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## Tuning the electronic properties of transition-metal trichalcogenides *via* tensile strain†

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A comprehensive study of the effect of tensile strain ( $\epsilon = 0\%$  to  $8\%$ ) on the electronic structures of two-dimensional (2D) transition-metal trichalcogenide (TMTC) monolayers  $\text{MX}_3$  ( $M = \text{Ti, Zr, Hf, Nb}$ ;  $X = \text{S, Se, Te}$ ) is performed on the basis of density functional theory (DFT) computation. The unstrained  $\text{TiS}_3$ ,  $\text{ZrS}_3$ ,  $\text{ZrSe}_3$ ,  $\text{HfS}_3$ ,  $\text{HfSe}_3$  and  $\text{NbS}_3$  monolayers are predicted to be semiconductors with their bandgap ranging from 0.80 to 1.94 eV. Our DFT computations show that the biaxial and uniaxial tensile strains can effectively modify the bandgap of many TMTC monolayers. In particular, we find that  $\text{ZrS}_3$  and  $\text{HfS}_3$  monolayers undergo an indirect-to-direct bandgap transition with increasing tensile strain. The indirect bandgaps of  $\text{ZrSe}_3$  and  $\text{HfSe}_3$  monolayers also increase with the tensile strain. Both  $\text{ZrTe}_3$  and  $\text{HfTe}_3$  monolayers are predicted to be metals, but can be transformed into indirect bandgap semiconductors at  $\epsilon = 4\%$  and  $\epsilon = 6\%$ , respectively. Importantly, the  $\text{TiS}_3$  monolayer can retain its direct-bandgap feature over a range of biaxial or uniaxial tensile strains (up to  $8\%$ ). The highly tunable direct bandgaps of  $\text{MS}_3$  ( $M = \text{Hf, Ti, and Zr}$ ) by strain and the availability of metallic and semiconducting properties of  $\text{MTe}_3$  ( $M = \text{Hf and Zr}$ ) provide exciting opportunities for designing artificial layered structures for applications in optoelectronics and flexible electronics.

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### Introduction

In recent years, 2D layered nanomaterials have attracted intensive interest due to their novel electronic, optical, thermal, and mechanical properties for potential applications in various fields. With regard to transition-metal based 2D materials, thus far, predominant investigations have been focused on the transition metal dichalcogenides (TMDCs) such as  $\text{MoS}_2$ , not only because of their novel electronic and catalytic properties but also their high tunability *via* strain or a vertical electric field.<sup>1–6</sup> Remarkably, large-scale growth of monolayered  $\text{MoS}_2$  films with spatial homogeneity and high electrical performance has been recently demonstrated in the laboratory.<sup>7</sup> It has also been demonstrated that  $\text{MoS}_2$  exhibits many exotic characteristics that are absent in its bulk counterpart.<sup>8–10</sup>  $\text{MoS}_2$  is a semiconductor with a direct bandgap, although the bulk  $\text{MoS}_2$  possesses an indirect bandgap.<sup>11</sup> The direct bandgap character of 2D layered materials such as monolayered  $\text{MoS}_2$  is highly desired for applications in thinner transistors, thermoelectrics

and solar cells. Towards this end, several new chemical approaches to contrive new 2D nanomaterials have been reported,<sup>12–14</sup> which renders synthesis of new monolayered nanomaterials more accessible.

Like TMDCs, many bulk transition metal trichalcogenides (TMTCs) exhibit layered structures with weak interlayer van der Waals interactions. Most TMTCs, *i.e.*  $\text{MX}_3$  ( $M = \text{Ti, Zr, Hf}$ ;  $X = \text{S, Se, Te}$ ), possess monoclinic crystalline structures with the space group  $P2_1/m$ ,<sup>15,16</sup> while the space group of  $\text{NbS}_3$  is  $P1$  and its most stable crystalline structure is triclinic.<sup>17,18</sup> Although many bulk  $\text{MX}_3$  compounds have been studied for several decades,<sup>19–26</sup> 2D  $\text{MX}_3$  layered materials have received little attention until very recently when the new monolayered  $\text{TiS}_3$  was isolated,<sup>27,28</sup> and was also predicted to possess exciting electronic properties such as a direct band gap (1.06 eV) close to that of silicon.<sup>29</sup> Note that the bulk  $\text{TiS}_3$  is an n-type semiconductor with an indirect band gap. Previous studies also showed that  $\text{TiS}_3$  possesses lower cleavage energy than graphite.<sup>29,30</sup> Indeed, Island *et al.* demonstrated that a  $\text{TiS}_3$  film can be exfoliated down to single layers with high photoreponse and fast switching rates.<sup>31</sup>

As pointed out previously, 2D layered semiconducting materials with direct and tunable bandgaps are highly desired for nanoelectronic and optoelectronic applications.<sup>32–38</sup> It is known that engineering 2D layered materials by strain is a viable approach to achieve tunable electronic properties.<sup>39–46</sup> Over the past few years, effects of strains on electronic

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properties of TMDCs have been extensively studied, especially from the theoretical viewpoint.<sup>47–53</sup> It was predicted that some TMDC monolayers can undergo an indirect-to-direct bandgap transition under the tensile strain. Hence, it is timely and important to explore whether the indirect-to-direct bandgap transition can occur when TMDC monolayers are under tensile strain. In this study, effects of both biaxial and uniaxial strains on the bandgap of a series of  $\text{MX}_3$  monolayers ( $\text{M} = \text{Ti}, \text{Zr}, \text{Hf}, \text{Nb}$ ;  $\text{X} = \text{S}, \text{Se}, \text{Te}$ ) are investigated. We find that as in the case of TMDCs, the tensile strains can strongly modify the bandgap of many TMDC monolayers.

## Computational methods

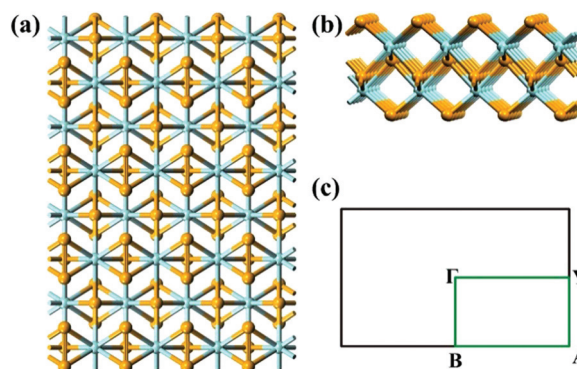
All computations were performed within the framework of density functional theory (DFT), using the Vienna ab initio simulation package (VASP 5.3).<sup>54</sup> The core–valence interaction was described by the projector augmented wave (PAW) method.<sup>55</sup> The generalized gradient approximation (GGA) in the form of Becke86 was adopted for the exchange–correlation functional.<sup>56</sup> More specifically, the optB86b–vdW functional, implemented to account for weak van der Waals (vdW) interactions,<sup>57</sup> was used for structure optimization (we also examined two other GGA functionals with the vdW correction, namely optPBE–vdW and optB88–vdW, and found that the optB86b–vdW functional gives the best agreement with experiments in predicting the lattice constants of bulk TMDCs). It is known that GGA functionals tend to underestimate the band gap of semiconductors. So the electronic structures were computed using the Heyd–Scuseria–Ernzerhof (HSE06) hybrid functional.<sup>58</sup> The same computations were also performed with the optB86–vdW functional to confirm the general trend of strain-dependent bandgaps. Energy cut off for the plane-wave expansion was set to 500 eV. Brillouin zone sampling was performed with Monkhorst–Pack (MP) special  $k$ -point meshes. The 2D Brillouin zone integration using the  $\Gamma$ -center scheme was sampled with a  $7 \times 10 \times 1$  grid for geometry optimizations ( $7 \times 10 \times 4$  for bulk systems), and the  $k$ -point grid scaled with respect to the supercell size. A vacuum layer greater than 15 Å was taken to avoid interaction between adjacent images. All atoms were allowed to relax during the geometry optimization until the computed Hellmann–Feynman force on each atom was smaller than  $0.02 \text{ eV \AA}^{-1}$ . The convergence threshold was set as  $10^{-4} \text{ eV}$  in energy. Spin–orbit coupling (SOC) was included when computing the band structures. Tensile strain ranging from 0 to 8% was considered. The tensile strain was undertaken in three different ways: (1) biaxial expansion in both the  $x$  and  $y$  directions ( $xy$ ), uniaxial expansion of the monolayer in the  $x$  direction ( $xx$ ) or the  $y$  direction ( $yy$ ).<sup>51</sup> For the uniaxial strain, the Poisson effect is considered. The strain scale is defined as  $\epsilon = \Delta m/m_0$ . For biaxial tensile strain,  $m_0$  is the unstrained cell parameter, and  $\Delta m + m_0$  is the strained cell parameter. For uniaxial tensile strain,  $m_0$  is the projection of the unit-cell vector in the  $x$  or  $y$  direction, and  $\Delta m$  is the associated change from  $m_0$ .

## Results and discussion

As mentioned above, the optimized lattice vectors based on the optB86b–vdW functional agree well with the experimental data. For example, the optimized lattice constants of  $\text{ZrS}_3$  bulk are  $a_0 = 5.133 \text{ \AA}$ ,  $b_0 = 3.624 \text{ \AA}$ ,  $c_0 = 9.008 \text{ \AA}$ , and  $\beta = 97.15^\circ$ , in good agreement with the experimental values ( $a_0 = 5.124 \text{ \AA}$ ,  $b_0 = 3.624 \text{ \AA}$ ,  $c_0 = 8.980 \text{ \AA}$ , and  $\beta = 97.28^\circ$ ). Note that the TMDC bulks often have many allotropes.<sup>15–17</sup> In this study, we only consider TMDC monolayers cleaved from the most stable bulk allotrope at 0 K. For  $\text{TiX}_3$ ,  $\text{ZrX}_3$ , and  $\text{HfX}_3$ , the most stable crystalline structure is monoclinic, while for  $\text{NbS}_3$  the most stable crystalline structure is triclinic. Next, the band structures of  $\text{MX}_3$  bulks are computed using the HSE06 functional. The HSE06 bandgaps of  $\text{TiS}_3$ ,  $\text{ZrS}_3$ ,  $\text{ZrSe}_3$ ,  $\text{HfS}_3$ ,  $\text{HfSe}_3$  and  $\text{NbS}_3$  bulks are 1.05 eV, 1.87 eV, 0.68 eV, 1.90 eV, 0.59 eV and 1.07 eV, respectively, in good agreement with the measured bandgaps from experiments.<sup>32–38</sup> For example, the measured bandgap of  $\text{ZrS}_3$  and  $\text{HfS}_3$  is 1.91 and 1.95 eV, respectively.

The optimized lattice constants of TMDC monolayers (see Fig. 1 for structures) based on the optB86b–vdW functional are summarized in Table 1, together with the computed HSE06 bandgaps. For the band-structure computation, the Brillouin zone of  $\Gamma\text{YA}\Gamma\text{B}$  (Fig. 1c) is selected.

As shown in Table 1, the unstained  $\text{TiS}_3$  monolayer is the only TMDC considered with a direct bandgap. Table 1 also shows that  $\text{ZrS}_3$ ,  $\text{ZrSe}_3$ ,  $\text{HfS}_3$ ,  $\text{HfSe}_3$ , and  $\text{NbS}_3$  monolayers are also semiconductors but with an indirect bandgap.  $\text{ZrTe}_3$  and  $\text{HfTe}_3$  are predicted to have the electronic structures of metals. Previously, we have examined the dynamical stability of the  $\text{TiS}_3$  monolayer by computing its phonon spectrum.<sup>29</sup> Here we have also computed the phonon spectrum of two prototype monolayers,  $\text{HfS}_3$  and  $\text{HfSe}_3$ , one is the direct semiconductor under biaxial strain while another is the indirect semiconductor under all types of strain. As shown in ESI Fig. S1,<sup>†</sup> there is no negative frequency in the computed phonon spectrum of  $\text{HfS}_3$  and  $\text{HfSe}_3$  monolayers.



**Fig. 1** (a) Top view and (b) side view of a  $4 \times 4 \text{ MX}_3$  monolayered sheet, (c) the first Brillouin zone and the high symmetry points associated with the  $\text{MX}_3$  monolayer. The orange and cyan spheres refer to M and X atoms, respectively.



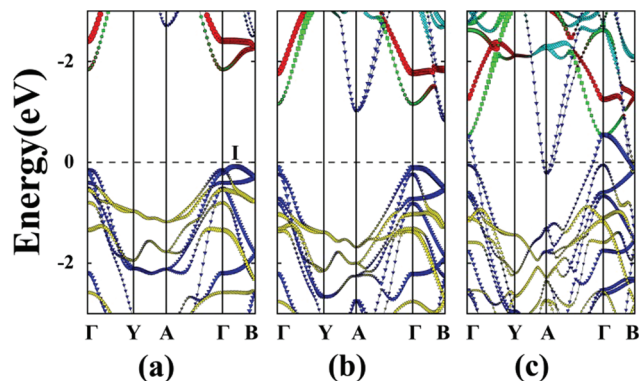
**Table 1** Optimized lattice constants  $a_0$  (Å) and  $b_0$  (Å) of  $\text{MX}_3$  monolayers ( $M = \text{Ti, Zr, Hf, Nb}$ ;  $X = \text{S, Se, Te}$ ), based on the optB86b-vdW functional, and computed bandgaps, based on the HSE06 functional. The direct or indirect bandgap is also denoted by D or I

	$a_0$ (Å)	$b_0$ (Å)	Bandgap (eV)	Direct/indirect
$\text{ZrS}_3$	5.138	3.619	1.92	I
$\text{ZrSe}_3$	5.423	3.745	0.92	I
$\text{ZrTe}_3$	5.942	3.909	Metal	—
$\text{HfS}_3$	5.092	3.576	1.94	I
$\text{HfSe}_3$	5.402	3.709	0.80	I
$\text{HfTe}_3$	5.941	3.882	Metal	—
$\text{TiS}_3$	4.970	3.386	1.08	D
$\text{NbS}_3$	4.992	6.746	1.18	I

Next, the effect of tensile strain on the electronic structures of  $\text{MX}_3$  monolayers ( $M = \text{Zr, Hf}$ ;  $X = \text{S, Se, Te}$ ) is investigated in detail. The computed HSE06 bandgaps of  $\text{MX}_3$  monolayers ( $M = \text{Zr, Hf}$ ;  $X = \text{S, Se, Te}$ ), subjected to biaxial or uniaxial strain ranging from 0% to 8% are summarized in Fig. 2.

### $\text{ZrX}_3$ and $\text{HfX}_3$

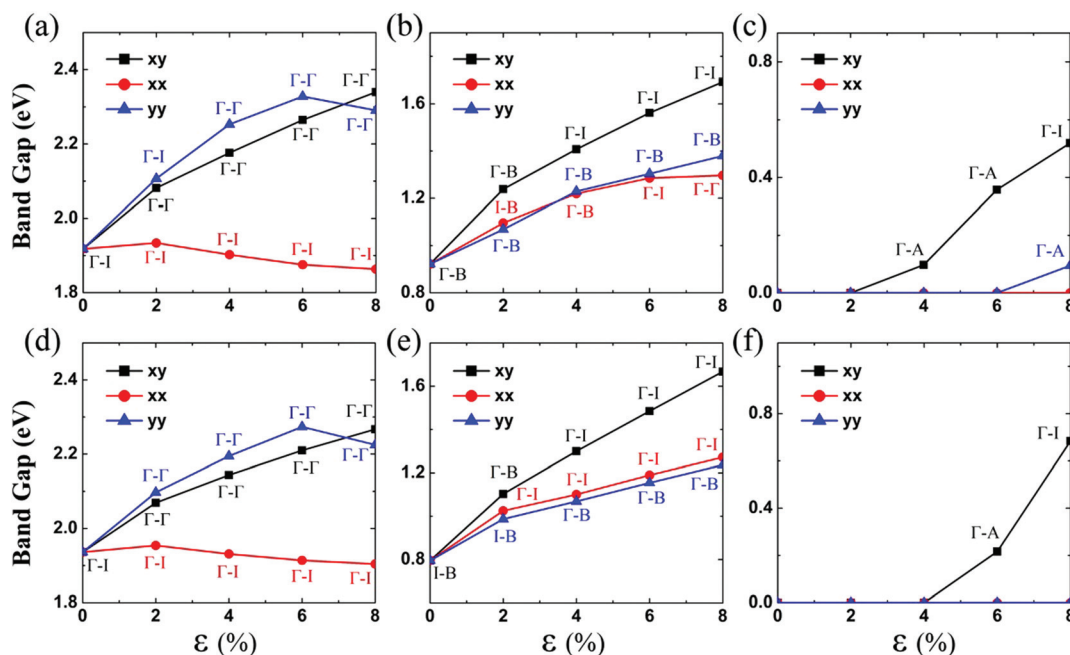
The unstrained  $\text{ZrS}_3$  monolayer is a semiconductor with an indirect bandgap of 1.92 eV. As shown in Fig. 3(a), the conduction band minimum (CBM) and valence band maximum (VBM) are located at  $\Gamma$  point and I point, respectively. Here, the energy at I point is only 0.07 eV higher than that at the  $\Gamma$



**Fig. 3** Band structures of unstrained monolayers (a)  $\text{ZrS}_3$ , (b)  $\text{ZrSe}_3$ , and (c)  $\text{ZrTe}_3$ . The red lines denote the  $d_{z^2}$  orbital of the Zr atom. The green lines denote the  $d_{x^2-y^2}$  orbitals of the Zr atom. The cyan lines denote the  $d_{xy}$ ,  $d_{yz}$  and  $d_{xz}$  orbitals of the Zr atom. The blue lines denote the  $p_x$  and  $p_y$  orbitals of (a) S, (b) Se, (c) and Te atoms, and the yellow lines denote the  $p_z$  orbital of (a) S, (b) Se, and (c) Te atoms. The dashed lines indicate the Fermi level. The I point refers to the VBM not located at the  $\Gamma$  point.

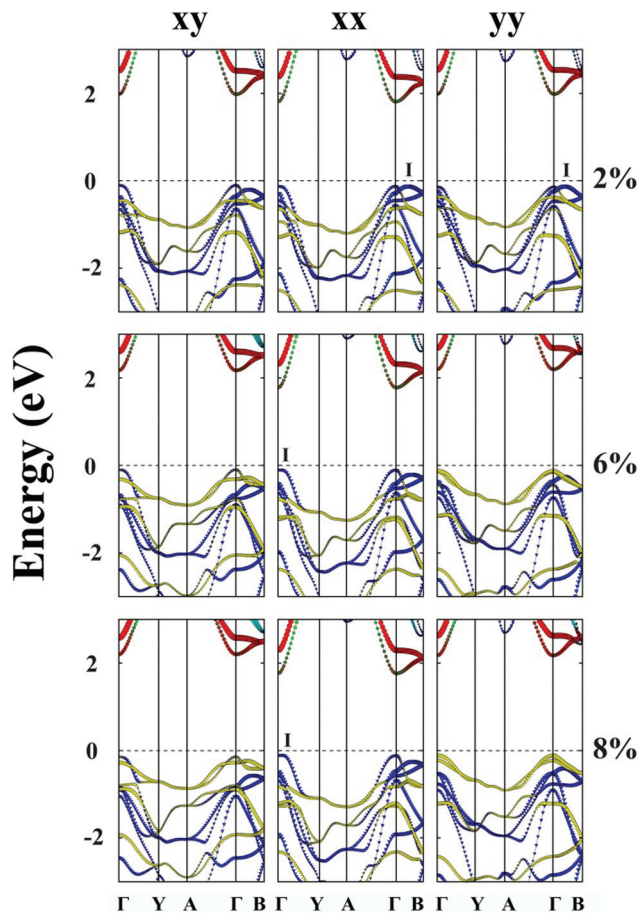
point. The CBM is mainly contributed by  $d_{z^2}$  and  $d_{x^2-y^2}$  orbitals of the Zr atom, while the VBM is mainly contributed by  $p_x$  and  $p_y$  orbitals of the S atom. The partial density of states (PDOS) is depicted in ESI Fig. S2.†

When the  $\text{ZrS}_3$  monolayer is subjected to the biaxial tensile strain of  $\varepsilon = 2\%$  in both the  $x$  and  $y$  directions, its bandgap increases to 2.08 eV. More interestingly, as illustrated in Fig. 4,



**Fig. 2** Computed bandgaps of (a)  $\text{ZrS}_3$ , (b)  $\text{ZrSe}_3$ , (c)  $\text{ZrTe}_3$ , (d)  $\text{HfS}_3$ , (e)  $\text{HfSe}_3$ , and (f)  $\text{HfTe}_3$  monolayers versus the biaxial or uniaxial tensile strain, ranging from  $\varepsilon = 0\%$  to  $8\%$ . The black lines denote the bandgap versus biaxial tensile strain in both the  $x$  and  $y$  directions. The red lines denote the bandgap versus the uniaxial tensile strain in the  $x$  direction, and the blue lines denote the bandgap versus the uniaxial tensile strain in the  $y$  direction.  $\Gamma$ , A and B represent the special points in the first Brillouin zone (Fig. 1(c)), while I refers to either the valence band maximum or conduction band minimum that is not located at the  $\Gamma$  point. Hence,  $\Gamma$ - $\Gamma$  denotes the direct bandgap, whereas  $\Gamma$ -A,  $\Gamma$ -B and  $\Gamma$ -I denote the indirect bandgap.





**Fig. 4** Computed band structures of strained monolayered ZrS<sub>3</sub> under the biaxial tensile strain in both the *x* and *y* directions (*xy*), or under the uniaxial tensile strain in the *x* direction (*xx*) or the *y* direction (*yy*). The red and green lines illustrate the *d*<sub>z<sup>2</sup></sub> orbital and the *d*<sub>x<sup>2</sup>-y<sup>2</sup></sub> orbital of the Zr atom, respectively. The cyan lines denote the *d*<sub>xy</sub>, *d*<sub>yz</sub> and *d*<sub>xz</sub> orbitals of the Zr atom. The blue lines denote the *p*<sub>x</sub> and *p*<sub>y</sub> orbitals of the S atom, and the yellow lines denote the *p*<sub>z</sub> orbital of the S atom. The dashed lines indicate the Fermi level. The I point refers to the VBM not located at the  $\Gamma$  point.

the ZrS<sub>3</sub> monolayer transforms from an indirect to direct bandgap semiconductor, as both the VBM and CBM are located at the  $\Gamma$  point. This transformation is mainly due to the energy (of the *p* orbital of the S atom) at the  $\Gamma$  point shifting above the energy at I point, thereby the VBM is changed from I point to  $\Gamma$  point. The CBM however is still located at the  $\Gamma$  point, resulting in a direct bandgap. Moreover, upon increasing the biaxial strain to a high value of  $\epsilon = 8\%$ , the direct bandgap character is still retained although the bandgap is increased from 1.92 to 2.34 eV.

Likewise, the uniaxial tensile strain of  $\epsilon = 4\%$  along the *y* direction can also lead to the indirect-to-direct bandgap transition for the ZrS<sub>3</sub> monolayer. The direct bandgap character is maintained even when the strain is as high as 8%. Meanwhile, the uniaxial expansion in the *y* direction initially increases the bandgap from 1.92 to 2.33 eV at  $\epsilon = 6\%$ , and then slightly reduces the bandgap to 2.29 eV at  $\epsilon = 8\%$ .

When the monolayered ZrS<sub>3</sub> is subjected to uniaxial tensile strain in the *x* direction, as shown in Fig. 4, the indirect bandgap character is maintained even when the strain is as high as 8%. In addition, uniaxial expansion in the *x* direction only slightly changes the bandgap from 1.92 to 1.93 eV at  $\epsilon = 2\%$ , while it reduces the bandgap to 1.86 eV at  $\epsilon = 8\%$ .

Unstrained monolayered ZrSe<sub>3</sub> is a semiconductor with an indirect bandgap of 0.92 eV (Fig. 3(b)), and the VBM and CBM are located at the  $\Gamma$  and B points, respectively. Both VBM and CBM are mainly contributed by *p*<sub>x</sub> and *p*<sub>y</sub> orbitals of the Se atom. When the monolayered ZrSe<sub>3</sub> is subjected to biaxial tensile strain from 2% to 8%, the bandgap increases from 1.24 to 1.69 eV (Fig. 2 and ESI Fig. S3<sup>†</sup>). The ZrSe<sub>3</sub> monolayer remains an indirect bandgap semiconductor, as the VBM is always located at the  $\Gamma$  point, while the CBM shifts from B to I point at  $\epsilon = 4\%$ . As shown in ESI Fig. S3,<sup>†</sup> upon increasing the strain to  $\epsilon = 8\%$ , the CBM is still located at the I point.

Upon applying the uniaxial tensile strain of  $\epsilon = 2\%$  along the *x* direction to the monolayered ZrSe<sub>3</sub>, the VBM shifts from the  $\Gamma$  to the I point. Interestingly, at  $\epsilon = 4\%$ , the VBM shifts back to the  $\Gamma$  point. At  $\epsilon = 8\%$ , the energy (of the *p* orbital of the S atom) at the B point shifts above that at the  $\Gamma$  point. Consequently, the CBM shifts from the B point to the  $\Gamma$  point, whereas the VBM is still located at the  $\Gamma$  point, resulting in a direct bandgap. The uniaxial tensile strain in the *x* direction increases the bandgap from 1.10 to 1.30 eV at  $\epsilon = 8\%$ .

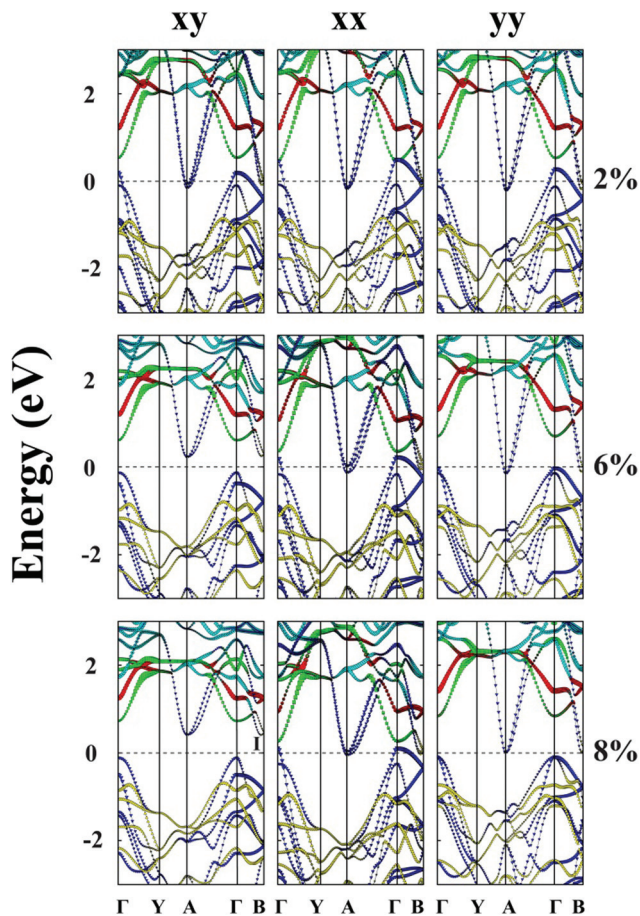
When the monolayered ZrSe<sub>3</sub> is subjected to uniaxial tensile strain in the *y* direction, the VBM is always located at the  $\Gamma$  point, and the CBM is always located at the B point. In any event, the uniaxial expansion in the *y* direction can modulate the indirect bandgap from 1.07 to 1.38 eV.

For HfS<sub>3</sub> and HfSe<sub>3</sub> monolayers, the strain-dependent bandgap behavior is quite similar to that of ZrS<sub>3</sub> and ZrSe<sub>3</sub>. The detailed electronic structure *versus* tensile strain for HfS<sub>3</sub> and HfSe<sub>3</sub> is shown in ESI Fig. S4–S6.<sup>†</sup>

Unlike MS<sub>3</sub> and MSe<sub>3</sub>, unstrained ZrTe<sub>3</sub> and HfTe<sub>3</sub> monolayers are predicted to be metals. Importantly, when the ZrTe<sub>3</sub> monolayer is subjected to biaxial tensile strain of  $\epsilon = 4\%$ , it transforms from a metal to semiconductor with an indirect bandgap of 0.10 eV. The VBM and CBM are located at the  $\Gamma$  point and A point, respectively. As shown in Fig. 5, the valence band near the Fermi level is mainly contributed by *p*<sub>x</sub> and *p*<sub>y</sub> orbitals of the Te atom, and the CBM is mainly contributed by the *p*<sub>z</sub> orbital of the Te atom. The energy splitting between the *p* orbital at  $\Gamma$  point and at A point increases with increasing the biaxial tensile strain, leading to the metal-to-semiconductor transition. At  $\epsilon = 8\%$  the CBM shifts from A to I point and the bandgap increases to 0.52 eV. Uniaxial expansion in the *y* direction to  $\epsilon = 8\%$  can open a bandgap of 0.10 eV. In contrast, upon applying uniaxial tensile strain along the *x* direction, the metallic character of the ZrTe<sub>3</sub> monolayer is retained even at  $\epsilon = 8\%$ .

Like ZrTe<sub>3</sub>, upon applying uniaxial tensile strain along the *x* direction, the metallic character of the HfTe<sub>3</sub> monolayer is still retained, even at  $\epsilon = 8\%$  (ESI Fig. S7<sup>†</sup>). HfTe<sub>3</sub> also keeps the metallic character even under uniaxial stain of  $\epsilon = 8\%$  in the *y*



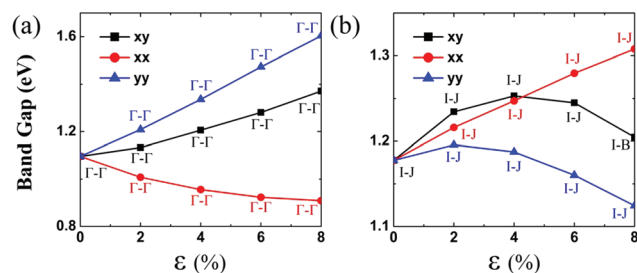


**Fig. 5** Computed band structures of strained monolayered  $\text{ZrTe}_3$  under the biaxial tensile strain ( $xy$ ) in both the  $x$  and  $y$  directions, or under the uniaxial tensile strain in the  $x$  direction ( $xx$ ) or the  $y$  direction ( $yy$ ). The red lines denote the  $d_{z^2}$  orbital of the Zr atom. The green lines denote the  $d_{x^2-y^2}$  orbitals of the Zr atom. The cyan lines denote the  $d_{xy}$ ,  $d_{yz}$  and  $d_{xz}$  orbitals of the Zr atom. The blue lines denote the  $p_x$  and  $p_y$  orbitals of the Te atom, and the yellow lines denote the  $p_z$  orbital of the Te atom. The dashed lines indicate the Fermi level. The I point refers to the CBM not located at the  $\Gamma$  point.

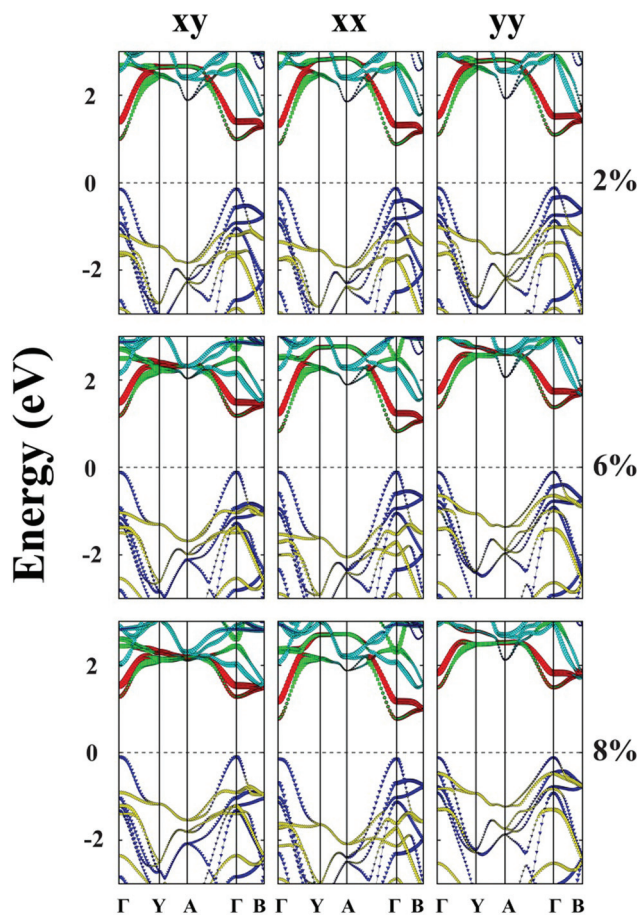
direction. Only the biaxial tensile strain can open a bandgap of  $\text{HfTe}_3$ , *e.g.*, to 0.22 eV at  $\varepsilon = 6\%$  and to 0.68 eV at  $\varepsilon = 8\%$ . At the two strains, the VBM is located at the  $\Gamma$  point while the CBM is located at the A point and I point, respectively.

### $\text{TiS}_3$ and $\text{NbS}_3$

Lastly, the effect of tensile strain on the bandgap of the  $\text{TiS}_3$  monolayer is also investigated. The  $\text{TiS}_3$  monolayer is a semiconductor with a direct bandgap of 1.08 eV. As illustrated in Fig. 6(a) and 7 and ESI Fig. S8,<sup>†</sup> Both VBM and CBM are located at the  $\Gamma$  point, consistent with the results of previous studies.<sup>29</sup> The bandgap can increase up to 1.37 eV at the biaxial tensile strain  $\varepsilon = 8\%$ . Likewise, upon applying uniaxial strain along the  $y$  direction, the direct bandgap character is maintained even at  $\varepsilon = 8\%$ , and the bandgap is enlarged from 1.21 to 1.60 eV. The latter is wider than the enlarged bandgap



**Fig. 6** Bandgap of (a)  $\text{TiS}_3$  and (b)  $\text{NbS}_3$  monolayers versus the biaxial and uniaxial tensile strain ranging from 0% to 8%. The black lines denote the bandgap versus biaxial tensile strain both in the  $x$  and  $y$  directions. The red lines denote the bandgap versus the uniaxial tensile strain in the  $x$  direction. The blue lines denote the bandgap versus the uniaxial tensile strain in the  $y$  direction.



**Fig. 7** Computed band structures of the strained monolayered  $\text{TiS}_3$  subjected to the biaxial tensile strain both in the  $x$  and  $y$  directions ( $xy$ ), the uniaxial tensile strain in the  $x$  direction ( $xx$ ) or the  $y$  direction ( $yy$ ). The red and green lines illustrate the  $d_{z^2}$  and  $d_{x^2-y^2}$  orbitals of the Ti atom, respectively. The cyan lines represent the  $d_{xy}$ ,  $d_{yz}$  and  $d_{xz}$  orbitals of the Ti atom. The blue lines represent the  $p_x$  and  $p_y$  orbitals of the S atom, and the yellow lines show the  $p_z$  orbital of the S atom. The dashed lines indicate the Fermi level.



at the biaxial strain of  $\varepsilon = 8\%$ . In contrast, when the monolayered  $\text{TiS}_3$  is subjected to uniaxial tensile strain in the  $x$  direction, although its direct gap character is maintained even at  $\varepsilon = 8\%$ , the bandgap is actually reduced from 1.08 eV to 1.01 eV at  $\varepsilon = 2\%$ , and to 0.91 eV at  $\varepsilon = 8\%$ . The opposite trend of bandgap change is due to the downward shift of CBM at the  $\Gamma$  point. Here, the VBM is mainly contributed by  $p_x$  and  $p_y$  orbitals of the S atom, while the CBM is mainly contributed by  $d_{z^2}$  and  $d_{x^2-y^2}$  orbitals of the Ti atom.

Bulk  $\text{NbS}_3$  is a triclinic structure with the space group of  $P1$ . As shown in Fig. 6(b) and ESI Fig. S8,<sup>†</sup> the unstrained  $\text{NbS}_3$  monolayer is a semiconductor with an indirect bandgap of 1.18 eV. The CBM, located on the  $\Gamma$ -B line, is mainly contributed by the  $d_{xz}$  orbital of the Nb atom, while the VBM, located on the Y-A line, is mainly contributed by the  $d_{z^2}$  and  $d_{x^2-y^2}$  orbitals of the Nb atom. The  $\text{NbS}_3$  monolayer retains its indirect bandgap, regardless of the biaxial and uniaxial tensile strain. Moreover, the strain can only change the bandgap modestly.

## Conclusions

In conclusion, we present a comprehensive study of the effect of tensile strain on the electronic structures of transition-metal trichalcogenide monolayers, based on density functional theory computations. Our computations predict that  $\text{MS}_3$  and  $\text{MSe}_3$  ( $M = \text{Ti, Zr, Hf, Nb}$ ) monolayers are all semiconductors, while  $\text{MTe}_3$  monolayers are metals. Both  $\text{ZrS}_3$  and  $\text{HfS}_3$  monolayers can undergo an indirect-to-direct bandgap transition with increasing tensile strain. The indirect bandgap of  $\text{ZrSe}_3$  and  $\text{HfSe}_3$  monolayers increases with the tensile strain, but the indirect character is retained in most cases. The  $\text{ZrTe}_3$  and  $\text{HfTe}_3$  monolayers can be transformed from a metal to semiconductor with an indirect bandgap at  $\varepsilon = 4\%$  and  $\varepsilon = 6\%$ , respectively. The  $\text{TiS}_3$  monolayer can retain its direct bandgap under either the biaxial or uniaxial strain, ranging from  $\varepsilon = 0\%$  to  $8\%$ . The  $\text{NbS}_3$  monolayer retains its indirect bandgap, regardless of the tensile strain. Overall, the bandgaps of  $\text{MX}_3$  monolayers can be modulated from 0.68 eV to 2.34 eV at  $\varepsilon \leq 8\%$ .

We note that as the atomic number of X increases from S to Te, the bandgap decreases significantly. For instance, the bandgap of  $\text{ZrS}_3$  is about 1.92 eV, whereas the bandgap of  $\text{ZrSe}_3$  is 0.92 eV. Note also that in their TMDC counterparts, the  $\text{ZrS}_2$  monolayer can transform from an indirect to a direct bandgap semiconductor when the uniaxial tensile strain is at  $\varepsilon = 8\%$ .<sup>51</sup> The  $\text{TiS}_2$  monolayer can also undergo the indirect-to-direct bandgap transition under the uniaxial strain of  $\varepsilon = 10\%$ . In contrast, the  $\text{ZrS}_3$  and  $\text{HfS}_3$  monolayers can undergo the indirect-to-direct bandgap transition at a much lower tensile strain ( $\varepsilon = 2\%$ ). It seems that the indirect-to-direct bandgap transition can be induced more easily for the  $\text{MX}_3$  monolayers than for their  $\text{MX}_2$  counterparts by the tensile strain. The direct bandgap character and high bandgap tunability by strain as well as the availability of metallic and semiconducting properties of  $\text{MTe}_3$  ( $M = \text{Hf}$  and  $\text{Zr}$ ) provide new

opportunities for designing artificial layered structures for applications in optoelectronics and flexible electronics.

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