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Shading in TXRF: calculations and experimental validation using a color X-ray camera

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Absorption effects in total reflection X-ray fluorescence (TXRF) analysis are important to consider, especially if external calibration is to be applied. With a color X-ray camera (CXC), that enables spatially and energy resolved XRF analysis, the absorption of the primary beam was directly visualized for μL -droplets and an array of pL-droplets printed on a Si-wafer with drop-on-demand technology. As expected, deposits that are hit by the primary beam first shade subsequent droplets, leading to a diminished XRF signal. This shading effect was quantified with enhanced precision making use of sub-pixel analysis that improves the spatial resolution of the camera. The measured absorption was compared to simulated results using three different model calculations. It was found they match very well (average deviation < 10%). Thus errors in quantification due to absorption effects can be accounted for in a more accurate manner.

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1. Introduction

In the semiconductor industry the impurities on a silicon-wafer are collected in a single droplet by vapor phase decomposition-droplet collection (VPD-DC), where the SiO_2 surface is dissolved in HF. That single droplet is then analyzed with TXRF.¹

The amount of impurities is crucial, because every impurity changes the doping of the Si-crystal and therefore its electrical properties.² For the quantification of these impurities, in general, external calibration is used.³ The standards for the calibration method ideally are required to show no absorption effects, meaning the thin film approximation is valid for the incoming beam as well as for the emitted fluorescence.⁴ For amounts of sample that exceed the critical thickness saturation effects are observed, which lead to errors in quantification.⁵

In total reflection X-ray fluorescence analysis the primary beam hits the sample and the fluorescence is usually detected by a semiconductor detector perpendicular to the surface. To achieve total reflection conditions the incident angle on the sample holder has to be 0.1° or below.⁶ The beam is then totally

reflected off the sample holder which has two major effects: the excitation of the sample on the sample holder is enhanced – because simplified the beam passes the sample twice – and the beam penetration of the sample holder is drastically reduced.⁷ Both these effects improve the lower limit of detection into the ppb region, sometimes even better.⁸ With a primary beam almost parallel to the sample holder, matrix effects are important to consider. In an ideal thin sample below the critical thickness, matrix effects are eliminated and the fluorescence signal is directly proportional to the analyte concentration and to the thickness of the sample.⁴ The number of counts for low energy photons, emitted by low Z elements like scandium, and high energy photons, *e.g.* those emitted from copper, is the same for equal concentrations after their relative sensitivities (most notably fluorescence yield and efficiency of detection) have been taken into account. However real samples often exceed the critical thickness and matrix effects do occur: the sample absorbs way more of the primary beam, shading itself, so that parts further down in the beam path do not experience the same excitation than those hit by the beam first. This has an effect on the accuracy of the results for every specimen exceeding the critical thickness. If, for example, an internal standard is distributed in homogeneously and the sample exceeds the critical thickness, the fluorescence signal will be either too high if the standard is hit by the primary beam first, or too low if the standard is shaded by the sample.^{9,10} This shading effect is especially important if external calibration is to be applied.¹¹

The second major effect besides the shading effect (absorption of the primary beam) is the absorption of the X-ray

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fluorescence within the sample. Low energy photons are readily absorbed prior to leaving the material and reaching the detector, which results in a lower peak area. This, like the primary beam absorption, can be described by eqn (1) assuming a monochrome parallel bundle of rays, where the mass-attenuation coefficient expresses the dependence of the absorption from the composition of the material and the energy of the X-ray photons.⁶

$$I = I_0 e^{-\frac{\mu}{\rho} d \rho} \quad (1)$$

In eqn (1) I is the intensity, I_0 the primary beams intensity, μ/ρ the mass attenuation coefficient and d the distance the beam passes through the specimen of the density ρ .

Experimental visualization of the actual absorption is challenging, since it requires not only spatially resolved detection, but also covering enough of the studied specimen without moving it to monitor the brightened and the shaded parts of the sample at the same time. Scanning techniques change the illumination of the sample with each step of movement in the primary beam and are therefore not suitable. In the approach presented here the requirements are met by a new compact pnCCD-based color X-ray camera with high spatial and energy resolution.¹² The camera enables full field XRF imaging and therefore the two major matrix effects described before can be measured. The severe influence of these effects is demonstrated for μL -droplets, which were analyzed immediately after preparation before drying. In principal liquids should be ideal objects to study absorption effects. A homogeneous mass distribution and a defined continuous shape can be assumed in an aqueous droplet. However, our experimental results show, that these assumptions need to be refined.

Absorption effects in TXRF have been the subject of model calculations.^{11,13} Horntrich *et al.* proposed a model in search for the ideal sample shape, meaning the highest fluorescence intensity and the lowest saturation effect.^{14–16} In their comparison of sample types of a cuboid, cylinder, spherical segment and ring shapes the ring shape exhibited the lowest saturation effect and lead to the highest fluorescence intensity.

Experimental validation of this model however was difficult, since liquids do not dry to give defined morphologies. This is where the sample preparation needs to provide as much a defined morphology as possible. Arrays of pL-droplets can be printed with ink jet printing technology.¹⁷ This technique provides fairly uniform deposits which can be analyzed with the CXC. The first results introducing this procedure were published recently in ref. 18. However, the data evaluation in that work was hampered, by the spatial resolution of the 2D fluorescence maps. Additionally, a simplified physical structure was assumed. In order to improve upon the initial results, sub-pixel analysis¹⁹ was used to enhance the spatial resolution of the CXC. This approach is especially important in assigning fluorescence counts to the deposits from which they are emitted. In this work we compare the experimental results to model calculations obtained with three different models. Since model calculations depend on the accuracy of the parameters used in

the models a detailed analysis of the sample morphology was done with atomic force microscopy. This technique provides detailed information of the physical structure of the residues from the pL-droplets. The data enabled modeling using two other numerical approaches. The refinements on the physical structure in combination with these models will eventually enable to eliminate uncertainties introduced by morphology and allow to better understand other factors *e.g.* scattering and divergence of the primary beam. The work presented here significantly improves on the work reported in ref. 16. It presents the next logical step to a considerable improvement of TXRF analysis understanding of the shading effects.

It should be noted this initial modeling is designed to explain the measurements obtained. At this point it is not intended to do in-depth statistical evaluations of the merits of the different calculation models. However the quantification of absorption effects in TXRF analysis starts with understanding the measured data and this work shows the feasibility of this approach.

2. Experimental

2.1. Chemicals

Cu, Sc, Ni and Mn single element standard solutions (1 g L⁻¹, Certipur ICP-standards, Merck, Darmstadt, Germany) were used for the preparation of the liquid drops on the microscope slide. A Ni standard solution (10 g L⁻¹) was used for the preparation with the pL-pipette.

2.2. Sample preparation

2.2.1. μL -droplets. Droplets of 10 μL of four different standard solutions (Cu, Sc, Ni and Mn with 1 g L⁻¹) were pipetted on a microscope slide and immediately analyzed with SR-TXRF at the BAMline@BESSY II (Berlin, Germany) before drying. The Cu and Sc droplets merged to one single droplet of 20 μL containing both elements.

2.2.2. pL-droplets. An array of 62 droplets of 110 pL Ni standard solution containing 5 g L⁻¹ was printed with an ultrasonically driven micropipette²⁰ (GIX Microplotter II, Sono-Plot, Inc., Middleton, WI, USA) on a 200 mm Si-Wafer. The amount of Ni measured is 550 pg per droplet is supported by the volume of the dried residues which was determined by AFM measurements. The picoliter droplet array was analyzed with SR-TXRF at the BAMline@BESSY II (Berlin, Germany).

2.3. Measurements

Synchrotron TXRF measurements were carried out at the BAMline@BESSY II (Berlin, Germany) with an incident angle of 0.05°. The energy of the primary beam was set to 9.67 keV using a double W/Si multilayer monochromator system. This particular energy was selected due to its frequent use in lab instruments with X-ray tubes equipped with a tungsten target. In addition the excitation of the Ni K_z in the pL samples is high at 9.67 keV. More details about the beam line can be found elsewhere.²¹



2.4. Instruments

2.4.1. SLcam®. The X-ray fluorescence emitted from the samples was detected by the color X-ray camera SLcam®. It is a compact, pnCCD-based X-ray camera. The pnCCD detector is designed for ultrafast readout (1000 Hz) and contains 264×264 pixels, with a pixel size of $48 \times 48 \mu\text{m}^2$, which results in an imaged area of $12.67 \times 12.67 \text{ mm}^2$. The combination of the pnCCD with a parallel polycapillary optic with approximately 70 000 capillaries ($\varnothing = 20 \mu\text{m}$) enables full field X-ray imaging.¹² Additionally, measurements with a higher spatial resolution were carried out using a prototype $8\times$ magnifying conical shaped optic.²² This particular type of polycapillary lens ($\varnothing = 2 \mu\text{m}$) increases the resolution limit down to several micrometers. However, the prototype exhibited strong optical defects and could not be used for quantitative analysis.

2.4.2. AFM. A Nanowizard® from JPK Instruments (Berlin, Germany) was used for atomic force microscopy measurements in intermittent contact-mode. The standard Si tip had a diameter of 10 nm, the resonance frequency was 180 kHz and the constant force 25 N m^{-1} .

2.4.3. Optical microscopy. An optical microscope (VHX 2000 series, Keyence, Osaka, Japan) was used to determine the diameter of the pL-droplet residues as well as the distance between the deposits.

3. Results and discussion

3.1. μL -droplets

Absorption in droplets having μL volumes was studied with SR-TXRF. A homogeneous elemental distribution in each droplet was assumed. Besides the perimeter of the droplets, where fluorescence is lower due to lower heights of the droplet, an equal number of counts would be expected over the whole droplet if no absorption effects occur. Instead, because of the nearly parallel excitation beam a reduction of the incoming beam intensity over the traveled distance in the droplet is expected. For example by assuming a constant concentration of Cu and Sc of 1 g L^{-1} and using a diameter of 0.28 cm (which is the diameter determined from the fluorescence profile) calculation of the signal according to eqn (1) results in the reduction of the signal to $I/I_0 = 0.187$. Similar reduction is observed by the experimental approach. Fig. 1 shows the result of a SR-TXRF measurement with 10 min live time. The combined Cu and Sc droplet (green, $4.7 \times 2.8 \text{ mm}^2$) absorbs the primary beam in such a way, that the Ni (purple, $\varnothing = 3.1 \text{ mm}$) and Mn (red, $\varnothing = 3.0 \text{ mm}$) droplets get only partly excited (note lighter color means higher intensity). The highest signals for these droplets are observed where the primary beam misses the combined droplet. Fig. 2 shows the middle part ($1.5 \times 3.2 \text{ mm}^2$) of the combined Cu and Sc droplet seen in Fig. 1. In Fig. 3 the Cu and Sc fluorescence over the course of the droplet diameter is shown as a line scan. Within this volume the primary beam is almost completely absorbed.

Besides the shading effect, the absorption of low energy fluorescence photons is the second effect, which has to be taken into account. The experimental data show that the Sc

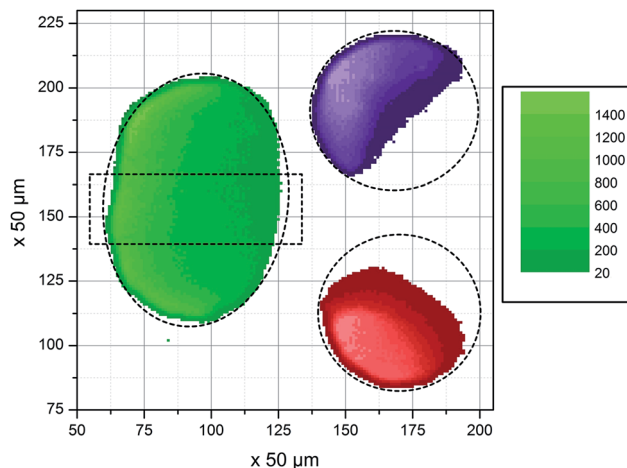


Fig. 1 Absorption of the primary beam (coming from the left) demonstrated with four μL -droplets containing different elements: combined Cu and Sc droplet (green), Ni (purple) and Mn (red). Dashed lines represent assumed position of the droplets, as well as the part of the Cu & Sc droplet shown in Fig. 2.

fluorescence count rate decreases stronger than the Cu counts in the middle of the droplet (Fig. 3). This is due to the higher mass attenuation coefficient for the Sc K_{α} radiation compared to Cu K_{α} radiation. The dimensions of the droplet are beyond thin film approximation,⁴ thus absorption effects occur and a reduction of fluorescence intensity of around 80% for Sc and around 50% for Cu compared to a thin film can be expected. The ratio between the counts of the Cu and the Sc fluorescence found here is around 1 at the upstream boundary of the droplet, and then increases over $350 \mu\text{m}$ into the droplet to stay between 6 and 8 over the middle of the droplet and decreases to around 1

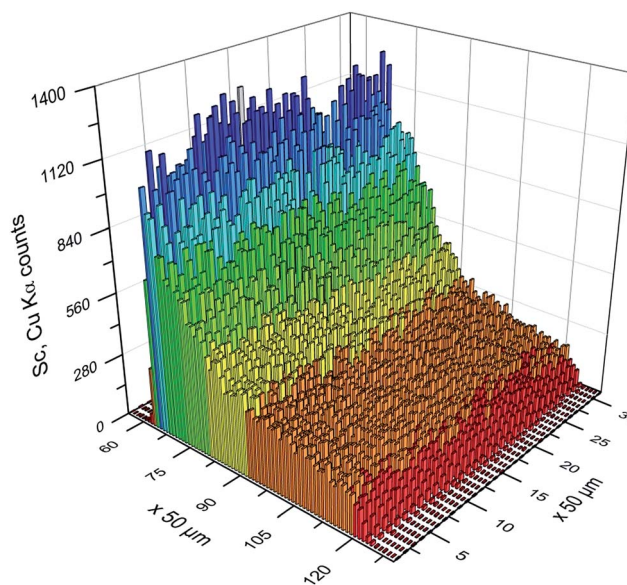


Fig. 2 Detailed view on the fluorescence of the middle of the combined Cu and Sc droplet, showing the decreasing signal and hence the almost complete absorption of the primary beam.



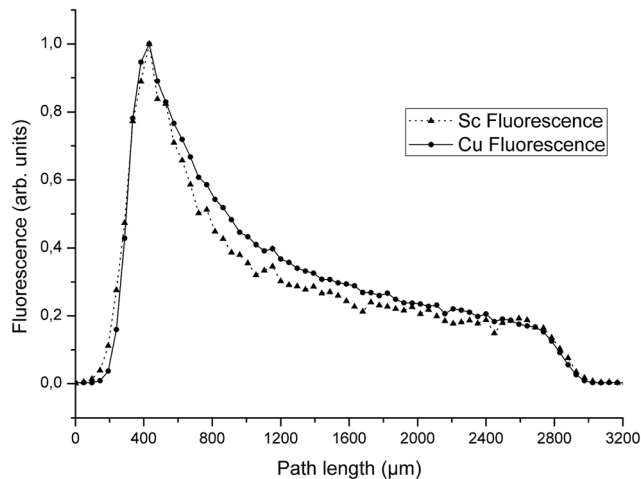


Fig. 3 Normalized Sc and Cu fluorescence through a part of the middle of the droplet. The Sc fluorescence decreases more rapidly following the maximum and increases relatively to Cu at the end of the droplet.

at the downstream boundary (Fig. 4). It has to be stressed, that this comparison is only possible, because each pixel of the camera records a full spectrum from 3 to 40 keV.¹²

Though the concentration of Cu and Sc in the droplet are the same, the relative sensitivities for detecting their respective K_{α} -lines are different. For a better understanding of the experimental Cu/Sc ratio the expected ratio can be estimated from fundamental parameters. Therefore the fluorescence signal of an element (I_e) in TXRF can be calculated by the equation (Table 1):^{23–27}

$$I_e = C_e \alpha I_0 \tau_e \left(\frac{S-1}{S} \right) P_{e,K_{\alpha}} \omega_{e,K} \quad (2)$$

In order to calculate the expected intensities for both elements Sc and Cu the most significant values are the photoelectric cross section (τ_e) and the fluorescence yield ($\omega_{e,K}$). c_e , I_0

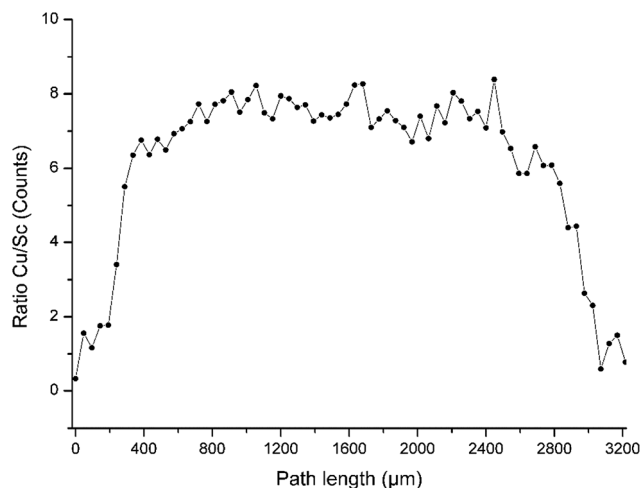


Fig. 4 The ratio Cu to Sc X-ray fluorescence intensity shown for a part of the droplet is between 6 and 8 for most of the droplet except at the edges of the droplet.

and $P_{e,K_{\alpha}}$ are considered to be equal, as well as α , where the differences in detector efficiency are neglected. Although the difference in the edge jump ratio is small, it is not neglected. With data tabulated in ref. 28 the Cu/Sc intensity ratio was calculated for the energy of exiting X-ray beam (9.67 keV), as well as for 17.4 keV, for which relative sensitivities from a commercial benchtop instrument were available for comparison. The obtained results are shown in Table 2.

The values calculated from fundamental parameters match quite well with the value calculated from relative sensitivities. In Fig. 4 the fluorescence ratio of Cu/Sc at the beginning of the droplet starts at 1, since no significant counts are recorded. The ratio then increases over the course of 350 μm into the droplet to Cu/Sc = 6.4. Cu/Sc ratios above 5 as determined from the relative sensitivities can be interpreted as a result of the absorption of the Sc fluorescence within the droplet, hence less Sc fluorescence reaches the detector and the ratio of Cu/Sc increases. The ratio ranges from 6 to 8 over the course of the droplet and then the ratio decreases similar to the increase observed at the beginning of the droplet.

Although these values seem reasonable, the absorption of the fluorescence within the droplet is very low. The primary beam intensity ($E = 9.74$ keV) as shown in Fig. 2 was reduced to 30% halfway through the droplet (*ca.* 1400 μm). Consequently the low energy Sc fluorescence should experience strong absorption on its way through the droplet towards the detector. By assuming constant concentration (*i.e.* fluorescence) over the droplet height (assuming 1400 μm) and calculating the reduction due to absorption for Sc and Cu fluorescence separately, then integrating the reduced fluorescence intensities over the height of the droplet the fluorescence intensity is reduced to 13% ($I/I_0 = 0.126$) for Sc and to 56% ($I/I_0 = 0.560$) for Cu compared to the intensity expected without any absorption such as in a thin film. With the relative sensitivities taken into account the ratio of Cu/Sc should rise to values around 20. Hence, based on our calculations, the expected absorption leads to much higher ratios while assuming a homogeneous distribution and constant density near 1 g cm^{-3} , as well as the height of the droplet of 0.14 cm.

Higher intensity of the Sc fluorescence could be caused by secondary excitation. The energy of the Cu fluorescence is sufficient to excite the Sc atoms, whereas no fluorescence is able to excite the Cu and the ratio of Cu/Sc decreases. By taking the photoelectric cross section of Sc at 8.04 keV (Cu K_{α} line) into account and calculating the fraction absorbed by Sc over a distance of 1400 μm the resulting intensity ratio is $I/I_0 = 0.97$, which means 3% of the Cu K_{α} photons are absorbed by Sc and can give rise to additional fluorescence. Accordingly, the secondary fluorescence cannot account for the differences between measurement and calculation. Ratios of 6–8 for Cu/Sc can only occur if the absorption of fluorescence is much lower than assumed for our calculations. Accordingly, either the concentration or the distance assumed in the calculations according to eqn (1) are lower. It is most probable both situations are the case. Deegan²⁹ has convincingly shown that “coffee-ring” like drying of droplets is caused by an outward transportation of material in the droplet which in the edges end



Table 1 Description of variables in eqn (2)

Variable	Description	Comment
I_e	Intensity of K_{α} fluorescence for element e	
c_e	Concentration of element e	
α	Geometry factor	Includes setup intrinsic influences (incoming and outgoing angles, detector efficiency)
I_0	Intensity for a given energy of primary beam	
τ_e	Photoelectric cross section	
$\left(\frac{S-1}{S}\right)$	Edge jump ratio	Considers only the K edge, not L
$P_{e,K_{\alpha}}$	Ratio of K_{α} to all possible K transitions	$\frac{K_{\alpha}}{\sum(K_{\alpha} \cdots K_{\omega})}$
$\omega_{e,K}$	Fluorescence yield	

Table 2 Calculated ratios from intensities of X-ray fluorescence from fundamental parameters compared with values calculated from relative sensitivities from a commercial benchtop instrument^a

	Cu/Sc
Calculated 9.67 keV	4.92
Calculated 17.4 keV	5.44
Calculated from rel. sensitivities 17.4 keV ^a	5.07

^a Benchtop instrument: Model S2 Picofox (Bruker nano, Berlin, Germany), which was not used in this work for any measurements, only the rel. sensitivities are consulted for comparison, the energy of the primary beam is given by the molybdenum tube target.

up with all material at the rim of the dried droplet and no material in the inner region. This is supported by the final appearance of the dried deposit which is shown in Fig. 5.

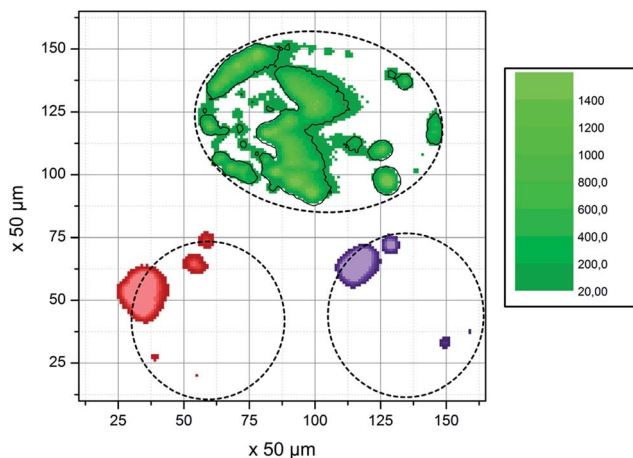


Fig. 5 Dried residues from the droplets shown in Fig. 1. No uniform residue is formed, but rather small spots that tend to be near the edges of the droplets. It should be noted that the sample was moved between measurements, so the position of the pixels on the sample differs from Fig. 1.

These processes have already negated our assumption of a constant concentration throughout the droplet. Additionally, it is likely that the droplet is already shrunken to a reduced height by evaporation by the time the measurements were performed.

3.2. pL-array

In TXRF usually dried residues from μL -sized volumes are analyzed. Dried residues from such large volumes do not produce a well-defined specimen, which makes it difficult to design a sample with defined morphology. A well-defined morphology of the specimen is desired to model and better understand the matrix effects. The Microplotter used here provides arrays of pL droplets, which dry to give well-defined residues. Fig. 6 shows a measurement displaying the 62 deposits of the array.

As expected, the deposits hit by the primary beam first usually show the highest fluorescence. Each deposit shades the subsequent deposits. The absorption of the primary beam is equivalent to the reduction in fluorescence intensity. Therefore, the fluorescence intensity of each deposit needs to be determined.

The mean diameter of the deposits was found to be $25 \mu\text{m}$ and the distance between the deposits varied from 171 to $224 \mu\text{m}$ using optical microscopy. This translates to 1/2 pixel covered by a deposits and 4–5 pixel covering the space in-between deposits. The spatial resolution of the polycapillary optic is in the range of the pixel diameter, so that the spatial resolution of the camera is determined by the pixel size of $48 \times 48 \mu\text{m}^2$.³⁰ Although the fluorescence signal of a $25 \mu\text{m}$ deposit is smaller than one pixel, the signal may expose more than one pixel, e.g. the boundary of two pixels is exposed. Consequently the deposits may overlap to a certain level, which hampers resolving of the individual residue intensities.

One approach to solve this problem is to define a high, linear background, so that only pixels with high fluorescence remain,

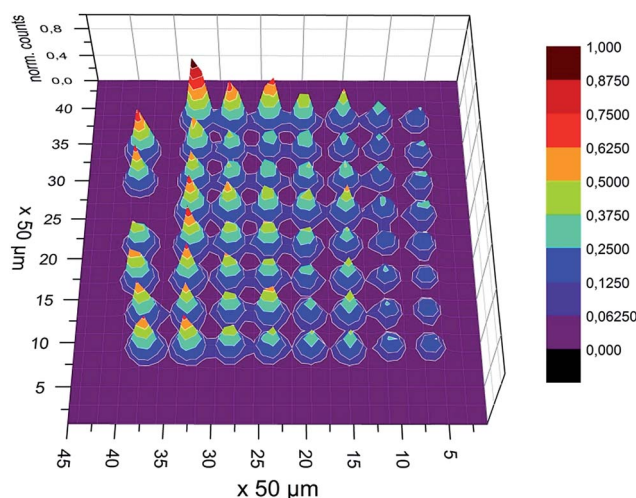


Fig. 6 Ni XRF signal intensity measured with the color X-ray camera from the 62 deposits array with the exciting beam coming from the left.



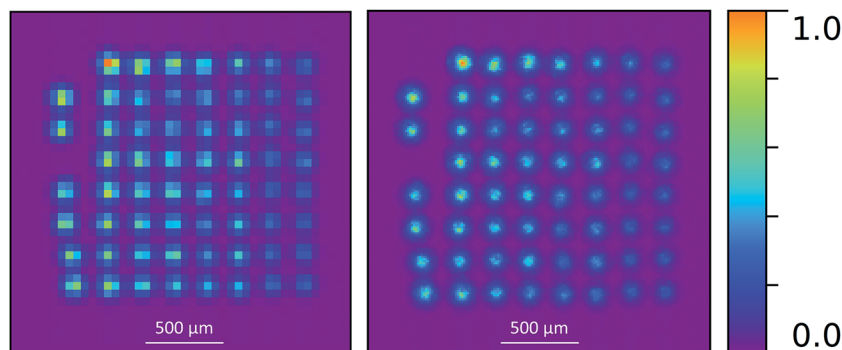


Fig. 7 Comparison between no sub-pixel (left) and 4×4 (right) sub-pixel analysis. The latter shows a better resolution and more detailed structure.

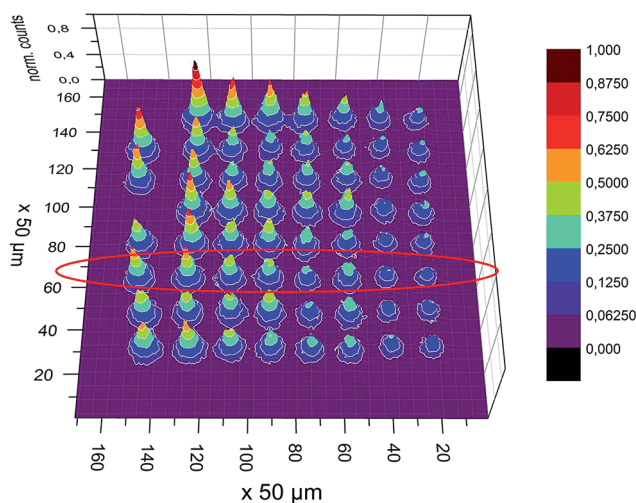


Fig. 8 The same measurement as in Fig. 6, but with 4×4 sub-pixel analysis, clearly showing a more detailed structure. The red circled row of deposits were used in the model comparison.

and those are easier to assign to single deposits.¹⁶ Another way is to take into account additional information which is available on the position of an electron cloud generated by incoming fluorescence photons on the detector. That can be done by sub-pixel analysis, where the position of the photon hit is

Table 3 The attenuation of the fluorescence yield measured for 30 min at the BAMline@BESSY II for the indicated line of the pL-array. This data is from a single measurement. Errors resulting from counting statistics are below 1%

	Counts	Percentage
I_1	26 166	100%
I_2	24 862	95.02%
I_3	21 758	83.15%
I_4	19 915	76.11%
I_5	14 314	54.70%
I_6	17 298	66.11%
I_7	11 522	44.03%
I_8	9808	37.48%

approximated from the electron cloud distribution.²⁸ As a result one real pixel is separated in several theoretical sub-pixels, in this case 4×4 . Sub-pixel analysis improves the spatial resolution to $\sim 45 \mu\text{m}$ (ref. 28) but more importantly it increases the available contrast and pixel separation between the deposits. We can then distinguish between the deposits without losing counts as is illustrated in Fig. 7 and 8. Of particular note, in Fig. 8, most deposits have been clearly resolved compared to the deposits shown in Fig. 6, where a majority of the between-deposit space appears to be filled with signal.

After implementing the sub-pixel data processing procedure the fluorescence intensity was integrated over each individual deposit. The results for the selected line of deposits circled in Fig. 8 are given in Table 3 going from left to right.

The fluorescence of the first deposit is set to 100%, assuming that the deposit hit by the beam first should show the highest signal. In order to understand how exactly the absorption took place three different models were used to simulate the data and are discussed in the following section.

3.3. Calculations

3.3.1. Model A. Absorption processes can be described by eqn (1) assuming a monochrome parallel bundle of rays which was already described in ref. 16. This model assumes a beam parallel to the wafer that is not reflected, and considers only the absorption of the primary beam and no absorption of fluorescence. The shape of each deposit was modeled as a cylindrical volume. However, the dimensions of the deposits were refined. The dimensions of the height and the diameter were derived from measurements with atomic force microscopy with the open-source software Gwyddion.³¹ The AFM measurement of one deposit is shown in Fig. 9.

Another parameter that was subject to consideration is the density. In (16) only the density of Ni is considered. In this work the density of the residue $\text{Ni}(\text{NO}_3)_2 \times 6\text{H}_2\text{O}$ is taken into account, where the amount of Ni is known through the preparation process. We assume the formation of $\text{Ni}(\text{NO}_3)_2 \times 6\text{H}_2\text{O}$, since it is very stable and the sample is used in ambient air, so no anhydrous form, which is hygroscopic, can be expected. The tabulated value for the density of $\text{Ni}(\text{NO}_3)_2 \times 6\text{H}_2\text{O}$ is 2.05 g cm^{-3} .³² However it is reasonable to assume the actual density is



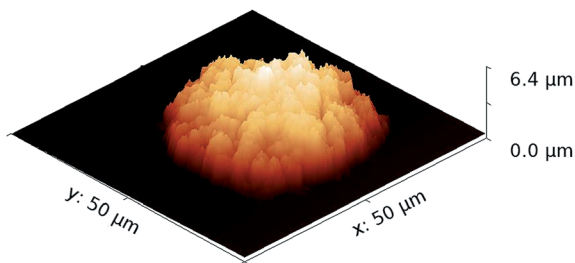


Fig. 9 AFM measurement of one of the pL droplet residues with a maximum height of 6.39 μm and 2527 μm^3 volume. The volume was determined from summing up the height of each pixel.

lower, since the residue does not dry to form a single crystal, is not completely uniform and might include cavities. Consequently, in this work the density of the residues was a fitting parameter. A density near 1 g cm^{-3} gave the best results, presumably because the deposit is not a single crystal.

3.3.2. Model B. The second model was developed by Christine Horntrich³³ and applied by Peter Hischenhuber.³⁴ The dried residues are approximated by hemispherical segments which are built by a discrete number of towers. While perfectly aligned residues are assumed, the volume for each residue as determined by the AFM measurements was used. The density derived from the calculations with model A was used for all residues. The sample is excited by the incident and the reflected beam. Whole sample irradiation is simulated by evaluating the footprint of the system dependent on the incident angle. The calculation of the fluorescence intensity is done for every tower separately, considering absorption of the primary beam by the preceding towers. The incoming X-rays consisted of many individual beams corresponding to the width of each sample tower. For each deposit tower it is distinguished if it could be fully irradiated, partially irradiated or not irradiated by any individual beam. To obtain the total emitted fluorescence the intensities emitted by each tower are summed up. Beam divergence is neglected as well as secondary absorption of the emitted fluorescence.

3.3.3. Model C. A third model, developed by Stanisław Nowak,³⁵ uses a two dimensional ray tracing approach based on the concept of Geometrical Optics (GO), which tracks the full evolution of plane waves from their source to the point, where they are absorbed. The model takes reflection, refraction, primary absorption effects and the roughness of the structures surface into account. The model uses information from microscopic images to estimate the exact shape and position of the deposits. In order to construct an adequate morphology input, the AFM images for each deposit were aligned with positions obtained from the optical microscope image. Finally the deposits were approximated by a set of cuboidal towers, each corresponding to a pixel of a given height taken from the AFM images. Again it was assumed the residue consists of $\text{Ni}(\text{NO}_3)_2 \times 6\text{H}_2\text{O}$. In order to get the best agreement with the measured data the density obtained from model A was used. The best fit to measured intensities was found slightly varying the alignment of the primary beam with respect to the deposit

pattern. Similarly to the previous models the intensities emitted by each tower are summed up within a droplet resulting in the total emitted fluorescence. Again beam divergence and secondary absorption of the emitted fluorescence were neglected.

3.4. Comparison of the calculation models to measured data

The main difficulty in modeling the TXRF intensities of dried deposits is related to the density of the residues. It appears that in all three models the density had to be significantly lowered ($\rho = 1.15 \text{ g cm}^{-3}$) with respect to the tabulated value for $\text{Ni}(\text{NO}_3)_2 \times 6\text{H}_2\text{O}$ ($\rho = 2.05 \text{ g cm}^{-3}$). We believe that this reduced density is caused by the morphology of the deposits, which does not dry to give a single crystal. We observed scratches, granulation and cavities in the optical images of the deposit. Provided that the density variation is justified, all calculation models appear to describe the measured decrease of TXRF intensity rather well. However, an unusual variation of the intensity for the fifth (I_5) and sixth deposit (I_6) is only reproduced by model C.

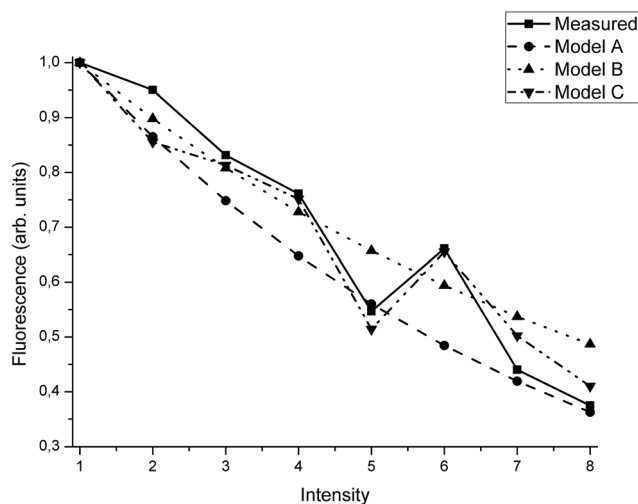


Fig. 10 Comparison of the measured intensity and the three calculation models. The agreement is good, and model C is able to follow the measured values best. The values are shown in Table 4.

Table 4 The deviations between the measured value given in Table 3 and the three calculation models are shown, with the average value in the bottom row. This shows model C is best, because it can account for the difference in the sixth droplet (I_6), which the other models can't, and still give a good fit

	Model A	Model B	Model C
I_1	0.00%	0.00%	0.00%
I_2	8.51%	5.22%	9.47%
I_3	8.31%	2.35%	1.84%
I_4	11.36%	3.31%	0.96%
I_5	1.31%	11.00%	3.27%
I_6	17.65%	6.71%	0.59%
I_7	2.11%	9.67%	6.20%
I_8	1.22%	11.22%	3.53%
Average (without I_0)	7.21%	7.07%	3.70%



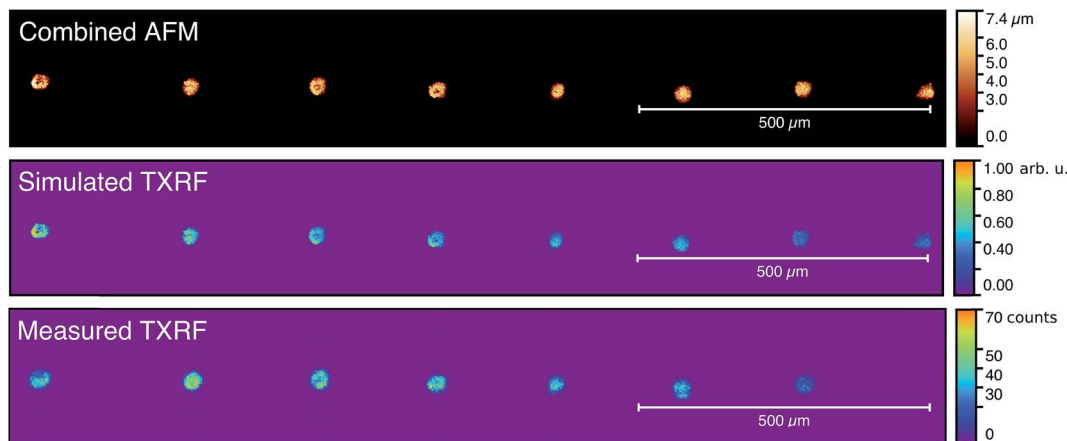


Fig. 11 Comparison of deposit morphology (top panel), TXRF intensity simulated with model C (middle panel), and intensity measured with X-ray Color Camera image equipped with 8 : 1 magnifying optics (bottom panel). X-ray beam direction is from left to right.

Models A and B do not take into account the refined sample morphology. Both models assume the deposits to be perfectly aligned and have the same idealized shape. The AFM measurements clearly show that is not the case.

When a droplet is printed on the wafer it occupies a certain area. The evaporation of the solvent leads to a smaller residue. Due to the hydrophobic surface of a Si wafer, the residue usually forms within the area that was once occupied by the droplet, because the droplet did not spread out, but contracts as it dries. However the fact that the residue is smaller than the original liquid droplet is conceivable because the residue is within a much larger area wetted by the original liquid droplet. This means there is some degree of variability for the final location of the residue, and results in the residues not being perfectly aligned on the micrometer scale. As a consequence consecutive deposits are not shaded in the same way and fluorescence variations are expected to occur.

Model C uses information from microscopic images to estimate the exact shape and position of the deposits. Therefore this model can “see” the morphological alternations and consequently approximate the resulting intensity variations.

The comparison of the measured XRF and the simulated results of the three different models are shown in Fig. 10 and Table 4.

On average, model C predicts the deposit intensity better by a factor of 2 compared to models A and B. On the other hand, the simple models require less information to work properly.

The performance of model C is illustrated in the following section. It produces a spatially resolved fine structure of fluorescence correlated to specimen morphology. The comparison to high resolution Ni fluorescence maps show that this fine structure is also found in the experiment. In order to identify the local variation of fluorescence intensity and trace the shading effects an additional measurement was carried out using an 8 : 1 magnifying polycapillary optic. Unfortunately the quality of the measurements was low due to the diminished XRF signal caused by the magnifying optic. Therefore the measurements compared to the calculation models were performed with a straight polycapillary without magnification. In

Fig. 11 the image recorded with the color X-ray camera is compared to the simulation using model C as well as to a combined AFM image that provided the morphology input for the model. The pictures are aligned with the X-ray beam direction which runs from left to right. Accordingly, for each pixel row, calculations were performed independently.

For all images deviation in the alignment of the deposits is clearly visible. In addition simulated TXRF shows the correlation between height of the droplet and fluorescence intensity. Shading is visible for at least three effects: (1) the total intensity from consecutive deposits decreases, (2) the deposits hit by the primary beam first exhibit higher fluorescence intensity, and (3) for the deposits that are not fully shaded by the previous residues (*e.g.* deposits 4 and 6) the shaded region has a much lower intensity. Accordingly increased intensity of deposit 6 (I_6) can be explained by the deviation from the perfect alignment caused by the drying process of the residue. At the same time the intensity drop for the fifth residue (I_5) can be explained by a reduced volume.

The image recorded with the X-ray color camera shows the same features as the simulation. Positioning, deposit size and shading effects correspond well to the modeled ones. However, due to polycapillary imperfections the relative intensity varies much along the structure, *e.g.* the first deposit appears less intense and the last deposit is totally missing as it lies beyond the field of view of the magnifying optic. Therefore the measurement with magnifying optic is not suited for qualitative comparison of the intensity.

4. Conclusions and outlook

The color X-ray camera measurements of the absorption in liquid μL -droplets deposited on microscope slide and excited with SR-TXRF show that shading is a severe effect. Until recently – though model calculations had predicted effects of the magnitude found here – no experimental approach for visualizing the shading was available. We show that within a few millimeters of a combined Cu and Sc standard (1 g L^{-1}) the monochromatic synchrotron beam of 9.67 keV is absorbed almost completely. Within the same droplet the absorption of



fluorescence photons could be shown by the ratio of Sc/Cu counts over the course of the droplet. However, there are still open questions *e.g.* the calculations show a less steep decrease in intensity. The proposed experimental approach will allow detailed study and refinement of our knowledge on shading and may eventually probe the mass transport in a drying droplet by applying the refined models.

Turning to smaller droplets in the pL-range we show that even the small, dried residues from pL-droplets printed with the SonoPlot Microplotter show considerable absorption of the primary beam. Within one line of eight subsequent deposits each containing 550 pg Ni the last deposit gets excited by only about 40% of the primary beams intensity. However, the precision of the measurements was greatly improved with the use of sub-pixel analysis. The amount of absorption was simulated with three different models in good agreement with the measured data. Best results were obtained with the most sophisticated model; however model C requires the most detailed knowledge of the samples morphology and alignment of the deposits. The good agreement of calculation and experiment enables the calculation and quantification of absorption effects, although it should be noted that the morphology of the sample should be as well-known as possible to ensure accurate results.

It seems evident that without precise knowledge on sample morphology a detailed analysis of dried deposits would be hindered. Dedicated TXRF stations that would combine AFM imaging with X-ray intensity measurements seems to be a potential challenge. Even though the current simulation procedure seems demanding the authors suggest that simpler physical models, such as the attenuation law can be adapted to accept more advanced morphology input. In that respect a combination of AFM with the X-ray color camera, preferably with a high-quality, high-resolution optic, appears to be the most suitable method for advanced investigations.

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References

1 C. Neumann and P. Eichinger, Ultra-trace analysis of metallic contaminations on silicon wafer surfaces by

vapour phase decomposition/total reflection X-ray fluorescence (VPD/TXRF), *Spectrochim. Acta, Part B*, 1991, **46**, 1369–1377.

- U. Hilleringmann, in *Silizium-Halbleitertechnologie*, B.G. Teubner: Stuttgart Leipzig, 1999, p. 150.
- Y. Mori, Summary of ISO/TC 201 Standard: XIX ISO17331: 2004—Surface chemical analysis—Chemical methods for the collection of elements from the surface of silicon-wafer working reference materials and their determination by total-reflection X-ray fluorescence (TXRF) spectroscopy, *Surf. Interface Anal.*, 2005, **37**, 522–523.
- R. Klockenkämper and A. von Bohlen, Determination of the critical thickness and the sensitivity for thin-film analysis by total reflection X-ray fluorescence spectrometry, *Spectrochim. Acta, Part B*, 1989, **44**, 461–469.
- Y. Gohshi, Y. Mori, N. Yabumoto, K. Kawai, K. Araki, A. Urano, S. Kozono, H. Shibata, A. Shimazaki, S. Taniike, T. Nakama, K. Nishihag, H. Horie, M. B. Shabani, K. Yakushiji and M. Yamagami, ISO/TC201/WG2 Activities: VPT-TXRF Round Robin Results and Perspective, *TXRF conference*, Trento, Italy, 2007.
- R. Klockenkämper, in *Total-Reflection X-Ray Fluorescence Analysis*, John Wiley & Sons, New York, 1997, pp. 2–17.
- P. Wobrauschek, Total reflection X-ray fluorescence analysis – a review, *X-Ray Spectrom.*, 2007, **36**, 289–300.
- R. Klockenkämper and A. von Bohlen, Elemental Analysis of Environmental Samples by Total Reflection X-Ray Fluorescence: a Review, *X-Ray Spectrom.*, 1996, **25**, 1556–2162.
- A. Prange and H. Schwenke, Trace element analysis using total reflection X-ray fluorescence spectrometry, *Adv. X-Ray Anal.*, 1992, **35**, 899–923.
- C. Horntrich, S. Smolek, A. Maderitsch, R. Simon, P. Kregsamer and C. Strelí, Investigation of element distribution and homogeneity of TXRF samples using SR-micro-XRF to validate the use of an internal standard and improve external standard quantification, *Anal. Bioanal. Chem.*, 2011, **400**, 2649–2654.
- C. Horntrich, P. Kregsamer, S. Smolek, A. Maderitsch, P. Wobrauschek, R. Simon, A. Nutsch, M. Knoerr and C. Strelí, Influence of the excitation energy on absorption effects in Total Reflection X-ray analysis, *J. Anal. At. Spectrom.*, 2012, **27**, 340–345.
- O. Scharf, S. Ihle, V. Arkadiev, A. Bjeoumikhov, G. Buzanich, R. Hartmann, M. Kühbacher, M. Lang, M. Langhoff, A. Liebel, M. Radtke, U. Reinholz, H. Riese-meier, H. Soltau, L. Strüder, A. F. Thünemann and R. Wedell, Compact pCCD-Based X-ray Camera with High Spatial and Energy Resolution: A Color X-ray Camera, *Anal. Chem.*, 2011, **83**, 2532–2538.
- D. Hellin, W. Fyen, J. Rip, T. Delande, P. W. Mertens, S. de Gendt and C. Vinckie, Saturation effects in TXRF on micro-droplet residue samples, *J. Anal. At. Spectrom.*, 2004, **19**, 1517–1523.
- C. Horntrich, P. Kregsamer, P. Wobrauschek and C. Strelí, Considerations on the ideal sample shape for Total



- Reflection X-ray Fluorescence Analysis, *Spectrochim. Acta, Part B*, 2011, **66**, 815–821.
- 15 C. Horntrich, S. Smolek, A. Maderitsch, R. Simon, P. Kregsamer and C. Strel, Investigation of element distribution and homogeneity of TXRF samples using SR-micro-XRF to validate the use of an internal standard and improve external standard quantification, *Anal. Bioanal. Chem.*, 2011, **400**(8), 2649–2654.
 - 16 C. Horntrich, P. Kregsamer, J. Prost, F. Stadlbauer, P. Wobrauschek and C. Strel, Production of the ideal sample shape for Total Reflection X-ray Fluorescence analysis, *Spectrochim. Acta, Part B*, 2012, **77**, 31–34.
 - 17 U. E. A. Fittschen and G. J. Havrilla, Picoliter Droplet Deposition Using a Prototype Picoliter Pipette: Control Parameters and Application in Micro X-ray Fluorescence, *Anal. Chem.*, 2010, **82**, 297–306.
 - 18 U. E. A. Fittschen, M. Menzel, O. Scharf, M. Radtke, U. Reinholz, G. Buzanich, V. M. Lopez, K. McIntosh, C. Strel and G. J. Havrilla, Observation of X-ray shadings in synchrotron radiation-total reflection X-ray fluorescence using a color X-ray camera, *Spectrochim. Acta, Part B*, 2014, **99**, 179–184.
 - 19 S. H. Nowak, A. Bjeoumikhov, J. Baronay, J. Buchriegler, F. Munnik, M. Petric, M. Radtke, A. D. Renno, U. Reinholz, O. Scharf and R. Wedell, Sub-pixel resolution with color X-ray camera SLcam, arXiv:1501.06825v1 [physics.ins-det], 2015.
 - 20 B. J. Larson, S. D. Gillmor and M. G. Lagally, Controlled deposition of picoliter amounts of fluid using an ultrasonic driven micropipette, *Rev. Sci. Instrum.*, 2004, **75**(4), 832–836.
 - 21 H. Riesemeier, K. Ecker, W. Görner, B. R. Müller, M. Radtke and M. Krumrey, Layout and first XRF applications of the BAMline at BESSY II, *X-Ray Spectrom.*, 2005, **34**, 160–163.
 - 22 S. H. Nowak, A. Bjeoumikhov, J. von Borany, J. Buchriegler, F. Munnik, M. Petric, A. D. Renno, M. Radtke, U. Reinholz, O. Scharf, L. Strüder, R. Wedell and R. Ziegenrucker, Examples of XRF and PIXE imaging with few microns resolution using SLcam® a color X-ray camera, *X-Ray Spectrom.*, 2015, **44**(3), 135–140.
 - 23 R. Glocker and H. Schreiber, Quantitative Röntgenspektralanalyse mit Kalterregung des Spektrums, *Ann. Phys.*, 1928, **390**, 1089–1102.
 - 24 J. Sherman, The theoretical derivation of fluorescent X-ray intensities from mixtures, *Spectrochim. Acta*, 1955, **7**, 288–306.
 - 25 J. Sherman, Simplification of a formula in the correlation of fluorescent X-ray intensities from mixtures, *Spectrochim. Acta*, 1959, **15**, 466–470.
 - 26 T. Shiraiwa and N. Fujino, Theoretical Calculation of Fluorescent X-ray Intensities in Fluorescent X-ray Spectrochemical Analysis, *Jpn. J. Appl. Phys.*, 1966, **5**, 886–899.
 - 27 J. V. Gilfrich and L. S. Birks, Spectral distribution of X-ray tubes for quantitative X-ray fluorescence analysis, *Anal. Chem.*, 1968, **40**, 1077–1080.
 - 28 www.csrii.iit.edu/periodic-table.html.
 - 29 R. D. Deegan, O. Bakajin, T. F. Dupont, G. Huber, S. R. Nagel and T. A. Witten, Capillary flow as the cause of ring strains from dried liquid drops, *Nature*, 1997, **389**, 827–829.
 - 30 S. H. Nowak, A. Bjeoumikhov, J. von Borany, J. Buchriegler, F. Munnik, M. Petric, M. Radtke, A. D. Renno, U. Reinholz, O. Scharf and R. Wedell, Sub-pixel resolution with color X-ray camera SLcam® arXiv.org>Physics, arXiv preprint arXiv:1501.06825., 2015, pp. 1–8.
 - 31 D. Nečas and P. Klapetek, Gwyddion: an open-source software for SPM data analysis, *Cent. Eur. J. Phys.*, 2010, **10**, 181–188.
 - 32 GESTIS Stoffdatenbank, CAS Nr. 13478-00-7, last accessed 15.07.2015.
 - 33 C. Horntrich, Characterization of the influence of the sample shape on accuracy, statistics and reproducibility in TXRF analysis of semiconductor surfaces, Doctoral Thesis, TU Wien, 2011.
 - 34 P. Hischenhuber, Diploma thesis, TU Wien, 2014.
 - 35 S. H. Nowak, F. Reinhardt, B. Beckhoff, J.-C. Dousse and J. Szlachetko, Geometrical optics modelling of grazing incidence X-ray fluorescence of nanoscaled objects, *J. Anal. At. Spectrom.*, 2013, **28**, 689–696.

