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# Hydration and ion pair formation in aqueous $Y^{3+}$ -salt solutions†

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Raman spectra of aqueous yttrium perchlorate, triflate (trifluoromethanesulfonate), chloride and nitrate solutions were measured over a broad concentration range (0.198–3.252 mol L<sup>-1</sup>). The spectra range from low wavenumbers to 4200 cm<sup>-1</sup>. A very weak mode at 384 cm<sup>-1</sup> with a full width at half height at 50 cm<sup>-1</sup> in the isotropic spectrum suggests that the  $Y^{3+}$  – octa-aqua ion is thermodynamically stable in dilute perchlorate solutions (~0.5 mol L<sup>-1</sup>) while in concentrated perchlorate solutions outer-sphere ion pairs and contact ion pairs are formed. The octa-hydrate,  $[Y(OH_2)_8]^{3+}$  was also detected in a 1.10 mol L<sup>-1</sup> aqueous  $Y(CF_3SO_3)_3$  solution. Furthermore, very weak and broad depolarized modes could be detected which are assigned to  $[Y(OH_2)_8]^{3+}(aq)$  at 100, 166, 234 and 320 cm<sup>-1</sup> confirming that a hexa-hydrate is not compatible with the hydrated species in solution. In yttrium chloride solutions contact ion pair formation was detected over the measured concentration range from 0.479–3.212 mol L<sup>-1</sup>. The contact ion pairs in  $YCl_3(aq)$  are fairly weak and disappear with dilution. At a concentration <0.2 mol L<sup>-1</sup> almost all complexes have disappeared. In  $YCl_3$  solutions, with additional HCl, chloro-complexes of the type  $[Y(OH_2)_{8-n}Cl_n]^{+3-n}$  ( $n = 1, 2$ ) are formed. The  $Y(NO_3)_3(aq)$  spectra were compared with a spectrum of a dilute  $NaNO_3$  solution and it was concluded that in  $Y(NO_3)_3(aq)$  over the concentration range from 2.035–0.198 mol L<sup>-1</sup> nitrate-complexes  $[Y(OH_2)_{8-n}(NO_3)_n]^{+3-n}$  ( $n = 1, 2$ ) are formed. The nitrate-complexes are weak and disappear with dilution <0.1 mol L<sup>-1</sup>. DFT geometry optimizations and frequency calculations are reported for both the yttrium–water cluster in the gas phase and the cluster within a polarizable continuum model in order to implicitly describe the presence of the bulk solvent. The bond distance and angle for the square antiprismatic cluster geometry of  $[Y(OH_2)_8]^{3+}$  with the polarizable dielectric continuum is in good agreement with data from recent structural experimental measurements. The DFT frequency of the Y–O stretching mode of the  $[Y(OH_2)_8]^{3+}$  cluster, in a polarizable continuum, is at 372 cm<sup>-1</sup> in satisfactory agreement with the experimental value.

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## 1. Introduction

Yttrium is a silvery-metallic transition metal in group 3 and chemically similar to the lanthanides. Yttrium is almost always found combined with the lanthanides in rare earth minerals but is never found in nature as a free element. The most important use of yttrium is in making phosphors and also in the production of electrolytes, electronic filters, lasers and superconductors.<sup>1–3</sup> Its radioactive isotope, <sup>90</sup>Y, has a wide use in radiation therapy to treat cancer.<sup>4</sup> Yttrium has no known biological role though it is found in most, if not all, organisms and tends to concentrate in the liver, kidney, spleen, lungs,

and bones of humans.<sup>5</sup> The coordination numbers in crystalline  $Y^{3+}$ -compounds vary widely from 3 to 12<sup>6</sup> but eight and nine fold coordination are the most frequent.<sup>7–11</sup>

In aqueous solution, yttrium exists exclusively in the trivalent state,  $Y^{3+}$ , and the ion is strongly hydrated judging by its high hydration enthalpy,<sup>3</sup> due to its high charge to radius ratio. The hydration number for  $Y^{3+}$  in aqueous solution was determined based on structural techniques such as X-ray diffraction (XRD), anomalous X-ray diffraction (AXD) and large angle X-ray scattering (LAXS).<sup>12–16</sup> The local structure of aqueous  $Y^{3+}$  salt solutions was also studied applying extended X-ray absorption fine structure (EXAFS), and X-ray absorption fine structure (XAFS) methods.<sup>17–20</sup> A combined study of neutron scattering and EXAFS measurements applying reversed modeling on  $YCl_3(aq)$  must be mentioned.<sup>21</sup> A summary of experimental structural results is presented in Table 1. From the Table, it is clear that  $Y^{3+}$  is hydrated by 8 water molecules in the first-shell forming a square-antiprismatic geometry. The  $Y^{3+}$ –O bond distance was found at

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Table 1 Coordination numbers and Y–O bond distances for aqueous Y<sup>3+</sup>–salt solutions at room temperature (298 K)

Method	Solution composition	La <sup>3+</sup> /mol L <sup>-1</sup>	CN	Y–O bond distance/Å	Remarks	Ref.
XRD	Y(ClO <sub>4</sub> ) <sub>3</sub>	1.094	8.0 ± 0.3	2.37 ± 0.005	Second sphere: 4.52 Å	12
	Y <sub>2</sub> (SeO <sub>4</sub> ) <sub>3</sub>	0.77	8.0 ± 0.3	2.33 ± 0.005	Second sphere: 4.47 Å	
		0.89		2.325 ± 0.005	Second sphere: 4.47 Å	
AXD	YCl <sub>3</sub>	0.5	8.1 ± 0.3	2.46 ± 0.02		13
		1.0	8.2 ± 0.5	2.51 ± 0.02		
EXAFS	YCl <sub>3</sub>	0.6	7.5 ± 0.3	2.34 ± 0.02	Y K-edge additionally Raman spectra of YCl <sub>3</sub> in H <sub>2</sub> O and D <sub>2</sub> O are given	17
		1.2	7.6 ± 0.3	2.34 ± 0.02		
		2.3	7.9 ± 0.3	2.34 ± 0.02		
	YBr <sub>3</sub>	0.5	7.5 ± 0.3	2.33 ± 0.02		14
		1.0	8.5 ± 0.3	2.33 ± 0.02		
		2.1	7.5 ± 0.3	2.34 ± 0.02		
XRD	YCl <sub>3</sub>	2.73	7.7 ± 0.3	2.36 ± 0.02		14
	YBr <sub>3</sub>	2.67	7.8 ± 0.3	2.36 ± 0.02		
EXAFS	YCl <sub>3</sub>	0.1	9.1 ± 0.2	2.36 ± 0.02	Temperature dependent measurements from 25–340 °C	18
	Y(NO <sub>3</sub> ) <sub>3</sub>	0.05	9.4 ± 0.2	2.367 ± 0.006		
EXAFS/ LAXS	Y(ClO <sub>4</sub> ) <sub>3</sub> acidified with HClO <sub>4</sub>	1.71	8.0 ± 0.1	2.368 ± 0.005	Mean value of second hydration sphere consisting of ~16 oxygen atoms at a mean Y–O distance of 4.40(4) Å	19
		1.14				
EXAFS/ XANES	YBr <sub>3</sub>	0.005 mol kg <sup>-1</sup>	8.6 ± 0.1	2.352 ± 0.003	Concentration profile from 0.005–2.00 mol kg <sup>-1</sup>	20
		2.00 mol kg <sup>-1</sup>	8.8 ± 0.1	2.353 ± 0.001		
AXD	YCl <sub>3</sub>	3.5 mol kg <sup>-1</sup>	8	2.33	Second sphere at 4.77 YCl <sub>3</sub> ; contact ion pairs between Y <sup>3+</sup> and Cl <sup>-</sup>	15
XRD	Y(NO <sub>3</sub> ) <sub>3</sub>	2.89	8.0 ± 0.1	2.36 ± 0.01	Additionally Raman spectrum of Y(NO <sub>3</sub> ) <sub>3</sub> in H <sub>2</sub> O was given	16
ND/EXAFS	YCl <sub>3</sub>	1 mol kg <sup>-1</sup>	~7.4 ± 0.5 Y–O <sub>w</sub> ~0.8 ± 0.2 Y–Cl	2.33	Contact ion pairs between Y <sup>3+</sup> and Cl <sup>-</sup> were established	21

2.366 Å. In addition to the experimental work, a computer simulation significantly contributed to clarifying the details of the structure and dynamics of the waters in the first hydration shell of Y<sup>3+</sup>.<sup>22</sup> This simulation study confirmed the Y<sup>3+</sup> octahydrate and its square antiprismatic geometry. Furthermore, the structural results show that X-ray measurements and EXAFS investigations were carried out at high and low solute concentrations using different anions as counter ions. This, however, poses a problem because contact ion pairs may form in concentrated solutions and this fact has been reported in an earlier XRD study on yttrium selenate solutions.<sup>12</sup> A recent notable structural study on an aqueous 1 mol kg<sup>-1</sup> YCl<sub>3</sub> solution applying a local structure refinement model of disordered material<sup>21</sup> revealed contact ion pairs between Y<sup>3+</sup> and Cl<sup>-</sup>.

Raman spectroscopy which probes the immediate environment of metal ions in solution was frequently used to study hydrated cations by measuring the vibrational modes of a [M(H<sub>2</sub>O)<sub>n</sub>]<sup>x+</sup> species.<sup>23–28</sup> A highly polarized band in the 250–550 cm<sup>-1</sup> region due to the symmetrical metal–oxygen mode of the hydrated cation is the most characteristic peak. This peak is sensitive to possible ion pair formation. Occasionally, all the bands of the metal–oxygen modes may be observed and used to support the assignment of the point group symmetry and coordination number in aqueous solution. Raman scattering measurements on Y<sup>3+</sup>(aq) should allow, in principle, the characterization of the solution structure in greater detail. However, aqueous Y<sup>3+</sup> solutions were measured by Raman

spectroscopy only on a few occasions.<sup>16,17,29</sup> Due to the limitations of Raman spectroscopic technique at the time, the quality of the spectra in the low frequency range<sup>17,29</sup> was poor. Furthermore, no reduced spectral treatment of the data in the low frequency range was applied. It has been shown on a variety of aqueous metal salt solutions that for meaningful Raman spectroscopic analysis, reduced spectra (spectra in *R*-format) are necessary in the terahertz frequency range<sup>23–28</sup> in order to account for the Bose-Einstein correction and scattering factor.<sup>23,30</sup>

The present study was undertaken to characterize the hydration and speciation in aqueous Y<sup>3+</sup> solutions and to this end Y<sup>3+</sup> – salt solutions with common anions (ClO<sub>4</sub><sup>-</sup>, CF<sub>3</sub>SO<sub>3</sub><sup>-</sup>, Cl<sup>-</sup>, NO<sub>3</sub><sup>-</sup>) were studied over a broader concentration range and down to the terahertz frequency range. Triflate and perchlorate are considered non-complex-forming anions and were therefore chosen to measure the Y–O modes in aqueous solution so as to identify and assign bands unique to the first hydration sphere of Y<sup>3+</sup>(aq). A Y(ClO<sub>4</sub>)<sub>3</sub> solution in heavy water was also measured in order to characterize the vibrational isotope effect by changing from [Y(H<sub>2</sub>O)<sub>8</sub>]<sup>3+</sup> to [Y(D<sub>2</sub>O)<sub>8</sub>]<sup>3+</sup>. In a variety of di- and trivalent metal ion solutions with chloride and nitrate as counterions, however, it has been shown that these anions readily form complexes<sup>24–28</sup> and the question arises as to whether these complexes also occur with Y<sup>3+</sup>(aq). Specifically, the following aqueous systems were measured by Raman spectroscopy at 23 °C: Y(ClO<sub>4</sub>)<sub>3</sub> and



$Y(\text{ClO}_4)_3$  plus  $\text{HClO}_4$ ,  $Y(\text{CF}_3\text{SO}_3)_3$ ,  $Y\text{Cl}_3$  and  $Y\text{Cl}_3$  plus additional  $\text{HCl}$ , and  $Y(\text{NO}_3)_3$ .  $Y(\text{ClO}_4)_3$  solutions in heavy water were measured not only to determine the isotope effect on the Y–O modes (Y–OH<sub>2</sub>/D<sub>2</sub>O) but also to measure the influence of the salts on the water and heavy water stretching and deformation bands as a function of the  $Y^{3+}$  salt concentration.

Calculations on yttrium–water clusters with six and eight waters in the first sphere were considered applying density functional theory (DFT) in the gas phase. However, gas phase clusters do not reflect the aqua-cluster geometry nor the vibrational modes of metal ions in solution<sup>23–28</sup> and therefore,  $Y^{3+}$ –clusters with a polarizable dielectric continuum were simulated in order to take into account the effects of the bulk solvent. Frequency calculations were carried out *via* the calculation of the second derivative of the energy with respect to the nuclear positions of  $Y^{3+}$ –water clusters.

## 2. Experimental details; data analysis and DFT calculations on $Y^{3+}$ –water clusters

### A. Preparation of solutions

The yttrium ion concentrations of all solutions were analysed by complexometric titration.<sup>31</sup> The solution densities were determined with a pycnometer at 23 °C and the molar ratios water per salt were calculated ( $R_w$ -values). For Raman spectroscopic measurements the solutions were filtered through a fine sintered glass frit (1–1.6 μm pore size). The solutions showed no Tyndall effect and were “optically empty”.<sup>32</sup>

Yttrium perchlorate solutions were prepared from  $Y_2O_3$  (Sigma-Aldrich, 99.9%) and  $\text{HClO}_4$  in a beaker until all oxide dissolved. A  $Y(\text{ClO}_4)_3$  stock solution was prepared at 2.559 mol L<sup>-1</sup> ( $R_w = 16.25$ ). This solution was acidified with a slight amount of  $\text{HClO}_4$  and a pH value at ~3.5 for the concentrated solutions was measured. From this stock solution, the following dilution series was prepared: 2.378 mol L<sup>-1</sup> ( $R_w = 21.46$ ), 1.785 mol L<sup>-1</sup> ( $R_w = 25.67$ ), 1.280 mol L<sup>-1</sup> ( $R_w = 37.81$ ), 0.853 mol L<sup>-1</sup> ( $R_w = 59.45$ ), 0.640 mol L<sup>-1</sup> ( $R_w = 81.10$ ) and 0.256 mol L<sup>-1</sup> ( $R_w = 210.9$ ). The solutions were analysed for dissolved chloride with a 5%  $\text{AgNO}_3$  solution. The absence of a white  $\text{AgCl}$  precipitate was proof that the stock solution was free of  $\text{Cl}^-$ .

Two  $Y(\text{ClO}_4)_3$  solutions in heavy water were prepared from a deuterated  $Y(\text{ClO}_4)_3$  stock solution and with 99.9 atom % D (Sigma-Aldrich) at 2.30 mol L<sup>-1</sup> and 1.73 mol L<sup>-1</sup>.

A 1.10 mol L<sup>-1</sup>  $Y(\text{CF}_3\text{SO}_3)_3$  solution was prepared from anhydrous  $Y(\text{CF}_3\text{SO}_3)_3$  (Sigma-Aldrich, 99.9%) and triply distilled water.

Seven  $Y\text{Cl}_3$  solutions were prepared from  $Y\text{Cl}_3 \cdot 6\text{H}_2\text{O}$  (Sigma, 99.9%) and triply distilled water. The solution concentrations were found at 3.212 mol L<sup>-1</sup> ( $R_w = 15.40$ ), 2.378 mol L<sup>-1</sup> ( $R_w = 21.46$ ), 2.141 mol L<sup>-1</sup> ( $R_w = 24.00$ ), 1.175 ( $R_w = 45.30$ ), 1.010 mol L<sup>-1</sup> ( $R_w = 53.53$ ), 0.803 mol L<sup>-1</sup> ( $R_w = 67.19$ ) and 0.479 mol L<sup>-1</sup> ( $R_w = 113.82$ ). Furthermore, a solution series

with an excess of  $\text{HCl}$  was prepared ( $Y\text{Cl}_3$  plus  $\text{HCl}$ ): (A) 2.13 mol L<sup>-1</sup>  $Y\text{Cl}_3$  + 4.03 mol L<sup>-1</sup>  $\text{HCl}$  and (B) 2.17 mol L<sup>-1</sup>  $Y\text{Cl}_3$  + 1.31 mol L<sup>-1</sup>  $\text{HCl}$ . Two  $\text{HCl}$  solutions were also prepared at 3.97 mol L<sup>-1</sup> and at 1.325 mol L<sup>-1</sup>.

Three  $Y(\text{NO}_3)_3$  solutions were prepared from  $Y(\text{NO}_3)_3 \cdot 6\text{H}_2\text{O}$  and triply distilled water: 2.035 mol L<sup>-1</sup> ( $R_w = 23.04$ ), 1.036 mol L<sup>-1</sup> ( $R_w = 49.20$ ) and 0.198 mol L<sup>-1</sup> ( $R_w = 275.88$ ).

### B. Spectroscopic measurements

Raman spectra were measured in the macro chamber of the T 64000 Raman spectrometer from Jobin Yvon in a 90° scattering geometry at 23 °C. These measurements have been described elsewhere.<sup>30,33</sup> A quartz cuvette from Hellma Analytics (Müllheim, Germany) with 10 mm path length and a volume 1000 μL was used. Briefly, the spectra were excited with the 514.532 nm line of an  $\text{Ar}^+$  laser at a power level of 1100 mW at the sample. After passing the spectrometer in subtractive mode, with gratings of 1800 grooves per mm, the scattered light was detected with a cooled CCD detector.  $I_{VV}$  and  $I_{VH}$  spectra were obtained with fixed polarization of the laser beam by rotating the polarizer at 90° between the sample and the entrance slit to give the scattering geometries:

$$I_{VV} = I(Y[ZZ]X) = 45\alpha^2 + 4\gamma'^2 \quad (1)$$

and

$$I_{VH} = I(Y[ZY]X) = 3\gamma'^2. \quad (2)$$

The isotropic spectrum,  $I_{\text{iso}}$  is then constructed:

$$I_{\text{iso}} = I_{VV} - 4/3 \cdot I_{VH}. \quad (3)$$

The polarization degree of the Raman bands,  $\rho$  ( $\rho = I_{VH}/I_{VV}$ ) was determined using a polarizer and if necessary adjusted before each measuring cycle using  $\text{CCl}_4$ . A detailed account on this procedure may be found in ref. 30 and 33.

In order to obtain spectra defined as  $R(\bar{\nu})$  which are independent of the excitation wavenumber  $\nu_L$ , the measured Stokes intensity should be corrected for the scattering factor  $(\nu_L - \bar{\nu})^3$ . In the case of counting methods used, the measured count rates were corrected with the factor  $(\nu_L - \bar{\nu})^3$ . The spectra were further corrected for the Bose-Einstein temperature factor,  $B = [1 - \exp(-h\bar{\nu}c/kT)]$  and the frequency factor,  $\bar{\nu}$ , to give the so called reduced spectrum,  $R(\bar{\nu})$ . It is also possible to calculate the isotropic spectrum in  $R$ -format from the corrected  $R_{VV}$  and  $R_{VH}$  spectra according to eqn (4):

$$R(\bar{\nu})_{\text{iso}} = R(\bar{\nu})_{VV} - 4/3R(\bar{\nu})_{VH}. \quad (4)$$

In the low wavenumber region, the  $I(\bar{\nu})$  and  $R_Q(\bar{\nu})$  spectra are significantly different and only the spectra in  $R$ -format are presented. It should be noted that one of the advantages of using isotropic  $R$ -spectra is that the baseline is almost flat in the 50–700 cm<sup>-1</sup> wavenumber region allowing relatively unperturbed observation of the presence of any weak modes.<sup>23,30,33</sup>



### C. DFT calculations

The calculations were carried out using the Gaussian03 package<sup>34</sup> employing the unrestricted B3LYP functional.<sup>35</sup> The LANL2DZ (Los Alamos National Laboratory 2 Double Zeta) basis set was used which adequately reproduces the geometrical parameters, in particular the experimentally observed Y–O distance. LANL2DZ uses a relativistic effective core potential (ECP) for the inner electrons of  $Y^{3+}$ , and its valence electrons. All electrons for the other atoms are described by D95 V (Dunning/ Huzinaga valence double-zeta) functions. The 6-31G (double-zeta Pople type) basis set and application of diffuse and polarization functions for the atoms O and H resulted in small changes. Placing the cluster in a solvent continuum employing the Polarized Continuum Model (PCM) which takes into account the solvation effect of bulk water gave significantly better results compared with the experimental frequencies. The PCM used was the version described in ref. 36 where the solvent is modelled as an isotropic and homogeneous continuum, characterized by its dielectric properties. The cavity is defined as a set of interlocking spheres attached to the solute atoms. The electrostatic solute–solution interaction is calculated introducing an apparent charge distribution spread on the cavity surface.

Geometries of gas phase clusters with 8 water molecules surrounding the  $Y^{3+}$  ion, were optimized applying different basis sets and several cluster geometries for  $[Y(H_2O)_8]^{3+}$  with different symmetries namely  $D_4$ ,  $C_2$  and  $S_8$  were considered. A  $[Y(H_2O)_8]^{3+}$  cluster with symmetry  $S_8$  including a polarizable dielectric continuum (PC) was simulated in order to take into account the solvent effect. The cluster with  $S_8$  symmetry was the only cluster which led to an energy minimum without imaginary frequencies. The frequencies of the  $[Y(H_2O)_8]^{3+}$  cluster including a polarizable dielectric continuum were calculated (B3LYP/LANL2DZ). The DFT simulations on  $[Y(H_2O)_6]^{3+}$  gave a stable geometry with symmetry  $T_h$ . The  $[Y(H_2O)_6]^{3+}$  cluster imbedded in a PC was optimized and frequencies were calculated. The geometric data and the frequency of the breathing mode of the  $[Y(H_2O)_8]^{3+}$  cluster in comparison with the  $[Y(H_2O)_6]^{3+}$  will be discussed below.

## 3. Results and discussion

### 3.1. The $[Y(OH_2)_8]^{3+}(aq)$ ion

$Y^{3+}$  is strongly hydrated in aqueous solution as indicated by its large standard molar enthalpy of hydration ( $\Delta H_{hyd}^0$ ) at  $\sim -3640$  kJ mol<sup>-1</sup> but it should be stressed that  $\Delta H_{hyd}^0$  – values reported in the literature scatter from  $-3583$  to  $-3733$  kJ mol<sup>-1</sup>.<sup>37–42</sup> Our DFT value for  $\Delta H_{hyd}^0$  is  $-3951$  kJ mol<sup>-1</sup> which is smaller than the thermodynamic value (calculation procedure in Appendix A). The  $Y^{3+}$  ion, hydrated by eight water molecules in the first hydration shell with a Y–O bond distance at 2.366 Å, and a second hydration shell, much more diffuse, at 4.40 Å consisting of  $\sim 16$  water molecules was observed.<sup>19</sup> The optimized  $[Y(H_2O)_8]^{3+}$  geometry in the gas phase and also with a polarizable continuum gave a square antiprismatic  $YO_8$

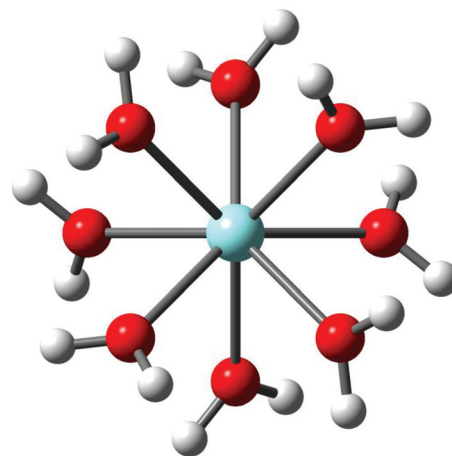


Fig. 1 Structure of the octa-aqua  $Y^{3+}$ -ion ( $S_8$  – symmetry).

coordination polyhedron with symmetry  $S_8$  (Fig. 1). The cluster,  $[Y(H_2O)_8]^{3+}$ , was also optimized applying higher basis sets which led to geometries with symmetry  $D_4$  and  $C_2$  (Table S1†). However, only the  $[Y(H_2O)_8]^{3+}$  cluster with  $S_8$  symmetry imbedded in a PC could be successfully simulated. The calculated Y–O bond distance of the  $[Y(H_2O)_8]^{3+}$  cluster with a solvation sphere, taking into account the influence of the bulk water, is in good agreement with the experimental value (Table 1). The  $[Y(H_2O)_8]^{3+}$  cluster in the gas phase, however, shows a larger value compared to the experimental Y–O bond distance (lack of bulk water). These DFT results are given in Table 2 together with the experimental data and a Car-Parrinello molecular dynamics (CPMD) simulation result.<sup>22</sup>

A  $Y^{3+}$ -hexa-hydrate was also successfully optimized but a noticeably smaller Y–O bond distance (Table S2†) was found compared to the measured one at 2.366 Å (ref. 19) which shows that the hexa-hydrate may be ruled out as a valid species in aqueous solution.‡ The results for the  $[Y(H_2O)_6]^{3+}$  in the gas phase and modelled with a solvation sphere are also given in Table S2.† (In contrast to solution state, in crystalline compounds CNs vary from 3–12.<sup>3,6</sup>)

The *vibrational analysis* of the  $[Y(OH_2)_8]^{3+}$  ( $S_8$  symmetry) with its 69 normal modes (n.m.'s) leads to the following irreducible representation:  $\Gamma_{\nu}(S_8) = 8a(Ra) + 9b(i.r.) + 18e_1(Ra, i.r.) + 18e_2(n.a.) + 16e_3(n.a.)$ . The modes with character a and  $e_1$  are Raman active and those with character b and  $e_1$  are infrared active. The vibrations can be divided into 48 internal and external vibrations of the eight coordinated water molecules plus 21 n. m.'s of the  $YO_8$  skeleton.

The vibrations of the water modes are decoupled from those of the  $YO_8$  skeleton and the water molecules of the first shell are considered point masses. The  $YO_8$  skeleton ( $D_{4d}$  symmetry) with its 9 atoms leads to 21 n.m.'s. The irreducible representation of these skeleton modes is as follows:  $\Gamma_{\nu}(D_{4d}) = 2a_1(Ra) + b_1(i.a.) + 2b_2(i.r.) + 3e_1(i.r.) + 3e_2(Ra) + 2e_3(Ra)$ . Although

‡ In early literature<sup>29</sup> a  $Y^{3+}$ -hexahydrate was assumed in the solution state.



**Table 2** Geometrical parameters such as bond distances and bond angles of  $[\text{Y}(\text{H}_2\text{O})_8]^{3+}$  imbedded in a polarizable dielectric continuum. Comparison of the DFT results (B3LYP/LANL2DZ) with published MD simulation and experimental results

Bond distances (Å) and angles (°)	DFT data/ gas phase cluster	DFT data/ cluster + PC model	Ref. 22 <sup>a</sup>	Ref. 12 <sup>b</sup>	Ref. 19 <sup>c</sup>	Ref. 18 <sup>d</sup>
Y–O	2.399	2.354	2.38	2.37	2.368	2.618
O–H	0.981	0.989	0.96			
H–O–H	109.6	110.9	106			

<sup>a</sup> CPMD; O–H bond distance and H–O–H angle from Fig. 5.<sup>22</sup> <sup>b</sup> XRD: results for  $\text{Y}(\text{ClO}_4)_3(\text{aq})$ . <sup>c</sup> EXAFS: results for  $\text{Y}(\text{ClO}_4)_3(\text{aq})$ . <sup>d</sup> EXAFS: results on diluted  $\text{YBr}_3(\text{aq})$ .

the  $\text{YO}_8$  skeleton possesses no symmetry centre, the mutual exclusion rule is nevertheless effective. The 7 modes with the character  $a_1$ ,  $e_2$  and  $e_3$  are Raman active while the six modes with the character  $b_1$ ,  $b_2$  and  $e_1$  are infrared allowed. The symmetric Y–O stretch, the breathing mode, is only Raman active and appears strongly polarized in the Raman spectrum as the strongest band of the skeleton. Two additional depolarized Raman active stretching modes are expected (character  $e_2$  and  $e_3$ ) as well as four other Raman deformation modes (character  $a_1$ ,  $e_2$  and  $e_3$ ). In I.R., two stretching modes (character  $b_2$  and  $e_1$ ) are expected and the remaining are deformations. In reality, however, the skeleton modes may not always be easily detected because they appear quite broad, weak and even obscured.

Considering the coordinated water molecules of the  $[\text{Y}(\text{OH}_2)_8]^{3+}$  cluster, the internal and external n.m.'s of the water molecules may be divided into 24 internal and 24 external vibrations. These vibrations are derived from the rotational- and translational degrees of freedom of the isolated water molecule. The n.m.'s of these waters, the external modes, are librations such as wag, twist, and rock.<sup>43</sup> Generally, the water molecules in the metal-aqua complexes possess weak, very broad modes below  $1200\text{ cm}^{-1}$ . In addition to these librations, internal water modes are observed: the deformation mode,  $\nu_2(\text{H}_2\text{O})$  and two stretching OH modes,  $\nu_1$  and  $\nu_3$ . The deformation mode in liquid water is found at  $1640\text{ cm}^{-1}$  and the stretching modes at  $\sim 3400\text{ cm}^{-1}$  appear as a very broad structured band of H-bonded water molecules. The water modes are modified when coordinated to metal ions such as  $\text{Y}^{3+}$  but are difficult to separate from the contributions of the librational and internal water modes of the bulk phase. In neat liquid water, the H-bonded water molecules show broad and weak librational modes and internal water modes, the deformation band,  $\delta$  H–O–H, and the stretching O–H bands.<sup>43</sup> Spectra of liquid water and heavy water, bands and band assignments are given elsewhere.<sup>44–46</sup>

The hydration sphere of  $\text{Y}^{3+}(\text{aq})$  is somewhat labile and a water-exchange rate constant  $k_{\text{ex}}$  at  $25\text{ }^\circ\text{C}$  was given at  $2 \times 10^7\text{ s}^{-1}$  (from  $\text{H}_2\text{O}-\text{SO}_4^{2-}$  interchange rates) with a water residence time  $\tau = 50\text{ ns}$ . The hydration sphere of  $\text{Y}^{3+}(\text{aq})$ , however, is

less labile compared to  $[\text{La}(\text{OH}_2)_9]^{3+}(\text{aq})$ .<sup>47,48</sup> § The mechanistic path for the water exchange for  $[\text{Ho}(\text{OH}_2)_8]^{3+}$  follows an associative water exchange process.<sup>51–53</sup> It is safe to assume a similar water exchange mechanism for  $\text{Y}^{3+}(\text{aq})$  because of its similar ionic radius compared to  $\text{Ho}^{3+}(\text{aq})$ .<sup>54</sup>

Chemically, yttrium resembles the heavy rare earth elements more closely than scandium,<sup>3,6</sup> its neighbor in the periodic table, and especially holmium in its chemical behavior.<sup>3</sup>  $\text{Y}^{3+}(\text{aq})$  is less basic in aqueous solution ( $\log K_{\text{h},1} = -7.8$ ) compared to  $\text{La}^{3+}(\text{aq})$  ( $\log K_{\text{h},1} = -8.81$ ).<sup>55</sup> A first principle MD simulation on the stepwise hydrolysis reaction of  $\text{Y}^{3+}$  in aqueous solution has been presented recently.<sup>56</sup>

### 3.2. $\text{Y}(\text{ClO}_4)_3$ and $\text{Y}(\text{CF}_3\text{SO}_3)_3$ solutions in water and heavy water

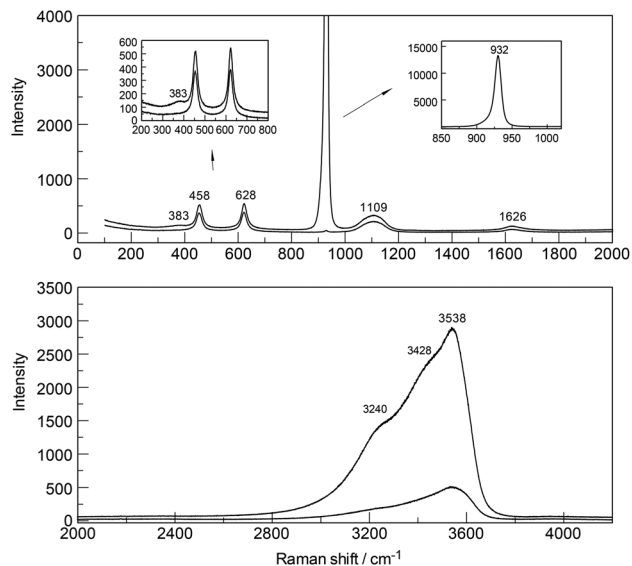
**$\text{Y}(\text{ClO}_4)_3$  solution spectra.** An overview Raman spectrum of a  $1.28\text{ mol L}^{-1}$   $\text{Y}(\text{ClO}_4)_3$  solution ( $R_w = 37.7$ ) is presented in Fig. 2 and additionally the Raman spectrum of a  $0.256\text{ mol L}^{-1}$  solution ( $R_w = 211$ ) in the terahertz frequency range in Fig. S1.† The perchlorate ion has been chosen as a counterion because it is known as a non-complex ion which is only weakly hydrated. A high frequency band at  $3538\text{ cm}^{-1}$  (fwhh =  $90\text{ cm}^{-1}$ ) is observed in  $\text{Y}(\text{ClO}_4)_3$  solutions which is attributed to an O–H band weakly hydrated perchlorate ion¶ (Fig. 2, lower panel). A concentration profile of  $\text{Y}(\text{ClO}_4)_3$  solutions in comparison with the OH stretching profile of neat water is given in Fig. S2.† The decoupled O–H oscillator of HDO for a  $2.559\text{ mol L}^{-1}$   $\text{Y}(\text{ClO}_4)_3$  solution appears at  $3563\text{ cm}^{-1}$  and Raman profiles of the polarized, depolarized and isotropic scattering are given in Fig. S3.† For a detailed discussion on the influence of  $\text{ClO}_4^-$  on the stretching band of water in, for instance,  $\text{Ca}(\text{ClO}_4)_2(\text{aq})$  see ref. 24. It is noteworthy to mention that the stretching band of  $\text{O}-\text{H}\cdots\text{OClO}_3^-$  is slightly cation dependent which is caused by their different charge to radius ratios (polarizing power). In  $\text{Y}(\text{ClO}_4)_3(\text{aq})$ , the band appears at  $3538\text{ cm}^{-1}$ , slightly lower than in  $\text{Ca}(\text{ClO}_4)_2(\text{aq})$  where it shows at  $3550\text{ cm}^{-1}$ .<sup>24</sup> The  $\nu$  O–D $\cdots\text{OClO}_3^-$  band in solutions of  $\text{Y}(\text{ClO}_4)_3/\text{D}_2\text{O}$  solution appears at  $2583\text{ cm}^{-1}$  with the Raman spectrum given in Fig. S4.†

The  $\text{ClO}_4^-$  ion ( $T_d$  symmetry) has nine vibrational degrees of freedom and its internal vibrations span the representation  $\Gamma_{\text{vib}}(T_d) = a_1(\text{Ra}) + e(\text{Ra}) + 2f_2(\text{Ra}, \text{i.r.})$ . All four n.m.'s are Raman active, but in i.r. only the  $f_2$  modes are active. The Raman and infrared spectra of  $\text{ClO}_4^-(\text{aq})$  are well characterized<sup>24–26</sup> and therefore shall be only, briefly, discussed. In dilute solution, the symmetric Cl–O stretch,  $\nu_1(a_1)$

§ The vibrational duration for the Y–O breathing mode is 0.09 ps. Approximately  $\sim 5.6 \times 10^5$  vibrations occur before the cluster experiences a water exchange.

¶ In addition to the stretching mode  $\nu(\text{O}-\text{H}\cdots\text{ClO}_4^-)$  at  $3538\text{ cm}^{-1}$  a very weak, broad mode appears in the terahertz region at  $\sim 170\text{ cm}^{-1}$  in  $\text{Y}(\text{ClO}_4)_3$  solutions ( $R_{\text{iso}}$ ) as very broad and very weak. This mode has an equivalent in pure water at  $\sim 175\text{ cm}^{-1}$  where it is moderately intense and slightly polarized (restricted translational mode of the H-bonded water molecules (O $\cdots$ O–H)). In concentrated  $\text{Y}(\text{ClO}_4)_3$  solutions other H-bonds are important, namely  $\text{OH}\cdots\text{ClO}_4^-$  and the intensity of the band due to  $\text{HOH}\cdots\text{ClO}_4^-$  is extremely weak in the isotropic Raman scattering.<sup>24,49,50</sup>

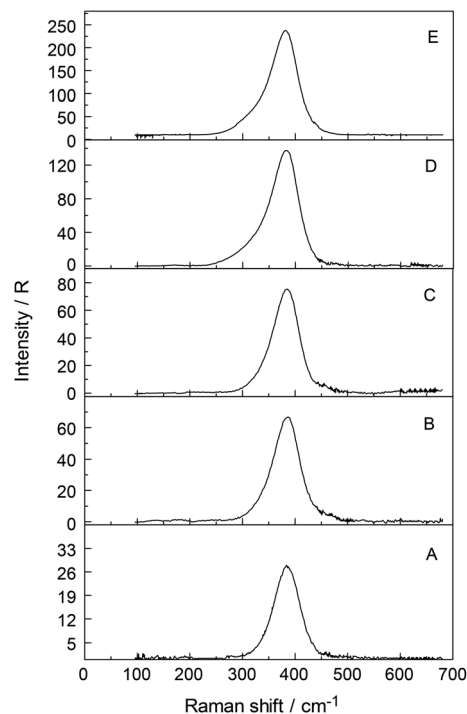




**Fig. 2** Overview Raman spectrum (polarized and depolarized) of a  $1.28 \text{ mol L}^{-1}$   $\text{Y}(\text{ClO}_4)_3$  solution ( $R_w = 37.7$ ). Upper panel: bands of  $\text{ClO}_4^-$ (aq) and the water deformation mode at  $1626 \text{ cm}^{-1}$ . The inset at the LHS shows spectra in the terahertz frequency range in greater detail. The inset at the RHS shows the  $\nu_1(a_1)$   $\text{ClO}_4^-$  band at full detail. Lower panel: OH-stretching band of water and the O–H...O\* band of the weakly H-bonded water,  $\text{ClO}_4^- \cdots \text{H}_2\text{O}$  at  $3538 \text{ cm}^{-1}$ . The peak positions of the O–H water bands are given at  $3240$  and  $3428 \text{ cm}^{-1}$ .

$\text{ClO}_4^-$  appears at  $931.5 \text{ cm}^{-1}$ , is totally polarized ( $\rho = 0.005$ ) and has a band width equal to  $7.1 \text{ cm}^{-1}$ . The antisymmetric stretch,  $\nu_3(f_2)$   $\text{ClO}_4^-$  centred at  $1105 \text{ cm}^{-1}$  and the deformation modes  $\nu_4(f_2)$   $\text{ClO}_4^-$  at  $629 \text{ cm}^{-1}$  and  $\nu_2(e)$   $\text{ClO}_4^-$  at  $458 \text{ cm}^{-1}$  are depolarized. In a  $\text{Y}(\text{ClO}_4)_3$  solution at  $0.256 \text{ mol L}^{-1}$ , the  $\nu_1(a_1)$   $\text{ClO}_4^-$  band, the strongest Raman band, appears at  $931.8 \text{ cm}^{-1}$  (fwhh at  $7.4 \text{ cm}^{-1}$ ), shifts to  $934.5 \text{ cm}^{-1}$  and broadens considerably (fwhh =  $13.1 \text{ cm}^{-1}$ ) in a solution of  $2.559 \text{ mol L}^{-1}$ . At the same time, the antisymmetric stretch,  $\nu_3(f_2)$   $\text{ClO}_4^-$  shifts to slightly higher wavenumbers and broadens. The concentration behavior of the  $\text{ClO}_4^-$  modes in a similar system,  $\text{La}(\text{ClO}_4)_3(\text{aq})$ , is given in ref. 25.

The Raman spectra of  $\text{Y}(\text{ClO}_4)_3(\text{aq})$  reveal, in addition to the perchlorate-bands, weak bands in the terahertz frequency region in the  $R_{VV}$  orientation which will be discussed further below (Fig. 2, upper panel). In the isotropic scattering profile, a band appears at  $384 \text{ cm}^{-1}$  but does not exist in  $\text{NaClO}_4(\text{aq})$  or  $\text{HClO}_4(\text{aq})$ . The band must therefore stem from vibrations connected to the  $\text{YO}_8$  skeleton. This strongly polarized band is assigned to the symmetric stretching mode, the breathing mode of the  $[\text{Y}(\text{OH}_2)_8]^{3+}$  cluster. In a fairly dilute  $\text{Y}(\text{ClO}_4)_3$  solution at  $0.256 \text{ mol L}^{-1}$  the band appears symmetrical with a fwhh =  $50 \text{ cm}^{-1}$  (Fig. S1†). With increasing  $\text{Y}(\text{ClO}_4)_3$  concentration, it widens and shifts to slightly lower wavenumbers. In a concentrated solution at  $2.559 \text{ mol L}^{-1}$ , the breathing mode,  $\nu_1\text{YO}_8$  of the  $[\text{Y}(\text{OH}_2)_8]^{3+}$  cluster appears at  $382 \text{ cm}^{-1}$ . The concentration profiles of the isotropic breathing mode,  $\text{YO}_8$  is



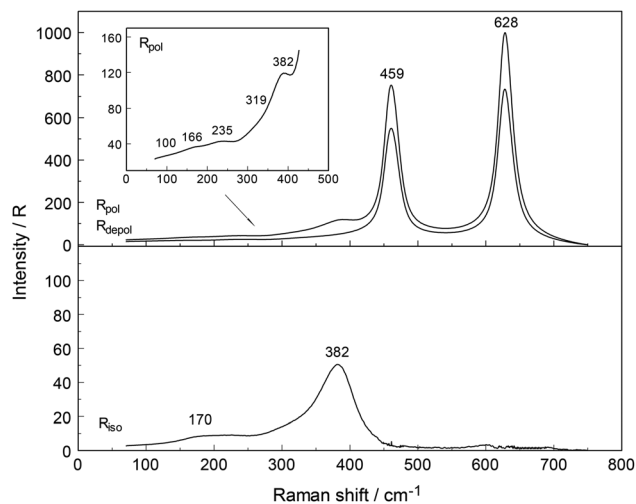
**Fig. 3** Concentration plot of isotropic Raman spectra ( $R$ -format) of five  $\text{Y}(\text{ClO}_4)_3$  solutions. From bottom to top: (A)  $0.256 \text{ mol L}^{-1}$  ( $R_w = 211.0$ ), (B)  $0.640 \text{ mol L}^{-1}$  ( $R_w = 81.4$ ), (C)  $0.853 \text{ mol L}^{-1}$  ( $R_w = 59.3$ ), (D)  $1.280 \text{ mol L}^{-1}$  ( $R_w = 37.7$ ) and (E)  $2.559 \text{ mol L}^{-1}$  ( $R_w = 15.7$ ). Note, that the peak position of the  $\text{YO}_8$  breathing mode at  $384 \text{ cm}^{-1}$  for a  $0.256 \text{ mol L}^{-1}$  solution shifts only slightly to lower wavenumbers at  $382 \text{ cm}^{-1}$  for a  $2.559 \text{ mol L}^{-1}$   $\text{Y}(\text{ClO}_4)_3$  solution. At the same time, the band broadens and a shoulder at  $336 \text{ cm}^{-1}$  appears for the two most concentrated solutions.

shown in Fig. 3. The integrated band intensity of this  $\nu_1\text{YO}_8$  mode, depending on the  $\text{Y}(\text{ClO}_4)_3$  solute concentration, plots as a straight line and the linear function:  $A_{384} = 1331.2 \cdot C_0$  (coefficient of determination,  $R^2 = 0.997$ ) with  $A_{384}$  the integrated band intensity of  $\nu_1\text{YO}_8$  and  $C_0$  the stoichiometric  $\text{Y}(\text{ClO}_4)_3$  concentration. Replacing water with heavy water leads to an isotope shift to lower wavenumbers by a factor of  $\sim 0.948$  in  $\text{Y}(\text{ClO}_4)_3(\text{D}_2\text{O})$ . The effect of deuteration on the  $\text{YO}_8$  breathing mode was measured in  $\text{Y}(\text{ClO}_4)_3\text{-D}_2\text{O}$  solutions and a band at  $365 \text{ cm}^{-1}$  observed. The theoretical shift of  $\nu_1$  on deuteration ( $\text{H}_2\text{O}/\text{D}_2\text{O}$  considered as point masses) is given according to:

$$\begin{aligned} \nu'_1 &= \nu_1 [m(\text{H}_2\text{O})/m(\text{D}_2\text{O})]^{1/2} = (384 \text{ cm}^{-1}) \cdot 1.054 \\ &= 364.2 \text{ cm}^{-1}. \end{aligned} \quad (5)$$

Relative intensity measurements confirm that the scattering intensity of the  $\nu_1\text{Y-O}$  mode is very weak with the scattering coefficient,  $S_h = 0.0380$ . The  $S_h$  values, defined as the  $R$ -corrected relative scattering efficiency of the M–O bands, were published for a variety of stretching modes of hexa-aqua metal ions in solution.<sup>24,25,27,28</sup> The  $\nu_1$  breathing mode for





**Fig. 4** Raman scattering profiles ( $R_{VV}$  and  $R_{VH}$ ) of a 2.559 mol L<sup>-1</sup>  $Y(ClO_4)_3$  solution ( $R_w = 15.7$ ). Upper panel: polarized and depolarized scattering profiles dominated by the  $ClO_4^-(aq)$  deformation bands at 459 cm<sup>-1</sup> and 628 cm<sup>-1</sup>. The inset shows the very weak, depolarized scattering contributions at 100, 166, 235, 319 cm<sup>-1</sup> and the strongly polarized band 382 cm<sup>-1</sup> in the polarized scattering ( $R_{VV} = 45\alpha^2 + 4\gamma^2$ ). Lower panel: isotropic scattering profile ( $R_{iso}$ ) showing the breathing mode,  $\nu_1 YO_8$  and the weak and broad restricted translational band at ~170 cm<sup>-1</sup>.

$[La(H_2O)_9]^{3+}$  at 343 cm<sup>-1</sup> (ref. 26) also possesses a small relative intensity of 0.025. Both ions,  $Y^{3+}$  and  $La^{3+}$ , have a low polarizability and are classified as hard cations according to the HSAB concept of Pearson.<sup>57</sup>

In addition to the breathing mode of the  $[Y(OH_2)_8]^{3+}$  cluster, four other modes appear at 100.5, 166, 233.5 and 319.5 cm<sup>-1</sup> in the anisotropic scattering (Fig. 4). These weak, broad modes stem from the  $YO_8$  skeleton fundamentals of the  $[Y(OH_2)_8]^{3+}$  and break the symmetry of the  $YO_8$  skeleton and therefore appear only in the anisotropic scattering but not in the isotropic profile. These depolarized modes were also observed slightly down-shifted in  $Y(ClO_4)_3(D_2O)$  which is caused by the isotope effect going from  $[Y(OH_2)_8]^{3+}$  to  $[Y(OD_2)_8]^{3+}$ . In  $[Y(OD_2)_8]^{3+}(D_2O)$  these bands appear at 90, 143, 221, and 302.5 cm<sup>-1</sup>. The isotope effect on the coordinated heavy water modes was calculated according to eqn (5), however,  $\nu_1$  was substituted with  $\nu_i$  (where index  $i$  denotes the frequency of the depolarized  $YO_8$  modes). Table 3 shows the summarized band parameters of the five observed skeleton modes of  $YO_8$  in water and heavy water. From these Raman spectroscopic results, it follows directly that the  $Y^{3+}$  hydration shell cannot constitute a hexa-hydrate with  $T_h$  symmetry which has been, for instance, characterized for  $[Al(OH_2)_6]^{3+}(aq)$ .<sup>43,58</sup> Group theoretical considerations expect only three skeleton modes in Raman; one of which should be totally polarized (breathing mode for the  $AlO_6$  skeleton) and the remaining two depolarized. All of these bands were detected in the Raman spectrum of an  $Al(ClO_4)_3$  solution with the symmetric stretching mode of  $[Al(OH_2)_6]^{3+}$  at 525 cm<sup>-1</sup>

**Table 3** The Raman data of the  $YO_8$  skeleton modes of  $[Y(H_2O)_8]^{3+}(aq)$  and  $[Y(D_2O)_8]^{3+}(D_2O)$  taken from an aqueous 2.559 mol L<sup>-1</sup>  $Y(ClO_4)_3$  solution and a 2.30 mol L<sup>-1</sup>  $Y(ClO_4)_3$  solution in heavy water

$[Y(H_2O)_8]^{3+}$			$[Y(D_2O)_8]^{3+}$		
Peak position/cm <sup>-1</sup>	Band area	FWHM/cm <sup>-1</sup>	Peak position/cm <sup>-1</sup>	Band area	FWHM/cm <sup>-1</sup>
100.5 (dp)	78	50	90 (dp)	33.5	76
166 (dp)	696	87.5	143 (dp)	138	69.8
233.5 (dp)	570	63	221 (dp)	189	63
319.5 (dp)	331	67	302.5 (dp)	131	53
382 (pp)	3410	58	365 (pp)	2050	53

dp = depolarized mode; pp strongly polarized.

strongly polarized and the other two at 438 cm<sup>-1</sup> and 332 cm<sup>-1</sup> depolarized.<sup>43,58</sup>

Although the perchlorate ion was chosen as the counter ion because it is known as a non-complexing anion, penetration into the first hydration sphere of the  $Y^{3+}$  seems plausible in the most concentrated  $Y(ClO_4)_3(aq)$ . In the  $Y(ClO_4)_3(aq)$  at 2.559 mol L<sup>-1</sup> the mole ratio solute to water is 16.3. This water content is enough to completely hydrate the  $Y^{3+}$  ion with 8.3 water molecules remaining. It is clear that in these concentrated solutions solvent – separated ion pair formation is simply forced on  $Y^{3+}$  because of the lack of water. At such a concentration state the outer-sphere ion pairs,  $[Y(OH_2)_8]^{3+} \cdot ClO_4^-$ , may exist in equilibrium with contact ion pairs ( $Y^{3+} \cdot ClO_4^-$ ). These ion pairs may explain the slight concentration dependence of the peak position, the shoulder at 336 cm<sup>-1</sup> mentioned previously and the broadening of the  $\nu_1 YO_8$  band. In a 0.256 mol L<sup>-1</sup>  $Y(ClO_4)_3$  solution, however, the  $\nu_1 YO_8$  band occurs as a symmetrical band at 384 cm<sup>-1</sup> and a FWHM at ~50 cm<sup>-1</sup>. Furthermore, to rule out a hydrolysis effect, ternary solutions  $Y(ClO_4)_3/HClO_4/H_2O$  were studied.  $Y(ClO_4)_3$  solution at 2.160 mol L<sup>-1</sup> plus 1.518 mol L<sup>-1</sup>  $HClO_4$  and a more dilute one at 1.080 mol L<sup>-1</sup>  $Y(ClO_4)_3$  plus 0.759 mol L<sup>-1</sup>  $HClO_4$  were measured in the terahertz frequency range in order to check the influence of the hydrolysis of  $Y^{3+}(aq)$ . Isotropic bands at 382.5 and 381.5 cm<sup>-1</sup> appeared with a 15% larger band width than those in  $Y(ClO_4)_3(aq)$  without additional  $HClO_4$ . This result shows that the hydrolysis of  $Y^{3+}$  cannot be the reason for the variation of the band parameters such as peak position and FWHM of the isotropic Y–O mode and reinforces the assumption of contact-ion-pair formation in the most concentrated solutions.

The DFT frequency of the  $\nu_1 YO_8$  for  $[Y(H_2O)_8]^{3+}$  imbedded in a polarizable dielectric continuum simulating the bulk water phase was calculated at 372 cm<sup>-1</sup> in satisfactory agreement with the measured value (Table 3) and in contrast to the breathing mode for the cluster in the gas phase at 336.5 cm<sup>-1</sup>. Imbedding the  $[Y(H_2O)_8]^{3+}$  species in a PC to simulate the bulk water is necessary to achieve acceptable agreement with the experimental frequencies. The DFT frequency of the  $\nu_1 YO_8$  mode for  $[Y(D_2O)_8]^{3+}$  imbedded in a PC was calculated at



351  $\text{cm}^{-1}$  and in satisfactory agreement with the measured value at 365  $\text{cm}^{-1}$  (Table 3). DFT frequencies for the whole  $[\text{Y}(\text{H}_2\text{O})_8]^{3+}$  cluster which includes  $\text{YO}_8$  skeletal, librational and internal water modes are given in Table S3 ESI.† The Y–O bond distance of the  $[\text{Y}(\text{H}_2\text{O})_8]^{3+}$  is 2.354 Å in good agreement with the experimental structural data (Table 1).

Similar cluster calculations on  $\text{Y}^{3+}$  with 6 water molecules surrounded by a polarizable dielectric continuum lead to a stable cluster geometry  $[\text{Y}(\text{H}_2\text{O})_6]^{3+}$  which possesses  $T_h$  symmetry. The  $\text{Y}^{3+}$ -hexa-hydrate has a much shorter Y–O bond distance at 2.28 Å. The DFT frequency for the breathing mode,  $\nu_1\text{YO}_6$  at 408  $\text{cm}^{-1}$  is 7% higher than the experimental one. These results on the  $[\text{Y}(\text{H}_2\text{O})_6]^{3+}$  cluster show that the hexa-hydrate can be ruled out as a valid cluster geometry for  $\text{Y}^{3+}$  in solution. The  $\nu_1\text{YO}_6$  frequency, geometrical parameters and the electronic energy of the cluster  $[\text{Y}(\text{H}_2\text{O})_6]^{3+}$  with a solvation sphere, modelled with a PC and for comparison with a gas phase cluster (no bulk-sphere taken into account) are given in Table S3.† To reiterate, the DFT results for  $[\text{Y}(\text{H}_2\text{O})_8]^{3+}$  are in better agreement with the experimental data than for  $[\text{Y}(\text{H}_2\text{O})_6]^{3+}$ .

The Raman spectroscopic analysis clearly shows that in dilute  $\text{Y}(\text{ClO}_4)_3(\text{aq})$  a mode appears at 384  $\text{cm}^{-1}$  (fwhh = 50  $\text{cm}^{-1}$ ) which represents the breathing mode of the  $\text{YO}_8$  skeleton. However, four additional weak and broad bands, depolarized in character, could be characterized in concentrated  $\text{Y}(\text{ClO}_4)_3(\text{aq})$ . The five bands observed in  $\text{Y}(\text{ClO}_4)_3(\text{aq})$  show that the  $\text{Y}^{3+}$  cannot form a hexa-hydrate in aqueous solution. In concentrated  $\text{Y}(\text{ClO}_4)_3(\text{aq}) > 1.5 \text{ mol L}^{-1}$ , outer-sphere ion pair formation is observed indicated by the slight shift of the  $\nu_1\text{YO}_8$  mode, an asymmetry at 336  $\text{cm}^{-1}$ . DFT simulations support the existence of the  $[\text{Y}(\text{H}_2\text{O})_8]^{3+}$  cluster and the calculated breathing mode of the cluster is in satisfactory agreement with the measured one.

### 3.2.2 $\text{Y}^{3+}$ -trifluoromethanesulfonate in aqueous solution.

In  $\text{Y}(\text{CF}_3\text{SO}_3)_3(\text{aq})$  the Y–O band is slightly overlapped with a polarized triflate band at 319  $\text{cm}^{-1}$  and appears at  $\sim 384 \text{ cm}^{-1}$ . The Raman spectrum is shown in Fig. S5.† A band separation resulted in two bands with the first band component at 319  $\text{cm}^{-1}$  and the second band at 384  $\text{cm}^{-1}$  (fwhh = 48  $\text{cm}^{-1}$ ). The first band, a polarized band, stems from  $\text{CF}_3\text{SO}_3^-(\text{aq})$  but the second band is the  $\text{YO}_8$  breathing mode of  $[\text{Y}(\text{H}_2\text{O})_8]^{3+}$ . The triflate in aqueous solution acts as a non-complexing anion and is suited therefore for studying metal ion hydration. Band parameters and assignments of  $\text{CF}_3\text{SO}_3^-(\text{aq})$  modes are given in Table S4.†

### 3.3. $\text{YCl}_3(\text{aq})$

An overview Raman spectrum of a 3.212  $\text{mol L}^{-1}$   $\text{YCl}_3$  solution ( $R_w = 15.37$ ) is presented in Fig. 5 and 6 from 100–4200  $\text{cm}^{-1}$ . Additionally, concentration plots of four  $\text{YCl}_3(\text{aq})$  solution spectra from 2.378 to 0.479  $\text{mol L}^{-1}$  are presented in the low frequency region of the spectrum (50–1100  $\text{cm}^{-1}$ ) in Fig. S6† and the O–H stretching region of the solvent, water, in Fig. S7† (2500–4200  $\text{cm}^{-1}$ ). The broad bands in Fig. 5 in the polarized scattering at 189  $\text{cm}^{-1}$ , which is overlapped with a component

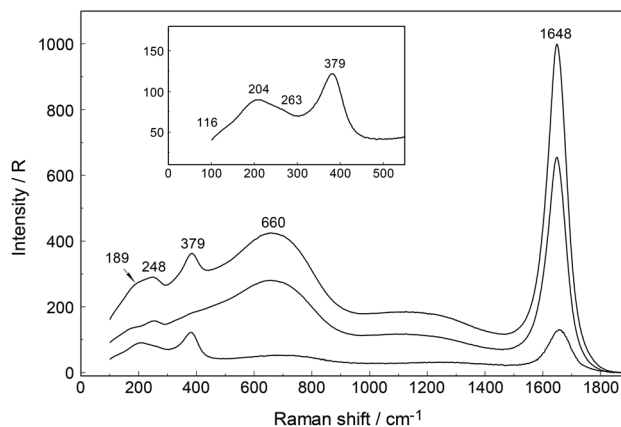


Fig. 5 Raman scattering spectra (*R*-format) of a 3.212  $\text{mol L}^{-1}$   $\text{YCl}_3$  solution. The two top curves are the polarized and depolarized scattering profiles and the lower curve represents the isotropic scattering. The Y–O breathing mode to 379  $\text{cm}^{-1}$  is slightly downshifted compared to the one in  $\text{Y}(\text{ClO}_4)_3(\text{aq})$  at 384  $\text{cm}^{-1}$  which is caused by the penetration of  $\text{Cl}^-$  into the first hydration sphere, forming a species. In the polarized scattering profile, the mode at 248  $\text{cm}^{-1}$  is due to an anisotropic  $[\text{Y}(\text{OH}_2)_{8-n}\text{Cl}_n]^{3-n}$  skeleton vibration and the broad overlapped band at 189  $\text{cm}^{-1}$  to the restricted translation of water/ $\text{Cl}^-(\text{aq})$ . The extremely broad mode at 660  $\text{cm}^{-1}$  is due to the librational water band. The band at 1648  $\text{cm}^{-1}$  is due to the deformation mode of the solvent, water. The inset shows the isotropic Raman spectrum in the terahertz region in greater detail. The mode at 204  $\text{cm}^{-1}$  is due to the restricted translational band, O–H...O/ $\text{Cl}^-$  of water/ $\text{Cl}^-(\text{aq})$  and the broad feature 263  $\text{cm}^{-1}$  is assigned to a  $\nu \text{Y}^{3+}-\text{Cl}^-$  mode.

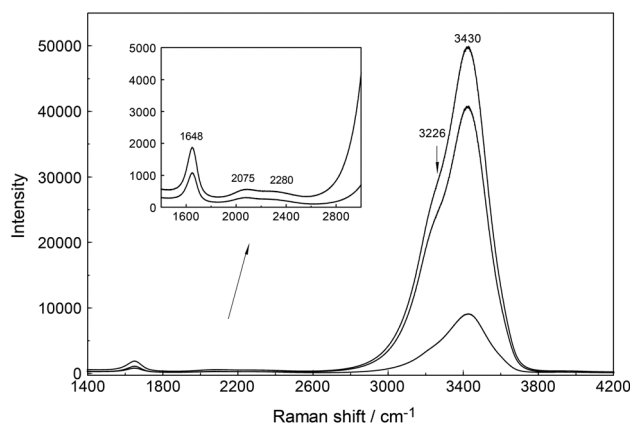


Fig. 6 Raman scattering spectrum (polarized, isotropic (darker line) and depolarized scattering profiles) of a 3.212  $\text{mol L}^{-1}$   $\text{YCl}_3$  solution from 1400–4200  $\text{cm}^{-1}$ . The inset (only polarized and depolarized scattering) gives the deformation mode at 1648  $\text{cm}^{-1}$  and its combination band, which is split into two components at 2075 and 2280  $\text{cm}^{-1}$ , of the solvent, water, in greater detail. The O–H stretching band shows two band components at 3226  $\text{cm}^{-1}$  and 3430  $\text{cm}^{-1}$ .

at 248  $\text{cm}^{-1}$  and at 660  $\text{cm}^{-1}$  are caused by the solute, water. The broad band at 189  $\text{cm}^{-1}$  represents the restricted translation and the band at 660  $\text{cm}^{-1}$  librations and a concentration plot in this wavenumber region for four  $\text{YCl}_3$  solutions from



2.378 to 0.479 mol L<sup>-1</sup> is given in Fig. S6.† The deformation band of water appears at 1648 cm<sup>-1</sup> in the 3.212 mol L<sup>-1</sup> YCl<sub>3</sub> solution and the O–H profile shows peaks at 3228 cm<sup>-1</sup> and 3430 cm<sup>-1</sup> (Fig. 6). Scattering profiles for the same four YCl<sub>3</sub> solutions in the water O–H stretching region at the high frequency range from 2500–4200 cm<sup>-1</sup> showing the O–H stretching profiles are given Fig. S7.† The influence of the solute YCl<sub>3</sub> on the restricted translation, librations, the H<sub>2</sub>O deformation mode and O–H stretching band (Fig. S6 and S7†) with increasing YCl<sub>3</sub> concentration is discussed for a similar system, CaCl<sub>2</sub>(aq) in greater detail.<sup>24</sup> The similarity of both spectral profiles of CaCl<sub>2</sub>(aq) and YCl<sub>3</sub>(aq) in the O–H stretching region reinforces two facts: one that the O–H stretching profile is mostly influenced by anions, in our case Cl<sup>-</sup> and second that Cl<sup>-</sup> forms H-bonds of the type O–H...Cl<sup>-</sup> almost as strong as the ones between water molecules (O–H...O) in neat water.<sup>24</sup> This stands in contrast to the influence of ClO<sub>4</sub><sup>-</sup> on the O–H stretching band of water which forms very weak H-bonds with the solvent as mentioned in section 3.1.

Focusing further on the terahertz frequency region, the Y–O stretching mode in this solution appears at 379 cm<sup>-1</sup> and is down shifted compared to the unassociated cluster which occurs at 384 cm<sup>-1</sup>. In addition to the very broad isotropic component at 202 cm<sup>-1</sup>, mentioned above, a broad shoulder appears at ~263 cm<sup>-1</sup> and this new isotropic component must stem from a Y<sup>3+</sup>–Cl<sup>-</sup> stretching mode. This finding is clear evidence that Cl<sup>-</sup> has penetrated into the first hydration shell of Y<sup>3+</sup> forming a [Y(OH<sub>2</sub>)<sub>8-n</sub>Cl<sub>n</sub>]<sup>+3-n</sup> (*n* = 1, possibly 2). With dilution, the Y–O stretching mode shifts to higher wavenumbers from 379 cm<sup>-1</sup> for a 3.212 mol L<sup>-1</sup> solution (*R<sub>w</sub>* = 15.4) (Fig. 5) to 384 cm<sup>-1</sup> obtained in a 0.479 mol L<sup>-1</sup> solution (*R<sub>w</sub>* = 113.82) (see dilution plot of four YCl<sub>3</sub> spectra from 2.378 to 0.479 mol L<sup>-1</sup> in Fig. S6†). This fact shows that with dilution of the concentrated solution, the chloro-complex formation disappears rapidly and extrapolation of our Raman data shows that in YCl<sub>3</sub>(aq) < 0.2 mol L<sup>-1</sup> the Y<sup>3+</sup> cation is fully hydrated. Additionally, the intensity of the band of ν<sub>1</sub>YO<sub>8</sub> as a function of concentration does not increase linearly, which would be expected if the octa-hydrated Y<sup>3+</sup> species remained stable, but curves toward smaller intensities at concentrated solutions. This shows that chloro-complexes must have formed in higher concentrated solutions at the expense of the fully hydrated Y<sup>3+</sup>, [Y(H<sub>2</sub>O)<sub>8</sub>]<sup>3+</sup> (Fig. S8†).

To further verify chloro-complex formation in YCl<sub>3</sub>(aq), addition of excess HCl was investigated. Isotropic spectra of YCl<sub>3</sub>–HCl solutions at a fixed concentration of YCl<sub>3</sub> at 2.03 mol L<sup>-1</sup> with 0, 1.0 and 4.0 mol L<sup>-1</sup> HCl added are shown in Fig. 7. The isotropic band for YCl<sub>3</sub>(aq) without added HCl is at 383 cm<sup>-1</sup>, shifts to 380 cm<sup>-1</sup> with 1.0 mol L<sup>-1</sup> HCl added and to 376 cm<sup>-1</sup> with 4.0 mol L<sup>-1</sup> additional HCl. The decreasing peak position of the ν<sub>1</sub>YO<sub>8</sub> band with increasing HCl concentration reflects the rise in the concentration of the Y<sup>3+</sup>–chloro-complex, [Y(OH<sub>2</sub>)<sub>8-n</sub>Cl<sub>n</sub>]<sup>+3-n</sup> (*n* = 1, 2). Fig. 8 presents a difference spectrum of YCl<sub>3</sub>(aq) at 2.03 mol L<sup>-1</sup> plus 4.0 mol L<sup>-1</sup> HCl(aq) from which the isotropic scattering profile of a 4 mol L<sup>-1</sup> HCl(aq) was subtracted and reveals broad bands at

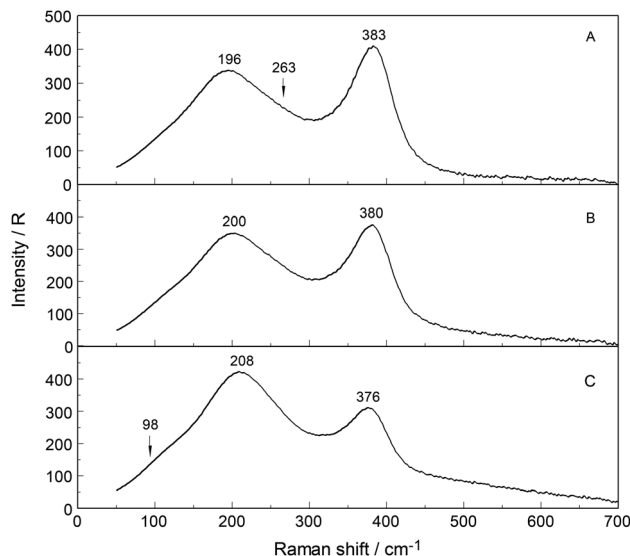


Fig. 7 Isotropic Raman spectra of a 2.13 mol L<sup>-1</sup> YCl<sub>3</sub> solution and two additional solutions where HCl is added: (A) 2.03 mol L<sup>-1</sup> YCl<sub>3</sub> without HCl; (B) 2.13 mol L<sup>-1</sup> YCl<sub>3</sub> + 1.13 mol L<sup>-1</sup> HCl and (C) 2.13 mol L<sup>-1</sup> YCl<sub>3</sub> + 3.97 mol L<sup>-1</sup> HCl. The broad shoulder at 263 cm<sup>-1</sup> in (A) increases in intensity in solutions B and C and may be assigned to Y<sup>3+</sup>–Cl<sup>-</sup> stretch.

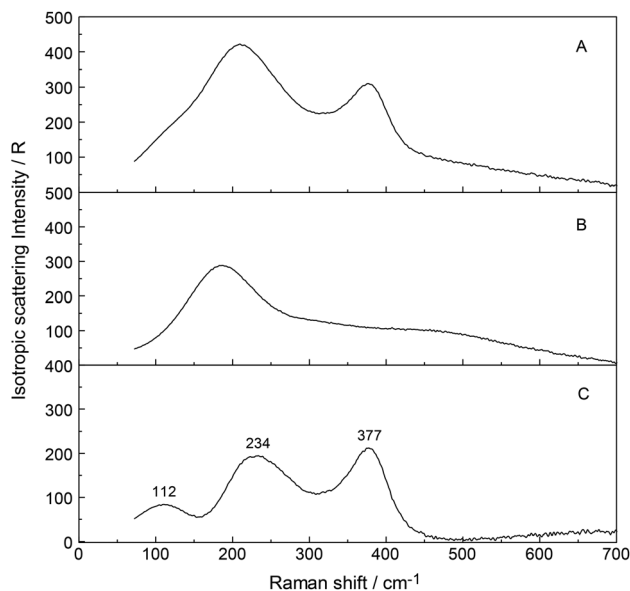
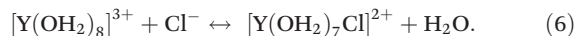


Fig. 8 Difference Raman spectrum (trace in panel C) of the isotropic scattering profile of a 2.13 mol L<sup>-1</sup> YCl<sub>3</sub>(aq) plus 3.97 mol L<sup>-1</sup> HCl (trace in panel A) from which an isotropic profile of HCl(aq) at 3.98 mol L<sup>-1</sup> (trace in panel B) was subtracted. Panel C: the band at 377 cm<sup>-1</sup> stems from the Y–O mode of the complex, [Y(OH<sub>2</sub>)<sub>8-n</sub>Cl<sub>n</sub>]<sup>+3-n</sup> (*n* = 1, 2) and the broad mode at 234 with a shoulder at 263 cm<sup>-1</sup> and a band at 112 cm<sup>-1</sup> are due to Y<sup>3+</sup>–Cl<sup>-</sup> vibrations of the chloro-complex species.

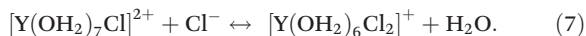
326 cm<sup>-1</sup>, at 228 cm<sup>-1</sup> and a small scattering contribution at 102 cm<sup>-1</sup>. Clearly chloro-complexes are formed in these solutions. The formation of the chloro-complex increases with an



increase in  $\text{Cl}^-$  concentration and the first equilibrium steps according to the eqn (6) may be formulated:



Results of anion exchange experiments of metal ions in aqueous  $\text{HCl}(\text{aq})$  including  $\text{Y}^{3+}$  showed that yttrium has a negligible adsorption.<sup>59</sup> Therefore, higher  $\text{Y}^{3+}$ -chloro-complexes (complex anions) with  $n > 3$  may be ruled out. The formation of a second complex cation, the di-chloro-complex according to eqn (7) may be possible:



The estimated value of the  $\log \beta_1$  for eqn (5) equal to  $\sim 0.1$  reveals the weak nature of the chloro-complex in  $\text{YCl}_3(\text{aq})$  at 23 °C. Thermodynamic data on  $\text{YCl}_3(\text{aq})$  confirm the weak nature of the complex/complexes and equilibrium constants for reaction 6 may be found in ref. 60. The existence of a weak chloro-complex species in  $\text{LaCl}_3(\text{aq})$  using Raman spectroscopy in the terahertz region was presented recently.<sup>26</sup> In the most concentrated  $\text{YCl}_3$  solution, the mole ratio solute to water is 1 to 15.4 which means that there are not enough water molecules to form a complete second hydration sphere around all ions forcing outer-shell ion pairing. The chloride ions penetrate the flexible hydration shell of  $\text{Y}^{3+}$  into the first hydration shell, while in  $\text{LaCl}_3(\text{aq})$  weak chloro-complex formations occur,<sup>26</sup> in  $\text{AlCl}_3$  solutions, however, even in very concentrated ones,  $\text{Cl}^-$  does not penetrate into the first hydration shell of  $\text{Al}^{3+}$ .<sup>43,58</sup> The hydration shell of  $[\text{Al}(\text{OH}_2)_6]^{3+}$  is quite inert. Further experimental support for chloride penetrating into the first hydration shell of  $\text{Y}^{3+}$  and formation of a chloro-complex stems from a recent combined neutron scattering and X-ray scattering study in which information from EXAFS were incorporated<sup>20</sup> into their applied analytical data treatment. This high quality structural study<sup>21</sup> on a 1.0 mol  $\text{kg}^{-1}$   $\text{YCl}_3(\text{aq})$  showed that  $\text{Y}^{3+}$  is hydrated by seven water molecules and one chloride ion, forming an inner-sphere ion complex in which the water molecules maintain angular configurations consistent with a square antiprismatic configuration. In an earlier EXAFS study on  $\text{YCl}_3(\text{aq})$  and  $\text{YCl}_3(\text{aq})$  plus an excess of  $\text{LiCl}$ , it was also demonstrated that  $\text{Cl}^-$  leads to chloro-complex formation in concentrated  $\text{YCl}_3$  solutions.<sup>13</sup>

To summarize, the  $[\text{Y}(\text{OH}_2)_{8-n}\text{Cl}_n]^{3-n}$  modes in chloride solutions could be detected and formation of weak chloro-complexes with  $\text{Y}^{3+}$  were detected. In dilute solutions ( $c < 0.2 \text{ mol L}^{-1}$ ) the chloro-complex species disappeared upon dilution and  $[\text{Y}(\text{OH}_2)_8]^{3+}(\text{aq})$  and  $\text{Cl}^-(\text{aq})$  are formed. The chloro-complex formation in concentrated solutions may be one reason for the data scatter for Y–O bond distance and coordination numbers presented for  $\text{Y}^{3+}(\text{aq})$  and this fact was highlighted recently.<sup>21</sup>

### 3.4. $\text{Y}(\text{NO}_3)_3(\text{aq})$

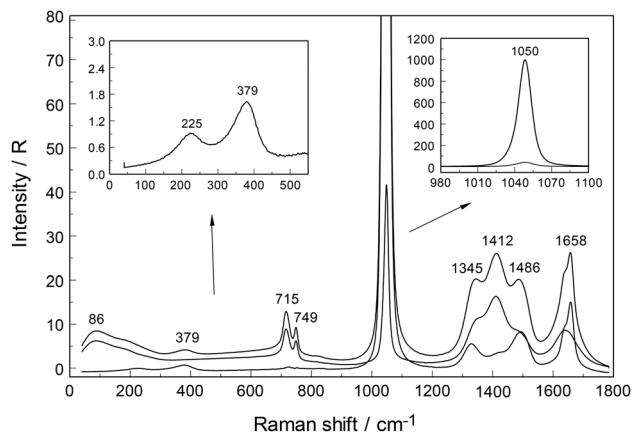
When nitrate replaces water in the first coordination sphere of a cation, marked changes occur in the spectrum of the ligated nitrate, so that it is possible to differentiate between the

modes of the ligated and the unligated nitrate. Nitrate-complex formation has been observed for a variety of divalent and trivalent metals in solutions.<sup>24–28</sup> The modes of the unligated nitrate, the fully hydrated nitrate,  $\text{NO}_3^-(\text{aq})$ , were measured recently<sup>24–26</sup> and for a 0.409 mol  $\text{L}^{-1}$   $\text{NaNO}_3$  solution ( $R_W = 134.1$ ) the Raman spectrum is given in ref. 26 together with the vibrational spectroscopic data of the bands and their assignments. Nitrate-complex formation is not only characterized by the ligated  $\text{NO}_3^-$  but also by the fact that the M–O symmetric stretch of the metal ions (M = metal ion) show two bands, a band of the fully hydrated cation and a band of the partially hydrated metal ion. A ligand mode M–L (L =  $\text{NO}_3^-$ ) should appear at low frequencies as well.

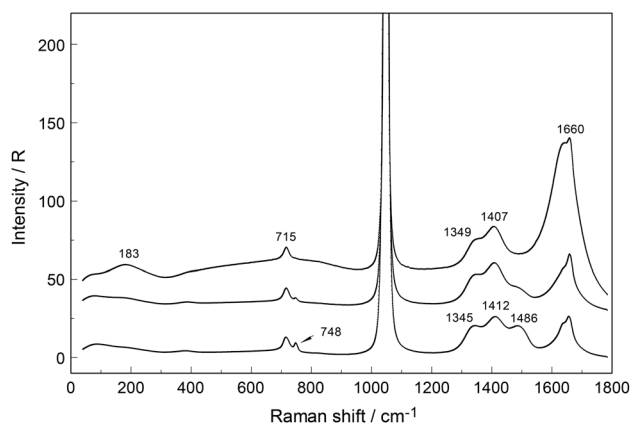
A brief summary for the vibrational data on  $\text{NO}_3^-(\text{aq})$  shall be presented before discussing the spectroscopic features in  $\text{Y}(\text{NO}_3)_3(\text{aq})$ . The “free”  $\text{NO}_3^-$  anion possesses  $D_{3h}$  symmetry and four modes should be observed (two doubly degenerate). The n.m.’s span the representation  $\Gamma_{\text{vib}}(D_{3h}) = a'_1(\text{Ra}) + a''_2(\text{i.r.}) + 2e'(\text{Ra, i.r.})$ . The  $\nu_1(a'_1)$  symmetric stretching mode N–O is Raman active but forbidden in infrared, while the  $e'$  modes,  $\nu_3$  (N–O antisymmetric stretch) and  $\nu_4$  (bending mode) are Raman and infrared active. The out-of plane deformation mode with the character  $a''_2$  is only infrared active. In  $\text{NO}_3^-(\text{aq})$ , the polarized Raman mode at 1047.4  $\text{cm}^{-1}$  is the strongest band in Raman scattering and appears quite narrow with a fwhh = 6.55  $\text{cm}^{-1}$ . This band is assigned to the symmetric N–O stretch vibration,  $\nu_1(a'_1)$ . Its depolarization degree at 0.034 is quite low and confirms that it represents a symmetrical normal mode. The mode  $\nu_3(e')$ , the asymmetric N–O stretching mode which is depolarized and relatively weak appears not as a single band but as two band components at 1347 and 1408  $\text{cm}^{-1}$  and appears as a doublet even in very dilute solutions of  $\text{NaNO}_3(\text{aq})$ . Asymmetric hydration of the nitrate anion in aqueous solution explains the double band (*cf.* for instance<sup>24,60</sup>). The depolarized mode  $\nu_4(e')$  at 716  $\text{cm}^{-1}$  is active in Raman and infrared and is much weaker than the symmetric stretching mode  $\nu_1(a'_1)$ . The infrared active mode,  $\nu_2(a''_2)$  occurs at 830  $\text{cm}^{-1}$  and its overtone  $2 \times \nu_2$  at 1660  $\text{cm}^{-1}$  is Raman active ( $a'_1$ ) and appears polarized.

An overview Raman spectrum (*R-format*) of a 2.035 mol  $\text{L}^{-1}$   $\text{Y}(\text{NO}_3)_3$  solution ranging from 40–1800  $\text{cm}^{-1}$  is presented in Fig. 9. A concentration series of polarized Raman spectra of three  $\text{Y}(\text{NO}_3)_3$  solutions at 2.035 mol  $\text{L}^{-1}$  ( $R_W = 23.04$ ), 1.036 mol  $\text{L}^{-1}$  ( $R_W = 49.20$ ) and 0.198 mol  $\text{L}^{-1}$  ( $R_W = 257.9$ ) from 100 to 1800  $\text{cm}^{-1}$  are presented in Fig. 10. A comparison of Raman spectra of a solution with 2.035 mol  $\text{L}^{-1}$   $\text{Y}(\text{NO}_3)_3$  with a solution at 0.198 mol  $\text{L}^{-1}$  in the low frequency range from 45–900  $\text{cm}^{-1}$  is detailed in Fig. S9.† Additionally, in Fig. S10† the same concentrations are compared in the high frequency region from 800–1800  $\text{cm}^{-1}$  including the  $\nu_3(e')$  anti-symmetric stretching region and  $2 \nu_2$  overtone. In these spectra, the nitrate split into bands of free, hydrated nitrate,  $\text{NO}_3^-$  free and nitrate bound,  $\text{NO}_3^-$  bound to  $\text{Y}^{3+}$ . This is a result of the fact that nitrate penetrates into the first hydration sphere forming inner-sphere complexes. The Raman spectra of





**Fig. 9** Raman spectrum of a 2.035 mol L<sup>-1</sup> ( $R_W = 23.04$ ) Y(NO<sub>3</sub>)<sub>3</sub> solution from 45–1800 cm<sup>-1</sup>. The curves for  $R_{\text{pol}}$  and  $R_{\text{depol}}$  scattering are shown on top of  $R_{\text{iso}}$  (darker, dotted line). The inset at the LHS shows the isotropic scattering at the low wavenumber range while the inset at the RHS depicts the NO<sub>3</sub><sup>-</sup>(aq) mode at 1050 cm<sup>-1</sup> at its full intensity scale.



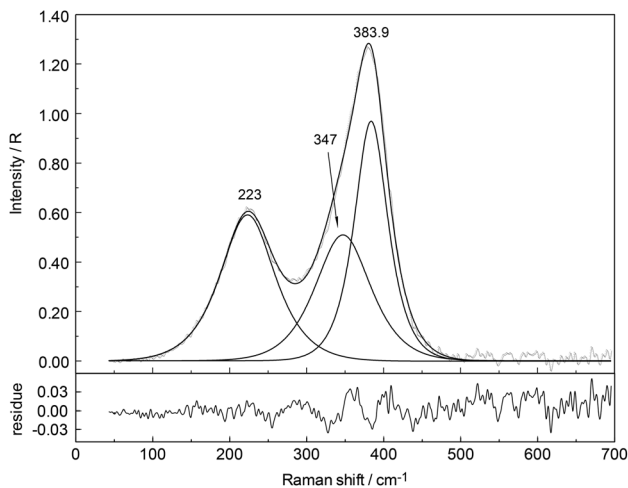
**Fig. 10** Raman spectra ( $R$ -polarized) of three Y(NO<sub>3</sub>)<sub>3</sub> solutions from bottom to top: at 2.035, 1.036 and 0.198 mol L<sup>-1</sup> solute concentrations. The Raman bands in the low frequency range from 40–900 cm<sup>-1</sup> at the highest and lowest solution concentration (2.035 and 0.198 mol L<sup>-1</sup>) are given in greater detail in Fig. S9† (panel (A): 2.035 and (B): 0.198 mol L<sup>-1</sup>). Note, that the  $\nu_1$  N–O stretching mode at  $\sim 1047$  cm<sup>-1</sup> is presented at its full scale in insets of Fig. S10† (panel (A): 2.035 and (B): 0.198 mol L<sup>-1</sup>) for both concentrations including the bands between 1200 and 1800 cm<sup>-1</sup>.

Y(NO<sub>3</sub>)<sub>3</sub>(aq) are, therefore, more complex than the ones for NaNO<sub>3</sub>(aq) resulting in bands of “free” nitrate and bound nitrate. The Raman spectrum of the concentrated Y(NO<sub>3</sub>)<sub>3</sub> solution, at 2.035 mol L<sup>-1</sup>, may illustrate this (Fig. 9). The first evidence of the ligated nitrate is the split of the  $\nu_4(e')$  NO<sub>3</sub><sup>-</sup> bending mode into bands at 715 cm<sup>-1</sup> (fwhh = 21 cm<sup>-1</sup>), at 724.5 cm<sup>-1</sup> (fwhh = 18.3 cm<sup>-1</sup>) and 748 cm<sup>-1</sup> (fwhh = 13.5 cm<sup>-1</sup>). The band at 715 cm<sup>-1</sup> represents the NO<sub>3</sub><sup>-</sup> bending mode of “free” NO<sub>3</sub><sup>-</sup>(aq) and the bands at 724.5 cm<sup>-1</sup>

and 748 cm<sup>-1</sup> represent the bending modes of the bound nitrate. Furthermore, a very weak and broad band at  $\sim 826$  cm<sup>-1</sup>, normally Raman forbidden  $\nu_2(a''_2)$ , appears in the concentrated Y(NO<sub>3</sub>)<sub>3</sub> solution (Fig. 9). The  $\nu_1$  N–O symmetric stretching band appears broadened (fwhh = 12.2 cm<sup>-1</sup>) and slightly shifted to higher wavenumbers at 1049.3 cm<sup>-1</sup> compared with the N–O stretching band in dilute NaNO<sub>3</sub>(aq) solutions. A moderately weak shoulder containing  $\sim 11\%$  of the whole band contour at lower wavenumbers is also visible at 1037 cm<sup>-1</sup> (fwhh = 21 cm<sup>-1</sup>). The antisymmetric stretching mode,  $\nu_3(e')$  broadens and the split of the two band components mentioned earlier widens considerably. Additional isotropic band contributions of the N–O antisymmetric stretch appear at 1328 and 1470 cm<sup>-1</sup> and this is shown in Fig. 9 and S10.† Finally, the Raman active overtone  $2\nu_2$ , which is broadened, appears at 1658 cm<sup>-1</sup>. All these features appear in concentrated Y(NO<sub>3</sub>)<sub>3</sub>(aq) solutions and are clear indications that NO<sub>3</sub><sup>-</sup> penetrated into the first hydration sphere of Y<sup>3+</sup>. With dilution the bands of the bound nitrate disappear rapidly and are vanished in dilute solutions (Fig. 10). It is noteworthy to mention that Cabaco *et al.*<sup>16</sup> could not detect inner-sphere nitrate-complexes in a concentrated Y(NO<sub>3</sub>)<sub>3</sub> at 2.89 mol L<sup>-1</sup> using XRD analysis and Raman spectroscopy (no  $R$ -normalized Raman spectra have been used).

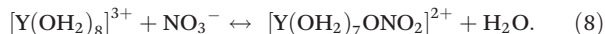
In the aqueous Y(NO<sub>3</sub>)<sub>3</sub>(aq), the weak symmetric stretching mode Y–O at 384 cm<sup>-1</sup> shows a dependence on Y(NO<sub>3</sub>)<sub>3</sub> concentration. With an increase in Y(NO<sub>3</sub>)<sub>3</sub> concentration the band shifts to lower wavenumbers, namely from 384 cm<sup>-1</sup> in dilute solutions to 379 cm<sup>-1</sup> in a 2.035 mol L<sup>-1</sup> solution and the band broadens as well with increasing concentration. For quantitative purposes, the broad  $\nu_1$ Y–O band was fitted with two Gauss–Lorentz bands resulting in a component at 384 cm<sup>-1</sup> (fwhh = 51.6 cm<sup>-1</sup>) indicative of the octa-aqua yttrium<sup>3+</sup> species while the second band component at 347 cm<sup>-1</sup> (fwhh = 84 cm<sup>-1</sup>) is due to the hydrated yttrium-nitrate complex, [Y(OH<sub>2</sub>)<sub>8-n</sub>(NO<sub>3</sub>)<sub>n</sub>]<sup>3-n</sup>. The results of the curve fit are given in Fig. 11. The ligand mode of the nitrate-complex appears as a polarized band at 223 cm<sup>-1</sup>. In the concentrated solution, 45% of Y<sup>3+</sup> exists in the form of a nitrate-complex. With dilution the nitrate-complex formation diminishes quickly and in the dilute solution at 0.198 mol L<sup>-1</sup> only  $\sim 10\%$  of Y<sup>3+</sup> is coordinated by nitrate. Upon further dilution the nitrate-complex disappears and from extrapolations of  $\alpha$ -values (the degree of nitrate-complex formation) as a function of solution concentration, it becomes obvious that in solutions  $< 0.1$  mol L<sup>-1</sup> 99% of the Y<sup>3+</sup> is fully hydrated and the nitrate-complex with only  $\sim 1\%$  becomes insignificant. The nitrate is tentatively assumed to be monodentate, although in solid state compounds of hydrated Y(NO<sub>3</sub>)<sub>3</sub> such as Y(OH<sub>2</sub>)<sub>4</sub>(NO<sub>3</sub>)<sub>3</sub>·2H<sub>2</sub>O nitrate occurs in bidentate fashion.<sup>61</sup> It may be deduced from the work by Dobler *et al.*<sup>62</sup> investigating Ln(III) cations interacting with NO<sub>3</sub><sup>-</sup>, that in aqueous solution with enough water to fully hydrate the trivalent cation Ln(III) (Ln = Lu<sup>3+</sup>) nitrate acts as a monodentate ligand. A second shell of water molecules stabilizes the first water sphere *via* hydrogen bond formation including the nitrate. Therefore,





**Fig. 11** Isotropic Raman spectrum (*R*-format) of 2.035 mol L<sup>-1</sup> Y(NO<sub>3</sub>)<sub>3</sub> solution in the terahertz frequency range (40–700 cm<sup>-1</sup>). Given are the measured spectrum (darker line), the sum curve and the component bands of the fit at 223 cm<sup>-1</sup> (fwhh = 165 cm<sup>-1</sup>; A<sub>1</sub> = 58.02), 347 cm<sup>-1</sup> (fwhh = 165 cm<sup>-1</sup>; A<sub>2</sub> = 49.6) and 384 cm<sup>-1</sup> (fwhh = 51.6 cm<sup>-1</sup>; A<sub>3</sub> = 59.3). The index *i* denotes the integrated band intensities of the band intensities A<sub>*i*</sub> (*i* = 1–3). Note the residue curve as the difference between measured curve and sum curve is given underneath.

the formation of the nitrate-complex with Y<sup>3+</sup> may be expressed by eqn (8):



and in a possible second step the formation of a di-nitrate complex in concentrated solutions (9):



An estimate of the log β<sub>1</sub> value at ~0.1 reveals the weak nature of the nitrate-complex in Y(NO<sub>3</sub>)<sub>3</sub>(aq) at 23 °C. Thermodynamic data on the weak nitrate complex formation may be found in ref. 63. Ultrasound absorption measurements were carried out on yttrium nitrate solutions applying a one-step mechanism and revealed the formation of a mono-nitrate complex.<sup>64</sup> The behaviour of the Y<sup>3+</sup>-nitrate-complex solution is comparable to the nitrate-complex formation in La(NO<sub>3</sub>)<sub>3</sub>(aq)<sup>26</sup> where the complex formation is apparent albeit weak. In contrast to the weak nitrate-complex formation in aqueous Y(NO<sub>3</sub>)<sub>3</sub>, in Al(NO<sub>3</sub>)<sub>3</sub> solutions from dilute to high concentrations, the aluminium(III) hexahydrate, [Al(OH<sub>2</sub>)<sub>6</sub>]<sup>3+</sup> exists as a stable cluster. The Raman scattering bands, especially the breathing mode at 525 cm<sup>-1</sup>, indicate the existence of the hexahydrate.<sup>58</sup> In concentrated solutions outer-sphere ion pairs, [Al(OH<sub>2</sub>)<sub>6</sub>]<sup>3+</sup>·NO<sub>3</sub><sup>-</sup> are formed. However, nitrate does not penetrate the first hydration shell of Al<sup>3+</sup> indicated by the unchanged Raman signature of the AlO<sub>6</sub> of [Al(OH<sub>2</sub>)<sub>6</sub>]<sup>3+</sup>.<sup>58</sup>

## 4. Conclusions

Raman spectra of aqueous Y<sup>3+</sup> perchlorate, triflate, chloride and nitrate solutions were measured over a broad concentration range (0.198 mol L<sup>-1</sup>–3.252 mol L<sup>-1</sup>). The terahertz frequency range has been measured as well as spectra in the O–H stretching region. The weak, polarized mode at 384 cm<sup>-1</sup> (fwhh = 50 cm<sup>-1</sup>) was assigned to ν<sub>1</sub>Y–O of the YO<sub>8</sub> skeleton. In deuterated Y(ClO<sub>4</sub>)<sub>3</sub> solution, a mode at 365 cm<sup>-1</sup> was assigned to the breathing mode, ν<sub>1</sub>Y–O of the [Y(OD<sub>2</sub>)<sub>8</sub>]<sup>3+</sup>. Raman spectroscopic data suggest that the [Y(OH<sub>2</sub>)<sub>8</sub>]<sup>3+</sup> ion is thermodynamically stable in dilute perchlorate and triflate solutions. But inner-sphere complexes could not be detected, spectroscopically. Outer-sphere ion pairs of the type [Y(OH<sub>2</sub>)<sub>8</sub>]<sup>3+</sup>·ClO<sub>4</sub><sup>-</sup> and possibly inner-sphere ion pairs are formed in concentrated Y(ClO<sub>4</sub>)<sub>3</sub>(aq). DFT frequency calculations of a [Y(OH<sub>2</sub>)<sub>8</sub>]<sup>3+</sup> imbedded in a polarizable dielectric continuum gave a ν<sub>1</sub> Y–O equal to 372 cm<sup>-1</sup> in fair agreement with the experiment. Bond distances and angles of the [Y(OH<sub>2</sub>)<sub>8</sub>]<sup>3+</sup> imbedded in a polarizable dielectric continuum were also presented. The symmetry of the octa-aqua complex is S<sub>8</sub> while the YO<sub>8</sub> skeleton has D<sub>4d</sub> symmetry.

In YCl<sub>3</sub> solutions, Cl<sup>-</sup> penetrates the first hydration sphere of Y<sup>3+</sup>(aq) and chloro-complexes are formed. However, the chloro-complexes disappear rapidly upon dilution and at a concentration <0.2 mol L<sup>-1</sup> the chloro-complexes have almost vanished. This Raman spectroscopic finding is substantiated from recent results applying neutron – and X-ray scattering as well as EXAFS.<sup>12,16</sup>

In concentrated Y(NO<sub>3</sub>)<sub>3</sub> solutions, NO<sub>3</sub><sup>-</sup> penetrates the first hydration sphere of Y<sup>3+</sup> and a nitrate-complex was characterized; the nitrate-complex disappears fairly rapidly upon dilution and in solutions <0.1 mol L<sup>-1</sup> no nitrate-complexes could be observed.

## Appendix A

The binding energy for the cluster in the gas phase consisting of Y<sup>3+</sup> ion with 8 water molecules in the first sphere was calculated according to eqn (10):

$$\Delta E_e = E_e[\text{Y}(\text{OH}_2)_8(\text{g})]^{3+} - E_e[\text{Y}^{3+}(\text{g})] - 8 \cdot E_e[\text{OH}_2(\text{g})]. \quad (10)$$

This equation corresponds to a gas-phase reaction at *T* = 0 K of isolated molecules with stationary nuclei, but thermochemical measurements are carried out with vibrating molecules usually at 298 K. Comparison of the theoretical with experimental data, therefore, requires correction for the translational, rotational and vibrational energy. For one mole molecules of an ideal gas, one obtains the enthalpy:

$$H(T) = E_e + E_t(T) + E_r(T) + E_v(T) + RT. \quad (11)$$

Here, *E<sub>e</sub>* stands for the electronic energy, *E<sub>t</sub>*(*T*) the translational energy, *E<sub>r</sub>*(*T*) the rotational energy, and *E<sub>v</sub>*(*T*) = *Nh* ∑ ν<sub>*i*</sub> (1/2 + 1/(e<sup>hν<sub>*i*</sub>/k*T*</sup> – 1)) is the thermal vibrational <sup>*i*</sup> energy. The gas-phase hydration enthalpy



$\Delta H_{\text{hyd(g)}}(T)$  is then obtained with an equation similar to eqn (10). Using results of our DFT calculations and harmonic frequencies, we obtain for the cluster  $[\text{Y}(\text{OH}_2)_8]^{3+}$  the standard hydration enthalpy  $\Delta H_{\text{hyd(g)}}(298) = -2541 \text{ kJ mol}^{-1}$  in the gas phase. The estimation of the hydration enthalpy in the liquid state,  $\Delta H_{\text{hyd(l)}}$  for  $[\text{Y}(\text{OH}_2)_6]^{2+}$  requires consideration of additional contributions. According to a Born-Haber cycle it follows:

$$\Delta H_{\text{hyd(l)}} \approx \Delta H_{\text{hyd(g)}} + \Delta H_{\text{vap}} + \Delta H_{\text{solv}}. \quad (12)$$

Here,  $\Delta H_{\text{vap}}$  is the heat of water vaporization<sup>65</sup> and  $\Delta H_{\text{solv}}$  means the solvation energy resulting from the transfer of the gas phase cluster to the liquid state. The solvation enthalpy of the cluster can be estimated with the Polarized Continuum Model by placing the  $[\text{Y}(\text{OH}_2)_6]^{3+}$  gas phase cluster in a polarizable dielectricum and so taking implicitly into account the bulk water and comparing with the naked cluster. From the difference of the calculated enthalpies, the solvation energy  $\Delta H_{\text{solv}}(298)$  results in  $-1762 \text{ kJ mol}^{-1}$ . Taking into account the vaporization heat of the 8 water molecules, we obtain for the hydration enthalpy  $\Delta H_{\text{hyd(l)}}(298) = -3951 \text{ kJ mol}^{-1}$ .

Experimental values for the standard molar hydration enthalpy  $\Delta H_{\text{hyd(l)}}(298)$  of  $\text{Y}^{3+}$  in the liquid state are:  $-3710 \text{ kJ mol}^{-1}$ ,<sup>37</sup>  $-3599 \text{ kJ mol}^{-1}$ ,<sup>38</sup>  $-3733 \text{ kJ mol}^{-1}$ ,<sup>39</sup>  $-3583 \text{ kJ mol}^{-1}$ ,<sup>40</sup>  $-3590 \text{ kJ mol}^{-1}$ ,<sup>41</sup>  $-3620 \text{ kJ mol}^{-1}$ .<sup>42</sup> The correspondence with the theoretical values is satisfactory in consideration of the simple set of basis functions that has been used.

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