Charge-transfer excited states in phosphorescent organo-transition metal compounds: a difficult case for time dependent density functional theory?†

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Light emitting organo-transition metal complexes have found widespread use in the past. The computational modelling of such compounds is often based on time-dependent density functional theory (TDDFT), which enjoys popularity due to its numerical efficiency and simple black-box character. It is well known, however, that TDDFT notoriously underestimates energies of charge-transfer excited states which are prominent in phosphorescent metal–organic compounds. In this study, we investigate whether TDDFT is providing a reliable description of the electronic properties in these systems. To this end, we compute 0–0 triplet state energies for a series of 17 pseudo-square planar platinum(II) and pseudo-octahedral iridium(III) complexes that are known to feature quite different localization characteristics ranging from ligand-centered (LC) to metal–to-ligand charge transfer (MLCT) transitions. The calculations are performed with conventional semi-local and hybrid functionals as well as with optimally tuned range-separated functionals that were recently shown to overcome the charge transfer problem in TDDFT. We compare our results against low temperature experimental data and propose a criterion to classify excited states based on wave function localization. In addition, singlet absorption energies and singlet–triplet splittings are evaluated for a subset of the compounds and are also validated against experimental data. Our results indicate that for the investigated complexes charge-transfer is much less pronounced than previously believed.

1. Introduction

Phosphorescent organo-transition metal complexes play a key role in several modern optoelectronic applications, such as organic light emitting diodes (OLEDs),1–11 light emitting electrochemical cells,12 optical sensors,13–15 photo-catalysts,16,17 as well as cell imaging systems.18–20 For OLED triplet emitters, for example, spin–orbit coupling (SOC) induced by the central heavy metal atom leads to efficient intersystem crossing, fast radiative decay from the lowest triplet state (T1) and thus to efficient harvesting of electrically generated electron–hole pairs.1,4,11 Organo-transition metal compounds are also used in dye-sensitized solar cells,19–21 here the long wavelength part of the solar spectrum can be utilized by SOC allowed singlet–triplet excitations.21 Therefore, one of the crucial quantities for a rational design of all these applications is the transition energy (ΔET1 = ET(T1) – ES0) from the ground to the excited state (or vice versa). Important is also the energy difference between excited singlet and triplet states that are spin–orbit coupled. A small value of this singlet–triplet splitting favors large radiative rates, which for example minimize the roll-off of OLED efficiency due to saturation.24

In the past, pseudo-square planar platinum(II) and pseudo-octahedral iridium(III) complexes have shown to be excellent emitter materials for phosphorescent OLEDs and were synthesized with a variety of organic ligands.1,4,25–29 In order to obtain suitable candidate materials for future applications, a reliable computational screening procedure covering a large number of ligands and combinations thereof would be highly rewarding. As a numerically efficient quantum chemical method that provides useful accuracy for the key quantity ΔET1, time dependent density functional theory (TDDFT) has become the major tool in this regard over the last years. With recent relativistic extensions, spin–orbit interaction can be accounted for and enables the computation of triplet zero-field splittings and radiative rates for phosphorescence.30,31 These parameters can then directly be compared to experimental data. As reviewed by Escudero and Jacquemin,32 also the deactivation pathways of excited phosphors have been the subject of TDDFT simulations recently.
Although TDDFT frequently provides excited state energies with fairly systematic errors of 0.2–0.4 eV, there are also several well documented failures of the theory. One of these, the severe underestimation of charge-transfer excited state energies, seems to undermine the potential use of TDDFT in the field of organo-transition metal photophysics and photochemistry. This is because low lying excited states of these compounds are often characterized as MLCT states, based on experimental observations and also on more sophisticated correlated quantum chemical methods. This shortcoming of TDDFT is well understood by now and we summarize the main arguments below for the later discussion.

Let us assume the system of interest is a closed shell molecule and the excited state is dominated by a transition from the occupied orbital \( i \) into the unoccupied orbital \( a \). The difference between the Kohn–Sham orbital energies associated with this transition is called \( \Delta E_{\text{KS}} \). In this case, the TDDFT eigenvalue problem that leads to the singlet (\( \Delta E_s \)) and triplet (\( \Delta E_t \)) excitation energies may be drastically simplified:

\[
\Delta E_{ST} = \Delta E_{\text{KS}} + K_{ST}
\]

\[
K_S = 2\langle i|\alpha\alpha \rangle + \langle \alpha\beta |f^{\dagger}_{\alpha\beta} |\alpha\alpha \rangle - \langle \beta\beta |\alpha\alpha \rangle - b(\alpha\alpha\alpha) (1)
\]

\[
K_T = \langle \alpha\beta |f^{\dagger}_{\alpha\beta} |\alpha\alpha \rangle - \langle \beta\beta |\alpha\alpha \rangle + b(\alpha\alpha\alpha). (2)
\]

Here \( \langle i|\alpha\alpha \rangle \) denotes a two-electron integral in the Mulliken notation and \( f_{\sigma\tau}^{\dagger} = \frac{\partial^2 E_{\text{KS}}}{\partial \sigma \partial \tau} \) is the functional derivative of the DFT exchange–correlation (xc) energy with respect to the density for spin-up (\( n^+ \)) and spin-down (\( n^- \)) electrons (\( \sigma, \tau \in \{+, -\} \) are spin indices). Eqn (1)–(3) are valid both for functionals that depend on the density only (termed local in the following) or depend on the density and its gradient (i.e., semi-local functionals in the generalized-gradient approximation (GGA)). They hold as well for hybrid functionals that incorporate a fraction \( b \) of Hartree–Fock (HF) exchange. In the limit \( f_{\sigma\tau}^{\dagger} = 0 \) and \( b = 1 \), the equations above reduce to the TD-HF case. For a general charge-transfer excitation, the overlap of orbitals \( i \) and \( a \) is small, such that the correction terms \( K_{ST} \) can be neglected for local and semi-local functionals \( (b = 0) \). The singlet–triplet splitting therefore tends to zero and excitation energies reduce to the Kohn–Sham gap. The latter differs strongly from the quasiparticle gap, defined as the difference of ionization potential (IP) and electron affinity (EA). This is because the electrons in occupied and virtual orbitals experience the same local potential in DFT. This needs to be compared with HF theory, where an additional electron in a virtual orbital feels the potential of all N electrons. Because of the exact cancellation of self-interaction, an electron in the occupied set feels the potential of \( N - 1 \) electrons in contrast. The orbital energy differences \( \Delta E_{\text{KS}} \) for hybrid functionals are therefore much larger as differences from pure functionals and provide reasonable approximations for the quasiparticle gap. In fact, the excitation energy for a transition from donor (D) and acceptor (A) molecules separated by a large distance \( R \) is given by \( \Delta E = \text{IP}^D - \text{EA}^A - 1/R \). In this limit the last term of eqn (2) simplifies to \(-b/R\), which shows that hybrid functionals account at least partially for the electron–hole stabilization which is completely absent for currently available LDA/GGA functionals. Recently, range-separated functionals that exhibit 100% HF exchange at large electron–electron distances gained a lot of popularity. These functionals are designed to suppress the self-interaction error and provide good approximations to quasiparticle gaps. They were also shown to solve the erratic description of long range charge-transfer excitations.

Given the discussion above and the fact that the excited states of phosphorescent organo-transition metal complexes have partial MLCT character, it surprising that several previous case studies show very good agreement with the experiment using simple hybrid functionals like B3LYP. Admittedly, the charge-transfer is not long range inter-molecular but intra-molecular in these systems, but questions remain how general these findings are. This information is of great importance for the rational design and computational screening of OLED emitter materials in order to assess the expected accuracy of a given calculation. In this investigation, we therefore analyze the performance of TDDFT for a comprehensive set of 17 cyclometallated platinum(II) and iridium(III) complexes with high phosphorescence quantum yields. Instead of discussing vertical absorption energies, we compute 0–0 emission energies including zero-point energy corrections to make direct contact with the experimentally relevant quantities. For a subset of the compounds, also the S1 energy and the singlet–triplet splittings \( \Delta E_{ST} = \Delta E_{S1} - \Delta E_{T1} \) are determined. Through a comparison of results for GGA, hybrid and range-separated exchange–correlation functionals, we finally attempt to answer the question, whether metal-to-ligand excitations pose significant problems for modern TDDFT.

2. Experimental

Organotransition metal compounds with Pt(II) and Ir(III) ion centers have been studied extensively in recent years to provide a deeper background, especially for the understanding of emission properties, which are dominantly governed by the lowest excited triplet states and which crucially determine the performance of most opto-electronic devices, in particular of OLEDs. For example, by application of methods of high-resolution spectroscopy, it was possible to determine the 0–0 energies of the substrates I, II, and III of the lowest \( T_1 \) states and the corresponding transition rates with respect to the electronic ground state \( S_0 \). These investigations were particular successful for compounds doped at low concentrations of about 10\(^{-5}\) mol L\(^{-1}\) into adequate crystalline matrices, so-called Shpol’skii matrices. In most cases alkane...
matrices and, in particular, octane were used. The resulting environment around the emitter complexes is relatively rigid and thus, geometry changes upon transitions between the lowest excited triplet state and the ground state are largely prevented. This is displayed in the vibrational satellite structures of the highly resolved emission spectra measured at low temperature. For example, for compound 4 doped into n-octane the Huang–Rhys parameter for the most prominent progression is even smaller than $S = 0.1$.27,64,75

The corresponding studies were usually carried out down to $T = 1.3$ K and techniques of site-selective emission and excitation spectroscopy under variation of temperature and magnetic fields as well as time-resolving methods were applied. The compounds to which it is referred in this study1,27,28,37,64,65,67–75 are summarized in Fig. 1. Table 1 displays the experimental 0–0 substrate averaged transition energies of the T1 state. Moreover, we give the matrix used and the classification as worked out for the respective T1 state.

The classification of the lowest triplet states of the investigated compounds has been based on their zero-field splittings $\Delta E(ZFS)$, their radiative emission decay times, and, if available, to the (normalized) emission intensities of the vibrational satellites of metal–ligand character.28,37,72,74,75 Thus, T1 states with $\Delta E(ZFS)$ values < 2 cm$^{-1}$ are assigned to a $^3LC(\pi\pi^*)$ character. To have a course guide line, we classify states that show splitting values up to about 10 cm$^{-1}$ or 20 cm$^{-1}$ as $^3LC(\pi\pi^*)$/3MLCT(d$\pi^*$) states and for the range of about 20 cm$^{-1}$ < $\Delta E(ZFS)$ < 50 cm$^{-1}$, we use the notation $^3MLCT(d\pi^*)$/3LC(\pi\pi^*), while states with

![Fig. 1 Chemical structures of compounds discussed. Complexes 11 and 13 are occasionally also abbreviated as Pt(bzq)(dpm) and Pt(bzq)$_2$, respectively.](image)
Table 1  Triplet energies $\Delta \varepsilon_{T^0}^0$ (6–311G*) for different exchange–correlation functionals compared to experiment. All energies are given in eV. A characterization of the dominant single particle excitation together with the percental participation of the metal atom according to a Löwdin population analysis is given in the third column. Values in parentheses are for the PBE/6–311G* and B3LYP/6–311G* functional, respectively. Metal participations are only shown beyond the threshold of 8% for PBE and 9% for B3LYP. For the LC–PBE functional, the optimal range separation parameter $\gamma$ [A$_h^{-1}$] is given in parentheses. Experimental $\Delta \varepsilon_{T^0}^0$ values have been measured in a n–octane matrix, apart from 12 (CH$_2$Cl) and 13 (n–decane). References to the original articles are given in square brackets. The last two columns provide a classification of the excited states based on experimental and theoretical data, respectively, according to the criteria described in the main text.

<table>
<thead>
<tr>
<th>#</th>
<th>Compound</th>
<th>$S_0 \rightarrow T_1$ transition</th>
<th>PBE B3LYP</th>
<th>LC–PBE ($\gamma$)</th>
<th>Exp.</th>
<th>Class [exp.]</th>
<th>Class [theo.]</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Pt(qol)$_2$</td>
<td>5d</td>
<td>$\pi_{qol} \rightarrow \pi^{*}_{qol}$</td>
<td>1.48</td>
<td>1.85</td>
<td>1.99 (0.21)</td>
<td>1.91 (ref. 65)</td>
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<tr>
<td>2</td>
<td>Pt(ppy$_2$Bu$_2$)</td>
<td>5d</td>
<td>$\pi_{pppy} \rightarrow \pi^{*}_{pppy}$</td>
<td>1.47</td>
<td>1.94</td>
<td>1.97 (0.16)</td>
<td>1.99 (ref. 37 and 98)</td>
</tr>
<tr>
<td>3</td>
<td>Pt(piq)(acac)</td>
<td>5d</td>
<td>$\pi_{pic} \rightarrow \pi^{*}_{pic}$</td>
<td>1.90</td>
<td>2.07</td>
<td>2.18 (0.20)</td>
<td>2.09 (ref. 99)</td>
</tr>
<tr>
<td>4</td>
<td>Pt(2-thpy)$_2$</td>
<td>5d</td>
<td>$\pi_{2-thpy} \rightarrow \pi^{*}_{2-thpy}$</td>
<td>1.88</td>
<td>2.11</td>
<td>2.20 (0.29)</td>
<td>2.13 (ref. 64)</td>
</tr>
<tr>
<td>5</td>
<td>Pt(bhq)(acac)</td>
<td>5d</td>
<td>$\pi_{thpy} \rightarrow \pi^{*}_{thpy}$</td>
<td>2.12</td>
<td>2.19</td>
<td>2.06 (0.40)</td>
<td>2.23 (ref. 71)</td>
</tr>
<tr>
<td>6</td>
<td>Ir(pbt)$_2$</td>
<td>5d</td>
<td>$\pi_{pbt} \rightarrow \pi^{*}_{pbt}$</td>
<td>1.93</td>
<td>2.29</td>
<td>2.28 (0.16)</td>
<td>2.26 (ref. 37)</td>
</tr>
<tr>
<td>7</td>
<td>Pt(dpipy)(CO)</td>
<td>5d</td>
<td>$\pi_{dipipy} \rightarrow \pi^{*}_{dipipy}$</td>
<td>2.06</td>
<td>2.32</td>
<td>2.46 (0.21)</td>
<td>2.38 (ref. 37)</td>
</tr>
<tr>
<td>8</td>
<td>Pt(ppy$_2$fluoren)</td>
<td>5d</td>
<td>$\pi_{ppy} \rightarrow \pi^{*}_{ppy}$</td>
<td>2.05</td>
<td>2.42</td>
<td>2.45 (0.18)</td>
<td>2.41 (ref. 37 and 98)</td>
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<td>9</td>
<td>Pt(pppy$_2$C$_2$)</td>
<td>5d</td>
<td>$\pi_{pppy} \rightarrow \pi^{*}_{pppy}$</td>
<td>2.05</td>
<td>2.48</td>
<td>2.67 (0.27)</td>
<td>2.42 (ref. 37 and 98)</td>
</tr>
<tr>
<td>10</td>
<td>Pt(pppy)$_2$</td>
<td>5d</td>
<td>$\pi_{pppy} \rightarrow \pi^{*}_{pppy}$</td>
<td>2.05</td>
<td>2.48</td>
<td>2.67 (0.29)</td>
<td>2.43 (ref. 37)</td>
</tr>
<tr>
<td>11</td>
<td>Pt(bhq)(dpym)</td>
<td>5d</td>
<td>$\pi_{bhbq} \rightarrow \pi^{*}_{bhbq}$</td>
<td>2.02</td>
<td>2.40</td>
<td>2.28 (0.36)</td>
<td>2.44 (ref. 37 and 73)</td>
</tr>
<tr>
<td>12</td>
<td>Ir(ppy)$_2$</td>
<td>5d</td>
<td>$\pi_{ppy} \rightarrow \pi^{*}_{ppy}$</td>
<td>2.05</td>
<td>2.53</td>
<td>2.47 (0.16)</td>
<td>2.45 (ref. 70)</td>
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<tr>
<td>13</td>
<td>Pt(bhq)$_2$</td>
<td>5d</td>
<td>$\pi_{bhbq} \rightarrow \pi^{*}_{bhbq}$</td>
<td>1.99</td>
<td>2.46</td>
<td>2.55 (0.28)</td>
<td>2.51 (ref. 37)</td>
</tr>
<tr>
<td>14</td>
<td>Pt(4,6-dFppy)$_2$</td>
<td>5d</td>
<td>$\pi_{4,6-dFppy} \rightarrow \pi^{*}_{4,6-dFppy}$</td>
<td>2.20</td>
<td>2.57</td>
<td>2.72 (0.26)</td>
<td>2.56 (ref. 67)</td>
</tr>
<tr>
<td>15</td>
<td>Pt(pppy)(acac)</td>
<td>5d</td>
<td>$\pi_{pppy} + \pi_{acac} \rightarrow \pi^{*}_{pppy}$</td>
<td>2.29</td>
<td>2.57</td>
<td>2.43 (0.41)</td>
<td>2.56 (ref. 4 and 73)</td>
</tr>
<tr>
<td>16</td>
<td>Pt(dpFthiq)(dpym)</td>
<td>5d</td>
<td>$\pi_{dpFthiq} + \pi_{dpym} \rightarrow \pi^{*}_{dpFthiq}$</td>
<td>2.48</td>
<td>2.69</td>
<td>2.80 (0.21)</td>
<td>2.71 (ref. 37)</td>
</tr>
<tr>
<td>17</td>
<td>Pt(ppz)$_2$</td>
<td>5d</td>
<td>$\pi_{ppz} \rightarrow \pi^{*}_{ppz}$</td>
<td>2.66</td>
<td>2.95</td>
<td>3.11 (0.28)</td>
<td>2.85 (ref. 100)</td>
</tr>
</tbody>
</table>

Equation (4)

$$\frac{1}{r} = \frac{1 - \text{erf} (\gamma r)}{r} + \text{erf} (\gamma r).$$

The first term is a Coulomb operator decaying to zero on a length scale of $\approx 1/\gamma$ and is therefore short-ranged (SR), while the second term dominates at large $r$ accounting for the long-range (LR) behavior. This gives rise to a decomposition of the xc energy functional according to

$$E_{xc} = E_{xc}^{SR} + E_{xc}^{LR} + E_{xc}^{SDFT}.$$  

In the case of LC–PBE, $E_{xc}^{SR}$ is the short-range form of the gradient-corrected PBE exchange functional, and $E_{xc}^{LR}$ denotes the Hartree–Fock exchange energy evaluated with the long-range part of the interaction in eqn (4), while the correlation part $E_{xc}^{SDFT}$ is left unchanged with respect to the usual form of PBE. There are different strategies to determine the value of the parameter $\gamma$. One possibility is choosing it to minimize the deviation of various molecular properties with respect to experimental or accurate first principles data on large test sets (see, e.g., ref. 81 and 82), leaving the parameter fixed in further applications. Another route is the system specific tuning proposed by Baer and co-workers, which we will follow here. Given that DFT with the exact exchange–correlation functional should obey Koopmans' theorem, one can find the optimal $\gamma$ for the compound in question by minimizing the following error function:

$$\frac{1}{r} = \frac{1 - \text{erf} (\gamma r)}{r} + \text{erf} (\gamma r).$$
\[ \Delta \text{IP}(\gamma) = |e_{\text{HOMO}}^\gamma - [E_{\text{tot}}^\gamma(N) - E_{\text{tot}}^\gamma(N-1)]|, \]

where \( e_{\text{HOMO}}^\gamma \) denotes the orbital energy of the highest occupied molecular orbital (HOMO) and \( E_{\text{tot}}^\gamma(N) \) and \( E_{\text{tot}}^\gamma(N-1) \) stand for the total energy of the charge neutral system with \( N \) electrons and the ionized one with \( N - 1 \) electrons, respectively. In this study the latter is obtained by means of a spin unrestricted calculation. The minimization was carried out using a golden section search. At the minimum, the remaining error \( \Delta \text{IP} \) was found to be 0.06 eV on average and less than 0.3 eV maximally for all compounds studied. Besides the LC-PBE functional with optimal range-separation parameter, we also performed calculations using a fixed value of \( \gamma = 0.3a_0^{-1} \) in order to assess the impact of the tuning procedure.

For all mentioned functionals, linear response TDDFT calculations (also known as Casida approach) were performed in the adiabatic approximation. Depending on the actual value of \( \gamma \), the range-separated functionals may incorporate a large fraction of Hartree–Fock exchange. As shown by Tozer and Brédas, triplet instabilities in the ground state may lead to a significant underestimation of triplet excited state energies in such a case, especially in large \( \pi \)-conjugated systems. Since several of the ligands investigated in this study fall into this class, we also perform calculations in the Tamm–Dancoff approximation, which is known to alleviate these problems. Metal atoms were treated at the same level as in the ground state, while for the remaining atoms a split-valence basis set of triple-\( \zeta \) quality plus polarization functions (6-311G*) was employed. For a subset of the studied compounds also calculations including diffuse functions for the ligands (6-311+G**) and using the triple-\( \zeta \) basis LANL2DZ(f) for the metal have been performed. The results in the ESI (Table S4†) indicate a modest gain in accuracy (<0.1 eV).

Earlier TDDFT studies on transition metal complexes also indicate that solvent effects play a crucial role. For simulations in the gas phase, it was frequently observed that the ligand-to-ligand charge-transfer character is exaggerated, with a concomitant underestimation of excitation energies with respect to experiment. Here we employ the COSMO solvent model as implemented in NWChem with a dielectric constant of 1.95 corresponding to \( n \)-octane. This is the solvent that was used in the majority of measurements that are reported here. In order to estimate the influence of the solvent model we also tested the so-called solvation model based on density (SDM, solvent octane) put forward by Truhlar and co-workers and implemented in version 6.5 of NWChem. The corresponding results in the ESI (Table S5†) show only very minor changes (<0.01 eV) with respect to the COSMO model.

Based on Kasza’s rule, we limit the investigation of luminescence energies to the lowest singlet and triplet state, respectively. Also, structural relaxation in the excited state is not taken into account. This reflects the experimental situation, where the matrices provide a rigid environment for the emitter molecule. Admittedly, this rigidity does not rule out the possibility of inward relaxations that reduce the occupied volume. Given the difficulties in modelling the precise morphology of the molecular environment, we discard this possibility. In order to estimate 0–0 transitions \( \Delta E_{0-0} \), we therefore compute vertical absorption energies \( \Delta E_{\text{vert}} \) at the optimized \( S_0 \) geometry which are corrected according to:

\[ \Delta E_{0-0} = \Delta E_{\text{vert}} + \text{ZPE}_{T_1} - \text{ZPE}_{S_0}. \]

(see also Fig. 2).

Here \( \text{ZPE} \) denotes the unscaled B3LYP/6-31G* zero-point energy at the minimum of the \( T_1 \) and \( S_0 \) potential energy surfaces, respectively. The \( T_1 \) geometry optimization was carried out at the unrestricted Kohn–Sham level with the \( S_0 \) minimum as initial geometry. Singlet excited state geometry optimizations based on TDDFT are computationally still very demanding. In addition, the problem of state crossing is frequently encountered during the optimization, especially for the organo-transition metal complexes discussed here with a relatively dense set of low lying states. Due to the these difficulties in obtaining \( \text{ZPE}_{S_0} \), we applied the correction protocol of eqn (7) also for singlet excited states, coarsely assuming parallelity of the \( T_1 \) and \( S_1 \) potential energy surfaces. Results for the correction terms and more computational details are provided in the ESI†.

4 Results and discussion

### 4.1 Triplet state emission

We start with an examination of the computed triplet emission energies. Table 1 lists the results, which are graphically displayed in Fig. 3. In addition, Table 2 provides a statistical summary for the full set of complexes. All studied exchange-correlation functionals are able to provide the general energetical ordering of the luminescence energies, with large discrepancies in absolute values. Turning first to the results for the local PBE functional, we find that \( T_1 \) energies are systematically lower than experimental values by 0.35 eV. This underestimation of triplet energies is typical for local functionals.

![Fig. 2 Potential energy surfaces for ground and excited states indicating the key quantities calculated.](image-url)
although the actual amount is slightly smaller than reported in
earlier benchmark studies on organic chromophores. The
PBE results may be further analyzed by investigating the CI
expansion of the excited state $|\Phi\rangle$ in terms of singly excited
determinants

$$|\Phi\rangle = \sum_{ia} d_{ia} |\phi_i\rangle.$$  (8)

Strictly speaking, TDDFT does not provide direct access to
the excited state wave function. As shown by Casida, eqn (8)
might still be used for diagnostic purposes as an approximation
to the true excited state. The coefficients $d_{ia}$ are readily avail-
able from the solution of the eigenvalue equations in TDDFT.
For all complexes studied here, the HOMO–LUMO transition is
the dominating excitation for PBE in the expansion of eqn (8) with
participation ratios of more than 93%. This allows us to estimate the two electron integral $(ia)^{n} - (ia)^{p}$ according to eqn (1) from the difference of the excitation energy and Kohn–Sham energy gap. We obtain consistent values of roughly 0.1 eV
which are smaller than corresponding integrals for $\pi \rightarrow \pi^*$ and
n$ \rightarrow \pi^*$ transition in typical organic molecules. This indicates a small but non-vanishing overlap between the HOMO and LUMO orbitals and hence, a partial charge-transfer character of the transition. These findings are in line with the localization of the frontier orbitals that are depicted in the ESI (Fig. S1 to S17†).

The excitations may be broadly classiﬁed as a metal–ligand to
ligand charge-transfer. A more quantitative measure is obtained
from a Löwdin analysis of the atomic population ($P_i^n$) for a
given molecular orbital $i$:

$$P_i^n = \sum_{\nu} \left( \sum_{\alpha} S_{\nu\alpha} \xi_{\nu\alpha} \right)^2 \quad \text{with} \quad \sum_{\nu} P_i^n = 1, \quad \text{for all} \quad i.$$  (9)

Eqn (9) contains the square root of the overlap matrix $S$
between atom-centered basis functions and the molecular orbital coefficients $c_{\nu\alpha}$. As it is well known, the division of molecular density into atomic contributions is not unique. Löwdin populations provide a better estimate for charge
distributions than the more common Mulliken scheme for extended basis sets like the ones used in this study. They are
used here as a simple and robust measure of wave function localization providing consistent results for a given basis set
and functional.

In Table 1 the populations of the central metal atom are
listed for the PBE and B3LYP functional. As can be seen, the
HOMO is delocalized over the central metal atom and one or
more ligands, while the LUMO is a $\pi^*$ orbital on the same ligand(s) in the majority of cases (compounds 7 and 17 show some Pt participation in the LUMO). Unexpectedly, the computed $d$-orbital contribution to the HOMO is larger in PBE than in B3LYP by about 10%. This is surprising as the self interaction error present in PBE (and reduced in B3LYP) gives usually rise to an overly delocalized electron density and exaggerated covalency. Given this fact, the charge-transfer character of the triplet states should also be larger for PBE and lead to larger deviations from experiment.

Table 2 Mean signed error (MSE = $\frac{1}{n} \sum_{i}^n (E_i^{\text{TDDFT}} - E_i^{\text{exp}})$) and root
mean square deviation (RMS = $\left(\frac{1}{n} \sum_{i}^n (E_i^{\text{TDDFT}} - E_i^{\text{exp}})^2\right)^{\frac{1}{2}}$) of TDDFT
energies ($E_i^{\text{TDDFT}}$) with respect to experiment ($E_i^{\text{exp}}$) for the sets pre-

<table>
<thead>
<tr>
<th></th>
<th>PBE</th>
<th>B3LYP</th>
<th>Tuned</th>
<th>TDA</th>
<th>$\gamma = 0.3a_0^{-1}$</th>
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<tbody>
<tr>
<td>$\Delta E_T^{0.0}$</td>
<td>MSE</td>
<td>0.33</td>
<td>0.00</td>
<td>0.06</td>
<td>0.28</td>
</tr>
<tr>
<td></td>
<td>RMS</td>
<td>0.35</td>
<td>0.05</td>
<td>0.14</td>
<td>0.32</td>
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<tr>
<td>$\Delta E_S^{0.0}$</td>
<td>MSE</td>
<td>0.44</td>
<td>0.09</td>
<td>0.41</td>
<td>0.47</td>
</tr>
<tr>
<td></td>
<td>RMS</td>
<td>0.46</td>
<td>0.10</td>
<td>0.46</td>
<td>0.53</td>
</tr>
<tr>
<td>$\Delta E_T^{0.0}$</td>
<td>MSE</td>
<td>0.11</td>
<td>0.13</td>
<td>0.37</td>
<td>0.26</td>
</tr>
<tr>
<td></td>
<td>RMS</td>
<td>0.14</td>
<td>0.13</td>
<td>0.46</td>
<td>0.31</td>
</tr>
</tbody>
</table>

Coming to the results for the B3LYP functional, one observes
in Fig. 3 an excellent agreement with the experimental data with a
RMS error of only 0.05 eV, which is even smaller than the deviation found for supposedly simpler organic systems (namely hydrocarbons, heterocycles and carbonyl compounds) with this functional. Compared to the local PBE, a higher number of singly excited determinants mixes into the excited state wave function. For complex 5, as an example, the contribution of the most important determinant drops to 56%.$\dagger$ This is due to the fraction of exact exchange in B3LYP which leads to larger matrix elements $K_{ij}$ and hence also increased coupling of individual single-particle transitions. The Kohn–Sham gap $\Delta E_{ia}$ likewise increases substantially by 1.3–1.6 eV due to the exact exchange. In the computation of the final emission energies, both effects

$\dagger$ In such a situation the analysis is better based on the concept of natural transition orbitals introduced by Martin, which is not yet implemented in NWChem.
cancel to a large degree (see eqn (3), $K_T < 0$) such that the B3LYP energies are only modestly larger than the PBE ones.

Based on the Löwdin population analysis mentioned above, we propose a simple guideline to classify the excited states as being ligand-centered, metal-to-ligand charge-transfer like or extensive mixtures of these basics types. To this end we consider the difference density $\Delta \rho(r) = \rho_S(r) - \rho_T(r)$, which simplifies to $\Delta \rho(r) \approx |\psi_0(r)|^2 - |\psi_\alpha(r)|^2$ if the triplet state is well described by a single-particle transition from orbital $\psi_\alpha$ to $\psi_0$. A Löwdin projection on the central metal atom $M$ then leads to a measure $n_{CT} = P_M - P_M^M$ of the fractional number of electrons that take part in the metal to ligand transition (cf. eqn (9)). This quantity may be used to estimate the charge-transfer character of a given excitation according to:

$$
\begin{array}{ll}
\text{LC} & \text{for } 0 < n_{CT} \leq 0.2 \\
\text{LC/MLCT} & \text{for } 0.2 < n_{CT} \leq 0.35 \\
\text{MLCT/LC} & \text{for } 0.35 < n_{CT} \leq 0.5 \\
\text{MLCT} & \text{for } 0.5 < n_{CT}.
\end{array}
$$

As seen in Table 1, this assignment correlates rather well with the experimentally derived classification and lends further support to the quality of the B3LYP results. With adapted limits for the different excitation types, a similar procedure might also be applied at the PBE level. The agreement with experiment, however, turns out to be inferior in this case. A more refined measure that takes not only the dominant determinant into account could be based on an analysis of the difference density and the transition density, which both are readily available in DFT/TDDFT. Here we use the parameter $n_{CT}$ as an easily accessible quantity which allows for a quick and pragmatic classification of the excited state.

Despite the general agreement with measurements in terms of emission energies and excitation character, it should be noted that there are still remaining qualitative discrepancies. The d-orbital participation seems to be exaggerated by DFT in general. According to eqn (10), excitations with $n_{CT}$ up to 0.2 are still classified as $^3$LC, although the d-orbital participation is experimentally found to be almost negligible. In line with this, zero field splittings computed by TDDFT including SOC are slightly, but systematically, overestimated with respect to experiment. In our study, the neglect of structural relaxation in the excited state might also contribute to the magnified metal character.

Before discussing the performance of the range-separated LC-PBE functional, a short digression on the optimal values for the parameter $\gamma$ seems to be appropriate. Although $\gamma$ is practically found by application of the IP criterion (eqn (6)), this parameter should reflect the electronic structure of the system and is expected to depend directly on quantities like the electron density or microscopic dielectric function. In fact, a clear dependence of the optimal range-separation parameter with the conjugation length of polymers was found. Since the conjugation length strongly influences the optical gap in polymers, it is interesting to verify whether there is a direct link also in the present organo-transition metal compounds. Inspection of Table 1 reveals that there is actually no correlation between the range-separation parameter and emission energies. The values of $\gamma$ vary between 0.16$a_0^{-1}$ and 0.41$a_0^{-1}$ in a rather arbitrary fashion. The LC-PBE results for the emission energies are on average slightly less accurate than the B3LYP results with a RMS deviation of 0.14 eV (cf., Table 2). Interestingly, the LC-PBE functional with a fixed value of $\gamma = 0.3a_0^{-1}$ performs only slightly worse than the tuned variant. Only for compound 2 a clear benefit of the tuning procedure is discernible.

### 4.2 Singlet excitation energies and singlet–triplet gap

For most organo-transition metal complexes, fluorescence is difficult to detect due to the strong spin–orbit coupling and concomitant fast inter-system crossing. Only under suitable conditions, it is possible to identify the 0–0 transition energies of S$_0$ to S$_1$ transitions even at low temperature. Examples are summarized in Table 3. The data result from highly resolved and site-selectively detected excitation spectra measured at $T = 1.3$ K. However, very frequently, the corresponding transitions are hidden under overlapping transitions that belong to other sites, to other electronic states lying in this energy range, and/or to vibrational and phonon satellites that refer to the lower lying triplet substates. Moreover, the corresponding transitions are lifetime-broadened and thus, smeared out. Consequently, the possibility to measure a fairly well resolved 0–0 transition corresponding to S$_0$ to S$_1$ is very restricted.

<table>
<thead>
<tr>
<th>#</th>
<th>Compound</th>
<th>PBE</th>
<th>B3LYP</th>
<th>LC-PBE (tuned)</th>
<th>Exp.</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Pt(qol)$_2$</td>
<td>1.74</td>
<td>2.39</td>
<td>2.66</td>
<td>2.33</td>
</tr>
<tr>
<td>2</td>
<td>Pt(ppy$_2$-Bu$_2$S)</td>
<td>1.67</td>
<td>2.20</td>
<td>2.22</td>
<td>2.16</td>
</tr>
<tr>
<td>3</td>
<td>Pt(2-thpy)$_2$</td>
<td>2.08</td>
<td>2.64</td>
<td>3.03</td>
<td>3.03</td>
</tr>
<tr>
<td>4</td>
<td>Pt(2-ppy)$_2$</td>
<td>2.08</td>
<td>2.64</td>
<td>3.03</td>
<td>3.03</td>
</tr>
<tr>
<td>5</td>
<td>Pt(dpqpy)$_2$</td>
<td>2.60</td>
<td>2.63</td>
<td>2.82</td>
<td>2.58</td>
</tr>
<tr>
<td>6</td>
<td>Pt(dpqpy)$_2$</td>
<td>2.22</td>
<td>2.63</td>
<td>2.82</td>
<td>2.58</td>
</tr>
<tr>
<td>7</td>
<td>Pt(dpppy)$_2$</td>
<td>2.34</td>
<td>2.97</td>
<td>3.36</td>
<td>2.86</td>
</tr>
</tbody>
</table>

The radiative lifetime ($\tau$) is derived from the computed oscillator strengths according to the Strickler–Berg relationship including the effect of the dielectric environment. References for the experimental data are given in square brackets.
For the theoretical analysis it should also be kept in mind that the $\Delta E_{S0}^{0} - \Delta E_{T0}^{0}$ values were approximated using the zero-point energy values of the $T_1$ potential energy surface. Although a statistical analysis should be performed with caution for such a small number of test cases, we also report the average errors for $\Delta E_{S0}^{0} - \Delta E_{T0}^{0}$ and the singlet–triplet gap $\Delta E_{ST} = \Delta E_{S1}^{0} - \Delta E_{T1}^{0}$ in Table 2. Note that the first excited singlet and triplet state are not necessarily strongly coupled by the spin–orbit interaction.\textsuperscript{30,73,106} Strictly speaking, the parameter $\Delta E_{ST}$ is in these cases not crucial for radiative lifetimes and OLED device performance. We include it here to obtain a broader picture of the TDDFT accuracy for organo-transition metal complexes.

Turning to the results, the gradient-corrected PBE functional strongly underestimates transition energies, but it does so consistently for both triplets and singlets. As a result, the computed singlet–triplet gap $\Delta E_{ST}$ is in surprisingly good agreement with the experiment. Considering eqn (1)–(3), this can be traced back to the cancellation of the Kohn–Sham gap, which is too small to provide accurate absolute singlet and triplet energies. The exchange integral $(i\alpha|i\alpha)$ that remains after subtraction is qualitatively correct also at the PBE level. In contrast, the hybrid B3LYP yields reasonable singlet energies with an RMS deviation of 0.10 eV in good agreement with earlier more extensive benchmarks on vertical singlet excitations.\textsuperscript{91,111} The singlet–triplet gap is systematically overestimated by only 0.13 eV, which allows for a reliable determination of this important parameter in large scale computational screenings.

Coming to the tuned LC-PBE functional, we find a strong overestimation of singlet energies and a pronounced error for the singlet–triplet gap. These trends are likewise already documented in the literature for vertical excitations of organic compounds.\textsuperscript{30,99,111} For singlet excitations, the tuning of the LC-PBE functional turns out to be beneficial and reduces the error compared to a fixed range-separation parameter significantly. Since $\Delta E_{ST}$ is strongly dependent on the amount of HF exchange in the functional, it is not surprising that LC-PBE with 100% long-range unscreened exchange considerably overestimates this quantity with respect to the experiment. Comparison of the radiative lifetimes between the different methods reveals that PBE exhibits shorter values compared to B3LYP and LC-PBE, for 14 the difference even amounts to 2–3 orders of magnitude. In their study of TDDFT oscillator strengths for small organic molecules, Caricato et al.\textsuperscript{112} find similar trends and show that range-separated functionals (like LC-PBE) provide results close to higher level theory. In summary it can be stated that B3LYP outperforms the other studied functionals also in the description of singlet excited states.

5. Conclusion

The objective of this article was to investigate whether TDDFT in its current implementations is accurate enough to provide a reliable and general description of optical properties of organo-transition metal complexes. Although a statistical evaluation of the results is inevitable in such a context, we also tried to rationalize the general trends by analyzing the structure of the TDDFT eigenvalue equations for the different functionals. The main finding of our study is that the hybrid B3LYP functional is an excellent choice and provides a balanced treatment of LC, LC/MLCT, MLCT/LC, and MLCT excited states. Somewhat surprising, range-separated functionals do not provide a clear advantage even for states with strong intra-molecular charge-transfer character. In addition, the tuning of the range-separation parameter leads to improvements only for singlet excited states. If the interest is only in singlet–triplet gaps, the semi-local PBE functional might serve as a cost effective alternative to B3LYP.

With respect to the computational protocol, we find that vibrational contributions in the form of zero-point energies are necessary to match the experimental $\Delta E_{S0}^{0} - \Delta E_{T0}^{0}$ energies, while excited state relaxation is not crucial for emitters embedded in a rigid matrix. The B3LYP average error of only 0.05 eV for triplet emission energies is highly encouraging. This paves the way for further \textit{in silico} pre-screening of possible OLED materials. We hope that the extended experimental and theoretical data set provided in this article might also be useful also in the development of novel exchange–correlation functionals which aim at a coherent description of valence, Rydberg and charge-transfer excited states in real world materials.

Our results show that charge transfer excitations in the investigated compounds do not pose a significant challenge for TDDFT. This is mainly because transitions that are often characterized as MLCT states actually involve transitions out of a strongly hybridized metal d-orbital. As mentioned in Section 4.1, there are even indications that the calculated d-orbital contribution is overestimated. This calls for further studies which connect calculated metal participations, SOC matrix elements and singlet–triplet gaps with measurements of zero-field splittings and radiative lifetimes. Such a combination of theory and experiment should be extremely helpful in the detailed understanding and further optimization of metal-organic emitters.

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References


