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## Operational constraints and strategies for systems to effect the sustainable, solar-driven reduction of atmospheric CO<sub>2</sub>

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The operational constraints for a 6-electron/6-proton CO<sub>2</sub> reduction system that operates at the concentration of CO<sub>2</sub> in the current atmosphere ( $p_{\text{CO}_2} = 400$  ppm) have been evaluated on a variety of scale lengths that span from laboratory scale to global scale. Due to the low concentration of CO<sub>2</sub> in the atmosphere, limitations due to mass transport of CO<sub>2</sub> from the tropopause have been evaluated through five different regions, each with different characteristic length scales: the troposphere; the atmospheric boundary layer (ABL); the canopy layer; a membrane layer; and an aqueous electrolyte layer. The resulting CO<sub>2</sub> conductances, and associated physical transport limitations, will set the ultimate limit on the efficiency and areal requirements of a sustainable solar-driven CO<sub>2</sub> reduction system regardless of the activity or selectivity of catalysts for reduction of CO<sub>2</sub> at the molecular level. At the electrolyte/electrode interface, the steady-state limiting current density and the concomitant voltage loss associated with the CO<sub>2</sub> concentration overpotential in a one-dimensional solar-driven CO<sub>2</sub> reduction cell have been assessed quantitatively using a mathematical model that accounts for diffusion, migration and convective transport, as well as for bulk electrochemical reactions in the electrolyte. At  $p_{\text{CO}_2} = 400$  ppm, the low diffusion coefficient combined with the low solubility of CO<sub>2</sub> in aqueous solutions constrains the steady-state limiting current density to  $<0.1 \text{ mA cm}^{-2}$  in a typical electrochemical cell with natural convection and employing electrolytes with a range of pH values. Hence, in such a system, the CO<sub>2</sub> capture area must be 100- to 1000-fold larger than the solar photon collection area to enable a  $>10\%$  efficient solar-driven CO<sub>2</sub> reduction system (based on the solar collection area). This flux limitation is consistent with estimates of oceanic CO<sub>2</sub> uptake fluxes that have been developed in conjunction with carbon-cycle analyses for use in coupled atmosphere/ocean general circulation models. Two strategies to improve the feasibility of obtaining efficient and sustainable CO<sub>2</sub> transport to a cathode surface at  $p_{\text{CO}_2} = 400$  ppm are described and modeled quantitatively. The first strategy employs yet unknown catalysts, analogous to carbonic anhydrases, that dramatically accelerate the chemically enhanced CO<sub>2</sub> transport in the aqueous electrolyte layer by enhancing the acid–base reactions in a bicarbonate buffer system. The rapid interconversion from bicarbonate to CO<sub>2</sub> in the presence of such catalysts near the cathode surface would in principle yield significant increases in the steady-state limiting current density and allow for  $>10\%$  solar-fuel operation at the cell level. The second strategy employs a thin-layer cell architecture to improve the diffusive transport of CO<sub>2</sub> by use of an ultrathin polymeric membrane electrolyte. Rapid equilibration of CO<sub>2</sub> at the gas/electrolyte interface, and significantly enhanced diffusive fluxes of CO<sub>2</sub> in electrolytes, are required to increase the steady-state limiting current density of such a system. This latter approach however only is feasible for gaseous products, because liquid products would coat the electrode and therefore thicken the hydrodynamic boundary layer and accordingly reduce the diffusive CO<sub>2</sub> flux to the electrode surface. Regardless of whether the limitations due to mass transport to the electrode surface are overcome on the laboratory scale, at global scales the ultimate CO<sub>2</sub> flux limitations will be dictated by mass transport considerations related to transport of atmospheric CO<sub>2</sub> to the boundary plane of the solar-driven reactor system. The transport of CO<sub>2</sub> across the troposphere/ABL interface, the ABL/canopy layer interface, and the canopy layer/electrolyte interface have therefore been assessed in this work, to provide upper bounds on the ultimate limits for the solar-to-fuel (STF) conversion efficiency for systems that are intended to effect the reduction of atmospheric CO<sub>2</sub> in a sustainable fashion at global scale.

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### Broader context

Development of a sustainable, solar-driven CO<sub>2</sub> reduction system is still in the proof-of-concept stage, and faces significant challenges both in fundamental materials discovery and engineering designs of cell and system architectures. Despite the lack of active, selective and stable electrocatalysts for the CO<sub>2</sub> reduction reaction (CO<sub>2</sub>RR), it is important to understand the operational constraints and attainable system efficiencies based on the CO<sub>2</sub> mass transport properties from the atmosphere towards the electrode surface for atmospheric cell operation. In this work, we describe two strategies that could significantly enhance the CO<sub>2</sub> transport and increase the steady-state limiting current density at  $p_{\text{CO}_2} = 400$  ppm. We have additionally evaluated analytically the transport limitations of CO<sub>2</sub> from the tropopause down to the cathode surface, through five different regions with five different length scales (from tens of nanometers to tens of kilometers), to understand the transport limitations of the CO<sub>2</sub>RR for a system that might eventually be deployed at global scale.

## I. Introduction

A solar-fuels generation system designed to effect the sustainable reduction of CO<sub>2</sub> includes components for light absorption and charge separation, electrocatalysis of both the CO<sub>2</sub>-reduction reaction (CO<sub>2</sub>RR) and the oxygen-evolution reaction (OER), and a mechanism to transport ions between the two reaction chambers while maintaining robust product separation for both efficiency and safety reasons. Efficient electrochemical or photoelectrochemical conversion of CO<sub>2</sub> into usable fuels under mild pressure and temperature conditions entails greater physical and chemical constraints than efficient solar-driven water-splitting systems that can generate renewable H<sub>2</sub>(g).

At the laboratory scale, no currently known catalyst can perform the multi-electron, multi-proton, electrochemical or photoelectrochemical CO<sub>2</sub>RR efficiently and selectively. Polycrystalline metal electrodes are among the most studied class of materials for electrocatalysis of the CO<sub>2</sub>RR, and most metals have been classified as being selective for CO, HCOO<sup>-</sup>, or H<sub>2</sub>.<sup>1</sup> Copper and copper-containing metal alloys have shown promise for forming hydrocarbons and C–C coupled products with a wide array of major and minor products, albeit at high overpotentials and with limited stability under operating conditions.<sup>2</sup> Recent work on single-crystal,<sup>3</sup> nanostructured Au substrates<sup>4</sup> or oxide-derived Cu substrates<sup>5</sup> has shown the preferred formation of certain products with limited selectivity and activity. The low activity for the hydrogen-evolution reaction (HER) of semiconductor surfaces may provide opportunities to improve the electrocatalytic performance of GaAs,<sup>6–8</sup> GaP,<sup>9,10</sup> InP,<sup>6,11</sup> and of other semiconductors for the CO<sub>2</sub>RR.

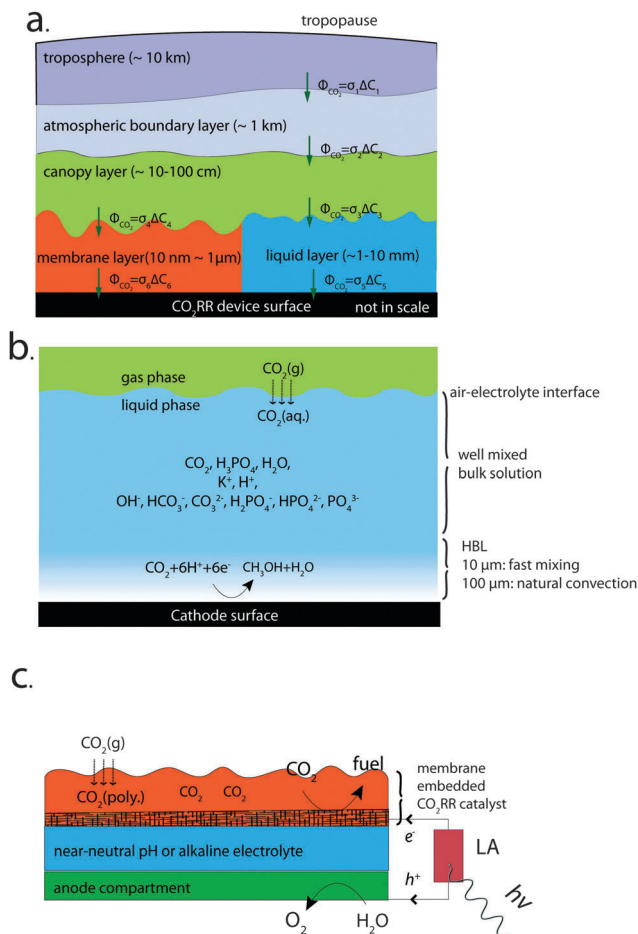
Assuming the discovery of a suitable catalyst, robust and efficient couplings between the CO<sub>2</sub>RR, the oxygen-evolution reaction (OER), and the necessary ionic transport processes between two potentially different electrolytes or solvent environments will be required for operation of a full, efficient, sustainable CO<sub>2</sub>RR system. Traditional three-electrode, two-compartment electrochemical cells are typically employed to study the catalytic and energy-conversion performance of electrocatalysts and semiconductor/catalyst assemblies.<sup>12</sup> However, the transport of ions between the working electrode compartment (cathode chamber) and the counter electrode compartment (anode chamber) is often far from ideal, and the resistive losses and concentration overpotentials are typically compensated for by the additional external bias applied by the potentiostat.<sup>13</sup> The efficient and sustainable coupling of the CO<sub>2</sub>RR and OER, with low potential losses and minimal product crossover between the two chambers, has been

investigated only to a very limited degree. Moreover, in the absence of perfectly selective catalysts for both the CO<sub>2</sub>RR and OER, a robust and efficient separator needs to be developed to prevent product crossover and thus provide efficient and safe operation of a CO<sub>2</sub>RR system. While traditional membrane separators such as Nafion<sup>TM</sup><sup>14–19</sup> are highly conductive and effective for preventing gas crossover in water-splitting systems, Nafion membranes yield high crossover losses in direct methanol fuel cells and would not be suitable for solar-driven CO<sub>2</sub>RR devices that produce alcohols as products. Development of membranes with the desired permeability and ionic conductivity in the presence of a variety of solution species thus constitutes a significant research opportunity for CO<sub>2</sub>RR systems.

Regardless of the performance of the full electrochemical cell at the laboratory scale, the sustainable reduction of CO<sub>2</sub> at global scale will additionally require effective mass transport and uptake of atmospheric CO<sub>2</sub> on large areas of the Earth's surface. The large-scale, sustainable reduction of CO<sub>2</sub> requires a robust and cost-effective method for the delivery of CO<sub>2</sub> to the cathode surface of the device. Whereas liquid water or water vapor is readily able to produce sufficient reactant flux to allow for construction of an efficient solar-driven water-splitting system,<sup>20</sup> the low concentration of CO<sub>2</sub> in the atmosphere (~400 ppm), and the low solubility of CO<sub>2</sub> in aqueous solutions (~34 mM at standard temperature and pressure), present significant physical limitations to obtaining sufficient reactant transport to achieve technologically relevant efficiencies for the operation of a solar-driven CO<sub>2</sub>RR system with atmospheric CO<sub>2</sub>. Passage of 10 mA cm<sup>-2</sup> of current density for 5 h of solar-driven water splitting would consume a column height of 0.018 cm of liquid water, whereas in the absence of transport, the same total amount of charge passed for a 6-electron CO<sub>2</sub>RR would consume all of the atmospheric 400 ppm CO<sub>2</sub> in a column extending 160 m above the earth's surface. To produce a reasonable partial pressure of CO<sub>2</sub> by direct air capture, the surface area for the CO<sub>2</sub> collection and concentration is likely to be many orders of magnitude larger than the surface area for the solar photon collection and conversion part of the system. Use of separate CO<sub>2</sub> concentration and reduction systems would present additional challenges for integration and coupling of the two technologies. While active research and development has been pursued to achieve efficient capture of CO<sub>2</sub> from air,<sup>21–25</sup> significant advances are still needed to make such technologies cost effective and functional in the presence of humidity and temperature variations in the atmosphere.

In this work, we have evaluated analytically the transport limitations of CO<sub>2</sub> from the tropopause down to a cathode





**Fig. 1** (a) Schematic illustration of CO<sub>2</sub> transport in five different regions with five different length scales. (b) Schematic illustration of the model used for CO<sub>2</sub> transport near the cathode surface that contains an aqueous layer with a variety of solution species. (c) Schematic illustration of the CO<sub>2</sub>RR reactor that incorporates a light absorber (LA), a catalyst-embedded, thin-layer membrane assembly (orange), an anode compartment for OER (green) and a proton-transport electrolyte (blue).

surface, through five different regions with five different length scales (from tens of nanometers to tens of kilometers) (Fig. 1a) that are coupled in series from a mass transport perspective. In each case, an effective mass transfer coefficient,  $\sigma_i$ , has been obtained. The mass transfer coefficients will add reciprocally to produce the reciprocal of the overall CO<sub>2</sub> mass transfer coefficient of the system,  $\sigma_{\text{system}}$ :

$$\frac{1}{\sigma_{\text{system}}} = \sum_i \frac{1}{\sigma_i} \quad (1)$$

The approach allows estimates of the concentration overpotentials and achievable solar-to-fuels efficiency for a hypothetical CO<sub>2</sub> reduction reactor fed by air that contains the same concentration of CO<sub>2</sub> as the surrounding atmosphere. We describe and model quantitatively the effects of two strategies to improve the feasibility of producing efficient and sustainable CO<sub>2</sub> transport to a cathode surface at  $p_{\text{CO}_2} = 400$  ppm: development of new catalysts analogous to metalloenzymes such as carbonic

anhydrase, to dramatically enhance the kinetics of the inter-conversion of bicarbonate ions and CO<sub>2</sub> in the bicarbonate buffer system and thus improve the ability to maintain the concentration of CO<sub>2</sub> in the aqueous solution at  $p_{\text{CO}_2} = 400$  ppm; and the use of a thin-layer cell architecture that minimizes the required CO<sub>2</sub> transport in an aqueous or polymeric electrolyte. These two strategies could, in principle, yield significant increases in the air/electrolyte CO<sub>2</sub> conductance relative to the natural transport at global scale of CO<sub>2</sub> across the atmosphere/ocean interface. The atmospheric transport of CO<sub>2</sub> between the troposphere and the atmospheric boundary layer (ABL), and the corresponding constraints for the transport of CO<sub>2</sub> to the reactor at regional scale, have also been evaluated to complete the expression for the overall system CO<sub>2</sub> conductance and in turn to establish the ultimate limit on the efficiency of a sustainable solar-driven CO<sub>2</sub>RR system deployed at global scale.

## II. Modeling

### 2.1 CO<sub>2</sub> transport

Fig. 1a shows a schematic illustration of the CO<sub>2</sub> transport from tropopause towards the surface of a CO<sub>2</sub>RR device. Five different layers with different characteristic length scales are coupled in series with the same CO<sub>2</sub> flux. Three distinctive types of phase boundaries: gas/gas (troposphere/atmospheric boundary layer (ABL), ABL/canopy layer), gas/electrolyte (canopy layer/membrane layer, or canopy layer/liquid layer) and electrolyte/electrode interface (liquid layer/cathode surface, or membrane layer/cathode surface) were included in the transport schematics. The CO<sub>2</sub> concentrations within the troposphere, the ABL, and the canopy layer were assumed to separately be constant due to rapid turbulent mixing within each layer, while the net CO<sub>2</sub> flux across the troposphere/ABL interface and across the ABL/canopy interface results in CO<sub>2</sub> concentration differentials between the different gas-phase layers. The equilibrium CO<sub>2</sub> concentrations at the various gas/electrolyte interfaces were assumed to follow Henry's law. At the electrolyte/electrode interfaces, a 4-electron/4-proton OER was assumed and a 6-electron/6-proton CO<sub>2</sub>RR was assumed, to represent a favorable situation for the ratio of CO<sub>2</sub> molecules to electrons in the electrochemical cell.

At the phase boundaries, the CO<sub>2</sub> flux across the interface,  $\Phi_{\text{CO}_2}$  [mol cm<sup>-2</sup> s<sup>-1</sup>] was expressed as  $\Phi_{\text{CO}_2} = \sigma \Delta C$ , where  $\sigma$  is an effective mass transfer coefficient [cm s<sup>-1</sup>] and  $\Delta C$  is the concentration differential of CO<sub>2</sub> [moles cm<sup>-3</sup>] between the two neighboring layers. Two transport pathways, one containing the membrane layer ( $\sigma_1$ ,  $\sigma_2$ ,  $\sigma_4$  and  $\sigma_6$ ) and the other containing the liquid layer ( $\sigma_1$ ,  $\sigma_2$ ,  $\sigma_3$  and  $\sigma_5$ ), were modeled and evaluated in this study. The CO<sub>2</sub> flux across all of the interfaces,  $\Phi_{\text{CO}_2}$ , can be expressed as  $\Phi_{\text{CO}_2} = \sigma_{\text{system}}(C_{\text{troposphere}} - C_{\text{cathode}})$ , where  $\sigma_{\text{system}}$  is the overall effective mass transfer coefficient of the system, which can be expressed as  $\frac{1}{\sigma_{\text{system}}} = \frac{1}{\sigma_1} + \frac{1}{\sigma_2} + \frac{1}{\sigma_3} + \frac{1}{\sigma_5}$  for the system that contains the liquid layer and as  $\frac{1}{\sigma_{\text{system}}} = \frac{1}{\sigma_1} + \frac{1}{\sigma_2} + \frac{1}{\sigma_4} + \frac{1}{\sigma_6}$  for the system that contains the membrane layer. As a result of



the reciprocal summation relation, the overall effective mass transfer coefficient of the system,  $\sigma_{\text{system}}$ , is smaller than any individual mass transfer coefficient, and is dominated by the process with the smallest mass transfer coefficient in the system.

## 2.2 One-dimensional traditional cell design

Fig. 1b illustrates the one-dimensional (1-D) model used in this work to evaluate the CO<sub>2</sub> transport near a cathode performing a 6-electron/6-proton CO<sub>2</sub>RR. The electrode was assumed to have a sufficiently high catalytic activity that under operating conditions the CO<sub>2</sub> concentration was driven to zero at the electrode surface. A well-mixed bulk solution was assumed, and two hydrodynamic boundary layers (HBL), that accounted for forced convective mixing ( $l_{\text{HBL}} = 10 \mu\text{m}$ ) or natural convection ( $l_{\text{HBL}} = 100 \mu\text{m}$ ), respectively, were introduced near the cathode surface. Rapid equilibration of CO<sub>2</sub> was assumed at the air–electrolyte interface, and the acid–base equilibria for the carbonate buffer and for the phosphate buffer, as well as the equilibria for the corresponding chemical reactions, were included in the model for the liquid regions. The same configuration, representing a well-mixed bulk solution layer and two HBLs, was assumed for the OER at the anode.

Table 1 summarizes the forward and reverse rate constants for the bicarbonate buffer solution, that were used in the simulation.<sup>26,27</sup> Note that the total CO<sub>2</sub> concentration in Table 1 has been defined as the sum of the dissolved CO<sub>2</sub> in aqueous solution, CO<sub>2</sub>(aq), and the carbonic acid concentration, H<sub>2</sub>CO<sub>3</sub>. The forward and reverse reaction rate constants,  $k_{1+}$  and  $k_{1-}$ , respectively, fully describe the acid–base equilibrium between CO<sub>2</sub>(aq), H<sub>2</sub>CO<sub>3</sub> and HCO<sub>3</sub><sup>−</sup> in the buffer system.<sup>26,27</sup> The transport loss in the system was assumed to be independent of the detailed electrocatalytic parameters for the cathode and anode, and was assumed to be a function only of the operating current density at the electrode surfaces. In some situations, an interconversion enhancement factor was introduced to increase both the forward and reverse rates for reactions (1–4) in Table 1, to represent the behavior of a hypothetical catalyst for these reactions with the catalyst having a reactivity analogous to that exhibited by the enzyme carbonic anhydrase.

**Table 1** The forward and the backward rate constants the bicarbonate buffer solution and used in the simulation

$\text{CO}_2 + \text{H}_2\text{O} \xrightleftharpoons[k_{1-}]{k_{1+}} \text{H}^+ + \text{HCO}_3^-$	$k_{1+} = 0.037 \text{ s}^{-1}$ $k_{1-} = 7.83 \times 10^4 \text{ M}^{-1} \text{ s}^{-1}$
$\text{CO}_2 + \text{OH}^- \xrightleftharpoons[k_{2-}]{k_{2+}} \text{HCO}_3^-$	$k_{2+} = 2.23 \times 10^3 \text{ M}^{-1} \text{ s}^{-1}$ $k_{2-} = 4.85 \times 10^{-5} \text{ s}^{-1}$
$\text{HCO}_3^- \xrightleftharpoons[k_{3-}]{k_{3+}} \text{H}^+ + \text{CO}_3^{2-}$	$k_{3+} = 2.5 \text{ s}^{-1}$ $k_{3-} = 5 \times 10^{-10} \text{ M}^{-1} \text{ s}^{-1}$
$\text{HCO}_3^- + \text{OH}^- \xrightleftharpoons[k_{4-}]{k_{4+}} \text{H}_2\text{O} + \text{CO}_3^{2-}$	$k_{4+} = 6 \times 10^9 \text{ M}^{-1} \text{ s}^{-1}$ $k_{4-} = 1.2 \text{ s}^{-1}$

## 2.3 Catalyst-embedded, thin-layer membrane assembly for rapid transport of CO<sub>2</sub>

Fig. 1c illustrates a conceptually distinct system that consists of a CO<sub>2</sub>-reduction reactor based on a catalyst-embedded, thin-layer membrane device architecture. The cell consists of a solar-driven CO<sub>2</sub>RR reactor that incorporates a light absorber (LA), a catalyst-embedded thin-layer membrane assembly, an anode compartment, and an electrolyte that is either buffered at near-neutral pH or is maintained under alkaline conditions. The LA (red) captures the solar photons and converts them into energetic electrons and holes for the fuel-forming reactions. The device has been designed to achieve large mass transport fluxes of CO<sub>2</sub> to the electrode surface, based purely on diffusional transport of CO<sub>2</sub> in the ultrathin electrolyte, because the catalyst-embedded, thin-layer membrane assembly (orange) reduces the length of the pathways for CO<sub>2</sub> transport within the polymer electrolyte.

In this device, the equilibrium CO<sub>2</sub> concentration at the gas/polymer electrolyte interface was assumed to follow Henry's law. Three different permeabilities for CO<sub>2</sub> transport in the polymer electrolyte were assumed. The buffered near-neutral pH or alkaline electrolytes (blue) were chosen so that the small proton concentration at the cathode surface would suppress the rate of the hydrogen-evolution reaction (HER) relative to the rate of the CO<sub>2</sub>RR. The anode compartment (green) performed the OER and provided the necessary proton source for the cathode. The anode compartment also contained an anion-exchange membrane for alkaline operation or a bi-polar membrane for CO<sub>2</sub>RR and OER at two different pHs, to facilitate the ionic transport and reduce the product crossover in the system.

## 2.4 Governing equations

Ionic species and neutral species in the electrolyte solution were modeled using the Nernst–Planck equation,<sup>12</sup> in which the diffusion, migration and bulk reactions of water and buffer dissociation were explicitly included. Forced convection was approximated by the use of the hydrodynamic boundary layers.

The total voltage requirement ( $\Delta\phi_{\text{cell}}$ ) for the electrochemical cell was calculated as the sum of the equilibrium potential ( $E_0$ ), kinetic overpotentials ( $\eta$ ), solution potential drop losses ( $\Delta\phi_{\text{solution}}$ ), and the Nernstian potential losses associated with pH gradients, ( $\Delta\phi_{\text{pH gradient}}$ ), as well as the potential drops associated with CO<sub>2</sub> concentration gradients, ( $\Delta\phi_{\text{CO}_2 \text{ gradient}}$ ) at the surface of the electrodes:

$$\Delta\phi_{\text{cell}} = E_0 + \eta_{\text{OER}} - \eta_{\text{HER}} + \Delta\phi_{\text{solution}} + \Delta\phi_{\text{pH gradient}} + \Delta\phi_{\text{CO}_2 \text{ gradient}} \quad (2)$$

The solution losses, ( $\Delta\phi_{\text{solution}}$ ), were calculated as the sum of the ohmic resistive loss (first term) and the electrodiffusion loss (second term). These losses can be expressed as:

$$\Delta\phi_{\text{solution}} = \int \frac{J}{\kappa} dx + \sum_i \int \frac{Fz_i D_i \nabla c_i}{\kappa} dx \quad (3)$$

where  $\phi$  is the electric potential,  $\kappa$  is the conductivity of the electrolyte,  $J$  is the current density,  $x$  is distance along the axis of the 1-D model,  $F$  is Faraday's constant,  $z$  is the charge



number,  $D_i$  is the diffusion coefficient and  $c_i$  is the molar concentration of the  $i$ th species,  $R$  is the gas constant, and  $T$  is the absolute temperature. The distribution of the ionic conductivity,  $\kappa(x)$ , and of the species concentrations,  $c_i(x)$ , obtained from COMSOL Multiphysics software were used in the above equations to calculate the ohmic and electrodiffusion losses of the system.

The Nernstian potential losses associated with the pH gradients ( $\Delta\phi_{\text{pH gradient}}$ ) and  $\text{CO}_2$  concentration gradients ( $\Delta\phi_{\text{CO}_2 \text{ gradient}}$ ) at the surface of the electrodes can be expressed as:

$$\begin{aligned}\Delta\phi_{\text{pH gradient}} &= 2.303\frac{RT}{F}(\text{pH}_{\text{cathode}} - \text{pH}_{\text{anode}}) \\ &= 59 \text{ (mV)}(\text{pH}_{\text{cathode}} - \text{pH}_{\text{anode}}) \\ \Delta\phi_{\text{CO}_2 \text{ gradient}} &= -\frac{RT}{nF}\ln\left(\frac{p_{\text{CO}_2,\text{cathode}}}{p_{\text{CO}_2,\text{bulk}}}\right) \\ &= -\frac{59 \text{ (mV)}}{n}\log\left(\frac{p_{\text{CO}_2,\text{cathode}}}{p_{\text{CO}_2,\text{bulk}}}\right)\end{aligned}\quad (4)$$

where  $n$  is number of electrons transferred in the  $\text{CO}_2$  reduction process, with  $n = 6$  assumed as a favorable case for the purposes of this study.  $p_{\text{CO}_2,\text{cathode}}$  and  $p_{\text{CO}_2,\text{bulk}}$  are the partial pressures of  $\text{CO}_2$  at the cathode surface and in the bulk solution, respectively.

### III. Results

#### 3.1 Limiting performance of cells operated using a 400 ppm $\text{CO}_2$ feedstock

At 400 ppm of  $\text{CO}_2$  in the reactant atmosphere,  $\text{CO}_2$  transport at the electrolyte/electrode interface, specifically,  $\Phi_{\text{CO}_2} = \sigma_5\Delta C_5$  in

Fig. 1a, produced significant concentration polarization and limited the device efficiency. Fig. 2a shows the steady-state limiting current density as a function of the electrolyte pH for a 6-electron/6-proton  $\text{CO}_2$  reduction process. Two HBL thicknesses, 100  $\mu\text{m}$  (red) and 10  $\mu\text{m}$  (blue) were used to account for natural convection and forced convection, respectively. In addition to the bicarbonate buffer system, in which the dissolved  $\text{CO}_2$  concentration was set to the solubility limit, the electrolyte solution was buffered at different pHs with a 1.0 M phosphate buffer. The steady-state limiting current density was  $<0.2 \text{ mA cm}^{-2}$  for all cases, which is  $\sim 2$  orders of magnitude smaller than the current density required to produce a  $\text{CO}_2\text{RR}$  reactor with a 10% solar-to-fuels efficiency. In the higher pH solutions ( $\text{pH} > 10.2$ ), a slight increase in the obtainable steady-state limiting current densities was observed. The higher concentration of bicarbonate in higher pH electrolytes at  $p_{\text{CO}_2} = 400 \text{ ppm}$  resulted in an enhanced conversion from bicarbonate species to  $\text{CO}_2$ .

Fig. 2b shows the change of the  $\text{CO}_2$  concentration at the cathode surface relative to the bulk equilibrium value,  $\Delta[\text{CO}_2]$ , as a function of the operating current density for a 6-electron/6-proton  $\text{CO}_2$  reduction process at two different partial pressures of  $\text{CO}_2$ . A linear relationship between  $\Delta[\text{CO}_2]$  and the operating current density was observed for two different partial pressures of  $\text{CO}_2$ . At a given HBL thickness, a constant slope was observed at different partial pressures of  $\text{CO}_2$ . When  $\Delta[\text{CO}_2]$  approached the solubility limit for  $\text{CO}_2$ , a steady-state limiting current density was reached. For a cell fed by a 25-fold higher  $\text{CO}_2$  partial pressure than found in air, *i.e.*,  $p_{\text{CO}_2} = 0.01 \text{ atm}$ , the limiting current densities were  $0.3 \text{ mA cm}^{-2}$  and  $3 \text{ mA cm}^{-2}$  for  $l_{\text{HBL}} = 100 \mu\text{m}$  and  $l_{\text{HBL}} = 10 \mu\text{m}$ , respectively. Although numerous solution species and chemical reactions in the liquid layer are associated with the inter-conversion of  $\text{CO}_2$  species,

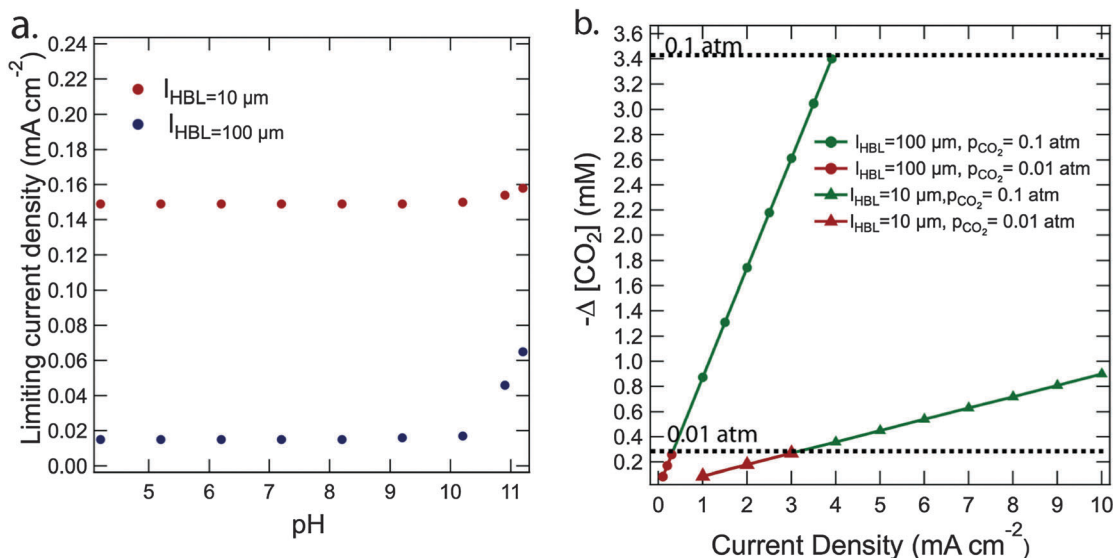


Fig. 2 (a) Steady-state limiting current densities as a function of solution pH for a 6-electron/6-proton  $\text{CO}_2$  reduction process fed by air containing  $\text{CO}_2$  at  $p_{\text{CO}_2} = 400 \text{ ppm}$  for  $l_{\text{HBL}} = 100 \mu\text{m}$  (red) and  $l_{\text{HBL}} = 10 \mu\text{m}$  (blue). (b) The change of  $\text{CO}_2$  concentration at the electrode surface from the bulk equilibrium values as a function of the operating current density for a 6-electron/6-proton  $\text{CO}_2$  reduction process at the  $p_{\text{CO}_2} = 0.1 \text{ atm}$  (green) and  $p_{\text{CO}_2} = 0.01 \text{ atm}$  (red) and for  $l_{\text{HBL}} = 100 \mu\text{m}$  (circle) and  $l_{\text{HBL}} = 10 \mu\text{m}$  (triangle). The concentration of  $\text{CO}_2$  at the solubility limit in aqueous solutions at  $p_{\text{CO}_2} = 0.01 \text{ atm}$  and  $p_{\text{CO}_2} = 0.1 \text{ atm}$  were indicated by the black dotted lines.



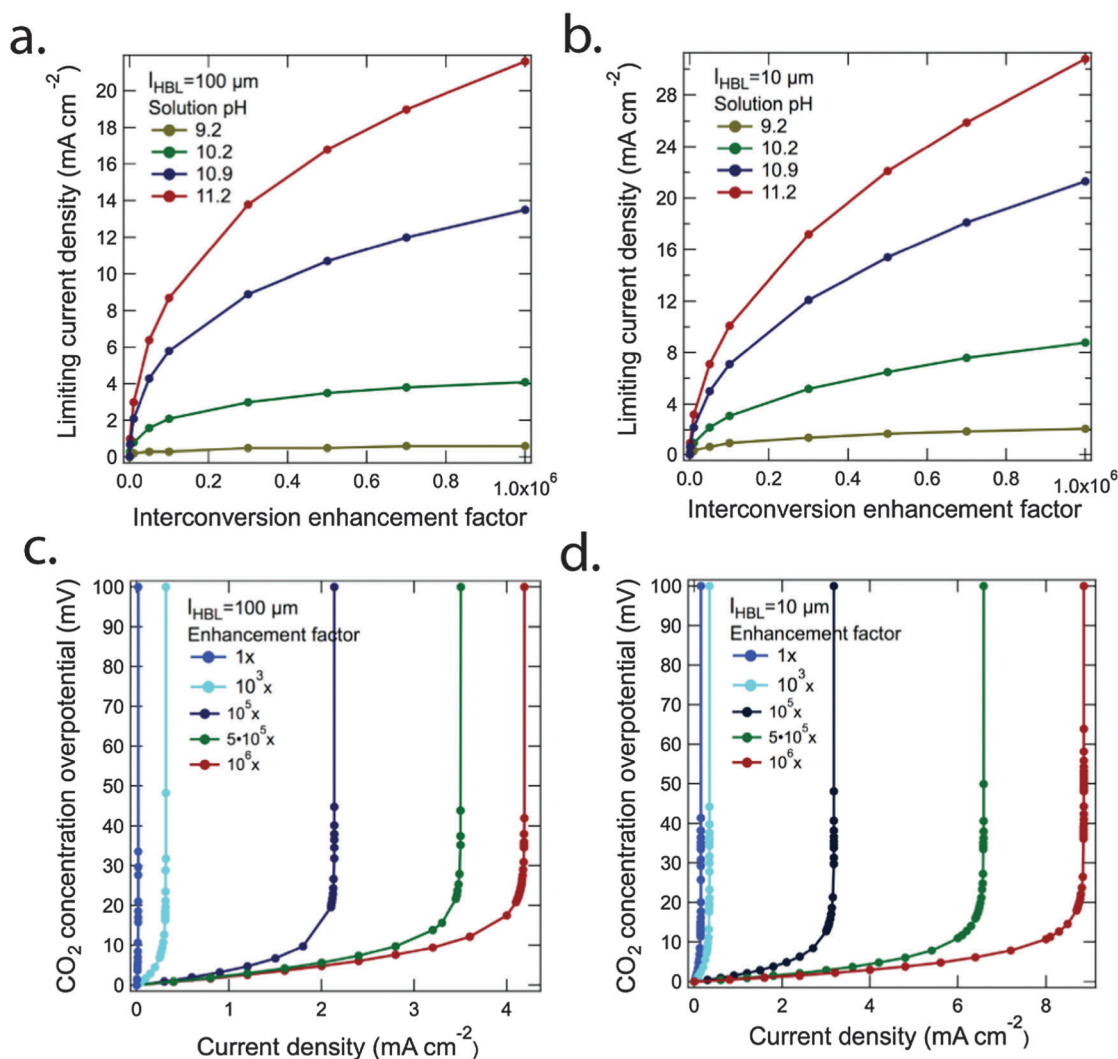
a linear relation,  $\Phi_{\text{CO}_2} = \sigma_5 \Delta C_5$ , was sufficient to describe the  $\text{CO}_2$  transport process at the gas/electrolyte interface. Effective mass transfer coefficients,  $\sigma_5 = 0.002 \text{ cm s}^{-1}$  and  $0.018 \text{ cm s}^{-1}$ , were obtained for  $l_{\text{HBL}} = 100 \text{ }\mu\text{m}$  and  $l_{\text{HBL}} = 10 \text{ }\mu\text{m}$ , respectively. Note that the value of the effective mass transfer coefficient reflected both the diffusive transport of the neutral  $\text{CO}_2$  species and the chemically enhanced transport due to the interconversion of  $\text{CO}_2$  and the bicarbonate ion.

### 3.2 Effect of enhancing the rates of interconversion for the bicarbonate buffer system

The low mass transfer coefficient,  $\sigma_5$ , at the electrolyte/electrode interface significantly limited the attainable operating current density in the system. One approach to in principle accelerate the rate of chemically enhanced transport in the system involves the

development of catalysts that can rapidly interconvert dissolved  $\text{CO}_2$ , carbonic acid, and bicarbonate.

Fig. 3a and b show the steady-state limiting current density as a function of a hypothetical interconversion-enhancement factor for the bicarbonate buffer system for  $l_{\text{HBL}} = 100 \text{ }\mu\text{m}$  and  $l_{\text{HBL}} = 10 \text{ }\mu\text{m}$ , respectively. The bulk  $\text{CO}_2$  concentration was equilibrated with  $p_{\text{CO}_2} = 400 \text{ ppm}$  and was set to  $14 \text{ }\mu\text{M}$ . The situation for four different pH values, 9.2, 10.2, 10.9 and 11.2, which correspond to bicarbonate concentrations of 0.01 M, 0.1 M, 0.5 M and 1.0 M, respectively, were evaluated. A significant increase in the steady-state limiting current density required an increase of 6 orders of magnitude in the rates for the interconversion of carbon dioxide and bicarbonate (or vice versa) relative to the natural interconversion rate. In particular, in higher pH solutions, where the bicarbonate concentration was higher, the reverse reactions,  $\text{H}^+ + \text{HCO}_3^- \rightarrow \text{CO}_2 + \text{H}_2\text{O}$



**Fig. 3** The limiting current density of a 6-electron/6-proton  $\text{CO}_2$  reduction process as a function of the interconversion-enhancement factor in four solutions with different pH values and fed by air with  $p_{\text{CO}_2} = 400 \text{ ppm}$  for (a)  $l_{\text{HBL}} = 100 \text{ }\mu\text{m}$  and (b)  $l_{\text{HBL}} = 10 \text{ }\mu\text{m}$ , respectively. The Nernstian potential loss resulting from the  $\text{CO}_2$  concentration gradient which develops near the surface of a cathode in contact with an electrolyte with pH = 10.2, as a function of the operating current density for (c)  $l_{\text{HBL}} = 100 \text{ }\mu\text{m}$  and (d)  $l_{\text{HBL}} = 10 \text{ }\mu\text{m}$ , respectively. The concentration of the dissolved  $\text{CO}_2$  in at the HBL was assumed to follow Henry's law and was set to  $14 \text{ }\mu\text{M}$  for  $p_{\text{CO}_2} = 400 \text{ ppm}$ .



and  $\text{HCO}_3^- \rightarrow \text{CO}_2 + \text{OH}^-$ , were significantly increased at higher interconversion-enhancement factors. For instance, for  $l_{\text{HBL}} = 10 \mu\text{m}$ , the steady-state limiting current density exceeded  $20 \text{ mA cm}^{-2}$  for  $\text{pH} = 10.9$  and  $11.2$  in the presence of this hypothetical million-fold increase in equilibration rate relative to the natural situation.

Fig. 3c and d show the Nernstian potential losses associated with the development of  $\text{CO}_2$  gradients near the surface of a cathode in contact with an electrolyte with  $\text{pH} = 10.2$ , as a function of the operational current density, for five different interconversion-enhancement factors with  $l_{\text{HBL}} = 100 \mu\text{m}$  and  $l_{\text{HBL}} = 10 \mu\text{m}$ , respectively. The  $\text{CO}_2$  concentration overpotential increased exponentially when the operating current density approached the steady-state limiting current density according to the Nernst equation. Minimization of the potential losses ( $< 100 \text{ mV}$ ) due to concentration overpotentials requires that the operating current densities remain below the values at

which the concentration-overpotential curves rise nearly vertically in Fig. 3c and d. The solution loss and the Nernstian potential losses associated with pH gradients at the electrode surfaces were small ( $< 50 \text{ mV}$ ) in the assumed cell design, and were additionally minimized by the use of a phosphate buffer and a convected electrolyte. Similar results were also reported recently in an analytical assessment of solar driven water-splitting systems at near-neutral pH.<sup>28</sup>

Fig. 4 shows the spatially resolved concentration profile of the ionic and neutral species between the cathode surface and the hydrodynamic boundary layer (HBL) at an operational current density of  $1 \text{ mA cm}^{-2}$ . At the bulk-solution edge of the HBL, the concentration of the dissolved  $\text{CO}_2$  was set to  $14 \mu\text{M}$ . In a cell fed by air with  $p_{\text{CO}_2} = 400 \text{ ppm}$ , and containing a  $\text{pH} = 10.2$  solution and  $1.0 \text{ M}$  phosphate buffer, minimal pH gradients were observed (Fig. 4a). Fig. 4b shows the steady-state  $\text{CO}_2$  generation/consumption rate within the HBL. As the

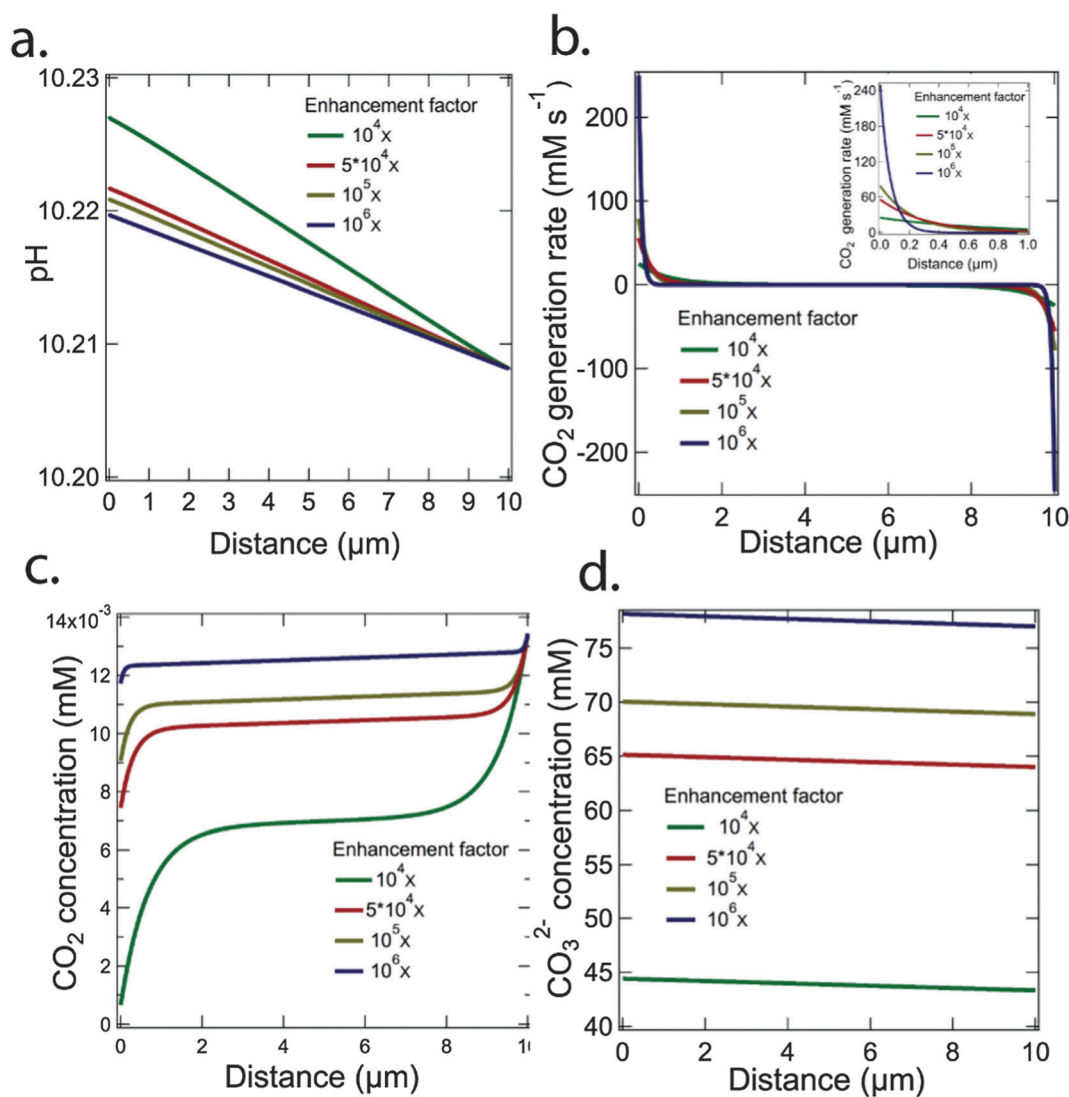


Fig. 4 (a) The pH profile, (b)  $\text{CO}_2$  generation/consumption rate in the HBL and close to the electrodes (b, insert), (c)  $\text{CO}_2$  concentration and (d) bicarbonate concentration within the HBL as a function of distance from the cathode for a cell operating at a current density of  $1 \text{ mA cm}^{-2}$  and for four different interconversion enhancement factors.



enhancement factor increased, a rapid increase of the CO<sub>2</sub> generation rate near the cathode surface, and a rapid increase of uptake of CO<sub>2</sub> at the edge of the HBL, were observed. In the middle region, an acid–base equilibrium with near-zero CO<sub>2</sub> generation/consumption was observed. The increased CO<sub>2</sub> generation rate near the cathode surface increased the steady-state limiting current density of the system at higher enhancement factors. Fig. 4c and d also depict the corresponding CO<sub>2</sub> concentration and the bicarbonate concentration profile, respectively.

### 3.3 Performance of the catalyst-embedded, thin-layer membrane assembly for rapid transport of CO<sub>2</sub>

Instead of dramatically accelerating the chemically enhanced transport in aqueous solutions, an alternative strategy to significantly improve the CO<sub>2</sub> transport would involve the use of a thin-layer electrochemical cell design (Fig. 1c). The CO<sub>2</sub> transport at the polymer-electrolyte/electrode interface, specifically,  $\Phi_{\text{CO}_2} = \sigma_6 \Delta C_6$  in Fig. 1c, and the resulting limiting current density, can in principle be significantly enhanced by use of a thin-layer membrane electrolyte, and consequently relying on purely diffusive fluxes to achieve the desired current density at sufficiently small membrane thicknesses.

Fig. 5 shows the limiting current density as a function of the membrane thickness for three different permeabilities of CO<sub>2</sub> in the polymer electrolytes of the catalyst-embedded thin-layer membrane-assembly design (Fig. 1c). The solubility and the diffusion coefficient of CO<sub>2</sub> in the polymer electrolytes, *i.e.*, Nafion, are highly dependent on the polymer morphology, the polymer segmental dynamics, the hydration conditions, and the operating temperature.<sup>29–32</sup> The permeability of CO<sub>2</sub> and other gases for Nafion membranes is the product of the diffusion coefficient and the solubility. The permeability is the key figure of merit for CO<sub>2</sub> transport in membrane-based

systems, and has been measured experimentally by others under various conditions. The black curve used a typical value,  $3 \times 10^{-11}$  [cm<sup>3</sup>(STP) cm cm<sup>-2</sup> s<sup>-1</sup> Pa<sup>-1</sup>], for the permeability of CO<sub>2</sub> in Nafion near room temperature.<sup>31,32</sup> The red and green curves represent results for permeability values of  $3 \times 10^{-10}$  and  $3 \times 10^{-12}$  [cm<sup>3</sup>(STP) cm cm<sup>-2</sup> s<sup>-1</sup> Pa<sup>-1</sup>], respectively, and represent the upper and lower bounds for the calculation. The attainable current density in the membrane-based system was independent of the pH conditions and was determined by the solubility and the diffusion coefficient of CO<sub>2</sub> in the membrane, as well as by the thickness of the membrane. The effective mass transfer coefficient at the polymer-electrolyte/electrode interface,  $\sigma_6$ , at a membrane thickness of 100 nm was 0.038 cm s<sup>-1</sup> and 3.8 cm s<sup>-1</sup> for the upper and lower limit of the membrane permeability values, respectively. The thin layer of the catalyst-embedded membrane minimized the CO<sub>2</sub> transport losses in the aqueous solution or polymeric media, and enabled the direct electrochemical reduction of CO<sub>2</sub> from air at current densities in excess of 10 mA cm<sup>-2</sup> without mass transport limitations in the liquid layer.

## IV. Discussion

### 4.1 Assumptions and limitations of the treatment of CO<sub>2</sub>RR systems

The limiting electrochemical current densities and concentration polarization losses obtained in this study pertain solely to the cathode and the electrolyte region near the cathode, in a fashion analogous to evaluating the flux-limited current densities at the working electrode in a traditional 3-electrode electrochemical experiment. In an actual two-electrode photoelectrosynthetic system comprised of catalysts that effect the CO<sub>2</sub>RR and OER, the current density at the cathode is likely to be nonuniform,<sup>33</sup> resulting in even higher local CO<sub>2</sub> flux demands by a factor of 10 or more than those assumed herein for an isopotential electrode surface. The cathodic reduction products and CO<sub>2</sub>RR intermediates were assumed to have negligible reactivity with O<sub>2</sub>(g) in the atmosphere, and despite the much higher concentration of O<sub>2</sub> relative to CO<sub>2</sub> in ambient air, O<sub>2</sub>(g) was assumed to be electroinactive at the cathode at potentials required to effect the CO<sub>2</sub>RR, despite the >1 V driving force for O<sub>2</sub>(g) reduction to H<sub>2</sub>O and the ease of reducing O<sub>2</sub>(g) to H<sub>2</sub>O<sub>2</sub> at these potentials. No CO<sub>2</sub> catalysts or electrode systems known to date meet any of these criteria. The CO<sub>2</sub>RR products and intermediates at the cathode were assumed to be separated from the anode, which was assumed to have 100% faradaic efficiency for O<sub>2</sub>(g) evolution. The ohmic resistive loss, pH gradients, and electrodiffusion due to the incorporation of an cation exchange membrane or an anion exchange membrane in the near-neutral pH system,<sup>28</sup> such as the bicarbonate buffer system, which can individually or collectively produce significant and in some cases overwhelming voltage losses in the operating cell, have not been considered in the present assessment.

Standard temperature conditions 273.15 K were assumed for the operational temperature of the CO<sub>2</sub>RR systems in the

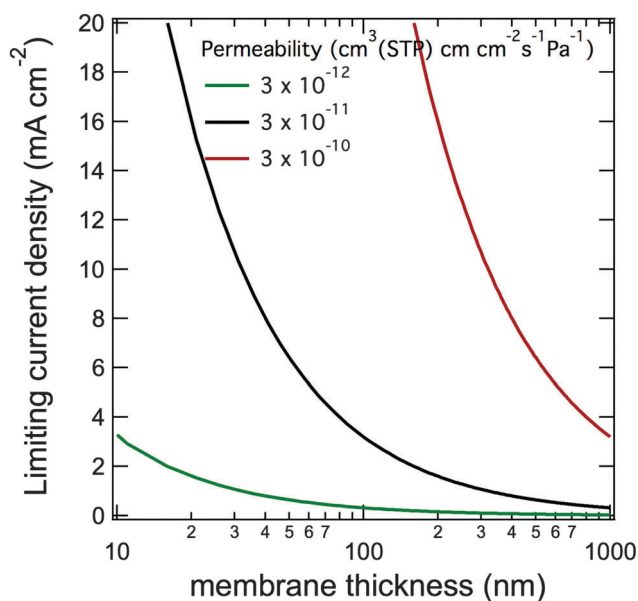


Fig. 5 The calculated limiting current density as a function of the membrane thickness for three different permeabilities of CO<sub>2</sub> in the membrane.



simulations performed herein. Solar-driven CO<sub>2</sub>RR systems may operate at elevated temperatures. The solubility of CO<sub>2</sub> in water is strongly temperature dependent, and the Henry's law constant for CO<sub>2</sub> decreases from 34 mM atm<sup>-1</sup> to 13 mM atm<sup>-1</sup> when the operational temperature is increased from 273 K to 333 K.<sup>34</sup> Hence, at elevated temperatures, the decreased solubility of CO<sub>2</sub> in water would lead to a further reduction the mass-transport-limited current density in the cell. One approach to increase the solubility of CO<sub>2</sub> in the electrolyte is to use ionic liquids. For instance, the solubility of CO<sub>2</sub> in imidazolium-based ionic liquids can be ~40 fold larger than the CO<sub>2</sub> solubility in aqueous bicarbonate solutions at standard temperature.<sup>35</sup> However, the ~10–20 fold lower diffusion coefficient of CO<sub>2</sub><sup>36,37</sup> in ionic liquids as compared to in aqueous solutions, combined with the lack of chemically enhanced CO<sub>2</sub> transport in the ionic liquids, will produce mass-transport limited current densities in such media that are on the same order of magnitude as those in aqueous solutions (Fig. 2).

#### 4.2 Conductance at the atmosphere/aqueous electrolyte interface

Regardless of the ideal activity, selectivity and coupling between the OER and CO<sub>2</sub>RR in the full electrochemical cells, the CO<sub>2</sub> flux at the atmosphere/aqueous electrolyte interface imposes constraints on the mass transfer and thus on the efficiency for the system. For aqueous electrolytes that have thicknesses larger than the width of the hydrodynamic boundary layer, the low solubility of CO<sub>2</sub> in water, combined with the relatively small diffusion coefficient of CO<sub>2</sub> in liquid water compared to in the gas phase, produces very low CO<sub>2</sub> fluxes and conductances. Hence, over large areas, either with natural convection or with forced convection sufficient to thin the hydrodynamic boundary layer in the aqueous phase to 10 μm, a value comparable to that obtained according to the Levich equation with a rotating disk electrode at a rotation velocity of 10<sup>6</sup> rpm,<sup>12</sup> the steady-state limiting CO<sub>2</sub> flux even with a 6-electron reduction of each CO<sub>2</sub> molecule is 100–1000 fold lower than the 10 mA cm<sup>-2</sup> current density produced by the solar photon flux in an efficient single or tandem photoelectrode system.<sup>38,39</sup> Hence regardless of the activity of an electrocatalyst for CO<sub>2</sub> reduction, the solar-to-fuels conversion efficiency of such a system will be limited to <0.1% based on the active area of the solar collection component. Additionally, the concentration overpotential will require higher voltages for a complete CO<sub>2</sub> reduction system than are expected based on the potential differences between the CO<sub>2</sub>RR half-reaction and the OER half-reaction alone, including their associated kinetic overpotentials at each electrode surface.

This conclusion is in accord with the CO<sub>2</sub> uptake fluxes that have been established previously for the air/ocean boundary for use in assessing the global carbon cycle in coupled air/ocean general circulation models. Specifically, extensive studies of CO<sub>2</sub> exchange at the air–sea interface have shown that the effective mass transfer coefficient of CO<sub>2</sub> across the air–liquid interface, specifically,  $\sigma_3$ , in Fig. 1c, is on the order of 10<sup>-3</sup>–10<sup>-2</sup> cm s<sup>-1</sup>, corresponding to a current density of ~10–100 μA cm<sup>-2</sup> for a 6-electron/6-proton CO<sub>2</sub>RR, over a large range of temperatures,

wind velocities, salinities and pH conditions.<sup>40–42</sup> In situations where the effective mass transfer coefficient,  $\sigma_3$  or  $\sigma_4$ , presents a transport limitation, the air/electrolyte interface equilibrium according to Henry's law may not be achieved. In this case, the device efficiency would be yet lower and would ultimately be limited by the rate of CO<sub>2</sub> transport across the air/electrolyte interface. Hence, without strategies to circumvent the inherently low CO<sub>2</sub> conductance at the air/water interface, very low solar-to-fuel conversion efficiencies will be obtained and/or the CO<sub>2</sub> capture and collection area will have to greatly exceed, by a factor of 100–1000, the active solar photon collection area of a sustainable solar-driven, aqueous-based, CO<sub>2</sub>RR system.

#### 4.3 Enhancement of interconversion rates for the bicarbonate buffer system

One strategy to circumvent the conductance limit imposed by liquid-phase transport, specifically by,  $\Phi_{\text{CO}_2} = \sigma_5 \Delta C_5$ , involves chemically enhancing the rate of CO<sub>2</sub> uptake by equilibrating the dissolved CO<sub>2</sub> with the bicarbonate and carbonic acid reservoirs in aqueous solutions buffered to pH values >7. Carbonic anhydrases are among the most well-known metallo-enzymes that catalyze the rapid interconversion of carbon dioxide and water to bicarbonate and protons.<sup>43</sup> In the absence of a catalyst, the reversible reaction occurs relatively slowly, as reflected in the rate constants tabulated in Table 1. At a CO<sub>2</sub> concentration of 14 μM, the catalyzed rate for the buffer interconversion reaction, as described using Michaelis–Menten kinetics for carbonic anhydrases, is ~200 s<sup>-1</sup> (assuming a maximum rate of conversion of 4 × 10<sup>5</sup> s<sup>-1</sup> and a Michaelis constant of 26 mM).<sup>44,45</sup> As a result, a carbonic anhydrase concentration of ~2.5 mM would be required to achieve an interconversion enhancement factor of 10<sup>6</sup> relative to the uncatalyzed case. The concentration of carbonic anhydrase in sea water is estimated to be <~100 nM,<sup>46</sup> so a 10<sup>6</sup> enhancement of the interconversion rate using such enzymes would require an enzyme concentration ~25 000-fold higher than the peak value in sea water systems.<sup>46</sup>

A hypothetical catalyst that had analogous catalytic activity to carbonic anhydrase, and that extremely rapidly replenished dissolved CO<sub>2</sub> near the cathode surface due to enhanced rates for the reverse reactions, reaction H<sup>+</sup> + HCO<sub>3</sub><sup>-</sup> → CO<sub>2</sub> + H<sub>2</sub>O and reaction HCO<sub>3</sub><sup>-</sup> → CO<sub>2</sub> + OH<sup>-</sup>, could in principle produce significant increases in the limiting current density for a CO<sub>2</sub>RR reactor, even when  $l_{\text{HBL}} = 100 \mu\text{m}$ , *i.e.*, for the natural convection case. As shown in Fig. 3, an interconversion-enhancement factor of at least 10<sup>5</sup> would however be needed before a CO<sub>2</sub>RR cell with 10% solar-to-fuels conversion efficiency could be constructed, other transport limitations notwithstanding (*vide infra*). The heretofore unknown interconversion catalyst must of course itself be robust, electrochemically inert at both of the electrodes in the system, and operate under conditions with which the other components of the CO<sub>2</sub>RR device are compatible.

#### 4.4 Implementation of thin-layer membrane assembly

The required CO<sub>2</sub> flux to the cathode could in principle alternatively be obtained by use of a thin-layer membrane-based



system (Fig. 5). The efficient transport in a thin-layer (tens of nanometers thick) membrane (Fig. 5) exploits the very small distance between the gas phase CO<sub>2</sub> and the catalyst at the cathode surface. Due to the required short length of the pathways, the implementation of this strategy in the CO<sub>2</sub>RR cell constrains the reduction products to be highly volatile/gaseous species such as methane or ethylene. Liquid fuel products, such as methanol or ethanol, which will form a liquid layer of the product at the electrocatalyst surface, will impede the CO<sub>2</sub> reactant transport towards the catalyst, and hence will result in unacceptably low CO<sub>2</sub> fluxes to the electrode surface, as in the case when the electrode is coated with a layer of liquid water (*vide supra*).

#### 4.5 Transport between the canopy layer and the electrolyte

The gas-phase transport of CO<sub>2</sub> near the electrode surface, specifically, at the canopy layer/membrane layer interface,  $\Phi_{\text{CO}_2} = \sigma_4 \Delta C_4$ , or the canopy layer/liquid layer interface,  $\Phi_{\text{CO}_2} = \sigma_3 \Delta C_3$ , does not impose significant limitations on the ability to deliver CO<sub>2</sub> to the CO<sub>2</sub>RR reactor. According to the kinetic theory of gases, the rate of surface bombardment of CO<sub>2</sub> molecules at  $p_{\text{CO}_2} = 400$  ppm is  $\sim 10^{20}$  molecules cm<sup>2</sup> s<sup>-1</sup>, which could produce a mass-transport-limited current density many orders of magnitude higher than the photon flux in unconcentrated solar illumination. Another more practical estimation of the CO<sub>2</sub> flux at the air/membrane or air/liquid interfaces can be obtained by using Fick's first law:

$$\Phi_{\text{CO}_2} = D \frac{[\text{CO}_2]_{\text{atmosphere}} - [\text{CO}_2]_{\text{ground}}}{l}, \quad (5)$$

where  $D$  is the diffusion coefficient of CO<sub>2</sub> in the atmosphere and  $l$  is the characteristic length for the diffusion gradient. Assuming laminar flow near the electrode surface of the CO<sub>2</sub>RR reactor at a modest wind velocity, 5 m s<sup>-1</sup>, the characteristic diffusion length,  $l$ , is given by  $l \sim L/(UL/D)^{1/2}$ ,<sup>47,48</sup> where  $L$  is the characteristic length scale of the device,  $U$  is the velocity magnitude, and  $D$  is the characteristic diffusion coefficient. Assuming  $[\text{CO}_2]_{\text{ground}} = 0$  yields a mass transport limited equivalent current density of  $\sim 5$  mA cm<sup>-2</sup> ( $\sim 5 \times 10^{15}$  molecules cm<sup>2</sup> s<sup>-1</sup>) for a 6-electron/6-proton CO<sub>2</sub> reduction process. A more turbulent, convective mixing in the canopy layer would produce a higher CO<sub>2</sub> flux to the electrolyte. Hence, from these estimations, rapid gas-phase transport near the electrode surface would be able to produce an equilibrium CO<sub>2</sub> concentration that follows Henry's law and would not serve as the ultimate practical constraint on the system efficiency.

The rapid transport between the canopy layer and the electrolyte is a result of the relatively high gas-phase diffusion coefficient of CO<sub>2</sub>. In the natural photosynthetic system, the terrestrial plant-based CO<sub>2</sub> fixation rate is significantly higher than the CO<sub>2</sub> flux across the air/ocean interface. Terrestrial plant-based photosynthesis thus takes advantage of the rapid CO<sub>2</sub> transport in the gas-phase as well as the 3-dimensional structure of the plants and trees on an  $\sim 1$  m height scale, which leads to a significant increase in the contact area per unit of geometric area on the earth's surface and results in a more

optimal "contactor" design than can be achieved at a planar air/water boundary over large horizontal length scales.

#### 4.6 Gas-phase transport of CO<sub>2</sub> between the troposphere and the ABL and between the ABL and the canopy layer for regional-scale deployment of CO<sub>2</sub>-reduction reactors

The fluxes of CO<sub>2</sub> between the troposphere and the atmospheric boundary layer (ABL), and between the ABL and the canopy layer, specifically,  $\Phi_{\text{CO}_2} = \sigma_1 \Delta C_1$  and  $\Phi_{\text{CO}_2} = \sigma_2 \Delta C_2$ , in Fig. 1c, also impose a constraint on the CO<sub>2</sub> conductance of CO<sub>2</sub>RR systems deployed at regional-scale, for which the length-scale of the CO<sub>2</sub>RR system is larger than the scale height of the atmosphere, broadly defined in the range between 10<sup>4</sup> and 10<sup>6</sup> km<sup>2</sup> (*i.e.* when vertical transport in the atmospheric column is more important than advection in determining the CO<sub>2</sub> concentration in the column), regardless of strategies used to enhance the conductance at the air/water or air/polymer interfaces. An estimate of the CO<sub>2</sub> mass transport limitation on scale lengths comparable to or larger than the scale height of the atmosphere can also be obtained by eqn (5), where now  $D$  is the turbulent diffusion coefficient of the atmosphere and  $l$  is the vertical gradient scale height. The minimal value for  $l$  is set by the scale height of the atmosphere, which is  $\sim 100$  km. In conjunction with an approximate value for the atmospheric turbulent diffusivity,  $D$ , of 10<sup>6</sup> cm<sup>2</sup> s<sup>-1</sup>, the maximum CO<sub>2</sub> flux is thus  $\sim 10^{15}$  molecules cm<sup>-2</sup> s<sup>-1</sup>, which for a 6-electron/6-proton CO<sub>2</sub>RR corresponds to a CO<sub>2</sub>-transport-limited current density of  $\sim 1$  mA cm<sup>-2</sup>.

Another estimation of the mass-transport-limited CO<sub>2</sub> flux can be obtained by reference to the net ecosystem-exchange (NEE) rate for CO<sub>2</sub>, which has been directly measured and monitored by various techniques, including eddy covariance methods, over long periods (months or years) in different regions worldwide.<sup>49–52</sup> Satellite retrieval methods that allow extraction of the vertical profile of CO<sub>2</sub> in an atmospheric column in turn allow formulation of a flux relationship between the CO<sub>2</sub> concentration differential "*i.e.* draw-down" in the ABL relative to the CO<sub>2</sub> concentration in the troposphere, as a function of the local NEE rate. A quasi-linear relationship at regional spatial scales between the net CO<sub>2</sub> flux and the CO<sub>2</sub> draw-down between the troposphere and the ABL has been observed, as expected.<sup>49,53</sup> On average, an  $\sim 2$  μmol m<sup>-2</sup> s<sup>-1</sup> net CO<sub>2</sub> flux between the troposphere and the ABL results in  $\sim 10$  ppm reduction in the CO<sub>2</sub> concentration in the ABL,<sup>49</sup> which corresponds to an effective mass transfer coefficient of 0.44 cm s<sup>-1</sup>. If a sustained 10% solar-to-fuel (STF) conversion efficiency were achieved for a 6-electron/6-proton CO<sub>2</sub> reduction process at the cell level, and such a system were deployed on a regional scale, extrapolation of this linear relationship indicates that a daily average CO<sub>2</sub> draw-down of  $\sim 130$  ppm would be produced between the troposphere and the entire (well-mixed) ABL, 2–2.5 km in height (assuming a 20% capacity factor for the CO<sub>2</sub>RR reactor), by the sustained mass flux, and consumption, of CO<sub>2</sub> at the electrode surface. During the peak operation of a solar-driven CO<sub>2</sub>RR system deployed on a regional scale, a significantly larger drawdown of CO<sub>2</sub> and a large temporal variation of the CO<sub>2</sub> concentration near the surface of CO<sub>2</sub>RR reactor would be



expected. The decreased CO<sub>2</sub> levels at the electrode surface would in turn require even more active catalysts. Moreover, the height of the ABL and the concentration of CO<sub>2</sub> in the ABL are also highly dependent on storms, and weather conditions in the atmosphere, *etc.* The flux into the ABL can even under some conditions invert in sign. Hence, the significant alteration of the CO<sub>2</sub> concentration in the ABL, and concomitant spatial and temporal variations in the attainable CO<sub>2</sub> uptake flux at the surface of the Earth, present significant practical and engineering impediments to the deployment of regional-scale systems that would involve rapid CO<sub>2</sub> consumption rates at the electrode surface, assuming that such a system can be achieved through unprecedented catalyst development, along with aggressive strategies to increase the CO<sub>2</sub> uptake flux into the reactor (*i.e.*, new CO<sub>2</sub> reservoir interconversion catalysts and/or for gaseous products implementing an ultra-thin polymeric cathode electrolyte) to significantly enhance the diffusive CO<sub>2</sub> flux relative to the value observed for natural air/ocean boundaries. It is reasonable to surmise that the peak net primary productivity of plant-based photosynthesis is constrained, in part due to down-regulation of photosynthesis at high light intensities, to minimize the sensitivity of the system to atmospheric CO<sub>2</sub> concentration and transport fluctuations, because otherwise these fluctuations that occur as a function of changes in the physical state of the atmosphere due to weather, storms, and other processes would significantly affect the CO<sub>2</sub> concentration in the ABL and thus the performance of the CO<sub>2</sub>RR system at the Earth's surface.

The CO<sub>2</sub> flux between the ABL and the canopy layer has an effective mass transfer coefficient,  $\sigma_2 = 0.44 \text{ cm s}^{-1}$  that is comparable to the mass transfer coefficient,  $\sigma_1$ , at the troposphere/ABL interface. Hence, at the CO<sub>2</sub> flux required to sustain a 10% efficient CO<sub>2</sub>RR cell at the electrode surface, a daily average CO<sub>2</sub> concentration differential of 260 ppm would be produced between the canopy layer and the troposphere. The lower CO<sub>2</sub> concentration in the canopy layer, to which the dissolved CO<sub>2</sub> concentration in electrolytes is equilibrated, would further increase the CO<sub>2</sub> concentration overpotential by  $\sim 100\text{--}200 \text{ mV}$  in the system, but at peak operation, the transient and temporal depletion of CO<sub>2</sub> at the surface of the CO<sub>2</sub>RR reactor system would produce a much larger overpotential.

## V. Conclusions

The limited CO<sub>2</sub> transport in the presence of bulk electrolyte layers ( $>10 \mu\text{m}$ ) at a cathode surface serves as a physical limitation to the construction of a sustainable, scalable solar-driven CO<sub>2</sub>RR cell with a technologically relevant efficiency that operates at  $p_{\text{CO}_2} = 400 \text{ ppm}$ . Rapid replenishment of CO<sub>2</sub>(aq) near a cathode surface using catalysts with activities and reactivities analogous to the carbonic anhydrase enzymes, that enhance the interconversion between the bicarbonate and CO<sub>2</sub>, could hypothetically significantly increase the achievable steady-state limiting current density and concomitantly reduce the CO<sub>2</sub> concentration overpotential for such a system. For instance, an interconversion enhancement factor of  $10^6$  could

in principle increase the steady-state limiting current density to  $>20 \text{ mA cm}^{-2}$  in a pH = 11.2 aqueous solution. Alternatively, a catalyst-embedded, thin-layer architecture that minimizes the CO<sub>2</sub> transport pathways in electrolyte layers could in principle also produce large and sustainable CO<sub>2</sub> reduction current densities at  $p_{\text{CO}_2} = 400 \text{ ppm}$ , for gas-phase products and reactants. The CO<sub>2</sub> flux at the troposphere/ABL interface and at the ABL/canopy layer interface imposes significant physical constraints on the realization of an efficient, sustainable, and globally scalable CO<sub>2</sub>RR solar-fuels system. Large-scale implementation of CO<sub>2</sub>RR cells with a 10% solar-to-fuel (STF) conversion efficiency for a 6-electron/6-proton CO<sub>2</sub> reduction process would entail a 130 ppm steady-state troposphere/ABL drawdown of the CO<sub>2</sub> concentration over the entire 2.5 km high ABL, with much higher depletion of the CO<sub>2</sub> concentration during periods of high solar insolation onto the reactors. This level of CO<sub>2</sub> depletion would have profound environmental impacts in the region, and would produce a system performance that was subject to large variability in response to the weather conditions as well as to the presence and intensity of storms, *etc.* and other conditions that affect the CO<sub>2</sub> transport at the troposphere/ABL boundary as well as in the ABL.

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