Introduction

The self-assembly of amphiphilic molecules is fundamental in nature and everyday life; the membranes of living cells are comprised of self-assembled phospholipids and countless consumer products contain self-assembled surfactants acting as detergents, emulsifiers and foaming agents. Consequently, the solution self-assembly of amphiphilic molecules is an area of significant research.1–5 A small molecule amphiphile consists of a hydrophobic tail and a hydrophilic head group. Amphiphiles self-assemble in selective solvents to minimize unfavourable hydrophobic–hydrophilic interactions and the resulting morphology of the self-assembly is determined by the packing parameter, \( p = \nu/a_o l_c \), where \( \nu \) is the volume of the hydrophobic tail, \( a_o \) is the contact area of the hydrophilic head group and \( l_c \) is the length of the hydrophobic tail. Spherical micelles are favoured when \( p < 1/3 \), cylindrical micelles are favoured when \( 1/3 < p < 1/2 \) and vesicles when \( 1/2 < p < 1 \).6

The development of living and controlled polymerization techniques has allowed the preparation of well-defined amphiphilic polymers that will undergo analogous self-assembly in a selective solvent to yield well-defined aggregates. These self-assembled polymeric aggregates exhibit greater stability than small molecule aggregates as a result of their superior mechanical and physical properties7 and consequently polymeric self-assemblies have been utilized as catalytic nanoreactors,8–10 drug delivery vehicles11–18 and molecular imaging agents.19,20 Among the possible architectures of amphiphilic polymers, linear block copolymer systems are by far the most studied and as a result the self-assembly of linear block copolymers is well established and has been extensively reviewed.11,18,21–24

A wide range of aggregate morphologies are accessible via the self-assembly of linear block copolymers,25 including spherical and cylindrical micelles, vesicles and lamellae, as well as morphologies that possess greater complexity, such as multi-compartment micelles,26,27 helical micelles28 and multi-lamellar “onion” vesicles.29 The resulting morphology of a block copolymer aggregate is determined by three factors which govern the free energy of the system: the degree of stretching of the core forming block, the interfacial tension between the core and the solvated corona and the repulsive interactions of the corona chains.11,21 Consequently, the morphology of polymeric assemblies can be influenced by a wide range of variables that affect these three factors, including polymer composition, concentration, water content, assembly technique and the presence of additives. Furthermore, block copolymer assemblies may be defined as either thermodynamically stable or kinetically frozen, depending on the mobility of the constituent polymer chains with respect to unimer exchange and the employed method of assembly.30,31

Polymer architecture is also known to influence self-assembly behaviour, however, in contrast to the self-assembly of linear block copolymers, reports of the self-assembly of non-linear amphiphilic polymers are limited.32–39 The major advancement of controlled and living polymerization techniques has enabled the preparation of a range of well-defined non-linear polymer architectures, including star,33,40–42 graft,43–47 branched48–51 and cyclic.52–56 Of these architectures, cyclic polymers are perhaps the least explored as a consequence of the difficulties encountered during both their synthesis and purification. However, despite these difficulties cyclic polymers are of significant interest as a result of the...
unique properties they exhibit in comparison to analogous linear polymers.\textsuperscript{54,57} Interest in the solution self-assembly of cyclic polymers began in the mid 1990s,\textsuperscript{58} not long after initial investigations into the solution self-assembly of linear block copolymers. However, as a consequence of the synthetic difficulties encountered in the preparation of well-defined, high purity cyclic polymers, this area of research remained comparatively limited. Recent developments in the preparation of cyclic polymers\textsuperscript{55} have allowed these synthetic difficulties to be overcome and the self-assembly of cyclic polymers has received increasing attention. This review will begin with a brief introduction to the synthesis of cyclic polymers and the unique properties that cyclic polymers exhibit in comparison to their linear counterparts. An overview of the limited but growing field of cyclic polymer self-assembly will follow in an attempt to elucidate the effect of cyclization on polymer aggregation. This overview will discuss the assembly of amphiphilic cyclic block copolymers, in addition to more complex amphiphilic cyclic architectures, highlighting topological differences observed in comparison to the self-assembly of equivalent linear systems where appropriate.

**Synthesis of cyclic polymers**

The existence of cyclic polymers has been long established in nature with the discovery of circular DNA\textsuperscript{59} and in synthetic chemistry as cyclic contaminants in step-growth polymerization. Indeed, original synthetic methods to prepare cyclic polymers were based upon the ring-chain equilibrium of poly-(dimethylsiloxane),\textsuperscript{60,61} where cyclic species were separated from linear polymers through laborious fractional precipitations and preparative size exclusion chromatography (SEC).\textsuperscript{62} Despite the obvious limitations of this method, it allowed the first investigation of cyclic polymer properties, verifying the unique behaviour of cyclic topologies.

Recent synthetic breakthroughs have since allowed the preparation of well-defined cyclic polymers in the absence of linear impurities, as well as a diverse range of more complex cyclic architectures. There are now two main approaches to prepare cyclic polymers; ring-closure,\textsuperscript{63–65} and ring-expansion\textsuperscript{66} (Fig. 1). The synthesis of cyclic polymers has been extensively reviewed,\textsuperscript{52–55,67} therefore here only an overview of these techniques will be given.

Ring-closure techniques involve the coupling of the reactive chain ends of a linear polymer to yield a cyclic polymer (Fig. 1(a)). Ring-closure can be achieved through the bimolecular homodifunctional coupling of a linear polymer with a small molecule linker (Fig. 1(a)-1 and (a)-2) or the unimolecular homodifunctional (Fig. 1(a)-3) or heterodifunctional coupling of a linear polymer (Fig. 1(a)-4). The development of living and controlled polymerization techniques has allowed the preparation of polymers with high chain end functionality, enabling the success of these techniques. Furthermore, in all ring-closure techniques, the use of highly efficient
couples. In contrast, for unimolecular ring-closure techniques, electrostatic interactions between the linear polymer chain ends and small molecule linker is needed. To overcome the limitations of bimolecular ring-closure, electrostatic interactions between the linear polymer chain ends and small molecule linker can be used to template cyclization (Fig. 1(a)-2).68 In contrast, for unimolecular ring-closure techniques (Fig. 1(a)-3 and (a)-4), high dilution alone is required to suppress polymer–polymer coupling side reactions, as such this method has been highly successful in the preparation of well-defined cyclic polymers and is generally favored over bimolecular ring-closure.

Ring-expansion techniques involve the successive insertion of a cyclic monomer into a cyclic catalyst69 initiator66 or propagating species70 (Fig. 1(b)). Ring-expansion techniques do not require high dilution and therefore afford cyclic polymers in considerably higher yields than ring-closure techniques. However, careful catalyst design is required to ensure the formation of high molecular weight cyclic polymers with low dispersities and to ensure elimination of the catalyst from the final polymer.

The advances made in cyclic polymer synthesis, controlled polymerization techniques and highly efficient “click” coupling reactions,71 have also allowed for the preparation of a diverse range of cyclic polymer topologies including tadpole,72 jellyfish,73 sun-shaped,74 theta-shaped,75 figure-of-eight76 and other multi-cyclic topologies.68

**Fig. 1 Synthesis of cyclic polymers via ring-closure (a) and ring-expansion techniques (b).**

**Topological effects**

Cyclic polymers possess many unique physical properties in comparison to their linear polymer analogues in both solution and bulk.52,54,56,57 These differences provide opportunities for exploitation in many applications, as well as increasing our fundamental understanding of structure–property relationships. Cyclic polymers possess smaller hydrodynamic volumes77,78 and radii of gyration79,80 in comparison to their linear counterparts as a consequence of the more confined conformation of cyclic polymer chains. This difference has been exploited in the characterization of cyclic polymers by SEC analysis, where cyclic polymers exhibit longer retention times and therefore lower apparent molecular weights than the equivalent linear polymers of the same molecular weight.

As a consequence of their smaller hydrodynamic volume and lack of chain ends, cyclic polymers exhibit significantly higher critical entanglement molecular weights than analogous linear polymers. Similarly, the solution viscosities and melt viscosities of cyclic polymers are lower than the equivalent linear polymers.79,81 Interestingly, the melt viscosities of blends of cyclic and linear polymers are higher than either component, as a consequence of the threading of linear chains through cyclic polymer chains.82

The glass transition temperatures ($T_g$) of analogous linear and cyclic polymers exhibit very different trends.83,84 For low and medium molecular weight polymers ($10^3$–$10^4$ kDa), cyclic polymers exhibit higher $T_g$ values than their linear counterparts as a consequence of the different mobilities of cyclic and linear polymers. Cyclic polymers are inherently less mobile than linear polymers because of their confined nature, smaller volumes and lack of chain ends. For high molecular weight polymers ($>10^5$ kDa), the effect of end-groups becomes negligible and cyclic and linear polymers possess the same value of $T_g$. Furthermore, because of a lack of polymer chain ends, cyclic polymers show very little dependence of $T_g$ on molecular weight and exhibit values of $T_g$ similar to those of high molecular weight linear polymer ($T_g(\infty)$). The melting transition
temperatures ($T_m$) of cyclic and linear polymers exhibit similar trends in behaviour.

Cyclic and linear polymers are known to exhibit different modes of diffusion. The accepted mode of diffusion for linear polymers is a reptation mechanism: this process is governed by the mobility of the polymer chain ends. As cyclic polymers do not possess chain ends, diffusion must occur by a different mechanism, however this precise mode of diffusion has yet to be elucidated.

The unique structural and physical properties of cyclic polymers have been exploited in a variety of applications. Hawker and coworkers recently reported the use of cyclic diblock copolymers to prepare thin films for lithography applications, where the reduced volume of the cyclic polymer allowed a 30% decrease in domain spacing, compared to the corresponding linear diblock copolymer (Fig. 2). Zhang et al. prepared cyclic polymer based gels via a combination of ring-opening metathesis polymerization and thiol–ene chemistry. The gels prepared from cyclic polymers were found to exhibit markedly different swelling and mechanical properties in comparison to the equivalent gels comprised of linear polymers. In addition, Szoka and coworkers reported that cyclic polymers exhibit longer in vivo circulation times and higher tumour accumulation compared to linear analogues.

### Self-assembly of cyclic block copolymers

The earliest reported investigations into the effect of polymer cyclization on self-assembly were undertaken by Booth and coworkers, studying cyclic diblock copolymers comprised of either polylethylene oxide-$b$-poly(butylene oxide) (cyclic-$b$-PPO$_b$) or poly(ethylene oxide)-$b$-poly(propylene oxide) (cyclic-$b$-PPO$_b$). The self-assembly behaviour of the cyclic diblock copolymers was compared with the self-assembly of linear triblock copolymers and linear diblock copolymers of equivalent block composition. The authors reported similar aggregation behaviour for the cyclic diblock and linear triblock copolymers, with both polymers forming micellar assemblies, with comparable values of hydrodynamic radii ($R_h$) and critical micelle concentrations (cmc). However, one notable difference was observed when comparing the aggregation numbers ($N_{agg}$) of the cyclic diblock and linear triblock assemblies, with values of $N_{agg}$ consistently higher for the cyclic diblock micelles, suggestive of a more dense assembly (cyclic-$b$-PPO$_b$-$b$-PBO$_b$ $R_h = 4.4$ nm, $N_{agg} = 16$, PEO$_{21}$-$b$-PBO$_8$-$b$-PEO$_{21}$ $R_h = 4.0$ nm $N_{agg} = 6$). When comparing the cyclic diblock copolymers with the linear diblock copolymers, a more distinct difference in self-assembly behaviour was observed. The linear diblock copolymer assemblies consistently exhibited significantly larger values of $R_h$ and $N_{agg}$ and lower cmc values ($\text{PEO}_{41}-b$-$\text{PPO}_8$ $R_b = 7.1$ nm, $N_{agg} = 44$, cmc = 0.3 g L$^{-1}$), compared to both the cyclic diblock and linear triblock systems.

The findings of these initial studies can be explained by considering the respective conformation of the three polymer architectures in a micellar state (Fig. 3). The cyclic diblock and linear triblock copolymers are entropically disfavoured because each polymer chain has two block junctions located at the solvent-core interface, in comparison to linear diblock copolymers which possess only one block junction. To this end, the cmc values for cyclic diblock and linear triblock copolymers are expected to be higher than the equivalent linear diblock assemblies. The relative size of the resulting assemblies will also be influenced by the conformation of the different architectures. As the core-forming block of the linear diblock copolymer assembly is not required to loop and can stretch without restriction, the value of $R_h$ for a linear diblock micellar assembly is expected to be larger than that of equivalent cyclic diblock or linear triblock assemblies. Furthermore, as a consequence of their unrestricted structure, allowing better packing, linear diblock copolymer micelles are expected to be denser than micelles comprised of the equivalent cyclic diblock or linear triblock. In addition, because cyclic polymers possess smaller hydrodynamic volumes than linear polymers, the assembly of the cyclic diblock copolymer may also be smaller than the assembly of the linear triblock copolymer. Thus the observed respective particle sizes of cyclic diblock, linear diblock and linear triblock copolymers are a
balance between their hydrodynamic volume, conformation and relative stretching and packing abilities.

Subsequent studies by other research groups have also compared the self-assembly of cyclic diblock and linear diblock copolymers and reported similar findings. Ge et al. studied the self-assembly of cyclic poly(2-(2-methoxy-ethoxy) ethyl methacrylate)-b-poly(oligo(ethylene glycol) methyl ether methacrylate) (cyclic-PME02MA35-b-POEGMA12) and cyclic poly(2-(dimethylamino) ethyl methacrylate)-b-poly(2-(diethylamino) ethyl methacrylate) (cyclic-PDMAEMA110-b-PDEAEMA105-PEG26 nm).95

...Fig. 4 (Top) Cyclization and self-assembly of PEG-b-PCL. (Bottom) Light scattering data (number distributions) for cyclic and linear PCL-b-PEG. Adapted with permission from ref. 94. Copyright 2013 American Chemical Society.

Isono et al. reported the self-assembly of cyclic poly(decyl glycidyl ether)51-b-poly(2-(2-(2-methoxethoxy)ethoxy ethyl glycidyl ether))50 and the equivalent linear diblock copolymer.96 The cmc of the cyclic diblock copolymer assemblies was observed to be higher than that of the linear diblock copolymer (cyclic cmc = 1.8 × 10⁻³ g L⁻¹, linear cmc = 1.4 × 10⁻³ g L⁻¹), but in contrast to previous examples, the cyclic diblock copolymer assemblies were observed to be larger than the assemblies of the linear diblock (cyclic Dₙ = 166 nm, linear Dₙ = 122 nm). However, considering the fully extended chain lengths of the linear and cyclic copolymers, these assemblies cannot be classical core–shell micelles and indeed further analysis of the assemblies by transmission electron microscopy (TEM) revealed large spherical compound structures. The increased complexity of these aggregates makes it harder to elucidate the effect of cyclization on the particle dimensions. However, the observed difference in particle size may result from the reduced packing ability of cyclic polymer chains within the compound micelle compared to linear polymers, resulting in a greater value of Dₙ for the cyclic diblock assembly.

Yamamoto and Tezuka compared the self-assembly behaviour of cyclic poly(butyl acrylate)-b-poly(ethylene oxide) (PBA12-b-PEO9) with respect to the precursor linear triblock PBA6-b-PEO59-b-PBA6.97 Upon micellization the hydrophilic block of the linear triblock copolymer is looped and in contrast to previous studies the linear triblock assembly is conformationally restricted in the corona and not the core. The cyclic diblock and linear triblock assemblies displayed comparable values of Dₙ and cmc (cyclic Dₙ = 20 nm, cmc = 0.14 g L⁻¹, linear Dₙ = 20 nm, cmc = 0.13 g L⁻¹). However, significantly different thermal stabilities were exhibited by the cyclic and linear assemblies, with the micelles comprised of cyclic diblock copolymer displaying cloud points >40 °C higher than the micelles comprised of the linear triblock copolymer. The lower thermal stability of the linear triblock assemblies was attributed to the occurrence of inter-micelle bridging via dangling polymer chains in combination with dehydration, resulting in agglomeration at lower temperatures (Fig. 5). In comparison, the cyclic polymer chains cannot form inter-micelle bridges and agglomeration will only occur as a consequence of polymer dehydration, resulting in a higher transition temperature. Through coassembly of the cyclic and linear polymers, micelles with tuneable cloud point temperatures were observed. The same group has also reported that micelles of cyclic PBA₆-b-PEO₉ and cyclic poly(methyl acrylate)-b-poly(ethylene oxide) (PMA₃₋₅-b-PEO₉) exhibit greater robustness in response to salt additives (NaCl and MgSO₄), i.e. the cyclic diblock assemblies displayed higher salting-out concentrations in comparison to their linear PBA₆₋₅₋₅-b-PEO₉₋₅₋₅ and PMA₃₋₅₋₅-b-PEO₉₋₅₋₅ counterparts.98 The greater thermal and salt stabilities of the cyclic diblock assemblies were exploited through their use as catalytic nanoreactors in reactions that required elevated temperatures and high salt concentrations.

Yamamoto and Ree have subsequently reported a detailed small angle X-ray scattering (SAXS) investigation that high-
highlighted subtle structural differences between assemblies of cyclic PBA\textsubscript{10}-b-PEO\textsubscript{69} and linear PBA\textsubscript{5}-b-PEO\textsubscript{69}-b-PBA\textsubscript{5}. Both micelles were found to exhibit a core-fuzzy-shell structure, however the core and corona of the cyclic diblock copolymer micelle were more compact than the linear triblock copolymer micelle, as a result of the greater confinement and smaller effective volume of cyclic polymers.

The work highlighted so far has focused on the aggregation of cyclic block copolymers that possess a longer hydrophilic block relative to the hydrophobic block or comparable hydrophilic and hydrophobic block lengths; such polymers assemble to form so-called “star-like” micelles. Borsali and coworkers reported the self-assembly behaviour of cyclic poly(styrene)-b-poly(isoprene) (PS\textsubscript{x}-b-PI\textsubscript{y}) copolymers, that possess a significantly longer core-forming PS block than the corona-forming PI block; these assemblies are commonly referred to as “crew-cut”.\textsuperscript{100–106} In contrast to the “star-like” assemblies discussed above, these “crew-cut” assemblies exhibited much greater structural and morphological differences with respect to their linear PS\textsubscript{x}-b-PI\textsubscript{y} analogues. The linear PS\textsubscript{x}-b-PI\textsubscript{y} copolymers were observed to form spherical micelles of consistent size and low dispersities, regardless of polymer concentration, temperature or solvent choice (various \textit{n}-alkanes selective for the PI block). However, the morphology of the cyclic PS\textsubscript{x}-b-PI\textsubscript{y} copolymers was found to change dramatically as these parameters were varied and a transition from spherical flower-like micelles to giant worm-like micelles was observed (Fig. 6). As was discussed in previous examples, the contrasting self-assembly behaviour between the cyclic and linear polymers was attributed in part to the looped nature of the core block of the cyclic polymer, restricting the packing of the core and resulting in a greater number of unfavourable PS-solvent interactions. However, as a consequence of the large solvophobic PS block in these “crew-cut” assemblies, this effect is more pronounced compared to examples of “star-like” micelles. To minimize unfavourable PS-solvent interactions, the flower-like micelles of the cyclic diblock copolymer cohere forming more energetically favourable worm-like micelles. The transition from flower-like micelles to worm-like micelles is more pronounced as polymer concentration and temperature are increased, as the probability of cohesive collisions increases. Furthermore, as the solvent quality for PS is reduced (\textit{n}-pentane < \textit{n}-heptane < \textit{n}-decane), the driving force for cohesion is greater. Conversely, without the restrictive loop structure the spherical micelles of the linear polymer are more energetically favourable than the equivalent cyclic assemblies and possess no driving force for cohesion.

The effect of cyclization on the aggregation behaviour of a crystallization-driven self-assembly\textsuperscript{107} has also been investi-
 gated. Cyclic and linear amphiphilic diblock polypeptoids, poly[N-decylglycine]10−b-poly(N-methylglycine)105 were found to initially form spherical micelles upon self-assembly in methanol, a selective solvent for the poly(N-methylglycine) block. However, a morphological transition from spheres to cylindrical micelles was observed by cryo-TEM for both cyclic and linear polymers as the core-forming poly(N-decylglycine) block crystallized over time. This morphological transition was observed to take approximately twice as long for the cyclic diblock polypeptoid (15 days) compared to the linear diblock polypeptoid (8 days). This difference in behaviour was attributed to retarded crystallization of the cyclic diblock polypeptoid as a consequence of the restricted conformation of cyclic polymers. The resulting cylindrical micelles comprised of cyclic and linear polypeptoids exhibited similar dimensions by cryo-TEM (cyclic average core diameter = 12.2 nm, linear average core diameter = 12.6 nm).

Self-assembly of complex cyclic architectures

In addition to the self-assembly of amphiphilic cyclic diblock copolymers, some examples of the self-assembly of more complex amphiphilic cyclic architectures have been reported. Wan et al. reported the self-assembly of an amphiphilic tadpole-shaped polymer; where a tadpole-shaped polymer consists of a cyclic polymer attached to a linear polymer chain.109 The ring of the tadpole consisted of hydrophilic poly(N-isopropylacrylamide), whereas the linear tail consisted of hydrophobic poly(ε-caprolactone) [(cyclic-PNiPAm45)-b-PCL60]. When the self-assembly behaviour of the amphiphilic tadpole was compared with that of the equivalent linear diblock assembly, the tadpole-shaped polymer was reported to form slightly larger assemblies than the linear diblock copolymer (tadpole Rh = 70 nm, linear Rh = 62 nm). This suggested that the incorporation of cycles in the tadpole-shaped polymer hindered packing of the polymer during aggregation, resulting in larger, less compact particles. Such a hypothesis could be confirmed by determination of Nagg for the tadpole-shaped and linear polymers. As the values of Rh for both the tadpole-shaped polymer and linear polymer were larger than the maximum polymer chain length, the particles were ascribed to large compound structures. The viability of these tadpole and linear assemblies as drug carriers was investigated by loading the particles with doxorubicin hydrochloride and monitoring the subsequent release of the drug. The assemblies consisting of the tadpole-shaped polymer were found to exhibit faster release profiles, further indicating that the tadpole assembly was less compact than the equivalent linear system.

In direct contrast, when Isono et al. studied the self-assembly of tadpole-shaped polymers with a hydrophilic ring (poly-(2-(2-(2-methoxyethoxy)ethoxy)ethyl glycidyl ether)19) and hydrophobic tail (poly(decyl glycidyl ether)31), the tadpole assemblies displayed significantly smaller solution diameters than the equivalent linear assemblies (tadpole Dh = 83 nm, linear Dh = 123 nm).96 These aggregates were also reported to be large compound structures.

The self-assembly behaviour of tadpole-shaped polymers comprised of a hydrophobic ring and a hydrophilic tail has also been studied. Dong et al. prepared tadpole-shaped polymers with a poly(styrene) ring and a poly(ethylene oxide) tail ([cyclic-PNiPAm65]-b-PEO45).110 Subsequent self-assembly afforded vesicles with an average solution diameter, Dh, of 160 nm, whereas vesicles prepared from the analogous linear PS65-b-PEO45 copolymer displayed a smaller solution diameter, Dh, of 70 nm. This difference in particle size was further confirmed by TEM analysis (Fig. 7).

Lonsdale and Monteiro compared the self-assembly behaviour of different tadpole architectures comprised of hydrophobic poly(styrene) rings and hydrophilic poly(acrylic acid) (PAA) tails.111 Depending on the block length of the PAA tails, either micelles or vesicles were formed during self-assembly (Fig. 8). Assemblies that possessed two PAA tails but only one PS ring (C in Fig. 8) formed the smallest structures with the lowest values of Nagg as a consequence of the relatively low hydrophobic volume of these assemblies. Conversely, as a con-

![Fig. 7 TEM images of (a) linear PS-b-PEO and (b) tadpole PS-b-PEO. Reprinted with permission from ref. 110. Copyright 2009 American Chemical Society.](image1)

![Fig. 8 TEM images of PS-b-PAA tadpole-shaped polymers with varying architectures. Reprinted with permission from ref. 111. Copyright 2011 Wiley Periodicals, Inc.](image2)
sequence of increased hydrophobic volume, assemblies with only one PAA tail but two PS rings (B in Fig. 8) formed the largest structures and exhibited the largest values of $N_{agg}$. The greater restriction of two polymer rings per chain may also hinder the packing of the hydrophobic block in comparison to tadpole-shaped polymers with only one ring, contributing to the larger size of this assembly.

Similarly, when Fan et al. studied the self-assembly of an amphiphilic figure-of-eight shaped polymer in comparison to its precursor, a 4-armed amphiphilic star polymer, the assembly of the figure-of-eight polymer exhibited a significantly larger solution diameter (figure-of-eight $D_h = 42$ nm, star $D_h = 18$ nm).112 The 4-armed star polymer consisted of two PS arms and two PEO arms, whereas both rings in the figure-of-eight shaped polymer possessed a diblock PS-$b$-PEO$_y$ structure. The conformation of the figure-of-eight shaped polymer is extremely restricted upon aggregation, which greatly limits its ability to pack during self-assembly and results in a considerably larger micelle size compared to the star copolymer system. Furthermore, micelles of the figure-of-eight polymer possess three core-solvent junctions reducing their entropic favourability, whereas micelles comprised of the star copolymer possess only one core-solvent junction.

Meanwhile, Wang et al. studied the self-assembly of figure-of-eight shaped cyclic-(PS$_x$-$b$-PAA$_y$)$_2$ in comparison to linear-(PS$_x$-$b$-PAA$_y$)$_2$ (Fig. 9).113 Through variation of PS and PAA block lengths either conventional core–shell micelles ((PS$_x$-$b$-PAA$_y$)$_2$) or large compound structures ((PS$_x$-$b$-PAA$_y$)$_2$) were formed. In both cases the figure-of-eight polymer formed larger structures that possessed lower values of $N_{agg}$ compared to the equivalent linear polymer (figure-of-eight $R_h = 46$ nm, $N_{agg} = 250$, linear $R_h = 35$ nm, $N_{agg} = 367$), providing further evidence of the loose nature of aggregates prepared from figure-of-eight shaped polymers.

The self-assembly of jellyfish-shaped amphiphilic polymers has also been briefly investigated. Cai et al. prepared jellyfish-shaped polymers with a hydrophobic block copolymer ring comprised of PCL and poly(pentafluorostyrene) (PPFS), with hydrophilic PEG side arms attached to the latter block, yielding cyclic-PCL-$b$-(PPFS$_x$-g-PEG$_y$).114 Upon self-assembly in water, spherical micelles with a diameter of 50–60 nm were observed by scanning electron microscopy (SEM). However, no comparison with an equivalent linear structure was reported. In another example, Coulembier et al. prepared jellyfish-shaped polymers with a cyclic poly(t-lactide) (PLLA$_{40}$) back-bone and three poly(methyl methacrylate) (PMMA) side arms.73 When a solution of the polymer in THF was deposited on a mica substrate and analyzed by atomic force microscopy (AFM), short cylindrical structures, toroids and other structures were observed. The height and width of the cylinders and toroids corresponded to the diameter of the PLLA ring, suggesting the jellyfish assembled in a cofacial manner.

In a similar manner, Schappacher and Deffieux prepared well-defined polymeric nanotubes via the self-assembly of densely grafted, high molecular weight cyclic brush copolymers.115 The cyclic polymer backbone consisted of poly(chloroethyl vinyl ether)$_{1000}$ that had been grafted with a mixture of randomly distributed PS$_{170}$ and PI$_{50}$ arms (Fig. 10). The cyclic brush copolymers were found to self-assemble in $n$-heptane, a selective solvent for PI, to afford nanotubes with a diameter of ca. 100 nm and length of up to 700 nm. The diameter of the
assemblies corresponded to the diameter of the cyclic brushes, again suggesting self-assembly occurred in a cofacial manner between cyclic brush copolymers. These last two examples highlight the significant and unique self-assembly behaviour of polymers that possess a cyclic architecture, where these particular examples of self-assembly are impossible to achieve with polymers that possess a linear architecture.

Conclusions

As a consequence of improved synthetic methods, enabling the preparation of well-defined, high purity cyclic polymers, the self-assembly of amphiphilic cyclic polymers has received increasing attention in recent years. By comparing the aggregation of cyclic polymers with equivalent linear polymers, we can determine the effect of cyclization on self-assembly and increase our understanding of structure–property relationships. Indeed, the examples discussed in this review have highlighted the profound effect cyclization can have on particle dimensions, stability, and morphology, as well as the packing of polymer chains within the assembly. In general, cyclic diblock copolymers form smaller, entropically disfavoured aggregates in comparison to linear diblock copolymers, as a consequence of the confined and looped nature of cyclic polymers, resulting in a greater number of unfavourable core-solvent junctions. The self-assembly of cyclic diblock copolymers is however similar to that of linear triblock copolymers, which are also required to loop upon aggregation. For the self-assembly of more complex cyclic topologies, assemblies of cyclic polymers are often larger than the equivalent linear polymer assembly as a consequence of poor polymer packing. Furthermore, the cyclization of amphiphilic polymers can lead to unique self-assembly behaviour that cannot be achieved through the self-assembly of linear polymers or can impart improved properties to the resulting nanostructures, for example, greater thermal stability and robustness towards salt additives.

Notes and references