface, which can be picked up by a conventional objective lens. Initially, this technique had been developed for commercial SiO₂ spheres submerged in air environment, achieving 50 nm resolution of a gold-coated anodic alumina oxide membrane. However, due to the limitation of the low refractive index of SiO₂ spheres, the super-resolution window of SiO₂ spheres was confined to the diameter (D) range of 2–9 μm. Silica spheres with diameters larger than 10 μm even failed in 100 nm resolution imaging tests. Large diameter (30–100 μm) polystyrene microspheres (refractive index of the particle: \( n_p = \sim 1.59 \)) were also reported for the super-resolution imaging of a blue-ray disc in an air atmosphere, achieving a resolution of 120 nm.\(^{11}\) However, in these cases, the microspheres exposed in an air environment usually resulted in a low imaging contrast. When SiO₂ spheres were semi-immersed in a thin layer of ethanol or SU-8 resist,\(^{15,16}\) the imaging contrast could be strongly strengthened; however, it was not easy to resolve features below 100 nm because of their low refractive index (\( n_p = \sim 1.46 \)). Darafsheh et al. found that when BaTiO₃ (\( n_p = 1.9 \)) glass spheres were totally submerged in a liquid of isopropyl alcohol,\(^{12}\) the small spheres (diameter = 4.2 μm) were able to discern features as small as 75 nm (\( \sim \lambda/7 \)), while for large microspheres (50 μm < diameter < 220 μm), the resolved feature sizes were only \( \sim \lambda/4 \). Li et al. reported water submerged BaTiO₃ (diameter = 100 μm) for the imaging of an adenovirus with a resolution of 75 nm.\(^{14}\)

To date, microspheres coupled to optical super-resolution imaging were focused on commercial SiO₂, PS and high RI BaTiO₃. However, these spheres have either a low refractive index or poor processability, which make them less attractive in practical applications. Introducing high RI inorganic nanoparticles into a polymer matrix may be a promising strategy to obtain high refractive index nanocomposites, which combine the advantages of an organic matrix (low weight, good impact resistance and excellent processability) and inorganic materials (high RI and good thermal stability).\(^{18}\) In fact, the high RI nanocomposite films\(^{19,21}\) or bulk nanocomposites\(^{22}\) have already been reported by some researchers. However, due to the arguable difficulty, the fabrication of high RI nanocomposite microspheres with high optical transparency for the super-resolution imaging has barely been reported to the best of our knowledge. Herein, we report a facial suspension polymerization method for the preparation of optically transparent and high RI ZrO₂/PS nanohybrid colloidal microspheres. Compared with the femtosecond laser direct writing method, which is usually applied to the fabrication of lenses composed of low refractive index photosensitive molecules, the suspension polymerization method used here can fabricate spheres with high and controllable refractive index. Herein, as high as 50.8 wt% of ZrO₂ nanoparticles can be uniformly distributed in the final composite microspheres, which makes these colloidal microspheres have a controllable refractive index (\( n_p = 1.590–1.685 \)). These microspheres are used for optical super-resolution imaging and features as small as 50–60 nm are clearly resolved.

**Experimental**

**Materials**

Zirconium(IV) isopropoxide–isopropanol complex (99.9%) was purchased from Aldrich. Anhydrous benzyl alcohol (99.8%), 3-(trimethoxysilyl)propyl methacrylate (MPS, 97%), styrene (S, 99%), oleic acid (OA), lauroyl peroxide (98%), divinylbenzene (DVB, 80%), and cedarwood-oil were purchased from Aladdin Reagent Co., Ltd (China). Polystyrene alcohol (PVA1788), tetrahydrofuran (THF, ≥99.5%), anhydrous methanol (≥99.5%), anhydrous ethanol (≥99.7%), and dimethyl-silicone were obtained from Sinopharm Chemical Reagent Corp (China). Styrene was distilled under reduced pressure to remove the inhibitor hydroquinone, which was then stored in a refrigerator at 4 °C. Other reagents were used as received.

**Synthesis of ZrO₂ nanoparticles**

ZrO₂ nanoparticles were synthesized according to a method described elsewhere.\(^{23}\) Briefly, zirconium(IV) isopropoxide–isopropanol complex (6.25 g) and benzyl alcohol (60 mL) were charged into a 100 mL Teflon-lined autoclave. This Teflon-lined autoclave was sealed and placed into an oven at a temperature of 240 °C. After 4 days, the reaction mixture was allowed to cool down, and a white turbid suspension was obtained.

**Modification of ZrO₂ nanoparticles**

The as-synthesized ZrO₂ nanoparticle suspension was centrifuged to obtain a white precipitate and then washed by three cycles of sonication and centrifugation with ethanol. The wet ZrO₂ nanoparticles were dispersed in the pre-made THF/MPS solution based on a molar ratio of 0.4/1 for MPS-to-ZrO₂ and 1.22 wt% of ZrO₂. The dispersion was sonicated for 30 min at room temperature, and then oleic acid (OA, 500 μL) was added and the mixture was sonicated for another 30 min. The transparent dispersion was placed into an oven at a temperature of 60 °C for 20 h and at 80 °C for another 3 h. The dispersion was centrifuged at 7000 rpm for 10 min to remove the possible aggregates and then concentrated by a rotary evaporator to remove most of the THF. The concentrated MPS and oleic acid modified ZrO₂ nanoparticles slurry was precipitated and washed by two cycles of sonication and centrifugation in ethanol. The purified MPS/OA/ZrO₂ nanoparticles were added into a styrene monomer to obtain a yellowish transparent solution upon ultrasonication, which was then stored in a refrigerator.

**Preparation of ZrO₂/PS nanohybrid colloidal microspheres**

Suspension polymerization was used to synthesize the ZrO₂/PS nanohybrid colloidal microspheres. In detail, polyvinyl alcohol was added into deionized water and heated at 60 °C for 20 min to obtain a 0.175 wt% of PVA aqueous solution, and then it was allowed to cool. Various amounts of MPS/OA/ZrO₂ nanoparticles
dispersed in styrene, 10 wt% of DVB in terms of S and 4 wt% of lauroyl peroxide in terms of S as the initiator were mixed and then poured into a PVA aqueous solution, and emulsified with a homogenizer at 6000 rpm for 3 min. The emulsified dispersion was then poured into a 250 mL four-neck round-bottom flask equipped with a mechanical stirrer, a reflux condenser, a thermometer, and a nitrogen gas inlet. The system was degassed with nitrogen for 30 min to remove oxygen in the reactor, which was heated to 70 °C for polymerization at 250 rpm for 12 h under a nitrogen atmosphere. The products were labelled as M1, M2, M3, M4, and M5, corresponding to 10.5, 23.5, 30.3, 38.2, and 50.8 wt% of ZrO2 incorporated microspheres based on TGA analysis. As a control, bare polymer microsphere M0 was prepared in the same way but without ZrO2 nanoparticles. The as-synthesized microspheres were obtained by centrifugation and washing by three cycles of sonication and centrifugation with ethanol, and dried under vacuum for characterization.

Super-resolution imaging by composite microspheres
To demonstrate the super-resolution property of the microspheres, the as-synthesized nanohybrid colloidal microspheres were observed with an Olympus optical microscope (BX63) under an objective lens of 100× with a numerical aperture of 0.8 and reflective mode illumination with a halogen light source for the optical imaging. The sub-diffraction-limited objects used in the experiment were semiconductor chips with nano-patterned structures of 75 nm and 60 nm gaps between specific stripes with widths of 145 nm and 115 nm, respectively. For imaging the 75 nm gaps, the microspheres were first spread on the surfaces of the sub-diffraction-limited objects through the evaporation of ethanol drops; subsequently, dimethyl-silicone (refractive index of the medium is n = 1.400) was dropped onto the substrates to make the microspheres be semi-immersed in silicon oil after spin-coating at a speed of 3000 rpm for 5 min. For imaging the 60 nm gaps, the microspheres were semi-immersed in cedarwood oil (n = 1.515) through spin-coating in the same way as dimethyl-silicone; then, most of the cedarwood-oil was washed away by tetrachloroethylene to reduce the accumulation of oil around the spheres. The sub-diffraction virtual images of the nano-patterned surfaces were acquired by focusing through the monomer droplets containing MPS/ZrO2 were suspended in PVA aqueous solution and polymerized through suspension polymerization, resulting in collapsed spheres. This behavior may be attributed to the lack of hydrophobicity of the MPS molecules. To improve the hydrophobicity of the MPS/ZrO2 nanoparticles, OA with a longer hydrophobic alkyl chain was used as the second ligand, which could effectively anchor to the ZrO2 surface through coordination between its carboxyl group and the Zr atom. The MPS/OA/ZrO2 can not only be dispersed in the monomers of S and DVB in a high concentration, but also polymerize with them by suspension polymerization, forming nearly perfect ZrO2/PS composite microspheres with ZrO2 nanoparticles evenly distributed within the microspheres. A small amount of DVB was used as the crosslinking agent to accelerate the polymerization rate and form the cross-linked network structure, which would further prevent the possible movement of ZrO2 nanoparticles towards the surfaces of spheres during suspension polymerization. This synthesis process is highly repeatable and designable. The most critical step is the modification of ZrO2. Once the well modified ZrO2 nanoparticles are prepared, they can be dispersed in monomer such as styrene in various amounts (0–50.8 wt%), thus the refractive index of the ZrO2/PS nanohybrid colloidal microspheres can be designed by the ZrO2 content.

Results and discussion
Synthesis of ZrO2/PS nanohybrid colloidal microspheres
The nonaqueous synthesis of zirconium(IV) isopropoxide in benzy alcohol produced a white precipitate of ZrO2. To prepare a transparent dispersion of ZrO2 in an organic monomer, MPS was first chemically bonded to the ZrO2 nanoparticles through condensation between the alkoxy groups of MPS and the surface hydroxyl groups of the ZrO2. MPS provides not only steric stabilization of the ZrO2 nanoparticles in organic monomer but also a double bond for the subsequent polymerization. However, in the experiment, if only MPS was used as the ligand, the MPS-modified ZrO2 (MPS/ZrO2) nanoparticles were well dispersed in styrene, but tended to migrate from the interior of the monomer drops to their surfaces when the monomer droplets containing MPS/ZrO2 were suspended in a PVA aqueous solution and polymerized through suspension polymerization, resulting in collapsed spheres. This behavior may be attributed to the lack of hydrophobicity of the MPS molecules. To improve the hydrophobicity of the MPS/ZrO2 nanoparticles, OA with a longer hydrophobic alkyl chain was used as the second ligand, which could effectively anchor to the ZrO2 surface through coordination between its carboxyl group and the Zr atom. The MPS/OA/ZrO2 can not only be dispersed in the monomers of S and DVB in a high concentration, but also polymerize with them by suspension polymerization, forming nearly perfect ZrO2/PS composite microspheres with ZrO2 nanoparticles evenly distributed within the microspheres. A small amount of DVB was used as the crosslinking agent to accelerate the polymerization rate and form the cross-linked network structure, which would further prevent the possible movement of ZrO2 nanoparticles towards the surfaces of spheres during suspension polymerization. This synthesis process is highly repeatable and designable. The most critical step is the modification of ZrO2. Once the well modified ZrO2 nanoparticles are prepared, they can be dispersed in monomer such as styrene in various amounts (0–50.8 wt%), thus the refractive index of the ZrO2/PS nanohybrid colloidal microspheres can be designed by the ZrO2 content.

Characterization
Thermogravimetric analysis (TGA) was carried out using a Perkin Elmer TGA-7 instrument (USA) at a heating rate of 10 °C min−1 from room temperature to 800 °C in air. Fourier transform infrared spectra (FTIR) were acquired with a Nicolet Nexus 470 spectrometer (USA). High resolution transmission electron microscopy (HRTEM) was performed on a Tecnai G2 F20 S-Twin field emission transmission electron microscope (USA).
Morphology and structure of the ZrO$_2$ nanocrystals and ZrO$_2$/PS nanohybrid colloidal microspheres

Fig. 1 demonstrates the typical TEM images of the MPS/OA/ZrO$_2$ nanoparticles. The sample was dispersed well in THF with a uniform crystal size of about 3.5 nm (Fig. 1a). The high crystalline lattice of the nanoparticles, as shown in Fig. 1b, belongs to the cubic phase (JCPDS: 27-991). The FTIR spectrum of MPS/OA/ZrO$_2$ nanoparticles shows the absorption peaks at 500–700 cm$^{-1}$ and 800–1100 cm$^{-1}$ assigned to Zr–O and Si–O–Zr vibrations (Fig. 2a), respectively, indicating that MPS has been chemically bonded to the ZrO$_2$ nanoparticles. The peaks at 1547 and 1460 cm$^{-1}$ belong to the characteristic absorption of $\text{–COO}^-$ groups, meaning that OA has been chemically absorbed to the surface of ZrO$_2$ nanoparticles as well. All these results unveil the successful modification of both MPS and OA on the surface of the ZrO$_2$ nanoparticles. The FTIR spectrum of ZrO$_2$/PS nanohybrid microspheres (Fig. 2b) shows absorption peaks at 500–700 cm$^{-1}$ for the Zr–O vibration, at 1451 cm$^{-1}$ and 1492 cm$^{-1}$ for the characteristic peaks of phenyl stretching vibration and at 757 cm$^{-1}$ and 700 cm$^{-1}$ for flexural vibration ($\delta_{\text{C–H}}$) of the benzene ring, which demonstrates the successful encapsulation of ZrO$_2$ in the hybrid microspheres.

Fig. 3a and b present the typical SEM images of the ZrO$_2$/PS nanohybrid colloidal microspheres M1 and M5, which have a smooth spherical surface morphology. All the samples from M1 to M5 have smooth surfaces even at a high ZrO$_2$ content of 50.8 wt%, which can be further seen from their high magnification SEM images (see Fig. S1, ESI†). Typical SEM mapping graphs of the nanohybrid colloidal microsphere clearly reveal the existence of Zr, C, and O elements in hybrid microspheres (Fig. 4a–d), with well-defined spherical structure. A SEM linescan of the individual microsphere further demonstrates the uniform distribution of Zr in the hybrid microspheres (Fig. 4e). From the corresponding linescan spectrum in Fig. 4f, the relative weight contents of Zr, C, and O are found to be 36.0%, 49.6%, and 14.4%, respectively. The composition of samples M1–M4 were also analysed by SEM linescan analysis; all the samples show uniform distribution of Zr, C, and O in the hybrid microspheres, and their relative weight contents of Zr, O, and C are summarized in Table 1.

Fig. 5 shows the thermogravimetric analysis (TGA) results of the modified ZrO$_2$ nanoparticles and ZrO$_2$/PS composite.
Table 1  SEM linescan results of Zr, O, and C content in M1–M5

<table>
<thead>
<tr>
<th>Sample code</th>
<th>Zr (wt%)</th>
<th>O (wt%)</th>
<th>C (wt%)</th>
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<tbody>
<tr>
<td>M1</td>
<td>5.79</td>
<td>4.64</td>
<td>89.6</td>
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<tr>
<td>M2</td>
<td>14.9</td>
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<td>78.2</td>
</tr>
<tr>
<td>M3</td>
<td>19.3</td>
<td>10.1</td>
<td>70.6</td>
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<tr>
<td>M4</td>
<td>27.4</td>
<td>11.6</td>
<td>61.1</td>
</tr>
<tr>
<td>M5</td>
<td>36.0</td>
<td>14.4</td>
<td>49.6</td>
</tr>
</tbody>
</table>

Fig. 5  TGA curves of MPS/OA/ZrO2 nanoparticles and ZrO2/PS nanohybrid colloidal microspheres M1–M5.

microspheres M1–M5. The weight loss of the modified nanoparticles below 200 °C is 1 wt%, which is attributed to the loss of physically absorbed water and organic solvent. The weight loss between 200 and 800 °C is 25 wt%, corresponding to the chemically bonded OA and MPS on the ZrO2 nanoparticles. The residual inorganic substances are about 10.5, 23.5, 30.3, 38.2 and 50.8 wt% for samples M1, M2, M3, M4, and M5, respectively, and are mainly composed of ZrO2.

The refractive index of M0–M5 could be theoretically estimated according to the following formula:

\[
\eta_p = \eta_{org} \times V_{org} + \eta_{ZrO2} \times V_{ZrO2}
\]

where \(\eta_{org}\) and \(\eta_{ZrO2}\) are the refractive indices of polymer (\(\eta_{org} \approx 1.59\)) and ZrO2 nanoparticles (\(\eta_{ZrO2} \approx 2.2\)). \(V_{org}\) and \(V_{ZrO2}\) are the volume fractions of polymer and ZrO2 in the microspheres. Based on the TGA analysis, the theoretical refractive indices were calculated to be 1.590, 1.600, 1.622, 1.634, 1.651 and 1.685 for samples M0–M5, respectively.

Super-resolution imaging: wide-field mode and white-light illumination.

The super-resolution imaging configuration is illustrated in Fig. 6a. The semi-immersed microspheres collect the underlying near-field information of the substrate, magnify it and form a magnified virtual image located at a certain position below the surface of the substrate, which can be picked up by a 100× objective lens (NA = 0.8, Olympus BX63). When dimethylsilicone is used as the medium to reinforce the imaging contrast, it is less volatile and can easily spread on the substrate and 50.8 wt% for samples M1, M2, M3, M4, and M5, respectively, and are mainly composed of ZrO2.

According to the Rayleigh equation, \(d = 0.5\lambda/\eta_p NA\) in which \(\lambda\) is the illumination wavelength and NA is the numerical aperture of the objective lens. The resolution limit is 344 nm under white-light illumination, which peaked at \(\lambda = 550\) nm and NA = 0.8 for the optical microscopy used here. Obviously, this microscopy cannot resolve the nanoscale surface features of the chip (see Fig. S2, ESI†). However, when the dimethyl-silicone semi-immersed microspheres (diameter = 10 μm) are used as a superlens, the imaging resolutions of the microscope are obviously improved. Nonetheless, the pure polymer microspheres M0 (\(\eta_p = 1.590\)) and hybrid microsphere M1 (\(\eta_p = 1.600\)) still cannot resolve 75 nm gaps (indicated by the arrows in Fig. 6d and e). With the increase in refractive index of the microspheres, 75 nm gaps between three stripes with a width of 145 nm can be clearly discerned (Fig. 6f and g). As the diameter of the nanocomposite microsphere is increased, with the sample M5 as an example, not only can the 75 nm features be observed, but the imaging windows significantly increase, as shown in Fig. 6h–k. The only drawback is that the dimethyl-silicone semi-immersed microspheres still cannot image the texturing structure with 60 nm gaps.

To further improve the image resolution, cedarwood-oil was used as the immersion medium instead of dimethyl-silicone for observing the chips with 60 nm gaps between four 115 nm wide stripes (Fig. 7a). The three-dimensional images of the microspheres semi-immersed in cedarwood-oil are shown in Fig. 7b. All the microspheres M0, M1, M3, and M5 have almost the same diameter of ~13 μm and can resolve the 75 nm gaps between three 145 nm wide stripes of the chips (Fig. 7c–e), but only the microsphere M5 with the highest refractive index can resolve the 60 nm gaps of the chip (Fig. 7f). These results further demonstrate that the microspheres with higher refractive index produce higher resolution and imaging quality compared to those with low refractive index microspheres. The reason is explained below.

Super-resolution imaging: confocal mode and laser illumination.

Furthermore, we investigated the imaging behaviour of the microsphere coupled confocal microscopy. As shown in Fig. 8a, the chip has a periodic structure with minimum gaps of 50 nm. This nanotexturing cannot be resolved by confocal microscopy (Olympus OLS4100 LEXT) with a 100× and NA = 0.95 objective at the laser illumination of \(\lambda = 405\) nm (Fig. 8b). However, when the dimethyl silicone semi-immersed microspheres M1, M3, and M5 with almost the same diameters of 13.3 μm were placed on top of the chips, the 50 nm gaps can be resolved (Fig. 8c–e). As the refractive index of the microsphere increased from 1.600 to 1.634 and 1.685 for spheres of M1, M3 and M5, the corresponding image magnifications increased from 1.50 to 1.81 and 2.05, respectively, indicating that alcohol, as shown in the three dimensional image in Fig. 6b. The chip has nano-patterned structures of 60 nm and 75 nm gaps between specific stripes with widths of 115 nm and 145 nm, as indicated by the arrows in the SEM image (Fig. 6c).

The semi-immersed microspheres couple confocal microscopy. As shown in Fig. 8a, the chip has a periodic structure with minimum gaps of 50 nm. This nanotexturing cannot be resolved by confocal microscopy (Olympus OLS4100 LEXT) with a 100× and NA = 0.95 objective at the laser illumination of \(\lambda = 405\) nm (Fig. 8b). However, when the dimethyl silicone semi-immersed microspheres M1, M3, and M5 with almost the same diameters of 13.3 μm were placed on top of the chips, the 50 nm gaps can be resolved (Fig. 8c–e). As the refractive index of the microsphere increased from 1.600 to 1.634 and 1.685 for spheres of M1, M3 and M5, the corresponding image magnifications increased from 1.50 to 1.81 and 2.05, respectively, indicating that
Microspheres with higher refractive index can produce better super-resolution imaging.

Super-resolution mechanism

The basic mechanism of microsphere superlens imaging was explained in our previous study on the technique. The microspheres function as a superlens, producing sub-wavelength focusing, which illuminates the sample for imaging. Taking the case of cedarwood-oil ($n_m = 1.51$) as an example (Fig. 7 experiments), Mie theory calculations show that a 13 μm microsphere can generate an illumination spot of ~120 nm (M0), 117 nm (M1), 112 nm (M3), 110 nm (M5) at the sample surface plane, as shown in Fig. 9 (red curve, labelled as bright stripes). All the spheres (M0–M5), therefore, have the capability of resolving 145 nm strip features; this agrees with our experimental observations (Fig. 7c–f). On the other hand, only M3 and M5 are predicted to be able to see 115 nm features. Our experiments confirm that M5 can indeed visualize the 115 nm stripes (Fig. 7f), but M3 failed (Fig. 7e); this could be caused by imperfection in the microspheres and optical systems or wave interference between particle and samples. Once the 115 nm features are picked up by the M5 lenses (Fig. 7f), they were magnified by 2.1 times (becoming 241.5 nm) and projected into the conventional objective lens (NA: 0.8); here, the magnification M of M5 lenses in Fig. 7f was obtained by calculating the ratio of the image size of the stripes and corresponding real size of the stripes. Using the following equation, we can inversely calculate the minimum gap size (i.e., gap resolution $d_{gap}$) between two strips, which is resolvable by the M5 microsphere superlens:

$$\frac{(d_{gap} + d_{strip})}{2} = \frac{l}{2NA}$$

where $d_{strip} = 115$ nm is the strip size; $M = \sim 2.1$ is the magnification factor; $l = 550$ nm and NA = 0.8; the gap resolution $d_{gap}$ was found to be 49 nm. This explains why the M5 superlens can resolve 115 nm features with 60 nm gaps. According to our calculation, the gap resolution can go to as low as 20 nm for $n = 1.76$ microspheres, with stripes sized larger than 140 nm. On the other hand, the strip resolution can go to

![Fig. 6](image-url)
Fig. 7  (a) SEM image of the nano-patterned chips with 60 nm gaps between four 115 nm wide stripes; (b) three dimensional image showing the distribution of cedarwood-oil around the sphere; (c to f) optical super-resolution imaging of the chips by M0, M1, M3, and M5, respectively, the dotted bordered rectangles in these pictures indicate locations of the structure containing 75 nm and 60 nm gaps between 145 nm wide stripes (upper three stripes) and 115 nm stripes (lower four stripes).

Fig. 8  (a) SEM image of the chip with periodic structures containing 50 nm gaps; (b) confocal image at $\lambda = 405$ nm of the same chip in (a); (c to e) imaging of the chips at $\lambda = 405$ nm through 13.3 $\mu$m spheres of M1, M3, and M5, respectively; the dotted bordered rectangles in these images indicate locations of the structure containing 50 nm gaps that are resolved by these spheres, the corresponding magnified images are shown in the bottom right corners. The parameters of the objective lens are 100×, NA = 0.95, and the bars are 2 $\mu$m in (b–e).
transparent ZrO$_2$/PS hybrid microspheres are used as a superlens, with a resolvable gap size of 60 nm.

Conclusions

Based on this study, a novel type of nanohybrid colloidal microspheres with high refractive index and optical transparency have been successfully synthesized through suspension polymerization of MPS and OA modified ZrO$_2$ nanoparticles with styrene. Because these modified ZrO$_2$ nanoparticles have very good compatibility and reactivity with the monomers, as high as 50.8 wt% of ZrO$_2$ nanoparticles can be homogeneously dispersed in the hybrid microspheres. When this new class of high refractive index and optically transparent ZrO$_2$/PS hybrid microspheres are used as a superlens, the dimethyl-silicone oil semi-immersed microspheres can discern surface features at 75 nm, and the cedarwood-oil semi-immersed microspheres can reach a super-resolution imaging of 60 nm under white-light microscopy. Under laser illumination at $\lambda = 405$ nm, these microspheres can even resolve more complicated structures with 50 nm gaps. The synthesis of hybrid microspheres is feasible, easily repeatable and designable in shape, size and refractive index. Accordingly, the approach that we have described here is quite general, and can be readily extended to prepare a series of hybrid microspheres with various refractive index and optical transparency, by changing the types of polymers and nanoparticles. The as-synthesized nanohybrid colloidal microspheres can be used not only in optical nanoscopy for super-resolution imaging with visible frequency, but also in some potential fields of nanolithography, optical memory storage, and optical nano-sensing.

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Notes and references