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# Stabilization of $H_3^+$ in the high pressure crystalline structure of $H_nCl$ ( $n = 2-7$ )

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The particle-swarm optimization method has been used to predict the stable high pressure structures up to 300 GPa of hydrogen-rich group 17 chlorine ( $H_nCl$ ,  $n = 2-7$ ) compounds. In comparison to the group 1 and 2 hydrides, the structural modification associated with increasing pressure and hydrogen concentration is much less dramatic. The polymeric HCl chains already present in the low temperature phase under ambient pressure persist in all the high pressure structures. No transfer of electrons from the chlorine atoms into the interstitial sites is found. This indicates the chemical bonding at high pressure in group 17 elements is fundamentally different from the alkali and alkaline elements. It is found that almost perfectly triangular  $H_3^+$  ions can be stabilized in the crystalline structure of  $H_5Cl$ .

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## Introduction

The suggestion that the hydrides of main group elements at high pressure may be superconductors with high critical temperature has stimulated recent interest in the search for the possible existence of hydrogen-rich alloys by theoretical and experimental means.<sup>1</sup> The former has been greatly facilitated by the recent developments in practical strategies for the prediction of crystal structures. Although, the predicted hydrides have yet to be confirmed by experiment, the theoretical studies have revealed a myriad of structures for the high pressure hydrides and enriched the understanding of the nature of chemical bonding in the rarely explored high pressure regime.

The hydrides of group 1 and 2 elements formed from the reaction of the metal and hydrogen molecules have been the most studied.<sup>2-6</sup> Most of the structures and structural trends can be explained from the simple concept of electron transfer from the metal to the hydrogen due to the large electronegativity differences between the alkali and alkaline elements and hydrogen molecules. The predicted compounds display rich H species distinguished from the well-known H-ion in hydrides at traditional stoichiometric ratios. Perhaps one of the most exciting predictions is the emergence of symmetric and linear  $H_3^-$  at high pressures as observed in dense  $CsH_3$  and  $BaH_6$ .<sup>7,8</sup> Moreover, the formation pressures of these compounds of just a few tens of GPa are accessible by experiments. In comparison, the bonding pattern is quite different for group 14 and

transition elements. For example, a Van der Waals solid with such molecular  $H_2$  units was found experimentally in  $SiH_4$  at low pressure.<sup>9</sup> At higher pressure, the atoms of group 14 elements tend to aggregate to form a 2D layered structure decorated with molecular like  $H_2$  species as predicted for  $SiH_4$  and  $SnH_4$ .<sup>10,11</sup> In comparison, the high pressure chemistry of hydrogen with electron-rich group 17 halogens has not been investigated. In this paper, we present results on a study of the crystal structures and phase stabilities of hydrogen-rich HCl- $H_2$  system. A major finding is the stabilization of cationic  $(H_3)^+$  ( $H_2$ ) species in  $H_5Cl$ . The geometry of  $H_3^+$  becomes almost an equilateral triangle under very high pressure.

The observation of a triatomic hydrogen cation  $H_3^+$  in the solid state is new and significant. The isolated molecule is important in various branches of science, such as physics, chemistry and astronomy. For example, it is known that the  $H_3^+$  ion with a triangular configuration is stable in the interstellar medium thanks to the low temperature and low density of the interstellar space and the  $H_3$  molecule is commonly formed from the neutralization reaction of  $H_3^+$  and an electron, and rather evanescent as a result of the repulsive nature of its ground state.<sup>12</sup> Furthermore, the multicenter  $(H_3)^+$  ( $H_2$ ) bond in group 17 Cl compounds signifies a deviation in the nature of chemical bonding from the charge transfer interactions in group 1 and 2 hydrides and covalent bonding in group 14 hydrides.

## Computational details

The search for stable high pressure structures of the  $H_nCl$  system was based on global minimization of free energy surfaces using *ab initio* total energy calculations and the particle-swarm-optimization scheme as implemented in the CALYPSO (Crystal structure ANALysis by Particle Swarm

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Optimization) code.<sup>13,14</sup> The performance and reliability of this method has been demonstrated on many known systems. An example is the success on the prediction<sup>15–17</sup> of an insulating orthorhombic (*Aba2*, Pearson symbol *oC40*) structure of Li and, more recently, two low-pressure monoclinic structures of Bi<sub>2</sub>Te<sub>3</sub>. In both cases, the predicted structures were later confirmed by experiments.<sup>18,19</sup> Structural searching was performed at 100, 200, and 300 GPa with a simulation cell consisting of 1–4 formula units. *Ab initio* electronic structure calculations and structural relaxations were carried out using density functional theory with the Perdew–Burke–Ernzerhof (PBE) exchange–correlation<sup>20</sup> implemented in the Vienna *ab initio* Simulation Package (VASP) code.<sup>21</sup> The predicted stable structures were carefully optimized at a high level of accuracy. A plane wave energy cutoff of 1000 eV was employed. Large Monkhorst-Pack *k* point sampling grids<sup>22</sup> were used to ensure that all the enthalpy calculations were well converged to an accuracy of 1 meV per atom. The atomic charges were obtained from Bader topological analysis<sup>23–25</sup> with very large grids to ensure sufficient accuracy. We also performed additional calculations employing the DF-2 van der Waals (vdW) functional<sup>26</sup> to validate the results, in particular for the low pressure structures. Phonons were calculated with the supercell method<sup>27</sup> implemented in the PHONOPY program.<sup>28</sup> In essence, from finite displacements, the Hellmann–Feynman atomic forces computed at the optimized supercell by the VASP code were input to the PHONOPY code to construct the dynamical matrix. Diagonalization of the dynamical matrix gives the normal modes and their frequencies. Converged results were obtained with the use of a 2 × 2 × 1 supercell and 4 × 4 × 6 *k*-meshes for the *Cc* structure, and a 2 × 2 × 1 supercell and 4 × 4 × 6 *k*-meshes for the *C2/c* structure.

## Results and discussion

Before embarking on a detailed discussion of the structures of the predicted high pressure H<sub>*n*</sub>Cl polymers, the relative energetics of the H–Cl system with H-rich stoichiometry from 100 to

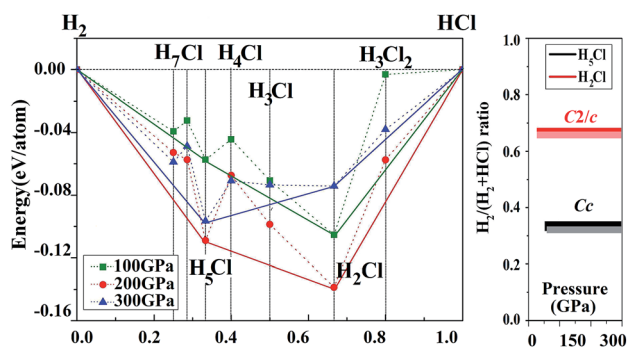


Fig. 1 Stability of new hydrogen chlorides. (A) Enthalpies of formation ( $\Delta H$ , with respect to HCl and H<sub>2</sub> of their most stable phases at selected pressures) of H<sub>*n*</sub>Cl ( $n = 1–7$ ). The abscissa  $x$  is the fraction of H<sub>2</sub> in the structures. Circles on the solid lines represent stable ground-state compounds under the corresponding pressure. (B) Pressure-composition phase diagram of the H–Cl system. The lighter colored lines represent the vdW corrections to corresponding structures.

300 GPa are summarized in the convex hull plot shown in Fig. 1. The enthalpies of formation were evaluated as the difference in the enthalpy of the predicted H<sub>*n*</sub>Cl structure with solid HCl and H<sub>2</sub> at the selected pressures. Since hydrogen has a small atomic mass, the zero point energy (ZPE) may be important. To investigate the vibrational effects on the phase stability, ZPEs for H<sub>2</sub>Cl and H<sub>5</sub>Cl were estimated at 100–300 GPa from the corresponding phonon spectra using the quasi-harmonic approximation.<sup>29</sup> It is found that the ZPEs are quite small and the inclusion of ZPEs in the phase diagram only resulted in a slight shift in the formation pressures but the stability of both phases remains unaltered. Structures lying on the convex hull are thermodynamically stable or metastable and, in principle, can be synthesized. Fig. 1 reveals that only two HCl–H<sub>2</sub> complexes, H<sub>2</sub>Cl and H<sub>5</sub>Cl are stable at 100 GPa. At this pressure H<sub>2</sub>Cl has the most negative enthalpy of formation. With increasing pressure, the stability of H<sub>5</sub>Cl relative to H<sub>2</sub>Cl increases and becomes the most stable phase at 300 GPa.

vdW effects may play an important role in the stabilization of a molecular solid. We have thus performed additional calculations on the H–Cl system with the vdW-DF2 method.<sup>26</sup> The results show that the differences between calculations with and without vdW corrections on the formation enthalpies of the structures considered in Fig. 1 are small. The formation pressures were found to change slightly. For example, the stabilized pressure of H<sub>2</sub>Cl increased from 21.2 to 21.3 GPa, while for H<sub>5</sub>Cl it increased from 50 to 60 GPa. Otherwise, the energetic order remains the same.

Now we examine the development of the high pressure crystal structures in H<sub>*n*</sub>Cl ( $n = 2–7$ ). The starting point is the crystal structure of HCl under ambient pressure. At low temperature, X-ray and neutron diffraction show HCl crystallized in an orthorhombic structure (*Bb2<sub>1</sub>m*).<sup>30</sup> In the crystal, HCl molecules are linked *via* the H atoms forming zigzag chains running parallel to the crystallographic *b* axis. The nearest neighbour Cl–H and second nearest neighbour Cl⋯H distances are 1.25 Å and 2.44 Å, respectively. The Cl⋯Cl separation is 3.88 Å and the H–Cl⋯H valence angle is 93.6°. The predicted crystalline phase of H<sub>2</sub>Cl at 100 GPa has a *C2/c* space group and the structure is shown in Fig. 2. The crystal is formed from HCl chains interposed with H<sub>2</sub> molecules. In this case, the H in the HCl chain is midway between the two Cl atoms with an H–Cl

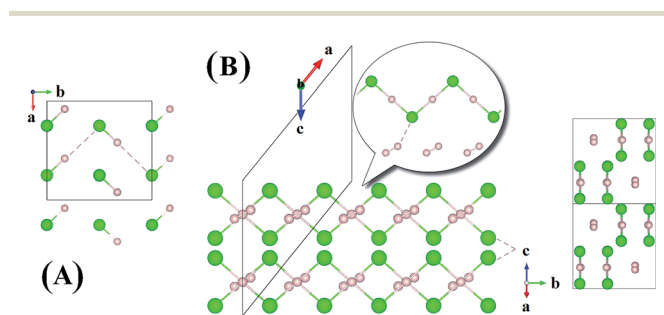


Fig. 2 Crystal structures of hydrogen chlorides. (A) Experimental structure of HCl at ambient pressure and low temperature, (B) *C2/c*-H<sub>2</sub>Cl recovered at 100 GPa along a different angle.



distance of 1.45 Å. The H–Cl–H angle has opened to 97.9° and the Cl⋯Cl separation is shortened to 2.90 Å. The H<sub>2</sub> units in the structure all have a H–H distance of 0.74 Å, which is almost identical to that of the isolated molecule. The Bader charges for the H in the chain and Cl atoms are +0.44 and –0.35, respectively and 0.0 for the H atoms in the H<sub>2</sub> units. The closest contact between a Cl atom and the H<sub>2</sub> molecule is 1.98 Å. The crystal structure of H<sub>2</sub>Cl at 300 GPa differs little from that at 100 GPa. The H atoms in the H–Cl chains are still situated at the middle of the two neighbouring Cl atoms with a H–Cl distance of 1.35 Å. The H–Cl–H angle is 95.5° and the shortest separation between two Cl atoms has reduced further to 2.69 Å. The H–H bond length in the H<sub>2</sub> unit is 0.73 Å. The closest H<sub>2</sub>⋯Cl distance is 1.70 Å. Compression has a significant effect on the interatomic distances of the H–Cl chains but does not alter fundamentally the underlying bonding pattern. A longer H–Cl distance in the chain suggests increased ionicity of the Cl–H bonds.

Although H<sub>3</sub>Cl and H<sub>4</sub>Cl are only metastable, it is instructive to examine the evolution of the crystal structure with increasing H<sub>2</sub> concentration. The structures of H<sub>3</sub>Cl at 100 and 300 GPa are shown in Fig. 3. Both are composed of zigzag H–Cl chains. Like H<sub>2</sub>Cl, the H atom is equidistant from the two nearest Cl atom with H–Cl bond distances of 1.44 Å at 100 GPa and 1.43 Å at 300 GPa. The most significant difference between the low and high pressure structures is that the Cl–H–Cl angle is almost linear at 100 GPa but bends to 135° at 300 GPa. At 300 GPa, the closest contact between the H<sub>2</sub> and the H in the chain is 1.27 Å. However, in both cases, the H–H distance of the H<sub>2</sub> molecule remains 0.73 Å. The structure of H<sub>4</sub>Cl at 100 GPa differs dramatically from all the structures within this series of compounds. Instead of H–Cl chains, the structure is composed of isolated HCl and H<sub>2</sub> molecules. The H–Cl distance is 1.38 Å and the H–H bond length is 0.74 Å. For comparison, the H–Cl bond of a free molecule is 1.276 Å. Therefore, the distance in the solid state at 100 GPa is slightly longer. The structure of H<sub>4</sub>Cl at 300 GPa again is different from that at 100 GPa. The basic building units are isolated Cl atoms, H<sub>2</sub> molecules with H–H distance of 0.74 Å and a novel 2-D layer of slightly puckered fused hexagonal rings formed from 3 HCl units with additional H atoms attached to the Cl atoms. Each H atom in the ring is bonded to three Cl atoms. In addition, each Cl is bonded to an

extra H atom which is not coordinated to other species in the crystal. The H–Cl distances in the fused ring are 1.59 Å and the terminal H–Cl is substantially shorter at 1.49 Å. Interestingly, the terminal H–Cl–H (ring) angles are 77° and the in-plane H–Cl–H and Cl–H–Cl angles are between 114–115°.

An interesting structure was observed in H<sub>5</sub>Cl at 100 GPa. Although chains formed from Cl and H atoms are still clearly visible, the detailed construction of the chain is very different. In H<sub>5</sub>Cl, instead of placing one H atom midway between the two nearest neighbour Cl atoms, it is replaced by an H<sub>3</sub> unit. The H<sub>3</sub> is a distorted isosceles triangle and can be described as a loosely bound unit of an H atom and an elongated H<sub>2</sub> with an apical angle of 63.8°. The apical H atom is linked to the two nearest Cl atoms in the chain with H–Cl distances of 1.47 Å. The distances from the apical H atom to the two H forming the H<sub>2</sub> are 1.01 Å and 0.97 Å, respectively and the intermolecular H–H distance is 0.81 Å. The remaining H<sub>2</sub> units in the structure have H–H distances of 0.74 Å. Moreover, the shortest distance from these H<sub>2</sub> to the H<sub>3</sub> is 1.36 Å and, therefore, may be considered as non-interacting molecules.

Compression of H<sub>5</sub>Cl to 300 GPa does not change the space group symmetry. The chain pattern with interpose H<sub>3</sub> units is still maintained, but the local H⋯H interactions have changed dramatically. The H<sub>3</sub> unit now approaches an equilateral triangle. The H–H lengths are 0.87, 0.87 and 0.88 Å with bond angles 59.7, 59.7 and 60.5°. The Cl–H distance has elongated from 1.47 Å at 100 GPa to 1.60 Å! The large lengthening of the Cl–H clearly suggests a substantial change in the Cl–H bonds. More significantly, the isolated H<sub>2</sub> molecules are now pushed towards the H<sub>3</sub> units and interact with one of the H atoms forming almost two H⋯H bonds at 1.15 Å. Concomitantly, the distance in H<sub>2</sub> is lengthened to 0.76 Å. The Bader charges for the H atom in the H<sub>3</sub> and H<sub>2</sub> units and for the Cl atom are +0.16 and +0.014 and –0.48 respectively. In comparison to H<sub>2</sub>Cl the ionicity on both the H and Cl atoms have increased substantially. The plot of the electron localization function (ELF) shown in Fig. 4 shows localized spin paired electron density within the H<sub>3</sub> ring and in the H<sub>2</sub> molecule (ELF over 0.8). Weak pairing is also observed between one of the H in the H<sub>3</sub> ring with the two H atoms of H<sub>2</sub>.

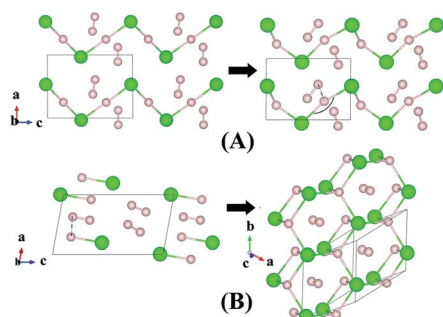


Fig. 3 Crystal structures of hydrogen chlorides. Predicted metastable phase H<sub>3</sub>Cl (A) and H<sub>4</sub>Cl (B) at pressures of 100 to 300 GPa.

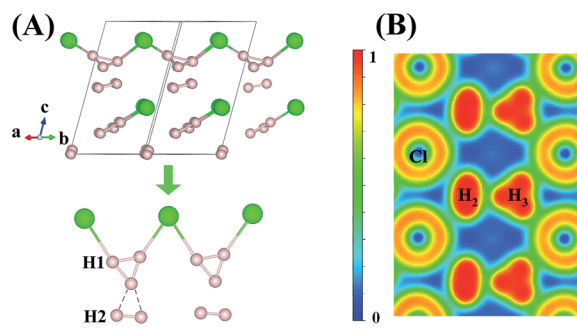


Fig. 4 (A) crystal structure of Cc-H<sub>5</sub>Cl recovered at 100 GPa and its chain style when compressed to 300 GPa. (B) Electron localization function (ELF) maps of the planes where the hydrogen and chloride atoms lie for the Cc structure at 300 GPa.



It is tempting to relate the positively charged  $H_3^+$  unit to an isolated trihydrogen cation  $H_3^+$ .

$H_3^+$  has a perfect triangular structure with H–H bond distance of 0.90 Å. For comparison, at 300 GPa the average intramolecular H–H distance in the  $H_3$  unit in  $H_5Cl$  is 0.87 Å and a total charge of +0.48 ( $3 \times 0.16$ ). In addition, the H–H distance of 0.76 Å in the  $H_2$  unit is only slightly perturbed from the isolated molecule. Therefore, it is not unreasonable to suggest that the high pressure  $H_5Cl$  structure is composed of  $H_3^+$  stabilized in the solid state through primarily ionic interactions with the Cl atoms and secondary weak interactions with a pair of  $H_2$  molecules. To investigate further the properties of the  $H_3^+$  unit in  $H_5Cl$ , the phonon densities of states calculated at 300 GPa are shown in Fig. 5. The low-energy vibrations from 100–500  $cm^{-1}$  are dominated by the Cl atomic motions. The phonon modes in the region from 1800 to 3400  $cm^{-1}$  can be assigned to  $H_3^+$  molecular vibrations and then near 4000  $cm^{-1}$  to the  $H_2$  molecule. The  $H_3^+$  bend vibrations are split into two bands centered at 1800  $cm^{-1}$  and 2000  $cm^{-1}$ . The peak at 3350  $cm^{-1}$  is attributed to the stretching vibration. In comparison, the fundamental frequencies for isolated  $H_3^+$  are  $\nu$  (stretch) =  $3220 \times 48 cm^{-1}$  and  $\nu$  (bend) =  $2545 \times 99 cm^{-1}$ , the latter is a degenerated mode.<sup>31</sup> The vibration frequency is 4350  $cm^{-1}$  for a free  $H_2$  molecule. The main mechanism for the synthesis of  $H_3^+$  by experiment is *via* the chemical reaction:<sup>32</sup>  $H^+ + H_2 \rightarrow H_3^+$ . The concentration of  $H_2^+$  is the limiting factor on the rate of this reaction.  $H_2^+$  can only be produced in interstellar space by the ionization of  $H_2$  by a cosmic ray. In  $H_5Cl$ , the electronegative chlorine atoms acquire electrons from the hydrogen. From previous studies, it is known that high pressure facilitates the transfer of electrons from the more electropositive element into the interstitials of a crystal, forming electrodes. In this case, these electrons, being transferred to the chlorine, are originating from the hydrogen. The formation of multicenter  $H_3 \cdots H_2$  clusters helps to delocalize the positive charge and stabilizes the system. This explains the unexpected formation of  $H_3^+$ -like units in the crystal structure.

The nature of the bonding in the group 17 hydrides at high pressure is different from group 1 and 2 and group 14 hydrides. One observed a gradual shift in the chemical interaction from

electron transfer in electropositive group 1 and 3 compounds to covalent bonding group 14 and finally the ionic bonding in group 17 elements. Although this study was focused on Cl, we anticipate a similar bonding mechanism is applicable to other halogen hydrides.

## Conclusions

We have investigated the phase stability of the HCl– $H_2$  system at high pressure using the PSO algorithm in combination with *ab initio* density functional based electronic calculations. Between 100–300 GPa, two stable phases with the  $H_5Cl$  and  $H_2Cl$  stoichiometries were found. The basic structure of the high pressure phases is similar to the low temperature ambient pressure structure of HCl.  $H_2Cl$  consists of zigzag H–Cl chains and non-interacting  $H_2$  molecules. The most usual and informative finding is that while the chain like structure is preserved in  $H_5Cl$ , the H atoms connecting the Cl in the chains are replaced by units consisting of weakly interacting  $H_2 \cdots H_3$ . The  $H_3^+$  is positively charged and stabilized from the formation of multicenter bonds. The similarity in the local structure, vibrational frequencies and electronic charge compel us to relate the unit to the isolated  $H_3^+$  molecule. It is also found that the effect of pressure on the electronic structure of group 17 hydrides is very different from the more electropositive group 1 and 2 elements: the electron-rich Cl atom and anion do not transfer their electrons into interstitial space of the crystal under very high compression. In fact electrons are removed from the H atoms leading to the formation of cationic clusters that benefit from multicenter bonding.

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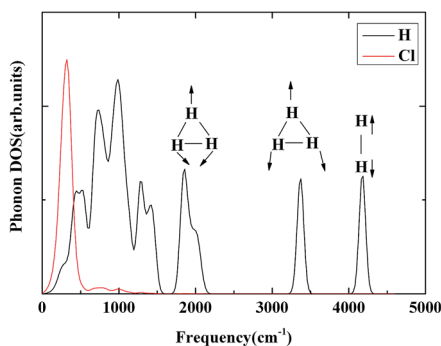


Fig. 5 The phonon densities of states for  $Cc-H_5Cl$  at 300 GPa are shown. The modes corresponding to the triatomic  $H_3^+$  stretch, as well as the  $H_2$  vibron are denoted.



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