1. Introduction

Even though the invention of bright blue light emitting diodes (LEDs) by Nakamura et al. nearly dates back a quarter of a century, LEDs still have a vast impact on advances in lighting technology. Meanwhile, LEDs have replaced more and more conventional light sources such as incandescent and discharge lamps. This is because of the fact that LEDs provide many benefits compared to thermal and gas discharge light sources, such as longer lifetimes, higher wall plug efficiency and higher colour rendering. Nowadays, most of the commercially available white light emitting LEDs comprise a blue emitting [In,Ga]N chip pumping a green-yellow emitting phosphor, e.g. (Y,Gd)3Al5O12:Ce3+. This setup provides a high luminous efficacy due to emission in the green spectral range. Unfortunately, these lamps suffer from high colour temperature and low colour rendering index due to the lack of emission in the red spectral range. Therefore, these light sources are unpopular for domestic lighting. To overcome these drawbacks, one approach is to use a phosphor blend comprising a blue, green, and red phosphor, which is excited by an ultraviolet emitting LED. Using this concept, cold and warm white emitting LEDs with excellent colour points can be realized. However, these packages undergo a loss in blue emission due to re-absorption by the green and red phosphors. For this reason, many research groups are developing single phase white emitting phosphors to convert UV radiation into white light.

One approach to realize a white emitting phosphor is to use the ion couple Eu2+ and Mn2+. The broad emission bands in the blue and red spectral range of Eu2+ and Mn2+ in many host structures complement each other to white light due to additive colour mixing. Furthermore, Eu2+ usually exhibits a broad excitation band in the UV range due to the spin and parity allowed [Xe]4f7–[Ar]3d5 excitation transitions of Mn2+ via interconfigurational electric-dipole transition. Therefore, Eu2+ is well appropriated for pumping by UV LEDs. In addition the blue emission band of Eu2+ is also suitable for sensitizing the spin and parity forbidden [Ar]3d5–[Ar]3d5 excitation transitions of Mn2+ via energy transfer (ET). To investigate the photoluminescence (PL) properties as well as the ET from Eu2+ to Mn2+, a series of co-doped BaCa2Si3O9:Eu2+,Mn2+ samples with various Mn2+ concentrations were synthesized. BaCa2Si3O9 was described for the first time in the work of Eskola in 1922. Later on, in 1965 Alfors et al. investigated the mineral walstromite. Based on their results on optical properties and X-ray powder diffraction data they stated that BaCa2Si3O9 is identical to walstromite. Glasser et al. reported on the crystal structure of synthetic BaCa2Si3O9 using photographic X-ray diffraction data in 1968. The crystal structure derived from a single crystal analysis of BaCa2Si3O9 was firstly published by Barkley et al. in 2011.
blue emission of Eu$^{2+}$ doped BaCa$_2$Si$_3$O$_9$.\textsuperscript{11} Moreover, Gaft \textit{et al.} published an article concerning the luminescence of natural walstromite in 2013.\textsuperscript{12}

BaCa$_2$Si$_3$O$_9$ crystallizes triclinically in the space group P1. The structure of triclinic BaCa$_2$Si$_3$O$_9$ is built up of layers consisting of alternating Si$_2$O$_5$ rings. Between these layers Ba and Ca atoms are incorporated. BaCa$_2$Si$_3$O$_9$ comprises two non-equivalent Ca sites, namely Ca1 and Ca2. The Ca1 site is coordinated by 8 oxygen atoms with a mean distance of 2.545 Å. The Ca2 site is surrounded by 6 oxygen atoms with an average bond length of 2.370 Å. The Ba atoms are 8-fold coordinated with an average distance of 2.841 Å. The ionic radii of Ca for 8 and 6-fold coordination are 1.12 and 0.96 Å. Ba$^{2+}$ in 8-fold coordination is 0.96 Å. BaCa$_2$Si$_3$O$_9$ possesses a white body colour. The DR spectrum of BaCa$_2$Si$_3$O$_9$ shows a broad absorption band between 250 and 800 nm. Thus, undoped BaCa$_2$Si$_3$O$_9$ exhibits high reflectance between 250 and 800 nm. However, samples with $x > 0.1$ show an additional reflex at about 25.9° which can be assigned to SiO$_2$. This proves the successful synthesis of the investigated BaCa$_2$Si$_3$O$_9$:Eu$^{2+}$, Mn$^{2+}$ phosphors with a Mn$^{2+}$ concentration up to $x = 0.1$.

Fig. 2 shows DR spectra of undoped BaCa$_2$Si$_3$O$_9$ host material and also of Ba$_{0.95}$Eu$_{0.05}$Ca$_2$Si$_3$O$_9$ and Ba(Ca$_{0.95}$Mn$_{0.05}$)$_2$Si$_3$O$_9$. Undoped BaCa$_2$Si$_3$O$_9$ exhibits high reflectance between 250 and 800 nm. Thus, undoped BaCa$_2$Si$_3$O$_9$ possess a white body colour. The DR spectrum of Ba$_{0.95}$Eu$_{0.05}$Ca$_2$Si$_3$O$_9$ shows a broad absorption band between 250 and 450 nm due to the allowed [Xe]$4f^7$-[Xe]$4f^5$d$^5$-transition of Eu$^{2+}$. Because of the absorption band in the blue range of the electromagnetic spectrum, Ba$_{0.95}$Eu$_{0.05}$Ca$_2$Si$_3$O$_9$ exhibits a slightly yellow body colour. The DR spectrum of Ba(Ca$_{0.95}$Mn$_{0.05}$)$_2$Si$_3$O$_9$ shows absorption in the UV region between 250 and 350 nm which can be tentatively assigned to a Mn$^{2+}$ charge transfer transition.\textsuperscript{15}

The PLE spectrum as well as the PL spectrum of Ba$_{0.95}$Eu$_{0.05}$Ca$_2$Si$_3$O$_9$ is depicted in Fig. 3a. The PLE spectrum was recorded monitoring the 460 nm emission of Eu$^{2+}$ and exhibits a broad band consisting of various unresolved bands.

2. Experimental

Preparation

Ba$_{0.99}$Eu$_{0.01}$(Ca$_{1-x}$Mn$_x$)$_2$Si$_3$O$_9$ samples were synthesized via conventional high temperature solid state reaction. High purity starting materials BaCO$_3$ (Alfa Aesar, 99.8%), CaCO$_3$ (Merck KGaA, Reag. Ph. Eur.), SiO$_2$ (Merck KGaA, Ph. Eur.), Eu$_2$O$_3$ (Treibacher Industrie AG, 99.99%) and Mn$_2$O$_3$·2H$_2$O (Dr Paul Lohmann, chem. pure) were weighed in stoichiometric amounts. 1 wt% H$_3$BO$_3$ (Merck KGaA, Ph. Eur.) was added as a flux. Subsequently, the educts were ground in acetone in an agate mortar. After drying at ambient temperature, the obtained powder blends were heated at 1000 °C for 2 h in air to decompose the carbonates. Afterwards the samples were ground and finally calcined in alumina boats at 1200 °C for 12 h in reducing forming gas flow (Westfalen, 5% H$_2$, 95% N$_2$). After calcination, hard sinter bodies with a slightly yellow body colour were obtained which were subsequently ground to a fine powder.

Characterization

Phase purity was investigated using X-ray powder diffractometry (XRD). XRD patterns were recorded on a Rigaku MiniFlex II diffractometer working in Bragg–Brentano geometry using Cu K$_\alpha$ radiation. Step width and integration time were 0.02 and 1 s, respectively.

PL spectra and photoluminescence excitation (PLE) spectra were recorded on an Edinburgh Instruments FSL900 spectrometer equipped with a Xe arc lamp (450 W) and a cooled (−20 °C) single-photon counting photomultiplier (Hamamatsu R2658P). PL spectra were corrected by using a correction file obtained from a tungsten incandescent lamp certified by the National Physical Laboratory, UK.

For photoluminescence decay (PLD) measurements on Eu$^{2+}$, the spectrometer was equipped with a picosecond pulsed laser (5 mW, pulse width = 76.6 ps, $\lambda_{\text{em}} = 375$ nm). For PLD measurements on Mn$^{2+}$ a microsecond pulsed Xe lamp (100 W, pulse width = 1 µs) was attached to the spectrometer.

For temperature dependent measurements the spectrometer was equipped with a cryostat (Oxford Instruments). Liquid nitrogen was used as a cooling agent. Temperature stabilization time was 60 s and tolerance was set to ±3 K.

Diffuse reflectance (DR) spectra were recorded on an Edinburgh Instruments FS900 spectrometer equipped with a Xe arc lamp (450 W), a cooled (−20 °C) single-photon counting photomultiplier (Hamamatsu R928) as well as a Teflon-coated integration sphere. BaSO$_4$ (99.998%, Sigma-Aldrich) was used as a reflectance standard.

External quantum efficiencies $\eta_{\text{ext}}$ were determined using the approach of Kawamura \textit{et al.}\textsuperscript{14} To this end, PL spectra of the sample as well as of the excitation source were recorded in the integration sphere. From this, $\eta_{\text{ext}}$ can be calculated by the following equation:

$$
\eta_{\text{ext}} = \frac{\int I_{\text{em}}(\lambda)\,d\lambda}{\int I_{\text{ex}}(\lambda)\,d\lambda - \int I_{\text{em}}(\lambda)\,d\lambda} \quad \text{(1)}
$$

where $I_{\text{em}}(\lambda)$ is the emission intensity of the sample, $I_{\text{ex}}(\lambda)$ and $I_{\text{em}}(\lambda)$ are the intensities of the excitation source in the absence and presence of the sample.

3. Results and discussion

Collected XRD patterns of doped and also of undoped BaCa$_2$Si$_3$O$_9$ samples as well as the ICDD reference cards of BaCa$_2$Si$_3$O$_9$ and SiO$_2$ are presented in Fig. 1. The XRD patterns indicate the formation of the triclinic BaCa$_2$Si$_3$O$_9$ phase. Furthermore, with increasing doping concentrations of Eu$^{2+}$ and Mn$^{2+}$, no change in the host structure can be observed. However, samples with $x > 0.1$ show an additional reflex at about 25.9° which can be assigned to SiO$_2$. This proves the successful synthesis of the investigated BaCa$_2$Si$_3$O$_9$:Eu$^{2+}$, Mn$^{2+}$ phosphors with a Mn$^{2+}$ concentration up to $x = 0.1$.

Fig. 2 shows DR spectra of undoped BaCa$_2$Si$_3$O$_9$ host material and also of Ba$_{0.95}$Eu$_{0.05}$Ca$_2$Si$_3$O$_9$ and Ba(Ca$_{0.95}$Mn$_{0.05}$)$_2$Si$_3$O$_9$. Undoped BaCa$_2$Si$_3$O$_9$ exhibits high reflectance between 250 and 800 nm. Thus, undoped BaCa$_2$Si$_3$O$_9$ possess a white body colour. The DR spectrum of Ba$_{0.95}$Eu$_{0.05}$Ca$_2$Si$_3$O$_9$ shows a broad absorption band between 250 and 450 nm due to the allowed [Xe]$4f^7$-[Xe]$4f^5$d$^5$-transition of Eu$^{2+}$. Because of the absorption band in the blue range of the electromagnetic spectrum, Ba$_{0.95}$Eu$_{0.05}$Ca$_2$Si$_3$O$_9$ exhibits a slightly yellow body colour. The DR spectrum of Ba(Ca$_{0.95}$Mn$_{0.05}$)$_2$Si$_3$O$_9$ shows absorption in the UV region between 250 and 350 nm which can be tentatively assigned to a Mn$^{2+}$ charge transfer transition.

The PLE spectrum as well as the PL spectrum of Ba$_{0.95}$Eu$_{0.05}$Ca$_2$Si$_3$O$_9$ is depicted in Fig. 3a. The PL spectrum was recorded monitoring the 460 nm emission of Eu$^{2+}$ and exhibits a broad band consisting of various unresolved bands.
This band is due to excitation from the $[\text{Xe}]4f^7$ ground state to the $[\text{Xe}]5d^1$ multiplet of Eu$^{2+}$. The PL spectrum of Ba$_{0.99}$Eu$_{0.01}$Ca$_2$Si$_3$O$_9$ ($\lambda_{\text{ex}} = 320$ nm) shows an emission band peaking at about 444 nm with FWHM of 47 nm (2333 cm$^{-1}$). This emission originates from relaxation of the excited $[\text{Xe}]5d^1$ state to the $[\text{Xe}]4f^7$ ground state. Further, Ba$_{0.99}$Eu$_{0.01}$Ca$_2$Si$_3$O$_9$ possesses an emission band in the red region of the spectrum. The PLE spectrum of this emission is shown as a dotted line. Fig. 3b illustrates the PLE and PL spectra of Ba(Ca$_{0.95}$Mn$_{0.05}$)$_2$Si$_3$O$_9$. Monitoring the 590 nm emission of Mn$^{2+}$, the PLE spectrum of Ba(Ca$_{0.95}$Mn$_{0.05}$)$_2$Si$_3$O$_9$ shows various bands centred at 326, 348, 359, 405, 432, and 510 nm. These peaks can be assigned to transitions from the $^6A_1(6S)$ ground state to $^4T_1(4P)$, $^4E(4D)$, $^4T_2(4D)$, $^4E(4G)$, $^4A_1(4G)$, $^4T_2(4G)$, and $^4T_1(4G)$, respectively. The PL spectrum of Ba(Ca$_{0.95}$Mn$_{0.05}$)$_2$Si$_3$O$_9$ was recorded under an excitation wavelength of $\lambda_{\text{ex}} = 405$ nm and exhibits a broad band with a maximum at about 594 nm resulting from a transition from the $^4T_1(4G)$ excited state to the $^6A_1(6S)$ ground state. This observation is in accordance with the results given by Gaft et al. regarding Mn$^{2+}$ emission in natural walstromite.\textsuperscript{12} In addition, the Mn$^{2+}$ emission band comprises a tailing to the red range of the visible spectrum indicating emission from different crystallographic sites. PLE as well as PL spectra of co-doped Ba$_{0.99}$Eu$_{0.01}$(Ca$_{0.95}$Mn$_{0.05}$)$_2$Si$_3$O$_9$ are depicted in Fig. 3c. The PL spectrum of Ba$_{0.99}$Eu$_{0.01}$(Ca$_{0.95}$Mn$_{0.05}$)$_2$Si$_3$O$_9$ shows two bands peaking at about 445 and 590 nm which can be assigned to electronic transitions of Eu$^{2+}$ ($[\text{Xe}]5d^1$ to $[\text{Xe}]4f^7$) and Mn$^{2+}$ ($^4T_1(4G)$ to $^6A_1(6S)$), respectively. PLE spectra of Ba$_{0.99}$Eu$_{0.01}$(Ca$_{0.95}$Mn$_{0.05}$)$_2$Si$_3$O$_9$ were recorded, monitoring the 460 nm emission of Eu$^{2+}$ as well as the 590 nm emission of Mn$^{2+}$. These PLE spectra appear similar to the PLE of singly...
doped $\text{Ba}_{0.99}\text{Eu}_{0.01}\text{Ca}_2\text{Si}_3\text{O}_9$ monitoring the blue emission of Eu$^{2+}$. This observation strongly implies the occurrence of ET from Eu$^{2+}$ to Mn$^{2+}$.

Fig. 4 illustrates the PL spectra of the synthesized $\text{Ba}_{0.99}\text{Eu}_{0.01}(\text{Ca}_1-x\text{Mn}_x)_2\text{Si}_3\text{O}_9$ series with $x = 0, 0.005, 0.010, 0.015, 0.020, 0.050, 0.100, 0.150$, and $0.200$. As can be concluded from the spectra, with increasing Mn$^{2+}$ concentration the PL intensity of Eu$^{2+}$ decreases. This behaviour reflects the assumption provided above regarding ET from Eu$^{2+}$ to Mn$^{2+}$. The inset in Fig. 4 depicts the relative PL intensities of Eu$^{2+}$ and Mn$^{2+}$. It was found that the PL intensity of Mn$^{2+}$ increases continuously up to a Mn$^{2+}$ concentration of $x = 0.15$ where a saturation effect begins. Concentration quenching of the Mn$^{2+}$ emission was not observed for the synthesized samples.

Furthermore, PLD measurements were performed monitoring the Eu$^{2+}$ emission to investigate the ET from Eu$^{2+}$ to Mn$^{2+}$ in more detail. Fluorescence lifetimes $\tau$ of $\text{Ba}_{0.99}\text{Eu}_{0.01}(\text{Ca}_1-x\text{Mn}_x)_2\text{Si}_3\text{O}_9$ samples with increasing Mn$^{2+}$ content were determined, monitoring the 445 nm emission of Eu$^{2+}$ under an excitation wavelength of $\lambda_{\text{ex}} = 375$ nm. Fig. 5 illustrates the obtained PLD curves. The PLD curves can be best fitted with a bi-exponential function applying the following equation:

$$I = A_1e^{-t/\tau_1} + A_2e^{-t/\tau_2} \quad (2)$$

Here, $I$ is the luminescence intensity, $A_1$ and $A_2$ are parameters and $t$ is the time. The terms $\tau_1$ and $\tau_2$ are the partial lifetimes for the exponential components. The bi-exponential shape of the PLD curves originates from two different emitting centres and suggests Eu$^{2+}$ emission from two distinct crystallographic sites. This is thoroughly possible since BaCa$_2$Si$_3$O$_9$ provides two different Ca sites and one Ba site, as mentioned above. This assumption is backed by PLD measurements monitoring the emission at 415 and 495 nm which yield different luminescence lifetimes ($\tau$ at 415 nm = 602 ns, $\tau$ at 415 nm = 702 ns) (Fig. S1 in the ESI†). The average luminescence lifetimes $\tau$ of Eu$^{2+}$ in BaCa$_2$(Si$_3$O$_9$):Eu$^{2+}$,Mn$^{2+}$ can be derived using the above mentioned parameters and the following equation:

$$\tau = \frac{A_1\tau_1^2 + A_2\tau_2^2}{A_1\tau_1 + A_2\tau_2} \quad (3)$$

Emission fractions frac$_1$ and frac$_2$, partial lifetimes $\tau_1$, and $\tau_2$ and also the calculated average lifetimes are summarized in Table 1. The results show a decreasing lifetime $\tau$ of Eu$^{2+}$ with increasing Mn$^{2+}$ concentration. Since ET processes are usually faster than radiative transitions, this circumstance clearly indicates the occurrence of an ET from Eu$^{2+}$ to Mn$^{2+}$. The ET efficiency $\eta_T$ can be calculated using following equation:16

$$\eta_T = 1 - \frac{\tau_S}{\tau_{50}} \quad (4)$$

In this equation $\tau_S$ and $\tau_{50}$ are the average lifetimes of Eu$^{2+}$ in the presence and absence of Mn$^{2+}$. The inset of Fig. 5 illustrates the calculated values for $\eta_T$ for the investigated BaCa$_2$Si$_3$O$_9$:Eu$^{2+}$,Mn$^{2+}$ samples as a function of the Mn$^{2+}$ content. This shows that the ET efficiency $\eta_T$ continuously

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**Table 1** Fluorescence lifetimes $\tau$ as well as partial lifetimes $\tau_1$ and $\tau_2$ and the emission fractions frac$_1$ and frac$_2$ of Eu$^{2+}$ in $\text{Ba}_{0.99}\text{Eu}_{0.01}(\text{Ca}_1-x\text{Mn}_x)_2\text{Si}_3\text{O}_9$

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**Fig. 4** PL spectra of $\text{Ba}_{0.99}\text{Eu}_{0.01}(\text{Ca}_1-x\text{Mn}_x)_2\text{Si}_3\text{O}_9$ and integrated PL intensity in dependence of the Eu$^{2+}$ and Mn$^{2+}$ concentration (inset).

**Fig. 5** PLD curves of $\text{Ba}_{0.99}\text{Eu}_{0.01}(\text{Ca}_1-x\text{Mn}_x)_2\text{Si}_3\text{O}_9$ and ET efficiency $\eta_T$ in dependence of the Mn$^{2+}$ concentration (inset).
increases with increasing Mn$^{2+}$ content. For the highest Mn$^{2+}$ concentration with $x = 0.20$, $\eta_T$ amounts to 12% whereas the PL intensity of Eu$^{2+}$ decreases around 70%. Due to faster competitive ET processes, e.g. migration to defect sites, a significant amount of emission energy is lost before it can be transferred to the Mn$^{2+}$ ions. This behaviour increases with increasing Mn$^{2+}$ concentration.

The average distance between Eu$^{2+}$ and Mn$^{2+}$ ($R_{\text{Eu-Mn}}$) in the host material at which ET occurs can be estimated by applying the following formula published by Blasse:17

$$R_{\text{Ce-Mn}} = 2\left[\frac{3V}{4\pi xN}\right]^{\frac{1}{3}}$$ (5)

Here, $V$ is the volume of the unit cell, $x$ the concentration of Eu$^{2+}$ and Mn$^{2+}$ in the host, and $N$ is the number of available sites for the dopants in the unit cell. For BaCa$_2$Si$_3$O$_9$, $V$ and $N$ are 396.01 Å$^3$ and 6, respectively. Using this equation for $x = 0.005, 0.010, 0.015, 0.020, 0.050, 0.100, 0.150,$ and 0.200, ($R_{\text{Eu-Mn}}$) is calculated to be 20.3, 18.5, 17.1, 16.1, 12.8, 10.5, 9.2, and also 8.4 Å, respectively. The Mn$^{2+}$ concentration where the Eu$^{2+}$ PL intensity is one-half of that in the sample without Mn$^{2+}$ is called critical concentration $x_c$. Plugging in $x_c$ into formula (5), the critical distance $R_c$ can be derived. $R_c$ is defined as the distance where the probability of ET from sensitizer to activator equals the probability of radiative transition in the sensitizer. For Ba$_{0.99}$Eu$_{0.01}$(Ca$_{1-x}$Mn$_x$)$_2$Si$_3$O$_9$, $x_c$ was determined to be 0.134. From this, $R_c$ is calculated to be 9.6 Å.

To elucidate the characteristics of the ET process in Ba$_{0.99}$Eu$_{0.01}$(Ca$_{1-x}$Mn$_x$)$_2$Si$_3$O$_9$, the obtained decay curves were analysed by applying the Inokuti–Hirayama model. Assuming a uniform distribution of Eu$^{2+}$ and Mn$^{2+}$ in the host structure, and neglecting further energy migration processes besides the ET from Eu$^{2+}$ to Mn$^{2+}$, the time-dependent course of the PL intensity of Eu$^{2+}$ can be described by following equation:18

$$I(t) = I_0 \times e^{-\frac{t}{\tau_0} - \alpha \left(\frac{t}{\tau_0}\right)^2}$$ (6)

In this equation, $t$ is the time, $I(t)$ is the PL intensity after excitation, $I_0$ is the PL intensity at $t = 0$, $\tau_0$ is the intrinsic luminescence lifetime of the sensitizer in the absence of the activator, $\alpha$ is a parameter for the probability of ET. $S$ is related to the electronic multipole character of the ET. $S = 6, 8, 10$ corresponds to dipole–dipole, dipole–quadrupole, and quadrupole–quadrupole interactions, respectively. Modifying eqn (6) leads to following relation:

$$\ln\left[-\ln\left(\frac{I(t)}{I_0}\right) - \left(\frac{t}{\tau_0}\right)^2\right] \sim \ln\left(\frac{t}{\tau_0}\right)^S$$ (7)

Plotting the PLD curves using this relation yields a straight line with a slope equal to $1/S$. The obtained curves for the measured Ba$_{0.99}$Eu$_{0.01}$(Ca$_{1-x}$Mn$_x$)$_2$Si$_3$O$_9$ samples with $x = 0.005, 0.010, 0.015, 0.020, 0.050, 0.100, 0.150,$ and 0.200 are depicted in Fig. 6. The calculated $S$ values are roughly coincident with the theoretical value of $S = 8$. This result suggests dipole–quadrupole interactions as the dominant mechanism of ET from Eu$^{2+}$ to Mn$^{2+}$ in co-doped BaCa$_2$Si$_3$O$_9$:Eu$^{2+}$, Mn$^{2+}$.

This finding is quite reasonable since the electronic [Xe]4f$^7$-[Xe]4f$^6$5d$^1$-transition in Eu$^{2+}$ is allowed whereas the electronic [Ar]3d$^5$-[Ar]3d$^5$-transition in Mn$^{2+}$ is forbidden. Therefore, the critical distance $R_c$ for ET from Eu$^{2+}$ to Mn$^{2+}$ can be calculated using the spectral overlap method:17,19

$$R_c^* = 0.63 \times 10^{28} \frac{\int dE \int dE \ A(E) \ F_X(E) \ F_A(E)}{\int dE A(E)}$$ (8)

In this formula, $f_A = 10^{-10}$ and $f_X = 10^{-7}$ are the oscillator strengths of dipole and quadrupole electronic absorption transitions, respectively, for Mn$^{2+}$. The absorption cross section $Q_A$ of Mn$^{2+}$ can be expressed using the relationship $Q_A = 4.8 \times 10^{-15} f_A$ derived by Blasse. $\lambda_{\text{E}}$ is the emission wavelength of Eu$^{2+}$. $E$ is the energy of maximal spectral overlap. From this, the critical distance $R_c$ is calculated to be 8.9 Å. This value is in accordance with the one calculated using Blasse’s approach (9.6 Å).

To investigate the temperature dependence of the PL of co-doped Ba$_{0.99}$Eu$_{0.01}$(Ca$_{0.90}$Mn$_{0.10}$)$_2$Si$_3$O$_9$, PL spectra were recorded from 100 to 800 K. The obtained PL spectra are depicted in Fig. 7. The spectra demonstrate that with increasing temperature PL intensity of Eu$^{2+}$ and Mn$^{2+}$ decreases due to thermal quenching. The inset of Fig. 7 illustrates the normalized PL integrals versus their temperature. From this, activation energy $E_A$ for thermal quenching can generally be
estimated by fitting the data points by a Fermi–Dirac distribution:

\[ I(T) = I_0 \frac{I_{0,b}}{1 + B \times e^{rac{E_{a,b}}{kT}}} + (1 - A) \frac{I_{0,a}}{1 + B \times e^{rac{E_{a,a}}{kT}}} \]  

(9)

In this equation, \( I(T) \) is the luminescence intensity at a certain temperature and \( I_0 \) is the luminescence intensity at zero Kelvin, \( B \) is the quenching frequency factor, \( T \) is the temperature and \( k \) is the Boltzmann constant. However, due to an additional turning point, the present data points cannot be fitted by ordinary Fermi–Dirac distribution. Therefore, eqn (9) is expanded to a sum of two weighed Fermi–Dirac distributions:

\[ I(T) = A \frac{I_{0,a}}{1 + B \times e^{rac{E_{a,a}}{kT}}} + (1 - A) \frac{I_{0,b}}{1 + B \times e^{rac{E_{a,b}}{kT}}} \]  

(10)

Here, \( I_{0,a} \) and \( I_{0,b} \) are the PL intensities at zero Kelvin. \( A \) describes the fraction of the first term. From this, \( E_{a,a} \) and \( E_{a,b} \) were determined to be about 0.07 and 0.84 eV, respectively. Plugging in the values for \( E_{a,a} \) and \( E_{a,b} \) in eqn (11) yields \( T_{1/2,a} \) and \( T_{1/2,b} \):

\[ T_{1/2} = \frac{-E_A}{k \times \ln \left( \frac{1}{B} \right)} \]  

(11)

\( T_{1/2} \) is the temperature at which PL intensity of a luminescent centre is decreased to one-half of its maximum. For Ba_{0.99}Eu_{0.01}(Ca_{0.90}Mn_{0.10})_2Si_3O_9, \( T_{1/2,a} \) and \( T_{1/2,b} \) were calculated to be 242 and 666 K, respectively. The PL intensities originating from Eu^{2+} and Mn^{2+} were plotted separately (Fig. S2 and S3 in the ESI†). From that it can be seen that the bi-sigmoidal behaviour strongly decreases if investigating the PL intensities of Eu^{2+} solely. Due to overlapping of the red emission band the bi-sigmoidal shape does not vanish completely. To examine the origin of this double sigmoidal quenching behaviour, PL of singly doped Ba_{0.99}Eu_{0.01}Si_3O_9 was measured in the temperature range from 100 to 800 K as well (Fig. S4 in the ESI†). At low temperatures an additional emission band extending from about 600 to 750 nm arises. PLD measurements of this emission band revealed a fluorescence lifetime of about 945 ns (Fig. S5 in the ESI†). This value matches well with the decay time of Eu^{2+}. Furthermore, the obtained PLD curve shows mono-exponential decay behaviour, indicating emission from one particular crystallographic site. These Eu^{2+} ions presumably occupy the 6-fold coordinated Ca2 sites in BaCaSi_2O_4. On this small site, the crystal field splitting of the d-orbitals of Eu^{2+} is rather high because of which the lower edge of the [Xe]5d~ multiplet is moved towards the ground state. Due to relatively low emission energies in the red spectral range and consequently strong multi-phonon relaxation as well as large Stokes shift, this emission exhibits a lower quenching temperature. Furthermore, with increasing temperature a blue shift of Mn^{2+} emission can be observed. This behaviour is due to an increasing average distance between the Mn^{2+} ions and their oxygen ligands with increasing temperatures. As a consequence, the crystal field splitting of the 3d orbitals of Mn^{2+} decreases resulting in a shift of the \( ^{4}T_{1}(^4G) \rightarrow ^{6}A_{1}(^6S) \) transition to higher energies.20

To obtain more detailed information regarding the temperature dependent behaviour of Ba_{0.99}Eu_{0.01}(Ca_{0.90}Mn_{0.10})_2Si_3O_9, PLD measurements were performed from 100 to 500 K. Fig. 8 depicts the PLD curves of Ba_{0.99}Eu_{0.01}(Ca_{0.90}Mn_{0.10})_2Si_3O_9 monitoring the 445 nm emission of Eu^{2+}. The curves can be best fitted with a bi-exponential function, suggesting Eu^{2+} emission from two distinct crystallographic sites as mentioned previously. The derived fluorescence lifetimes are presented in Table 2 and show an unusual increase with increasing temperatures. This phenomenon was only reported by a few authors and is still uncommon.21,22 According to Meijerink and Blasse, this behaviour is presumably caused by thermal population of...
higher energetic 4f\(^{6-5d}\) states. Excited states in Eu\(^{2+}\) can either be (spin) octets or sextets. The sextet states are at higher energies than the octet states according to Hund’s rule. With increasing temperature the higher energetic sextet states will be populated. For these states, transition to the \(8S_7/2\) ground state is spin-forbidden resulting in lower decay rates and thus longer fluorescence lifetimes.22 Fluorescence lifetimes of Mn\(^{2+}\) emission in dependency of temperature were measured, too. The obtained PLD curves are depicted in Fig. 9 and can be well fitted with a bi-exponential function. This result is consistent with the assumption made above that Mn\(^{2+}\) is located on two different crystallographic sites. The calculated average lifetimes of Mn\(^{2+}\) are summarized in Table 2. With increasing temperature, Mn\(^{2+}\) fluorescence lifetimes decrease continuously due to an increase in non-radiative relaxation to the ground state. Therefore, it can be concluded that thermal quenching of emission in BaCa\(_2\)Si\(_3\)O\(_9\):Eu\(^{2+}\),Mn\(^{2+}\) is primarily caused by Mn\(^{2+}\) ions. As deduced from PLD curves of Mn\(^{2+}\) emission as well as from ionic radii of Ba\(^{2+}\), Ca\(^{2+}\) and Mn\(^{2+}\), it can be concluded that Mn\(^{2+}\) ions preferably occupy the two Ca sites in BaCa\(_2\)Si\(_3\)O\(_9\). Since the ionic radii of 6- and 8-fold coordinated Mn\(^{2+}\) are smaller compared to those of Ca\(^{2+}\), the excited states of Mn\(^{2+}\) can strongly be polarized. This leads to an increase in the equilibrium distance between Mn\(^{2+}\) and its oxygen ligands and therefore to a shift of the ground and excited state parabolas in the configurational coordinate diagram. Further, the crossing point of the parabolas is shifted to lower energy, and thus to a lower activation energy for thermal quenching.

To investigate the PL efficiency of the Ba\(_{0.99}\)Eu\(_{0.01}\)\((\text{Ca}_{1-x}\text{Mn}_x)\)\(_2\)Si\(_3\)O\(_9\) samples, external quantum efficiencies \(\eta_{\text{ext}}\) were measured as mentioned above. To the best of our understanding, external quantum efficiency \(\eta_{\text{ext}}\) is defined as:

\[
\eta_{\text{ext}} = \frac{N_{\text{emission}}}{N_{\text{absorption}}} \tag{12}
\]

where \(N_{\text{emission}}\) is the number of photons emitted by the phosphor and \(N_{\text{absorption}}\) is the number of photons absorbed by the phosphor. The resulting quantum efficiencies \(\eta_{\text{ext}}\) were summarized in Table 3. For the investigated samples \(\eta_{\text{ext}}\) is around 30%. The low quantum efficiency of BaCa\(_2\)Si\(_3\)O\(_9\):Eu\(^{2+}\),Mn\(^{2+}\) can be ascribed to the overlap of the blue emission band and the excitation band of the red emission of Eu\(^{2+}\). Due to ET from the blue Eu\(^{2+}\) site to the red Eu\(^{2+}\) site which is thermally quenched, \(\eta_{\text{ext}}\) decreases. According to the relevant PL spectra, Commission International de l’Eclairage 1931 (CIE) chromaticity coordinates were calculated. Fig. 10 depicts the CIE chromaticity diagram.

### Table 2. Fluorescence lifetimes \(\tau\) as well as partial lifetimes \(\tau_1\) and \(\tau_2\), and the emission fractions frac\(_1\) and frac\(_2\) of Eu\(^{2+}\) and Mn\(^{2+}\) in Ba\(_{0.99}\)Eu\(_{0.01}\)((Ca\(_{1-x}\)Mn\(_x\))\(_2\)Si\(_3\)O\(_9\) from 100 to 500 K

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**Fig. 9** PLD curves of Ba\(_{0.99}\)Eu\(_{0.01}\)((Ca\(_{1-x}\)Mn\(_x\))\(_2\)Si\(_3\)O\(_9\) at 100, 300 and 500 K monitoring the emission of Mn\(^{2+}\). Fluorescence lifetimes in dependency of temperature (inset).
Table 3  External quantum efficiencies \( \eta_{\text{ext}} \) and CIE colour coordinates of \( \text{Ba}_{0.99}\text{Eu}_{0.01}\text{(Ca}_{1-x}\text{Mn}_{x})_{2}\text{Si}_{3}\text{O}_{9} \)

| Sample \( x \) | \( \eta_{\text{ext}} \) | \( x \) | \( y \) |
|-----------|-----------------|-----------------|
| 0.000     | 0.31            | (0.151|0.243) |
| 0.005     | 0.31            | (0.163|0.053) |
| 0.010     | 0.30            | (0.170|0.060) |
| 0.015     | 0.31            | (0.182|0.073) |
| 0.020     | 0.32            | (0.190|0.080) |
| 0.050     | 0.34            | (0.224|0.112) |
| 0.100     | 0.36            | (0.260|0.146) |
| 0.150     | 0.26            | (0.325|0.210) |
| 0.200     | 0.30            | (0.354|0.240) |

Fig. 10  CIE chromaticity diagram of \( \text{Ba}_{0.99}\text{Eu}_{0.01}\text{(Ca}_{1-x}\text{Mn}_{x})_{2}\text{Si}_{3}\text{O}_{9} \) with different \( \text{Mn}^{2+} \) concentrations.

for \( \text{Ba}_{0.99}\text{Eu}_{0.01}\text{(Ca}_{1-x}\text{Mn}_{x})_{2}\text{Si}_{3}\text{O}_{9} \) with \( x = 0, 0.005, 0.010, 0.015, 0.020, 0.050, 0.100, 0.150, \) and 0.200. By increasing the \( \text{Mn}^{2+} \) concentration, the chromaticity coordinates can be shifted from blue to magenta colour tones. Due to the lack of emission in the green spectral range, \( \text{BaCa}_{2}\text{Si}_{3}\text{O}_{9}:\text{Eu}^{2+},\text{Mn}^{2+} \) has to be combined with an additional green emitting phosphor to generate white light, such as \( \text{Ba}^{2+}\text{Sr}^{2+}\text{Si}_{2}\text{O}_{4}:\text{Eu}^{2+},\text{Sr}^{2+}\text{Al}_{2}\text{O}_{2}\text{Cl}_{2}:\text{Eu}^{2+} \) or \( \text{KBaB}_{2}\text{O}_{4}:\text{Th}^{4+},\text{Eu}^{2+} \). Fig. S6† shows a simulated white emission spectrum consisting of \( \text{Ba}_{0.99}\text{Eu}_{0.01}\text{Ca}_{0.08}\text{Mn}_{0.09})_{2}\text{Si}_{3}\text{O}_{9} \) and \( \text{Ba}_{0.48}\text{Sr}_{0.41}\text{Eu}_{0.11})_{2}\text{Si}_{3}\text{O}_{9} \). The CIE 1931 colour coordinates of the spectrum are \( x = 0.327 \) and \( y = 0.333 \) which result in a correlated colour temperature (CCT) of 5745 K. The colour rendering index (CRI) \( R_{\text{a}} \) of the simulated spectrum is equal to 82. This CCT is similar to that of a phosphor-converted white LED consisting of a blue LED chip and YAG:Ce\(^{3+}\) (CCT = 5600 K) whereas the CRI is higher compared to that of this phosphor-converted LED \( (R_{\text{a}} = 71) \).

4. Conclusions

A series of \( \text{BaCa}_{2}\text{Si}_{3}\text{O}_{9}:\text{Eu}^{2+},\text{Mn}^{2+} \) powder samples with various \( \text{Mn}^{2+} \) concentrations was prepared via high temperature solid state synthesis. Excited by UV radiation, \( \text{BaCa}_{2}\text{Si}_{3}\text{O}_{9}:\text{Eu}^{2+},\text{Mn}^{2+} \) shows two emission bands located at about 444 and 594 nm originating from \( \text{Eu}^{2+} \) and \( \text{Mn}^{2+} \), respectively. It turned out that \( \text{Eu}^{2+} \) ions in \( \text{BaCa}_{2}\text{Si}_{3}\text{O}_{9}:\text{Eu}^{2+},\text{Mn}^{2+} \) occupy the 8-fold coordinated Ba and Ca1 sites as well as the 6-fold coordinated Ca2 sites. \( \text{Mn}^{2+} \) ions tend to occupy both Ca sites. These results are confirmed by PLD measurements. The highest PL intensity of \( \text{Mn}^{2+} \) was found at a \( \text{Mn}^{2+} \) concentration of \( x = 0.15 \). It was further demonstrated that ET from \( \text{Eu}^{2+} \) to \( \text{Mn}^{2+} \) in \( \text{BaCa}_{2}\text{Si}_{3}\text{O}_{9}:\text{Eu}^{2+},\text{Mn}^{2+} \) is of resonant type and occurs via dipole-quadrupole interaction. The critical distance \( R_{\text{c}} \) between \( \text{Eu}^{2+} \) and \( \text{Mn}^{2+} \) was derived by using Blasse’s concentration quenching method as well as the spectral overlap method and was calculated to be 9.6 and 8.9 Å, respectively. Temperature dependent PL measurements prove a “double” sigmoidal decrease of the PL intensity of \( \text{Eu}^{2+} \). Therefore, \( \text{BaCa}_{2}\text{Si}_{3}\text{O}_{9}:\text{Eu}^{2+},\text{Mn}^{2+} \) has two \( T_{1/2} \) values, \( T_{1/2,a} \) and \( T_{1/2,b} \), which were calculated to be 242 and 666 K, respectively. In addition to that, PLD measurements revealed an unusual increase of \( \text{Eu}^{2+} \) fluorescence lifetime, which presumably originates from thermal population of higher excited energy levels. Temperature dependent PLD measurements on the \( \text{Mn}^{2+} \) emission suggest that thermal quenching in \( \text{BaCa}_{2}\text{Si}_{3}\text{O}_{9}:\text{Eu}^{2+},\text{Mn}^{2+} \) is primarily caused by \( \text{Mn}^{2+} \) ions. CIE 1931 colour points can be tuned from the blue to the magenta colour range.

Acknowledgements

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Notes and references