# PAPER



# Designing stimulus-sensitive colloidal walkers†

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Colloidal particles with DNA "legs" that can bind reversibly to receptors on a surface can be made to 'walk' if there is a gradient in receptor concentration. We use a combination of theory and Monte Carlo simulations to explore how controllable parameters, e.g. coating density and binding strength, affect the dynamics of such colloids. We find that competition between thermodynamic and kinetic trends imply that there is an optimal value for both the binding strength and the number of "legs" for which transport is the fastest. Using available thermodynamic data on DNA binding, we indicate how directionally reversible, temperature-controlled transport of colloidal walkers can be achieved. In particular, the present results should make it possible to design a chromatographic technique that can be used to separate colloids with different DNA functionalizations. **PAPER**<br> **Designing stimulus-sensitive colloidal walkers<sup>4</sup><br>
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## 1 Introduction

The study of DNA-coated colloids (DNACCs) started with two seminal papers, one by the group of Mirkin<sup>1</sup> and one by Alivisatos and collaborators.<sup>2</sup> Since then, DNACCs have become a vibrant area of research that includes experiments<sup>1-14</sup> and modelling.<sup>15</sup>–<sup>24</sup> Recent reviews covering both aspects of DNACC-based materials science can be found in ref. 25 and 26. The goal of most studies to date was to induce the selfassembly of the predesigned crystalline structure of DNACCs, by tuning the DNA-mediated colloidal interactions.<sup>3,4,12,13,15</sup> Yet, other promising areas where DNA programmability can be exploited are quickly emerging: a notable example is development of DNA-based motors<sup>27,28</sup> that move in a programmable and reproducible way. Such motors could find applications in the step-by-step synthesis of macromolecules,<sup>29-31</sup> or in DNA-based computing.<sup>32,33</sup>

Here we investigate how DNACCs functionalized with different nucleotide sequences can be used as nano- or microscale transporters. We study colloids coated with DNA molecules that are mostly composed of inert double-stranded DNA (dsDNA) sequences but have a 'sticky' single-stranded DNA (ssDNA) end. The colloids move on surfaces coated with concentration gradients of ssDNA strands with complementary

sequences. Using a combination of theory<sup>18,19</sup> and Monte Carlo (MC) simulations, we analyse how such directional motion depends on experimentally tunable parameters, such as the number of DNA "legs" on each colloid, the hybridisation freeenergy of their sticky ends, and the grafting density of the surface strands. We demonstrate that it is possible to engineer a system such that the motion can be reversed by changing temperature, pH, salt concentration, or other external parameters. Such switchability would enable novel applications like cyclable transport of specific substances on DNA tracks. Finally, we indicate how our results could be used to design a chromatographic tool to separate DNACCs with different functionalizations.

## 2 Modelling of DNA-based walkers

In Fig. 1 we show a typical setup for DNACCs walking on a coated surface. To model DNACCs we use a coarse-grained model<sup>23,34</sup> that has been shown to reproduce all features of the



Fig. 1 Nanocolloids walking on a DNA-coated surface. Atomistic detail (left) and coarse-grained representation (right).

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phase behaviour of DNACCs (Fig. 1b) (for details of the model please see the Methods section). In this model, the colloids are represented as hard-spheres with radius  $R_c$ . We assume that the DNA chains are long enough to be modelled as soft "blobs",<sup>35</sup> whose only degree of freedom is the position of the center of mass. Blobs interact with each other through a Gaussian repulsion and with colloids or the flat surface  $via$  an exponential repulsion. To each colloid, we attach a number  $\kappa$  of DNA chains. A harmonic spring represents the binding of the DNA chain to the surface. These attached blobs act as "legs" that can freely move along the surface of the colloids.<sup>34</sup> The surface  $z = 0$  is grafted with immobile DNA blobs that are distributed in a random way along the  $\nu$  axis and with a linear grafting density gradient along the  $x$  axis. In all cases discussed below, we average all observations over multiple realisations of the surface grafting points.

DNAs on the colloids have a single-stranded sticky end that is complementary to the sticky ends on the surface. A given pair of complementary DNAs is either bound or unbound. If two DNA blobs are bound, the free energy of the system shifts by an amount  $\beta f$  ( $\beta = 1/k_B T$ , where  $k_B$  is Boltzmann's constant and T the temperature), and the centers of mass of the bound blobs interact via an additional harmonic spring potential.<sup>34</sup> The binding energy  $\beta f$  is related by a constant shift to the hybridisation free energy of the sticky ends in solution under standard conditions, for colloids with a diameter 100 nm, we have  $f \approx$  $\Delta G_0$  + 11.6  $k_B T$  (see Materials and methods section for more detail), where  $\Delta G_0$  is the hybridisation free energy of complementary single-stranded sticky ends forming a bond.

On a surface with a receptor gradient, the DNACCs are subject to an effective force in the direction of the gradient. The interaction free-energy between the colloid and the substrate is determined by a combination of the hybridisation free energies of the single bonds and by the combinatorial entropy due to the formation of multiple bonds between the particles and the surface. The free energy profile can be evaluated using a recently developed self-consistent mean-field theory.<sup>18,19</sup>

The mean-field theory (described in detail in the Methods section) disregards DNA–DNA excluded volume interactions and is therefore approximate (but qualitatively correct) for nano-sized colloids that typically have relatively high coating densities. For micron-sized colloids, which display lower functionalization densities, the neglected interactions are almost negligible, hence the theory approaches quantitative accuracy18,19 and can be used as a powerful tool to explore the mechanisms of colloidal motility.

The calculated free energy profiles (see Fig. 4 in the Methods section) feature two regimes characterized by the dominance of either the enthalpy of hybridisation or the combinatorial entropy. As expected, the DNACCs generally experience a strong driving force to "walk" up the concentration gradient. This thermodynamic driving force monotonically increases as the number of DNAs per colloid  $\kappa$  and the binding strength ( $\beta f$  more negative) are increased.

However, the free-energy gradients do not completely determine the efficiency of colloidal transport on the surfaces: if the hybridisation free energy  $\beta f$  becomes too negative, the

kinetics of unbinding slows down. Similarly, when the number of "legs"  $\kappa$  is increased, it becomes more difficult for the colloid to move as it is anchored in multiple places. To explore the competition between the opposing thermodynamic and kinetic effects we performed kinetic MC simulations where we initially put the colloids at  $x = 0$  and let them diffuse freely. Details of the kinetic Monte Carlo moves are described in the Materials and methods section. For the trial moves that account for bondforming/bond-breaking we followed the procedure described in ref. 34. We kept track of the position of the colloid at different simulation times. Since we are interested in the regime where the motion of the colloid is entirely due to DNA hybridization, we impose the restriction that the translation moves of the colloid are only attempted if at least one of its DNA chains is hybridized.

In Fig. 2(A) we show the average of the distance travelled by colloids with different values of  $\kappa$  at  $\beta f = -3$ . The averaging was based on 2000 trajectories. On average, the colloids move in the direction of increasing concentration of surface DNA as time progresses. The kinetics of the system is governed by the rate of hybridisation and breaking of the single bonds. In ref. 36 the lifetime of a single bond has been shown to be of the order of  $\mu_s$ . Since we typically attempt about 10 to 100 binding/unbinding events in a single MC cycle, the corresponding real timescale can be estimated. A rough estimate predicts that the walking speeds can be up to microns per second, which is comparable to the speed of biological molecular motors. Of course, the actual speed depends on the design parameters of the system. Our kinetic simulations reveal (Fig. 2(B) and (C)) that an optimum value of  $\beta f$ and  $\kappa$  exist where colloids walk the fastest in the direction of the concentration gradient:  $k_{opt} \approx 5$  and  $\beta F_{opt} \approx -4$ . While these exact values should depend to some extent on the model and simulation details, the existence of an optimal parameter set  $(k_{\text{opt}}, \beta F_{\text{opt}})$  is due to the competition between kinetics and thermodynamics, and is thus a general feature of the system. Soft Master<br>
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Fig. 2 Walking efficiency of colloidal walkers in kinetic MC simulations on surfaces with a linear gradient of the receptor density. (A): distance travelled as a function of the simulation time, for colloids with different numbers of "legs"  $\kappa$  from 5 (top curve) to 20 (bottom curve). The value of the binding strength is fixed to  $\beta F = 3$ . The distance travelled in t<sup>\*</sup> cycles as a function of  $\kappa$  at fixed  $\beta F$  (B), and as a function of the binding strength  $\beta F$  at fixed  $k = 5$  (C). Note that the unit of distance is the radius of the colloid,  $R_c$ .

The observed behaviour suggests a chromatographic method to separate DNACCs with different functionalizations. In a traditional chromatographic column each reaction product moves over a different distance owing to a different interaction with the substrate, and the same happens for DNACCs that differ in the number of DNA "legs". Especially for the case of nano-sized colloids where the average number of strands shows greater relative variation due to their small size, obtaining uniformly functionalized colloids is important for applications. For instance, statistical fluctuations of the number of grafted DNA may interfere with the formation of ordered crystals. We suggest a simple method to characterize the colloids: on a coated surface with a gradient in receptor concentration the colloids coated with complementary sticky ends will move along the gradient. At a given temperature, their speed will depend on the functionalization  $\kappa$  and after a finite time they will be spatially separated. Since, due to the non-monotonic behavior of walking efficiency (Fig. 2), the separation will not be complete, we could repeat the process at a different temperature in order to further differentiate the colloids. Our results allow us to design – according to the experimental details of the system – an optimal temperature cycle for efficient separation. Paper Were Were on 11 Conserved behaviour suggests a chromatographic method on 11 February 11 February 2014. The method of the same images are a conserved under the same images for DNA ( $\frac{1}{\sqrt{2}}$ ,  $\frac{1}{\sqrt{2}}$ ,  $\frac{1}{\$ 

## 3 Designing reversible DNACC walkers

In the system described above, the colloidal motion can be controlled by external parameters, e.g. temperature, salt concentration or pH. As a proof of principle, we show here how to design DNACC walkers with the ability to reverse their direction of motion as a function of temperature. The approach that we propose is based on the possibility to swap between two kinds of linkages (see Fig. 3). This is encoded in the hybridisation free energies of the two competing linkages ( $\Delta G_{\alpha}$  and  $\Delta G_{\beta}$ ) that are designed to invert their relative strength as the temperature is lowered. In order to engineer this changeover behaviour, it is useful to decompose the hybridisation free energy into the configurational term  $(\Delta G_c)$  and the sticky-ends term  $(\Delta G_{x_0})$ 

$$
\Delta G_x = \Delta G_c + \Delta G_{x_0}, \, x = \alpha, \, \beta. \tag{1}
$$

 $\Delta G_{x_0}$  depends on the sticky-end sequences and is highly sensitive to the temperature, whereas  $\Delta G_c$  is an entropic term depending on the accessible configurations for the tethering part of DNA (i.e., that which is not involved in the hybridisation into dsDNA when bonds are formed). To a first approximation,  $\Delta G_c$ , when measured in units of the thermal energy  $k_BT$ , is independent of temperature. In principle one could use different tethering parts to control the binding free energy. However, this requires detailed calculation of  $\Delta G_c$ , which requires a detailed model of the tethering polymers and its interactions. Such a model may not always be available. For design purposes it is therefore better to consider a system of colloids for which all sticky ends are tethered to the colloidal surface by the same type of polymer. This implies that the tether



Fig. 3 Sticky-end architecture. The sticky ends on the colloidal "legs" are designed so that they can bind to two different receptors  $\alpha$  and  $\beta$ . The relative binding strength and thus the direction of motion can be regulated by temperature as shown in the plot of the binding free energy as a function of the temperature. The calculations were made for the strands in eqn (4); the data shown are for sticky ends  $S_{\gamma}$  binding to the substrate receptors  $S_\alpha$  (solid lines) and  $S_\beta$  (dashed lines). Results are plotted for two different salt concentrations: 0.06 M (black) and 1 M (red). The sequences have been designed so that there is a transition temperature  $T_c$ , at which the preferable binding changes from  $\alpha$  $(T < T_c)$  to  $\beta$  at  $T > T_c$ .

has no effect on the relative strength of different bonds and that the only parameter we need to tune is  $\Delta G_{x_0}$ , the hybridisation<br>free operator of the handing pairs. We recall that  $\Delta G_{x_0}$  is the sum free energy of the bonding pairs. We recall that  $\Delta G_x$  is the sum of enthalpic and entropic contributions

$$
\Delta G_0 = \Delta H_0 - T\Delta S_0,\tag{2}
$$

where – to a good approximation –  $\Delta H_0$  and  $\Delta S_0$  only depend on the salt concentrations and the nucleotide sequences. Both terms can be calculated reliably by the nearest neighbor rules of SantaLucia<sup>37</sup> that express these quantities for every possible pair of strands as a sum over twelve possible oriented nearest neighbour. Since the entropic term in the free energy  $T\Delta S$ increases linearly with temperature, whereas the enthalpic term remains roughly constant, the hybridisation free-energy will vary linearly with temperature.

In view of the above, we have constructed the sequences s as a series of non-reactive poly-T strands  $(T_n)$  that connect the tethering points with the reactive sticky ends S:

$$
s_x = 5' - (T_n)S_x - 3',
$$
 (3)

where index  $x = \gamma$ ,  $\alpha$ ,  $\beta$  is used to distinguish between the colloidal "legs"  $s_{\gamma}$ , and the two types of surface receptors  $s_{\alpha}$ ,  $\sharp$ . The notation  $5'$  and  $3'$  is the standard way to label the

 $\ddagger$  Note that the length of the  $(T_n)$  sequences contributes to the configurational part of the hybridisation free energy,  $\Delta G_c$ , which – as argued above – does not depend on temperature.

directionality of DNA sequences that affects the hybridisation free energy of the sticky ends,  $\Delta G_{x_0}$ .<br>In order to design appropriate st

In order to design appropriate sticky ends  $S_x$ , we considered the case where the sticky end of the colloidal "leg"  $S_{\gamma}$  consists of two nucleotide sequences,  $S_{\gamma} = \bar{S}_{\alpha} + \bar{S}_{\beta}$ , and can bind to two complementary receptor sequences  $S_\alpha$  and  $S_\beta$  (see Fig. 3). We chose the  $S_\alpha$  complementary part to be shorter than  $S_\beta$  but with a larger number of "strong" G–C bonds, as opposed to "weak" A-T bonds.<sup>37</sup> For such sequences, we expect the following behavior: at high temperatures, where the entropic term in eqn (2) dominates, the shorter  $S_{\gamma}$ – $S_{\alpha}$  pair will have a lower hybridisation free energy:  $\Delta G_{\alpha} < \Delta G_{\beta}$ . As temperature decreases, the entropic penalty becomes less relevant with respect to the enthalpic gain, and the free energy  $\Delta G_{\beta}$  of the longer  $S_{\gamma}$ – $S_{\beta}$  pair that is capable of forming more bonds will be lower. Since  $\gamma$  can bind either to  $\alpha$  or to  $\beta$  but not likely to both, $\S$  a crossover in binding affinity is expected at a temperature  $T_{\rm C}$ . By varying the length of the sequences and the relative number of strong G–C bonds, the relative hybridisation free energy of the two sequences and the crossover temperature  $T_{\rm C}$  can be controlled. We have used the DINAMelt web server<sup>38</sup> to evaluate the hybridisation free energy (eqn (2)) and designed the sticky-end sequences in such a way as to observe the crossover at temperature between 30 °C <  $T_{\rm C}$  < 50 °C. Two sticky-end sequence sets  $S_x$  that we designed in this way are:

$$
S_{\gamma} = \frac{\text{TTGAGAAATCCCCCCCCCC}}{S_{\alpha} = \frac{\text{GGGGGGG}}{\text{GGATTTCTCAA}}} \tag{4}
$$

and

$$
S_{\gamma} = \frac{GGATCAATCTTGGGGGGG}{C_{\alpha}S_{\alpha}} = \frac{CCCCCCC}{C_{\beta}S_{\beta}} = \frac{AGATTGATCC}{C}. \tag{5}
$$

The dependence of the hybridisation free energy  $\Delta G_0$  for one of the above solutions (eqn (4)) on temperature is shown in Fig. 3. We see that the binding free energy indeed has a crossover temperature, at which the relative binding strength of the colloidal legs to receptors  $\alpha$  and  $\beta$  changes sign. The red and black sets of curves illustrate the dependence of the crossover temperature on salt concentration.

Using our ability to switch the relative strength of  $\alpha$  and  $\beta$ bonds, we can now design a system where the direction of the walkers' motion can be changed with temperature. We assume that the surface has been prepared such that its overall grafting density  $\sigma$  is uniform, however, the densities of the two strands  $\sigma_{\alpha}$  and  $\sigma_{\beta}$  have gradients in opposite directions, e.g.  $\sigma_{\alpha} = \sigma(1 - x/L)$  and  $\sigma_{\beta} = \sigma x/L$ . On such a surface, the colloidal walker will follow the direction that maximizes the number of strong bonds, since the combinatorial entropy due to the different possible configurations of bonds remains constant throughout the system. However, the relative strength of the

bonds depends on temperature and hence, changing the temperature one can reversibly change the direction of walking. It is possible to design similar systems with the pH or salt concentration – instead of the temperature – as the control parameter. We note that many examples of unidirectional motion of colloids along surface gradients have been reported in the literature.<sup>27,28,39</sup> However, to the best of our knowledge, the technique that we propose to control the direction of motion of the colloids is new.

The driving force moving the reversible walkers is the replacement of weak bonds with stronger ones (this regime has been defined 'enthalpic' in Section 5.3). For this reason, directed motion (in contrast to random diffusion) can be achieved also when all strands on the colloids are hybridised. In this respect the reversible walkers are analogous to a vitrimer system, for which any rearrangement is achieved without varying the degree of cross-linking between polymers.<sup>40</sup> In vitrimers, swapping between different bonding configurations can be achieved only in the presence of an appropriate catalyst and at sufficiently high temperatures. These requirements stem from the necessity to effectively break strong covalent bonds before reforming them with different partners. Although DNA-hybridisation for the typical sequences we describe has a much lower energy than any covalent bond, the binding strength can still be considerable, especially at low temperatures, thus the single-bond breaking kinetics can be very slow. Under such conditions, the mobility of the colloid (i.e. the proportionality constant between its speed and the free-energy gradient) is dominated by this single-bond breaking process.<sup>20</sup> In the field of DNA-nanotechnology some strategies have been devised to alleviate this problem, e.g. toeholding mediated strands displacement.<sup>41</sup> However, a detailed discussion of how these schemes could be used in our system goes beyond the scope of the present work. Selectionally of DXA sequences that after the hybridistion<br>
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The ability to reverse the direction of colloidal motion could be interesting for a variety of applications. Moreover, it would allow us to refine the chromatographic method proposed above: if we coat the surface with two kinds of receptors  $\alpha$  and  $\beta$  with the binding free energies featuring a crossover as in Fig. 3 and if the two strands have density gradients in orthogonal directions, the direction of colloidal motion will depend on the temperature. By, e.g. gradually changing the temperature around the crossover temperature, we can drive the colloids along the curved trajectories, as well as separate them according to their functionalization. Finally, one could envisage separating colloids with similar sequences differing in only one or two nucleotides.

## 4 Methods

#### 4.1 Modeling polymers and bond formation

We use a previously developed coarse-grained model<sup>23,34</sup> to represent DNACCs (Fig. 1b). We model colloids as hard-spheres of radius  $R_c$  and the surface that they walk on as a hard halfspace  $z \leq 0$ . The bare colloid–colloid interaction  $V_{\text{HS}}(d)$ , is given by

$$
V_{\rm HS}(d) = \begin{cases} \infty, & d < 0; \\ 0, & d \ge 0, \end{cases}
$$
 (6)

<sup>§</sup> When tethered to a substrate, simultaneous binding of the same DNA filament to two other strands would require a high entropic penalty  $\Delta G_c$  and thus cannot occur. This is not true for free strands in solution, a difference that is exploited in the design of DNA-origami.

where  $d$  is the distance of the closest approach between two colloids or between a colloid and the surface  $(d = 2R_c$  for two colloids and  $d = R_c$  for colloid-surface).

The long, flexible dsDNA chains (gyration radius  $R_g = R_c/3$ ) are modelled as soft "blobs",<sup>35</sup> whose only degree of freedom is the position of the center of mass. Blobs interact with each other through a Gaussian repulsion, given by

$$
\beta V_{bb}(r) = 1.75 e^{-0.80(r/R_g)^2},\tag{7}
$$

where r is the distance between the centers of mass of two blobs. Blobs further interact with colloids or the flat surface at  $z = 0$  via an exponential repulsion

$$
\beta V_{bc}(z) = 3.20 e^{-4.17(z/R_g - 0.50)}, \tag{8}
$$

where z is the distance between the blob's center of mass and the surface (*i.e.*,  $z = r - R_c$  for the blob–colloid interaction). This specific form of the interactions and the values of the constants have been derived in ref. 35, and used previously in ref. 23, 34 and 42. To each colloid, we attach a number  $\kappa$  of DNA chains, with attachment modelled using the following radial harmonic spring potential:

$$
\beta V_{\text{tether}}(r) = \frac{3}{4} \left( \frac{r - R_{\text{c}}}{R_{\text{g}}} \right)^2,\tag{9}
$$

where  $r$  is the distance between the blob's center of mass and the center of the colloid. This form of attachment allows the DNA to move freely on the colloid surface.<sup>34</sup>

The colloids move on a DNA-coated surface, with each grafted DNA represented as a blob grafted at a specific point  $\mathbf{r}^0$  on the surface. The grafting is modelled using a harmonic spring potential, given by

$$
\beta V_{\text{gratt}}(r) = \frac{3}{4} \left(\frac{r}{R_{\text{g}}}\right)^2,\tag{10}
$$

where  $r$  is the distance between the blob's center of mass and the grafting point,  $\mathbf{r}^0$ . For a model surface with dimensions  $L \times L$ , we randomly choose  $N = \sigma L^2$  grafting points with the following probability distribution:

$$
P(x^{0}, y^{0}, z^{0}) \propto \left(\frac{x^{0}}{L}\right) \delta(z^{0} - 0). \tag{11}
$$

Here,  $\sigma$  is the grafting number density per unit area, and  $0 \leq$  $x^0$ ,  $y^0$  < L. With this distribution of grafting points, there is a roughly linear grafting density gradient along the  $x$  axis. In all cases discussed below, we average all observations over multiple realisations of the surface grafting points.

DNAs on the colloids have a sticky end that is complementary to an analogous sticky end on DNA on the surface. We model this binding as a binary event: a given pair of complementary DNAs is either bound or unbound. If bound, the energy of the system shifts by an amount  $\beta f$ , and the centers of mass of the blobs corresponding to the DNAs interact via a harmonic spring potential. Hence, each bond adds to the potential energy of the system a term given by

$$
\beta V_{\text{bond}}(r) = \beta f + 0.534 (r/R_{\text{g}} - 0.730)^2, \tag{12}
$$

where  $r$  is the distance between the centers of mass of the two blobs. The numerical values of the constants in eqn (12) – corresponding to the self-avoiding walk model for polymers – were calculated in ref. 35. The binding energy  $\beta f$  is related by a constant shift to the hybridisation free energy of the sticky ends in solution under standard conditions,  $\beta \Delta G_0$  that can be determined experimentally. Concretely,

$$
\beta f = \beta \Delta G_0 + \ln[\rho_0 R_g^3 q_{AB}], \qquad (13)
$$

where  $\rho_0 = 1$  M is the standard concentration, and  $q_{AB} = 41.15$  is a constant chosen so that free sticky ends in solution (modelled as point particles bound by  $V_{\text{bond}}(r)$  have the same binding constant as their experimental counterparts (see ESI† for a detailed derivation of this relation). For colloids with a diameter 100 nm, we have  $f = \Delta G_0 + 11.6 k_B T$ .

#### 4.2 Explicit simulations

In summary, the final Hamiltonian for a system with colloids centered at  ${R_a}$  and DNAs represented as blobs with centers of mass at  $\{r_i\}$  is

\n**Paper**  
\nwhere *d* is the distance of the closest approach between two  
\ncolloids or between a colloid and the surface (*d* = 2*R<sub>c</sub>* for two  
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\n The loop, flexible dsDNA chains (gyration radius 
$$
R_g = R_{c3}
$$
)    (10)   (12)   (12)   (13)   (14)   (15)   (16)   (17)   (18)   (19)  \n The world is an expression of the center of mass of the two  
\n the position of the center of mass. Blobs interact with each calculated in ref. 35. The binding energy *β* is related by a  
\n other through a Gaussian repulsion, given by  
\n the position of the center of mass. Blobs interact with each calculated in ref. 35. The binding energy *β* is related by a  
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\n the surface (*l.e.*, *z* = *r* − *R<sub>c</sub>* for the blob-cold interaction. This is the standard concentration, and *q<sub>AB</sub>* = 41.15 is  
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\n the surface (*l.e.*, *z* = *r* − *R<sub>c</sub>* for the blob-cold interaction. This is the constant chosen so that the same is not  
\n the surface (*l.e.*, *z* = *r* − *R<sub>c</sub>* for

In this expression,  $i \in \alpha$  denotes the set of DNAs i tethered to colloid a,  $i \in S$  denotes the set of DNAs i grafted on the surface at points  $\{r_t^{\,0}\}$ , and the primed sum is over all bound pairs of DNA chains,  $i$  and  $j$ . Respectively, the terms in the Hamiltonian capture the hard-sphere interaction between colloids, between colloids and the surface, the repulsion between DNAs and the surface, the repulsion between DNAs and colloids, the Gaussian repulsion between DNAs, the tethering of DNAs to particular colloids, the grafting of DNAs on the surface, and the binding energy between bound complementary DNAs.

Dynamics of this model is approximated by kinetic Monte Carlo simulations. Particle displacements with uniformly distributed step sizes are attempted at a frequency consistent with the free colloid having diffusion constant  $D = k_B T/6\pi\eta R_c$ , where  $\eta \approx 1$  cP is the viscosity of water. These moves define the correspondence between Monte Carlo steps and real time. Further, DNA blob displacements are attempted at the same frequency. Finally, hybridization is implemented via bondforming/bond-breaking MC moves as described in ref. 34, with a frequency chosen to mimic realistic DNA hybridisation kinetics. Such a model can realistically capture the stochastic nature of binding events, which dominates the dynamics of nanocolloids with relatively few "legs".

### 4.3 Implicit modelling of micron-size colloids: a mean field approach

For micron-sized DNACCs, a common grafting setup uses short dsDNA tethers (modeled as rigid rods) capped with short sticky ends.<sup>6,9,11</sup> We have used our previously developed self-consistent mean field theory<sup>18,19</sup> to map the free energy landscape experienced by such colloids. For concreteness, we have chosen to model tethers that are 20 nm long. The colloid is taken to have a radius  $R = 0.5$  µm and be coated with strands of type  $\gamma$ , randomly and uniformly, at a density,  $\sigma$ , equal to 1 tether per 5 nm. The surface is coated with a gradient of  $\alpha$  and  $\beta$ -type strands (please refer to Fig. 3 for details). At one end, the density of  $\alpha$ -type strands is  $2\sigma$ , and there are no  $\beta$  strands. The converse situation holds at the opposite end of the gradient. The parameter  $c$  measures progress along this linear gradient. The solution binding free energy of  $\alpha$  and  $\gamma$  sticky ends is given by  $\Delta G^0$  –  $\delta/2$ , while that of  $\beta$  and  $\gamma$  strands is given by  $\Delta G^0$  +  $\delta/2$ . No other pairs of stigly ands have approximately hinding other pairs of sticky ends have appreciable binding. Soft Master<br> **Examples Article is article in the Control of the Creative Commons are the control of the Control of the Control of t** 

To compute the colloid-surface interaction free energy at any point  $c$  on the surface, we first compute the interaction free energy per unit area,  $f(h')$ , of two plates with coats and grafting densities corresponding to the value of  $c$ , as a function of plate–plate separation,  $h'$ . We then use the Derjaguin approximation to estimate the interaction between a spherical colloid and the planar surface,  $F(h)$ , as a function of the distance of the closest approach, h, i.e.

$$
F(h) = 2\pi R \int_h^{\infty} dh' f(h').
$$

Since  $F(h)$  varies strongly with h, we assume that the particle sits at or very close to the height h that minimizes  $F(h)$ , which is usually equal to the tether length, i.e. 20 nm. The value of  $F$  at that height is used to estimate the free energy of binding. As long as the curvature of  $F(h)$  around this minimum is independent of  $c$ , this estimate differs from the real binding free energy by a constant amount, which does not affect the particle's surface dynamics.

Fig. 4 shows the free energy of binding as a function of the progress, c, along the surface coating gradient, for  $\delta = 8 k_{\rm B}T$ , as a function of mean sticky-end binding strength,  $\Delta G^0$ . At high overall binding strengths  $(\Delta G^0 \text{ around } 12 \text{ k T})$  there are two overall binding strengths  $(\Delta G^0 \text{ around } -12 k_B T)$ , there are two<br>electivisible regimes in this free energy landscene. For  $\epsilon \leq 0.5$ clearly visible regimes in this free energy landscape. For  $c < 0.5$ , it is impossible for all the  $\gamma$ -type strands in the colloid to bind to the more favorable surface  $\alpha$ -type strands as opposed to  $\beta$ -type strands. Hence, moving the particle along the surface-coating gradient results in a decrease in free energy owing to more favorable binding partners being available to the colloid's tethers. Essentially all  $\gamma$ -type strands on the colloid are bound, and the decrease in free energy is linear along the gradient, with a slope proportional to  $\delta$ . We call this regime the *enthalpic* regime. For  $c > 0.5$ , all  $\gamma$  strands can and do bind to  $\alpha$  strands on the surface. Hence, the gradient in free energy is driven purely by the increase in the number of  $\alpha$  partners available to the colloid. We call this regime the entropic regime.

At low binding strength (*i.e.*, high  $\Delta G^0$ ), entropic effects play<br>important role gion at  $\epsilon \leq 0.5$ . There many  $\alpha$  strands remain an important role even at  $c < 0.5$ . There, many  $\gamma$  strands remain unpaired, so that  $\alpha$ – $\gamma$  bonds are not saturated at  $c = 0.5$ . Indeed,



Fig. 4 Relative binding free energy of micron-sized DNACC to the surface along a linear surface coating gradient. The colloid is coated with  $\gamma$ -type strands with a density  $\sigma = 1/(5 \text{ nm})^2$ . Along the surface, the density of  $\alpha$ -type strands is  $2\sigma(1 - c)$  and that of  $\beta$ -type strands is  $2\sigma c$ .<br>The binding free energy of sticky ends  $\alpha$  and  $\gamma$  in solution is  $\Delta G^0 = A$ The binding free energy of sticky ends  $\alpha$  and  $\gamma$  in solution is  $\Delta G^0 - 4$ <br> $k$ -T and that of 8 and x strands is  $\Delta G^0 + 4 k$ -T. Free energy landscapes  $k_{\text{B}}T$ , and that of  $\beta$  and  $\gamma$  strands is  $\Delta G^0 + 4 k_{\text{B}}T$ . Free energy landscapes are shown for  $-\Delta G^0 = 12$ , 10, 8, 6 and 4  $k_B T$ . The last curve with  $\Delta G^0 =$ <br>
4  $k_T T$  corresponds to  $\Delta G = 0$  and  $\Delta G = 8$   $k_T T$  which is roughly  $-4 k_{\rm B}T$  corresponds to  $\Delta G_{\alpha} = 0$  and  $\Delta G_{\beta} = -8 k_{\rm B}T$ , which is roughly aquivalent to the system with only one type of receptors equivalent to the system with only one type of receptors.

for low enough binding strengths ( $\Delta G^0$  larger than about 4  $k_{\text{B}}T$ ), the free energy decreases linearly with constant slope from one end of the surface coating gradient to the other end. Decreasing the surface grafting density by an order of magnitude reduces all binding free energies by about the same amount, without significantly changing the qualitative features of Fig. 4. A rough estimate of whether this gradient is experimentally realizable can be obtained by supposing that the particle will only move appreciably if the free energy for moving by one tether length (20 nm) is 1  $k_BT$ . Under these conditions, the linear gradient in Fig. 4 would have to be no longer than about 100  $\mu$ m in size to realize both the enthalpic and entropic regimes, or no longer than about  $500 \mu m$  to realize only the enthalpic regime. These sizes should be within the range of current micro-patterning techniques like dip-pen nanolithography. The mean field approach presented in this section has thus proven to be a useful tool for exploring the rich phase space of the system as well as to predict novel behaviour.

## 5 Conclusions

We have presented a model study of the diffusion and directed motion of DNA-coated colloids on DNA-functionalized surfaces. For the case of DNACCs coated with a small number of DNA legs, we observed a non-monotonic dependence of the diffusion rate on the number of "legs" and on their hybridization free energy. As a general consequence of the competing kinetic and thermodynamic trends, optimal parameter values exist, such that the colloids move the fastest along the receptor concentration gradients.

For the case of DNACCs densely coated with DNA, we found instead two different diffusion regimes depending on the single-bond binding energy, and we identify the causes in the

enthalpic-vs.-entropic nature of binding in the two different cases. Finally, we have shown how insights into the thermodynamics of DNA and DNACC interactions provide a valuable way to design possible applications for this system, and we discuss the explicit case of reversible DNACC walkers as well as the use of DNA-grafted surfaces as a chromatographic tool to separate DNACCs with different functionalizations, a process that could improve their use in a number of important technological applications. The underlying mechanisms of the phenomena that we describe are not specific to particles coated with DNA. Any colloidal system with multivalent ligand–receptor interactions should exhibit similar behaviour. Paper<br>
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Thus the approach that we describe above could be used to separate multivalent nanoparticles according to their valence. Again, such separations would be potentially very useful for the purification of multivalent "magic bullets" for targeting specific pathogens.<sup>42</sup>

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