Theoretical analysis of [5.5.6]cyclacenes: electronic properties, strain energies and substituent effects†

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A novel class of cyclic conjugated molecules, composed of annelated five- and six-membered rings, is proposed and theoretically investigated using density functional theory and multireference methods with regards to their structures, strain energies, aromaticity (NICS values), electronic ground states, band gaps, and the effect of substituents. These [5.5.6]cyclacenes are predicted to be low band gap materials (below 1 eV) with, depending on their size, closed-shell singlet ground states. The strain energies from \( n = 4 \) upwards lie in the range of the synthetically known \([n]\)cycloparaphenylenes. An investigation of the effect of rim-substitution by methyl, alkynyl, thiomethyl or phenyl groups on the electronic ground states showed that thiomethyl-substitution leads to [5.5.6]n-cyclacenes with closed-shell singlet ground states for all sizes \( n \) investigated.

Introduction

Hoop-shaped molecules, consisting of linearly connected or annelated conjugated rings, have attracted chemists since 1954. Of particular interest are their potentially aromatic character, their conjugative and optoelectronic properties, and their use in host-guest chemistry. Prominent examples are \([6]_n\)cyclacenes \((1_n)\), which can be regarded as subunits of zig-zag carbon nanotubes (CNTs) as well as cyclo[\(n\)]phenacenes \((2_n)\) and \([n]\)cycloparaphenylenes \(([n]\)CPPs) \((3_n)\) as subunits of armchair CNTs (Fig. 1). A derivative of cyclo[10]phenacene and several \([n]\)CPPs have been synthesized, \([6]_n\)cyclacenes \((1_n)\) have remained elusive to synthesis up to date. The reason for this is likely found in their electronic character: \([6]_n\)cyclacenes, which have been the subject of a number of theoretical investigations, are predicted to possess open-shell singlet diradical ground states, while for cyclo[\(n\)]phenacenes \((2_n)\) large singlet-triplet splittings are expected. This difference in stability can, according to Clar, be deduced from the number of aromatic sextets that can be drawn: none for \(1_n\) and \(n\) for \(2_n\), resulting in a significantly higher stability for \(2_n\). Alternative structures to \(1_n\) consisting of not only six- but also five- to eight-membered rings have been proposed and in few cases synthesized. \([6.8]_n\)Cyclophenacene \((4)\) and several derivatives of \([4.8]_n\)cyclacenes \((5)\) could be synthesized, and \([5.7]_n\)cyclacenes as isomers of \(1_n\) were proposed and predicted to possess closed-shell singlet ground states. Cyclacenes consisting of annelated five- and six-membered rings have not been investigated yet, although this combination of ring sizes is prevalent in graphitic materials such as fullerences and the end-caps of CNTs and in optoelectronic materials. Herein, \([5.5.6]_n\)cyclacenes \((6_n)\) are proposed as a new cyclacene family and investigated with regards to their structures, strain energies, aromaticity, electronic ground states, band gaps, and the effect of substituents. In cyclacenes \(6_n\), an aromatic sextet can be drawn in every six-membered ring, thereby indicating that a high stability can be anticipated.

Fig. 1 [6]_nCycloacene \((1_n)\), cyclo[10]phenacene \((2_n)\), [6]cycloparaphenylen (3_n), [6.8]cycloacene \((4)\), (Cp)M-capped [4.8]cyclacene derivatives 5, and [5.5.6]cycloacene \((6_n)\).
Results and discussion

Computational details

The geometries and strain energies of \( 6_n \) (\( n = 3-8 \)) were calculated using density functional theory (DFT). The geometries and energies of triplet and open-shell singlet states were assessed using DFT and time-dependent DFT (TDDFT). For single-point energies a combination of complete active space self-consistent field (CASSCF)\(^{68,69} \) calculations with second-order perturbation theory (CASPT2) was employed.\(^7^0 \) NMR chemical shifts for NICS (Nucleus Independent Chemical Shift)\(^{71,72} \) values were calculated using the GIAO (Gauge Including Atomic Orbital)\(^7^3 \) method. All DFT calculations were performed with the Turbomole\(^7^4 \) program package including D3\(^7^5 \) and using the resolution-of-identity (RI)\(^7^6,7^7 \) CASSCF and CASPT2 calculations were done with Molpro.\(^7^8,7^9 \) All singlet and triplet geometries (\( 6_n \) and \( 10_n-13_n \)) were first optimized using PBE\(^8^0 \)-D3/def2-SVP\(^8^1 \) followed by harmonic vibrational frequency analyses to confirm minima as stationary points. The structures were then re-optimized using TPSS\(^8^2\)-D3 or BP86\(^8^3–8^5\)-D3 in combination with the triple-\( \zeta \) basis set def2-TZVP.\(^8^6 \)

Geometries and strain energies

The \([5.5.6]_{\text{cyclohexanes}} (6_n) (n = 3-8)\), optimized using TPSS-D3/def2-TZVP in \( C_1 \) symmetries) all possess almost perfect \( D_n \) symmetrical structures. Bond lengths of \( 6_3 \) and \( 6_4 \) as representative examples and diameters of \( 6_n \) are listed in Fig. 2. The strain energy of hoop-shaped molecules is an important parameter and can present a challenge to their synthesis. For \([5.5.6]_{\text{cyclohexanes}} (6_n)\), strain energies were estimated by comparison with the hypothetical strain-free subunit \( 7 \) at the TPSS-D3/def2-TZVP level of theory (Fig. 3).

The energy of \( 7 \) was calculated using the homodesmotic equation shown in Fig. 3 as the energy difference between dibenz[a,e]pentacene (DBP, 8) and benzene (9). Homodesmotic equations\(^8^7 \) have been used before to calculate strain energies of bent sp\(^3 \) hybridized structures.\(^6^0,6^4,8^8 \) Subtracting \( n \)-times the energy of \( 7 \) from the energy of cyclopane \( 6_n \) gives a measure of its strain energy.

With increasing hoop size the strain energies of \([5.5.6]_{\text{cyclohexanes}} (6_n)\) decrease from 151 kcal mol\(^{-1} \) for \( n = 3 \) to 44 kcal mol\(^{-1} \) for \( n = 8 \) (Fig. 2 and 3). In order to set these values in relation to experimentally known compounds, a comparison with the well-investigated \([n]_{\text{CPPs}} (3_n)\) is suitable. For \([6]_{\text{CPP}}\), which has been synthesized and is a stable compound,\(^{2^1,2^2} \) the strain energy was calculated according to Segawa et al.\(^{8^8} \) to be 86 kcal mol\(^{-1} \) (TPSS-D3/def2-TZVP), and recently the even smaller and more strained \([5]_{\text{CPP}}\) was synthesized.\(^{1^8} \) While for cyclopane \( 6_n \) for \( n = 3 \) and 4 higher strain energies were calculated (110 kcal mol\(^{-1} \) for \( 6_4 \)), from \( n = 5 \) upwards (83 kcal mol\(^{-1} \)) the strain energies of cyclopanes \( 6_n \) lie well below that of \([6]_{\text{CPP}}\).

An evaluation of the calculated bond lengths in \([5.5.6]_{\text{cyclohexanes}} (6_n)\) shows that four of the bonds in the five-membered rings vary between odd and even numbers of \( n \) (colored values in Fig. 2).

Fig. 3 Plot of strain energy vs. hoop size \( n \) of \([5.5.6]_{\text{cyclohexanes}} (6_n)\) (TPSS-D3/def2-TZVP, optimized in point group \( C_1 \); strain energies were calculated by subtracting \( n \)-times the energy of \( 7 \) from the energy of \( 6_n \) and homodesmotic equation used to calculate the energy of the strain-free subunit \( 7 \).

Aromatic character

NICS values were calculated (B3LYP\(^9^0\)/def2-QZVP\(^9^1\) on TPSS-D3/def2-TZVP optimized geometries) to assess the aromatic character of cyclopanes \( 6_n \) (Table 1). Strongly positive values denote anti-aromaticity, while significantly negative values point towards aromaticity.\(^7^1,7^2 \) As location the geometrical centers of the molecules were chosen as well a point \( 1 \) above the center of the individual five- and six-membered rings (NICS(1)).\(^7^1,7^2 \) The NICS values vary between odd and even numbers of \( n \); at the center of \( 6_n \), the NICS values are slightly positive for odd \( n \), while for even \( n \) strongly negative NICS values are found. For odd \( n \), the NICS(1) values above the five- and six-membered rings adopt values similar to those of DBP (8, Table 1) and show only small variations with increasing hoop size. The absolute NICS(1) values above the six-membered rings are small for both odd and even \( n \), giving no clear indication of aromaticity. The NICS(1) values above the five-membered rings are slightly larger in absolute value, but adopt a significant value only for \( n = 8 \) (11.2), indicating some degree of antiaromaticity. Hence, for odd sizes of \( n \) the NICS values indicate

Fig. 2 Calculated structures of \( 6_3 \) and \( 6_8 \), bond lengths (Å) in \( 6_3 \) and \( 6_4 \), and diameters \( \delta \) (Å) and strain energies \( \Delta E_s \) (kcal mol\(^{-1} \)) of \([5.5.6]_{\text{cyclohexanes}} (6_n)\) (TPSS-D3/def2-TZVP, optimized in point group \( C_1 \)).
properties similar to DBP (8), which is a stable compound in spite of its electron count (16x electrons).

Electronic ground states

Next the electronic ground states of [5.5.6] cyclacenes (6n) were investigated. Since 61 cyclacenes (1a) were predicted to possess open-shell singlet diradical ground states, which likely inhibited their synthesis up to date, 2,3,7,34–44 the stability of both the triplet and CSS states of cyclacenes (6n) is of interest. In order to increase computational speed, and since the optimized structures of cyclacenes 6n showed almost perfect Dn symmetries, their geometries were re-optimized in the respective Dn point group using TPSS-D3 and BP86-D3 in combination with def2-TZVP. The energy differences between structures optimized in C1 and in Dn symmetry were minimal.

To assess whether DFT, which is based on a single-reference configuration, is appropriate to describe the electronic states of [5.5.6]n cyclacenes (6n), single-point (SP) multireference CASSCF calculations were performed on the TPSS-D3/def2-TZVP-optimized geometries. For cyclacenes 63, 64, and 65, CASSCF(8,8)/def2-SVP calculations resulted in natural occupation numbers of the four highest occupied orbitals (see ESI, Table S2) between 1.93 and 1.91 (n = 3), 1.94 to 1.83 (n = 4), and between 1.93 and 1.92 for n = 5. For 61 cyclacene (1a) with a predicted open-shell singlet diradical ground state, the natural occupation numbers of the four highest occupied orbitals were calculated to be between 1.98 and 1.46 (CASSCF(8,8)/6-31G*), resulting in 0.76 electrons outside the closed-shell orbital space and indicating significant multi-configurational character of the singlet state. These values are significantly lower for [5.5.6] cyclacenes (6n); 0.32 for 63, 0.44 for 64, and 0.29 for 65. Hence, for cyclacenes 6n, the closed-shell orbital space is almost completely occupied, and a single-reference method such as DFT is considered appropriate.

The structures and energies of the triplet states (T) of cyclacenes 6n were assessed through optimizations at the BP86-D3/def2-TZVP level of theory using unrestricted wavefunctions (UHF), and their energies were compared to the closed-shell singlet (CSS) states (Fig. 4, T-CSS, and Table 2). For all sizes investigated (n = 3–8), the triplet states are higher in energy than the closed-shell singlet as well as the triplet states. A variation between odd and even numbers of n is observed, but the trend is reversed compared to the triplet states. The reason for this is not clear, however, an odd–even variation in energies differences has also been found for [6]n cyclacenes (see also Table 2).

A variation between odd and even numbers of n is observed, where for odd n the closed-shell singlets are more stabilized than for even n. This could be due to the total π electron count in 6n, resulting in (4m + 2) (odd n) or 4m π electrons (even n).

The geometries and energies of the open-shell singlet (OSS) states of cyclacenes 6n were assessed using TDDFT, and energies for n = 3 and 4 were also calculated at the CASPT2 level of theory. In attempted structure optimizations of the OSS states of cyclacenes 6n using unrestricted wavefunctions (UHF), relaxation to the CSS states occurred. Hence, OSS energies were obtained through structural optimizations of the lowest excited singlet states using TDDFT with BP86-D3/def2-TZVP and compared to the CSS energies (Fig. 4, OSS-CSS, and Table 2). For all sizes investigated (n = 3–8), the open-shell singlet states are higher in energy than the closed-shell singlet as well as the triplet states. A variation between odd and even numbers of n is observed, but the trend is reversed compared to the triplet states.

The bands of CSS and OSS excited singlet states of 6n are band gaps.

Table 1

<table>
<thead>
<tr>
<th>n</th>
<th>N-center</th>
<th>N-1 (5')</th>
<th>N-1 (6')</th>
<th>N-1 (even)</th>
<th>N-1 (odd)</th>
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<tr>
<td>3</td>
<td>7.5</td>
<td>6.9</td>
<td>-2.0</td>
<td>-2.0</td>
<td>-2.0</td>
</tr>
<tr>
<td>4</td>
<td>-33.7</td>
<td>6.9</td>
<td>-2.2</td>
<td>-2.3</td>
<td>-3.6</td>
</tr>
<tr>
<td>5</td>
<td>1.9</td>
<td>6.2</td>
<td>6.0</td>
<td>6.2</td>
<td>6.2</td>
</tr>
<tr>
<td>6</td>
<td>24.8</td>
<td>7.5</td>
<td>7.3</td>
<td>7.5</td>
<td>7.5</td>
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<td>0.6</td>
<td>6.2</td>
<td>6.2</td>
<td>6.2</td>
<td>6.2</td>
</tr>
<tr>
<td>8</td>
<td>-19.9</td>
<td>11.2</td>
<td>5.8</td>
<td>5.8</td>
<td>5.8</td>
</tr>
</tbody>
</table>

* B3LYP/def2-QZVP/TPSS-D3/def2-TZVP. ** NICS value in the center of the molecule. *** NICS(1) 1 Å above the 5-membered ring. **** NICS(1) 1 Å above the 6-membered ring (both outside the hoop).

Table 2

<table>
<thead>
<tr>
<th>n</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
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</thead>
<tbody>
<tr>
<td>ΔE (OSS-CSS)</td>
<td>12.9</td>
<td>19.4</td>
<td>7.3</td>
<td>12.8</td>
<td>5.3</td>
<td>9.1</td>
</tr>
<tr>
<td>ΔE (OSS-CSS)</td>
<td>5.3</td>
<td>14.4</td>
<td>—</td>
<td>12.8</td>
<td>5.3</td>
<td>9.1</td>
</tr>
<tr>
<td>ΔE (T-CSS)</td>
<td>11.4</td>
<td>5.5</td>
<td>5.0</td>
<td>2.5</td>
<td>3.5</td>
<td>0.8</td>
</tr>
<tr>
<td>ΔE (T-CSS)</td>
<td>25.3</td>
<td>-1.6</td>
<td>23.9</td>
<td>-10.5</td>
<td>30.5</td>
<td>-16.3</td>
</tr>
<tr>
<td>Band gap</td>
<td>0.72</td>
<td>0.60</td>
<td>0.44</td>
<td>0.35</td>
<td>0.33</td>
<td>0.22</td>
</tr>
</tbody>
</table>

CASSCF, dynamic electron correlation is included. As in the TDDFT calculations, the open-shell singlets have a higher energy than the closed-shell singlets (Fig. 4, OSS-CSS (CASPT2), and Table 2), but the energy differences are smaller. This result is not surprising, since it is known that the CASPT2 approximation overestimates the stabilization of biradical states.

The assessment of the electronic states of [5.5.6]cyclacenes \(6_n\) shows that at the BP86-D3/def2-TZVP level of theory their ground states are closed-shell singlets. However, with increasing \(n\) the triplet states become more stabilized, and hence the question arose which ground states other density functionals would predict. For this investigation a variety of exchange–correlation functionals was chosen: the generalized gradient approximation (GGA) functional BP86, the meta-GGA functional TPSS, the hybrid GGA functionals BHLYP,\(^{95}\) PW6B95,\(^{96}\) PBE0,\(^{97,98}\) and B3LYP, and the double-hybrid functional B2PLYP,\(^{99}\) each in combination with the quadruple-\(\zeta\) basis set def2-QZVP. SP energies of the singlet and triplet states of cyclacenes \(6_n\) were calculated on the respective TPSS-D3/def2-TZVP-optimized \(D_n\) geometries. A comparison of the resulting T-CSS energy differences (Fig. 4, Table 2 and ESI,† Table S8) allows several conclusions: a variation between odd and even numbers of \(n\) is found for all types of functionals. Its extent increases with growing amount of exact (HF) exchange in the functional (0% HF exchange in BP86 and TPSS vs. 28% in PW6B95 and 50% in BHLYP). However, with B2PLYP, which in addition to a large amount (53%) of HF exchange employs perturbative second-order correlation (PT2), the preference for odd or even \(n\) is reversed compared to all other functionals employed.

As a result, all hybrid (GGA) functionals investigated predict closed-shell singlet ground states for odd \(6_n\) with \(n = 3, 5, 7\) and triplet ground states for \(n = 6, 8\), while the (meta-)GGA functionals investigated predict a preference for the closed-shell singlet states for all \(n\). According to the double-hybrid functional B2PLYP, which has been shown to outperform the other functionals employed,\(^{100}\) the ground states of cyclacenes \(6_n\) are closed-shell singlets for all \(n (3–8)\) with significant energy differences to the triplet states between 8 and 20 kcal mol\(^{-1}\).

### Band gaps

The band gaps of cyclacenes \(6_n\) were estimated from TDDFT calculations as the excitation energies of the first singlet excited states (Table 2). This has been shown to give more accurate values than using the differences between the calculated HOMO and LUMO energies.\(^{101}\) The band gaps of [5.5.6]cyclacenes \(6_n\) decrease with growing hoop size from 0.72 eV \((n = 3)\) to 0.22 eV \((n = 8)\), classifying them as organic semiconductors with small band gaps. In comparison, the band gap for DBP \((8)\) is 1.98 eV at the same level of theory. The frontier molecular orbitals of cyclacenes \(6_n\) are predominantly localized on the pentalene units (Fig. 5). In the odd-membered cyclacenes \(6_n\) \((n = 3, 5, 7)\), HOMO and LUMO resemble their counterparts in DBP \((8)\), while for even \(n\) \((6_6, 6_8, \text{and } 6_9)\), the reverse is true: the HOMO resembles the LUMO in 8 and vice versa.

### Substituent effects

The stability of the closed-shell singlets of [5.5.6]cyclacenes \(6_n\) showed a strong dependence on the density functional employed. Hence it was wondered whether substituents on the cyclacene rim would lead to a stronger preference for the CSS states. This effect has been investigated for linear acenes, where substituents, in particular thioaryl substituents, were shown to stabilize the closed-shell singlet ground state.\(^{102}\) In cyclacenes \(6_n\), substituents can be attached either on the five- or on the six-membered rings. Considering the orbital coefficients at the respective carbon atoms in the HOMO and LUMO (Fig. 5), the strongest electronic influence (larger coefficient) can be expected from substitution at the five-membered rings. As substituents, methyl, thiomethyl, alkynyl and phenyl were chosen \((10_n–13_n, \text{Fig. 6})\). The structures of \(10_n–13_n\) were optimized in \(D_n\) symmetries (apart from \(13_3\) and the OSS of \(10_6\), for which minima were found only in \(C_1\) symmetry) using TPSS-D3/def2-TZVP as well as BP86-D3/def2-TZVP. SP energies of the closed-shell singlets and triplets were calculated using the two hybrid functionals PW6B95 and B3LYP as well as the GGA functional BP86 in combination with def2-QZVP for \(10_n–11_n\) and def2-TZVP for \(12_n–13_n\). OSS energies were calculated using TDDFT (BP86-D3/def2-TZVP).

A comparison of the relative energies (Fig. 6 and ESI†) shows that for methyl \((10_n)\), alkynyl \((11_n)\) or phenyl \((13_n)\) substituents, the T-CSS and OSS-CSS energies are similar to those of the unsubstituted cyclacenes \(6_n\) (Fig. 4) (apart from \(n = 8\) for \(10_8\) and \(13_8\)). Thiomethyl substituents \((12_n)\), on the other hand, have a stabilizing effect on the CSS states. With all functionals investigated, the closed-shell singlet states of \(12_n\) are more stable than the triplet or open-shell singlet states. Hence thiomethyl groups seem to be the best substituent in order to achieve electronically stable ground states.

### Conclusions

In summary, [5.5.6]cyclacenes \(6_n\), composed of annelated five- and six-membered rings, have been proposed as a new cyclacene family and theoretically investigated with regards to their structures, strain energies, aromaticity, electronic ground
states, band gaps, and the effect of substituents. Generally, a variation between odd and even numbers of $n$ is observed. While in the unsubstituted cyclacenes $6_n$ for even numbers of $n$ the calculated properties indicate structures with potentially antiaromatic character or low-lying diradical states, for odd $n$ closed-shell singlet ground states are predicted and electronic properties similar to dibenzopentalene (8). For all sizes $n$, low bandgaps below 1 eV were found. An investigation of substituent effects on the electronic ground states showed that rim-substitution by thiomethyl groups leads to cyclacenes with closed-shell singlet ground states for all sizes $n$ investigated. Hence cyclacenes $6_n$ or in particular their thiomethyl substituted derivatives $12_n$ are attractive synthetic targets, and studies towards their synthesis are currently underway in our laboratory.

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Notes and references

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