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# Plasmonic gold–poly(*N*-isopropylacrylamide) core–shell colloids with homogeneous density profiles: a small angle scattering study†

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Coating metal nanocrystals with responsive polymers provides a model case of smart, functional materials, where the optical properties can be modulated by external stimuli. However the optical response is highly sensitive to the polymer shell morphology, thickness and dielectric contrast. In this paper we study the nature of cross-linked, thermoresponsive polymer shells for the first time using four different scattering approaches to elucidate the density profile of the shells. Each scattering method provides unique information about the temperature-induced changes of shell thickness in terms of hydrodynamic radius and radius of gyration, the pair-distance distribution functions of the shells as well as the dynamic network fluctuations. Only a combination of these different scattering techniques allows to develop a morphological model of the core–shell particles. We further demonstrate control of the cross-linker distribution in core–shell synthesis by semi-batch precipitation copolymerization. Conducting the polymerization in three steps, we show for the first time that the polymer shell thickness can be successively increased without affecting the shell morphology and response behavior.

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## 1 Introduction

Nanostructures which exhibit localized surface plasmon resonances (LSPR) have gained significant attention due to their unique optical properties which lend themselves to applications in sensing,<sup>1–6</sup> plasmonic waveguiding<sup>7–9</sup> and as light harvesting structures in photovoltaics.<sup>10–13</sup> For these examples nanostructures with tailored optical properties are typically required, *i.e.* the LSPR must be tuned to a precise energy range. While this can be achieved by controlling the size, shape and composition of the objects, LSPR modes are also sensitive to the inter-particle separation<sup>3,14,15</sup> and the refractive index of the surrounding environment.<sup>3,16–18</sup> The inter-particle separation becomes important if optically functional materials shall be prepared *via* assembly

of plasmonic nanoparticles since plasmon resonance coupling at low particle separations will strongly alter the absorption and scattering properties of the particle array. Shelling plasmonic nanoparticles with dielectric spacer materials has been shown to a powerful means for modulating the optical properties of particle assemblies by controlling the spatial separation between the nanoparticles. However, the encapsulation by a dielectric material will affect the LSPR due to the variation in the surrounding refractive index. This variation becomes particularly complex for polymer-coatings because their radial density profile is usually inhomogeneous. Thus the refractive index is not constant in such a shell which makes a prediction and theoretical description of the LSPR properties of the plasmonic core–shell particles difficult. Conversely polymer encapsulation is a frequently used strategy because it can be achieved rather easily *via* ligand exchange<sup>19–21</sup> or polymerization in the presence of the plasmonic nanoparticles.<sup>22,23</sup> Furthermore polymer encapsulation allows the realization of inter-particle separations from a few nm up to a few hundred of nm. A versatile coating material for plasmonic nanoparticles such as gold and silver is cross-linked, thermoresponsive poly(*N*-isopropylacrylamide) (PNIPAM).<sup>24–26</sup> The free-radical polymerization of the monomer NIPAM at temperatures above the lower critical solution temperature (LCST) of PNIPAM (32–33 °C) allows for nanoparticle encapsulation since the growing oligomer chains, at the early stages of the reaction, can precipitate onto the nanoparticle surface. It has been shown

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that such a PNIPAM shell represents a soft spacer which can be employed to control the inter-particle separation in particle monolayers<sup>27</sup> and 3D nanocrystal superlattices.<sup>28</sup> This separation depends directly on the thickness of the polymer shell. Karg *et al.* have shown that the monomer concentration in the polymerization step can be used to tune the PNIPAM shell thickness on gold nanoparticle cores.<sup>25</sup> These authors have also shown that the optical properties of such inorganic–organic core–shell particles depend strongly on the shell thickness as well as the amount of the cross-linker *N,N'*-methylenebisacrylamide (BIS) used in the synthesis. However, a quantitative theoretical description of the optical properties is difficult because this requires knowledge of both the shell thickness and the shell morphology.

While control of the shell thickness is possible, control over the internal structure remains challenging. Wu *et al.* studied the kinetics of the polymerization of NIPAM and BIS and found a quicker consumption of the BIS molecules as compared to NIPAM.<sup>29</sup> Hence a rather inhomogeneous cross-linker distribution in these PNIPAM microgels is expected with higher cross-linked domains in the interior and a decreased degree of cross-linking towards the particle surface. Indeed such an inhomogeneous structure was revealed by small angle neutron scattering (SANS) of dilute microgel dispersions by Fernández-Barbero *et al.* pointing to a core–shell type structure with a dense core containing most of the cross-linker and a shell of lower density.<sup>30</sup> This was corroborated by a detailed SANS investigation of the microgel form factor by Stieger *et al.*<sup>31</sup> For measurements in the swollen state the authors identified a density profile with nearly constant density in the interior (box profile) and a rather large exterior volume with decaying density (error function). For a PNIPAM microgel prepared with 5.5 mol% BIS and relatively small dimensions (115 nm hydrodynamic radius, swollen) they found a radius of 38 nm for the inner, highly cross-linked part (box profile) and an exterior region with decaying density of 68 nm total thickness. In other words the inner volume with a rather homogeneous structure is significantly smaller than the outer inhomogeneous part. More recently Reufer *et al.* revealed the inhomogeneous network structure of PNIPAM microgels cross-linked with BIS by using dynamic light scattering (DLS) and static light scattering (SLS).<sup>32</sup> Karg *et al.* used DLS and SANS to study PNIPAM microgels prepared with different contents of BIS.<sup>33</sup> They found a rather strong dependence of the swelling behavior and the scaling behavior of the correlation length  $\xi$  on the cross-linking content. Their results indicated that the network homogeneity decreases with decreasing cross-linking. This was also shown by Varga *et al.* using SLS and DLS to investigate the structural inhomogeneities of PNIPAM microgels.<sup>34</sup> These authors demonstrated that the particle structures for low cross-linking densities have a core–shell type morphology with a shell of lower density whereas a more homogeneous structure is found for higher cross-linking. However it remains a challenge to visualize the network morphology of microgels in real space. Gawlitza *et al.* have indirectly confirmed the presence of differently sized meshes in PNIPAM microgels of different cross-linking by loading experiments with gold nanoparticles.<sup>35</sup> For weakly cross-linked microgels the gold nanoparticles of approximately 20 nm in diameter were distributed nearly

homogeneously in the microgels upon incubation with the nanoparticles. However for microgels prepared with 5 and 10 mol% of cross-linker BIS, the gold particles were inhomogeneously distributed in the microgels, *i.e.* for the highest cross-linking studied the particles were distributed mainly in the outer microgel regions. This suggests the presence of meshes smaller than the gold particle diameter in the inner microgel region and an outer region with a larger mesh size where the gold particles are trapped. This example illustrates that understanding the network morphology is crucial if microgels are to be considered as carrier systems. To circumvent the presence of a strong cross-linking gradient semi-batch polymerizations were performed by different authors. Meyer and Richtering have shown that a semi-batch synthesis of PNIPAM microgels leads to microgels with a more homogeneous internal network morphology as compared to simple batch polymerizations.<sup>36</sup> The difference in network structure was revealed by form factor analysis of SLS data. Later Acciaro *et al.* used a monomer feeding protocol to synthesize PNIPAM microgels with a homogeneously cross-linked network structure as analyzed by DLS and the optical appearance of microgel dispersions.<sup>37</sup> To obtain micrometer sized microgels with homogeneous networks, Still *et al.* performed semi-batch polymerizations using a cationic comonomer that controls the charge concentration on the seeds during the polymerization.<sup>38</sup> These authors used SLS to study the structure of their fairly large microgels. The SLS profile could be described by the core–shell model derived earlier by Stieger *et al.*<sup>31</sup> and revealed an inner, homogeneous microgel section with a radius of 495 nm and a thickness of 324 nm for the outer layer with decaying density profile.

In this work we have used for the first time a semi-batch precipitation polymerization approach in the presence of gold nanoparticle seeds in order to control the characteristic polymer network length scales, *i.e.* the global size and the internal network structure, in structurally well-defined core–shell colloids. We applied three successive polymerization steps to obtain inorganic–organic hybrid particles with different overall dimensions determined by different polymer shell thicknesses in the sub-micrometer range. Scattering techniques employing light, X-rays and neutrons, covering in total a range of momentum transfer of almost three orders of magnitude, were performed to investigate the particles on the length scales of relevance.

## 2 Experimental section

### 2.1 Chemicals

*N*-Isopropylacrylamide (NIPAM; Aldrich, 97%), *N,N'*-methylenebisacrylamide (BIS; Fluka,  $\geq 99.5\%$ ) and potassium peroxydisulfate (PPS; Fluka,  $\geq 99.0\%$ ) were used without further purification.

Gold(III) chloride trihydrate (Sigma-Aldrich,  $\geq 99.9\%$ ), sodium citrate dihydrate (Aldrich,  $\geq 99\%$ ), sodium dodecylsulfate (SDS; Ajax Laboratory Chemicals, Techn.) and butenylamine hydrochloride (BA; Aldrich, 97%) were used as received. Water was purified using a Milli-Q-system (Millipore). The final resistivity was 18 M $\Omega$  cm.



## 2.2 Synthesis

**Gold nanoparticle synthesis and functionalization.** Spherical gold nanoparticles were synthesized by citrate reduction according to the method of Turkevich.<sup>39</sup> Prior to the synthesis all glassware and stirrers were thoroughly cleaned with aqua regia and rinsed well with Milli-Q water and ethanol prior to use. In a conical flask, 200 mL of water with 1 mL of  $5 \times 10^{-4}$  M HAuCl<sub>4</sub> were heated until heavy boiling under continuous stirring. 10 mL of a hot, aqueous solution of trisodium citrate (1 wt%) were then added quickly and the solution was left to boil for 20 min, after which it was left to cool down to room temperature under stirring.

The prepared nanoparticles were then surface functionalized with butenylamine (BA). BA attaches to the gold nanoparticle surface through the amine, thus providing exposed free double bonds on the surface of the nanoparticles. Prior to the functionalization with BA, SDS was added to prevent aggregation induced by the increase in hydrophobicity caused by the BA coating. In addition we found that the SDS significantly helps to increase the colloidal stability upon concentration and purification by centrifugation. Without the addition of SDS, the gold nanoparticles are much more likely to aggregate during centrifugation. For a 200 mL amount of the previously prepared gold particle dispersion we added 1.2 mL of a 0.624 mM aqueous SDS solution dropwise under continuous stirring. After 20 min following the SDS addition, 0.392 mL of a 2.88 mM butenylamine hydrochloride solution in ethanol were added dropwise and stirring was continued for 20 min. The amount of BA corresponds to 3/4 of a monolayer assuming a surface coverage of 1 molecule per 0.4 nm<sup>2</sup>. Finally, the gold nanoparticles were concentrated by centrifugation, which was performed for 90 minutes at 3300 RCF. After centrifugation the supernatant was removed leaving only a few droplets of residue with highly concentrated gold nanoparticles. Since the supernatant still contained gold nanoparticles as evident from the red color, centrifugation was repeated with the supernatants. In total four centrifugation steps were performed this way in order to remove the majority of gold particles from solution. The residues were collected by adding only a few droplets of water for complete redispersion. The highly concentrated, nearly black particle stock solution was stored in the dark at room temperature.

**Semi-batch precipitation copolymerizations.** Core-shell microgels were prepared *via* free radical precipitation polymerizations without surfactant in a semi-batch fashion. The polymerizations were performed in a 500 mL three-neck round bottom flask equipped with a reflux condenser, a syringe pump and a magnetic stir bar. We mixed 339 mg of NIPAM and 77 mg of BIS with 200 mL of water in the flask. Under stirring and degassing with nitrogen the clear and colorless monomer solution was heated to 45 °C using an oil bath. After an equilibration time of approx. 30 min 3.15 mL of the stock solution of functionalized gold nanoparticles ([Au] = 0.01 M) was added dropwise using a syringe. After the addition of gold nanoparticles, the clear, red reaction mixture was heated to 70 °C. At this temperature the polymerization was initiated by the addition of 2 mg of potassium peroxodisulfate dissolved in 1 mL of water. After 5 minutes of

reaction time a further 39 mg BIS dissolved in 2 mL of water (degassed with nitrogen) were added continuously over a duration of 30 min using the syringe pump. After 1 hour of total reaction time, 60 mL of the particle dispersion were withdrawn from the reaction medium. This constituted sample Au-PNIPAM-1. A second reaction was carried out to grow a thicker PNIPAM shell around these particles. Firstly, 339 mg of NIPAM dissolved in 2 mL water (degassed with nitrogen) were added to the Au-PNIPAM-1 particles, which were left in the reaction flask, within 5 min. At the same time 116 mg of BIS dissolved in 2 mL of water (degassed with nitrogen) were added constantly over a duration of 30 min. Within the first 5 min of these monomer additions 2 mg of potassium peroxodisulfate dissolved in 1 mL of water were added quickly. After 1 hour of reaction time, 60 mL were withdrawn (sample Au-PNIPAM-2). This second shelling step was repeated one more time. The final product is referred to as Au-PNIPAM-3. The volume of all three microgel dispersions was diluted to 100 mL prior to purification by centrifugation for 90 min at 6500 RCF. This centrifugation step was sufficient to separate the core-shell colloids nearly completely from the solution as indicated by a clear and colorless supernatant. The supernatant was discarded from each sample and the residues were redispersed in 100 mL of water. Centrifugation and redispersion was repeated three times. After the third step the residues were redispersed in 5 mL of water and the samples were freeze-dried until constant weight was achieved.

The yields of the syntheses were determined gravimetrically after freeze-drying of the samples. A residual water content of 10% was assumed for all three samples. The yields in terms of total mass of the core-shell particles in relation to the total mass of the reactants are 27% after the first, 60% after the second, and 71% after the third polymerization step. It is worth noting that these yields cannot be directly related to the monomer conversion during the synthesis, which is expected to be much higher. The yields refer to the mass of particles obtained after purification from unreacted monomers and non-covalently bound oligomers.

## 2.3 Characterization

**Transmission electron microscopy (TEM).** Bright-field TEM images were recorded with a FEI TF 20 transmission microscope operated with an acceleration voltage of 200 kV. TEM samples were prepared on carbon-coated copper grids (200 mesh) by drying small droplets ( $\approx 7 \mu\text{L}$ ) of dilute, aqueous particle dispersions at ambient conditions.

**Atomic force microscopy (AFM).** AFM was performed with a multimode AFM operated with a Nanoscope III controller. All samples were examined in tapping mode under ambient conditions. Olympus AFM tips (OMCL-AC160TS) with spring constants of  $\approx 42 \text{ N m}^{-1}$  were used. The exact spring constants were not determined. Only the height profiles were used for further analysis using the WSxM software provided by Nanotec Electronica S.L.<sup>40</sup> Samples for AFM were prepared on 1 cm<sup>2</sup> pieces of bare silicon wafers with a thin (approx. 1.6 nm) negatively charged oxide layer. The wafers were first cleaned



by sonication in dichloromethane for 15 min followed by heating in a 5:1:1 mixture of H<sub>2</sub>O:NH<sub>4</sub>Cl:H<sub>2</sub>O<sub>2</sub> for 20 min at 70 °C. Monolayers of the samples were deposited by spin-coating of dilute, aqueous dispersions.

**UV-vis spectroscopy.** An Agilent 8453 spectrophotometer covering a spectral range of 190–1100 nm was used for absorbance spectroscopy. Spectra from dilute, aqueous particle dispersions (0.03 wt%) were recorded at 20 °C controlled by a circulating water bath (Lauda, Germany). The samples were measured in high optical grade quartz cells with 1 cm pathlength.

**Dynamic light scattering (DLS).** DLS measurements were performed with a HeNe laser (max. 35 mW constant output at 632.8 nm) as light source and a standard goniometer setup (ALV, Langen, Germany). For angular dependent measurements three intensity-time autocorrelation functions were measured per scattering angle in a range of 30°–150° in steps of 10°. The acquisition time for each run was 60 s. These measurements were done at 15 °C. The sample temperature was adjusted by a heat controlled toluene bath and monitored by a PT100 thermoelement. The PT100 was placed close to the sample position in the toluene bath. The stability in temperature was ±100 mK. Temperature dependent measurements were done at a constant scattering angle of 60° in a temperature range of 6–58 °C. At least three autocorrelation functions were measured per temperature. The acquisition times were between 60 and 300 s depending on the scattering intensity. All recorded intensity-time autocorrelation functions were analyzed by inverse Laplace transformations (ILT) using the software After-ALV version 1.0d by Dullware providing the mean relaxation rates  $\bar{\Gamma}$ . The polydispersity index was determined by cumulant analysis of autocorrelation functions measured at 60° scattering angle and sample temperatures of 6 and 58 °C. The samples were prepared by dissolving freeze-dried material and subsequent dilution to reach highly dilute conditions ( $\phi_{\text{eff}} < 10^{-4}$ ). All samples were filtered using PTFE syringe filters with a pore size of 5 μm and filled into dust-free, cylindrical quartz cells.

**Static light scattering (SLS).** SLS measurements were performed on a 3D LS spectrometer of LS Instruments AG (Fribourg, Switzerland) in 2D operation using a HeNe laser (max. 35 mW constant output at 632.8 nm) as light source and two APD detectors (pseudo-cross correlation). The time-average scattering intensities were measured in an angular range of 20°–150° in steps of maximum 2°. At each angle three measurements were performed with at least 30 s acquisition time. SLS profiles were recorded at 20, 30, 40 and 50 °C. The temperature was adjusted by a heat controlled decalin bath and monitored by a PT100 thermoelement. The PT100 was placed close to the sample position in the decalin bath. The stability in temperature was ±100 mK. The samples for SLS were the same as for DLS.

**Small angle neutron scattering (SANS).** SANS spectra were recorded on the KWS1 instrument of the JCMS at the Heinz Maier-Leibnitz institute (Garching, Germany). A neutron wavelength of 0.45 nm was used for all measurements. In order to cover a broad  $q$ -range spectra at three different sample-to-detector distances of 4, 8 and 20 m were measured. Due to the isotropic character of the recorded 2D detector images,

radial averaging was used for all data. Spectra for different sample-to-detector distances were merged, corrected for D<sub>2</sub>O and empty cell scattering and the incoherent scattering contribution of the sample. The scattering profiles were finally analyzed using the indirect Fourier transformation (IFT) method<sup>41</sup> to obtain the pair-distance distribution function  $p(r)$ . In addition the form factor was directly analyzed by the SASfit program by Kohlbrecher.<sup>42</sup> SANS profiles for the three core-shell systems dispersed in heavy water (1.0 wt%) were recorded at 25 °C.

**Small angle X-ray scattering (SAXS).** All SAXS data reported here were measured using a “Double Ganesha AIR” system (SAXSLAB, Denmark). The X-ray source of this laboratory-based system is a rotating anode (copper, MicroMax 007HF, Rigaku Corporation, Japan) providing a micro-focused beam at  $\lambda = 0.154$  nm. The scattering data were recorded by a position sensitive detector (PILATUS 300 K, Dectris). The samples were measured in 1 mm glass capillaries (Hilgenberg, code 4007610, Germany) at different sample-to-detector distances to cover a range of scattering vectors  $q$  between 0.026 and 2 nm<sup>-1</sup>. The temperature of the samples was controlled using a Linkam high temperature control stage with a ±0.01 K precision. The averaged data of different detector distances were merged to single scattering curves covering the whole  $q$ -range. The circularly averaged data were normalized to incident beam, sample thickness and measurement time in order to obtain absolute scale. Afterwards the scattering contribution of the solvent and the capillary were subtracted. The SAXS data were analyzed by the indirect Fourier transformation (IFT) method<sup>41</sup> to obtain the pair-distance distribution function  $p(r)$ . The pair-distance distribution functions for the different samples allow a better comparison of the particle structure than a comparison of the scattering curves.

In addition the scattering curves were fitted using the SASfit program by Kohlbrecher.<sup>42</sup>

### 3 Analysis of small angle scattering data

In a typical small angle scattering (SAS) experiment, the time-averaged scattering intensity is recorded as a function of scattering angle  $\theta$ . The length scales which are resolved in the experiment depend on the range of values of the momentum transfer  $q$ . The de Broglie wavelength of the incoming beam (*e.g.* neutrons or X-rays) and  $\theta$  define the magnitude of the momentum transfer  $q$  as follows:

$$|\vec{q}| = q = \frac{4\pi}{\lambda} \sin\left(\frac{\theta}{2}\right) \quad (1)$$

#### 3.1 SANS profiles of cross-linked microgels

First of all we will describe the small angle scattering profiles of purely organic, cross-linked microgels and neglect the gold core present in our core-shell system. This assumption is actually reasonable for neutron scattering due to the low scattering contrast of gold in heavy water ( $\Delta\eta = 1.7 \times 10^{-6}$  Å<sup>-2</sup>) and the



very low volume fraction of the gold core with respect to the overall core-shell particle volume (below 1% for all samples).

Scattering profiles for cross-linked polymer gels are typically determined by a static and a dynamic contribution:<sup>43</sup>

$$I(q) = I_{\text{stat}}(q) + I_{\text{dyn}}(q) + I_{\text{inc}} \quad (2)$$

$I_{\text{inc}}$  is the incoherent background, which was found to be nearly independent of  $q$  in the studied  $q$ -range and thus could be subtracted from the SANS profiles as a simple offset.  $I_{\text{stat}}(q)$  is directly related to the presence of cross-linker points in the network. In contrast, the dynamic contribution  $I_{\text{dyn}}(q)$  is caused by local concentration fluctuations<sup>44</sup> (Ornstein-Zernicke contribution) due to the liquid-like nature of the gel. Since these fluctuations appear typically on a length scale of a few nm, the dynamic contribution to the scattered intensity is observed at relatively large  $q$ . These liquid-like contributions can be well-described by a Lorentzian function:<sup>45</sup>

$$I_{\text{dyn}}(q) = \frac{I_L(0)}{1 + q^2 \xi^2} \quad (3)$$

Here,  $I_L(0)$  is the Lorentzian intensity and  $\xi$  the correlation length. For good solvent conditions  $\xi$  is often referred to as the blob size of a gel.<sup>30,45,46</sup> It has been shown experimentally that  $\xi$  depends on the network connectivity at a given swelling state of the network.<sup>43</sup> Furthermore  $\xi$  scales with the volume fraction of polymer, which has been experimentally revealed for cross-linked PNIPAM microgels by Stieger *et al.*<sup>47</sup>

For microgel particles with dimensions in the range of a few hundred nm the low  $q$ -part of the scattering profiles is dominated by the particle form factor  $P(q)$ . For spherical, non-interacting particles with radius  $R$  under dilute conditions,  $P(q)$  is given by:

$$P(q) = \left[ 3 \frac{\sin(qR) - qR \cos(qR)}{(qR)^3} \right]^2 \quad (4)$$

To account for polydispersity of the spherical particles this form factor is typically convoluted with a size distribution function (*e.g.* Gaussian size distribution). It has been shown in the literature that the form factor of polydisperse spheres is not sufficient to describe the low  $q$ -part of the scattering profiles of microgels.<sup>31,47</sup> This is related to an inhomogeneous network structure where the density profile deviates from the simple box profile valid for hard spheres. In contrast to microgels from a simple batch polymerization which were found to have a rather pronounced gradient in cross-link density, the network morphology of microgels from a semi-batch approach is more homogeneous.<sup>36</sup>

For our core-shell particles synthesized by a semi-batch process, we found that the density profile is rather homogeneous in the interior of the PNIPAM shell, but decreases in the outer region of the shell. To account for this density decrease we used a form factor model with an exponentially decaying scattering length profile  $\eta_{\text{exp}}(x)$  in the outer shell and a homogeneous scattering length profile in the homogeneous interior of the PNIPAM shell  $\eta_{\text{hom}}$  for the description of the experimental  $P(q)$ .<sup>42</sup>

Depending on the sign of the exponent  $\alpha$ , the exponentially decaying scattering length profile of the outer shell  $\eta_{\text{exp}}(x)$  is:

$$\eta_{\text{exp}}(x) = \begin{cases} \eta_{\text{in}} + [\eta_{\text{out}} - \eta_{\text{in}}]x \cdot \exp([1-x]\alpha) & \alpha < 0 \\ [\eta_{\text{in}} - \eta_{\text{out}}][1-x] \exp(-x\alpha) + \eta_{\text{out}} & \alpha \geq 0 \end{cases} \quad (5)$$

In this equation  $x$  is the relative distance of a segment of the exponentially decaying density shell, with a thickness  $\Delta R$ , to  $R_{\text{hom}}$ , the radius of the homogeneous shell section, according to:

$$x = \frac{r - R_{\text{hom}}}{\Delta R} \quad (6)$$

Furthermore, the scattering length density at  $R_{\text{hom}}$  is given by:

$$\eta_{\text{in}} = \phi_{\text{in}} \eta_{\text{solvent}} + (1 - \phi_{\text{in}}) \eta_{\text{shell}} \quad (7)$$

In the latter equation  $\eta_{\text{shell}}$  is the scattering length density of the pure shell material (cross-linked PNIPAM),  $\phi_{\text{in}}$  the volume fraction of solvent with the scattering length density  $\eta_{\text{solvent}}$  at  $r = R_{\text{hom}}$  and  $\phi_{\text{out}}$  the volume fraction of solvent at  $r = R_{\text{hom}} + \Delta R$ . The scattering length density at  $r = R_{\text{hom}} + \Delta R$  is given by:

$$\eta_{\text{out}} = \phi_{\text{out}} \eta_{\text{solvent}} + (1 - \phi_{\text{out}}) \eta_{\text{shell}} \quad (8)$$

Thus, the scattering length density profile with the homogeneous core and the decaying shell can be written as:

$$\eta(r, R_{\text{hom}}, \Delta R, \alpha, \phi_{\text{in}}, \phi_{\text{out}}) = \begin{cases} \eta_{\text{hom}}, & r \leq R_{\text{hom}} \\ \eta_{\text{exp}}(x), & R_{\text{hom}} < r < R_{\text{hom}} + \Delta R \\ \eta_{\text{solvent}}, & r > R_{\text{hom}} + \Delta R \end{cases} \quad (9)$$

The scattering intensity for such a radially symmetric scattering length profile is obtained by integration over  $r$ :

$$I_{\text{exp}}(q) = \int_0^\infty 4\pi r^2 \frac{\sin(qr)}{qr} \eta(r, R_{\text{hom}}, \Delta R, \alpha, \phi_{\text{in}}, \phi_{\text{out}}) dr \quad (10)$$

The SANS profiles of our smallest particles, Au-PNIPAM-1, can then be fully described by the sum of eqn (3) and (10):

$$I(q) = \frac{I_L(0)}{1 + q^2 \xi^2} + \int_0^\infty 4\pi r^2 \frac{\sin(qr)}{qr} \eta(r, R_{\text{hom}}, \Delta R, \alpha, \phi_{\text{in}}, \phi_{\text{out}}) dr \quad (11)$$

For the larger particles Au-PNIPAM-2 and Au-PNIPAM-3, the form factor is not well resolved in the accessible low  $q$  part. The scattering intensity in the low  $q$ -part of the accessible  $q$ -range is then dominated by scattering from the particle/solvent interface. For a smooth interface Porod's law can be used to describe the profiles in this region:<sup>48,49</sup>

$$I_{\text{stat}}(q) = \frac{A}{V} \frac{1}{q^4} \quad (12)$$

Exponents for the  $q$ -dependence larger than the value of 4 in Porod's law indicate a rather rough interface.<sup>50</sup>



### 3.2 SAXS profiles of core-shell colloids

For our Au-PNIPAM core-shell samples, the contrast situation for scattering using X-rays is rather different compared to neutron scattering. The high electron density gold cores cannot be neglected here and apparently will dominate the high  $q$  scattering due to the relatively small size of the gold cores. In this  $q$ -range background corrected SAXS profiles can be described using a form factor for polydisperse spheres (e.g. using eqn (4) convoluted with a Gaussian size distribution). The scattering contrast of the gold cores in relation to the PNIPAM shell is so large that the liquid-like contributions to the scattering profile are not resolved. Only at the lowest  $q$ -values do the PNIPAM shells contribute to the SAXS curves. This can be sufficiently described by an additional polydisperse sphere form factor with the radius of the sphere accounting for the overall Au-PNIPAM particle radius. The polymer-free volume due to the presence of the gold core does not have to be accounted in this description due to the rather small volume of the cores compared to the PNIPAM volume. For core-shell particles with larger cores this situation will be different and a core-shell form factor needs to be used rather than the sum of two polydisperse sphere contributions.

### 3.3 SLS profiles of core-shell colloids

A much lower  $q$ -range as compared to SAXS and SANS is available by light scattering due to the rather large wavelength of visible light. Hence, SLS can cover the low  $q$  part of the form factor. For all samples the Guinier region, providing the radius of gyration  $R_g$ , can be resolved:

$$\ln(I(q)) = \ln(I_0) - \frac{q^2 R_g^2}{3} \quad (13)$$

Here,  $I_0$  is the scattering intensity at  $q = 0 \text{ nm}^{-1}$ .

## 4 Results and discussion

Gold-PNIPAM core-shell particles were prepared by surfactant-free precipitation polymerizations of the monomer NIPAM and the cross-linker BIS in the presence of functionalized gold nanoparticles. The radical polymerizations were conducted above the LCST of PNIPAM. Under these conditions the monomers are still soluble in the reaction medium. Conversely short-chain oligomers will already phase separate and the gold nanoparticles will act as precipitation centers. Hence, the gold nanoparticles will be homogeneously encapsulated by cross-linked PNIPAM. In order to obtain polymer shells with a rather homogeneous network structure, *i.e.* with a homogeneous cross-linking in the interior of the shell, we performed the polymerizations in a semi-batch fashion with continuous feeding of monomer solutions. By dividing the feeding protocol into three steps we were able to prepare samples with three different shell thicknesses.

### 4.1 Particle morphology

In order to study the successful encapsulation of the gold nanoparticles we investigated all samples by TEM. Fig. 1(A)–(C)

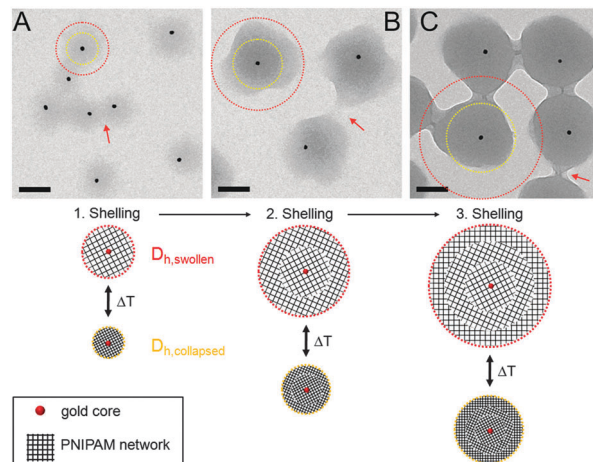


Fig. 1 Top: TEM images of Au-PNIPAM-1 (A), Au-PNIPAM-2 (B) and Au-PNIPAM-3 (C). The red arrows indicate overlapping polymer segments of the fuzzy corona of particles in close vicinity. The scale bars correspond to 100 nm. Bottom: schematic depiction of the three different core-shell systems. The red dotted circles correspond to the hydrodynamic dimensions in the swollen state. The yellow dotted circles correspond to the hydrodynamic dimensions in the collapsed state. See Table 1 for values of the hydrodynamic radii.

shows TEM images of the three samples. Lower magnification images showing a larger number of particles can be found in the ESI† (Fig. S1). Due to the large difference in electron density (gold core *vs.* PNIPAM shell), the core-shell structure of the particles is clearly visible: the gold cores appear as dark circles homogeneously surrounded by a grey corona (polymer shell). The percentage of particles without a core is lower than 5%.

Furthermore the difference in shell thickness after each shelling step can be seen (increasing from A to C). In the following the three samples will be referred to Au-PNIPAM-1, Au-PNIPAM-2 and Au-PNIPAM-3 being the samples obtained after the first, the second and the third shelling, respectively. The red dotted circles in the TEM images highlight the overall particle dimensions in the swollen state determined by DLS from highly dilute ( $\phi_{\text{eff}} < 10^{-4}$ ), aqueous dispersions, whereas the yellow dotted circles represent the dimensions in the fully collapsed state. The corresponding values for  $R_h$  are listed in Table 1. Details on the determination of  $R_h$  and the DLS analysis will be given in Section 4.3.

The dimensions of the particles imaged by TEM lie in between the hydrodynamic sizes in the swollen and collapsed state. This is due to the fact that the TEM images were recorded from particles adsorbed on a TEM grid under high vacuum conditions. The soft and fuzzy nature of the polymer shell is visible in areas where particles are in close vicinity and polymer chains seem to bridge the particles (highlighted by red arrows). These connections between neighboring particles are a result of the sample preparation. Under dilute dispersion conditions the particles are well separated and not agglomerated.

The schematic depictions in Fig. 1 illustrate the morphology of the three systems and are based on the experimentally determined particle size (according to DLS). After each shelling



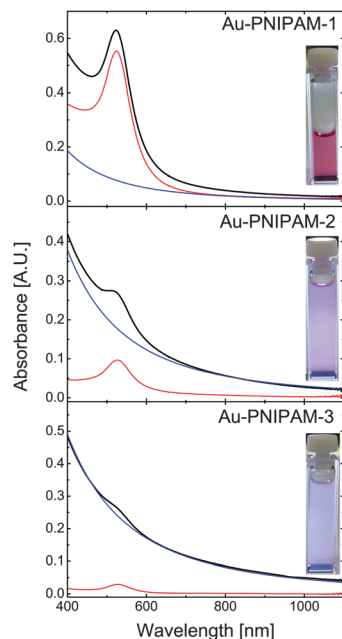
**Table 1** Hydrodynamic radii  $R_h$  from DLS in the fully collapsed state (58 °C) and the swollen state (6 °C) obtained from measurements at  $\theta = 60^\circ$  obtained from ILT analysis and second-order cumulant analysis (values in brackets). Molecular weight  $M_w$  (yield) of the core-shell particles determined using the yield of the syntheses, the amount of gold seeds used and assuming 100% encapsulation of the gold particles. Molecular weight  $M_w$  (UV-vis) determined from analysis of the UV-vis absorbance spectra

Sample	$R_h$ (58 °C) [nm]	$R_h$ (6 °C) [nm]	$M_w$ (yield) [ $10^8$ g mol $^{-1}$ ]	$M_w$ (UV-vis) [ $10^8$ g mol $^{-1}$ ]
Au-PNIPAM-1	50 (51)	83 (83)	$1.7 \pm 0.2$	$1.5 \pm 0.3$
Au-PNIPAM-2	78 (77)	146 (149)	$9.1 \pm 0.9$	$8.7 \pm 1.4$
Au-PNIPAM-3	109 (111)	194 (194)	$21.1 \pm 2.0$	$20.1 \pm 3.2$

step an additional shell of cross-linked PNIPAM is added to the particles. This leads to a constant increase of the shell dimensions whereas the core-shell morphology remains unaffected. This can also be seen from AFM images shown in the ESI† (Fig. S2).

## 4.2 Optical properties

The optical properties of the core-shell particles were studied by UV-vis absorbance spectroscopy. Fig. 2 shows the spectra obtained from dilute, aqueous dispersions at 20 °C (swollen state) along with digital photographs of all three samples. The photographs show a red, almost clear particle dispersion for Au-PNIPAM-1. This red color arising from the LSPR of the gold nanoparticle cores ( $\lambda_{\max} = 518$  nm prior to polymer encapsulation) is much less visible for Au-PNIPAM-2 and nearly invisible for Au-PNIPAM-3. At the same time Au-PNIPAM-2 and Au-PNIPAM-3



**Fig. 2** UV-vis absorbance spectra of the three core-shell systems. The black lines correspond to the core-shell spectra recorded at 20 °C. The blue lines are the modeled scattering contributions (RDG scattering) and the red lines are the modeled gold core absorbance spectra obtained by subtraction of the scattering contribution from the core-shell particle spectra. The insets show digital photographs of the samples in the quartz cells illuminated from the front.

appear turbid. This tendency can also be observed from the spectra (solid lines). Au-PNIPAM-1 shows a well pronounced LSPR peak at around  $\lambda_{\max} = 523$  nm. This value is redshifted by 5 nm compared to the gold nanoparticle cores before the polymer encapsulation. The redshift can be attributed to an increase in refractive index from water ( $n = 1.332$ ) to water swollen PNIPAM ( $n > 1.332$ ). Additionally the scattering contribution from the PNIPAM shell slightly affects the LSPR position since the scattering is wavelength dependent and will increase with decreasing wavelength causing the LSPR to appear slightly blue-shifted. The scattering from the polymer shell is visible in the spectrum of Au-PNIPAM-1 as an increase in absorbance towards wavelengths lower than the LSPR position. However, due to the relatively small dimensions of the Au-PNIPAM-1 particles the scattering from the PNIPAM shell is low. In contrast for Au-PNIPAM-2 the LSPR peak is much less intense and the rise in absorbance towards decreasing wavelength is much more pronounced. This means the scattering contribution for this sample is much stronger which is explained by the thicker PNIPAM shells and consequently larger overall particle dimensions. Due to the stronger scattering, the LSPR peak appears blueshifted ( $\lambda_{\max} = 521$  nm) as compared to Au-PNIPAM-1. In case of Au-PNIPAM-3, which has the thickest PNIPAM shell, the LSPR is barely visible and its position cannot be easily determined. For this sample the scattering dominates the spectrum.

The scattering contribution of the PNIPAM shells was simulated by using simple power law fits according to  $I_{sc} = A\lambda^{-b}$ , where  $I_{sc}$  is the scattering intensity,  $A$  an amplitude factor and  $b$  the scattering exponent. This method has been used in a previous work already.<sup>25</sup> The simulated scattering contributions are represented as the blue solid lines in Fig. 2. The values for  $A$  and  $b$  can be found in the ESI† (Table S1). Subtraction of the scattering contribution from the core-shell spectra allows us to determine the gold core spectra without the scattering contribution of the PNIPAM shells (red solid lines). The position of the LSPR should now be solely influenced by the refractive index environment. The positions are  $\lambda_{\max} = 524$  nm for Au-PNIPAM-1,  $\lambda_{\max} = 526$  nm for Au-PNIPAM-2 and  $\lambda_{\max} = 527$  nm for Au-PNIPAM-3. More information on the analysis procedure can be found in the ESI† (Fig. S3).

The calculated spectra of the gold cores can now be used to determine the molar mass of the core-shell particles since we know the exact mass concentration of core-shell particles (freeze-dried, 10% residual water) in the UV-vis samples, the diameter of the gold cores from TEM and the extinction cross-section for Au<sup>0</sup>. This allows us to determine the number concentration of gold nanoparticles in the particle dispersions (in particles per L), and assuming 100% encapsulation of the gold cores by PNIPAM (no multiple cores, no empty microgels), the determination of the mass of the core-shell particles. The molar masses of the three samples calculated this way are listed in Table 1. The mass clearly increases with increasing shell thickness from sample Au-PNIPAM-1 to Au-PNIPAM-3. We also calculated the molar mass based on the yield of core-shell particles from the different reaction steps. For this calculation we again assumed 100% encapsulation of the gold cores. The values match very nicely to the values obtained from UV-vis



analysis (see Table 1). This underlines the robustness of our approach, which is applicable to core-shell particles with fairly strong scattering contributions (Au-PNIPAM-3).

### 4.3 Hydrodynamic dimensions and swelling behavior

The overall dimensions of the core-shell colloids were investigated by dynamic light scattering (DLS). The detailed data analysis including angular dependent measurements can be found in the ESI† (Fig. S4–S6). All three core-shell systems show the typical VPT behavior of PNIPAM in water with transition temperatures around 33–35 °C. These values are slightly higher than for many reported PNIPAM microgels in water,<sup>33,49,51</sup> which can be explained by the higher cross-linking content we employed. We have previously shown that the VPTT increases slightly with increasing BIS content.<sup>33</sup> In addition the volume phase transitions of the samples are continuous with fairly broad transition ranges. This is also known for higher cross-linked microgels.<sup>33</sup>

The hydrodynamic radii in the fully collapsed (58 °C) and the nearly fully swollen state (6 °C) obtained from CONTIN and cumulant analysis are listed in Table 1. As expected the hydrodynamic radii measured at 58 °C are significantly smaller than at 6 °C. In addition it is evident from Table 1 that the shell thickness increased after each polymerization step. Furthermore the second cumulant  $\mu_2$  represents the variance of the relaxation rate distribution and can be used to determine the polydispersity  $\sigma = \sqrt{\mu_2/\Gamma_1^2}$ . The values for  $\sigma$  are  $<0.18$  for all samples measured in the swollen and collapsed state.

To compare the VPT of each sample we calculated the deswelling ratio  $V_{\text{shell}}(T)/V_{\text{shell}}(\text{swollen})$  for each sample and analyzed the temperature dependence. For this calculation only the volume of the PNIPAM shell was used  $V_{\text{shell}}(T) = V_{\text{core-shell}}(T) - V_{\text{core}}$  with  $V_{\text{core}}$  calculated on the basis of the diameter from TEM analysis (13.2 nm). The hard gold core does not contribute to the swelling. The reference volume  $V_{\text{shell}}(\text{swollen})$  was calculated using extrapolated values of  $R_h$  for  $T = 0$  °C since not all samples reach a constant size in the low temperature range (6–20 °C) but rather swell slightly with decreasing temperature.

Fig. 3 shows the temperature evolution of the deswelling ratio. As can be seen the curves match very well for all samples except for some deviations of sample Au-PNIPAM-1 at temperatures above the VPTT. In this range the deswelling of Au-PNIPAM-1 is slightly less pronounced than for Au-PNIPAM-2 and Au-PNIPAM-3. This may be related to a slightly higher cross-linking efficiency for the sample after the first polymerization step. However the deviation is only small and an interpretation at this stage is difficult. For all samples the maximum degree of deswelling lies around 0.1–0.2, which means that the final hydrodynamic volume of the swellable PNIPAM shell has only 10–20% of its swollen volume.

The results from temperature dependent DLS measurements show a clear increase in particle size after each polymerization step with very similar deswelling behavior for all samples. This is a first indication of the similarity of the PNIPAM network morphology of each shell (see schematic depiction in Fig. 1 for a visualization of the shell morphology).

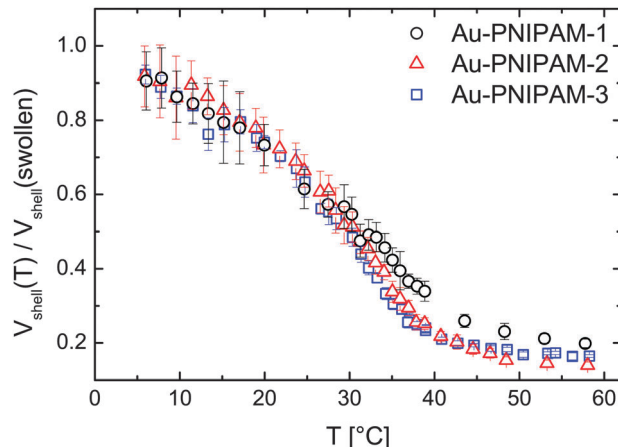


Fig. 3 Results from CONTIN analysis of temperature dependent DLS measurements performed at a constant scattering angle of 60°. Relative change of the polymer shell volume  $V_{\text{shell}}$  with respect to the swollen state (reference state) as a function of temperature.

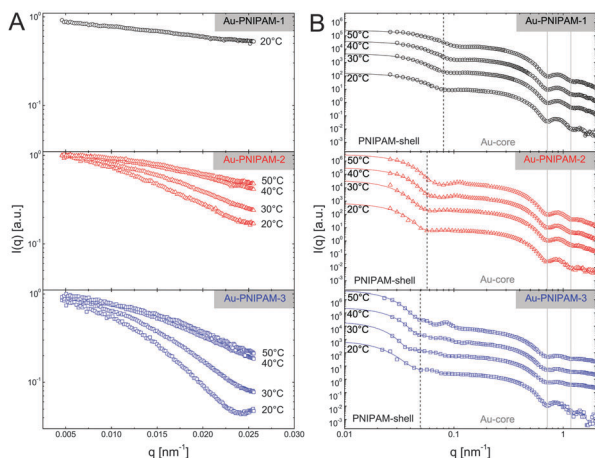
However DLS only probes the translational diffusion of our core-shell particles which is related to the hydrodynamic volume. This method does not provide any information about the internal shell morphology. Therefore we performed SLS, SAXS and SANS measurements as well.

### 4.4 Radius of gyration, core radius and pair-distance distribution functions

Due to the relatively small overall diameter  $d$  of all three core-shell samples, SLS can be used to resolve the Guinier region for which the requirement  $qR_g \ll 1$  typically needs to be fulfilled. Even for the largest sample, Au-PNIPAM-3, the Guinier region is resolved since the average refractive index of the water-penetrated PNIPAM shell is close to the refractive index of water. Hence the Rayleigh–Debye–Gans criterion is met although the particles do not fulfill the Rayleigh criterion for visible light ( $d < \lambda/20$ ). Fig. 4(A) shows normalized SLS profiles for all samples measured at different temperatures. Sample Au-PNIPAM-1 only provided reasonable SLS profiles in the fully swollen state. This may be attributed to the small dimensions in the collapsed state and the low scattering intensity. SLS curves measured at higher temperatures were relatively noisy (even for very long acquisition times) and showed almost no angular dependence. Hence only results for 20 °C are shown for Au-PNIPAM-1.

All SLS profiles shown in Fig. 4(A) reveal angular dependence of the scattering intensity  $I(q)$ . However the angular dependence of  $I(q)$  increases with increasing particle size from Au-PNIPAM-1 to Au-PNIPAM-3. The profile for Au-PNIPAM-1 at 20 °C shows only a slight but continuous decrease of  $I(q)$  with increasing  $q$  indicating that the low  $q$ -limit of the Guinier region is already probed. The form factor minimum of this fairly small sample is outside the accessible  $q$ -range and would appear at significantly larger  $q$ . In contrast to this, the first form factor minimum is already resolved by SLS for the largest sample, Au-PNIPAM-3, but only in the swollen state at 20 °C. With increasing temperature the sample Au-PNIPAM-3 shrinks





**Fig. 4** Results from temperature dependent SLS (A) and SAXS (B) experiments. Measurements were performed below (20 and 30 °C) and above the VPTT (40 and 50 °C). (A) SLS measurements normalized to  $I(q = 0 \text{ nm}^{-1}) = 1$ . (B) SAXS profiles and respective fits from IFT analysis (solid lines). The spectra were shifted horizontally by multiplication for the sake of clarity ( $\times 1$ ,  $\times 100$ ,  $\times 2000$ , and  $\times 40\,000$ , from bottom to top). The solid, grey lines highlight the position of the form factor minima of the gold cores. The dashed, black lines highlight the position of the first form factor minima of the swollen core-shell particles (at 20 °C).

and the form factor minimum shifts to larger  $q$ -values, which are again outside the accessible  $q$ -range. The particle shrinkage with increasing temperature leads to a decrease in the angular dependence of  $I(q)$ . The same trend is observed for sample Au-PNIPAM-2. Since this sample is significantly smaller than Au-PNIPAM-3 the form factor minimum is not resolved even for the swollen state at 20 °C. Looking at sample Au-PNIPAM-2 and Au-PNIPAM-3 it appears that the SLS profiles measured at 40 and 50 °C do not significantly differ for each sample. This illustrates that the difference in size is almost negligible under these conditions. This is in agreement with the observation from DLS (see Fig. 3). From DLS the strongest change in particle size is observed comparing 30 and 40 °C. This effect is nicely reflected by the SLS profiles measured at these temperatures.

All SLS profiles shown in Fig. 4(A) were used to calculate the radius of gyration  $R_g$  from Guinier analysis according to eqn (13). The respective values for SLS experiments at 20 °C and the corresponding hydrodynamic radii  $R_h$  from DLS are listed in Table 2. We also calculated the ratio between both radii  $\rho = R_g/R_h$ . The values of  $\rho$  range from 0.70 to 0.73 and are

**Table 2** Results from scattering studies: hydrodynamic radii  $R_h$  from DLS at 20 °C, radii of gyration  $R_g$  from SLS at 20 °C, ratio  $R_g/R_h$ , radii from IFT analysis of SAXS profiles measured at 20 °C, and radii from IFT analysis of SANS profiles measured at 25 °C

Sample	$R_h$ (20 °C) [nm]	$R_g$ (20 °C) [nm]	$R_g/R_h$	$R_{\text{SAXS}}$ (20 °C) [nm]	$R_{\text{SANS}}$ (25 °C) [nm]
Au-PNIPAM-1	77	54	0.70	65	65
Au-PNIPAM-2	135	98	0.73	100	100
Au-PNIPAM-3	180	129	0.72	130	125

close to the theoretically expected value of  $\sqrt{3/5} = 0.775$  for hard spheres. We attribute the slightly smaller values to a low-density outer layer which may contain mainly linear chain segments. Such a layer will have an impact on the hydrodynamic radius probed in DLS but not significantly on  $R_g$  probed by SLS. This tendency has been also observed by Varga *et al.*, who found values of  $\rho$  close to 0.6 for higher cross-linking contents ( $\approx 8 \text{ mol}\%$ ).<sup>34</sup> The cross-linking in this study is much higher and the values of  $\rho$  are significantly larger and closer to the hard sphere limit. We attribute this to a smaller exterior network domain with lower cross-linking.

To study a broader  $q$ -range and to resolve the form factor of all samples, we performed SAXS experiments at comparable temperatures to the SLS experiments. The SAXS spectra are shown in Fig. 4(B). The solid lines in the spectra are fits from IFT analysis. The results from the IFT analysis will be discussed in Section 4.5. Looking at the high  $q$ -limit of the SAXS profiles at least two well-pronounced oscillations of  $I(q)$  are observed for all samples independent of the temperature. The two minima of  $I(q)$  which can be clearly identified (indicated by grey, vertical lines) are related to the form factor of the gold cores. The position of the first minimum is at  $q_{\text{min}} = 0.72 \text{ nm}^{-1}$  which corresponds to a sphere radius of 6.2 nm. This value is in good agreement with the radius obtained by TEM ( $13.2 \text{ nm}/2 = 6.6 \text{ nm}$ ). Due to the high electron density of the gold cores as compared to the PNIPAM shell, the SAXS profiles are dominated by scattering from the gold cores at  $q > 0.1 \text{ nm}^{-1}$ . It is worth noting that the measured samples were dilute (1 wt%) and the volume fraction of the gold cores is below 1% for all samples. Looking at the lower  $q$ -part of the profiles a sudden increase in  $I(q)$  with decreasing  $q$  is observed for all samples. This increase is related to scattering from the PNIPAM shell. The black dotted, vertical lines in the spectra highlight roughly the position of the first form factor minimum of the shell for each sample at 20 °C. The position of the minimum shifts to lower  $q$  for increasing particle size and hence the minimum has the lowest  $q$  value for Au-PNIPAM-3. For each sample the minimum shifts to larger values of  $q$  for increasing temperature. This effect is related to the temperature-induced shrinkage and hence a reduction in particle size of the core-shell colloids.

For the smallest sample Au-PNIPAM-1 the lowest accessible  $q$  values in the SAXS experiments are already sufficiently low to perform a Guinier analysis. Hence the radii of gyration which were not accessible by SLS for Au-PNIPAM-1 at 30, 40 and 50 °C can be determined. This allows us to analyze the dependence of  $R_g$  on the molar mass  $M_w$  of the core-shell particles as determined by UV-vis analysis (see Table 1). In Fig. 5 the logarithm of  $R_g$  is plotted as a function of the logarithm of  $M_w$ . A linear dependence is observed for all states of swelling. The slopes of the linear fits (solid black lines) provide the Flory exponent  $\nu$  according to  $R_g \propto (M_w)^\nu$ . The values of the Flory exponent are  $\nu = 0.34$ – $0.39$  for all temperatures. These values are very close to the theoretical value for hard spheres ( $\nu = 1/3$ ). This indicates a homogeneous network structure for all samples independent of the state of swelling.



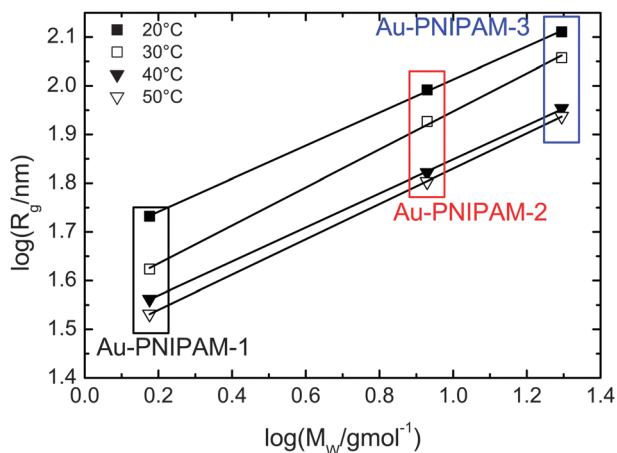


Fig. 5 Analysis of the Flory exponent for different temperatures. Shown is the dependence of the radius of gyration (logarithmic) determined from SLS on the molar mass (logarithmic) as determined from UV-vis absorbance spectroscopy. The values of  $R_g$  for Au-PNIPAM-1 at temperatures higher than 20 °C were determined from Guinier analysis of SAXS profiles.

#### 4.5 Form factor analysis

Due to the high electron density of the gold cores in comparison to the PNIPAM shell, which only contains the light elements C, H, N and O, the scattering profiles from SAXS are dominated by scattering from the gold cores. However this contrast situation changes completely in the case of neutron scattering of the core-shell particles dispersed in heavy water. Fig. 6 compares results from SAXS and SANS experiments performed on dilute samples (1 wt%) dispersed in  $H_2O$  and  $D_2O$ , respectively. In Fig. 6(A) and (B) scattering profiles of all samples measured under good solvent conditions are shown (20 °C for SAXS and 25 °C for SANS). The solid lines in (A) and (B) are fits from IFT analysis. These fits describe the SAXS and SANS data of all samples very well. As discussed in the previous subsection the SAXS spectra of the core-shell samples are dominated by scattering from the gold cores although the volume fraction of the gold cores with respect to the overall particle volume is below 1% for all core-shell samples. For comparison a SAXS curve from the bare gold cores, prior to polymer encapsulation, is shown in (A) as well. Except for the low  $q$  regime, where scattering from the PNIPAM shell contributes, the gold cores show the same features as the profiles of the core-shell particles. The first two form factor minima are nearly at the same position as for the core-shell colloids. In contrast the scattering contribution of the cores is not visible in the SANS profiles shown in (B). The high  $q$  part is dominated by the dynamic fluctuations of the PNIPAM network (Ornstein-Zernicke contribution). At lower values of  $q$  two distinct form factor minima can be observed for Au-PNIPAM-1. For Au-PNIPAM-2 and Au-PNIPAM-3 the form factor minima are not well resolved. For these larger particles the minima are at the low  $q$  limit where the resolution in  $q$  is poor and the scattering features are smeared out due to the wavelength and geometrical instrument resolution. In Fig. 6(C) and (D) the normalized pair-distance distribution functions as obtained from IFT

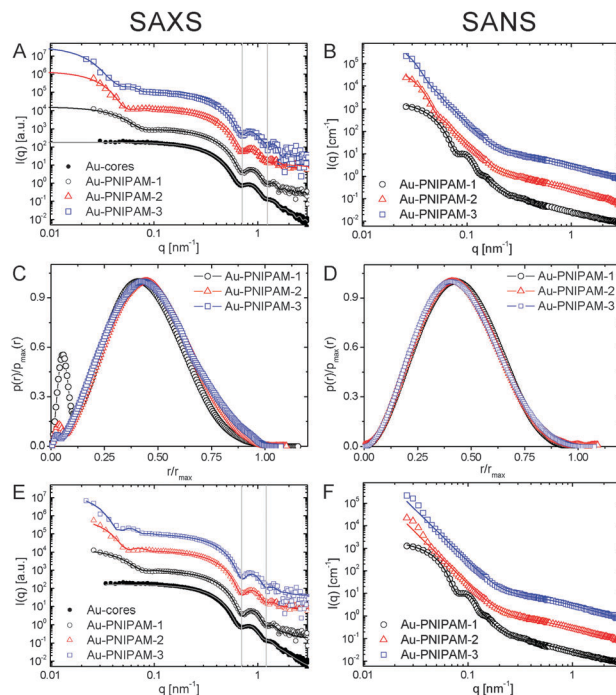


Fig. 6 Results from small angle scattering performed at 20 °C. Left column: SAXS. Right column: SANS. (A) and (B) show scattering profiles with fits determined from IFT analysis (solid lines). (C) and (D) show normalized pair-distance distribution functions as a result of IFT analysis. (E) and (F) show small angle scattering profiles with fits obtained from form factor analysis using SASfit (solid lines). For the sake of clarity the SAXS profiles in (A) and (E) were shifted by multiplication ( $\times 1$ ,  $\times 100$ ,  $\times 2000$ , and  $\times 40\,000$ , from bottom to top). The SANS profiles in (B) and (F) were also shifted by multiplication ( $\times 1$ ,  $\times 10$  and  $\times 100$ , from bottom to top).

analysis of the SAXS profiles shown in (A) and SANS profiles in (B) are presented. These profiles were normalized to the maximum value of  $p(r)$  and to the maximum radius  $r$  for a direct comparison between the different core-shell samples. The values for the particle radii  $R$  corresponding to the values of  $r_{\max}$  from this IFT analysis are listed in Table 2. Comparing the radii obtained by the different methods for the same sample a very good agreement is found. In addition, for Au-PNIPAM-2 and Au-PNIPAM-3 the radii from IFT analysis of the SAXS and SANS profiles are very close to the radii of gyration from SLS. For Au-PNIPAM-1 a deviation is observed with larger radii from IFT analysis as compared to the SLS analysis. For this sample the SLS characterization was difficult due to the rather small particle size and the weak scattering intensity leading to noisy SLS profiles with only small angular dependence indicating that SLS already probes the very low  $q$ -limit of the Guinier region for this sample.

Comparing the pair-distance distribution functions of the different samples a very nice match of the profiles for SAXS as well as for SANS is found. This is an indication for very similar shell morphologies. All profiles are highly symmetric and their maxima are close to  $r/r_{\max} = 0.5$ . Slight asymmetries for  $r/r_{\max}$  between 0.75–1 may be explained by an outer region of lower cross-linking or even no cross-linking. The presence of such a layer was already estimated from results of  $R_g/R_h$  discussed



previously in this subsection. The only noticeable difference comparing the pair-distance distribution functions from SAXS and SANS are the peaks at small relative radii in case of the SAXS profiles. These peaks are related to the gold cores. The intensity of the peak is decreasing with increasing PNIPAM shell size because the volume fraction of the core is decreasing. Pair-distance distribution functions obtained from SAXS without normalization to  $r_{\max}$  can be found in the ESI† (Fig. S7). These profiles show that the peaks related to the gold core appear at very similar radii indicating that the core size is comparable between all samples. This highlights the robustness of the IFT analysis.

In addition to IFT analysis of the SAXS and SANS curves, we performed form factor fits using the software SASfit. In case of the SAXS profiles the form factor of simple spheres according to eqn (4) convoluted with a Gaussian size distribution could be used to sufficiently describe the large  $q$ -range of the core-shell profiles where the gold core scattering dominates. For the SAXS profile measured from the bare gold cores (black circles) this polydisperse sphere model describes the whole scattering profile very well (solid, grey line) providing a core radius  $R_{\text{core}} = 6.5$  nm with 8% polydispersity. This value is in very good agreement with the results from TEM analysis ( $R_{\text{core}} = 6.6$  nm, 8% polydispersity). The lower  $q$ -part of the profiles from the core-shell particles could be satisfyingly described by an additional polydisperse sphere form factor which accounts for scattering from the PNIPAM shell. These fits are shown as solid lines in Fig. 6(E) and provided core radii of  $R_{\text{core}} = 6.3$  nm for all core-shell samples. The overall radii from the form factor of the PNIPAM shell were 52, 78 and 96 nm for Au-PNIPAM-1, Au-PNIPAM-2 and Au-PNIPAM-3, respectively. The value for Au-PNIPAM-1 is in good agreement with the radius of gyration obtained from SLS and slightly smaller ( $\approx 20\%$ ) than the radius obtained from IFT analysis of the SAXS profile. For Au-PNIPAM-2 and Au-PNIPAM-3 the overall radii from SASfit analysis are significantly smaller than the radii obtained from SLS and IFT analysis of the SAXS profiles. This is related to the poor resolution of the form factor at low  $q$  for these relatively large particles.

The SANS data were analyzed using SASfit and different form factor models as well. In case of Au-PNIPAM-2 and Au-PNIPAM-3 the sum of a Lorentzian function (eqn (3)) accounting for liquid-like concentration fluctuations (Ornstein-Zernicke contribution) and a Porod part (eqn (12)) could be used to describe the scattering curves quite well. However, slight deviations from a value of 4 in the exponent were found in Porod's law (eqn (12)) indicating that the PNIPAM/solvent interface is not smooth.<sup>50</sup> The exponents from the fits were 4.6 for both samples. Due to the very limited resolution of the form factor at small  $q$  for these rather large particles we did not analyze the data with a more complex model with more free fit parameters. Several authors have shown that the sum of eqn (3) and (12) can describe SANS profiles of cross-linked PNIPAM microgels.<sup>30,33,49,52</sup>

The form factor of Au-PNIPAM-1 is much better resolved at low  $q$  due to the much smaller dimensions of these particles.

In a first attempt we fitted the SANS profile of this sample using a sum of a Lorentzian function (eqn (3)) and a form factor for spheres according to eqn (4) convoluted with Gaussian polydispersity. Whereas the Lorentzian function describes the high  $q$ -part of the profiles very well, the polydisperse sphere model could not describe the scattering functions sufficiently at low  $q$ . In contrast a form factor for spheres with an exponentially decaying profile in the exterior of the spheres according to eqn (10) could be used to describe the low  $q$  scattering. The full SANS profile of Au-PNIPAM-1 could thus be fitted by eqn (11) with Gaussian polydispersity used for  $R_{\text{hom}}$ . This fit provided  $R_{\text{hom}} = 28$  nm,  $\Delta R = 33$  nm and  $\alpha = -2.4$ . A value  $\alpha = 0$  would lead to a linear density decrease in the outer shell layer. Forcing  $\alpha$  to 0 in the fitting process did not lead to a satisfying description of the scattering data. The volume fraction of solvent in the inner, homogeneous PNIPAM region is  $\phi_{\text{in}} = 0.8$ . In other words the inner shell part is swollen by 80 vol% of solvent. This value is in very good agreement with the value of 82 vol% determined using the molar mass of Au-PNIPAM-1, the density of PNIPAM ( $\rho = 1.174$  g cm<sup>-3</sup>, see *e.g.* ref. 53) and the particle radius based on SAXS and SANS ( $R = 65$  nm). More details on the fit parameters and the different contributions of the form factor model to the scattering profiles can be found in the ESI† (Fig. S8 and Table S2).

#### 4.6 Density profiles from SANS

The pair-distance distribution functions  $p(r)$  obtained from SANS measurements at 25 °C were convoluted into density profiles using the software DECON and a deconvolution procedure.<sup>54,55</sup> A representative DECON fit can be found in the ESI† (Fig. S9). Fig. 7(A) shows the density profiles of the different core-shell particles. All profiles show a constant density at low

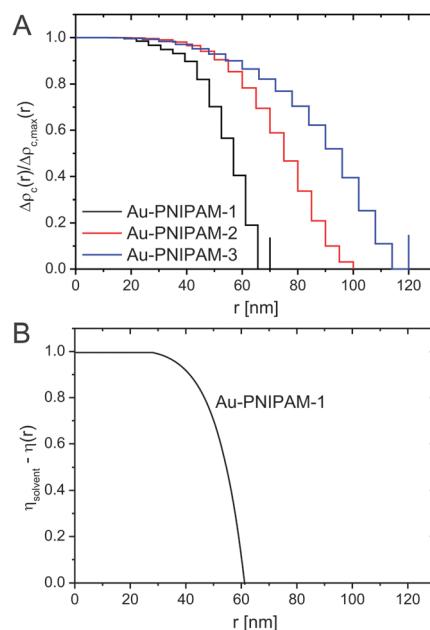


Fig. 7 Density profiles obtained from DECON analysis of SANS profiles (A) and from form factor analysis using SASfit (B).



radii, *e.g.* in the interior of the core-shell particles as typical for homogeneous spheres. In contrast at larger radii all profiles drop in an exponential fashion and the density decreases with increasing radius. This can be related to the lower cross-linked exterior of the core-shell particles. The presence of such a layer has already been experimentally observed for PNIPAM microgels prepared in classical batch syntheses.<sup>30,31,56</sup> However, we would like to point out that the density profile of Au-PNIPAM-1 is already very similar to a box profile, *i.e.* these particles behave almost like hard spheres. The region where the density drops from 0.8 to 0 is only about 15 nm wide. Looking at Au-PNIPAM-2 and Au-PNIPAM-3 these regions are significantly larger ( $\approx 40$  nm). This deviation may be due to the shelling procedure used for the particle syntheses but also due to the data analysis because of the poorly resolved form factors for these two, larger samples. Since the pair-distance distribution functions determined from SANS and SAXS analysis overlap very nicely for all three samples, we expect a rather similar shell morphology with lower cross-linked, outer regions of similar dimensions.

Fig. 7(B) shows the scattering length density profile relative to the solvent scattering length density ( $D_2O$ ) for sample Au-PNIPAM-1 as determined from SASfit analysis of the SANS profile using the form factor according to eqn (11). This profile matches very well with the profile obtained from DECON analysis. Again a constant density is found for the interior of the particles. At higher radii the density drops exponentially ( $\alpha = -2.4$ ) and reaches 0 at around 60 nm. The good agreement between the density profiles from DECON and form factor fitting demonstrates that the form factor model we have utilized in this study is well suited to describe the morphology of the core-shell particles. Due to the poor resolution of the rather large particles Au-PNIPAM-2 and Au-PNIPAM-3 and the limited accessible lower  $q$  values in the SANS experiment, scattering length density profiles for these two samples could not be generated. Only measurements on very low  $q$  instruments with a narrow wavelength distribution could provide the required scattering profiles for this analysis.

#### 4.7 Internal network structure of the shells

Fernández-Barbero *et al.* have shown that the inhomogeneity of PNIPAM microgels can also be studied by analyzing SANS data in Ornstein-Zernicke representations.<sup>30</sup> These authors determined three distinguishable regions in PNIPAM microgels from classical batch polymerization: a core region with a higher cross-linker density and smaller values of  $\xi$ , a shell region with lower cross-linking and larger values of  $\xi$ , and a surface region.

Fig. 8 shows the Ornstein-Zernicke representations of the SANS profiles for all three core-shell microgels used in the present study.

A single linear regime is found for all samples across a very wide range of momentum transfer values,  $q$ . Only at very low values of  $q$  is a deviation from linear behavior observed, which can be attributed to the form factor of the particles. Apart from this region the scattering profiles could be fitted linearly (solid lines) as shown in Fig. 8. The absence of other linear regions at lower  $q$  indicates that the majority of the PNIPAM shells are

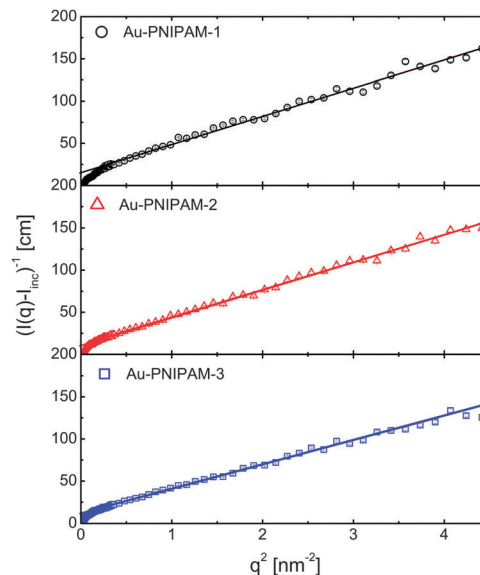


Fig. 8 Ornstein-Zernicke representation of the SANS profiles measured at 25 °C in heavy water. The solid lines are linear fits.

rather homogeneously cross-linked. The correlation lengths  $\xi$  determined from the intercepts and slopes of the linear fits are 1.5, 1.7 and 1.5 nm for Au-PNIPAM-1, Au-PNIPAM-2 and Au-PNIPAM-3, respectively. The effective volume fractions  $\phi_{\text{eff}}$  of the core-shell particles in the samples examined by SANS can be calculated on the basis of the hydrodynamic radii at 25 °C and the molar masses of the colloids providing  $\phi_{\text{eff}} = 0.06$  for all samples. It is worth noting that the particles are highly swollen with solvent ( $D_2O$ ) under this condition and the actual polymer volume fraction will be in the order of 10 times smaller. Stieger *et al.* analyzed SANS profiles of PNIPAM microgels with 5.5 mol% of BIS at 25 °C and found a significantly larger value of  $\xi$  for comparable effective volume fractions. Our PNIPAM shells were prepared with a nearly 5 times higher content of BIS, which explains the lower values of  $\xi$  found for our systems. In a recent work we have shown that the correlation length of semi-dilute PNIPAM microgel systems decreases with increasing BIS content.<sup>33</sup>

#### 4.8 Structural model for Au-PNIPAM core-shell particles

Applying DLS, SLS, SAXS and SANS to our Au-PNIPAM core-shell colloids provided information on different length scales, and with significantly different material contrasts. Fig. 9 shows a summarizing schematic depiction of the particle morphology as analyzed by the different scattering methods. The length scales in this example are drawn to scale for the Au-PNIPAM-1 sample, *i.e.* the core-shell dimensions are represented with the experimentally determined size ratios.

All core-shell particles studied in this work contain gold nanoparticle cores stemming from the same batch and hence with the same particle size and size distribution. The size of these cores was studied by TEM and SAXS prior to polymer encapsulation and by SAXS after the polymer encapsulation.



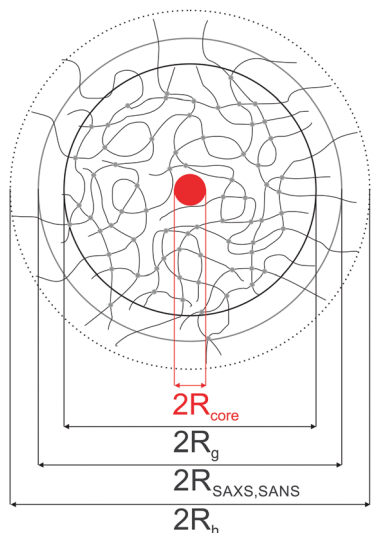


Fig. 9 Schematic depiction of the structure of the Au-PNIPAM core-shell particles with the gold core and PNIPAM shell dimensions drawn to scale with respect to sample Au-PNIPAM-1. The red circle in the center of the particle represents the gold core. The black, solid lines represent linear polymer chains and the cross-linker points are highlighted by grey circles. The experimentally determined radii from DLS ( $R_h$ ), SLS ( $R_g$ ), SAXS and SANS ( $R_{\text{SAXS,SANS}}$ ) and the core radius from SAXS and TEM ( $R_{\text{core}}$ ) are indicated.

The core radii and polydispersities determined before and after the shelling by polymer are in very good agreement.

The overall particle dimensions were studied by SAXS and SANS using IFT analysis as well as SLS using Guinier analysis. All radii were in good agreement for each sample except for the sample Au-PNIPAM-1. In the latter case the radii of gyration  $R_g$  from SLS were significantly smaller than the radii from IFT analysis of SAXS and SANS curves. This was attributed to uncertainties of the SLS profile and the respective Guinier fit obtained for this fairly small and weakly scattering sample. The hydrodynamic dimensions were studied by DLS providing values which have a smaller ratio in comparison to the radii of gyration as expected for simple hard spheres ( $R_g/R_h = 0.775$ ). This was explained by the presence of a thin outer layer of low density, *i.e.* low or even no cross-linking, contributing to  $R_h$  but not significantly to  $R_g$ .

The internal structure of the polymer shell as depicted in the sketch shown in Fig. 9 was derived from DECON analysis of the pair-distance distribution functions obtained from IFT analysis of the SANS profiles. This approach revealed density profiles with constant densities in an inner shell region and an exponentially decaying density in the outer shell domains. This evolution of the density profiles was confirmed for Au-PNIPAM-1 by fitting the SANS profile with a corresponding form factor model.

Although the applied scattering techniques were not able to resolve the form factor of Au-PNIPAM-2 and Au-PNIPAM-3 with the same quality as for Au-PNIPAM-1, the results from all applied scattering methods suggest that the structure of the polymer shells of these samples is nearly identical to the Au-PNIPAM-1 sample.

The presence of a large inner shell volume with nearly homogeneous cross-linking was proved by Ornstein-Zernicke analysis of the SANS profiles for all samples. Hence the schematic structure shown in Fig. 9 can be derived for our core-shell particles prepared from semi-batch polymerization.

## 5 Conclusions

Network homogeneity in responsive, cross-linked polymer shells employed for encapsulation of plasmonic gold nanoparticles is accessible by sequential semi-batch polymerization. Gold nanoparticle seeds acting as precipitation centers during the free-radical precipitation copolymerization of *N*-isopropylacrylamide (NIPAM) and the cross-linker *N,N'*-methylenebisacrylamide (BIS) can be homogeneously encapsulated by polymer where subsequent polymerization steps can be used to tailor the shell thickness without affecting its network architecture. We find that an outer shell region of lower crosslinking density cannot be avoided but a large inner volume of homogeneous density and hence homogeneous refractive index is achievable. A morphological model of these core-shell particles can only be derived using a combination of different scattering techniques. While the use of DLS is inevitable for following the swelling behavior based on the hydrodynamic particle dimensions, only a combination of SLS and SAXS provides the radii of gyration for the whole set of samples at different states of swelling. The form factor of the cores and the PNIPAM shells are accessible by SAXS at the same time, whereas only SANS resolves the dynamic fluctuations of the soft polymer shells.

In a future study we will theoretically simulate the optical properties of these plasmonic core-shell particles using the density profiles derived in this work.

Although not in the focus of the present study, the gold cores present in our core-shell systems represent optically active centers allowing for spectroscopic detection and can also be used as a photothermally active source for microgel collapse.

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