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Post deposition annealing of epitaxial $\text{Ce}_{1-x}\text{Pr}_x\text{O}_{2-\delta}$ films grown on Si(111)

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In this work the structural and morphological changes of $\text{Ce}_{1-x}\text{Pr}_x\text{O}_{2-\delta}$ ($x = 0.20, 0.35$ and 0.75) films grown on Si(111) due to post deposition annealing are investigated by low energy electron diffraction combined with a spot profile analysis. The surface of the oxide films exhibit mosaics with large terraces separated by monoatomic steps. It is shown that the Ce/Pr ratio and post deposition annealing temperature can be used to tune the mosaic spread, terrace size and step height of the grains. The morphological changes are accompanied by a phase transition from a fluorite type lattice to a bixbyite structure. Furthermore, at high PDA temperatures a silicate formation via a polycrystalline intermediate state is observed.

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I. Introduction

Cerium based oxides are discussed in a variety of research fields, e.g. microelectronics,^{1–3} catalysis^{4–6} or solid state fuel cells.^{7–9} The chemical and physical requirements for the different applications vary and are strongly dependent on the oxygen vacancy concentration. For instance, on the one hand in most electronic applications perfect structures with sharp interfaces and almost no defects are required. On the other hand in catalytic applications the reactivity and selectivity are strongly dependent on the vacancy density at the near surface region. Thus, detailed knowledge of the surface structure and morphology is mandatory to build catalysts and electronic devices with optimized performance. Here, thin film systems offer the opportunity to study these properties in a highly controlled environment using surface science techniques.^{10–12} Here we use High Resolution Low Energy Electron Diffraction combined with Spot Profile Analysis (SPA-LEED) to characterize structural surface properties of mixed ceria-praseodymia thin films while their bulk properties has been studied before.¹³

Recently, Zoellner *et al.*¹³ demonstrated that epitaxial $\text{Ce}_{1-x}\text{Pr}_x\text{O}_{2-\delta}$ films can be grown on Si(111) making model studies possible. They also revealed that for low and moderate praseodymium concentration a cubic fluorite based structure is preferred while high concentrations lead to a hexagonal crystal structure. Later on it was shown that the praseodymium concentration can be used to manipulate the redox^{16,17} as well

as the magnetic¹⁸ properties of these films. For future applications a detailed analysis of the surface properties is necessary.

However, up to now no such study is available. Hence, in the following a post deposition annealing study addressing the surface structure and morphology of these films is presented.

II. Experimental setup

The $\text{Ce}_{1-x}\text{Pr}_x\text{O}_{2-\delta}$ (111) ($x = 0-1$) films are grown on Si(111) following the recipe described in ref. 13. Ultrathin praseodymia buffer layers are used to suppress oxidation of the silicon substrate. The crystalline quality as well as the Ce/Pr ratio of the three investigated samples are characterized by *ex situ* X-ray diffraction (XRD) and photoelectron spectroscopy (XPS), respectively. All films exhibit cubic structure and stoichiometries of $\text{Ce}_{1-x}\text{Pr}_x\text{O}_{2-\delta}$ with $x = 0.20, 0.35$ and 0.75 are determined (data not shown). Furthermore, X-ray reflection (XRR) revealed that the thickness of the films is $\approx 20-25$ nm (data not shown). The cubic structure of the sample with the highest praseodymium content ($x = 0.75$) is in contrast to the previous growth study.¹³ We assume that the initial hexagonal structure changes into the cubic phase due to contact with atmospheric oxygen for an elongated time comparable to results reported for pure praseodymium oxide films.^{14,15}

For the post deposition annealing (PDA) studies the samples are transferred to an ultra high vacuum chamber (base pressure 10^{-10} mbar) equipped with a SPA-LEED instrument and a plasma chamber (base pressure 10^{-7} mbar). Prior to the PDA studies the samples are exposed to an oxygen plasma for 15 min to clean their surfaces and reduce the amount of oxygen vacancies. It has been shown that rare earth oxide films reach

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the highest degree of oxidation using this procedure.^{19,20} For this purpose an *in situ* microwave plasma source (2.45 GHz) is used with the plasma parameters of 80 sccm gas flow, 0.26 mbar oxygen pressure and 360 W power. Following the plasma cleaning the samples are subsequently annealed for 30 min at different temperatures using resistive heating. After each annealing step the samples are cooled to room temperature and electron diffraction measurements are performed. The temperature is controlled with an infrared pyrometer.

III. Results

A. LEED pattern

Fig. 1 shows the electron diffraction pattern of the appearing structures of the $\text{Ce}_{0.80}\text{Pr}_{0.20}\text{O}_{2-\delta}/\text{Si}(111)$ film after plasma cleaning. For the $\text{Ce}_{0.65}\text{Pr}_{0.35}\text{O}_{2-\delta}$ and the $\text{Ce}_{0.25}\text{Pr}_{0.75}\text{O}_{2-\delta}$ similar pattern are observed (data not shown). All cleaned samples exhibit a hexagonal (1×1) pattern with a threefold intensity distribution of the first order diffraction spots (*cf.* Fig. 1(a)) which is based on the ABC layer stacking sequence of the (111) oriented cubic fluorite structure.

At higher PDA temperatures several superstructures appear (*cf.* Fig. 1 and 2) which can be attributed to ordered oxygen vacancies. The individual temperature necessary to stabilize the fully reduced bixbyite (4×4) surface structure shifts to lower

Fig. 2 Surface phases against praseodymium content. The data of the pure cerium and praseodymium oxide phases are taken from ref. 24 and 33, respectively. Two ordered intermediate phases (Ce_7O_{12} at 660 °C and $\text{Ce}_{11}\text{O}_{20}$ at 680 °C) can be found in pure cerium oxide films. The sample with the lowest Pr content shows also a weak superstructure (*cf.* Fig. 1(b)) and we assume a similar phase as observed for Ce_7O_{12} . Note, the data set of the pure cerium oxide films was obtained for a 250 nm film. Hence, the silicate formation at the surface may differ for thinner films.

values with increasing praseodymium concentration. This effect is based on the lowered activation energy for oxygen vacancy formation and is in good agreement with previous studies.^{16,21}

Fig. 1 Two-dimensional electron diffraction pattern of the appearing structures of the $\text{Ce}_{0.80}\text{Pr}_{0.20}\text{O}_{2-\delta}$ sample taken at 61.6 eV electron energy. The patterns are normalized to the (surface) Brillouin-zone (BZ) size of the oxide. (a) At low temperatures a (1×1) pattern is visible which can be attributed to a fluorite type structure. (b) A PDA treatment at 600 °C results in the formation of a very weak superstructure which vanishes at 700 °C (data not shown). (c) (4×4) Pattern attributed to the bixbyite structure appears after annealing at 750 °C. (d) At 800 °C weak streaks between the main diffraction spots appear while the intensity of the (4×4) pattern is decreased. (e) A sharp (1×1) pattern superimposed with a strong $(\sqrt{3} \times \sqrt{3})R30^\circ$ structure is observed at 850 °C due to silicide formation. Additional diffraction spots located at concentric rings are visible indicating a formation of a polycrystalline species. (f) After annealing at 1000 °C the polycrystalline rings are replaced by a strong (2×1) pattern and a very weak $(\sqrt{3} \times \sqrt{3})R30^\circ$ spots close to the first order diffraction spots.

For the sample with low praseodymium content moderate temperatures (*cf.* Fig. 1(b)) result in a very weak superstructure which vanishes at higher PDA temperatures. Several intermediate bulk phases exist in the phase diagrams of ceria and praseodymia²² which can be stabilized in pure ceria thin film systems.^{23,24} Hence, we assume that this structure can be attributed to a reduced crystalline phase of the mixed oxide with low order. The samples with higher praseodymium content do not show this structure.

This fully reduced bixbyite structure dissolves if the temperature is increased to 800 °C (*cf.* Fig. 1(d)). In addition, streaks between the main diffraction spots become visible indicating a faceting of the surface.

At a PDA temperature of 850 °C a phase transition from the fully reduced oxide phase to a silicide phase begins (*cf.* Fig. 1(e)). The diffraction pattern consists of a sharp (1×1) structure superimposed with a strong $(\sqrt{3} \times \sqrt{3})R30^\circ$ superstructure and is known for rare earth disilicides.^{25,26} Also several concentric rings emerge pointing to the formation of polycrystalline intermediate silicide structures. These structures are stable up to a PDA temperature of 1000 °C. Here, the intensity of the $(\sqrt{3} \times \sqrt{3})R30^\circ$ spots decreases and the polycrystalline rings vanish. In addition, a (2×1) pattern in combination with a very weak $(\sqrt{3} \times \sqrt{3})R30^\circ$ superstructure appears. The transition from the $(\sqrt{3} \times \sqrt{3})R30^\circ$ to the (2×1) pattern has also been observed in a previous study²⁷ and was attributed to a complex surface structure. Note, these silicide transitions are independent of the Pr concentration and occur at the same temperature for all samples (*cf.* Fig. 2). Rather independent of composition of $\text{Ce}_{1-x}\text{Pr}_x\text{O}_{2-\delta}$ films on Si(111), it is found that the thermal stability under UHV annealing conditions is limited to temperatures below 850 °C. Therefore, the following SPA-LEED study covers only PDA steps up to 700 °C.

B. Spot profile analysis

For each PDA step a detailed spot profile analysis of the specular (00) spot is performed to analyse the surface morphology. Cross-sections along the $[11\bar{2}]$ direction are measured for different electron energies ($\propto K_\perp^2$). In the following the lateral and vertical component of the scattering vector are denoted by $K_\parallel$ and $K_\perp$, respectively. For the oxide phases a sharp central peak with a broad shoulder is observed which both can be fitted with Lorentzian functions (*cf.* Fig. 3(a)). The shoulder is caused by surface facets^{28,29} and shifts laterally in k -space for different energies. The full width half maximum (FWHM) of the central peak oscillates with increasing $K_\perp$ (*cf.* Fig. 3(b)) due to large terraces separated by single atomic steps. According to ref. 30 and 31 the oscillations can be described by

$$\text{FWHM}(K_\perp) = 100\% \text{BZ} \frac{a\sqrt{2^{2/3}-1}}{\pi} \left(\frac{1 - \cos(dK_\perp)}{\langle \Gamma \rangle} \right) \quad (1)$$

where a denotes the lateral row distance of the oxide, d the step height and $\langle \Gamma \rangle$ the mean terrace width. The prefactor $\sqrt{2^{2/3}-1}$ is necessary due to the isotropic exponentially decaying 2D correlation. Furthermore, a linear increasing offset of the FWHM

Fig. 3 Spot profile analysis of the $\text{Ce}_{0.65}\text{Pr}_{0.35}\text{O}_{2-\delta}$ sample after annealing at 400 °C for 30 min. (a) Cross section along the $[11\bar{2}]$ direction. The central peak (blue) and the shoulder (green) are fitted with Lorentzian functions. (b) FWHM of the central peak against $K_\perp$. The fit according to eqn (1) is in good agreement with the experimental data.

can be observed due to a mosaic spread of the surface crystallites. The slope of the offset corresponds to the mean angle of the mosaic spread.

The results of the analysis are depicted in Fig. 4. For all samples the atomic step height gradually increases for higher PDA temperatures (*cf.* Fig. 4(a)). This behavior can be directly associated with the oxygen loss at the surface. The generation of oxygen vacancies results in the formation of Pr^{3+} and subsequently Ce^{3+} cations¹⁶ with larger ionic radii compared to Pr^{4+} and Ce^{4+} , respectively, and thus in relaxation of the step edge atoms.

After growth for all samples the mean terrace width is ≈ 1.3 nm and stays stable until PDA temperatures above 600 °C are applied. Higher temperatures lead to a dramatic broadening of the terraces (*cf.* Fig. 4(b)). Here, a dependence on the praseodymium concentration can be found. The lower the concentration the larger terraces are observed. This effect is more clearly seen after PDA at 700 °C (*cf.* Fig. 4(b) inset).

Furthermore, the praseodymium concentration has a large impact on the mosaic spread (*cf.* Fig. 4(c)). Initially no mosaics are found for low and moderate praseodymium concentrations.

Fig. 4 Results of the spot profile analysis. For all samples the step height (a) linearly increases at higher PDA temperatures. The mean terrace width (b) is constant at low PDA temperatures independent of the praseodymium concentration. After annealing at 600 °C the mean terrace width increases dramatically. A correlation between terrace size and praseodymium concentration can be found. For lower concentrations larger terraces are observed. In addition, a strong temperature dependence of the mosaic spread (c) and PDA temperature is observed. The untreated sample with the high praseodymium concentration exhibit a large mosaic spread in contrast to the samples with the low and medium concentration which show almost no mosaic spread. With increasing PDA temperature the spread of all samples is approaching a value close to 0.9° .

In contrast, the sample with a high amount of praseodymium exhibits a large mosaic spread. We assume that the hex $\rightarrow$ cub transformation mentioned above is responsible for this effect since a similar increase of the mosaic spread can be observed for this transition in pure praseodymia films.^{32–34} With increasing PDA temperature the mosaic spread becomes larger for the samples with low and moderate praseodymium concentration while it decreases for the sample with high praseodymium concentration. All samples approach a final value of $\approx 0.9^\circ$ for the mosaic spread.

For the silicide phases the shoulder vanishes from the Bragg peaks. Furthermore, the FWHM of the central peak shows no more oscillations indicating both a large average terrace size and a large step height distribution a large step height distribution (data not shown) making a spot profile analysis impossible.

IV. Discussion

The two dimensional diffraction pattern lead to two general conclusions. On the one hand it is shown that at least one intermediate phase with long ranged ordered oxygen vacancies exist. On the other hand a transition from a crystalline oxide state over a polycrystalline state to a crystalline silicide state is found. These findings lead to several questions addressing the phase diagram of the mixed oxides. For instance, do the intermediate phases match the known phases from the pure oxide phase diagrams? In addition, the rather complex transition to the silicide phase has to be elucidated in future studies.

The spot profile analysis shows similarities to pure cerium and praseodymium oxide films grown on Si(111).^{32–34} The surfaces exhibit mosaics with terraces which are separated by monoatomic steps. However, the Ce/Pr ratio has a strong impact on the structure and morphology of the surfaces. A higher praseodymium content results in an increased oxygen loss at lower PDA temperatures which is in good agreement with the results of Zoellner *et al.*¹⁶ Thus, the Ce/Pr ratio can be used to manipulate the redox properties.

In addition, several effects on the surface morphology have to be considered. First of all the terrace size increases for higher PDA temperatures resulting in smoother surfaces on smaller scales. This effect differs from pure praseodymia films where the terrace size cannot be increased by annealing.^{33,34} The magnitude of the increment is directly related to the praseodymium concentration (*cf.* Fig. 4(b)).

In contrast, for low praseodymium content the mosaic spread of the surfaces increases with higher PDA temperatures resulting in strongly tilted crystallites and, therefore, a higher overall roughness. We assume that stress due to the expansion of the unit cell size is the reason for the formation of the mosaic spread at higher PDA temperatures.

The sample with the highest praseodymium concentration is an exception to this behavior. Here, a strong mosaic spread is observed which is lowered with increasing PDA temperatures. We assume that the initial hex $\rightarrow$ cub transformation due to

the plasma treatment is the reason for this. The energy provided by the plasma is possibly not sufficient for a full rearrangement of the cation lattice through the entire film resulting in increased stress which is relieved by forming the mosaics. With increasing PDA temperature this transition is completed and the mosaic spread is lowered.

V. Summary

In this work the surface structure and morphology of epitaxial $\text{Ce}_{1-x}\text{Pr}_x\text{O}_{2-\delta}$ films are explored. It is revealed that the Ce/Pr ratio has a strong impact on the structure and morphology of the film and can be used to tune these properties for future applications. Furthermore, a complex transition to the silicide phase *via* a polycrystalline intermediate state is found.

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