

Optimal vacancy concentrations to maximize the N–V yield in nanodiamonds†

Cite this: *Mater. Horiz.*, 2014, 1, 286

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Received 3rd December 2013
Accepted 21st January 2014

DOI: 10.1039/c3mh00157a

rsc.li/materials-horizons

In recent years fluorescent diamond nanoparticles have begun to fill the need for optically bright and stable, non-toxic probes for a growing range of biomedical applications. Significant attention has been given to finding ways of obtaining small particles with a higher yield of the optically active N–V defects, on-demand, by processing mass produced samples *post defacto*. While it has been established that a combination of irradiation (to introduce an abundance of vacancies) and annealing (to increase vacancy mobility) can achieve these goals, it is desirable to know how many vacancies to introduce *a priori*. In this paper a numerical model is developed to predict and compare the yield of different nitrogen/vacancy complexes in nanodiamond, as a function of the individual nitrogen and vacancy concentrations, the particle size and annealing temperature. The results reveal that, irrespective of the temperature and nitrogen content, this processing strategy is unlikely to work for detonation nanodiamond, but tuning these concentrations can promote the formation of N–V or H3 defects over ~20 nm.

For many years diamond nanoparticles were the proverbial ‘solution in search of a problem’. Although they presented a range of attractive properties,¹ the degree of structural control required to facilitate some of the more traditional applications remained challenging, and hindered the development of nanodiamond-based applications and devices. The luminescence emanating from optically active defects within the particles, which are also known from bulk diamond (and often referred to as color centers) is however a property that appears to be robust against the persistent polydispersity typical of nanodiamond samples. Bright, stable and spectroscopically distinct luminescence is easily obtained, provided that a sufficient concentration of defects can be created and maintained.

Defects in nanodiamond typically include intrinsic point defects, incidental impurities which result from the synthesis and/or purification processes, and defect complexes such as the range of optically active defects and color centers^{2–4} that may be incidental or deliberate. The most simple defect in diamond is a single neutral lattice vacancy, which is commonly referred to as a GR1 defect (where GR stands for general radiation). Vacancies are omnipresent in diamond, and so this defect has been extensively studied in various states.⁵

Since nitrogen is also widespread in diamond, numerous studies have also focussed on characterizing and understanding the properties of different types of N-related defects, including the single substitutional nitrogen impurity, known as the C-center. However, arguably the most widely studied defect in nanocrystalline diamond is the paramagnetic nitrogen–vacancy complex (N–V)⁶ which forms when a vacancy (GR1) migrates to bind with a C-center.^{7,8} The energy-level structure of the negatively charged N–V defect results in emissions characterized by a narrow zero-phonon line (ZPL) at 637 nm (the neutral N–V center has a zero-phonon line at 575 nm)⁹ accompanied by a wide structured side band of lower energy due to transition from the same excited state, but with formation of phonons localized on the defect. The optical emission from N–V centers in diamond nanocrystals has been shown to strongly depend on the crystal size^{8,10–13} and the charge state is related to the temperature.¹⁵

Defects such as GR1 centers and N–V centers are mobile within diamond, and may migrate if a driving force is sufficient to overcome the kinetic energy barriers associated with diffusion. The diffusion of an N–V center is vacancy-assisted, and the rate limiting step is the C–N exchange energy.¹⁴ During this migration, if an N–V center interacts with another single nitrogen atom (or a migrating vacancy interacts with a nitrogen dimer, known as an A-center) then a H3 center is formed. The H3 center consists of two N atoms surrounding a vacancy. It is one of the most studied in diamond,^{2,16} and may be formed abundantly by irradiation with 1 to 2 MeV electrons to doses of 10¹⁸ to 10²⁰ electrons per cm² and annealing at 1200 K for 20

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† Electronic supplementary information (ESI) available: Details of electronic structure simulations used to generate input parameter in this case. See DOI: 10.1039/c3mh00157a



hours in vacuum.¹⁷ If we continue this logical progression, then if a N-V center migrates to an A-center, or alternatively a H3 center migrates to a C-center (which is far less likely), then a N3 center may be formed. The N3 center consists of three nitrogen atoms surrounding a vacancy (whereas a vacancy completely surrounded by four N atoms is known as a B-center). Both the H3 and N3 provide photoluminescence and cathodoluminescence, are known to be thermally stable, and exhibit high quantum efficiency up to temperatures in excess of 500 K.¹⁸

A summary of the point group symmetry, zero phonon line (ZPL), central wavelength (λ_0) and photoacoustic imaging quantum yield for the GR1, N-V⁻, H3 and N3 defects is provided in Table 1, where we can see that the quantum yield for each of these defects is quite different. The quantum yield is defined as the number of photons emitted *via* photoluminescence *versus* the number of photons absorbed during excitation.¹⁹ The N-V and H3 defects are the most efficient, which somewhat explains their popularity in the scientific community. In addition to the quantum yield, the wavelength itself is very important, as it determines the penetration depth of the radiation. The penetration depth for 532 nm light is 0.6 mm, for 670 nm is 2.4 mm, and for 750 nm is 2.6 mm. This is insufficient to penetrate human skin, irrespective of the quantum yield.

Coupled with the lack of cytotoxicity and excellent biocompatibility,²¹ it is easy to see why nanodiamonds have now found applications in biomedicine; in drug delivery,^{8,22–26} diagnostic labeling,^{20,27–31} and most recently as a highly sensitive nanometer-scale thermal probe,³² and bimolecular detection.^{33–35} In the last two examples the functionality is due to the presence of N-V centers. An advantage of the characteristic spectrum of the N-V⁰ and N-V⁻ defects is that they are well separated from the endogenous fluorescence region, as shown in the comparative results of ref. 27 for N-V fluorescence from 35 nm nanodiamonds and flavin.

However, as pointed out above, efficiency in each case is contingent on sufficient defects being present in each particle, and herein lies the problem. Although these optical defects do occur naturally, greater efficiency can be gained if their abundance can be controlled. Efficient applications require smaller particles with a higher yield of the N-V defects, on-demand, and so most studies treat their samples with a combinations of irradiation and annealing to increase the N-V yield (brightness, stability and longevity), *post defacto*.

The most widely used method for increasing the quantity of N-V centers is by thermal annealing (at temperatures above

800 °C in vacuum) of type Ib nanodiamond containing atomically dispersed nitrogen atoms that has been irradiated with 1–2 MeV electron beams.²⁷ The increase in yield can be as high as eight times.³⁶ It has also been demonstrated using integrated absorption intensity of the sharp zero-phonon line (637 nm) at liquid nitrogen temperature, that an N-V⁻ density of 25 ± 6 ppm can be obtained with a substrate irradiated with a 3 MeV proton beam, at a dose of 1×10^{16} H⁺ per cm².³⁷ This type of treatment does not sufficiently damage the nanodiamond enough to prevent its use in very sensitive applications.³⁸ Alternatively, it has been shown that the implantation of carbon ions at an appropriate energy can introduce additional vacancies that, when combined with strategic implantation of nitrogen ions into an N-containing diamond lattice, can dramatically increase the N-V production yield by over 50%.³⁹

Therefore, to provide some insights as to the consequences of the generous insertion of nitrogen and lattice vacancies, and to provide a tool that can be use guide future work, a simple model that draws on a limited set of input parameters would be very useful. In the following paragraphs we will see that the optimal concentration of vacancies that need to be generated during these processes, for a given nitrogen concentration, can be predicted by modifying existing probabilistic models¹² to accommodate changes in the N and vacancy concentrations independently (as a function of the particle size and the annealing temperature). This new multivariate model is more flexible, more inclusive, and can be used in conjunction with any consistent set of input parameters to predict the optimal conditions for N-V generation, *a priori*.

Let us begin by assuming that the probability of observing a defect containing species *i* and *j* ($P_{\text{obs}}(i, j)$, where *i* and *j* can represent substitutional atoms and lattice vacancies) is related to the probability of that defect being included ($P_{\text{inc}}(i, j)$, either following implantation or a special process during synthesis) and the probability of the defect diffusing and annihilating with the free surfaces (or escaping, $P_{\text{esc}}(i, j)$)

$$P_{\text{obs}}(i, j) = P_{\text{inc}}(i, j) [1 - P_{\text{esc}}(i, j)]. \quad (1)$$

From previous works it has been shown, in good agreement with experiment,¹² that

$$P_{\text{esc}}(i, j) = \left[\frac{n_c}{n} \exp\left(-\frac{E_{\Delta,c}(i, j) - E_{d,c}(i, j)}{E_K}\right) + \frac{n_s}{n} \right] \times \exp\left(-\frac{E_{\Delta,s}(i, j) - E_{d,s}(i, j)}{E_K}\right) \quad (2)$$

where n_c is the number of carbon atoms (*n*) in the diamond-like core, and n_s is the number of carbon atoms in the reconstructed shell; $E_{d,c}(i, j)$ and $E_{d,s}(i, j)$ are the energies of the combined (*i, j*) defect (containing some mixture of *i* and *j*) in the core and shell, respectively; $E_{\Delta,c}(i, j)$ and $E_{\Delta,s}(i, j)$ are the diffusion energy barriers of the combined defect in the core and shell, respectively; and E_K is the kinetic energy of the optical probe. Note that all defects within the core must pass through the shell in order to escape, and although the core and shell are structurally similar in a fully passivated nanodiamond, a reconstructed bucky-diamond has a graphitized shell that traps the defects

Table 1 Point group symmetry, zero phonon line (ZPL), central wavelength (λ_0) and photoacoustic imaging quantum yield (Q) for optically active defects consisting of combinations of nitrogen and lattice vacancies in diamond²⁰

Defect	Point group	ZPL (nm)	λ_0 (nm)	Q
GR1	T_d	741	898	0.014
N-V ⁰	C_{1h}	575	600	—
N-V ⁻	C_{3v}	638	685	0.99
H3	C_{3v}	504	531	0.95
N3	C_{2v}	415	445	0.29



due to the higher energy barriers that inhibit diffusion. The importance of this will become apparent.

The probability of a defect being included, $P_{\text{inc}}(i, j)$, will be a function of the individual probabilities of i and j being included (P_i and P_j , weighted by the number of components n_i and n_j in each n_{ij} defect, respectively), and the probability of i and j combining, such that

$$P_{\text{inc}}(i, j) = P(i, j) \frac{n_c}{n} \exp\left(-\frac{E_{\text{d,c}}(i) - E_{\text{d,c}}(j)}{E_{\text{d,c}}(i, j)}\right) + \frac{n_s}{n} \exp\left(-\frac{E_{\text{d,s}}(i) - E_{\text{d,s}}(j)}{E_{\text{d,s}}(i, j)}\right) \quad (3)$$

with

$$P(i, j) = \frac{P_i P_j}{n_i n_j \left(\frac{P_i}{n_i} + \frac{P_j}{n_j}\right)} \quad (4)$$

and

$$P_i = C_i [1 - P_{\text{esc}}(i)], \quad (5)$$

where C_i is the concentration of defects present (created *via* irradiation or included during synthesis), and $P_{\text{esc}}(i)$ is the probability of i diffusing and annihilating with the free surfaces (escaping) before it interacts with j to form a defect complex. $P_{\text{esc}}(i)$ has the form of eqn (2), but with the annealing temperature rather than the probe temperature. As an example, the results of eqn (5) for vacancies is provided in ref. 37.

In the case of nanodiamond, many of the individual values for all E_{d} and E_{Δ} have been published before. The values of the defect energies, defect energies and diffusion barriers can be generated using any simulation method, provided consistency is preserved by calculating each parameter with the same computational method and convergence criteria. During the implementation of the model herein, all numerical parameters were generated using the density functional tight-binding theory with self consistent charges, as described in ref. 4, 12, 40, 42 and 43. As described in these references, >50 defect sites within a nanodiamond have been sampled to obtain good statistics for each defect/particle combination and clearly define the separation between the *core* and the *shell*. For convenience, the different defect energies (E_{d}) and the barrier heights (E_{Δ} , based on the energy of the configuration identified as the transition state), is provided in Table 2; and details of the computational method and raw data are provided in the ESI.†

The final result will provide the total number of observed (stable) defects, as a function of the annealing temperature, the observation temperature, the concentration of nitrogen present in the particle and the concentration of vacancies that are introduced. The greatest advantage of this model is that it can be used on N-V, H3 and N3 simultaneously, under the same conditions, and include other possible defects such as the V-N-V complex that would form if an extra vacancy migrated to an existing N-V. Since the V-N-V is not optically active, this would quench the luminescence, and is therefore highly unfavorable.

In Fig. 1 we find the predicted (maximum) probability of observation of these different defects formed from complexes of

Table 2 Defect energies and diffusion barriers for various point defects in diamond nanoparticles, calculated using the density functional tight-binding theory with self consistent charges, as described in ref. 4, 12, 40, 42 and 43. All energies are in eV

Configuration	GR1	V-N-V	N-V	H3	N3	N
Bucky-diamond						
$E_{\text{d,c}}$	6.74	2.15	6.87	7.25	7.25	1.86
$E_{\text{d,s}}$	1.76	-7.68	1.65	4.62	2.55	0.40
$E_{\Delta,c}$	1.80	8.61	6.68	4.51	9.95	667.8
$E_{\Delta,s}$	-3.18	-10.14	13.28	19.20	2.19	1327.9
Passivated nanodiamond						
$E_{\text{d,c}}$	6.62	6.76	6.77	6.75	7.18	4.26
$E_{\text{d,s}}$	3.40	6.50	4.80	4.29	6.52	2.29
$E_{\Delta,c}$	1.80	8.61	6.68	4.51	9.95	667.8
$E_{\Delta,s}$	-1.42	8.34	4.70	2.05	9.29	665.8

nitrogen and lattice vacancies (i and j), for hydrogen passivated nanodiamonds (all sp^3 -bonded). Fig. 1(a)–(c) provide results for nitrogen concentrations of 1 ppm, 10 ppm and 100 ppm, respectively. In each case the corresponding 1 ppm, 10 ppm, and 100 ppm vacancy content are represented by solid, dashed and dotted lines of the same color. Unsurprisingly the expected number of defects per particle (indicated by the final probability of observation) increases with increasing nitrogen concentration, though it is interesting to see the impact of the vacancy concentration. When the nitrogen concentration is small all the maximum defect concentration quickly saturates, and there is limited benefit to adding more vacancies. Most of the extra vacancies diffuse and escape, since there are insufficient nitrogen impurities for them to partner with. As the nitrogen concentration increases we can see a benefit to increasing the vacancy concentration, which can be used to tune the yield.

Irrespective of the vacancy and nitrogen concentration however, it is reassuring to see that the N-V defect has the highest probability of observation in passivated nanodiamonds. Saturation with a high concentration of vacancies does not give rise to a higher probability of the dark V-N-V defects (as many of these vacancies diffuse and escape instead), and a low supply of vacancies does not increase the probability of the H3 or N3 defects, since the N-V defect is still much more energetically favorable. This is not necessarily the case in clean, reconstructed bucky-diamonds.

In Fig. 2(a)–(c) we find the results for bucky-diamonds with nitrogen concentrations of 1 ppm, 10 ppm and 100 ppm, respectively. In this case the predicted number of defect complexes is provided as a function of the vacancy concentration, as well as the average particle diameter. This is because, unlike the passivated nanodiamonds, the N-V is not always the most likely outcome. At small sizes the dark V-N-V defect is more likely than the N-V, over almost the entire range of vacancy and N concentrations. The size at which N-V becomes more probable decreases with the N/V ratio, and over-saturating with vacancies should only be considered for larger high-pressure high-temperature (HPHT) nanodiamonds. Keeping the concentration of vacancies low does not necessarily increase the



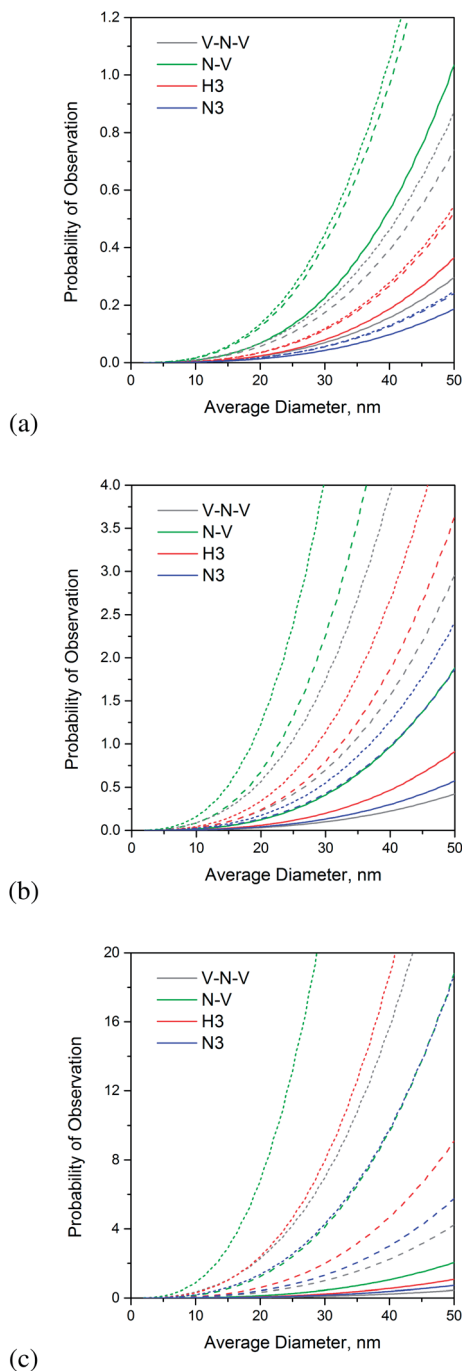


Fig. 1 Probable number of V–N–V, N–V, H3 and N3 defects in a hydrogen passivated nanodiamond, as a function of diameter, with (a) 1 ppm, (b) 10 ppm, and (c) 100 ppm nitrogen content. The corresponding 1 ppm, 10 ppm, and 100 ppm vacancy content are represented by solid, dashed and dotted lines of the same color.

probability of N–V, and actually means that the H3 defect becomes more likely than the N–V if the vacancy contraction is too small. This is because the energy barrier for the vacancy-assisted diffusion of the N–V defect is lower than the H3, and H3 defects are more unlikely to escape.

At this point it should be pointed out that this study has not included the possibility of vacancy clustering, and the formation of voids. This is because, at this stage, insufficient

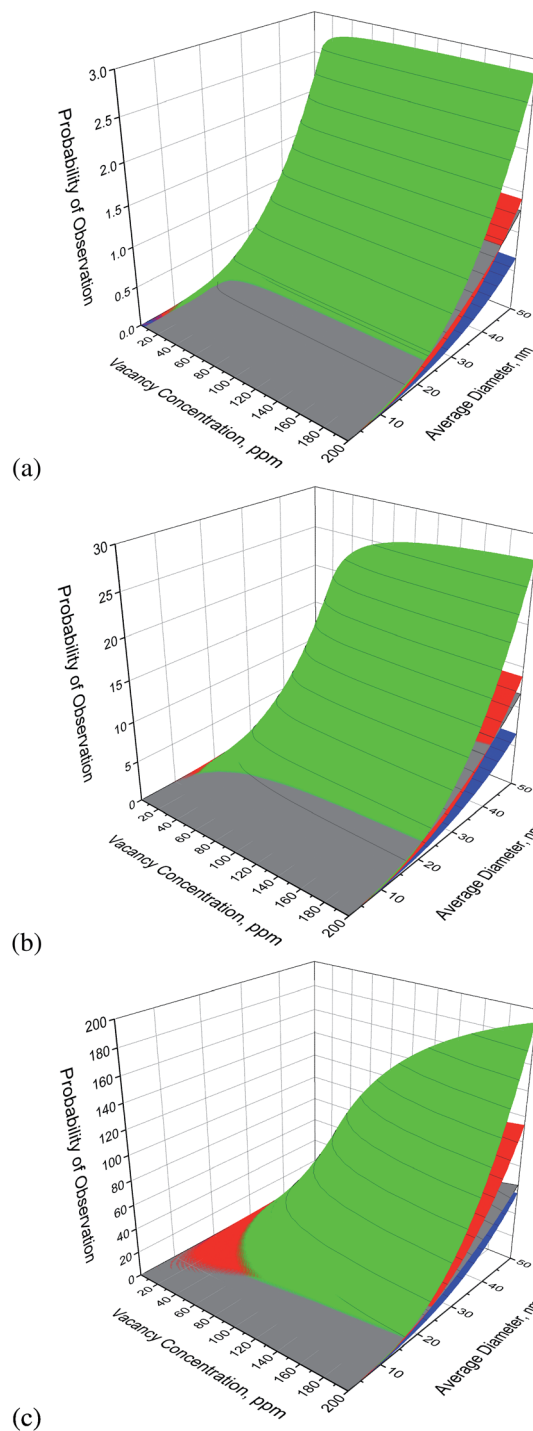


Fig. 2 Probable number of V–N–V (grey), N–V (green), H3 (red) and N3 (blue) defects in a reconstructed (clean) bucky-diamond, as a function of diameter and vacancy concentration with (a) 1 ppm, (b) 10 ppm, and (c) 100 ppm nitrogen content.

information is available on the structure of voids (either in the core, or in the shell), and in particular the structure of the inner (negative) surface of the void interior. When this information becomes available in the future the model can be extended, but will take a different form depending on whether the surfaces of the void are graphitized or not. It is also important to point out



that this model makes no assertions about the doping states of any of these defects once produced. This model is entirely based on thermodynamics and statistical mechanics, and the electronic structure of the defect is assumed at the outset. The intention is to predict how to make more defects, not predict what states those defects are likely to be in. If one were particularly interesting in the latter, this information could be routinely obtained from the original simulations used to parameterise the model, provided they were undertaken at sufficiently high level of theory.

Using this model it is apparent that the ideal vacancy concentration for a given sample will depend on the type (size) of the nanodiamond, and the pre-existing (or intentionally added) nitrogen content at the time of implantation. For a 28 nm nanodiamond with 50 ppm nitrogen, a concentration of >7 ppm of vacancies is recommended to ensure that N-V formation is preferred over H3, and it is always preferred over V-N-V. That is a very convenient ratio, and provides plenty of scope for (more imprecisely) increasing the N and vacancy concentrations to manage the overall yield. With an equal concentration of N and vacancies (50 ppm) the N-V yield in bucky-diamond is predicted to be ~12, and in a passivated nanodiamond it is predicted to be ~9; which is in excellent agreement with the observations and measurements of Hui *et al.* of 8 ± 1 .⁴¹ As other authors have demonstrated that the concentration of vacancies and nitrogen can be tuned simultaneously, by varying the implantation energy,^{27,36–39,44–48} it is suggested that similar experiments, combined with predictions obtained using this model, will provide further insights.

The temperature will also affect the yield, as it will encourage vacancy diffusion; but it also encourages vacancy 'escape', leaving fewer to join with N complexes to form functional defects. However, with the bucky-diamond shell to provide the high kinetic energy barrier varying the annealing temperature is unlikely to negatively impact the yield. This indicates that it is better to irradiate as-grown nanodiamond powders, and then functionalize the surfaces for specific applications later on.

Acknowledgements

Computational resources for this project were supplied by the National Computing Infrastructure (NCI) national facility under Partner Allocation Scheme, Grant q27.

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